Adversarially trained autoencoder

In part 1, we train an autoencoder using mean-squared-error (mse).

In part 2, we couple the same autoencoder to a discriminator similar to one use for a GAN and train the autoencoder using mse on images plus binary cross entropy on the discriminator loss.

We will train our GAN on images from CIFAR10, a dataset of 50,000 32x32 RGB images belong to 10 classes (5,000 images per class). To make things even easier, we will only use images belonging to the class "frog".

Part 1:

Schematically, the autoencoder looks like this:

- An encoder network maps images of shape (32, 32, 3) to vectors of shape (latent_dim,).
- A decoder network maps vectors of shape (latent dim,) to images of shape (32, 32, 3).
- An autoencoder network chains these together to give ae_image = decoder(autoencoder(x))

In part 1, this autoencoder is trained to reproduce images, using mse loss.

The autoencoder

First, develop an autoencoder model.

- You may use any network structure that you like, subject to a maximum of 4 million trainable parameters and a latent dimension of 32.
- It should input a batch of images of shape (32,32,3), funnel down to a batch of vectors 32 dimensional space, and reconstruct back to a batch of images of the same size as the original.
- You may make separate encoder and decoder models and chain them or make a single model. If you use separate models, you should show the summary for each plus the summary for the full model.

Use autoencoder as the name of your full model, and use autoencoder.summary() to show the structure of your autoencoder.

The final activation should be a sigmoid to provide output values in the range 0 to 1 to create a valid image.

```
In [1]: import keras
        from keras.models import Sequential
        from keras.layers import Reshape, Flatten, Dense, Conv2D, Conv2DTranspose, Batc
        hNormalization
        import numpy as np
        latent dim = 32
        height = 32
        width = 32
        channels = 3
        img input = keras.Input(shape=(height, width, channels))
        # Your network here to connect img input to img output
        encoder = Sequential()
        encoder.add(Conv2D(8, (7,7), activation='sigmoid', input_shape=(32,32,3)))
        encoder.add(BatchNormalization())
        encoder.add(Conv2D(16, (5,5), activation='sigmoid', input_shape=(26,26,8)))
        encoder.add(BatchNormalization())
        encoder.add(Conv2D(32, (3,3), activation='sigmoid', input_shape=(22,22,16)))
        encoder.add(BatchNormalization())
        encoder.add(Flatten())
        encoder.add(Dense(32, activation='sigmoid'))
        encoder.add(BatchNormalization())
        encoder.add(Dense(32, activation='sigmoid'))
        decoder = Sequential()
        decoder.add(Dense(32, activation='sigmoid'))
        decoder.add(BatchNormalization())
        decoder.add(Dense(20*20*32, activation='sigmoid'))
        decoder.add(BatchNormalization())
        decoder.add(Reshape((20,20,32)))
        decoder.add(Conv2DTranspose(16, (3,3), activation='sigmoid', input_shape=(20,20
        ,32)))
        decoder.add(BatchNormalization())
        decoder.add(Conv2DTranspose(8, (5,5), activation='sigmoid', input shape=(22,22,
        16)))
        decoder.add(BatchNormalization())
        decoder.add(Conv2DTranspose(3, (7,7), activation='sigmoid', input shape=(26,26,
        8)))
        autoencoder = Sequential()
        autoencoder.add(encoder)
        autoencoder.add(decoder)
        autoencoder.summary()
        autoencoder.compile(optimizer='rmsprop', loss='mse')
```

Using TensorFlow backend.

Layer (type)	Output Shape	Param #
sequential_1 (Sequential)	(None, 32)	420080
sequential_2 (Sequential)	(None, 32, 32, 3)	483891
Total params: 903,971 Trainable params: 878,083 Non-trainable params: 25,888		

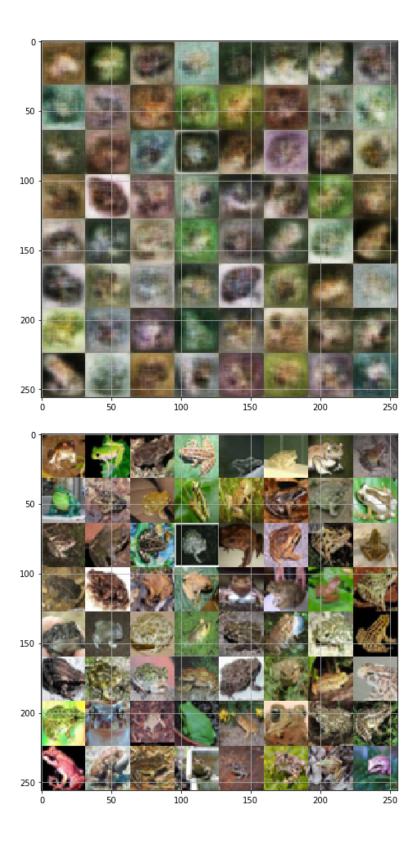
Here is some code to load the data and display images.

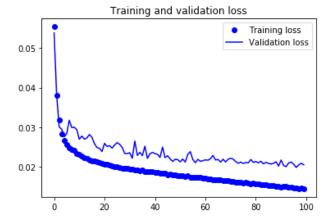
```
In [2]: # Load CIFAR10 data
         (x_train, y_train), (x_test, y_test) = keras.datasets.cifar10.load_data()
         # Select frog images (class 6)
         x train = x train[y train.flatten() == 6]
         x_test = x_test[y_test.flatten() == 6]
         # Normalize data
         x train = x train.reshape(
             (x train.shape[0],) + (height, width, channels)).astype('float32') / 255.
         x_{\text{test}} = x_{\text{test.reshape}}
             (x_test.shape[0],) + (height, width, channels)).astype('float32') / 255.
         import matplotlib.pyplot as plt
         # input a tensor of shape (num images, x size, y size, channels)
         # channels is 1 for greyscale and 3 for color images
         def show_images(images):
          # Display tiled images
          n_x = np.int(np.sqrt(images.shape[0]))
          n_y = np.int(np.ceil(images.shape[0]/n_x))
          tile_x = images.shape[1]
          tile y = images.shape[2]
          figure = np.zeros((tile_x * n_x, tile_y * n_y, images.shape[3]))
          for i in range(n_x):
             for j in range(n_y):
               cur_ind = i+n_x*j
               if (cur_ind >= images.shape[0]):
                 break
               cur_image = images[cur_ind, :,:,:]
               figure[i * tile x: (i + 1) * tile x,
                  j * tile y: (j + 1) * tile y] = cur image
          plt.figure(figsize=(n_x, n_y))
          plt.imshow(np.squeeze(figure))
          ax = plt.gca()
          ax.grid(b=None)
          plt.show()
```

Train your autoencoder for 100 epochs and display reconstructed and real images and training history. You should be able to get validation loss below 0.02.

```
In [3]: num_epochs = 100
         history = autoencoder.fit(x_train, x_train,
                            epochs=num_epochs,
                           batch_size=256,
                            shuffle=True,
                           validation_data=(x_test, x_test))
         ae_images = autoencoder.predict(x_train[0:64])
         show images (ae images)
         show_images(x_train[0:64])
         loss = history.history['loss']
         val_loss = history.history['val_loss']
         epochs = range(len(loss))
         plt.figure()
         plt.plot(epochs, loss, 'bo', label='Training loss')
plt.plot(epochs, val_loss, 'b', label='Validation loss')
         plt.title('Training and validation loss')
         plt.legend()
         plt.show()
```

```
Train on 5000 samples, validate on 1000 samples
Epoch 1/100
5000/5000 [=========================] - 59s 12ms/step - loss: 0.0554 - val
loss: 0.0539
Epoch 2/100
5000/5000 [========================] - 57s 11ms/step - loss: 0.0381 - val
loss: 0.0383
Epoch 3/100
loss: 0.0301
Epoch 4/100
loss: 0.0295
Epoch 5/100
loss: 0.0276
Epoch 6/100
loss: 0.0283
Epoch 7/100
loss: 0.0317
Epoch 8/100
5000/5000 [========================] - 56s 11ms/step - loss: 0.0244 - val
loss: 0.0299
Epoch 9/100
loss: 0.0300
Epoch 10/100
loss: 0.0294
Epoch 11/100
5000/5000 [========== ] - 57s 11ms/step - loss: 0.0230 - val
loss: 0.0269
Epoch 12/100
5000/5000 [=============== ] - 56s 11ms/step - loss: 0.0228 - val
loss: 0.0277
Epoch 13/100
5000/5000 [================= ] - 58s 12ms/step - loss: 0.0224 - val
loss: 0.0270
Epoch 14/100
loss: 0.0273
Epoch 15/100
loss: 0.0281
Epoch 16/100
loss: 0.0274
Epoch 17/100
5000/5000 [========== ] - 56s 11ms/step - loss: 0.0214 - val
loss: 0.0258
Epoch 18/100
5000/5000 [========= ] - 57s 11ms/step - loss: 0.0213 - val
loss: 0.0248
Epoch 19/100
5000/5000 [========== ] - 57s 11ms/step - loss: 0.0210 - val
loss: 0.0246
Epoch 20/100
loss: 0.0238
Epoch 21/100
```





Adversarially trained autoencoder

Part 2:

In part 2, we add the adversarial part by coupling the autoencoder with a discriminator.

- A discriminator network maps images of shape (32, 32, 3) to a binary score estimating the probability that the image is real.
- A gan network chains the generator and the discriminator together: gan(x) =
 discriminator(autoencoder(x)). Thus this gan network maps latent space vectors to the discriminator's
 assessment of the realism of these latent vectors as decoded by the generator.

We train the autoencoder using a weighted sum of the mse loss and binary cross entropy on the output of the discriminator.

To do this, the gan will need to have two outputs and two loss functions that are combined via a weighted sum. There is documentation about that here: multi-input-and-multi-input-and-multi-input-and-multi-input-and-multi-output-models)

In alternation, we train the discriminator using examples of real and fake images along with "real"/"fake" labels, as we would train any regular image classification model. This uses binary cross entropy loss.

The autoencoder

Use the same autoencoder structure from part 1. Do not use a saved version of that autoencoder - just use the same structure, but start with an untrained model. One of the points of this assignment is to compare the results of training with mse versus training with mse plus adversarial loss.

In [0]:

```
In [0]: import keras
        from keras import layers
        from keras.models import Sequential, Model
        from keras.layers import Input, Reshape, Flatten, Dense, Conv2D, Conv2DTranspos
        e, BatchNormalization
        import numpy as np
        latent dim = 32
        height = 32
        width = 32
        channels = 3
        img input = keras.Input(shape=(height, width, channels))
        # Your network here to connect img input to img output
        encoder = Sequential()
        encoder.add(Conv2D(8, (7,7), activation='sigmoid', input shape=(32,32,3)))
        encoder.add(BatchNormalization())
        encoder.add(Conv2D(16, (5,5), activation='sigmoid', input_shape=(26,26,8)))
        encoder.add(BatchNormalization())
        encoder.add(Conv2D(32, (3,3), activation='sigmoid', input_shape=(22,22,16)))
        encoder.add(BatchNormalization())
        encoder.add(Flatten())
        encoder.add(Dense(32, activation='sigmoid'))
        encoder.add(BatchNormalization())
        encoder.add(Dense(32, activation='sigmoid'))
        decoder = Sequential()
        decoder.add(Dense(32, activation='sigmoid'))
        decoder.add(BatchNormalization())
        decoder.add(Dense(20*20*32, activation='sigmoid'))
        decoder.add(BatchNormalization())
        decoder.add(Reshape((20,20,32)))
        decoder.add(Conv2DTranspose(16, (3,3), activation='sigmoid', input_shape=(20,20
        ,32)))
        decoder.add(BatchNormalization())
        decoder.add(Conv2DTranspose(8, (5,5), activation='sigmoid', input shape=(22,22,
        16)))
        decoder.add(BatchNormalization())
        decoder.add(Conv2DTranspose(3, (7,7), activation='sigmoid', input shape=(26,26,
        8)))
        autoencoder = Sequential()
        autoencoder.add(encoder)
        autoencoder.add(decoder)
        autoencoder.summary()
        autoencoder.compile(optimizer='rmsprop', loss='mse')
```

Layer (type)	Output Shape	Param #
	 ===================================	420000
sequential_9 (Sequential)	(None, 32)	420080
sequential_10 (Sequential)	(None, 32, 32, 3)	483891
Total params: 903,971 Trainable params: 878,083 Non-trainable params: 25,888		

Here is some code to load the data and display images.

```
In [0]: # Load CIFAR10 data
         (x_train, y_train), (x_test, y_test) = keras.datasets.cifar10.load_data()
         # Select frog images (class 6)
         x train = x train[y train.flatten() == 6]
         x_test = x_test[y_test.flatten() == 6]
         # Normalize data
         x train = x train.reshape(
             (x train.shape[0],) + (height, width, channels)).astype('float32') / 255.
         x_{\text{test}} = x_{\text{test.reshape}}
             (x_test.shape[0],) + (height, width, channels)).astype('float32') / 255.
         import matplotlib.pyplot as plt
         # input a tensor of shape (num_images, x_size, y_size, channels)
         # channels is 1 for greyscale and 3 for color images
         def show_images(images):
          # Display tiled images
          n_x = np.int(np.sqrt(images.shape[0]))
          n_y = np.int(np.ceil(images.shape[0]/n_x))
          tile_x = images.shape[1]
          tile_y = images.shape[2]
          figure = np.zeros((tile_x * n_x, tile_y * n_y, images.shape[3]))
          for i in range(n x):
             for j in range(n_y):
               cur_ind = i+n_x*j
               if (cur_ind >= images.shape[0]):
                 break
               cur_image = images[cur_ind, :,:,:]
               figure[i * tile_x: (i + 1) * tile_x,
                  j * tile_y: (j + 1) * tile_y] = cur_image
          plt.figure(figsize=(n_x, n_y))
          plt.imshow(np.squeeze(figure))
          ax = plt.gca()
          ax.grid(b=None)
          plt.show()
```

The discriminator

Then, we develop a discriminator model, that takes as input a candidate image (real or synthetic) and classifies it into one of two classes, either "generated image" or "real image that comes from the training set".

```
In [0]: discriminator input = layers.Input(shape=(height, width, channels))
        # Your code here for the discriminator
        # There is one example of a discriminator in Deep Learning with Python, section
        8.5
        # Your discriminator should end with the final binary classification layer:
        #discriminator output = Dense(1, activation='sigmoid')(x)
        discriminator = Sequential()
        discriminator.add(Conv2D(8, (7,7), activation='sigmoid', input shape=(32,32,3))
        discriminator.add(BatchNormalization())
        discriminator.add(Conv2D(16, (5,5), activation='sigmoid', input shape=(26,26,8)
        discriminator.add(BatchNormalization())
        discriminator.add(Conv2D(32, (3,3), activation='sigmoid', input shape=(22,22,16
        )))
        discriminator.add(BatchNormalization())
        discriminator.add(Conv2D(64, (3,3), activation='sigmoid', input shape=(20,20,32
        )))
        discriminator.add(BatchNormalization())
        discriminator.add(Flatten())
        discriminator.add(Dense(64, activation='sigmoid'))
        discriminator.add(BatchNormalization())
        discriminator.add(Dense(1, activation='sigmoid'))
        # discriminator = keras.models.Model(discriminator input, discriminator output)
        discriminator.summary()
        # To stabilize training, we use learning rate decay
        # and gradient clipping (by value) in the optimizer.
        discriminator_optimizer = keras.optimizers.RMSprop(lr=0.0008, clipvalue=1.0, de
        cay=1e-8)
        discriminator.compile(optimizer=discriminator optimizer, loss='binary crossentr
        opy')
```

Layer (type)	Output Shape	Param #
conv2d_18 (Conv2D)	(None, 26, 26, 8)	1184
batch_normalization_35 (Ba	tc (None, 26, 26, 8)	32
conv2d_19 (Conv2D)	(None, 22, 22, 16)	3216
batch_normalization_36 (Ba	tc (None, 22, 22, 16)	64
conv2d_20 (Conv2D)	(None, 20, 20, 32)	4640
batch_normalization_37 (Ba	tc (None, 20, 20, 32)	128
conv2d_21 (Conv2D)	(None, 18, 18, 64)	18496
batch_normalization_38 (Ba	tc (None, 18, 18, 64)	256
flatten_6 (Flatten)	(None, 20736)	0
dense_17 (Dense)	(None, 64)	1327168
batch_normalization_39 (Ba	tc (None, 64)	256
dense_18 (Dense)	(None, 1)	65

Total params: 1,355,505 Trainable params: 1,355,137 Non-trainable params: 368

The adversarial network

Finally, we setup an adversarial network (AN) that chains the autoencoder and the discriminator. This will move the autoencoder in a direction that improves its ability to fool the discriminator while still reproducing its input. The AN is meant to be trained with labels that are always "these are real images", so the weights of autoencoder will be updated to make discriminator more likely to predict "real" when looking at fake images. Very importantly, we set the discriminator to be frozen during training (non-trainable): its weights will not be updated when training gan. If the discriminator weights could be updated during this process, then we would be training the discriminator to always predict "real", which is not what we want!

Note: Setting nontrainable weights may give a warning about a mismatch between trainable and nontrainable weights, but you may ignore that.

You will need to set up your model to have a loss function that is a weighted sum of the mse on the autoencoder and the binary cross entropy from the discriminator. The link in the introduction gives information about how to do that.

Training you AN

Now we can start training. To recapitulate, this is schematically what the training loop looks like:

" for each epoch:

- * Draw a batch of training images
- * Reconstruct images with `autoencoder`
- * Mix the generated images with real ones.
- * Train `discriminator` using these mixed images, with corresponding targets, either "real" (for the real images) or "fake" (for the generated images).
- * Draw new random images.
- * Train `gan` using these random images, with targets that all say "these are real im ages". This will update the weights of the autoencoder (only, since discriminator is frozen inside `an`) to move them towards getting the discriminator to predict "these are real images" for generated images, i.e. this trains the autoencoder to fool the discriminator.

,,,

The code below does most of this. You'll need to set up the training on batches. You should also find a way to get and plot the validation loss - the loss on the test data. This is not included below.

```
In [0]: # Set discriminator weights to non-trainable
        # (will only apply to the `gan` model)
        discriminator.trainable = False
        # Set up the gan to output both the image and the real/fake value from the disc
        riminator
        # See https://keras.io/getting-started/functional-api-guide/#multi-input-and-mu
        lti-output-models
        inputs = Input(shape=(32,32,3))
        x = encoder(inputs)
        img = decoder(x)
        prob = discriminator(img)
        gan = Model(inputs=inputs, outputs=[img,prob])
        # loss = { "img": "mse", "prob": "categorical crossentropy", }
        # loss weights = { "img": 1.0, "prob": 1.0 }
        loss = ["mse", "binary crossentropy"]
        loss weights=[1.0, 0.1]
        qan optimizer = keras.optimizers.RMSprop(lr=0.0004, clipvalue=1.0, decay=1e-8)
        gan.compile(optimizer=gan_optimizer, loss=loss, loss_weights=loss_weights)
```

```
In [0]: | batch_size = 128
        num_epochs = 100
        print('Number of epochs = ' + str(num_epochs))
        adv_loss = np.zeros((num_epochs, 3))
        val_adv_loss = np.zeros((num_epochs, 3))
        disc_loss = np.zeros((num_epochs, 1))
        max ind = x train.shape[0]
        # Start training loop
        start = 0
        epoch = 0
        while epoch < num epochs:
            if (start == 0):
                cur perm = np.random.permutation(max ind)
            # Sample random training images
            stop = start + batch_size
            random_images = x_train[cur_perm[start:stop]]
            # Decode them to reconstructed images
            generated_images = gan.predict(random_images)[0]
            # Combine them with real images
            real_images = x_train[start: stop]
            combined images = np.concatenate([generated images, real images])
            # Assemble labels discriminating real from fake images
            labels = np.concatenate([0.95*np.ones((batch_size, 1)),
                                     np.zeros((batch_size, 1))]) # 0=real, 1=fake
            # Add random noise to the labels - important trick!
            labels += 0.05 * np.random.random(labels.shape)
            # Train the discriminator
            d loss = discriminator.train on batch(combined images, labels)
            # Assemble labels that say "all real images"
            misleading targets = np.zeros((batch size, 1))
            # Train the generator (via the AN model,
            # where the discriminator weights are frozen)
            a_loss = gan.train_on_batch(real_images, [real_images,misleading_targets])
            start += batch_size
            if start > len(x_train) - batch_size:
                start = 0
                # Print metrics
                print('discriminator loss at epoch %s: %s' % (epoch, d_loss))
                print('adversarial loss at epoch %s: %s' % (epoch, a_loss))
                adv loss[epoch,:] = a loss
                disc_loss[epoch,:] = d_loss
                # Calculate and save the validation loss (mse on image only)
                val adv loss[epoch,:] = gan.evaluate(x test, [x test, np.ones(x test.sh
        ape[0])])
                epoch += 1
```

Number of epochs = 100

/usr/local/lib/python3.6/dist-packages/keras/engine/training.py:490: UserWarnin g: Discrepancy between trainable weights and collected trainable weights, did y ou set `model.trainable` without calling `model.compile` after ?

'Discrepancy between trainable weights and collected trainable'

```
discriminator loss at epoch 0: 0.18028562
adversarial loss at epoch 0: [0.18032476, 0.093454756, 0.8687]
1000/1000 [=========== ] - 1s 1ms/step
discriminator loss at epoch 1: 0.15551665
adversarial loss at epoch 1: [0.14977415, 0.07991409, 0.69860053]
1000/1000 [========== ] - 0s 172us/step
discriminator loss at epoch 2: 0.34671268
adversarial loss at epoch 2: [0.15738052, 0.07327927, 0.8410126]
1000/1000 [======] - 0s 159us/step
discriminator loss at epoch 3: 0.14955622
adversarial loss at epoch 3: [0.18701223, 0.06767388, 1.1933835]
1000/1000 [========== ] - 0s 173us/step
discriminator loss at epoch 4: 0.14134766
adversarial loss at epoch 4: [0.16265929, 0.06852975, 0.9412953]
1000/1000 [=======
                    ======== ] - Os 156us/step
discriminator loss at epoch 5: 0.13194627
adversarial loss at epoch 5: [0.1432459, 0.065712914, 0.77532995]
1000/1000 [============ ] - 0s 184us/step
discriminator loss at epoch 6: 0.12471356
adversarial loss at epoch 6: [0.14919451, 0.06469269, 0.84501815]
1000/1000 [============= ] - 0s 178us/step
discriminator loss at epoch 7: 0.120787874
adversarial loss at epoch 7: [0.16098368, 0.06153433, 0.99449354]
1000/1000 [============ ] - Os 181us/step
discriminator loss at epoch 8: 0.12550056
adversarial loss at epoch 8: [0.17431979, 0.05933746, 1.1498233]
1000/1000 [========== ] - Os 180us/step
discriminator loss at epoch 9: 0.1217459
adversarial loss at epoch 9: [0.16072561, 0.060867567, 0.9985804]
1000/1000 [===========] - 0s 159us/step
discriminator loss at epoch 10: 0.12457724
adversarial loss at epoch 10: [0.14521411, 0.057543747, 0.8767037]
1000/1000 [========= ] - 0s 174us/step
discriminator loss at epoch 11: 0.12327406
adversarial loss at epoch 11: [0.1332396, 0.055106293, 0.78133297]
1000/1000 [========== ] - Os 163us/step
discriminator loss at epoch 12: 0.11302555
adversarial loss at epoch 12: [0.14320505, 0.052039113, 0.91165936]
discriminator loss at epoch 13: 0.12041547
adversarial loss at epoch 13: [0.13087624, 0.051115148, 0.7976109]
1000/1000 [============= ] - 0s 162us/step
discriminator loss at epoch 14: 0.12149854
adversarial loss at epoch 14: [0.12838358, 0.049119193, 0.79264385]
1000/1000 [============ ] - Os 172us/step
discriminator loss at epoch 15: 0.12402106
adversarial loss at epoch 15: [0.13228256, 0.049808905, 0.8247366]
discriminator loss at epoch 16: 0.1258336
adversarial loss at epoch 16: [0.1242679, 0.05014444, 0.74123454]
discriminator loss at epoch 17: 0.13646542
adversarial loss at epoch 17: [0.20735362, 0.05222407, 1.5512955]
1000/1000 [======] - 0s 158us/step
discriminator loss at epoch 18: 0.12054384
adversarial loss at epoch 18: [0.12931132, 0.047073223, 0.8223809]
1000/1000 [============= ] - 0s 171us/step
discriminator loss at epoch 19: 0.11518071
adversarial loss at epoch 19: [0.12818187, 0.048768613, 0.7941326]
discriminator loss at epoch 20: 0.11254447
adversarial loss at epoch 20: [0.124004945, 0.046606585, 0.7739836]
1000/1000 [========== ] - 0s 173us/step
```

Display a few reconstructed images and the training plots:

```
In [0]:
    ae_images, discrim = gan.predict(x_train[0:64])
    show_images(ae_images)
    show_images(x_train[0:64])

loss = adv_loss[:,1]  # Set up so this is mse on the images
val_loss = val_adv_loss[:,1]
    epochs = range(num_epochs)

plt.figure()

plt.plot(epochs, loss, 'bo', label='Training loss')
plt.plot(epochs, val_loss, 'b', label='Validation loss')
plt.title('Training loss')
plt.legend()

plt.show()
```

