

Overview and Schedule

Part I. Introduction (Monday)

Part 2. Continental Extension Tutorial (Monday)

Part 3. Melting at Mid-Ocean Ridge Tutorial (Tuesday)

Part 4. Detailed look at ASPECT and Tinker Time (Wednesday)



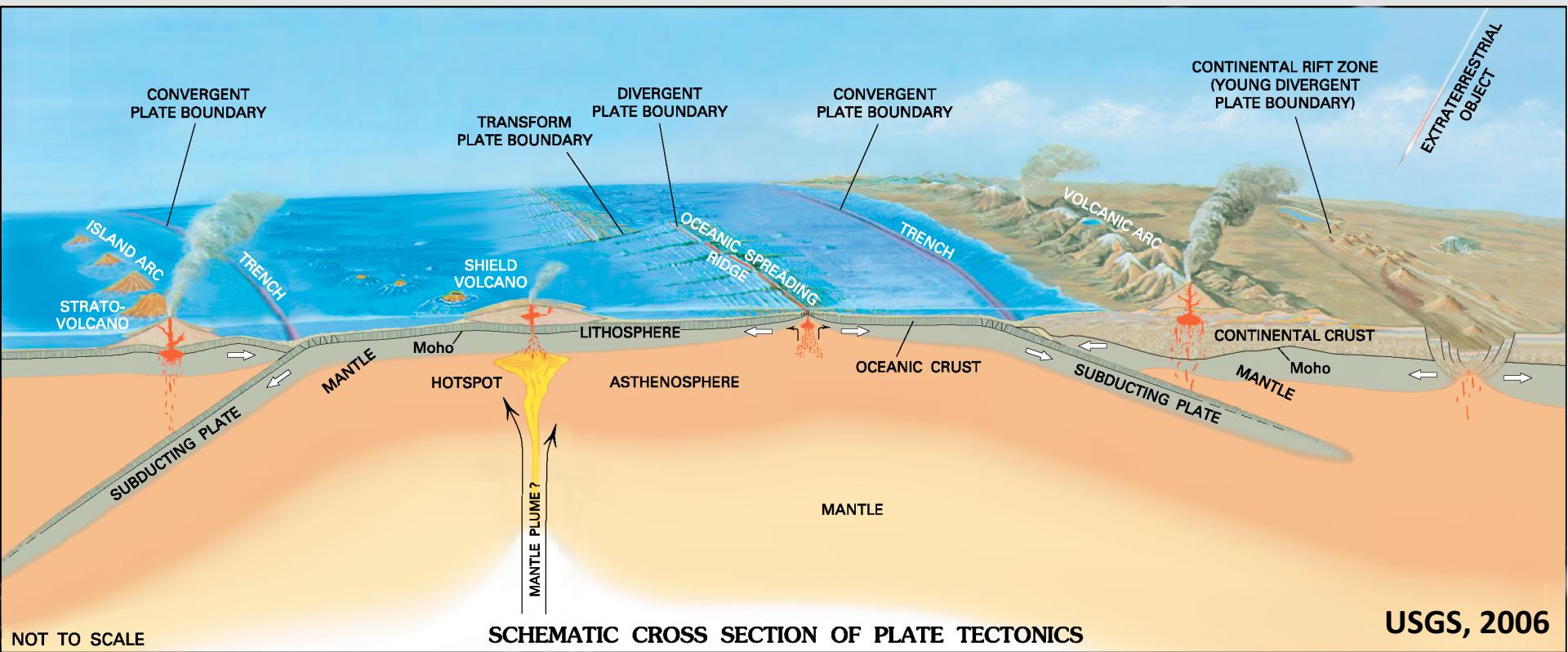
Numerical Modeling From Start to Finish



1. Define what physical processes to examine
2. Capture the physics through mathematical equations
3. Choose a numerical approximation to solve the equations
4. Design, write and validate software (or validate existing code)
5. Formulate a hypothesis to test
6. Design and run a series of models
7. Verify and interpret results



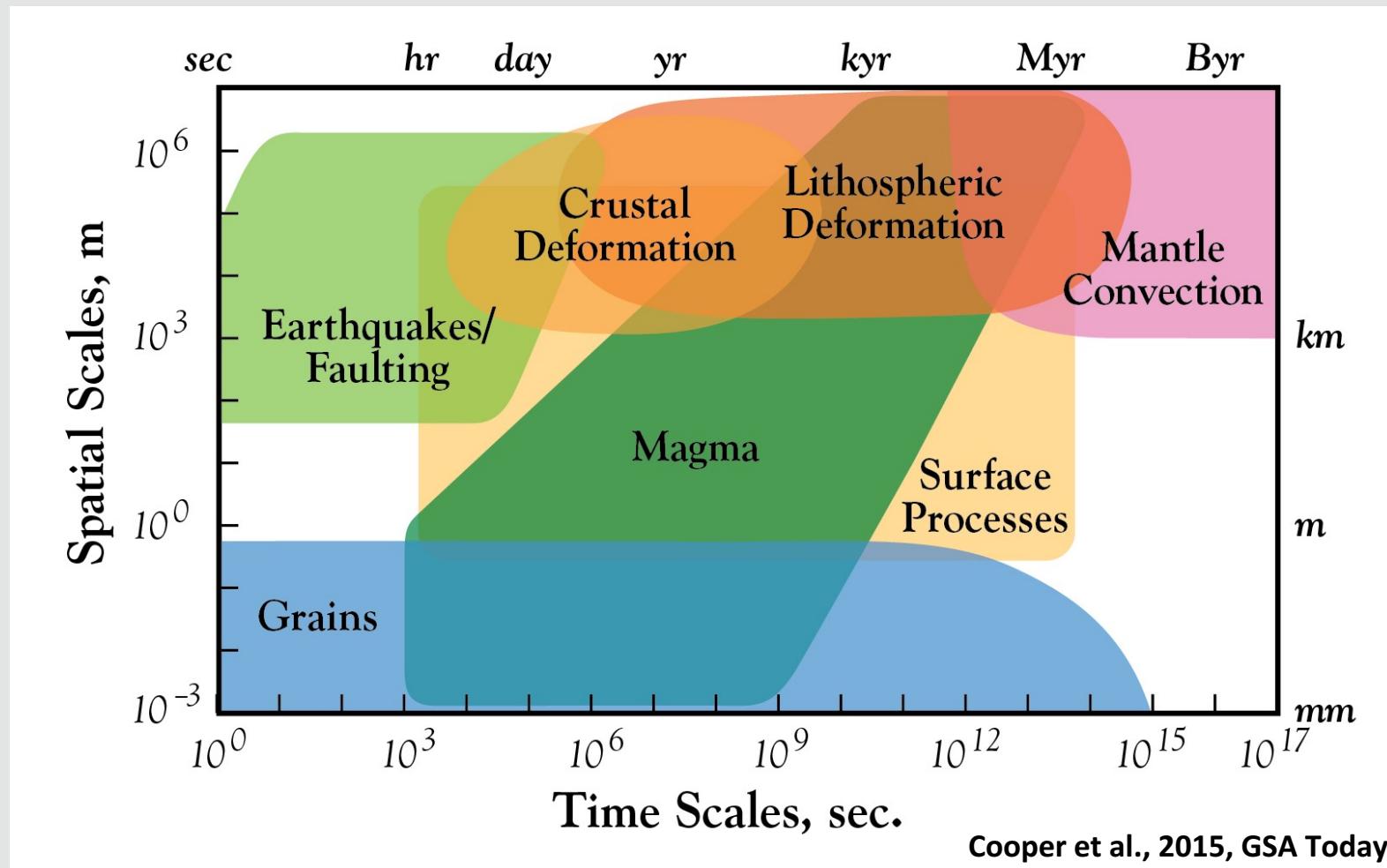
Physical Processes: Long-Term Tectonics



Crustal Deformation, Lithospheric Deformation, Mantle Convection

- Capture the physical processes through mathematical equations

Relevant Temporal and Spatial Scales



Long-Term Tectonics

10^3 to 10^8 years, 10's to 1000's of km



Capture Physics Through Equations

Governing Equations (Incompressible Viscous Flow)

$$\nabla \cdot u = 0$$
 Conservation of Mass

$$\nabla \cdot \sigma' - \nabla P + \rho g = 0$$
 Conservation of Momentum

$$\rho c \left(\frac{\partial T}{\partial t} + u \cdot \nabla T \right) = \nabla \cdot K \nabla T + H$$
 Conservation of Energy

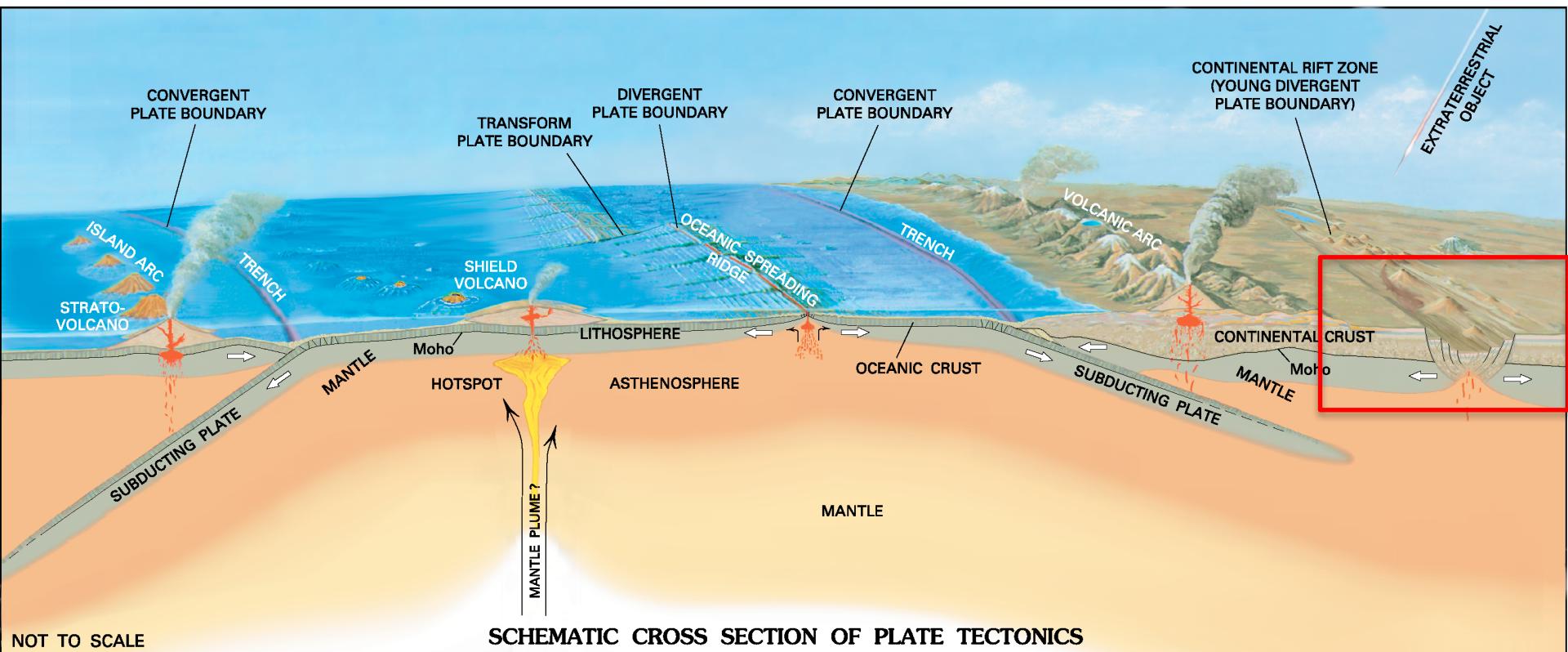
Constitutive Relationships (Rheology)

$$\sigma' = A^{-1/n} \dot{\varepsilon}^{-1/n} d^{m/n} e^{\frac{Q+PV}{nRT}}$$
 Nonlinear Viscous Flow

$$\sigma' = P \sin \theta + C \cos \theta$$
 Brittle Failure



Formulate a Hypothesis to Test



Controls on deformation patterns?

Rheology, Rates of Deformation, Inheritance, ...

Continental Extension

Geometry

$y = 0 \text{ km}$



$x = 0 \text{ km}$
 $y = 100 \text{ km}$

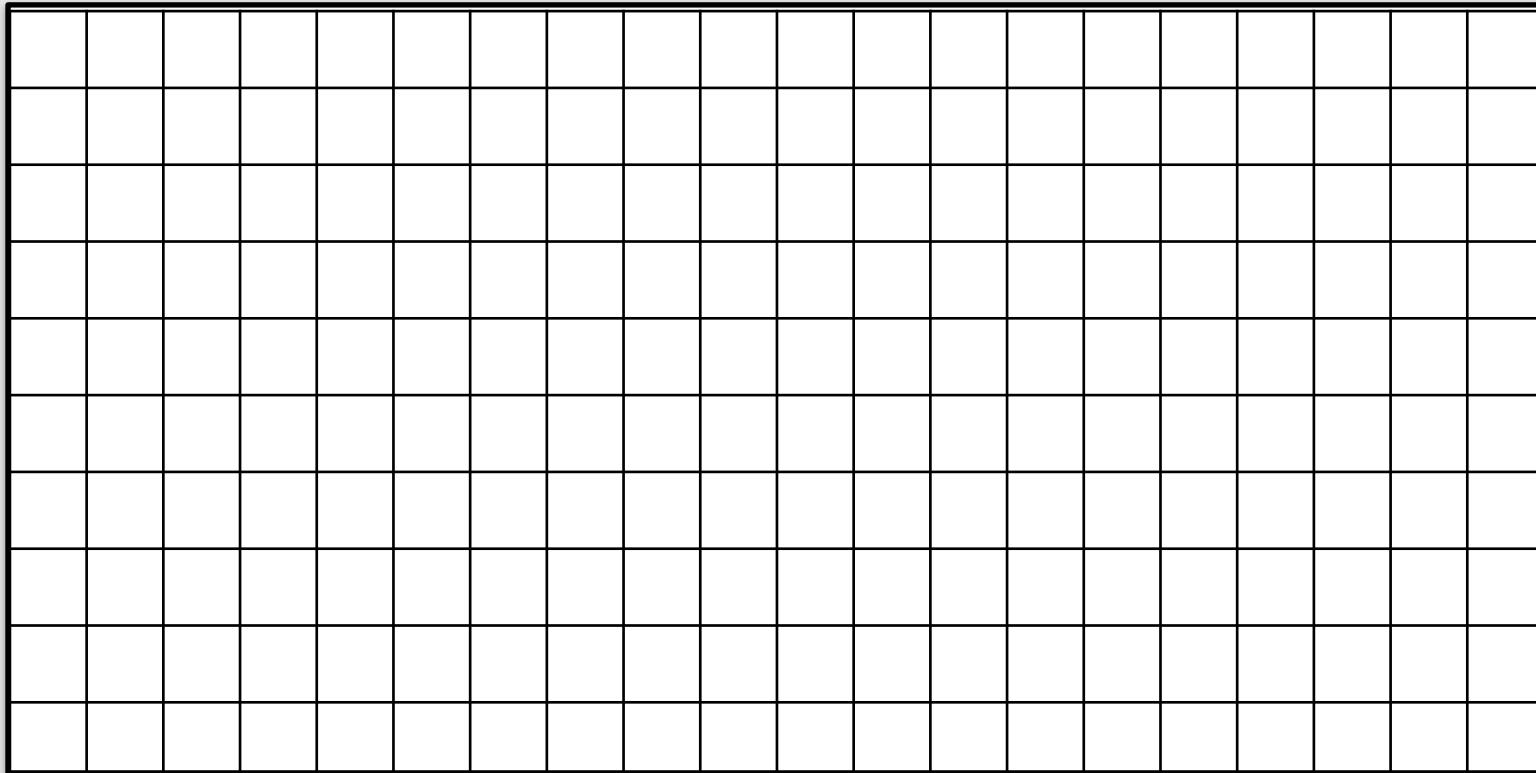
$x = 200 \text{ km}$
 $y = 100 \text{ km}$



Grid Resolution

$y = 0 \text{ km}$

10 km Spacing (Coarse Mesh)



$x = 0 \text{ km}$
 $y = 100 \text{ km}$

“Appropriate” resolution depends on process

Each study requires a resolution test

$x = 200 \text{ km}$
 $y = 100 \text{ km}$



Initial Conditions (Lithology)

$y = 0 \text{ km}$

Non-linear flow law
Brittle Yield Criterion

Crust (30 km)

2700 kg m^{-3}

Weak Seed

Non-linear flow law
Brittle Yield Criterion

Mantle (70 km)

3300 kg m^{-3}

$x = 0 \text{ km}$
 $y = 100 \text{ km}$

- ✓ Thermodynamic Properties
- ✓ Distinct Material Properties

$x = 200 \text{ km}$
 $y = 100 \text{ km}$



Initial and Boundary Conditions (Temperature)

Variable Temperature (Insulating)

$y = 0 \text{ km}$

Fixed Temperature

$T = 0^\circ \text{ C}$

Non-linear flow law
Brittle Yield Criterion

Crust (30 km)

2700 kg m^{-3}

$T = 500^\circ \text{ C}$

Weak Seed

Non-linear flow law
Brittle Yield Criterion

Mantle (70 km)

3300 kg m^{-3}

Variable Temperature (Insulating)

$x = 0 \text{ km}$
 $y = 100 \text{ km}$

Fixed Temperature

$T = 1200^\circ \text{ C}$

Continental Geotherm

$x = 200 \text{ km}$
 $y = 100 \text{ km}$



Numerical Model Design

Temporal Constraints, Discretization, Solver Settings

$y = 0 \text{ km}$

Free Surface ~ Stress Free ($V_y = \text{free}$, $V_x = \text{free}$)

$T = 0^\circ \text{ C}$

Non-linear flow law
Brittle Yield Criterion

Crust (30 km)

2700 kg m^{-3}

$T = 500^\circ \text{ C}$

Non-linear flow law
Brittle Yield Criterion

Weak Seed

Mantle (70 km)

3300 kg m^{-3}

$V_y: \text{free}$
 $V_x: \text{fixed}$

$V_y: \text{free}$
 $V_x: \text{fixed}$

($V_y: \text{fixed}$, $V_x: \text{free}$)

$T = 1200^\circ \text{ C}$

$x = 0 \text{ km}$
 $y = 100 \text{ km}$

$x = 200 \text{ km}$
 $y = 100 \text{ km}$



How long will the model run, time step-size, element type, solver tolerance?

Velocity Boundary Conditions

$y = 0 \text{ km}$

Free Surface ~ Stress Free ($V_y = \text{free}$, $V_x = \text{free}$)

$T = 0^\circ \text{ C}$

Non-linear flow law
Brittle Yield Criterion

Crust (30 km)

2700 kg m^{-3}

$T = 500^\circ \text{ C}$

\leftarrow
 $V_y: \text{free}$
 $V_x: \text{fixed}$

Weak Seed

Non-linear flow law
Brittle Yield Criterion

Mantle (70 km)

3300 kg m^{-3}

\rightarrow
 $V_y: \text{free}$
 $V_x: \text{fixed}$

$(V_y: \text{fixed}, V_x: \text{free})$

$T = 1200^\circ \text{ C}$

$x = 0 \text{ km}$
 $y = 100 \text{ km}$

$x = 200 \text{ km}$
 $y = 100 \text{ km}$



Options: free-slip, free surface, fixed (no-slip), periodic



Continental Extension Cookbook

Instructions

1. Open a terminal in the virtual machine
 2. Copy the continental extension cookbook file to the Desktop

cp aspect/cookbooks/continental_extension.prm Desktop/

3. Rename the file to continental_extension_res4km.prm

```
mv continental_extension.prm continental_extension_res4km.prm
```

Continental Extension Cookbook

Instructions continued

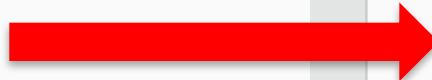
4. Open continental_extension_res4km.prm in a text editor (double click file)
5. Change the grid resolution from 2 km to 4 km (see images below)

Change the value of X repetitions from 200 to 100

Change the value of Y repetitions from 50 to 25

```
# Model geometry (400x100 km, 2 km spacing)
subsection Geometry model
    set Model name = box
    subsection Box
        set X repetitions = 200
        set Y repetitions = 50
        set X extent      = 400e3
        set Y extent      = 100e3
    end
end
```

```
# Model geometry (400x100 km, 4 km spacing)
subsection Geometry model
    set Model name = box
    subsection Box
        set X repetitions = 100
        set Y repetitions = 25
        set X extent      = 400e3
        set Y extent      = 100e3
    end
end
```

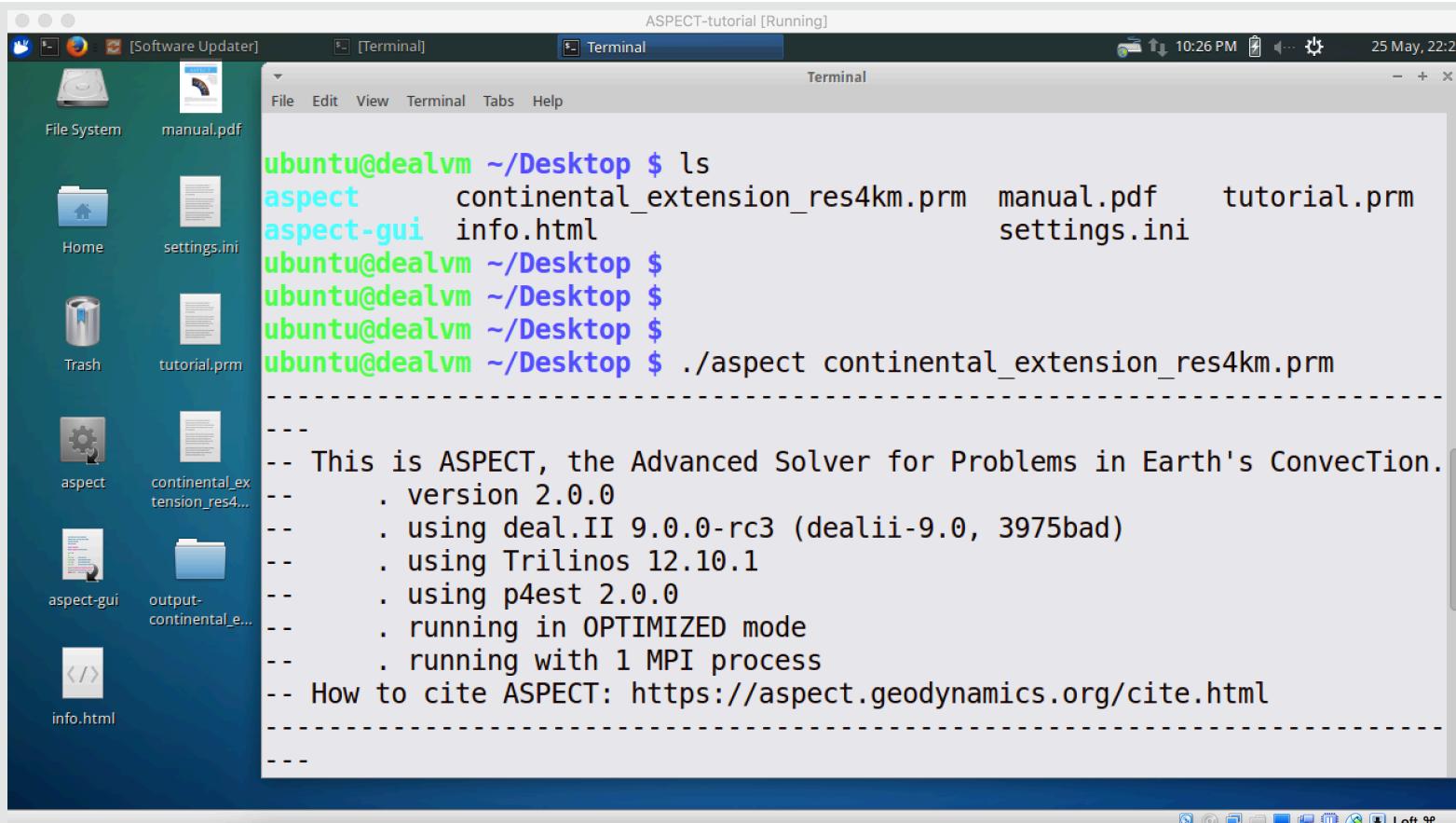


Continental Extension Cookbook

Instructions continued

6. Run the modified continental extension cookbook

./aspect continental_extension_res4km.prm



The screenshot shows a Linux desktop environment with a Unity interface. A terminal window titled "Terminal" is open, showing the command-line interface for the ASPECT solver. The terminal output is as follows:

```
ASPECT-tutorial [Running]
[Software Updater] [Terminal] Terminal
File Edit View Terminal Tabs Help
ubuntu@dealvm ~/Desktop $ ls
aspect      continental_extension_res4km.prm  manual.pdf    tutorial.prm
aspect-gui   info.html                  settings.ini
ubuntu@dealvm ~/Desktop $
ubuntu@dealvm ~/Desktop $
ubuntu@dealvm ~/Desktop $
ubuntu@dealvm ~/Desktop $ ./aspect continental_extension_res4km.prm
-----
-- This is ASPECT, the Advanced Solver for Problems in Earth's Convection.
-- . version 2.0.0
-- . using deal.II 9.0.0-rc3 (dealii-9.0, 3975bad)
-- . using Trilinos 12.10.1
-- . using p4est 2.0.0
-- . running in OPTIMIZED mode
-- . running with 1 MPI process
-- How to cite ASPECT: https://aspect.geodynamics.org/cite.html
-----
```



Parameter File: Global, Geometry & Mesh



```
set Dimension = 2
```

```
set Start time = 0
```

```
set End time = 5e6
```

```
set Use years in output instead of  
seconds = true
```

```
set Nonlinear solver scheme = single  
Advection, iterated Stokes
```

```
set Nonlinear solver tolerance = 1e-4
```

```
set Max nonlinear iterations = 10
```

```
set CFL number = 0.5
```

```
subsection Geometry model  
set Model name = box
```

```
subsection Box  
set X repetitions = 200  
set Y repetitions = 50  
set X extent      = 400e3  
set Y extent      = 100e3  
end
```

```
end
```

```
subsection Mesh refinement  
set Initial adaptive refinement      = 0  
set Initial global refinement        = 0  
set Time steps between mesh refinement = 0  
end
```



Parameter File: Boundary Velocity

```
subsection Free surface
```

```
    set Free surface boundary indicators = top  
end
```

```
subsection Boundary velocity model
```

```
    set Prescribed velocity boundary indicators = left x: function, right x: function, \  
                                bottom y: function
```

```
subsection Function
```

```
    set Variable names = x,y  
    set Function constants = cm=0.01, year=1  
    set Function expression = if (x<200e3 , -0.25*cm/year, 0.25*cm/year) ; 0.125*cm/year;  
end
```

```
end
```



Parameter File: Initial Temperature

subsection Initial temperature model

set Model name = function

subsection Function

set Variable names = x,y

set Function constants = h=100e3,ts1=273,ts2=681.5714,ts3=823., \
k1=2.5,k2=2.5,k3=3.3,A=1.5e-6, \
qs1=0.0653571,qs2=0.035357,qs3=0.035357,qb3=0.035357

set Function expression = if((h-y)<=20.e3, \
ts1 + (qs1/k1)*(h-y) - (A*(h-y)*(h-y))/(2.0*k1), \
if((h-y)>20.e3 && (h-y)<=30.e3, ts2 + (qs2/k2)*(h-y-20.e3), \
ts3 + (qs3/k3)*(h-y-30.e3)));

end

end

Parameter File: Boundary Temperature



```
subsection Boundary temperature model
```

```
    set Fixed temperature boundary indicators = bottom, top  
    set List of model names = box
```

```
subsection Box
```

```
    set Bottom temperature = 1573  
    set Top temperature     = 273
```

```
end
```

```
end
```



Parameter File: Composition

```
subsection Compositional fields
```

```
    set Number of fields = 4
```

```
    set Names of fields = upper, lower, mantle, seed
```

```
end
```

```
subsection Initial composition model
```

```
    set Model name = function
```

```
    subsection Function
```

```
        set Variable names = x,y
```

```
        set Function expression = if(y>=80.e3, 1, 0); \
```

```
                        if(y<80.e3 && y>=70.e3, 1, 0); \
```

```
                        if(y<70.e3 && y>-100.e3, 1, 0); \
```

```
                        if(y<68.e3 && y>60.e3 && x>=198.e3 && x<=202.e3 , 1, 0);
```

```
    end
```

```
end
```

```
subsection Boundary composition model
```

```
    set Fixed composition boundary indicators = bottom
```

```
end
```



Parameter File: Material Properties

subsection Material model

set Model name = visco plastic

subsection Visco Plastic

set Minimum viscosity = 1e18

set Maximum viscosity = 1e26

set Densities = 3300, 2800, 2900, 3300, 300

set Prefactors for dislocation creep = 6.52e-16, 8.57e-28, 7.13e-18, 6.52e-16, 7.13e-18

set Stress exponents for dislocation creep = 3.5, 4.0, 3.0, 3.5, 3.0

set Activation energies for dislocation creep = 530.e3, 223.e3, 345.e3, 530.e3, 345.e3

set Activation volumes for dislocation creep = 18.e-6, 0., 0., 18.e-6, 0.

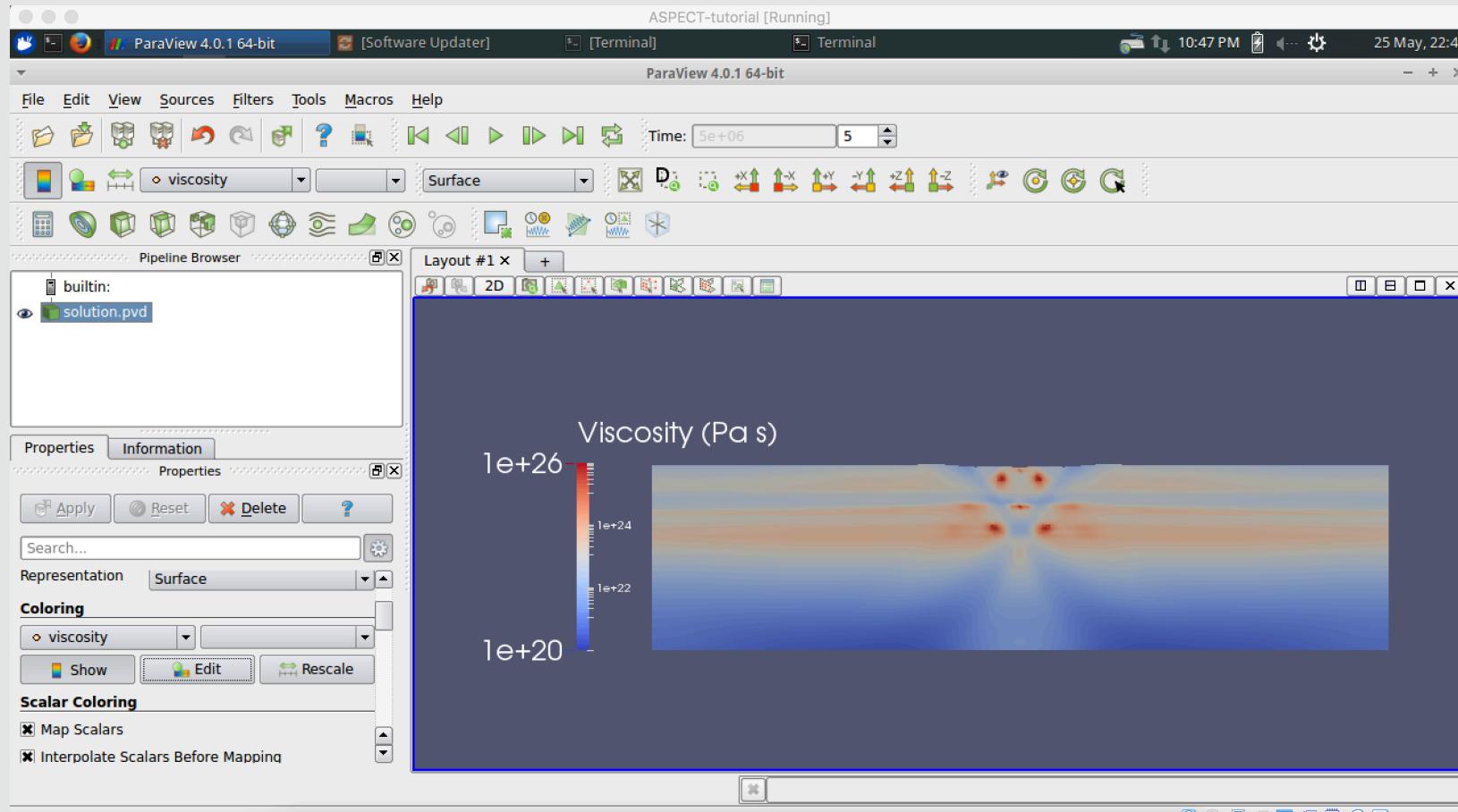
Plasticity parameters

set Angles of internal friction = 20., 20., 20., 20., 20.

set Cohesions = 20.e6, 20.e6, 20.e6, 20.e6, 20.e6

Model Postprocessing

Visualize the model results with Paraview



Sensitivity Analysis Parameters

- ✓ Grid Resolution
- ✓ Particles-Per-Cell
- ✓ Time-Step Size
- ✓ Model Geometry
- ✓ Initial Lithology
- ✓ Initial Temperature
- ✓ Boundary Conditions
- ✓ Solver convergence settings
- ✓ Viscous flow law
- ✓ Brittle Yield Mechanism
- ✓ Brittle parameters
- ✓ Strain-weakening (magnitude, rate)
- ✓ Elastic Constants

As an exercise, try varying some these parameters in the continental extension cookbook!

