

Cambridge International AS & A Level

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

8 4 8 9 3 5 4 9 7 3

FURTHER MATHEMATICS

9231/33

Paper 3 Further Mechanics

October/November 2020

1 hour 30 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- Where a numerical value for the acceleration due to gravity (g) is needed, use $10 \,\mathrm{m\,s^{-2}}$.

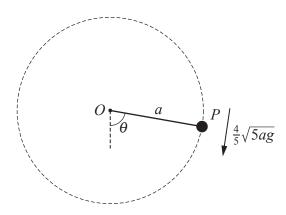
INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

This document has 16 pages. Blank pages are indicated.

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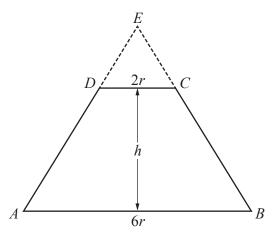
A l oth	article P of mass m is placed on a fixed smooth plane which is inclined at an angle θ to the horight spring, of natural length a and modulus of elasticity $3mg$, has one end attached to P er end attached to a fixed point O at the top of the plane. The spring lies along a line of the plane. The system is released from rest with the spring at its natural length.	and the
Fin mo	d, in terms of a and θ , an expression for the greatest extension of the spring in the subtion.	sequent [3]
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A particle P is attached to one end of a light inextensible string of length a. The other end of the string is attached to a fixed point O. The particle P is held with the string taut and making an angle θ with the downward vertical. The particle P is then projected with speed $\frac{4}{5}\sqrt{5ag}$ perpendicular to the string and just completes a vertical circle (see diagram).

Find the value of $\cos \theta$.	[5]

dow	rnward vertical through O. The length of the string during this motion	g inclined at an angle θ to the on is $(k+1)a$.
(a)	Find the value of k .	[4
(b)	Find the value of $\cos \theta$.	[:



The diagram shows the cross-section ABCD of a uniform solid object which is formed by removing a cone with cross-section DCE from the top of a larger cone with cross-section ABE. The perpendicular distance between AB and DC is h, the diameter AB is h and the diameter h is h and h is h is h is h is h in h is h in h in

Find an expression, in terms of h , for the distance of the centre of mass of the solid object from λ

The object is freely suspended from the point B and hangs in equilibrium. The angle between AB and the downward vertical through B is θ .

Given that $h = \frac{13}{4}r$, find the value of $\tan \theta$.	
	•••••

Derive the equation of the trajectory of P in	the form
Show that the x-coordinate of Q is $\frac{u}{2g}$.	[3]
	Derive the equation of the trajectory of P in $y = x \tan \alpha$

(c)	Find the other value of α for which P would pass through the point Q .	[4]
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ı he	e coefficient of restitution between the spheres is e .	
(a)	Find, in terms of u and e , the velocities of A and B after the collision.	[3
f <i>B</i> `he	esequently, <i>B</i> collides with a fixed vertical wall which makes an angle θ with <i>B</i> , where $\tan \theta = \frac{3}{4}$. The coefficient of restitution between <i>B</i> and the wall is $\frac{2}{3}$. Immediately after a kinetic energy of <i>B</i> .	
of <i>B</i> The he l	B, where $\tan \theta = \frac{3}{4}$. The coefficient of restitution between B and the wall is $\frac{2}{3}$. Immediately after a kinetic energy of A is $\frac{5}{32}$ of the kinetic energy of B.	B collides with the wal
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a)	Show that the velocity $v \text{m s}^{-1}$ of P is given by $v = \frac{10(1-2x)}{x}$.	[5]
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