

In an alternative approach, one can observe that, unless a sample $\phi(x^{(i)})$ is misclassified, $y^{(i)} - h_{\theta^{(i)}}(\phi(x^{(i)}))$ will be zero; otherwise, it will be ± 1 (or ± 2 , if the convention $y, h \in \{-1, 1\}$ is taken). The vector θ , then, can be represented as the sum $\sum_{\{i: y^{(i)} \neq h_{\theta^{(i)}}(\phi(x^{(i)}))\}} \alpha(2y^{(i)} - 1)\phi(x^{(i)})$ under the $y, h \in \{0, 1\}$ convention, and containing $(2y^{(i)})$ under the other convention. This can then be expressed as $\theta^{(i)} = \sum_{i \in \text{Misclassified}} \beta_i \phi(x^{(i)})$ to be in more obvious congruence with the above. The efficient representation can now be said to be a list which stores only those indices that were misclassified, as the β_i s can be recomputed from the $y^{(i)}$ s and α on demand. The derivation for (b) is then only cosmetically different, and in (c) the update rule is to add $(i + 1)$ to the list if $\phi(x^{(i+1)})$ is misclassified.