

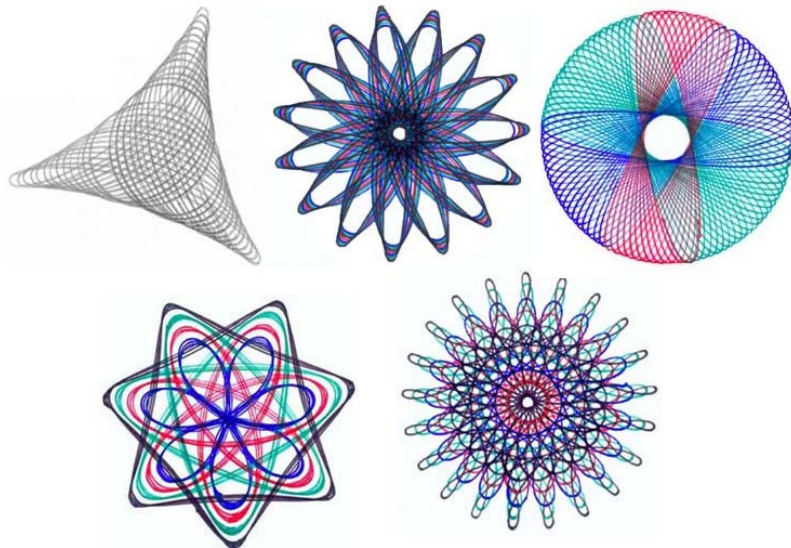
The Harmonograph

The Harmonograph

An harmonograph is a mechanical engine that uses the **swinging motion** of pendulums to **draw beautiful geometric forms** such as spirals, ellipses, hypotrochoids, epitrochoids, Lissajous figures and self-similar complex figures (called the harmonograms)

The first harmonographs date back to the **19th century**. These devices can work with two or three pendulums, and depending on the mechanism they can generate very complex figures. In the '60, British engineer Denys Fisher designed the **Spirograph**, a toy that worked as a simplified version of an harmonograph, using gears instead of pendulums. This toy became very popular.

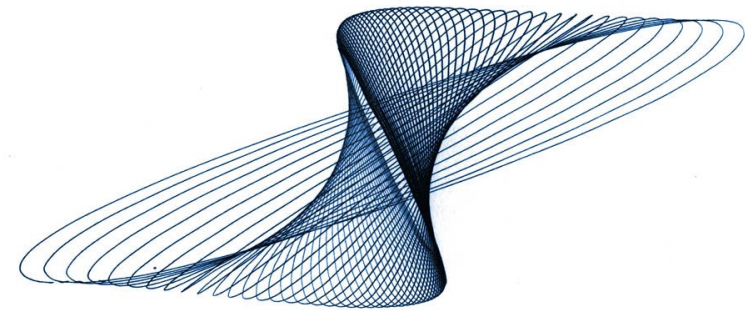
The goal of my term project is to design a **digital version of an harmonograph** in Python.



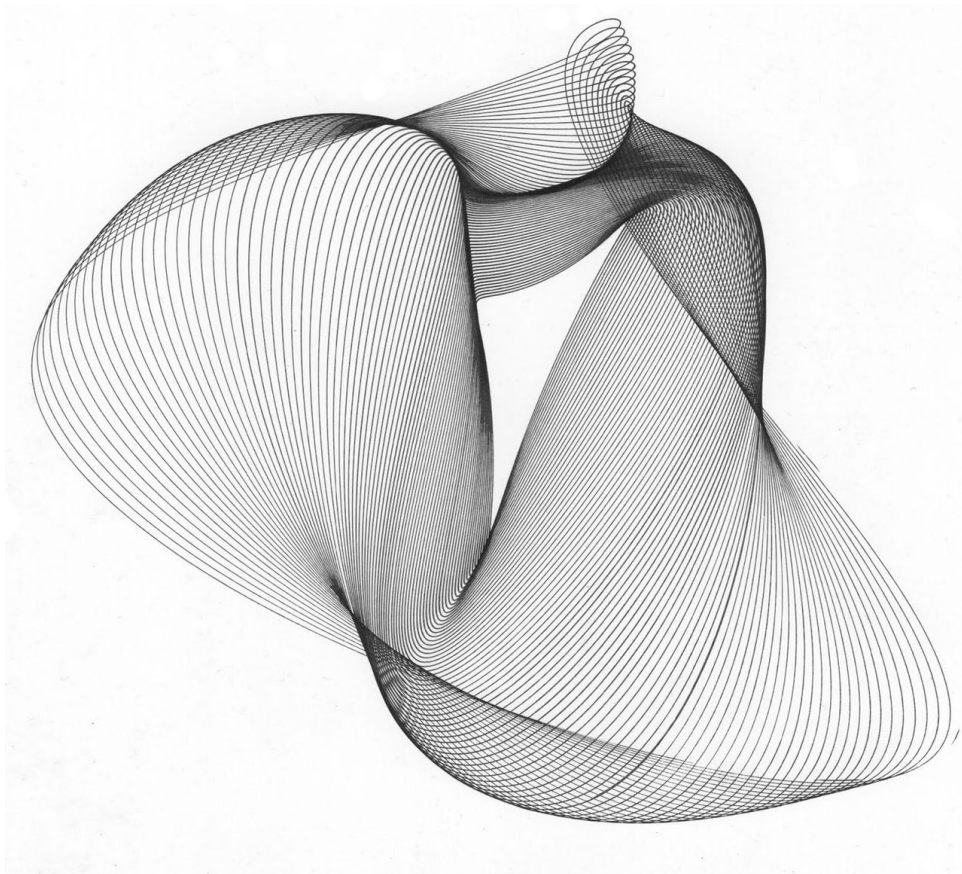
Drawings created with the Spirograph. Source: wikipedia.org



Source: <http://www.karlsims.com/>



Source: <https://anitachowdry.wordpress.com/>



$$x(t) = A_1 \sin(tf_1 + p_1)e^{-d_1t} + A_2 \sin(tf_2 + p_2)e^{-d_2t}$$

$$y(t) = A_3 \sin(tf_3 + p_3)e^{-d_3t} + A_4 \sin(tf_4 + p_4)e^{-d_4t}$$

Source: Wikipedia

The result of the project should be an **educational game** in two modalities:

A) The user **sets the mechanism** with different levels of customization freedom, including:

- the position of the gears
- the anchor points and length of the drawing arms
- the rotation speed of each gear
- the drawing speed

The program draws the harmonograph constrained to these settings.

The user can then interact with the result in a variety of different ways, zooming in/out, exporting a vector-graphic version and choosing a coloring pattern for the figure.

The info-mode of the game should display information about the harmonic equations and the trigonometry rules behind the drawing process. The math of harmonograph is not easy. My goal is to make it to use the program to make these rules simpler to understand for kids (and beautifully demonstrated).

B) The user is given a figure, and the challenge is to **retrieve the mechanical setting** that could generate that figure.

This can be a hard task, and can be imagined as a multilevel game starting with the basic harmonographs and increasing in difficulty to complex figures.

Technologies

I want to design the harmonograph in **Tkinter**.

Doing sophisticated work with sophisticated tools is great. Doing sophisticated work with basic tools is greater!

To make the GUI work more efficiently I will use:

Pillow

<https://python-pillow.org/>

“Python Imaging Library (abbreviated as PIL) is a free library for the Python programming language that adds support for opening, manipulating, and saving many different image file formats.” (from Wikipedia).

I will use pillow in Tkinter to speed-up the drawing

Cairo

<https://cairographics.org/pycairo/>

If I will include vector image exporting as a project feature, then I will use Cairo for Python to export the results as vector-images.

Competitive Analysis

There exist several type of analogic harmonographs and spiro-graphs. Recently, designer Joe Freedman kickstarted the Drawing Machine, a portable, high quality machine that comes with a wide range of different gears, allowing to produce a variety of beautiful harmonograms. I want to simulate Freedman's machine or similar machines, using gears instead of pendulums.

This is a link to Freedman's machine:

<https://www.youtube.com/watch?v=ygcGfnVM6Ho>

It found some examples of digital harmonographs. None of these provide the same level of direct user interaction that I would like to feature. I do not plan to build upon there existing codes (I want to code my own from scratch).

Worldtree.software offers an online virtual harmonograph:

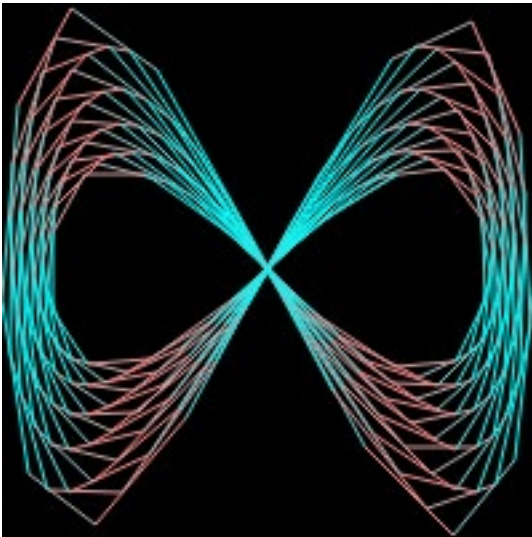
<http://www.worldtreesoftware.com/harmonograph.html>

STRENGTHS:

- freedom in parameter choice: I want to include a good level of freedom in parameter customization
- everything is online: since we are talking about an educational game, it would be great to have it online

WEAKNESSES:

- static interface: I wish to make the interface dynamic and have the harmonogram drawn in real time, also displaying the mechanism
- the graphic output is not compelling and a bit unprecise: I want the graphic output to be simple but precise and elegant, potentially with the possibility to customize line/blank space colors according to user preference or to a randomly assigned palette.



An image output from worldtree.software.

Source: <http://www.worldtreesoftware.com/apps/harmonograph>

David Chudzicki also provides a virtual version of an harmonograph on his website:

<http://www.davidchudzicki.com/harmonograph/>

STRENGTHS:

- the real-time drawing is really nice, simple and effective. I want to include such a feature in my project too
- good level of parameter customization

WEAKNESSES:

- again, the motion of the gears/pendulums is not displayed. I want to make it visible to the user for pedagogical purposes (the mechanism can be hidden by pressing “h” at anytime)

Harmonograph in JavaScript

<http://thomas.home.fmf.nl/harmonograph/>

A very nice digital harmonograph!

STRENGTHS:

- with a simple graphic interface, it clearly displays the mechanism of the pendulum. I want to do something similar, but replacing the pendulums with rotating gears (a simplification of the motion of a pendulum)
- you can speed up the drawing: this feature must be included in my project too
- you can easily export a jpg of the harmonogram.

WEAKNESSES:

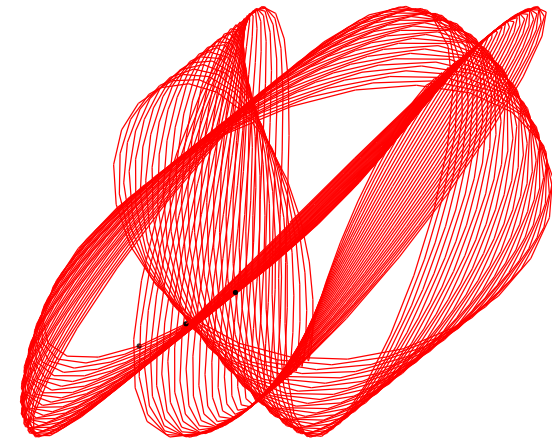
- the user does not interact directly on the pendulum or canvas: the interface is the parameters. I want the interface to be more intuitive (drag and place gears,...)



[David Chudzicki](#)

- [about](#)
- [posts](#)

Harmonograph



Settings

Frequencies:

<input type="text" value="f<sub>0</sub> 3.00"/>	<input type="text" value="f<sub>1</sub> 2.00"/>	<input type="text" value="f<sub>2</sub> 3.01"/>
<input type="text"/>	<input type="text"/>	<input type="text"/>
<input type="text"/>	<input type="text"/>	<input type="text"/>

Phases:

<input type="text" value="f<sub>0</sub> 0.00"/>	<input type="text" value="f<sub>1</sub> 0.00"/>	<input type="text" value="f<sub>2</sub> 0.00"/>
<input type="text"/>	<input type="text"/>	<input type="text"/>
<input type="text"/>	<input type="text"/>	<input type="text"/>

Amplitudes:

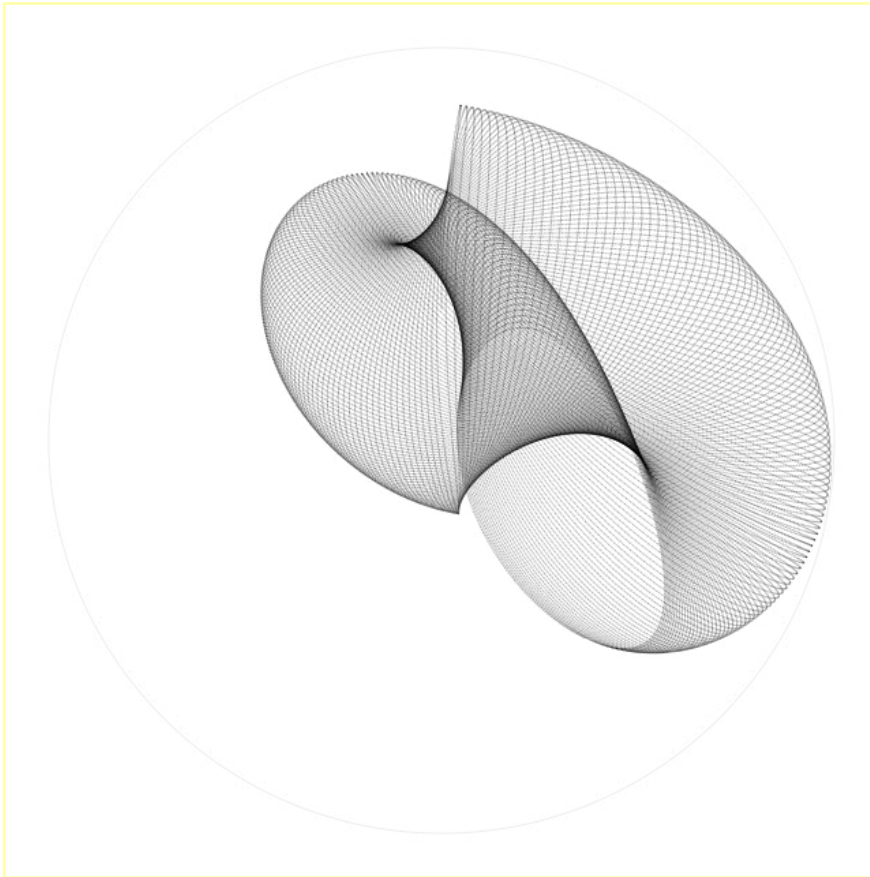
<input type="text" value="f<sub>0</sub> 1.00"/>	<input type="text" value="f<sub>1</sub> 1.00"/>	<input type="text" value="f<sub>2</sub> 1.00"/>
<input type="text"/>	<input type="text"/>	<input type="text"/>
<input type="text"/>	<input type="text"/>	<input type="text"/>

Fade out old points? ☐

Source: David Chudzicki website

Harmonograph in JavaScript

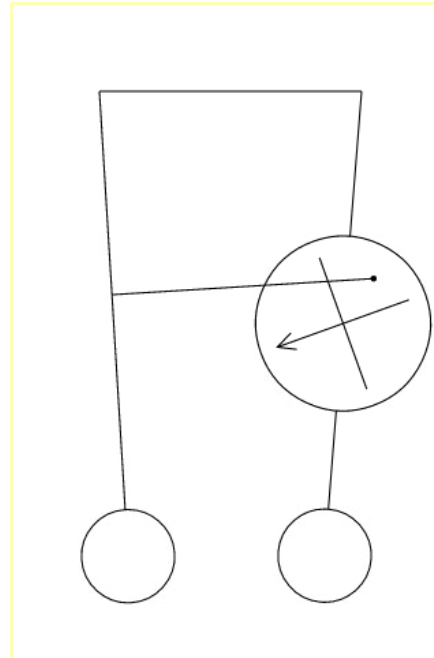
[Link to this creation](#)



Time speedup factor:

Reset

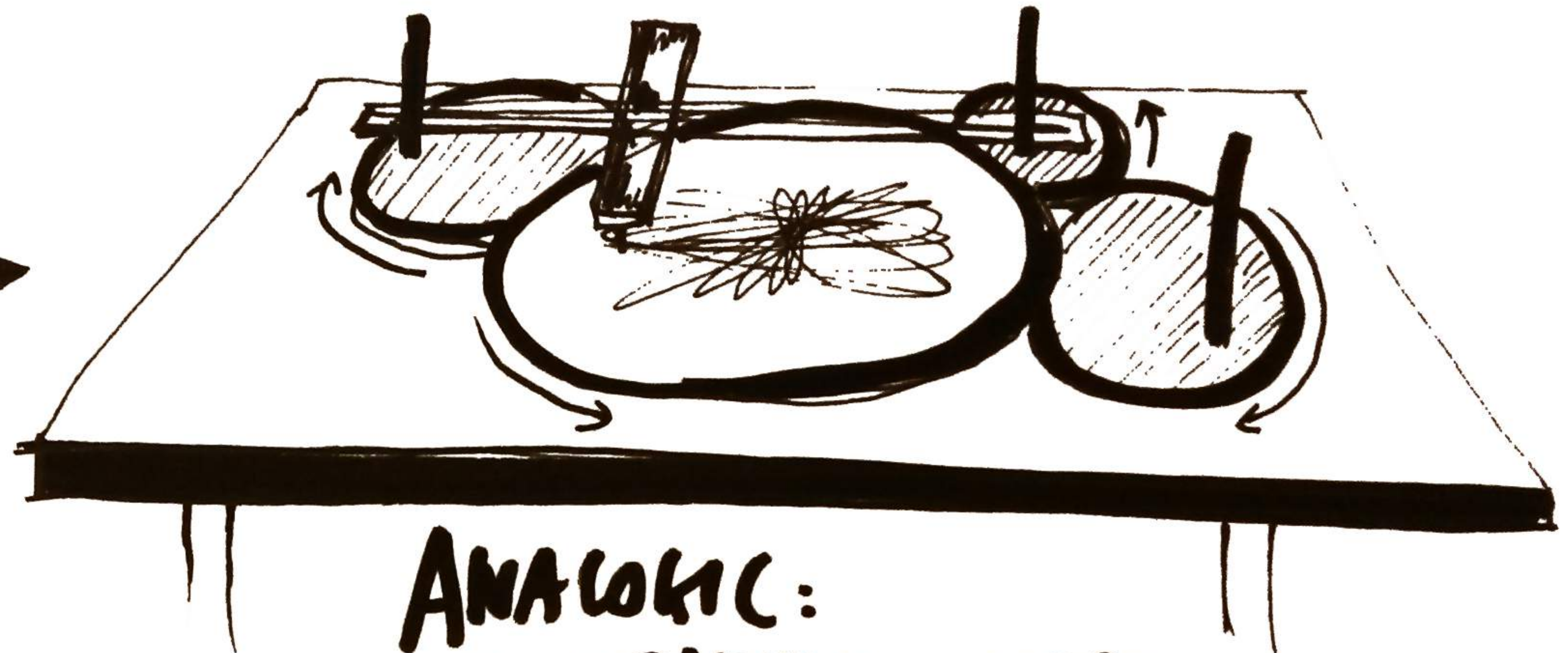
Start



Distance between pendulums $d =$ mm
Position of paper centre $c =$ mm
Length of pen arm $p =$ mm
Position of pen arm $q =$ mm
Radius of paper $r =$ mm
Amplitude of left pendulum $A =$ °
Amplitude of right pendulum $B =$ °
Phase of left pendulum $u =$ (0...1)
Phase of right pendulum $v =$ (0...1)
Damping of left pendulum $R =$ (0...)
Damping of right pendulum $S =$ (0...)
Frequency of left pendulum $f =$ Hz
Frequency of right pendulum $g =$ Hz
Frequency of paper rotation $h =$ Hz

AN HARMONOGRAPH
IS A MACHINE MADE OF
2 OR MORE PENDULUMS,
GEARS AND A DRAWING
ARM.

IT PRODUCES NICE
CYCLOID-LIKE DRAWINGS.



ANALOGIC:
3-PENDULUM MECHANISM



EDUCATIONAL APP/GAME

2-mode application:

- I. set the mechanism
and draw
- II. look at the drawing
& retrieve the mechanism

But can we design a Python version?
Let's do it!

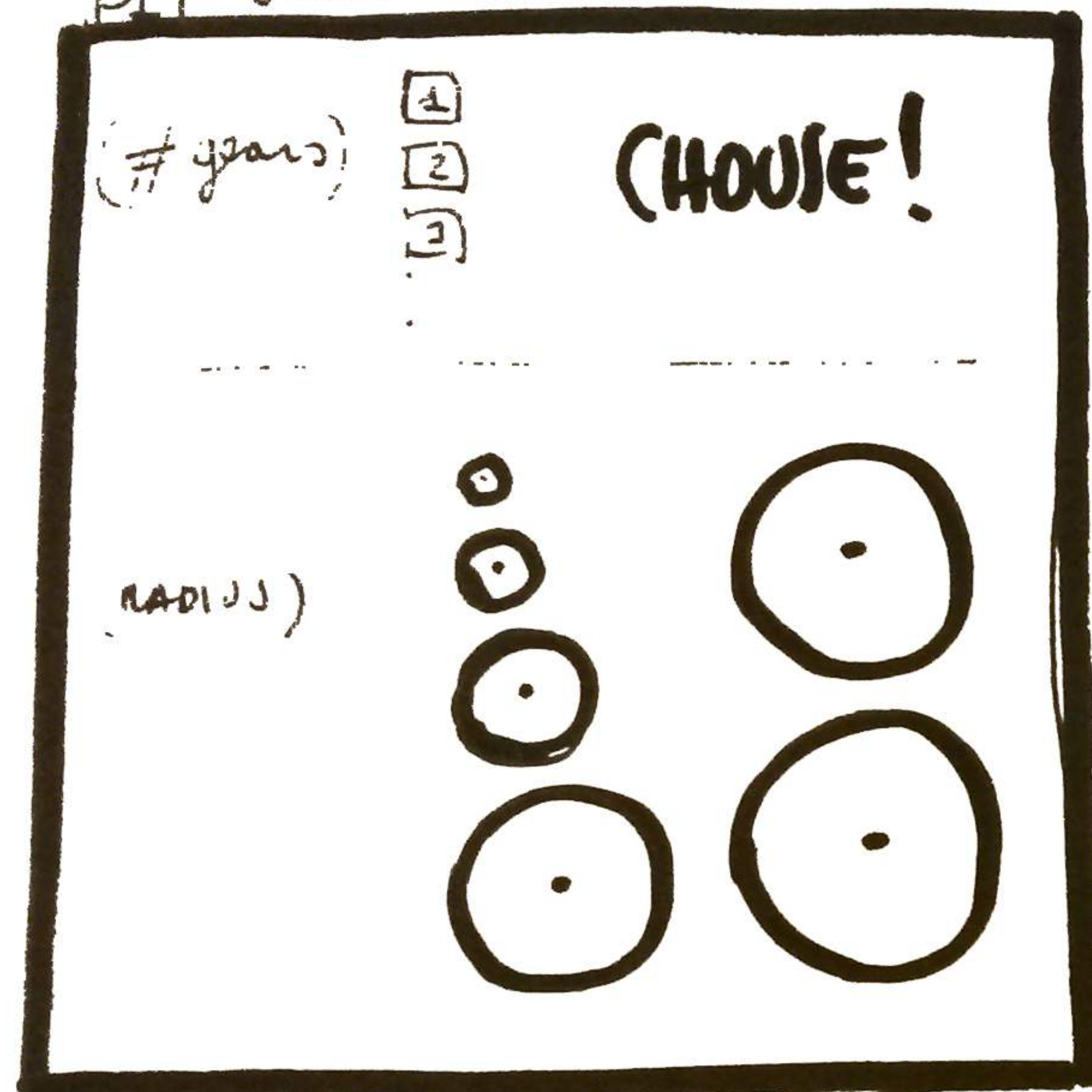
GOAL: design a TKinter Harmonograph on Python
to teach kids the beauty of pendulums,
cycloids and trigonometry

DIGITAL:
PYTHON TKINTER

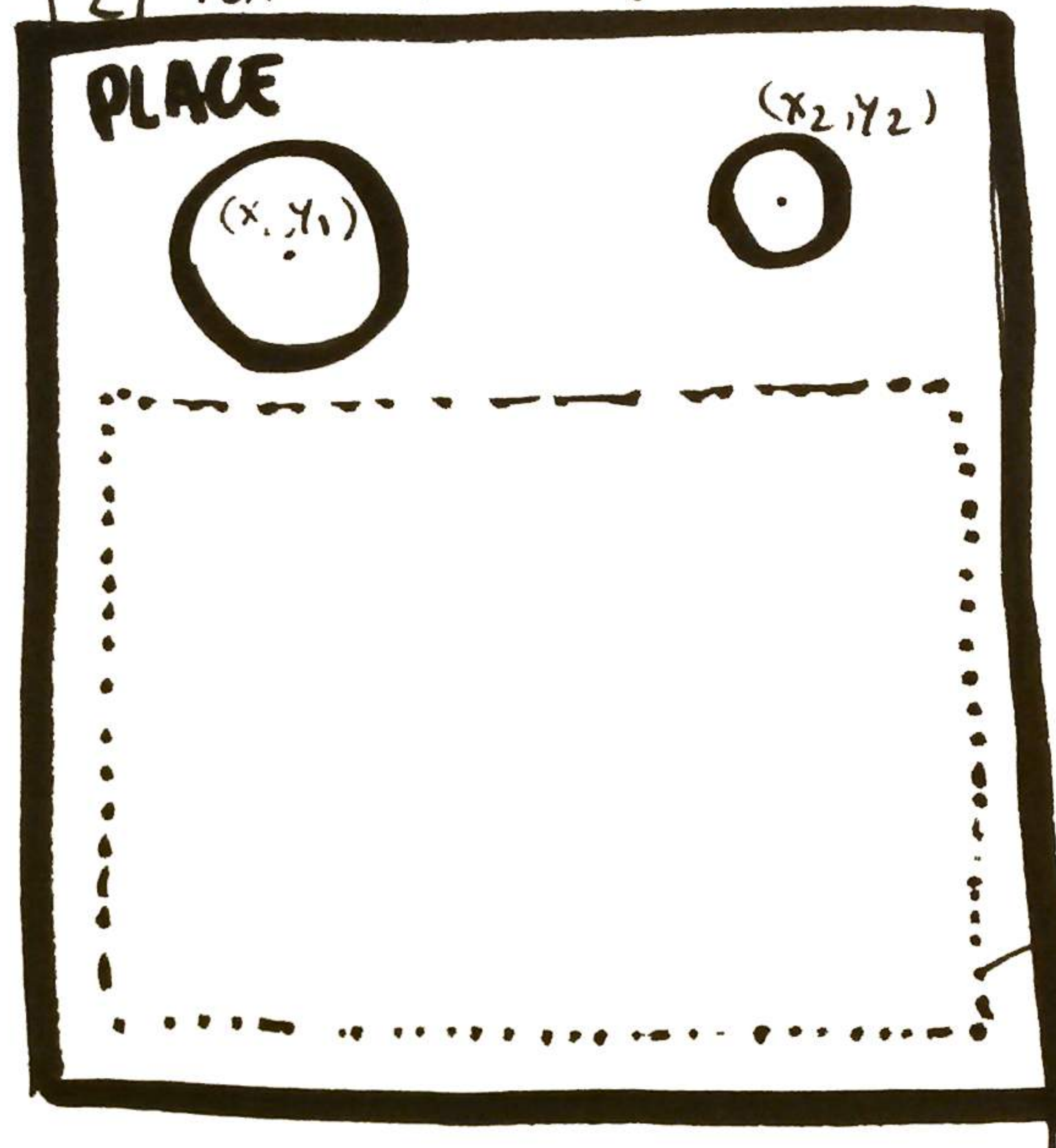
MODE (I)

SET THE MECHANISM, SEE THE RESULT

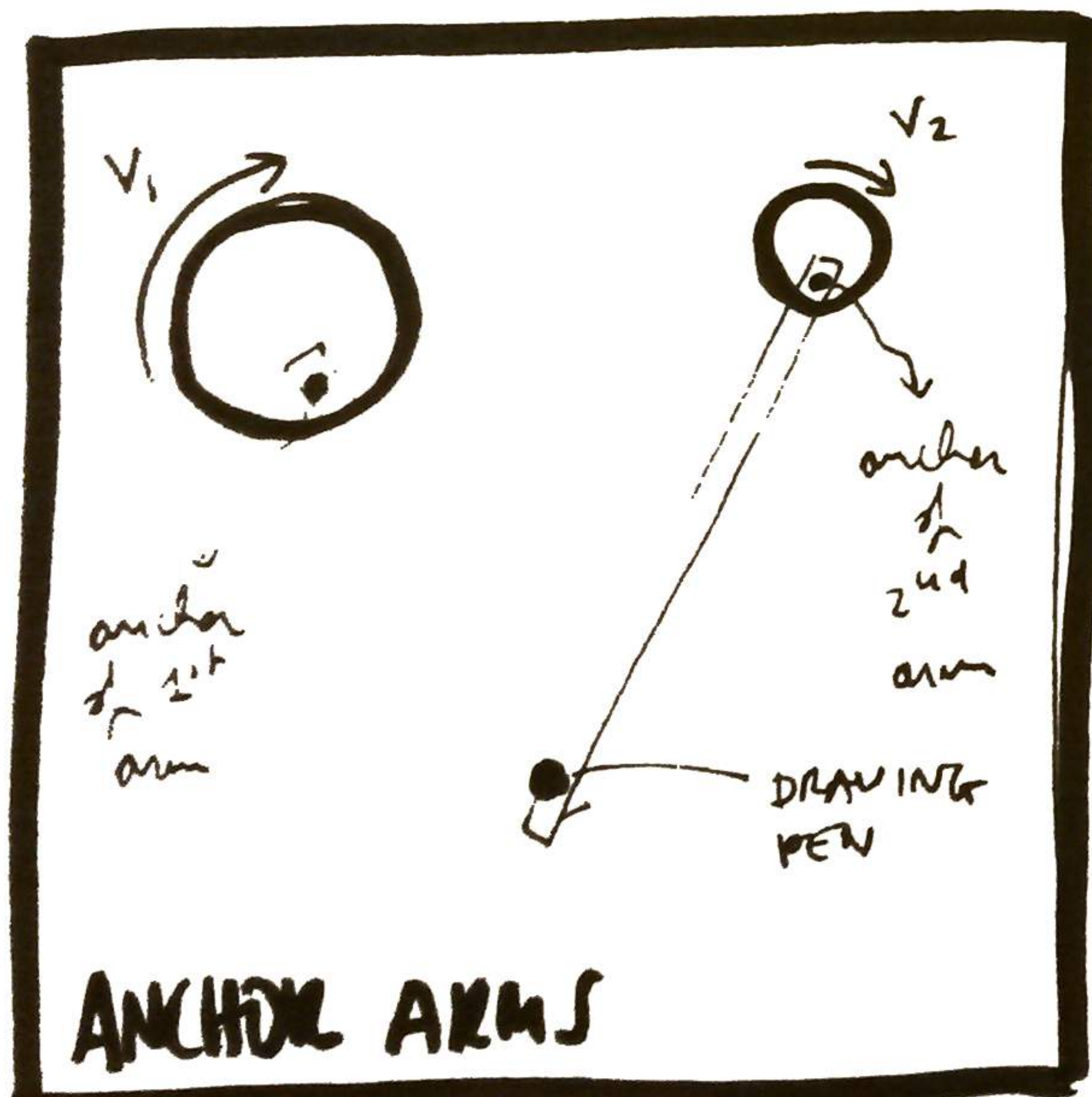
1 SELECT THE GEARS



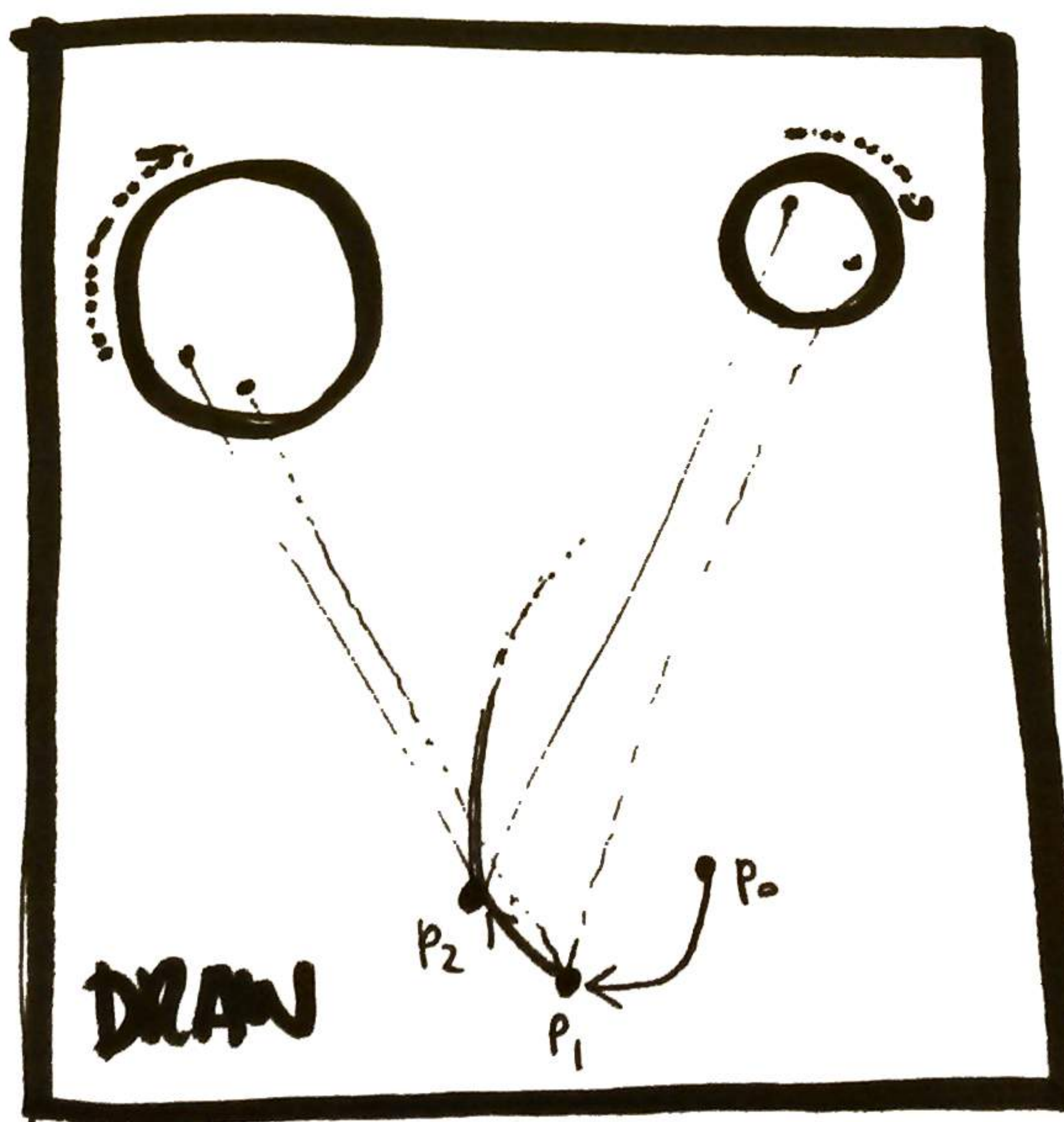
2 PLACE THE GEARS ON THE CANVAS



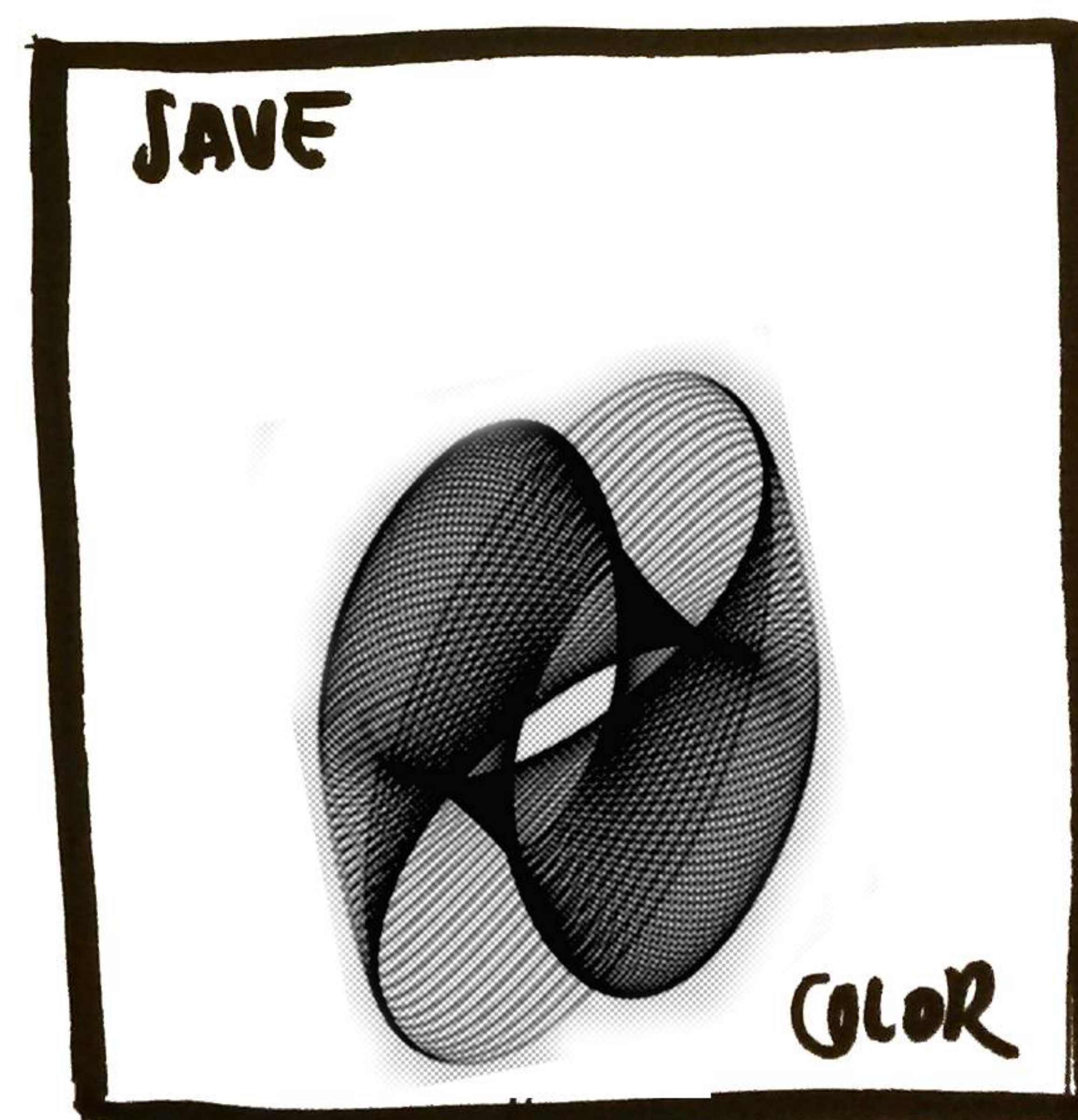
DRAWING AREA



3 choose rotation speed, choose the drawing arms



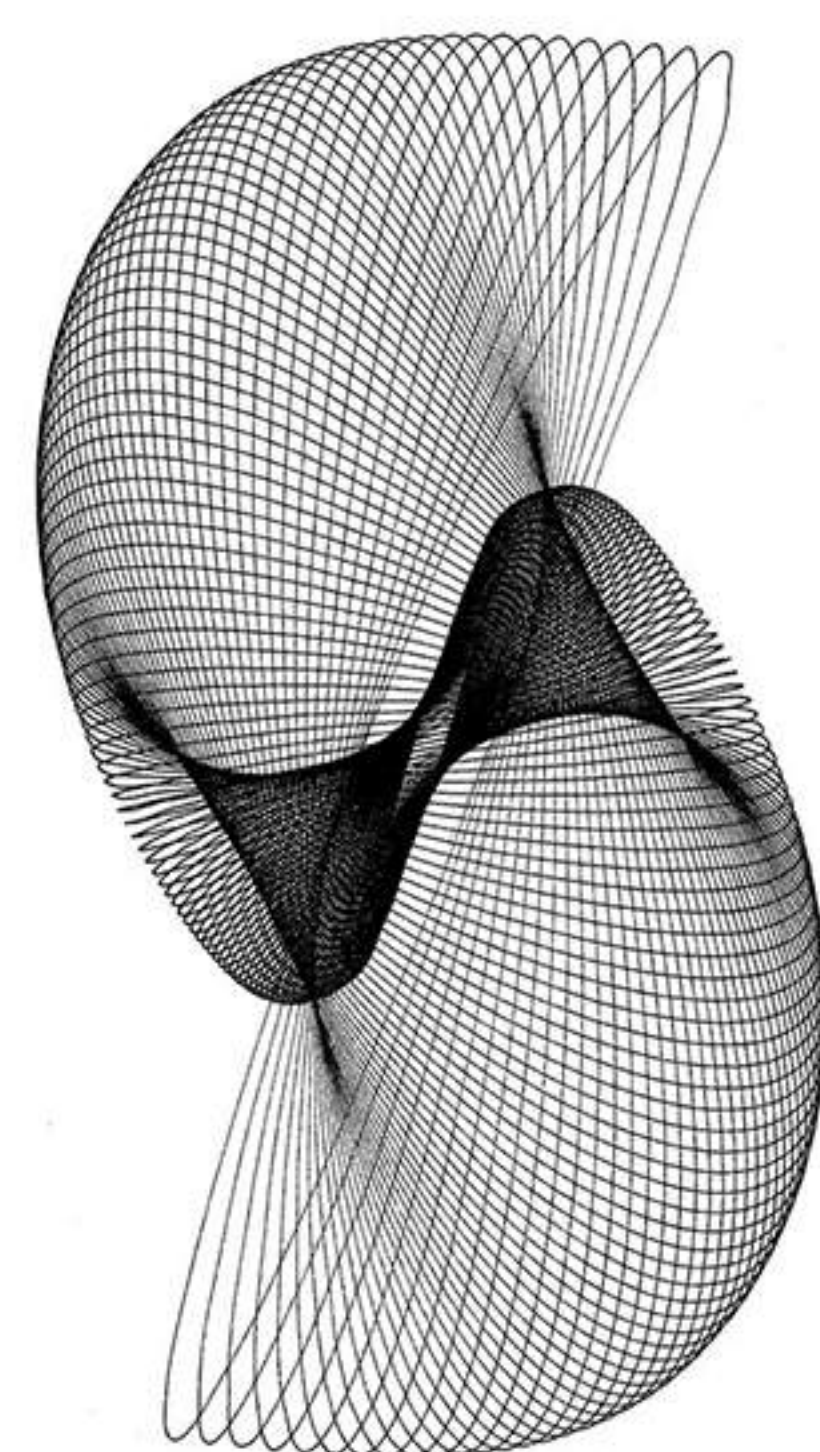
4 start drawing



5 Speed up and SEE THE RESULT

1 look at this cycloid

LOOK!



2 retrieve the gears position & dimensions

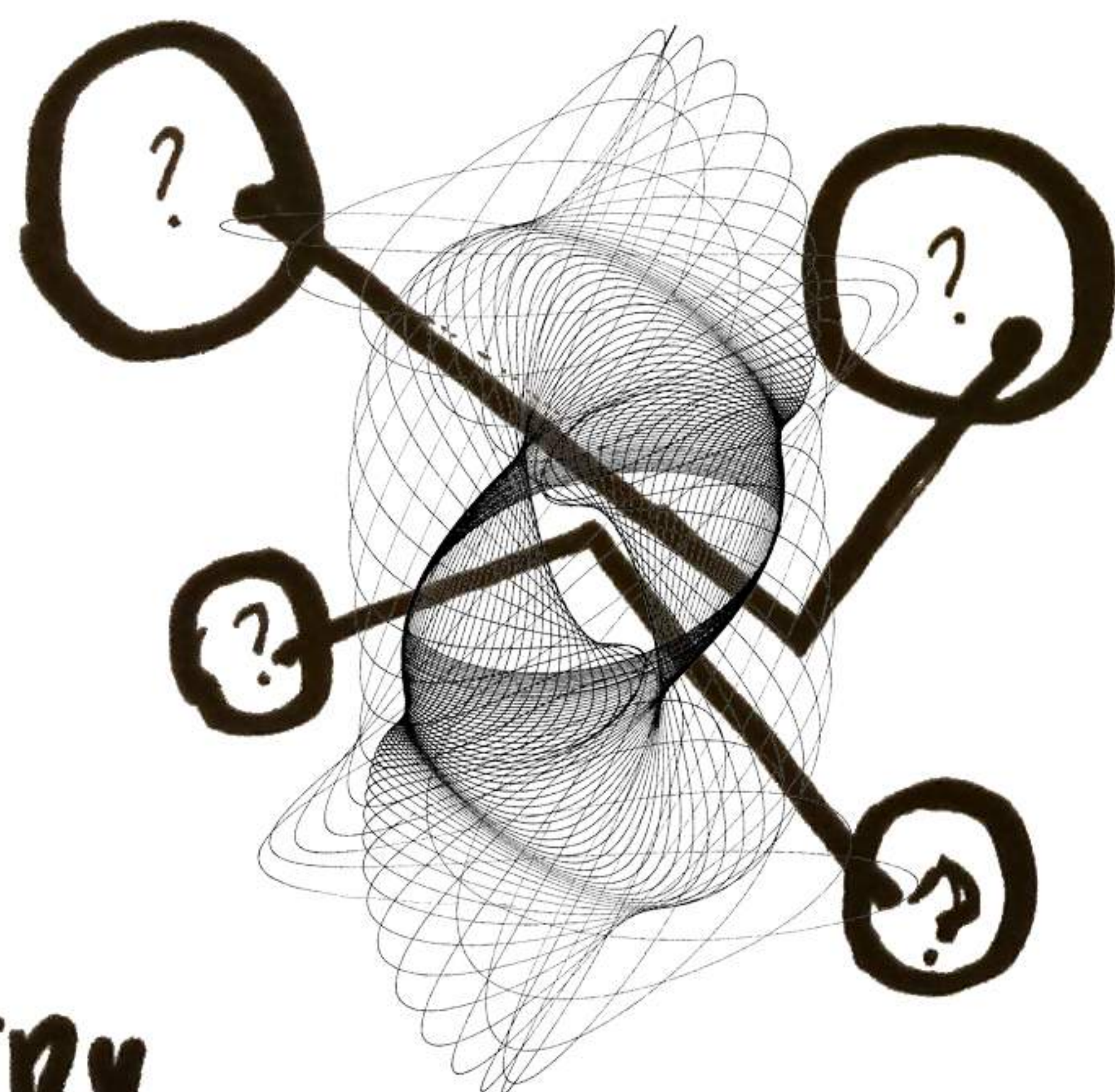
HOW WAS IT
MADE?

FEATURES

~~and display~~

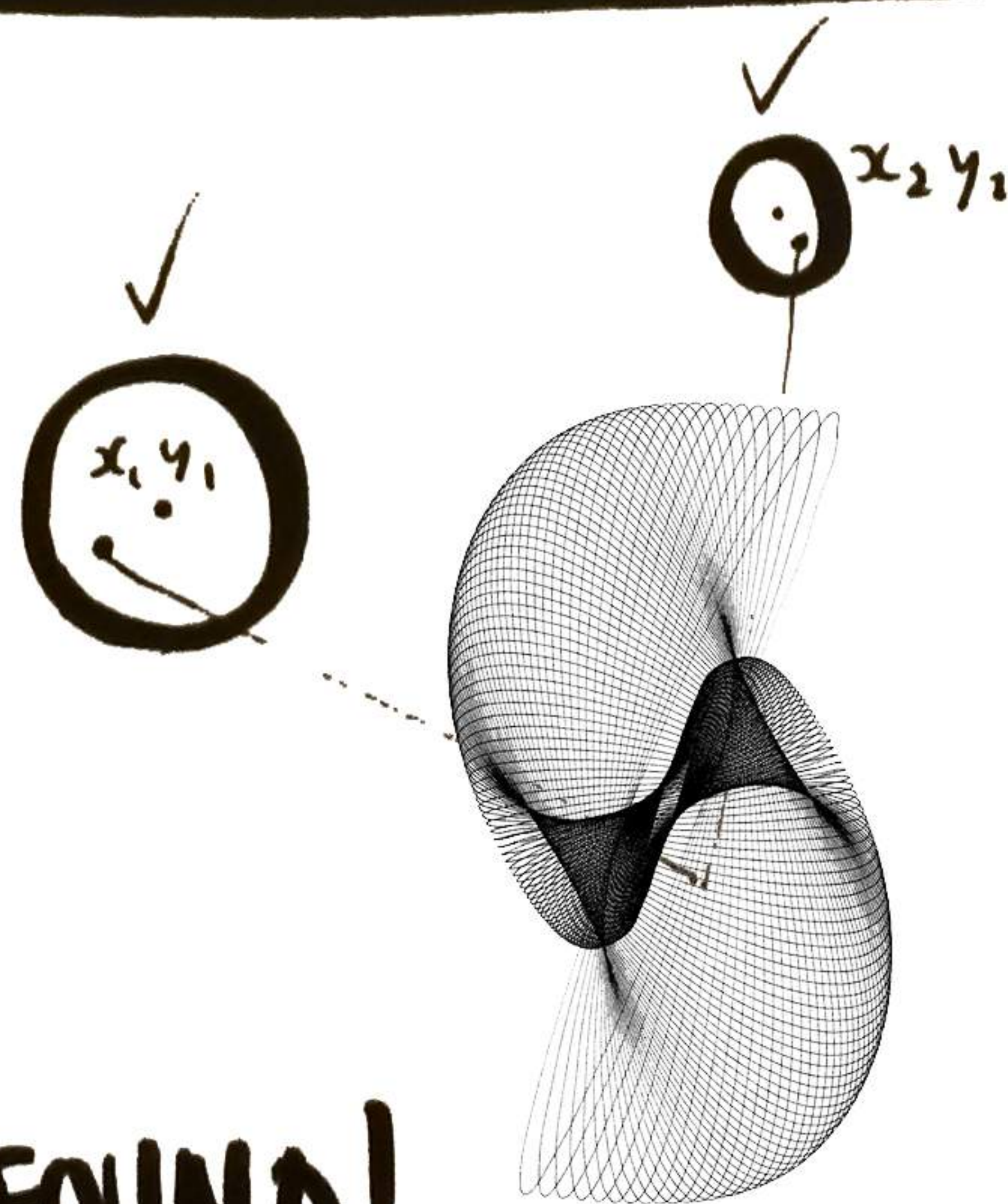
- speed up the drawing process (or slow down)
→ use timelined properly
- gears visualization $\begin{cases} \text{ON} \\ \text{OFF} \end{cases}$
- visualize with formulas
- color the cycloid by clicking inside the white spaces
- let Python color the drawing randomly

2 how was it made?
which gears? which radius?



TRY...

3 You Win!



FOUND!



MODE II

LOOK AT THE DRAWING, RETRIEVE THE ORIGINAL MECHANISM

CHALLENGES:

- TRIGONOMETRY (HARD MATH TO RECREATE THE MECHANISM)
- GRAPHIC USER INTERFACE (simple but precise!)
- EDUCATIONAL GOAL

EXTRA POSSIBLE FEATURES:

- COLOR THE CYCLOID ON TKINTER
- EXPORT TO DXF/DWG ...
- HISTORIC / MATH EXPLANATIONS