## 4. [20 points] Properties of VC dimension

In this problem, we investigate a few properties of the Vapnik-Chervonenkis dimension, mostly relating to how VC(H) increases as the set H increases. For each part of this problem, you should state whether the given statement is true, and justify your answer with either a formal proof or a counter-example.