

Cambridge International AS & A Level

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

MATHEMATICS 9709/21

Paper 2 Pure Mathematics 2

October/November 2021

1 hour 15 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

This document has 16 pages. Any blank pages are indicated.

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Find the exact value of $\int_{-1}^{2} (4e^{2x} - 2e^{-x}) dx.$	
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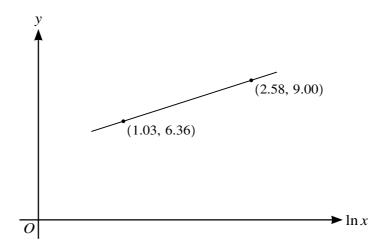
		4
2	(a)	Sketch, on the same diagram, the graphs of $y = 3x$ and $y = x - 3 $. [2]
	(b)	Find the coordinates of the point where the two graphs intersect. [3]

Deduce the solution of the inequality $3x < x - 3 $.	[1]

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(c)

3



The variables x and y satisfy the equation $a^y = kx$, where a and k are constants. The graph of y against $\ln x$ is a straight line passing through the points (1.03, 6.36) and (2.58, 9.00), as shown in the diagram.

Find the values of a and k , giving each value correct to 2 significant figures.	[5]

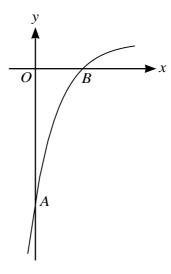
The curve with equation $y = xe^{2x} + 5e^{-x}$ has a minimum point M.

4

(a)	Show that the <i>x</i> -coordinate of <i>M</i> satisfies the equation $x = \frac{1}{3} \ln 5 - \frac{1}{3} \ln (1 + 2x)$.	[5]
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5



The diagram shows the curve with parametric equations

$$x = \ln(2t+3),$$
 $y = \frac{2t-3}{2t+3}.$

The curve crosses the y-axis at the point A and the x-axis at the point B.

(a)	Show that $\frac{dy}{dx} = \frac{6}{2t+3}$.	[4]

Find the gradient of the curve at R	
Find the gradient of the curve at B .	
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Find the gradient of the curve at <i>B</i> .	

6	The polyno	omials $f(x)$	and $g(x)$	are defined	by
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$$f(x) = 4x^3 + ax^2 + 8x + 15$$
 and $g(x) = x^2 + bx + 18$,

where a and b are constants.

(a)	Given that $(x + 3)$ is a factor of $f(x)$, find the value of a .	[2
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(b)	Given that the remainder is 40 when $g(x)$ is divided by $(x-2)$, find the value of b .	[2]
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Hence solve th	e equation f(co	sec θ) – g(cose	$c(\theta) = 0 \text{ for } 0 < \theta$	< 2π.	

[By first expanding $\cos(2\theta + \theta)$, show that $\cos 3\theta = 4\cos^3 \theta - 3\cos \theta$.
I	Find the exact value of $2\cos^3(\frac{5}{18}\pi) - \frac{3}{2}\cos(\frac{5}{18}\pi)$.

	$\int (12\cos^3 x)$							
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Additional Page

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