

# **Visualising Ant Colony Optimisation**

Final Report for CS39440 Major Project

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## **Abstract**

Ant Colony Optimisation algorithms are a commonly used family of swarm intelligence methods. The underlying concepts of such algorithms can be difficult to comprehend for people who have recently come across the subject area. The majority of existing applications that visualise such algorithms either inadequately do so or rely on the user having some prior knowledge about the underlying behaviours in order to fully utilise the application. The author of this project aims to create an application for deployment in educational environments allowing for a richer, more interactive experience in regards to the teaching of Ant Colony Optimisation methods. The author has set out to achieve a full visual representation of the algorithms execution whilst also providing an intuitive user interface enabling user defined algorithm parameters and a choice of algorithm types and modifiers.

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# Chapter 1

## Background

### 1.1 Algorithm Overview

Ant Colony Optimisation is a probabilistic technique usually used on problems which can be resolved by returning an optimal path through a graphical representation of a given problem. Ant Colony Optimisation refers to a collection of methods and techniques which represent a specific family in Swarm Intelligence. Swarm Intelligence “...deals with natural and artificial systems composed of many individuals that coordinate using decentralized control and self-organization. In particular, the discipline focuses on the collective behaviours that result from the local interactions of the individuals with each other and with their environment” [14]. In summary each agent is simple and follows a series of basic rules as it performs its operations. If you increase the population of these agents and allow them to communicate with each other then the world they populate will express an emergence of intelligence otherwise unavailable to any individual agent. Ultimately each agent collectively works towards the same goal increasing the quality and appropriateness of the result.

Ant Colony Optimisation algorithms stemmed from the initial proposal by Marco Dorigo et al. through the publication of his PhD in 1992 [6]. The Algorithms are based upon the real world behaviour of ant colonies. Ants in the real world will generally always find the most optimal path between two or more locations, often described as the route between their nest site and the location of the food source(s). As an ant leaves the colony in search of a food source it begins to deposit a chemical trail (pheromone) which can be analysed by other ants in the population. Once an ant has deposited the pheromone it is subject to decay. As the pheromone decays, new pheromone will be deposited by other ants in the colony. As more and more ants continue their tour the locations which have the highest concentration of pheromone are generally the most traversed locations. Ultimately the locations with the highest concentration of pheromone will not only be the most frequently used but will also form the optimal route between the start location and the destination(s). Every location is subject to such decay however the most commonly used locations will constantly be topped up by the population whereas the locations used less frequent will eventually decay to low pheromone levels. The pheromone levels are important because they directly influence the probabilistic function for any ant choosing its next location at any intersection. The higher the concentration of pheromone, the greater the probability that the ant will choose this location as the next stop on its tour. As this is a probabilistic decision the ant may not always choose the location with the highest concentration levels allowing for other solutions

to be sought after, enabling shifts in the current best route.

## 1.2 Double Bridge Experiment

The double bridge experiment is an early experiment devised to help understand the real world behaviour of ants and their path finding capabilities. The double bridge experiment, as the name suggests, involves a nest location separated from a single food source by two bridges. This experiment was designed and carried out by Deneubourg and colleagues in 1989-1990 and used real Argentine ants [12].

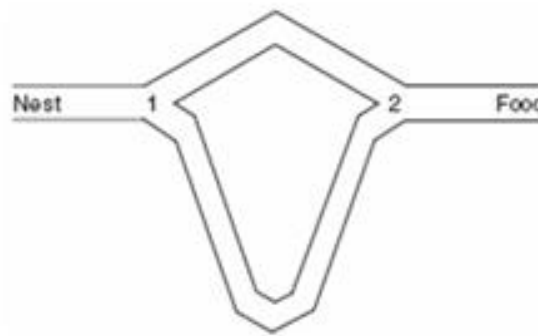


Figure 1.1: Image representing the Double Bridge Experiment. Image source [24]

Figure 1.1 represents the scenario the Argentine ant were faced with for the Double Bridge Experiment. Initially there will be no pheromone trails for the ants to follow, so as the first ant approaches intersection marked “1” in figure 1.1 the probability that they choose the top path, or lower path is therefore  $\approx 50\%$ . Regardless of which path the ant chose pheromone will now be deposited on the corresponding path. The next ant will approach the intersection marked “1” however, as there now exists a pheromone trail this ant now no longer has an equal probability to choose either path but instead is more likely to choose the same path as the previous ant. This process will continue for every ant in the colony. Generally speaking as the bottom path is significantly longer than the top path, the pheromone deposited on the lower path will ultimately have a lower pheromone concentration than the shorter top path. Overtime this will cause more and more ants to take the top path over the bottom path due to the higher pheromone level directly impacting the probability of the ant choosing this path. The same applies to intersection marked “2”, the ants will still tend to prefer the path with the greater pheromone concentration, the fact that the ant now has food does not affect the ants choice in anyway, aside from the fact that the ants new target is the nest and no longer the food source.

## 1.3 Travelling Salesman Problem

Ant Colony algorithms are commonly applied to the Travelling Salesman Problem (TSP). The TSP consists of a graph of  $n$  cities and a path between these  $n$  cities must be found however, each city must be visited exactly once. Generally this  $n$  value is rather large for example the Berlin52 [17] is a variation of the TSP where this  $n$  value is 52. The number of possible routes between these 52 cities is incredibly large and exploring every combination is a near impossibility. The application

of heuristic algorithms such as the Ant Colony methods enables solutions to be found within a reasonable time. One solution for the Berlin52.tsp problem is shown in figure 1.2.

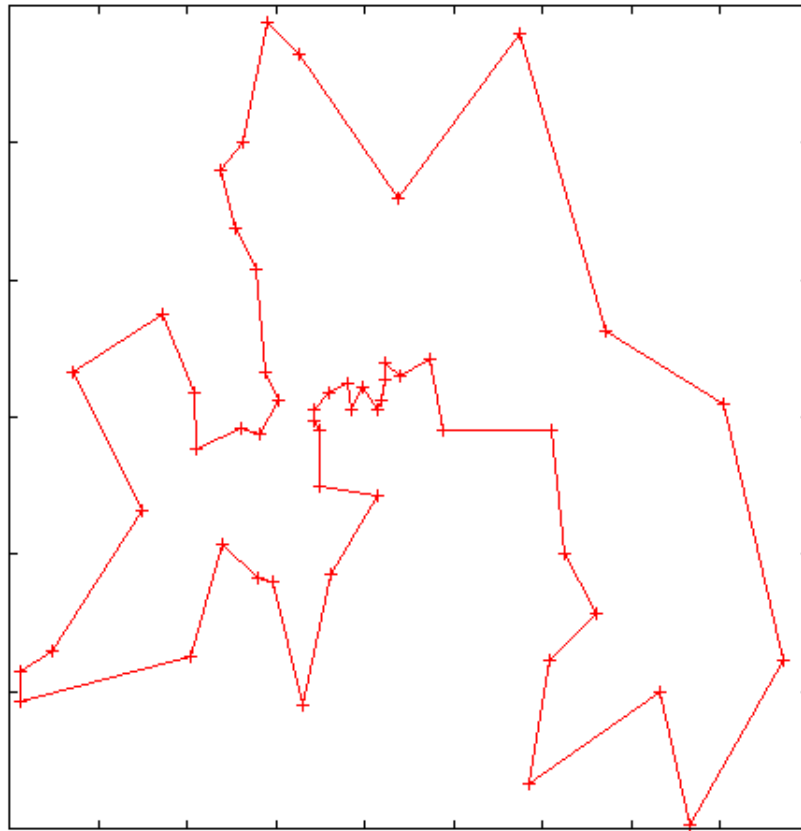


Figure 1.2: One solution to the Berlin52.tsp problem plotted using GNU Plot. Modified version from original image source [5]

The TSP is not the only problem which can be tackled using the Ant Colony family of methods. As these methods have metaheuristic properties the general behaviours and structure can be applied to several other problems such as image segmentation however, this project will not cover such application and will focus on the TSP style of problem.

## 1.4 Ant System

The Ant System is the most basic implementation of an Ant Colony Optimisation method, because of this it provides the basis for extensions and variations. Due to its basic nature, the Ant System is ideal for demonstrating and teaching the behaviours of a virtual ant colony to a user, and it can be done regardless of their prior background knowledge. In this implementation there is no recollection of the best path between iterations and every agent is equal in terms of its importance in finding a solution.

### 1.4.1 Formulæ

Sections 1.4.1.1 and 1.4.1.2 refer to the underlying formulae which govern the ants probability of selection and pheromone deposits for a given edge.

#### 1.4.1.1 Probability

The probability formula is as described in appendix B, section 2.6.2.1. This is the function which drives the ants movement and enabled ants to generally pick the best looking path (path with the strongest pheromone concentration) whilst also allowing for ants to select other paths helping to prevent localised solutions forming.

#### 1.4.1.2 pheromone

The pheromone function for the Ant System algorithm is as described in appendix B, section 2.6.2.2. This function is the main difference between the Ant System implementation and the Elitist Ant System.

## 1.5 Elitist Ant System

The Elitist Ant System is the first adaptation to the initial Ant System algorithm. The Elitist Ant System is again, proposed by Marco Dorigo et al. in his 1992 PhD Thesis [6]. The main difference between the Elitist Ant System and the Basic Ant System is the fact that the best ants for a given iteration have pheromone deposited upon their route. This means that the best  $x$  number of ants where  $x$  is an integer representing the number of elite ants will have their routes remembered across iterations preserving their best routes knowledge. This generally improves performance of the population as a whole as the extra pheromone on these elite paths will increase the probability that any ant traverses an elite edge (an edge that is part of a best routes).

### 1.5.1 Formulæ

Sections 1.5.1.1 and 1.5.1.2 refer to the underlying formulae which govern the ants probability of selection and pheromone deposits for a given edge.

#### 1.5.1.1 Probability

The probability function for the Elitist Ant System remains the same as it is in the Basic Ant System, see section 1.4.1.1 and appendix B, section 2.6.2.2

#### 1.5.1.2 pheromone

The pheromone function used in the Elite Ant System must acknowledge that there is pheromone to be deposited along the current  $x$  elite routes.

$$p_{xy}^k = (1 - \rho)\tau_{xy}^k + \Delta\tau_{xy}^k + e\Delta\tau_{xy}^{best} \quad (1)$$

Figure 1.3: Algebraic model of the pheromone deposit function for the Elitist Ant System [11]

The majority of the formula remains the same as defined in appendix B section 2.6.2.2 however, there is the addition  $e\Delta\tau_{xy}^{best}$ . This is the part of the formula which is responsible for the pheromone deposit on current the retained best (elite) paths.  $xy$  refers to the  $x$  and  $y$  coordinate for an edge in the best path this is where pheromone will be deposited. *best* simply donates that this edge belongs to one of the currently stored best paths. The  $e$  value is a constant, and varies between implementations. Research suggests that a good value for this constant,  $e$  is  $\frac{1}{4} \cdot \# \text{ of nodes}$  [23] however, there is evidence to support using  $\# \text{ of nodes}$  as the  $e$  value [13].

## 1.6 Existing Solutions

There are a number of pre-existing solutions which attempt visualise Ant Colony algorithms however, the majority of these based upon the authors experience are in fact sub-par in performance. Rather than visualising the algorithms execution in a logical manner, more often than not the existing solutions simply shows the algorithms final state without any detailed intermittent steps. This leaves the user confused about what has just actually happened and how was such a solution obtained.

Another problem associated with existing solutions is that the graphical user interface is too cluttered or complex. Many of the existing applications the author observed contained every interaction element in a tightly packed series of containers rather than splitting appropriate actions into separate views or menus. This is extremely confusing and makes it difficult to actually use the application as intended. If the user has selected that they want to use a specific variation of an Ant Colony algorithm then the user should only be able to interact with the features directly relevant to their selection.

One of the major problems the author faced when assessing the competition was the fact that there was rarely any visualisation of the agents themselves. As a result the user had to effectively guess which cities the agents were currently at. In addition to this there was no visualisation of the agents movement between city locations. This made it difficult to visualise the path the agents took aside from coming to your own conclusion based on the pheromone trails which were also often poorly represented.

## 1.7 User Interaction Methods

As discussed in section 1.6 the methods of user interaction must be superior to what is provided by the competition. This application will be authored in accordance with several preferred user interaction methods enabling a more user friendly experience for all users and not just those who are experienced with this or similar applications.

### **1.7.1 Law of Context**

The law of context refers to the users expectation that they should only see interface controls relevant to the current object they want to modify [1]. This relates to one of the fundamental problems found in competitor applications (see section 1.6). Should the user request a change of algorithm type which requires an extension to default features, these new controls will be self-contained and represented suitably so the user knows that the new dialogues or interaction methods are a direct result of a change in algorithm type.

### **1.7.2 Law of Feedback**

The law of feedback relates the ideology that every significant action has some form of informative, relative feedback associated with it [1]. This enables the users to quickly develop an understanding of which interaction controls which action. The application will be developed in such a way that any incorrect actions will be displayed to the user in a manner that anyone can understand and provide the user with the required knowledge to resolve said issue.

### **1.7.3 Law of Easing**

The law of easing is very important, especially for this application. This law suggests that complex actions should be segmented into simpler steps to allow the user to comprehend what they are actually doing [1]. The way this application will adopt this is that rather than specifying all of the algorithms parameters at once, each parameter will have its own method of interaction and its own series of user feedback prompts enabling any user to simply modify select parameters however they see fit, assuming the value is legal.



## Chapter 2

# Analysis

### 2.1 Key Tasks

Based upon the undergone research in chapter 1 the problem can be decomposed into several key tasks. These tasks will directly relate to the requirements described in appendix A, section 1.3.3.

#### 2.1.1 Problem Representation

The problem representation is key for both creating an application which is best suited to the proposed task whilst also ensuring the underlying algorithm can correctly calculate a solution in a reasonable manner. Chapter 1 explains two types of problem which could be represented in this application, the Double Bridge experiment (see section 1.2) and the Travelling Salesman Problem (see section 1.3) each of these problems has its own merits and demerits.

##### 2.1.1.1 Double Bridge Experiment

Opting to represent the problem in a similar format to the Double Bridge Experiment would enable the visualisation to be more user friendly as the actual problem itself is far simpler than the Travelling Salesmen Problem. In addition to this users may relate more to this style of problem as they can map the on screen representation of the nest and food to a real world scenario, this is not easily done with the Travelling Salesman Problem. The author feels that representing the problem in this basic form will negatively impact the applications success as having a nest location, a food source and two bridges for the agents to navigate across can only be represented so many ways before the user becomes fully aware of the expected outcome.

Instead of maintaining the exact ideas behind the Double Bridge Experiment, the key concepts can be extracted and applied to a more complicated problem representation. The idea that every agent will start and the same nest location and attempt to navigate to a food source is a fairly simple concept to understand however, as described in Appendix B, section 2.7.1 the world can be expanded to accommodate a greater number of paths which vastly increases the problems complexity.

### 2.1.1.2 Travelling Salesman Problem

Representing the problem in the form of a Travelling Salesmen Problem may come across as quite daunting to new users. As discussed with the Double Bridge problem representation the idea of a nest site and a food source is easily relatable to the real world for the majority of people however, the Travelling Salesman problem does not boast a similar mapping to real world ant colonies. One of the main advantages with the use of this representation is that the graph is fully connected and as a result the author does not have to worry about complications such as wrapping the edges of the graph to simulate connectedness. This would need to be considered in the case of the Double Bridge with the suggested modifications.

This form of representation is far more customisable thus, it may be more appropriate for use in an educational application such as this as it enables a greater degree of user customisation. Enabling the user to experiment with different configurations allows them to conceptualise the algorithms behaviour in a variety of scenarios.

Initially the author chose to use the suggested adaptation to the Double Bridge Experiment however, the result this produced happened to be very unsatisfactory. As a result the application underwent a somewhat agile re-design process to accommodate the change in problem representation to the Travelling Salesman problem.

### 2.1.2 Algorithm implementation

The applications success will be heavily dependent on having a working, customisable implementation of at least the Basic Ant System (see section 1.4). As this application has educational objectives an incorrect implementation of underlying algorithm(s) would cause improper algorithm behaviours to be both taught and demonstrated thus, the quality of the implementation is paramount to the success of the application. The combination of background research and a suitable test strategy will ensure the application exhibits expected behaviours.

### 2.1.3 User interaction

The methods of user interaction will be key in ensuring the users actually fully utilise the functionality provided. Using the key user interaction principles identified in section 1.7 the author will develop a simple yet effective user interface incorporating these key design concepts. The look and feel of the interface must be familiar to the user. Research will be carried out and will consist of looking at successful applications of similar design then adapting any suitable design styles to suit this applications needs.

### 2.1.4 Algorithm Variations

Given the time constraints of the project it is not realistic to attempt to implement every variation of Ant Colony algorithms. It is far more realistic for the application to support few algorithm variations which will at a minimum include two different algorithm variations so users can have some insight into how different algorithms impact the overall result. This does not mean that supporting the majority of algorithm variations cannot be a high level objective for the application.

## 2.2 Objectives

The objectives listed below are generalised overall system goals. The author fully expects to have objectives which are not achieved, however these will be used as a reference point to further develop the application. The design decisions will be made with these high level objectives in mind and any design implementation which negatively impacts the applications ability to meet one or more of these objectives needs strong rationale for doing so.

- Create an application which can visualise the execution of two different Ant Colony algorithms
- Provide a suitable user interface which enables the user to modify the algorithms key parameters enabling the user to experiment with different parameter combinations
- Provide a visual representation of the algorithms execution in real time
- Allow the user to set the algorithms execution speed enabling the user to slow the algorithm down if they want to focus on each agents movement or speed the algorithm up if they are more focused on the returned solution
- Support the majority of Ant Colony algorithm variations to enable the user to freely choose any algorithm they wish
- Support multiple problem representations enabling the user to change the problem representation as they wish
- When using the Travelling Salesman Problem representation allow for the ability for the graph to not be fully connected to see how the algorithm returns different results
- Support the option for paths between nodes to be weighted, these paths will cost more to travel one way than the other
- Allow configurations to be loaded from and exported to and from external files enabling the user to consistently apply the algorithm to the same problem

## 2.3 Requirements

These requirements are seen by the author as essential features that the application must provide. The requirements defined in appendix A, section 1.3.3 describes the immediate goals for the application however, there is some overlap between the overall objectives described in section 2.2 and the functional requirements. In addition to this each functional requirement defined does not have equal importance, some of the requirements are indeed critical and must be completed at the earliest convenience. The evaluation of these requirements is described in table A.2 which shows a summary of all requirements and their dependencies.

## 2.4 Desirable, non-essential Features

The features mentioned in this section are seen by the author as non-essential however, if implemented these features would significantly improve the applications performance. The implementation of these features will only be considered, if and only if the requirements mentioned in section appendix A, section 1.3.3 have been met to a significant degree of accuracy. The application will be designed in a way that will allow modification and maintenance to be less problematic, therefore the author feels there should be no reason why these features could not be implemented if there enough time during the development process to do so. The intentions and efforts of the author will reflect the functional requirements being a top priority.

- Enable the user to switch between automated solving and an iterative step-by-step process, enabling a greater teaching potential.
- Upon completion or stoppage, a summary or report should be displayed to the user enabling the user to perform analytics based on the contents of these reports.

## Chapter 3

# Process

This project is largest project the author has solely been responsible for however, this does not define the project as a large project. Given the time frame which the project has to be completed in the author to come to the conclusion that there is no single process model that would be fully suitable. The lack of one specific process gives the author the temptation adopt no process at all however, the lack of any rational structure is inappropriate for this project.

Rather than using one single process the author feels that he can modify existing processes in order to create a process which captures the principles necessary for a logical development cycle for this project. Agile methodologies, specifically eXtreme Programming (XP) are often used in small development teams. XP places heavy importance on quality and responding to customer demands through the use of multiple iterations and a simple design process. Some argue that small development teams are using XP as a scapegoat for not adhering to a specific process or methodology. XP is still very much focused around a development team and there is constant deliberation about the adaptation of XP for single developer projects [4]. There are XP principles which are well suited to this style of project for example, there is less emphasis on a heavy on design allowing for a more flexible development process. This has been vital for this project in particular as the proposed design had to be significantly changed during development (see section 4). The author feels that in a solo project, the ability to be flexible and independent of any concrete design is key to a successful project. As the author has created a brief design specification individually without the help of a specialised team (see appendix B) there is the possibility that there are some key elements missing which may not be noticed until the implementation stage. Capitalising on XP's flexibility reduces the impact of the exclusion of key features during design as it enables the author to easily adapt to system changes.

The process used is a hybrid process containing relevant ideologies from other software development processes. In conjunction with XP principles discussed above, the author has decided that there has to be some planned process involved in the projects development. The idea behind using a planned approach as the main underlying process is because the author feels that solo projects often lose track of project goals and the documentation of such goals will remove this complication. This planned process wont be as strict as it would be if a planned approach was the sole process being used for this project, instead the design and requirements phase will be much shorter than usual and will only cover the main requirements and overall system interactions.



Figure 3.1: Variant of the Waterfall Model used in this project. Modified from source image [21]

Figure 3.1 represents the variation of the waterfall model used for this project. The general waterfall structure has remained the same, the process starts off with a problem analysis stage which is reflected in appendix A and chapter 2. The introduction of the XP principles puts less emphasis on the design stage. This is intended to remove the dependency on any concrete design. The main adaptation comes from the approach to implementation and testing, the inclusion of XP principles enables the author to be more flexible during the implementation process. This hybrid process enables the author to focus on the implementation and testing of any changes rather than focusing on redesigning the system to accommodate such changes, this saved tremendous amounts of time during development. Each change is handled in small sections rather than implementing several changes at once. Each change will be broken down into logical sections which will go through the implementation and testing process. Design is not completely disregarded, the author still has the option to design any new changes should he feel the need to. This process continues until the requirements defined in appendix A have been adhered to. This hybrid process is based on the work by Tom Blanchard [3] and has been repurposed for this project as this process is very effective for use in solo projects.

## Chapter 4

# Design

This chapter describes the design rationale for the current system. This chapter will cover the overall system architecture, user interface designs as well pseudo code representations of the main, non-trivial algorithms. Chapter 3 states how the author has a somewhat flexible approach enabling adaptations to the initial design. The proposed design in appendix B, and the final structure of the system are very different.

### 4.1 Language

The author has identified that the choice of language is an essential decision which must be made early in the projects development. Appendix B, section 2.2 denotes the language decision process the author went through.

The use of an appropriate language became even more important due to the fact that the design has undergone significant modifications since the initial proposal. If the author had selected a language which he had little experience with then the changes made to the initial design may have been much more complicated to implement. The author is very familiar with Java, more specifically Java 7 (Java 1.7) or above and implementing new features or refactoring existing code is familiar territory. The initial language choice (appendix B, section 2.2) did not factor in the potential for radical design change however, if it did the outcome would not change and the existing rationale would still be applicable to the project. In the authors opinion Java is the most appropriate language for this project.

### 4.2 Development Tools

#### 4.2.1 Development Enviroment

##### 4.2.1.1 Command-line Tools

The author considered using a simple text editor such as Atom [10] to write the code, and the command-line to compile said code using the default Java complier. Atom is a free, open source hackable text editor provided by GitHub and provides syntax highlighting support for numerous

language including Java. This syntax highlighting is especially useful and makes the writing of the source code slightly easier, as it becomes much simpler to track the start and termination of specific code blocks. However, as Atom does not have built in Java compilation abilities, the compilation process can become complicated.

The problem with the above method of compilation is that error detection and correction can become a very tedious process. If any compilation errors are present the trace presented in the terminal window can sometimes be quite difficult to parse resulting in increased difficulties tracking down the errors source. For smaller projects, this method of compilation is perfectly suitable and can be effectively managed. This project as discussed in section 3 is a rather large project for the author to undertake. As a result, the combination of source code size and manual compilation leads the author to believe this method of writing and compiling code is not only inefficient, but also inappropriate for this project.

#### 4.2.1.2 Integrated Development Environment

The use of an Integrated Development Environment (IDE) can help to alleviate the problems that can come from using a writing and compilation process such as that defined in section 4.2.1.1. There are many IDE's which support Java, however the author's preference is the use of the Eclipse IDE for Java Developers [9]. The Eclipse IDE provides a multitude of useful features as part of their default package.

One of the main features which Eclipse provides is automatic building of the projects source. This is a major benefit when developing as you can simply write your code and run the built project without having the unnecessary complication of switching between several applications to achieve the same task. Also, as there is automatic building any compilation errors will be clearly highlighted using a system which is familiar to most computer users. If there are any misspellings of method or variables names for example, Eclipse will underline these in red to show there is a clear problem with this exact line of code. This is similar to the default scheme provided by most word processors, enabling a logical mapping between this red underlined line of code and an errors presence.

Another useful feature provided by the Eclipse IDE is the auto completion of variables and method names. This has sped up the development process for the author as there was no need to constantly look at the API's or other project source files for method names, the author could simply type the object of interests identifier and see a list of all methods and variables associated with such object. This is not easily done if the author used an approach similar to that discussed in section 4.2.1.1.

In addition to the built in compilation feature, Eclipse also provides an integrated debugging toolkit. The Eclipse debugger enables easy break point management, as well as all the usual features you would expect from a debugger such as; step through, step over and exploration of objects and variables. These features are also provided by command-line debugging tools however, the author is far more comfortable using a graphical interface to debug the application as it is easier to access the features of the debugger.

Eclipse also has built in JUnit support. This project will use the JUnit library as part of the testing process (more details see 4.2.3.1). Similar to how the IDE makes the writing of the applications code easier, the support of test suites such as JUnit makes the test process much easier. The code responsible for the tests will also have access to the features provided by the IDE as men-



tioned above. In addition to this you can run the tests inside the IDE and get accurate feedback on how many test executed and how many failed and why these tests failed.

## 4.2.2 Support Tools

### 4.2.2.1 Maven

Maven is tool used for building and managing projects, specifically Java-based projects [2]. The Maven framework provides a lot of useful utilities for developing successful projects and ensuring that such projects adhere to certain standards. The Maven framework aims to provide convention, over configuration. If there are multiple projects which have many different dependencies, for example external Jar files, then Maven can allow other projects to make use of these dependencies. As the author is working alone and is not expecting to have any other projects which will share dependencies with this one, the author has to weigh up if this framework would actually benefit the development process.

Maven provides some useful testing capabilities. When testing using the Maven framework, tests are still written using the JUnit libraries (see 4.2.3.1). The Maven framework provides some additional features which the author feels could be of use. Maven, will give the author a unit test report should one be required which will cover numerous details, most importantly a test coverage report will be produced. This enables the author to assess how well the unit testing has been done. Although this test report is a very useful feature, the Maven framework is not a necessity nor is it complication free.

The main complication that the author has with use the of Maven for this project is that fact that as this is generally a small project, Maven and its features would not be fully utilised but the hassle of configuring the framework would still be present. The initial project configuration would be time consuming, given that the author is inexperienced with the framework and this time could be spent on the actual project development. Generally the author feels that Maven would not be appropriate for use here however, the test reports would be extremely useful.

### 4.2.3 GitHub

The author has seen the use of GitHub as an essential part of the development process. GitHub has enabled the author have strict version control throughout the development process. As this is the case, the author has been able to store a local repository which will exist as the working directory for the applications development whilst also allowing a working copy with the most up-to-date fully working project code to be stored safely online using GitHub. At numerous times throughout the development lifecycle the author had to revert back to a previous version of the applications code GitHub has allowed this process to be almost hassle free. As it is so simple to manage different versions of the application each representing a different collection of working or non-working features the author has been able to develop in confidence as he knows that any mistakes or experiments are not as costly as there is always a backup version stored at the GitHub repository location.

Without the use of GitHub the author would have found it difficult to progress the application as expected. If there was no form of version control, then the mistakes the author made or external factors which then rendered the current development code unusable would be a far more disas-

trous. There was a time during development where the authors working directory became corrupt. This was easily resolved by simply retrieving the code stored in the projects GitHub repository. If GitHub was not being used here, there would be the possibility that the author would have lost progress on the application entirely.

#### 4.2.3.1 JUnit

JUnit is an open source framework for unit testing Java applications. The JUnit libraries provide a multitude of features that allow for a more simplistic approach to testing. Numerous other test frameworks are available however, the author is experienced with JUnit and feels that this framework is more than suitable for the unit testing of this application.

The author feels that a suitable testing framework is essential for efficient and accurate unit tests for any application. If the author had neglected to use a testing framework such as JUnit and manually tested the application (looking manually for abnormal output (LMFAO)) then the quality and coverage of the unit testing would reduce significantly. If the author used a manual approach which relied on outputs then the author could potentially have a situation where the code is outputting the correct result but is internally flawed this can't be manually checked. This means that you could ship a product which is assumed to be functioning as expected then suddenly the application is misbehaving. A testing framework such as JUnit not only allows for the tests to be fully automated, the tests also become scalable. Every code change would need to be re-evaluated against the existing unit tests, which is easily done if you have a series of tests which can be executed automatically. If a manual approach was used, then it becomes a near impossibility that every change can be tested as it would simply be too much to check as the addition of this new code has scaled the number of application inputs and outputs as well as the conditions in the code's logic.

### 4.3 Overall Architecture

The process used during this application's development has enabled the author to add additional features which were not additionally planned, this includes the addition of extra algorithm types and modifiers as well as refactoring of code into more logical methods and classes. The new application architecture is much more complex than the initial proposed design as a result each package will be represented as its own set of diagrams, then an overall representation showing the interactions between these packages will be explained. In all figures below, getter and setter methods are omitted but are assumed to be present. The packages referenced in this section will take the form of *che16.dcs.aber.ac.uk.xxx* where *xxx* is the corresponding package name.

#### 4.3.1 Controller

The Controller package has undergone several changes since the initial design of the system as defined in appendix B, section 2.3.3.3. The general ideologies have however remained the same the range of features provided by the application as a whole has increased thus, the author saw these modifications to the Control package contents as a necessity in order to correctly control these new features whilst also adhering to the existing Model-View-Controller framework.

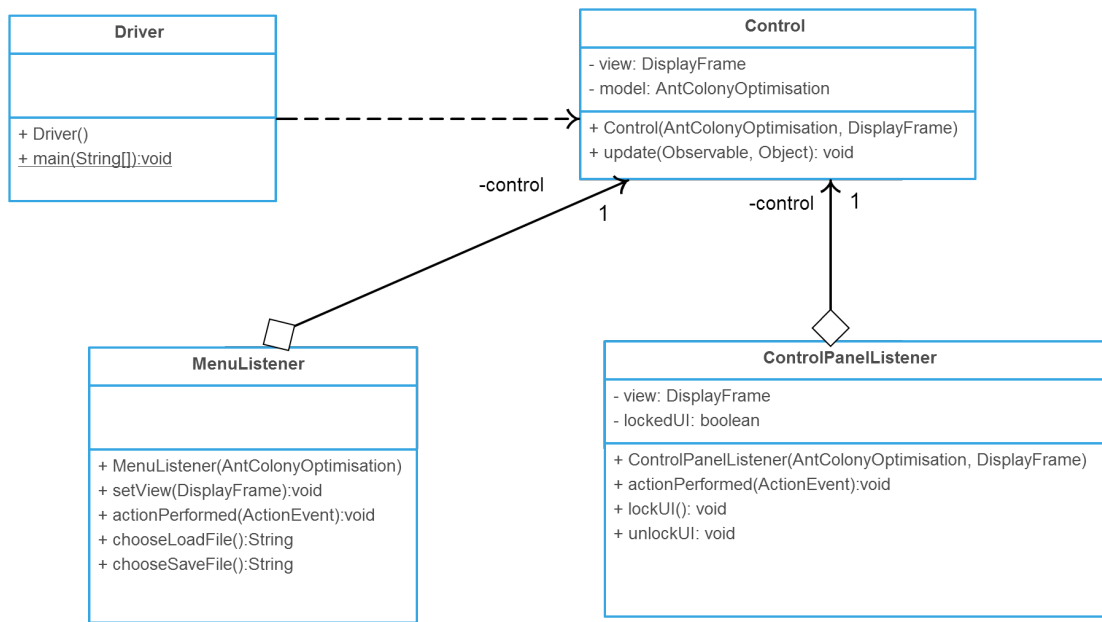


Figure 4.1: The contents of the Controller package in standard UML Class diagram notation

#### 4.3.1.1 Class Descriptions

The Driver class remains largely unchanged from its initial proposed design (see appendix B, section 2.4.1.1) however, it now interacts with the other components in a slightly different manner. The Driver class remains the sole entry point for the application. The Driver now has the additional responsibilities of instantiating the Control instance. The general purpose of the Driver class is still to ensure the system components are correctly instantiated, and holds no references to any instances of any object.

The Control as represented in figure 4.6 is designed to observe the model and notify the view should the state of the model change significantly. In addition to this, the required instances of MenuListener and ControlPanelListener are instantiated in this class and a reference to this Control object is maintained the created instances of said objects. The Control class is an additional feature not present in the initial design and is a result of the refactoring process. This class has the potential to be extended to support several other observable objects should this functionality be needed by the author in the future.

An instance of the MenuListener is used to listen the JMenuBar. This is designed to collectively manage the actions represented by the elements contained in the JMenuBar. The alternative approach is to give each element in the JMenuBar its own Action Listener. This is far from efficient and increases both the codes complexity, and reduces overall maintainability of the application. The author decided to use a dedicated object such as this to listen to the menu and perform appropriate actions. This class maintains an instance of the Control class to enable the instance of this class to have access to the model and view instances stored in the Control instance providing a simple way for the JMenuBar to have access to necessary functions.

A ControlPanelListener instance is designed to be a dedicated ActionListener for the Control-Panel (see section 4.3.3.1). Two separate ActionListeners are present in this application, this is

because the author wanted to have dedicated listeners for each component, rather than having a combined object representing this class and the MenuListener. The author feels that this is appropriate as any modifications to the object become simpler to implement if relevant behaviours are extracted into logical modules such as this design exhibits.

### **4.3.2 View**

The View package serves the same purpose as initial designed however, there has been a significant amount of refactoring applied to the initial design to enable a more effective graphical user interface to be created. The author has also added several new classes into this package to represent additional views which were not initially envisioned, but during development the author recognised that these new views were essential.

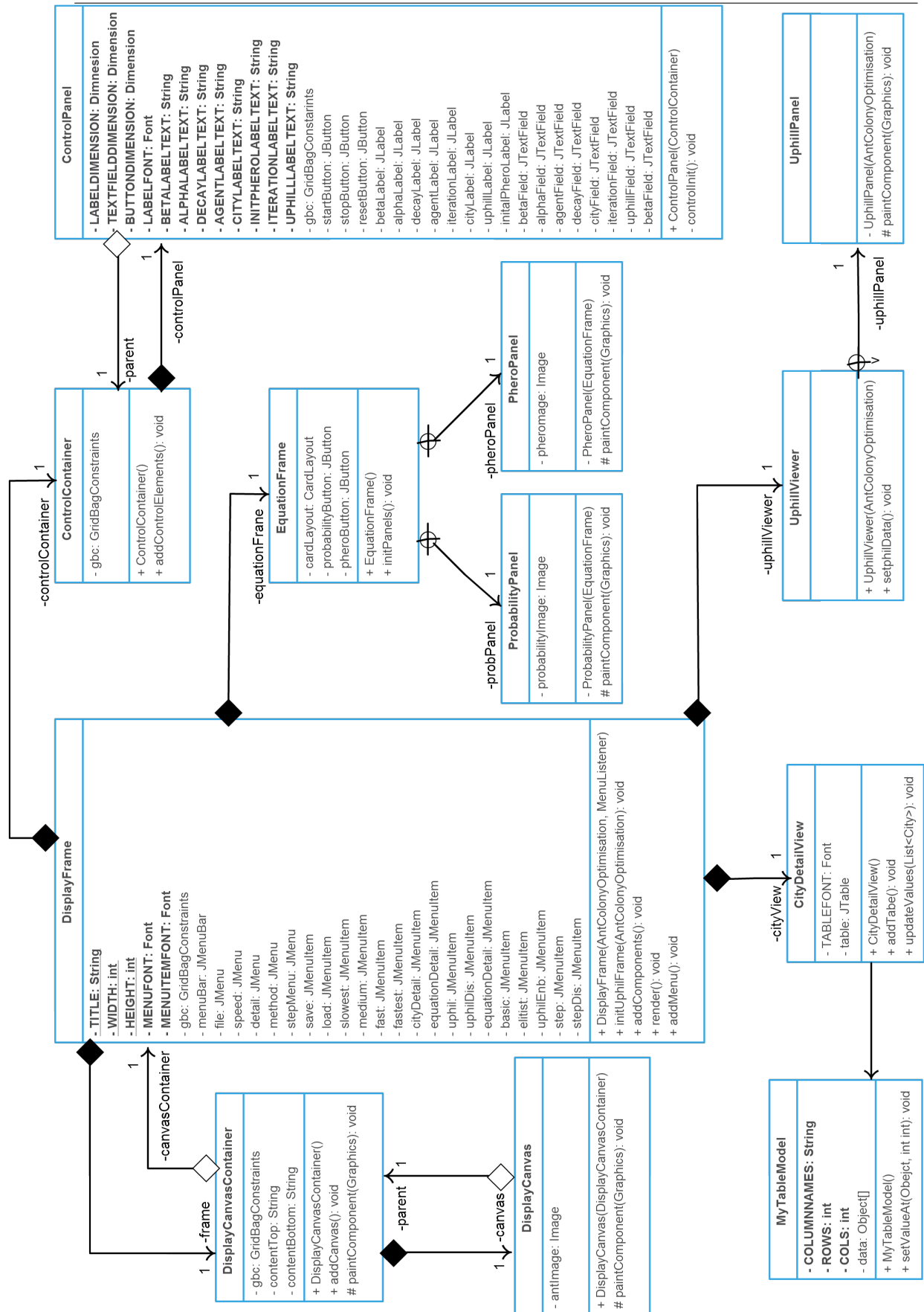


Figure 4.2: The contents of the View package in standard UML Class diagram notation

#### 4.3.2.1 Class Descriptions

Initially the `DisplayFrame` was designed to simply represent the highest level container which houses the remaining graphical user interface elements. As figure B.4 shows the initial design for this class was very simplistic and lightweight. The author's decision to include additional user interface elements which were not originally planned has resulted in modifications to the designed class. A `JMenuBar` has been added and as a result the `DisplayFrame` class grew in size in order to accommodate this `JMenuBar` and its necessary underlying elements. Although the size of this class has grown the complexity and functionality is largely unchanged, it remains as the highest level container for the graphical user interface and control the instantiation of such elements.

The `DisplayCanvasContainer` is the result of renaming the `DisplayPanel` class in the initial design (figure B.4). This class is designed as a container to the `DisplayCanvas` instance, this functionality is as designed and the author has not modified its behaviour.

An instance of the `DisplayCanvas` class is used to visualise the algorithms state of execution to the users. This is the component that is painted during the algorithms execution using the *paintComponent* method which it inherits from its `JFrame` super class. As the functionality provided by this class is very simplistic, the current implementation remains unchanged from the initial design proposal (figure B.4).

The addition of the `CityDetailView` is a simple `JFrame` container which is used to display a `JTable` with data representing the number of agents currently at each city location. The `JFrame` displayed by this class can be toggled between visible and invisible through user interaction with the respective `JMenuBar` item.

The structure of the table represented visually by the `CityDetailView`, is modelled by the `MyTableModel` class. Extracting the tables structure into a separate class enables easy modification of the structure as well as reducing the coupling between the view and the table itself.

Similar to the `DisplayCanvasContainer` class, the `ControlContainer` is used to encapsulate the user input elements in their own separate container. This is a result of refactoring the `UserInputPanel` class in the initial design (figure B.4) into this container and the `ControlPanel` class. The main purpose for this class is to allow for a more diverse range of `LayoutManagers` to become available allowing for an easily modifiable interface.

The `ControlPanel` class used to contain the interface elements which directly relate to the creation and modification of the problem and world. This includes housing the text fields and labels required to enable the user to customise the algorithm parameters, as well as providing a simple means to start and stop the execution using a simple `JButton` approach. This class is essentially an extended version of the `UserInputPanel` class in the initial design (figure B.4) aside from the fact that more interface elements have been added the functionality is the same.

The `EquationFrame` class an extension of the `JFrame` class which is used to display a graphic explaining the underlying algorithm functions. This class has no other functionality aside from the providing a means of displaying such graphics. Such graphics are contained within the `ProbabilityPanel` and `PheroPanel` instances.

Both `ProbabilityPanel` and `PheroPanel` are nested classes inside the `EquationFrame`. These classes subclass `JPanel` and are used to contain different graphics which will be used to represent information relevant to the underlying probability and pheromone functions respectively.

The `UphillViewer` class is another new addition which was not perceived in the initial design.

This class is a subclass of `JFrame` and is used to contain an `UphillPanel` instance. This `JFrame` can be toggled between visible and invisible with relevant user interaction with the `JMenuBar` contained in the `DisplayFrame`.

An instance of the `UphillPanel` class is used to display information about the current status of the uphill routes for the current algorithms execution. This is an extension the `JPanel` class, enabling the uphill route data to be painted to the component using the inherited *paintComponent* method. This is a nested class inside `UphillView` as no other objects uses or needs the knowledge of this a nested class is the most suitable way to contain it.

### 4.3.3 Model

The elements contained in the initial proposed design represented in figure B.4 has undergone significant refactoring which has produced a vastly different structure. During the development process the author found the the initial design happened to be inadequate for representing the algorithm in a suitable manner as it lacked necessary components and detail.

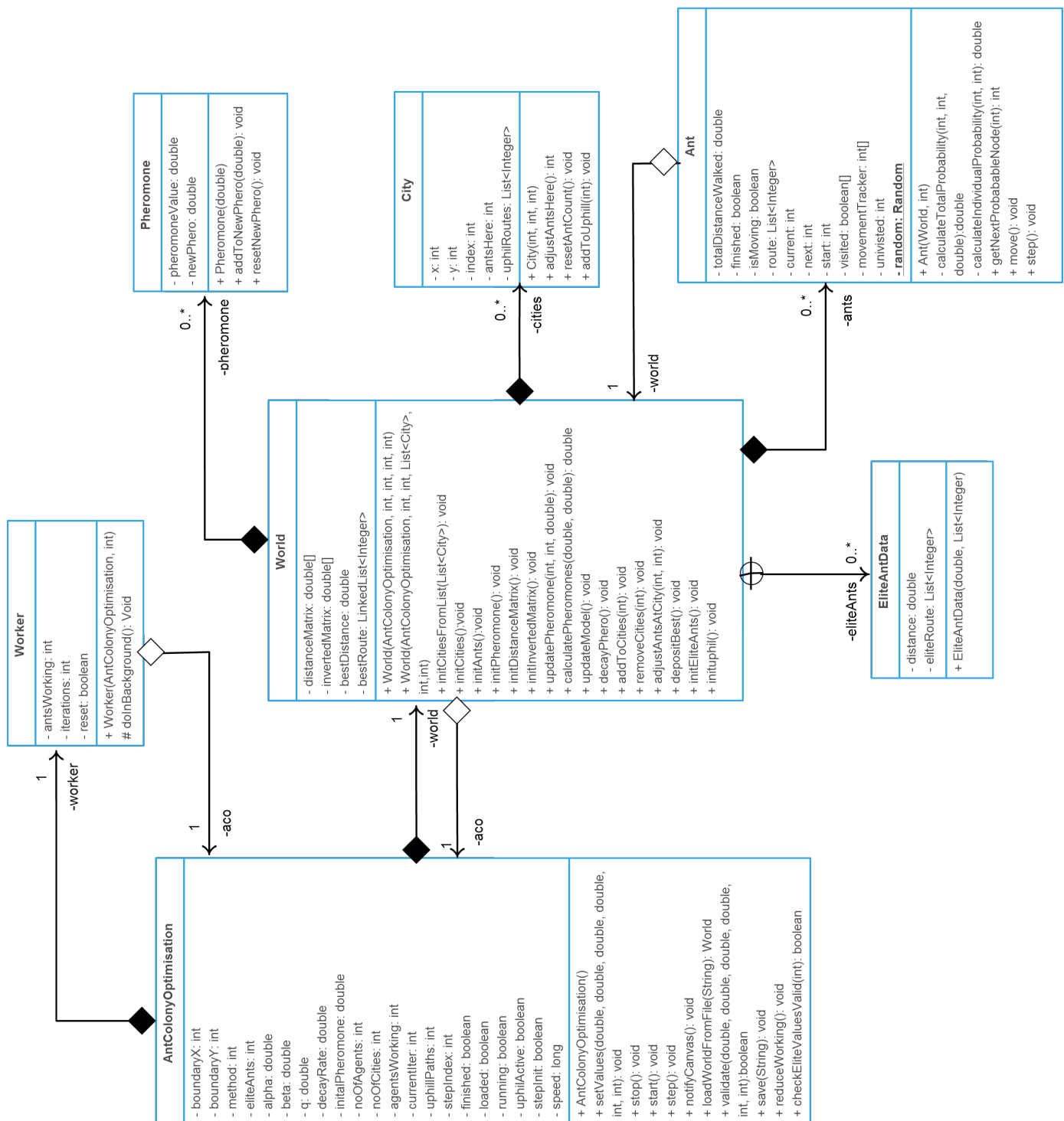


Figure 4.3: The contents of the Model package in standard UML Class diagram notation



#### 4.3.3.1 Class Descriptions

The initial concept behind the `AntColonyOptimisation` class is that this serves as the main control point and data centre for the algorithms execution. This class is used to store all the necessary parameter values and is also responsible for the instantiation of the `Word` representation. This class also controls external package access to the `Model` package and its data. This largely remains the same as designed however, there are slight modifications to accommodate additional functionality.

The `Worker` class was something that wasn't initially planned. As discussed in 5.5.1 there was a necessity for a way to control the algorithms execution without interfering with the performance of the interface. This class is an extension of the `SwingWorker` class and uses the inherited `doInBackground` method to perform the algorithms execution in a suitable manner.

The `World` class is used to model the problem representation and the environment for which the agents will be deployed during the algorithms execution. This class houses all the data relevant to such representations including a list of all `Ant` and `City` objects as well as having basic data structures which provide an effective representation of the pheromone concentrations for every edge within the graph and control the manipulation of pheromones on such edges. This class is generally the same as proposed in figure B.4 however slight modifications have been made to support additional features.

A `City` object is used to represent a node in the current problem representation graph. A collection of these `City` objects is maintained in the current `World` instance, and iterated through during both the solving and painting processes.

A `Pheromone` object is used to model the pheromone concentrations for any given edge. A two-dimensional array of these objects is maintained in the current `World` instance, and these Objects are constantly manipulated during the pheromone deposit and decay operations.

An `Ant` object is used to represent an agent which will be deployed in the current environment in order to solve the current problem. The `World` instance will maintain a collection of these objects. Each `Ant` has sufficient variables and methods to enable them to move and deposit pheromones accordingly. The initial design suggested the use of an `AntInterface`, however as the author has decided that there will only be one type of `Ant` thus, the interface is deemed to be unnecessary. Generally, this class is as designed in Figure B.4.

The `EliteAntData` is a nested class inside the `World` which is used to store the current elite routes. This feature is only necessary if the user has selected the `Elitist Ant System` as the current algorithm type. This is required to correctly preserve the best routes across iterations as the ant objects get reset each iteration. Rather than storing a whole ant object the author has opted only to store the best distances and best routes as this has less overheads when compared to storing an ant in full.

#### 4.3.4 Utils

During development the author noticed that some methods were being implemented in numerous locations. To prevent code duplication and promote re-usability the `Utils` package was implemented. This is a very simple package containing one class however, the contents of this class don't belong in any other package individually.

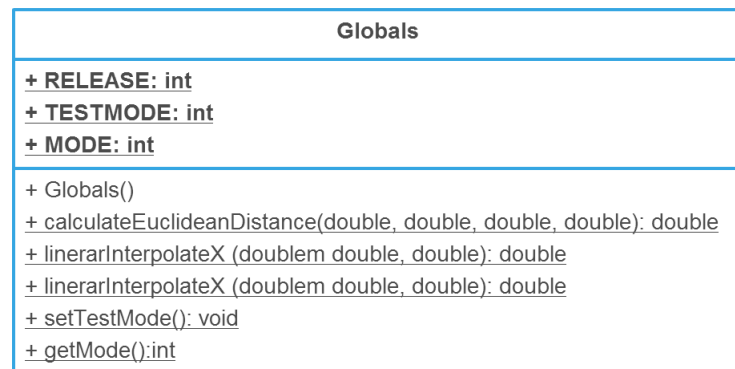


Figure 4.4: The contents of the Utils package in standard UML Class diagram notation

Figure 4.4 represents the single class contents of the Utils package. This Globals class contains several publicly available static variables and methods enabling application wide access. This enables the multiple packages which rely on the results of such methods to retain access to them whilst also reducing the amount of repeated code. In addition this class enables the execution mode to be switched from release to test mode. When in test mode the error messages require no user response enabling the automated test process to complete more easily.

### 4.3.5 System Interactions

The different packages and their contents have been described above however, the interactions between packages must be carefully designed to ensure correct implementation and of the Model-View-Controller design pattern.

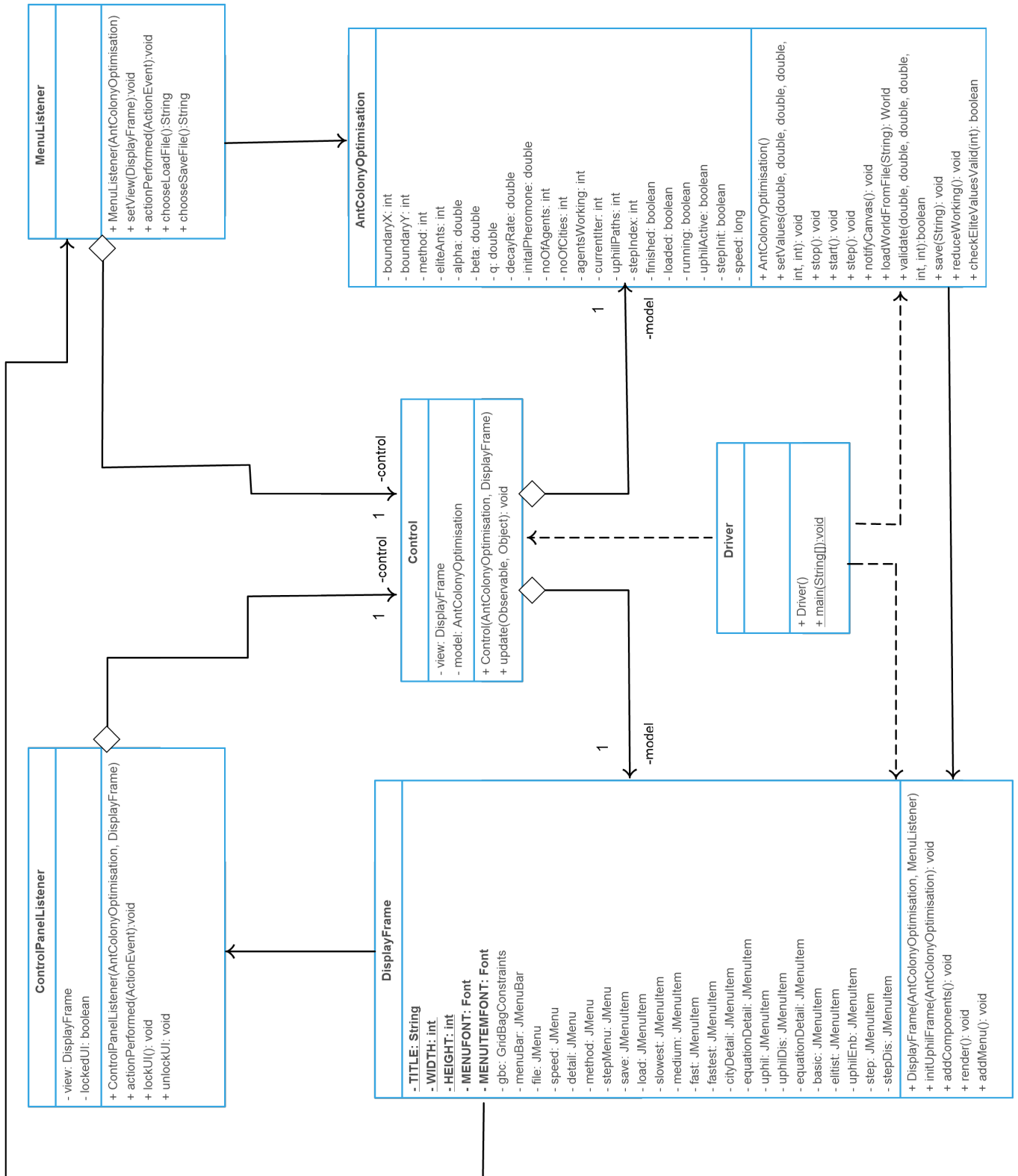


Figure 4.5: The proposed manner of package interaction expressed in standard UML Class diagram notation.

Figure 4.5 demonstrates how the access to the View and Model packages is governed by the instances of the DisplayFrame and AntConolonyOptimisation respectively. This keeps the interaction between packages simple and enables encapsulation of sensitive data. This design adheres to the Model-View-Controller principles as the Controller package and its contents govern the interactions between the Model and View. The view, has no reference to the model however, at runtime an instance of the AntConolonyOptimisation is passed to the View in order for the painting of necessary components to take place. As there is no explicit link between the model and view these packages can be easily modified or substituted in order to change the current representation there is no coupling between the contents of these packages.

## 4.4 Design Patterns

### 4.4.1 Model-View-Controller

The current design still adheres to the Model-View-Controller(MVC) principles discussed in Appendix B, section 2.3.1.1 however, the complexity of the different package elements has increased. As designed, the author has implemented an MVC compliant architecture through the use of the Observer and Observable relationship using the corresponding default Java framework. The general concept is implemented as defined in appendix B, section 2.3.2 slight modifications have been made to the classes representing the different components of the Observer and Observable concept.

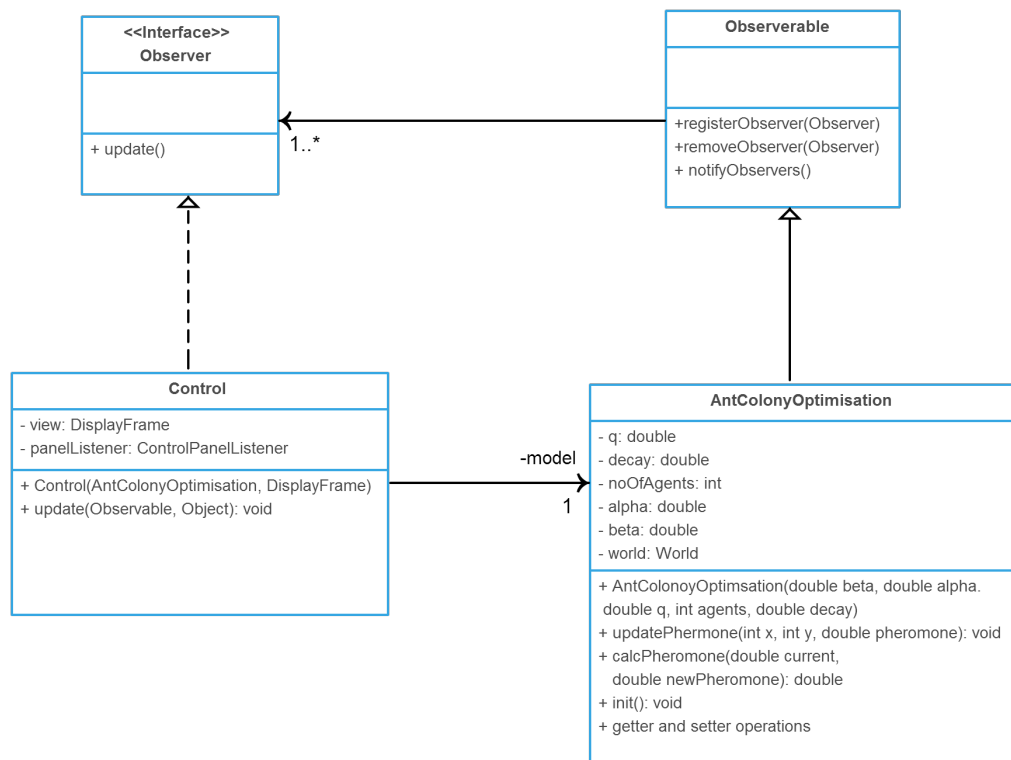


Figure 4.6: Implementation of the Observer and Observable Design pattern

Figure 4.6 demonstrates how the Control class will implement the Observer interface. This

Control instance listens to the Observable object and determines the correct actions based upon the source of update. The AntColonyOptimisation class is as defined in section 4.3.3.1 acts as the observable object through its extension of the Observable super class. This inheritance grants the AntColonyOptimisation instance access to key methods such as *registerObserver()* this allows the author to assign the Control instance as the designated observer. The *notifyObservers()* methods enables the author to dictate when updates are published to the Control instance which will then correctly update the View.

#### 4.4.2 Singleton

Initially the author proposed that classes that compose the user interface would implement the Singleton design pattern [7], an example this proposed design can be seen in appendix B, section 2.3.2.1. The author had initially implemented the interface with each class implementing the Singleton pattern which caused complications. As the instance of a Singleton object is globally accessible, difficulties arose during the application debugging. This issue happened to be more prevalent when extending the functionality provided by each of the Singleton classes, for example the DisplayFrame class now contains a wider range of functionality than initially planned. Not only did the Singleton instance complicate the addition of these extended features, debugging these features became more difficult as the global accessibility made it harder to track the source of the bug itself. This is due to the fact that it is easy to accidentally interact and modify a global variable or instance. Often the source of these bugs was not where the author expected and were often due to incorrect interactions with these new extensions in a separate package. This was the main reason the author decided to withdraw the use of the Singleton pattern as the author felt it was much simpler to not have global access to these instances and features.

Robert Martin propositioned the idea of the Single Responsibility Principle (SRP) in 1990 [19]. The general concept behind the SRP is that each logical module in the software should have one reason to change or model one specific responsibility rather than a collection of unrelated features or functions. If a module has been extended to support multiple unrelated features, the SRP states that the unrelated features should be extracted into relevant modules so that each module maintains its one responsibility. The author feels that implementing the Singleton in the proposed manner (see appendix B, section 2.3.2.1) violated the underlying concepts of the SRP. As the Singleton class is responsible for tracking and instantiation of its one allowed instance the functionality which the module presents now has more than one responsibility and violates the SRP. The author believes the SRP should be regarded highly during development in order to produce maintainable and extendable software. As a result he has opted for adhering to the SRP over the Singleton implementations. The author experimented with the idea of extracting the functionality of the Singleton classes and the tracking of the instance of such classes into separate system modules however, this vastly overcomplicated the architecture.

Overall, the author sees the implementation of the Singleton Design pattern as more of an anti-pattern. To enable easier modification the implementation of any Singleton class as initially designed has been removed. Solutions to the above problems could be refactored in, but this is seen as unnecessary complexity by the author and has therefore also been omitted.

## 4.5 User Interface

The user interface elements will be designed with the three laws of user interaction discussed in section 1.7 as a top priority. The interfaces will be consistent in theme and styling which will provide application wide consistency for the user.

### 4.5.1 Main Display

The design for the main display (general view the user will be presented) remains largely unchanged from the initial proposal as represented in figure B.5. There has been slight modifications to this design during the implementation phase. These changes were fairly trivial allowed the author to implement them without any prior design, section 5.1 displays the implementation of this design and said changes.

### 4.5.2 UphillViewer

The uphill viewer was not an element of the user interface which was initially planned, however the addition to implement the ability for a path to represent uphill terrain required a view to summarize which of these paths are in fact subject to this uphill modification. This interface is a result of the contents of the UphillViewer class (see section 4.3.2.1).

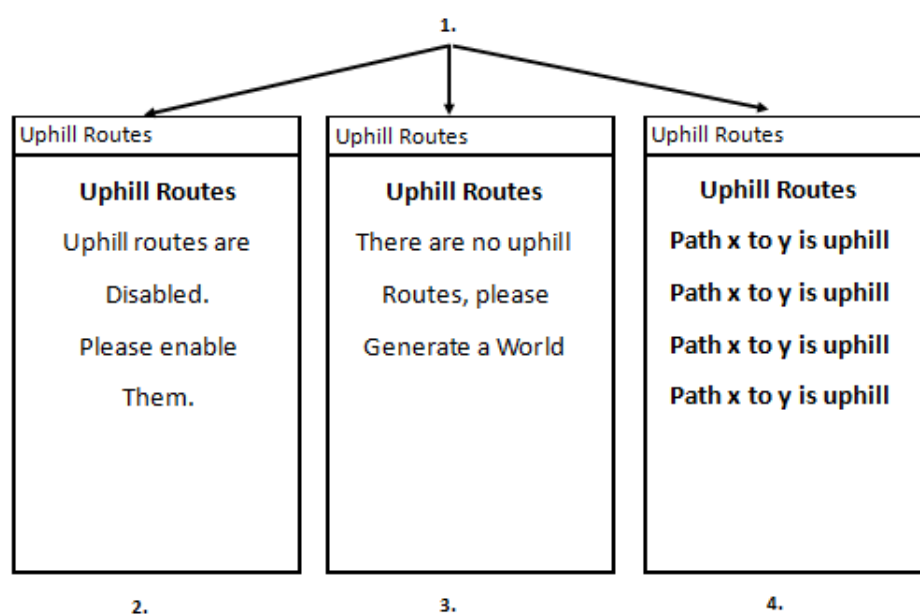


Figure 4.7: Proposal for the UphillViewer interface representing the different states possible at runtime.

**1.** in figure 4.7 is used to demonstrate each possible state for the UphillViewer contained in the same high level container. **2.** is used to show the default state and content for the UphillViewer interface. This state is shown to the user if uphill route generation is currently disabled, and prompts the user to enable them. **3.** is shown to the user if uphill routes generation is enabled, but

the current world is yet to be generated. **4.** is shown to the user when both uphill route generation is enabled and such routes have been generated. The  $x$  and  $y$  values in this figure will be replaced with indexes of valid cities to enable to the user to understand which routes are deemed uphill.

### 4.5.3 CityDetail View

The CityDetailView is used to summarize how many agents are currently at each City. This view was not initially designed however, the author felt that this was a necessary addition and therefore designed a rough outline of such interface.

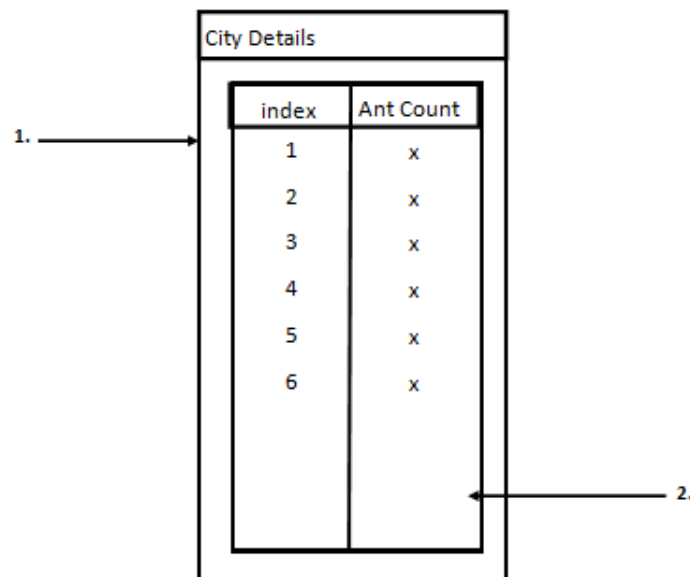


Figure 4.8: Proposal for the CityDetailView interface.

**1.** in figure 4.8 represents how this view is contained in a separate container to the main display. This enables the user to move this view around as desired in order to customise the current view to their liking. **2.** demonstrates how the contents of the CityDetailView will be displayed (see section 4.3.2.1). The number of rows will directly relate to the number of City objects in the current collection. The  $x$  values will be substituted for the correct number of ants at the corresponding city index.

### 4.5.4 EquationFrame

The Equation Viewer is used to explain the functions that the underlying algorithm uses. This view was not initially designed however, the author felt that this was a necessary addition and therefore designed a rough outline of such interface.

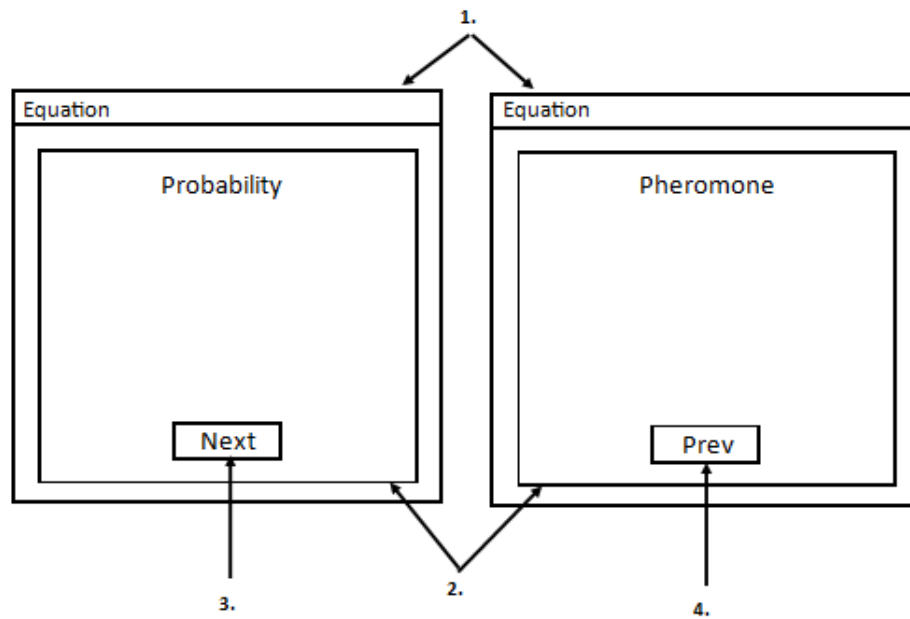


Figure 4.9: Proposal for the EquationFrame interface.

1. in figure 4.9 represents how this view is contained in a separate container to the main display. This enables the user to move this view around as desired in order to customise the current view to their tastes. 2. demonstrates how there will be one shared panel which will be used to display the content related to both the pheromone and probability equations. The content of the container signified by 2. will be substituted for the correct content when the user interacts with either one of the buttons signified by 3. and 4.. If the user interacts with button 3. then the content of the container will switch and will now represent details about the pheromone equation. When button 4. is pressed by the user, the content of the container will now reflect the information stored about the probability equation. The author has designed this such that any additional equations can be implemented in the same way using simple button navigation without the need of significant extensions to the existing framework.

### 4.5.5 Error Feedback

The interfaces responsible for error feedback have been carefully designed so that the author can effectively inform the user of the error, the cause of the error, and solution of such error. These interfaces are designed to be abstract in such a manner so the same interface can be used to represent several different related error responses.

#### 4.5.5.1 Parameter Errors

These errors are produced when a user has defined a value for an algorithm parameter which is deemed to be illegal. This illegal value could mean that the value the user has entered is outside of the scope of accepted value or the user has specified an illegal type for this parameter. An illegal type refers to a situation such as entering a double value where an integer is required.

The design for these error messages remains as shown in section 2.5.2, appendix B. This



design is simple and effective and provides the user with everything they need to know about the errors source and solution. This interface can be reused for any parameter related error as the only modification would be the change of the interfaces content, there would be no need to implement or design a new interface.

#### 4.5.5.2 File IO Errors

The ability for a user to load or save a problem configuration to a selected file is a new addition to the system. The design of these error interfaces is based off of the design for the parameter error interfaces described in section 4.5.5.1.

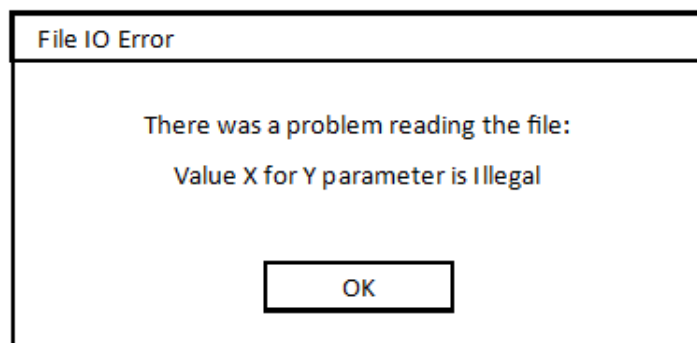


Figure 4.10: Design of the File IO error feedback interface.

Similar to the parameter error interface, this interface as described in figure 4.10 will provide the user with concise feedback as to how and why the file IO process did not complete as expected. From the error message displayed the user should be able to deduce their own solution to the problem. As there are numerous problems which could arise with file IO, the author decided to omit providing a explicit solution to the user. Instead the erroneous data is flagged to the user enabling them to locate the problem and resolve it. The  $x$  value in figure 4.10 will be replaced with the problematic value whereas the  $y$  value will refer to the problematic parameter.

## 4.6 Algorithms

This section covers the abstract implementation of the key algorithms used for both modelling the algorithms execution and the visualisation of such process.

### 4.6.1 General Overview

The general algorithm remains largely unchanged from the initially proposed algorithm in section 2.6, appendix B. The author has amended this design slightly to factor in the change of problem representation. As the TSP is the default problem representation the initial ideas behind ants collecting food and returning to the nest have been replaced by conditionals reflecting if an agent has visited every City or not.

**Algorithm 1** Pseudo-code for Ant System implementation

---

```

1: Initialise AntColonyOptimisation with defined parameters
2: if !parameters are legal then
3:   Display error message to user
4:   return
5: end if
6: Initialise World with algorithm parameters
7: Initialise Nodes and graph
8: Initialise pheromone values
9: Initialise Agents
10: while !all agents finished do
11:   for all Agents do
12:     while !visited all City locations do
13:       Calculate next move using probabilistic function
14:       Add location to Agent's memory
15:       update pheromone
16:       Update the View
17:     end while
18:   end for
19: if local best solution < global best solution then
20:   globalbest = local best solution
21: end if
22: end while
23: output global best solution

```

---

This pseudo code remains largely unchanged from the initial design represented by algorithm 5, appendix B. There has been modifications to the conditional statement represented by line 12 in algorithm 1. This change reflects the updated problem representation so that agents now visit all City locations rather than focussing on a nest and food situation.



Figure 4.11: Flow diagram representing the algorithm described in algorithm 1

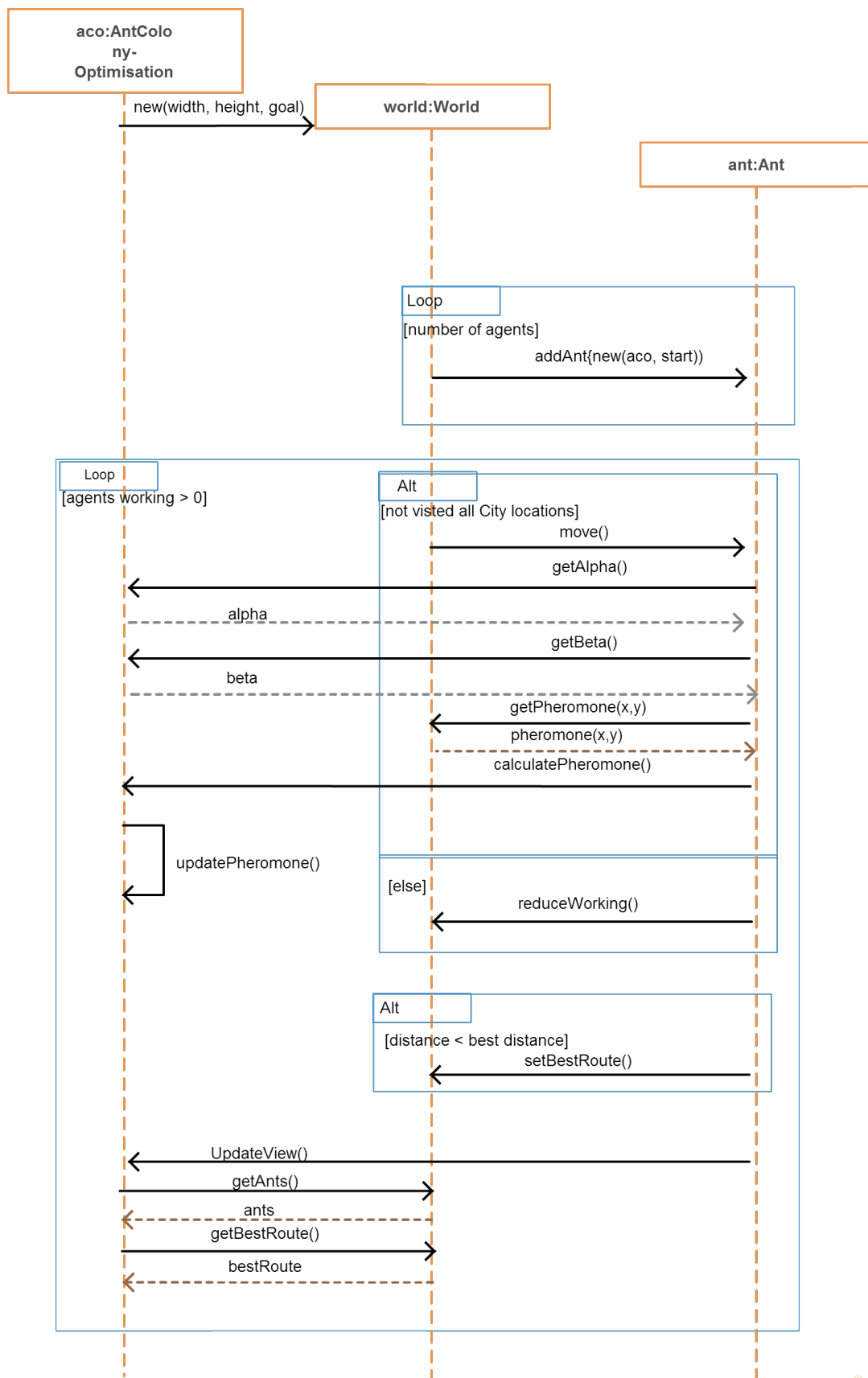


Figure 4.12: Overview of system interactions based on Algorithm 1

The sequence diagram described in figure 4.12 demonstrates at a high level how the algorithm executes. This differs slightly from the initial design (figure B.8) in order to correctly model the change of problem representation.

## **4.6.2 Formulae**

### **4.6.2.1 Probability**

The probability function is defined in section 2.6.2.1 appendix B. The design for this algorithm remains unchanged from the pseudo code represented in algorithm 6. The result of this algorithm is in fact, the probability associated with the agent moving to a specific location.

### **4.6.2.2 Pheromone**

The pheromone function is defined in section 2.6.2.2 appendix B. The design for the pheromone algorithm remains unchanged from the pseudo code represented in algorithm 7. This is the function that models the pheromone deposit and decay operations.

## **4.6.3 Elitist Ants**

The Elitist Ant algorithm was not initially planned as a feature provided by this application. The author decided that sufficient time was available to produce a brief design for the Elitist ant algorithm extension to allow for a smooth implementation of such design.

### **4.6.3.1 Overview**

The general premise for this Elitist Ant algorithm is defined in section 1.5. The probability function will remain the same as defined in algorithm 1 whereas the general behaviour of the system and the pheromone deposit function will differ slightly to that of the Basic Ant algorithm. The general system interactions will be the same as shown in figure 4.12.

**Algorithm 2** Pseudo-code for Elitist Ant System implementation

---

```

1: Initialise AntColonyOptimisation with defined parameters
2: if !parameters are legal then
3:   Display error message to user
4:   return
5: Initialise World with algorithm parameters
6: Initialise Nodes and graph
7: Initialise pheromone values
8: Initialise Agents
9: while !all agents finished do
10:   for all Agents do
11:     while !visited all City locations do
12:       Calculate next move using probabilistic function
13:       Add location to Agent's memory
14:       Update pheromone
15:       Update the View
16:       if total stored EliteAnts < total defined EliteAnts then
17:         add this ant to elite ants
18:       else
19:         for all EliteAnts do
20:           find the EliteAnt with the worst route
21:           if worst EliteAnt route is worse than this Ant route then
22:             replace worst EliteAnt with this ant
23:           end if
24:         end for
25:       end if
26:     end while
27:   end for
28: end while
29: if local best solution < global best solution then
30:   globalbest = local best solution
31: end if
32: end while
33: output global best solution

```

---

The difference between algorithms 2 and 1 is the manipulation of EliteAnts which is defined in lines 16 to 25. These lines enable the algorithm to constantly ensure that only the best (Elite)  $x$  number of ants are stored across iterations to ensure that pheromone is deposited on the best paths. In order to do this, every time an ant has completed its tour certain checks are made to see if this ant is eligible to become one of the  $x$  elite ants. An ant is deemed eligible if the current elite ant collection is not fully populated or if this ant has a better solution than the worst performing elite ant. If the later of these two conditions is met then the worst performing elite ant is then swapped with the current ant. This difference can also be observed in figure 4.13 which gives an even more abstract overview of the Elitist Ant System.

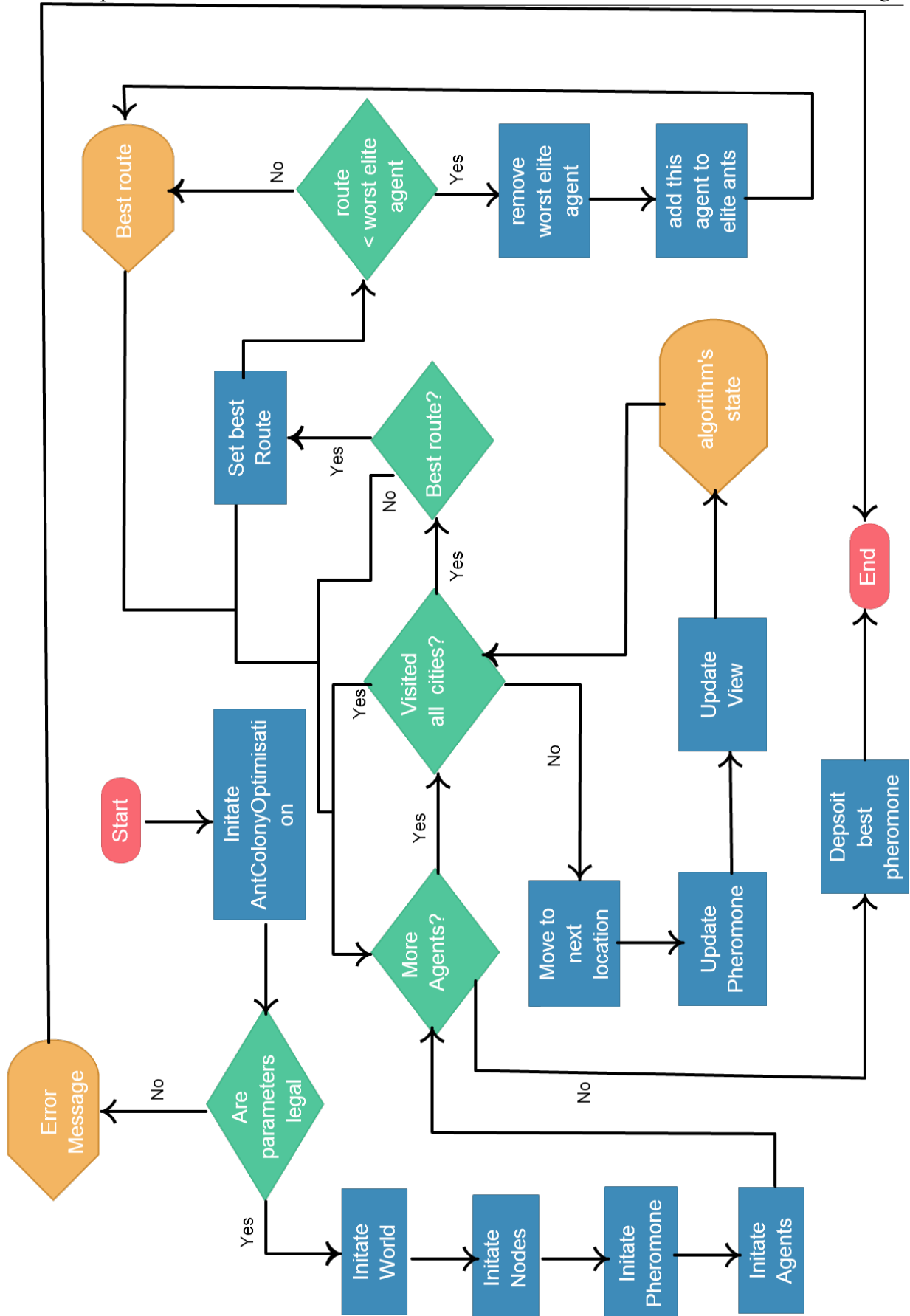


Figure 4.13: Flow diagram representing algorithm 2

### 4.6.3.2 Depositing Best Pheromone

As described in section 1.5, the Elitist Ant System has a slightly different pheromone function to that of the one described in section 2.6.2.2 for the Basic Ant system. This modified pheromone function is mostly the same as in the Basic Ant System however, the elite routes must be factored in.

---

**Algorithm 3** Elitist Ant System pheromone function pseudo-code
 

---

```

1: define the  $e$  value =  $e \times \#$  of cities
2: for all stored EliteAnts do
3:   initialise index  $i = 0$ 
4:   currentBest = EliteAnt path
5:   for all Cities along currentBest do
6:     get the City index at currentBest[ $i$ ]
7:     if  $i + 1 < \text{currentBest size}$  then
8:       get the Cityindex at currentBest[ $i + 1$ ]
9:       add  $e$  amount of new pheromone to pheromoneEdge[ $i$ ][ $i + 1$ ]
10:    end if
11:     $i++$ 
12:  end for
13: end for

```

---

Algorithm 3 demonstrates how the current elite ants are factored into the pheromone function. In general, this will enable the population of agents to converge towards a solution at a faster rate than the Basic Ant System as the increased amount of pheromone on edges used in the current best paths will be greater thus, ants will have a greater probability of traversing such edges.

### 4.6.4 Algorithm Rendering

Design and development of the algorithm responsible for visualising the Ant Colony algorithm's current state is one of the more important algorithms in the application as the visualisation process is key to the projects success.



**Algorithm 4** Pseudo-code for rendering of the algorithms execution

---

```

1: retrieve latest version of the model
2: if model !null then
3:   for all Cities in model.getWorld().getCities() do
4:     drawOval(City.X, City.Y, width, height)
5:     if algorithm !finished then
6:       for City do
7:         for all Cities do
8:           set opacity based on pheromone value at edge[city.index][cities.index]
9:           draw a line from Cityxy to every element in Citiesxy
10:        end for
11:      end for
12:    end if
13:  end for
14:  for all agents do
15:    for all cities do
16:      if agent location == City.index then
17:        draw agent at City.x, City.Y
18:        break
19:      end if
20:    end for
21:  end for
22:  if bestdistance > 0 then
23:    best route = model.getBestRoute()
24:    for i = 0 until i < best route.size() do
25:      if i + 1 < best route.size() then
26:        set colour as red
27:        drawLine(Cities[i].x, cities[i].y, cities[i + 1].x, cities[i + 1].y)
28:      end if
29:    end for
30:  end if
31: end if

```

---

The pseudo code represented in algorithm 4 defines the design of the general concept used to visualise the underlying algorithm. The author acknowledges that this is not the most efficient or elegant design and this is used as an implementation starting point and is by no means a concrete design. Lines 3 to 13 are used to represent the graph visualisation. Drawing a line from every City to every other City will simulate a fully connected graph of cities to the user. The opacity of these lines will be directly related to the pheromone concentration for the corresponding edge. Lines 22 to 30 show way in which the current best path will be rendered to the user, the author has designed this so that multiple pairs of lines are drawn which will ultimately form one continuous line representing the best path. Each line will have a start and end location, the end location of each line will become the starting location of the next line. This is done by iterating through the cities in the best route in pairs until there is no longer a valid pair of locations to draw a line between. Once this point is reached the best route is complete.

## Chapter 5

# Implementation

The chapter will describe the implementation rationale with the relation to the design as seen in chapter 4. In addition to this, the main obstacles the author faces during the development are discussed in this chapter.

### 5.1 User interface

The main display represents the general interface is displayed to the user. This is where the algorithms visual representation will be presented, as well as providing the location of the user interaction elements enabling modification of the algorithms parameters. The design for this view is almost as described in section 2.5.1, appendix B, however, there has been a slight modification to this proposed design.

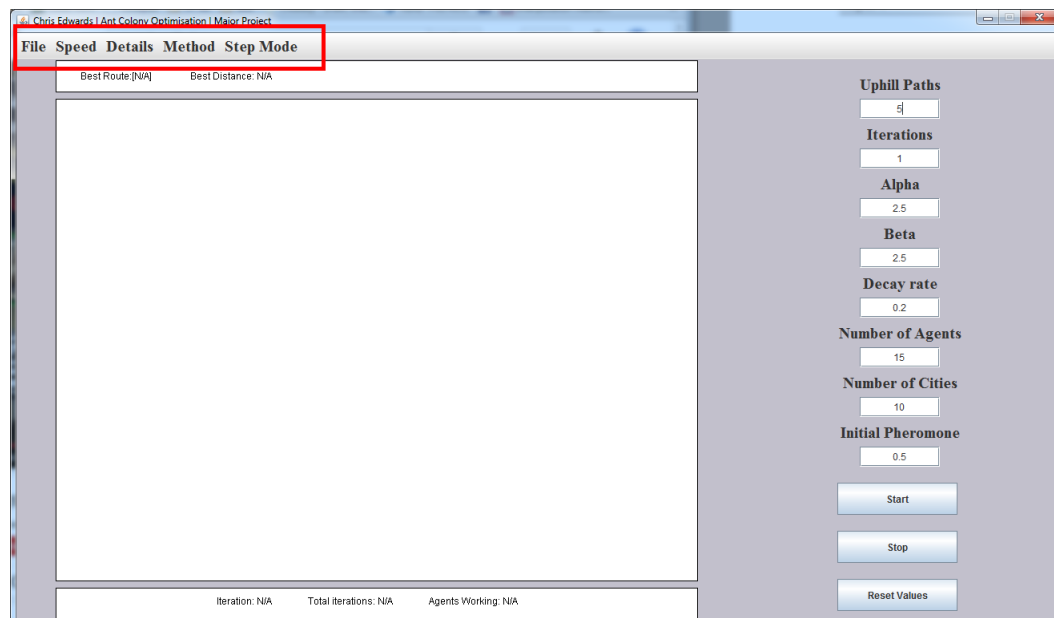


Figure 5.1: Implementation of the proposed user interface. The contents of the red polygon highlights the additional features not present in the initial design.

The additional features highlighted by the red polygon in figure 5.1 represent the features which were not initially designed. These features are represented in a separate location to the control panel (right hand side of figure 5.1) as there is no logical connection between the menu bar features, and the modification of the algorithm parameters. The author opted to use a menu bar to control the access to these features as the vast majority of users will recognise how to interact with a menu bar.

The different elements contained in this menu bar relate to general system interactions. The File option enables the user to either load or save a configuration to a specified file. The Speed option enables the user to change the thread speed which changes the algorithms rate of execution. The Details menu is used to control access to the following views; the UphillViewer (section 4.5.2), the CityDetailView (section 4.5.3) and the EquationViewer (section 4.5.4). In addition to the access of these extra views, the Detail menu also enables the user to disable and enable uphill route (section 5.7) generation for the current problem. The Method option allows the user to select the current algorithm type from a list of implemented algorithms however, the application currently only supports the Basic Ant System and an Elitist Ant algorithm types. The Step Mode menu enables the user to enable or disable the step-based iterations. When enabled, step mode will allow the user to step through the algorithms execution at their own pace without the application automatically solving the problem.

## 5.2 Data Structures

### 5.2.1 Pheromone and Distance Matrices

#### 5.2.1.1 Pheromone

A Pheromone object is used to represent the pheromone concentration for any given edge however, there is no data stored inside the Pheromone object which relates the object to a specific edge. Enabling logical indexing of these objects such that the author could continually extract the pheromone data for a specific edge is a fairly trivial task however, the method of doing so has changed since the initial proposed design as seen in section 2.7.2, appendix B.

The concept of a using two-dimensional array to store the pheromone data is still present however, the dimensions of such structure are now directly representational of the number of cities in the current problem. Assume there are  $x$  number of cities then the length of each array would become  $x$ . Therefore the instantiation of the pheromone data structure is of the format `Pheromone[] pheromone = new Pheromone[x][x]`. Assuming these  $x$  cities have the *index* values  $0, 1, \dots, x - 2, x - 1$  then indexing any edge would be done using the format `pheromone[x][y]`. Given this format  $x$  and  $y$  are any valid city indexes, For example, to access the pheromone concentration for the edge corresponding to the path from *City* 0 to *City* 5 would be accessed using `pheromone[0][5]`. As accessing an element in an array is a  $O(1)$  operation this method of access is extremely efficient and supports a problem of almost any size as the data structure scales with the problem. Figure C.1 represents how the pheromone matrix is initialised using the initial pheromone value for all edges.

### 5.2.1.2 Distance Matrices

Initially there was no proposed design for the of data structures representing the distances between each node in the graph as the initial design for the problem representation made it simple to calculate the distance between the current node and the destination node. The author decided that as the problem representation has changed to the TSP there needs to be a better method of accessing the distances between two nodes (Cities).

The design for the distance matrices are based on the implementation provided by Thomas Jungblut [22]. The implementation of these data structures is identical to that discussed in section 5.2.1.1 however, the data stored in each array element represents the *euclideanDistance* between two cities rather than the pheromone concentration. As defined in section 5.2.1.1 the size of distance matrices will represent the number of cities. If there are  $x$  cities in the current problem then the format for instantiation will be `double[][] distanceMatrix = newdouble[x][x]`. The way in which elements are accessed also remains the same as above, however once instantiated these values will remain constant as a City cannot move location. These matrices are easily populated after the cities have been instantiated. The code in figure C.2 represents how this has been implemented. A correct implementation would return a distance of 0.0 if `index[x][x]` were to be accessed where both  $x$  values are equal. This is because the distance from any *City* to itself is 0.0.

The probability to move to any node is modelled as  $p_{xy}^k = \frac{(\tau_{xy}^\alpha)(\eta_{xy}^\beta)}{\sum(\tau_{xy}^\alpha)(\eta_{xy}^\beta)}$  where  $\eta_{xy}$  represents  $\frac{1}{distanceMatrix[x][y]}$  (inverted distance). This function is used extremely often during the algorithms execution so instead of converting the value of `distanceMatrix[x][y]` every time an inverted value is needed it is far more efficient to store an inverted version of the *distanceMatrix*. The code snippet in figure C.3 demonstrates how this can be implemented. The `invertDouble(distanceMatrix[x][y])` in said figure simply returns the value of  $\frac{1}{distanceMatrix[x][y]}$  however if `distanceMatrix[x][y] == 0.0` then 0.0 is returned as  $\frac{1}{0.0}$  is illegal.

### 5.2.2 Agent and City Collections

Both Agent and City objects are designed to be stored using data structures which implement the List<type> Java interface. As the quantity of cities and agents present in the current problem is dynamic and user defined the size of the data structure must be established at runtime and therefore the data structure chosen must scale well and maintain performance regardless of its size. In addition to this, a user is able to modify the amount of agents and cities once instantiated therefore, the data structure must be able to be resized dynamically without complication. The ArrayList data structure has been chosen to store the agents and cities as it is scalable and can be dynamically resized. An array implementation could be used here however, if the array reached capacity then there would need to be conditionals put in place by the author to copy the contents of the full Array into a new, larger Array instance. The use of ArrayList means that the author does not have to worry about these conditionals are they are handled for the author by the ArrayList implementation. In addition to this, the order the elements in generally unimportant the accessing of a random index however is. Both Array and ArrayList implementations provide  $O(1)$  random element access implementation. Insertion into an ArrayList is a  $O(1)$  operation whereas an Array implementation would provide  $O(n)$  insertion operations as the next free index would have to be located. As the ordering in unimportant there is no reason to use a LinkedList data structure and the improved performance of the ArrayList versus an Array has enabled the author to confidently

select an ArrayList implementation as the best suited data structure.

Unless explicitly stated by loading a configuration from a file, the locations of the City elements in collection of cities is randomised. There are conditionals in place to ensure that two cities cannot be placed in the same location as this is a possibility when randomising locations. The implementation of the City instantiation can be found in figure C.4.

The starting location of the Ant objects represented as elements in the collection of agents is also randomised. This random value is however limited to a range of integers with a maximum possible value equal to *cities.size()* – 1. As indexes start at 0, this enables the random function to return any City index such that it is possible for an agent to start at any City location. The implementation of this agent instantiation is defined in a figure C.5.

### 5.2.3 Best Route Representation

Storing the current best route is slightly more complicated than storing the collection of agents or cities as the ordering must be preserved. As the ordering is important the accessing of random indexes is irrelevant as the elements stored in this data structure when parsed in order represent the order of cities which the agent visited to produce this best route. The indexing of random elements would enable the elements to be parsed in an incorrect order, thus this functionality will not be used by the author and therefore the data structures performance when executing such a task is nullified. The data structure used for this representation does not need to have dynamic resizing capabilities as the length of any best route will represent the number of cities in the problem as an agent must visit every City exactly once. The author reduced his choice to using an ArrayList or a LinkedList implementation. A LinkedList implementation has massive performance enhancements when compared to an ArrayList as a LinkedList can provide constant time ( $O(1)$ ) insertion and deletion operations using iterators which can be relied upon regardless of the magnitude of such data structure. An ArrayList cannot reliably provide such performance and its use is not justified in this scenario. This in addition to the fact that the ordering of elements is important, has lead the author to decide on using a LinkedList data structure for the representation of the best routes.

## 5.3 Pheromone Operations

The translation of the pseudo-code described in algorithm 7 was a simple process as the pheromone algorithm is itself relatively simple. Once implemented the author quickly realised that the pheromone operations (deposit and decay) were not behaving correctly. During the course of an agents *move()* method every time the agent moves from its current location to its next location pheromone proportional the distance travelled would be deposited on the corresponding edge. The problem was that every time this pheromone was deposited the global pheromone was in fact being decayed so the global pheromone was being decayed every time the agent moved. In order to prevent this problem from arising rather than directly updating the pheromone on the edge when the ant moves the pheromone deposit on this edge is instead added to a secondary *newPhero* variable in the Pheromone object for this corresponding edge. This variable is used to collate the total amount of new pheromone to be deposited for any edge. When it is time to update the edge pheromone, every Pheromone object is iterated through and value present in this *newPhero* variable is used in the pheromone calculation allowing for correct behaviours to be represented. This is slightly more

complicated than the author envisioned however, the additional complexity is essential to ensure correct behaviour. The implementation of this method is shown in figure C.6.

## 5.4 Solving the Problem

The author encountered unforeseen complications when implementing the pseudo-code represented in algorithm 1. The subsections below described the problems with the implementation process and their associated solutions.

### 5.4.1 Agent Movement

The author initial problem lay within his implementation of the probability based movement function. The problem caused every Ant that started at the same City index to take exactly the same route. Upon debugging the Ants *getNextProbableNode(int y)* function the author realised that there was in fact no random element associated with this method and the City with the highest probability was constantly selected thus, the Ants never had the ability to divert away from the best looking route causing local solutions to be present. The author attempted to implement this random element into his method however the algorithm did not perform as efficiently as expected. Thomas Jungblut had provided an open source implementation of a Basic Ant Colony System algorithm [22]. This implementation was provided free of charge and allowed modification which enabled the author to replace his lacklustre node selection function with the one provided in this working implementation. Once this method had been modified and implemented the node selection process for the Ant's next location worked as initially intended. The author realised that his implementation took completely the wrong approach which involved sorting the candidates locations based on their associated probability. Had the author not accepted that the reuse of a working implementation is the best way to progress the application then a reduction in project quality would have been a possibility. The implementation of this node selection method can be seen in figure C.7. If this method returns  $-1$  then the ant is deemed to have completed its walk.

### 5.4.2 Automated Solving

Implementing an algorithm which once started, executes until completion was in fairly simple to achieve. This simplistic implementation stemmed from the fact that initially the algorithm only considered the fact there was one iteration. As there was one interaction it was simple to define a stop condition which was in fact when every agent had completed its walk which meant the algorithm stopped when *Ant.getFinished()* returned *true* for every Ant. Once the author had implemented automatic execution for one interaction the ability for a user defined number of interactions was implemented. The addition to support  $x$  number of iterations where  $x > 0$  introduced several new complications. Each new iteration meant that the Ants need to be reset so that they forget everything from the previous iteration(s) but the pheromone levels, cities and current best route must all be persevered across iterations. In order for this to be possible, the author adapted the algorithms stop condition to now be relative to the number of iterations or in other words stop when *currentIteration == totalIterations*. A new iteration is started when all Ant's have finished their walk. Instead of checking every Ant for the condition *Ant.getFinished() == true* once an ant had finished a variable representing the total number of Ants current working (unfinished)

was reduced by 1. When this value reached 0, there are no ants currently working thus, the iteration has completed. Once an iteration has completed the Ants must be reset so the next iteration can start. This is done by calling the *initAnts()* method again on the current *World* enabling the old Ants to effectively be reset. The variable representing the number of Ants working is also reset so that *antsWorking == totalAnts* and the process starts again. During this reset operation the pheromone levels, cities and best route remained unchanged to preserve previous iteration results. The implementation for this algorithm can be found in figure C.8.

### 5.4.3 Step Based Iteration

An algorithm which executes on a step-by-step basis will require constant user interaction in order to execute to completion. In order to achieve this, several modifications have been made to the algorithms used in the process of automated solving. The first problem associated with step-based iteration is the fact that an ant must be stopped moving after it has moved to its next location. In comparison the fully automated approach uses an algorithm which ensures an ant continues moving until it is finished or move until the algorithm in figure C.7 returns  $-1$ . In order to stop the ant after one movement the algorithm in section 5.4.1 remains largely the same, however this while loop must be removed so that the movement function executes once and only once per step. This change alone however is not enough to stop the algorithm from executing until completion. Rather than using a *for each* loop to iterate through every ant and instructing it to move as described in figure C.8 there must now be a way to track the current ant under evaluation and update this tracker once said ant is complete. An index representing the location of current working ant is stored so that when the algorithm is stepped through only the ant at that index is signalled to move one step. Once this ant has finished this index is incremented until *index*  $\geq$  *agentsCollection.size()*. Similar to the algorithm described in section 5.4.2 once every Ant has finished walking, the iteration is complete and if there are more iterations to execute then the Ants and index are reset. Although this feature wasn't part of the initial or improved design, the ability to re-use the existing algorithm enabled the implementation of the feature to be far less complex. The implementation of this step based iteration can be seen in figure C.9.

## 5.5 Rendering the Algorithm

The implementation of the pseudo-code represented in algorithm 4 turned out to be far more complicated than the author actually planned. The subsections below segment the complications that arose and the steps the author took in order to ensure a proper visualisation process.

### 5.5.1 Swing Worker

Initially the algorithm was being executed on the AWT event-dispatching thread. The automated solving process is long and somewhat resource intensive. During the algorithms execution as the interface and algorithm are both on the same thread, the user interface would freeze and become unresponsive until the algorithm had completed. The implications of this are that literally none of the algorithms execution is visualised, which is the complete opposite of the intended implementation. The author realised that this is extremely bad design and in order to correct such complications concurrency should be introduced into the system. The graphical user interface is

built up of several Swing component and these components are not thread safe which can cause some concurrency problems. As a result of these components not being thread safe the Java language is defined such that any access to these components must be done from within the same thread which happens to be the Event Dispatch Thread. In order to both modify the user interface and execute the algorithm in a concurrent manner the author has used the `SwingWorker` interface provided by the Java language specification. A `SwingWorker` is designed to perform lengthy tasks which interact with a graphical user interface adhering to the language specification protocols. The `SwingWorker` has a `doInBackground()` method which is executed inside a separate Worker thread. During the execution of the `doInBackground()` method any interactions with the Swing components are dispatched on the correct Event Dispatch Thread by the `SwingWorker`. As a result the author has been able to implement concurrency to allow for the parallel execution of the algorithm and interface modification relatively complication free. The code contained within this applications `SwingWorker` is shown in figure C.8 and is the location of the algorithm discussed in section 5.4.2.

The step-based iteration method of solving does not need to worry about such complications as each step takes very little time to complete, thus the use of a `SwingWorker` to facilitate such behaviour is over complicating the situation and will not benefit the user in any way.

### 5.5.2 Visualising Agent Movement

One of the major problems associated with the visualisation of the algorithms execution is accurately representing the agents movement between two city locations. Initially the agents would move between cities without any indication to the user about which path the agent took as the agents themselves would seem to ‘teleport’ from one city to the next. This is not the kind of feature that should be present in an application of this kind. The author decided that there needed to be a way to visualise the agents movement between cities however, the visualisation of this movement should be simple so that it doesnt over complicate a simple action such as moving from one point to another. Every ant stores the indexes of the last two cities it visited in a variable called *movementTracker*. This variable is an array of integer values of size 2 and it will only ever contain the last 2 cities the agent visited thus, *movementTracker*[0] represents where the ant started prior to moving and *movementTracker*[1] is where the ant finished.

The author decided that as the coordinates of the two cities stored in this *movementTracker* variable are simple to obtain it would be straight forward to use linear interpolation to draw a visual aid along the Ant’s movement path in order to highlight the ants traversed path. Given a start and end coordinates for a line Linear Interpolation can be used to find the coordinates for any point along that line.

$$\begin{aligned} result_x &= x_1 \times (1 - \mu) + x_2 \times \mu \\ result_y &= y_1 \times (1 - \mu) + y_2 \times \mu \end{aligned}$$

Figure 5.2: Formula for Linear Interpolation where  $x_1, y_1$  are the start coordinates,  $x_2, y_2$  are the end coordinates and  $\mu$  is the location to find [18].

Once the coordinates of the two cities stored by index in the *movementTracker* variable have



been retrieved they can be passed to the *LinearInterpolateX(double x1, double x2, double mu)* and *LinearInterpolateY(double y1, double y2, double mu)* methods in order to find a point on the line between these two city locations. The correct  $\mu$  value must be selected in order to provide the best representation. The author opted to go for drawing a series highly visible ellipsis along the line with the distance between said ellipsis to be 0.2 which is the equivalent to approximately 20% of the lines total length. These ellipsis will therefore be drawn using the retuned values from the equations in figure 5.2 where  $\mu = 0.2, 0.4, 0.6, 0.8$ . This will enable the user to clearly identify which path has been taken and also enable the user to judge the length of said path as the longer the path the greater the spacing between the ellipsis. The code implementation of the equations in figure 5.2 is shown in figure C.10 and the code for drawing the path itself is shown in figure C.11.

### 5.5.3 Scaling

In order for the visual representation to be rendered in a suitable manner there has to be some form of scaling to ensure all the visual elements retain the correct aspect ratio. The size of the canvas area is fairly limited so the author had to decide on a scale factor which enabled the complete representation to be contained within the canvas bounds. The author decided that as the canvas area is 800px in width and 600px in height a scale factor of 20 is perfectly suited to this environment. 20 is a factor of both 800 and 600 this scale factor will provide the author with a 40 x 30 grid of 20 x 20 squares. If a scale factor greater 20 were to be used then the dimensions of this grid would change and if this scale factor was too large there would not be enough room to display an adequate amount of detail. Using a value less than 20 would cause the rendering to shrink significantly which would make it difficult to render in a manner which is accessible to all users as the little details would be far too small.

This scale factor will be applied when rendering any element on the canvas including city locations, agent locations and drawing paths between cities. If a city has the  $(x, y)$  coordinates of (18, 15) and the author did not scale this when rendering then the city would be rendered at (18px, 15px). If a further two cities had the  $(x, y)$  coordinates of (30, 5) and (2, 9) respectively, with no scaling applied these cities would be rendered extremely close to each other which would make it difficult to visualise the algorithm execution as the world would occupy an extremely small amount of canvas real estate. Applying this scale factor to same set of cities and coordinates causes the cities to be rendered at (360px, 300px), (600px, 100px) and (40px, 180px). This produces a world where the cities are suitably spaced such that there is sufficient room to render the algorithms execution and visualise the agents movements between such cities. This scaling factor is hidden from the users. As far as the user is concerned when creating a file for use in loading a problem configuration a cities  $(x, y)$  location is specified in terms of its grid square location rather than in terms of scaled coordinates as shown in figure D.5.

### 5.5.4 Painting the Canvas

Every aspect discussed in this section is vital in the painting of the algorithms execution for the reasons stated above. As every aspect of the algorithm needs to be visually represented the actual painting of the algorithm to the canvas became more complex than the author initially envisioned.

Representing the city locations simple to implement as every city stores the location for its  $(x, y)$  coordinates. In order to render each City at its correct location, the collection of cities is iterated through and the method *drawOval(City.X × 20, City.Y × 20, 20, 20)* is used to draw

an oval which has the width and height of  $20px$  and is represented in the correctly scaled location. There is a slight problem with this implementation however. As discussed in section 5.5.3 the canvas is segmented into  $40 \times 30$  grid therefore the coordinates representing a grid cell represent the top right corner of such cell. If a city is drawn at  $(20, 10)$  then this will be drawn in the top right corner of the grid square  $(20, 10)$ . The author found this to be visually off putting and didnt produce the intended look. In order to prevent this the location of the drawn city must be offset such that rather than being drawn in the top right of grid location it is drawn in the centre of such grid location. In order to do this a simple change to the *drawOval* methods parameters is required. The modified version of this method call now resembles *drawOval*(( $City.X \times 20$ ) - 10, ( $City.Y \times 20$ ) - 10, 20, 20) where 10 represents  $\frac{scaleFactor}{2}$ . This will now draw the cities centred into the correct grid square. These coordinates are also used to render the ants at a city location. As every ant stores the index of the city it is current at, it becomes trivial to found the location where it should be drawn by iterating through the collection of cities until the corresponding index is found.

Representing the path between these cities is also a somewhat simple task. These routes are used to visualise the routes which any agent can take to navigate between any two cities. As the graph is being represented as a fully connect graph where any city can be reached from any other city, the paths displayed to the user must reflect this. Each path will be displayed as defined in section 5.5.2 which is as a line drawn from one city to another. The collection of cities will be iterated through, and for each city in the collection the collection of cities will be iterated through again. The first iteration of the collection will represent the start location for each line then whilst keeping this location the same, the next iteration of the collection will be used as the end location for the line (path). This is a simple way to draw a line from each city to every other city.

As these lines represent the paths between cities, they are therefore used to represent the edges connecting nodes in the graph and as a result these lines are also to be utilised for the visualising of the pheromone concentrations on such edges. In order to represent the pheromone the author has decided that the opacity will change in proportion to the pheromone concentration on their given edge. As the pheromone values for a given edge can become incredibly small ( $<< 0$ ) depending on the number of iterations, cities and agents the opacity of such lines must be based on a suitably scaled version of the pheromone values on each edge. The author decided use a scale factor of 2000 when applying the pheromone concentration to the opacity of the corresponding line however, the opacity (alpha) level for a given line is an 8-bit integer thus 255 is the maximum value. To prevent conversions of  $pheromoneConcentration_{xy} \times 2000 > 255$  causing problems there is a condition to catch larger values and reduce their size to maximum legal value of 255. As the pheromone concentration gets lower and lower the paths with start to become less visible to the user so they can easily see which paths are being used most often.

Displaying the best route to the user is the most complex part of the visualisation process and also one of the most important. The implementation of this feature was far more complex that the author expected and its complexity extends further than simply drawing a red line. As a line requires a start and end location this means that the best route data structure (see section 5.2.3 must be iterated in pairs, and accessing these pairs is not as elegant as the author has planned. The best route will be created using a series of lines drawn between such pairs. Once the first city within a pair has been identified the next element in the data structure is the second city belonging to the pair however, the author first has to check if there is in fact a next element before such an action can take place. This involves the use of a condition similar to  $(elementIndex + 1) < bestRoute.size()$ . If this condition returns true then continue with the line drawing process as there is a valid pair

of cities to draw a line between. Once this pair of cities has been identified it is simple to draw a line between them as the coordinates are known. The complexity comes from the multiple nested iterations of the city collection in order to locate the city pairings, this makes the code block slightly more difficult to both debug and mentally visualise which made this feature slightly harder to implement. The code for such a feature is shown in figure C.12.

## 5.6 Elitist Ants

The addition of Elitist Ants was slightly more complex than the author initially thought however, as a whole it is not an overly complex feature. The algorithm remains largely unchanged from the Basic Ant System, the added complexity comes from the fact that pheromone needs to be deposited on the Elite Ant best routes every iteration. Correctly storing and updating the current  $x$  number of Elite Ants was simple to implement for the author and involved checking to see if this agent should be an Elite Ant based on its total distance travelled. The implementation for this is shown in algorithm 2, lines 19 to 24 and remains as designed. As discussed with the rendering of the best route, the deposit of pheromone along the path can be done so using a similar pair based iteration. This is slightly less complex than the rendering process as there is no need to retrieve the city coordinates. As the pheromone matrix is set up in a manner such as that stated in section 5.2.1.1 only the city indexes are needed. Once a pair of city indexes has been extracted from the best route pheromone can then be deposited along the route in a fashion similar to `pheromone[CityPair1.index][CityPair2.index].addToNewPheromone(pheromone[CityPair1.index][CityPair2.index].getPheromone + e)` where  $e$  is a constant representing *# of cities*. The code for depositing pheromone of the  $x$  number of elite routes is shown in figure C.13.

## 5.7 Uphill Path Generation

The implementation of uphill paths was itself quite simplistic and involves the process of locating the route's corresponding element in the distanceMatrix and doubling the contained value. This enables an uphill path to twice its usual cost. Depending on the current  $\beta$  value, the agents will generally have a higher probability of taking a shorter path. As this is the case the addition of such uphill paths allows the algorithm to potentially produce a wider range of solutions to the same problem configuration.

The selection of these uphill routes is slightly more complex than the author assumed them to be. The location of these uphill paths is currently randomly generated such location is determined by using the `Random.nextInt(# of cities)` method to randomly select an element from the distance matrix. There are problems with using a random selection process for selecting the start and end locations for this uphill path however. These start and end locations will be valid city indexes which means that these two randomly generated values cannot be the same as there is no edge from a city to itself. This is where the added complexity is introduced. The author must now check that the randomly generated values are in fact different, if they are equal then the random generation process must happen again. As the random value generated is in the range of `0...cities.size()` the likelihood of these random values being equal is dependent on the magnitude of the value range. If there are few cities then this random generation process may have to be executed an inefficient number of times until two non-identical values are generated, this is not

really a problem if there are a large number of cities. The code representation for the generation of uphill routes is shown in figure C.14.

## Chapter 6

# Testing

### 6.1 Overall Approach to Testing

This chapter presents a multitude of different testing types. There are automated unit tests to ensure the internal code logic behaves as expected. The User Interface tests are tests which are difficult to automate but are used to ensure that the user interface models the correct state of execution. Acceptance testing is used to assess how well the applications meets the specified requirements in section 2.3. Stress testing has been considered by the author but ultimately has been omitted. The author feels that the application is never subject to heavy loads, nor can the user exceed the normal operational load for the application. Overall the testing process is not as thorough as the author desires however, given the short time frame for the projects development the author feels that the testing suffices in ensuring correct functionality.

### 6.2 White-box Testing

#### 6.2.1 Unit Tests

There are features present in the application code which the author has excluded from the unit testing process. Any feature which relies on random numbers to perform its task has not been unit tested. The author feels that any methods which uses a random number cant reliably be tested therefore, it doesnt makes sense to attempt to. Instead the author has extracted the code which relies on such random numbers and tested the behaviour of such code using specifically defined values, this enables the author to accurately test for expected behaviours. In addition to this getter and setter methods or simple assignment operations have not been tested. The reason for excluding these methods from unit tests is because the code responsible is so simple it cant realistically fail so there is no real purpose in producing such tests.

The unit tests that the author has produced revolve around ensuring that only legal algorithm parameters are accepted and that the movement, probability and pheromone functions are behaving as expected and return legal values. These tests contain validation checks against a range of values for each parameter including boundary conditions to ensure that they are correctly dealt with, examples of such testing can be seen in figures D.1 to D.4. There are many more tests present in the test package for the application however the author has only briefly outlined a small number

of these. Evidence of such testing can be seen below in figure 6.1.

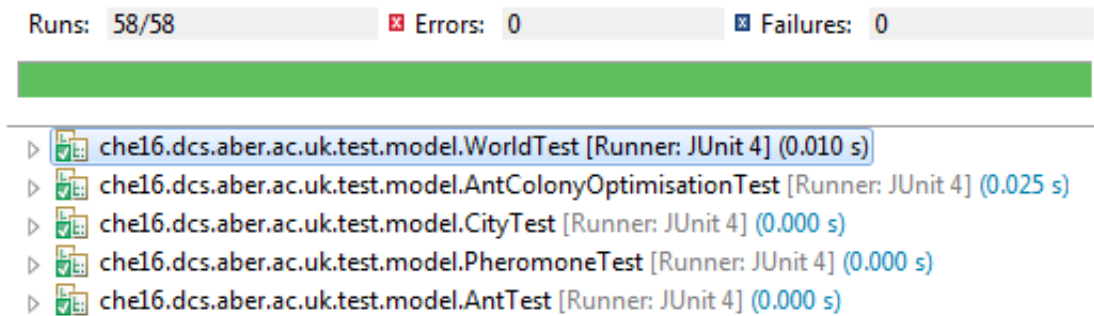


Figure 6.1: Evidence of the completed execution of the applications unit tests. The view present is the built in Eclipse JUnit interface.

## 6.3 Black-box Testing

### 6.3.1 User Interface Testing

It is difficult to reliably test the graphical user interface using a white-boxing testing approach. To overcome this obstacle the author has decided to manually test the user interface using a black-box testing approach to ensure the correct behaviour is exhibited. During this test process the author did not repeat any test previously executed in the unit testing process.

The file IO process will also be tested to ensure that configurations can be correctly loaded and saved to a specified file. Several test files will be produced, each file will be designed to test a variety of possible legal and illegal file contents. Tests will be done to ensure that the application rejects files that contain; missing data, incorrect type for a specified value and city coordinates which exceeds the bounds of the canvas. The saving of a configuration to a file doesn't need to be as rigorously tested as the algorithm has to be instantiated with legal values before the writing process can be executed therefore, the values of the written file will be legal and of the correct format. An example of such file contents can be found in appendix D, section 4.2.1. The full list of black-box tests performed by the author can be seen in section appendix D, section 4.2.3.

### 6.3.2 Acceptance Testing

Due to the lack of a dedicated client acceptance testing proved difficult for this project. For the purpose of these acceptance tests the author acted as the end user, and used the application in a non-bias manner and adapted the mind-set of a new user. This is far from an ideal way to perform acceptance tests and this process isn't truly representative of real acceptance testing. The application itself is not a finished deployment ready product. Before this would be the case the author would like to extend current functionality and provide a larger variety of algorithm types and modifiers. If the author had a larger time frame then a distinct customer or user group would be set up to ensure this acceptance testing process is performed to the highest quality. Similar tests have been grouped together, the results of this process can be found in appendix D, 4.2.2.

## Chapter 7

# Future Work

This chapter briefly discusses the additional work the author could complete if the project had a longer development time frame. These features are not essential but the author sees them as next logical steps in producing an educational tool which visualises several different classification of algorithms in a manner understandable by the majority of users.

### 7.1 Additional Algorithm Types

The application current only supports the Basic and Elitist Ant System algorithm variations. The author would like to increase the number of algorithm variations which are available for selection. As the framework is already in place, additional algorithm types would be simple to implement as the application has been designed in an abstract manner such that the model can be reused and modified without impacting the current functionality. The author would at least aim to implement the Max-Mix algorithm and would further implement additional variations such as; Rank-based Ant System, Ant Colony System and a Recursive Ant Colony algorithm if the opportunity arose.

$$pheromone_{xy} = [(1 - \rho) \times \tau_{xy} + \Delta\tau_{xy}^{best}]_{pheromone_{min}}^{pheromone_{max}}$$

Where;

$$[x]_{pheromone_{min}}^{pheromone_{max}} = \begin{cases} pheromone_{max} & \text{if } x > pheromone_{max} \\ pheromone_{min} & \text{if } x < pheromone_{min} \\ x & \text{otherwise} \end{cases}$$

Figure 7.1: Algebraic model of the pheromone deposit function for the Max-Min Ant System [15]

The Max-Min algorithm is an extension of the Elitist Ant system in some regards however in the Max-Min Ant System only the best Ant(s) update the pheromone trails and the amount of pheromone deposited has strict boundaries. Generally, this algorithm out performs the Elitist Ant System and will usually converge in less time. Figure 7.1 demonstrates how the pheromone

is deposited for the Max-Min algorithm variation. Currently this is the only non implemented algorithm the author has researched.

## 7.2 Bee Colony Optimisation

The author would like to include a different class of swarm intelligence methods which in this case would be the introduction of the artificial Bee Colony classification algorithms. The application would not have to change much in terms of design as the view and controller could be reused however there would need to be significant modification to the current model in order to support the Bee Colony algorithms. The additional swarm intelligence families would enable the user to not only switch between algorithm types they would also be able to switch between classes of algorithms and contrast both the execution and result of each. This will greatly increase the educational potential of the application. The author has not researched the Bee Colony algorithms in much detail of yet however he is aware of the general concepts. The implementation of such algorithms is likely to be a fairly complex task, although this is made slightly easier through the reusability of the view and controller but this process may still take a considerable amount of time which the author currently does not have at his disposal.

## 7.3 Search Algorithms

As the word can be represented as a graph, the current framework can be reused and modified to show the execution of different search algorithms. The author would like to include algorithms from both the informed and uninformed search algorithm classifications to maximise the applications educational value. The implementation of such algorithms should not be too difficult as there is a multitude of well documented resources describing the different algorithm types and their implementations in several languages. The author would initially aim to implement the more commonly used or well-known algorithms such as; Breadth-first search, Depth-first search, A\* search and Dijkstra's algorithm. As A\* search and Dijkstra's algorithm are informed search algorithms they can be used in conjunction with multiple different heuristic functions which will enable the user to contrast both algorithm and heuristic performance in a variety of scenarios.

## 7.4 Graph Representation

Currently the problem is represented as a fully connected graph. The author would like to implement the ability for the user to specify that they do not want a fully connected graph to be generated. This would cause the algorithm to behave very differently as the user could see how restricting the agents movement between specific cities drastically changes the returned route. The implementation of this feature was considered for inclusion in the current system by the author however, there are several complications which lead the author to leaving out such functionality. As the graph would not be fully connected there is the potential for the agent to get into a situation where it has no possible moves. If the agent has visited every city but one, and the current city has no connection to the last remaining city then the agent is in fact stuck. The potential solutions to this problem havent fully been explored by the author due to time constraints thus the author didnt feel completely confident implementing a feature which may be sub optimal in performance.



## Chapter 8

# Evaluation

### 8.1 Final System Evaluation

In my opinion the final system is well suited for its intended purpose which is to provide a visualisation of Ant Colony Optimisation methods for use in an educational environment. The application meets all of the functional requirements specified in section 1.3.3 which confirms that the application provides a solution to the initial problem. The application is fully capable of rendering an automated execution or a step-based iteration of two Ant Colony algorithms. The visualisation process can be heavily controlled through user interaction which enables the modification the algorithms execution speed, loading of configurations from a file, modification of the algorithms parameters and a choice of algorithm types and modifiers

Although I personally feel that the application meets the specified criteria, I am not fully satisfied with the current functionality provided. Before I would consider the deployment of this application I would like to implement some of the additional features discussed in chapter 7. The additional features, more specifically the addition of extra Ant Colony algorithm variations would be a high priority and personally they feel necessary in order to create the most suitable environment for the teaching of such methods. The currently implemented algorithm types are not inadequate in anyway, it would just not be in my personal interest to release an application which does not meet my full expectation. The implementation of several algorithm types is beyond the projects scope so some compromise has been made.

On reflection the initial design of the system was extremely inadequate this is due the fact that the projects complexity was underestimated. The process i used enabled me to stray from my proposed design and enabled refactoring and modification of such design to produce the current architecture. The revised design is far more reflective of the problems complexity and its far more logical. The decision to adhere to Model-View-Controller principles has allowed myself to produce a framework which is easy to maintain and modify and can be used to display multiple different algorithms as discussed in chapter 7. Using Java as the implementation language was a decision I started with and I am glad I did. My personal experience with the language in conjunction with the easy to develop Swing interfaces enabled me to create a simple yet efficient user interface which is cross-platform and accessible by the vast majority of potential users. The current user interface is however far from perfect. The main problem with such interface is that fact that the dimensions of each element are statically defined and as a result the application cannot be resized in anyway. Generally on modern computers the dimensions of the interface will cause

no problems but there is the potential for a user using a small display for the user interface render incorrectly resulting in an unusable application.

The process of visualising the algorithms execution is a good basis for future development but the current implementation of some of this visualisation process i am personally not fully satisfied with. As a whole the visualising of the city locations, the pheromone operations and the best route are more than appropriate whereas the visualisation of the agents and their movement between city locations is far from ideal. I wanted to keep the visual representation as simple as possible which I generally feel that I have achieved. As a result of this the agents movement between cities is not as detailed or as informative as I intended. The main problem with the current system is that the ants direction is not represented in anyway which is somewhat problematic. If I had more time I would focus on implementing a better means of displaying an agents movement, however given the short development timeframe and the fact that there is some form of visualisation in place i decided to leave it in its current state for now.

The application may meet all of the suggested requirements however, there are overall objectives which are current unachieved. The applications meets 6/9 ( 67%) of the objectives highlighted in section 2.2. This may seem that a large percentage of the objectives have been met and whilst this is technically true, I feel that the easiest objectives has been met and this percentage isnt truly representative of the remaining work. These remaining objectives relate to specifying a graph to be incomplete as discussed in section 7, the implementation of multiple problem representation support and the addition of a larger variety of Ant Colony algorithm variations. Meeting these three objectives is far from trivial but once complete I feel that they will significantly improve the overall user experience and success of the project.

Aside from the issues mentioned above i feel that the application is on track to outperform the majority of its existing competitors. This applications visualisation process and user interface in far more user friendly and caters for a wider variety of people. If given more time to further develop the project there is no reason why this application could not become one of the best educational tools for the teaching of Ant Colony algorithms. If the project were to be restarted the general approach would remain the same however, I would spend more time on the initial design as I feel I wasted valuable time when I had to redesign and refactor the initial sub-par design. As it currently standards the application should be considered to be in its alpha stage, and will be ready for deployment after the additional features have been implemented and tested.

## 8.2 Personal Evaluation

The project has been complicated, challenging, interesting and most importantly it has been enjoyable. I have learnt a significant amount about Ant Colony methods and swarm intelligence. I enjoying learning so this has helped me maintain my focus throughout the development process as complicated problems were often infuriating and disheartening.

Generally throughout the course of the projects lifespan I have made reasonable progress. Admittedly i did not make the amount of progress that I would have liked to during the early stages as commitments to other modules in terms of both lectures and assignments restricted the amount of time i had to work on this project. There were breakpoints during the development of the application, once these were broken progress improved significantly. The main breakpoint was the implementation of the underlying Basic Ant System and the user interface which happened to be quite time consuming. Once these had been implemented it became much easier to progress

with the application as it was simple to visually test additional features. The main complication during the development was ensuring that the algorithm executed on a separate thread to the user interface in order to prevent the interface from freezing whilst also enabling interaction between the current algorithms state and the view. I was not prepared for this kind of problem and reflecting on this I should have done more research in the early stages of development in order to prevent this kind of complication which ended up costing me a fairly large amount of time. The time lost here could have been put into the testing as the testing process was fairly rushed and I wish I had much more time to perform a series of more detailed tests.

In summary I feel that my project is a successful thus far and has a bright future. I have increased my knowledge in the subject area by a significant amount and I have greatly improved my software development skill set. Personally I have a feeling of self-pride as I have achieved a lot in a relative short space of time both in terms of technical achievement and personal skill development. I underestimated the problem originally and wrongly assumed I could create an interface and implement an algorithm and make the two elements interact and I would have a sufficient application, I am glad to say I have proved myself very wrong. If I were to do this project again I would like to properly time manage so that unforeseen complications werent as much of a problem as they were and I would like to have a lengthier test period. I think I have achieved my best work for the time available and the fact that I have met all of the proposed requirements allows me to call this project a success.

# Appendices

## Appendix A

# Requirements Specification

### 1.1 Introduction

#### 1.1.1 Purpose

The purpose of this document is to give a detailed description of the ‘Visualising Ant Colony Optimisation’ application. This document will cover interface interactions and methods as well as providing definitions to important terminology. The document is primarily intended to be used as a reference point for the initial stages of development.

#### 1.1.2 Scope

The ‘Visualising Ant Colony Optimisation’ application is a desktop application which is designed to demonstrate the behaviour of an underlying ACO algorithms given various parameters. These parameters will be user defined and can be modified at their convenience. The algorithms behaviour given these parameters will be visible and the users can make a clear assessment about how each of the parameters impacts the algorithms performance.

During the background research into this subject area there does not seem to be too many applications which offer ACO visualisations and there are even less which provide a ‘friendly’ environment which is simple and intuitive to use regardless of the users background knowledge.

The software will be deployed in an educational environment, with aims to provide a means for teaching ACO to students as part of an Artificial Intelligence course or for independent use as a self-learning exercise. As a result the software must cater for the majority of user groups to maximise its effectiveness. This means the software must be accessible on all major platforms and perform equally well on said platforms.

Term	Definition
ACO	Ant Colony Optimisation
user	Anybody who is using or wishes to use the software
user group	A collective group of users representing different user needs.
interface	A graphical user interface
standalone	Operates independently of other hardware or software
agent	The entities which will be traversing the graph

Table A.1: Definitions for the keys terms used throughout this document

### 1.1.3 Definitions

## 1.2 Overview

This section will give an overview of the proposed application. This section will also expand on the expected user groups and functionality required by said groups. The constraints and assumptions will also be stated.

### 1.2.1 Product Descriptive

The software will be a standalone application that does not need to communicate with another system or application because of this, there is no need for any form of network connection to be present in order to use the application to its maximum potential.

The application will communicate with the Operating System on the host machine in order to enable the save and load functionalities through simple file input and output. However the users access to the host machines file system will be restricted by the fact that the saving and loading will be restricted to the users home directory preventing the overwriting of important documents.

The application itself will not take up too many system resources even if a large problem is being handled. This allows the users on a system or network to run the application without it impacting the performance of other services. Given that the target audience is educational establishments this is especially important as many teaching fellows have multiple applications running during a lesson or lecture and a negative impact on their system could reduce the amount of information taught during said session.

### 1.2.2 Product functionality

The users will be able to view a world which represents the Agents and the nodes. The state of this world will be directly related to the algorithm parameters specified by the users using the interface provided. There are several parameters which can be modified by the user, each of which will have a different impact of the state of the world and the algorithms behaviour.

The parameters which can be modified will be clearly labelled and will be clearly defined as editable. As these parameters will be user defined there will be strict error checking measures in place to catch any illegal values before they can cause problems for the algorithm in addition, each parameter will have a range of legal limits applied. This will prevent the users from entering

values of the incorrect type (String when the systems needs a double) and will also prevent values from outside of the specified range being accepted. When a complication or error arises there will be a simple error message presented to the user informing them of both the error and why it occurred which should enable the user to resolve what they did incorrectly.

### 1.2.3 User Groups and Characteristics

There will be three main user groups associated with this application. Each of these user groups will interact with the application in a slightly different manner but the main purpose and result will remain the same.

**Teachers/Teaching fellows** will use the application with the underlying knowledge already in hand. They will be mainly be using the applications to visually portray ideas and will have expectations in regards to what to expect for a solution and will have some idea how the parameters impact the final result.

**Students** will use the application with some background knowledge of the underlying concepts but will still use the application in an experimental manner and may have little expectations or understanding of how changing certain parameters impacts the final result.

**People new to the subject area** will use the application with potentially no idea about the underlying concepts. There will be measures in place to explain the underlying metrics and give an insight into what the application is actually doing. Given that they have less knowledge of this subject area that the other two user groups mentioned above, they will still be able to achieve the same results and levels of functionality. The application will cater for all users regardless of prior knowledge.

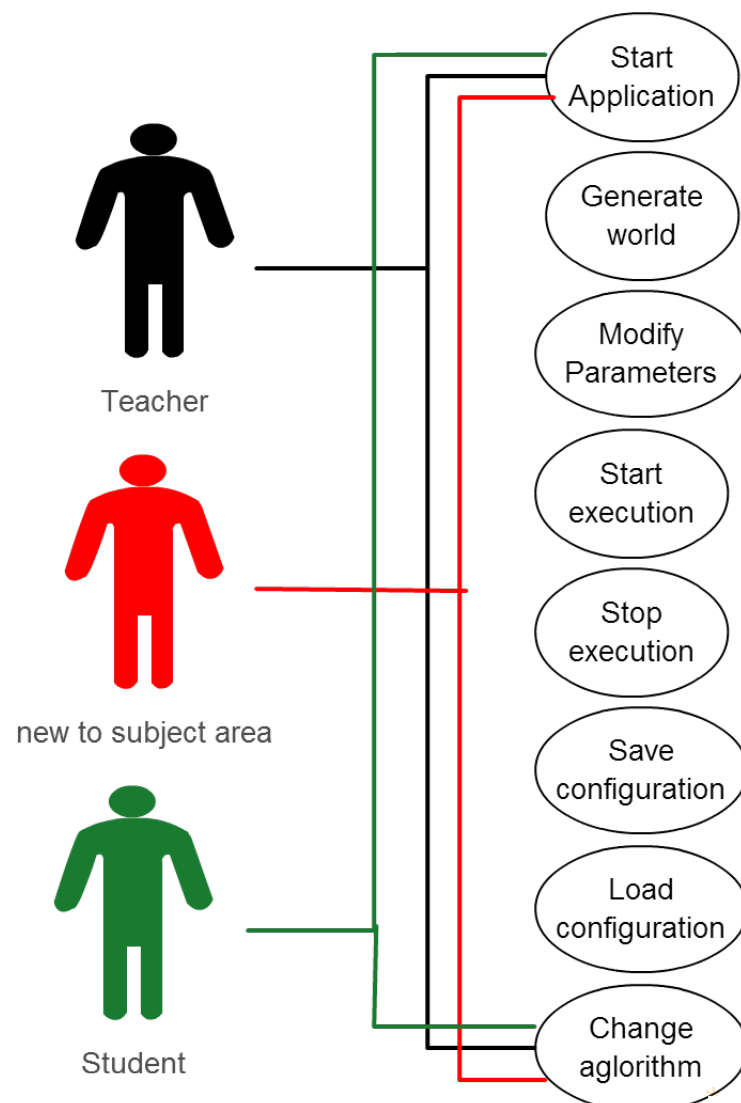


Figure A.1: Use Case Diagram showing how each of the above user groups can interact with the system. Regardless of the user, they can perform every action.

### 1.2.4 Constraints

As the application is standalone it reduces the number of constraints which it becomes subject to. The main constraint which the application is associated with is the dimensions of the users display. The interface has to contain numerous elements in order to produce a simple and effective environment, thus it takes up quite a lot of screen real estate. However in modern times the amount of space required for the application to perform as expected is far from unreasonable and the application will be developed with this in mind.

The algorithms execution time is directly proportional to the user defined parameters, more specifically the number of agents and the number of nodes in the graph. The more agents and nodes the larger the execution time and resource requirements will be. The application will be developed



with this in mind as there will be a constraint on how much memory and system resources the application should use. There is no expectation on the user to have a superfast high end machine therefore the application will be designed to accommodate a standard machine for these modern times.

The application does write the host systems file store so there must be adequate room to do so, however the files that will be written are simple text files which will not take up a lot of room on the host machines disk. Depending on the users machine this could still be a constraint. The responsibility and handling for this will belong to the users machine.

### **1.2.5 Assumptions**

It will be assumed that the user will have the correct drivers installed and their machine will be able to handle the algorithms execution. The applications algorithms are not too resource intensive, therefore this is a reasonable assumption given the modern era and the advancement of computer technology.

It will be assumed that users will meet the minimum display requirements thus no dynamic re-sizing of the interface based on the users display dimensions will be performed. This significantly reduces complexity.

Another assumption is that every user will have some experience of using similar software and the interface will be familiar and therefore will be easy to use and navigate. The interface will use traditional methods such as simple buttons, text boxes and drop down menus to provide the user access to certain functionality.

## **1.3 Specific Requirements**

This section contains the function requirements of the software as well as giving details about the different interfaces.

### **1.3.1 User Interface**

There will be one main user interface for this application. This interface will contain a display area which is where the algorithms current state of execution will be represented visually to the user. There will also be an area which will house the text boxes which will be used by the user to interact with the algorithm and modify the parameters.

The display area will be simple and will be clearly identifiable. The text boxes responsible for handling user inputs will be clearly labelled so the user knows exactly what parameter they will be modifying. The text boxes will be obviously editable and the user will associate the look and feel of these text boxes with the fact that their contents can be modified.

The display will represent everything about the algorithms current state. This will display all of the graphs Nodes and all of the Agents at their current Node. The display area will also show the current pheromone levels for each connecting edge for a given node, this will be done in a way that is clear and understandable by all of the user groups identified in section 1.2.3.

There will also be a textual representation of the current best agent. This will display the best route and the distance of the best route and will update as the global best is updated. There will also be textual representations of how many agents are currently working in addition to how many agents have finished.

### 1.3.2 Hardware Interface

The application does not require any specific hardware or host environment as it will be fully cross-platform compliant there are no direct hardware interfaces. There is no network use in this application thus there is no need to communicate with network adapters or anything of similar nature. The system interactions between this application and the host's Operating System file system will be delegated to the Operating System itself.

### 1.3.3 Functional Requirements

**ID: FR1**

Title: Launch the Application

Description: Regardless of the users host environment the application should be able to be launched by the user using an executable .jar file.

Dependencies: None

**ID: FR2**

Title: Generate a World

Description: The user must be able to randomly generate a world for the algorithm to be executed on.

Dependencies: FR1

**ID: FR3**

Title: Visualise a World

Description: The user must be able to visualise the world and its parameters including the number of agents, the agent locations and the number of nodes.

Dependencies: FR1, FR2

**ID: FR4**

Title: Provide a means to modify parameters

Description: The application must provide simple ways to modify the algorithms parameters.

Dependencies: FR1

**ID: FR5**

Title: Generate a World with specified values

Description: The user must be able to generate a world for the algorithm to be executed on. This world will have user defined properties such as the number of nodes and agents.

Dependencies: FR1, FR4, FR10

**ID: FR6**

Title: Visualise the Pheromone

Description: Every edge in the graph will have its own pheromone value. This must be visually displayed to the user and correctly model the pheromone deposit and decay operations.

Dependencies: FR1, FR2, FR3, FR13

**ID: FR7**

Title: Visualise the Agents movement

Description: As the algorithm is executing the agents will move through the graph. The movement of these agents must be displayed to the user in a logical manner.

Dependencies: FR1, FR2, FR3, FR8

**ID: FR8**

Title: Start the Algorithm's execution

Description: There must be a simple way for the user to start the algorithms execution.

Dependencies: FR1

**ID: FR9**

Title: Stop the Algorithm's execution

Description: There must be a simple way for the user to stop the algorithms execution anytime the user wishes to.

Dependencies: FR1

**ID: FR10**

Title: Validate parameters

Description: As the users will be able to define their own parameter values there must be correct measures in place to ensure the values entered are legal. If they are indeed illegal then suitable error messages will be displayed.

Dependencies: FR1

**ID: FR11**

Title: Display the best path

Description: As the algorithm is performing its task there must be a way to display the current best result to the user.

Dependencies: FR1, FR2, FR3, FR5, FR7, FR8, FR12

**ID: FR12**

Title: Agents must be able to move between Nodes

Description: In order for algorithm to perform as expected there must be a way for each Agent to move between Nodes in the graph.

Dependencies: FR1, FR2, FR3

**ID: FR13**

Title: Model Pheromone operations

Description: There must exist a way for the algorithm to correctly deposit and decay pheromones

on graph edges adhering to specific formulae.

Dependencies: FR1, FR2, FR3, FR11

**ID: FR14**

Title: Load Configuration from a file

Description: There must exist a way for the users to load a pre-existing configuration from a file of their choosing. This allows the algorithm to be executed on the same problem multiple times.

Dependencies: FR1, FR2, FR3

**ID: FR15**

Title: Save Configuration to a file

Description: There must exist a way for the users to save the current configuration to a file of their choosing. This allows the algorithm to be executed on the same problem multiple times.

Dependencies: FR1, FR2, FR3

**ID: FR16**

Title: Exit the application

Description: The user must be able to exit the application completely killing the process and freeing system resources.

Dependencies: FR1

### 1.3.4 Requirement Evaluation

Each of the functional requirements mentioned in section 1.3.3 differ in their levels of importance. The dependencies field for each requirement denotes which requirements must be completed before said requirement itself can be finished. As this is the case the following represents the order of importance for each functional requirement.

Each of the functional requirements mentioned in section 1.3.3 differ in importance levels. The dependencies field for each requirement denotes which requirements must be completed before said requirement itself can be finished. As this is the case the following represents the order of importance for each functional requirement.

Requirement	Dependant Requirements
FR1	FR2, FR3, FR4, FR5, FR6, FR7, FR8, FR9 ' FR10, FR11, FR12, FR13, FR14, FR15, FR16
FR2	FR3, FR6, FR7, FR11, FR12, FR13, FR14, FR15
FR3	FR6, FR7, FR11, FR12, FR13, FR14, FR15.
FR8	FR7, FR11, FR13
FR4	FR5
FR5	FR11
FR10	FR5
FR12	FR11
FR13	FR6
FR7	FR11
FR11	
FR6	
FR9	
FR14	
FR15	
FR16	

Table A.2: Table representing the Functional Requirements and which requirements are dependent on them.

As described in Table A.2 the number of dependant requirements a requirement has the more important it is to the progress of the application. FR1 is the first task that must be accomplished therefore every other requirement is dependent on this being completed. FR1 is the ability to launch the application, if the application cannot be launched then none of the other requirements can be completed, this is a critical requirement.

FR2 is another critical requirement which must be completed early in development as many other requirements are dependent on its completion. FR2 is the ability to generate a World. A World contains all the data that the algorithm needs in order to both execute and visualise, therefore if there is no way to generate a World there is no way to visualise or model the algorithms execution (FR3).

Apart from FR8 (start the algorithms execution) the remaining functional requirements are somewhat independent of each other and are less critical. However this does not mean that they can be avoided as they will be needed in the final application version.

## Appendix B

# Initial Design Proposal

## 2.1 Introduction

### 2.1.1 Purpose

The purpose of this document is to give a detailed description for the design of the Visualising Ant Colony Optimisation' application. This document will cover the proposed interface designs and interaction methods, choice of language and the underlying data structures and logical modules used in the application.

## 2.2 Language

The choice of implementation language for both the graphical user interface and the Ant Colony Optimisation algorithm is extremely important. The nature of the project suggests that an object-orientated approach would best suit as the implementation language. One of the main reasons for this is because the manipulation and use of objects in such languages allows for object-based decomposition allowing for more logical modules system wide when compared to a non-object-orientated approach. A non-object-orientated approach may be more subject to functional decomposition (the application is split into modules grouping similar functions rather than representing separate objects).

An object-orientated approach has been identified as most suitable. Therefore there are two main languages which are at the forefront of the selection process. These two languages are C# (*C Sharp*) and Java. Both languages have the potential to achieve a high level of success when applied to the projects problem however; they both have different consequences depending on the environment and their application. C++ (*C plus plus*) is another popular object-orientated language. C++ has been discounted due to lack of language experience therefore using a more familiar language such as the two specified above (Java and C#) is far more appropriate in this instance.

One of the major factors in deciding on the implementation language is the suitability of the languages features when applied to the projects problem including any external resources or compatible libraries. Both Java and C# are very similar at an abstract level in terms of provided

features by default. Both include everything that would be necessary to implement the proposed design for this application. Both languages provide the ability for objective decomposition and allow for polymorphic behaviours (multiple entities of different types using the same interface) which enables effective use of inheritance to allow multiple Agent variations (Ants in this case) to be supported easily.

C# has been created and is continually being developed by Microsoft and is focused around the .NET framework which is also a product of Microsoft. As C# is heavily Microsoft orientated its cross-platform capabilities are significantly reduced. The .NET framework(s) have only recently been open sourced so they lack full support on all platforms reduces the applications cross-platform reliability. This project is being developed with a focus on educational value; therefore cross-platform reliability is very important as maximisation of potential consumers is important (more people using the application implies more people are learning). A standard build will not be specified or assumed so there must be necessary measures in place to accommodate as many environments as possible. C# is heavily coupled with Windows based systems therefore; if C# were to be used there is a risk of alienating Macintosh and UNIX users. There are attempts to port .NET to other architectures (for example, Mono [16]) but the implementations of such approaches are not exact replicas of Microsoft .NET framework(s), therefore they cannot be relied upon. The use of Java would eliminate the cross-platform support issues as Java applications execute inside the Java Runtime Environment (JRE) which is available across most platforms and behaviours can be accurately modelled and predicted in the vast majority of cases.

Little differs between Java and C# in terms of feature presence (abstractly, how each language achieves each task is very different) thus, Java will be used for this project. The cross-platform constraints that come with the use of C# are not balanced by any necessary exclusive key features. As a result Java is the most appropriate language for the project, this all but ensures cross-platform reliability without sacrificing any important libraries or features.

## 2.3 Architecture

There have been considerations as to what key elements will be present in the composure of a suitable underlying architecture for the application. The architecture must accommodate both major elements of the application (graphical user interface and the Ant Colony Optimisation algorithm) in a manner that enables the best possible expansion/modification opportunities to accommodate any additional features or unforeseen changes. Selecting relevant Design Patterns will enable the above goals to become reality however; design patterns should be used respectfully and must present a general solution to a problem. The overuse or misuse of such patterns can cause significant complexity issues through the system, this needs to be avoided.

### 2.3.1 Design and Architectural Patterns

#### 2.3.1.1 Model-View-Controller

The Model-View-Controller (MVC) Architectural Pattern is designed to reduced coupling between system components, these are represented here as the user interface(s) (View) and the underlying data and its representation(s) (Model). The interaction(s) between the View and the Model “established using a subscribe and notify protocol” [8] (Controller). The Controller updates the View(s)

based on the model(s) current state or vice-versa however; The View(s) cannot directly communicate with the Model, the Controller must govern such interactions.

This project will make effective use of Model-View-Controller in order to produce an environment which is much easier to maintain and has little coupling between the Model and the View(s). This allows the Model(s) and/or View(s) to be substituted or modified in order allowing different representations of the current algorithm, or in fact different algorithms altogether.

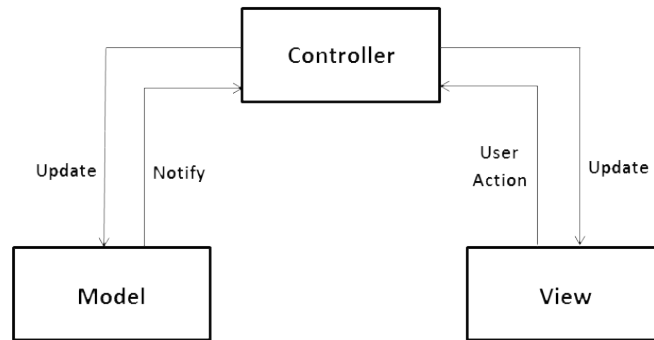


Figure B.1: Basic abstract overview of the Model-View-Controller pattern

- **Model** represents the underlying Ant Colony Optimisation algorithm. The Model also contains the required arithmetic functions and any additional operations required to execute the algorithm correctly.
- **View** represents the graphical user interface which will not only display the algorithms execution, but also enable the user(s) to modify the algorithms parameters.
- **Controller** represents the Observer required to enable interactions between the Model(s) and View(s).

### 2.3.2 Observer and Observable

The implementation of the Model-View-Controller design pattern is handled using the Observer and Observable interface provided as part of the default Java language specification. The general premise is that the Model will have an Observer which will have an update interface allowing it to receive signals from what it is observing (Model). The Model will implement the Observable interface which will enable it to send update signals to the Observer through the `notifyObservers()` method. This enables the Models dependencies to be updated as the Model itself changes ensuring the correct state of the Model is captured in the Views.

As figure B.2 demonstrates the View will Observe the Model and will wait for an update signal sent by the Model's `notifyObserver()` method. The Model can have multiple Observers using this pattern so there is the potential for future modification or enhancement without having to rework the existing system should the needs for extra views be needed.



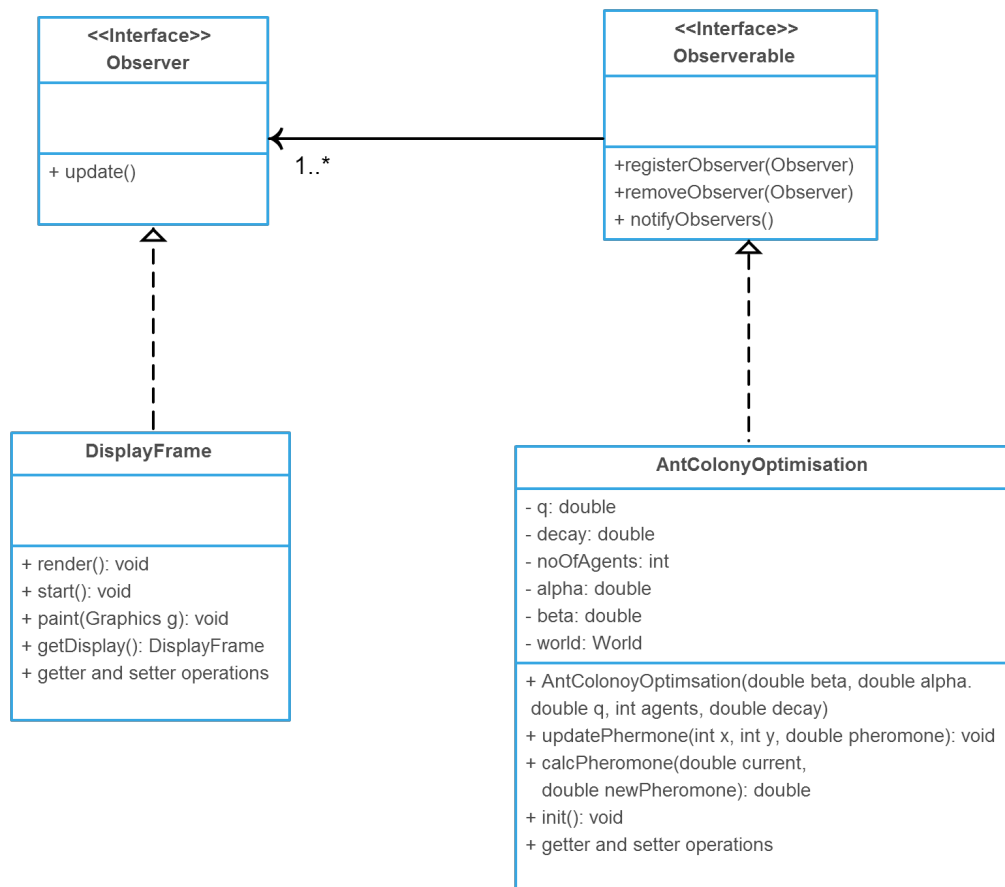


Figure B.2: Proposed implementation of the Observer and Observable Design pattern

### 2.3.2.1 Singleton

In order to maintain simplicity throughout the application the Singleton design pattern will be implemented for key objects where one and only one instance of an object must exist. The Singleton pattern prevents multiple instantiations of specific object(s) as the object itself is solely responsible for tracking the currently instantiated instance of itself [7].

The application will consist of a graphical user interface which in turn, will be composed of several different components. Such components must only be instantiated once in order to ensure correct interactions are performed. Without the presence of the Singleton pattern there exists the possibility of multiple instances of such components which could potentially cause unforeseen complications and undefined behaviours.

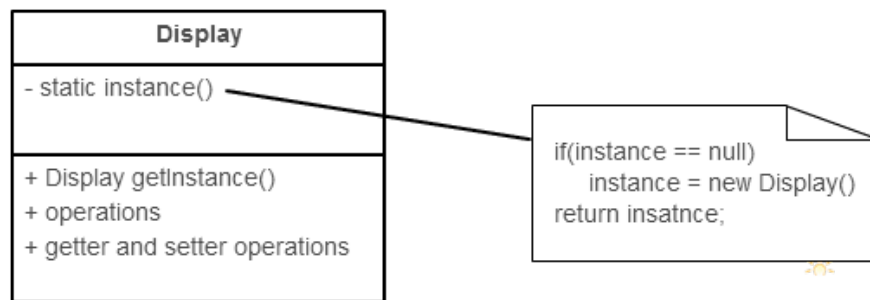


Figure B.3: Proposed high-level implementation of the Singleton pattern demonstrating how the sole instance of the graphical user interface will be tracked.

### 2.3.3 Structure

Adhering to the concepts of the patterns described in sections 2.3.1.1 and 2.3.2.1 the following class diagram shows proposed application structure. This is not concrete and could potentially change throughout development, the class diagram in question is represented below by figure B.4 and is represented using standard UML notation.

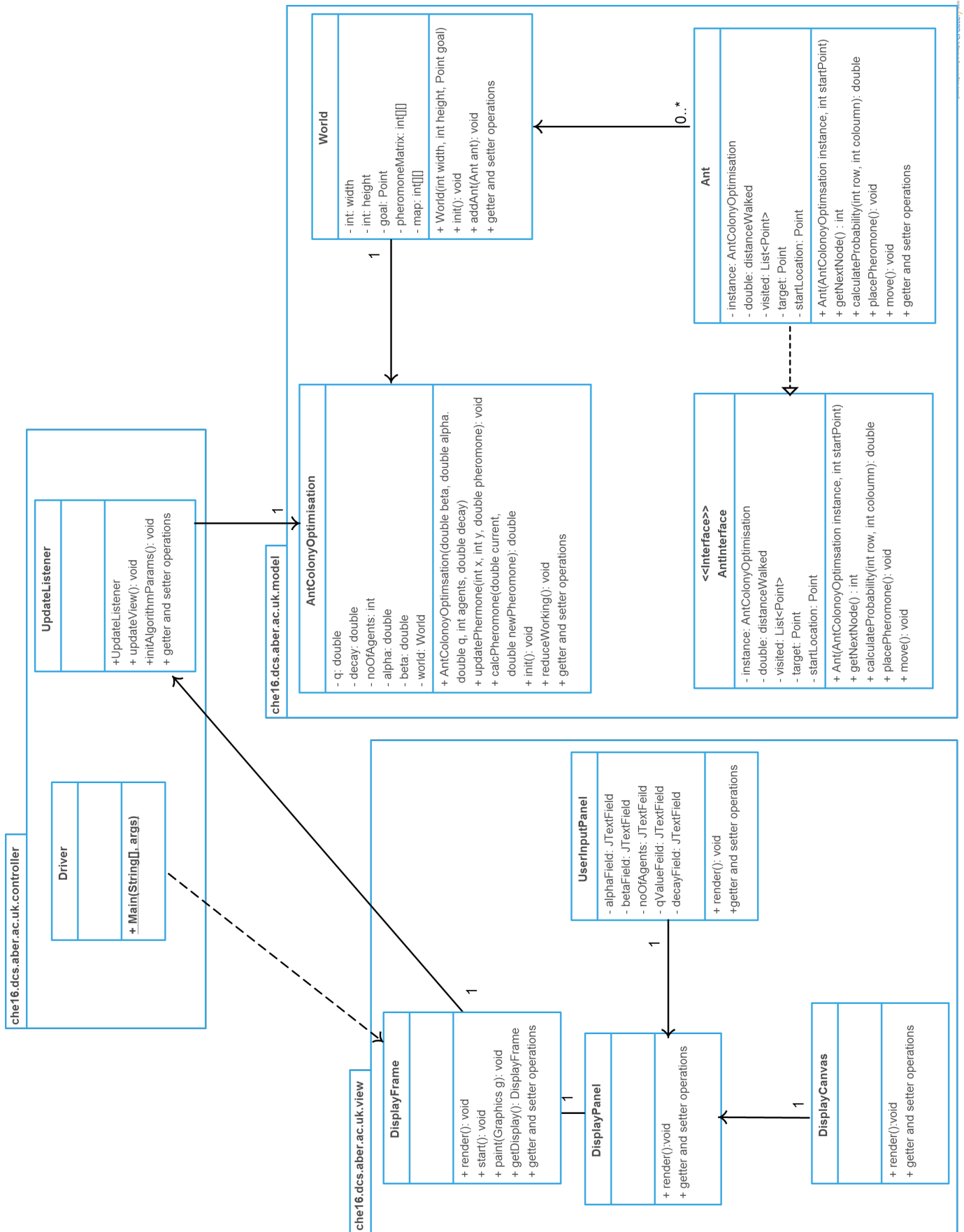


Figure B.4: Initial Class Diagram representing the main modules, packages and system interactions using UML notation.

### 2.3.3.1 View Package

The *che16.dcs.aber.ac.uk.view* package contains the graphical user interface components. The main concept behind this is the use of nested components such as JPanel, JTextFields and the like. These will be contained inside top level JFrame. This allows modification of each component in isolation without impacting the other components behaviours and/or elements. This is the first module of the application which is initialised, and is done so directly from the *main* method. This package has no direct knowledge of any package members mentioned in 2.3.3.2. Instead the *che16.dcs.aber.ac.uk.controller* package members handle the communication(s) between the model(s) and view(s), adhering to the principles discussed in section 2.3.1.1.

### 2.3.3.2 Model Package

The *che16.dcs.aber.ac.uk.model* package contains the necessary elements and attributes required in order to accurately represent the algorithms state(s) and ensure correct algorithm execution. This package has no direct knowledge of any package members mentioned in 2.3.3.1. Instead the controller package members handle the communication(s) between these the model(s) and view(s), adhering to the principles discussed in section 2.3.1.1.

### 2.3.3.3 Controller Package

The initial concept for the controller is basic and will grow in complexity during the development lifecycle as more and more control based mechanisms will become prevalent. This initial concept is a simple Observer which notifies the view(s) should the model change in a significant way; the inverse of this is also true.

## 2.4 Class Descriptions

The Classes defined in Figure B.4 are described textually below.

### 2.4.1 Controller

#### 2.4.1.1 Driver

The Driver class is fairly simplistic and exists as an entry point to the application. This will class handles any necessary instantiations and correctly assigns any key associations.

#### 2.4.1.2 UpdateListener

The UpdateListener class serves as a point of control for the update operations. The main updates will be handled internally by the relevant classes (as described by Figure B.2) however, this class will handle the updates caused when a user interacts with the application through the user interface. This includes, but is not limited to the modification of parameters or starting the algorithm's execution.

## **2.4.2 View**

### **2.4.2.1 DisplayFrame**

An instance of the DisplayFrame class will serve as the highest level container for the applications user interface elements. This class will be responsible for controlling access to, and the instantiation of the other graphical user interface elements.

### **2.4.2.2 DisplayPanel**

The DisplayPanel instance will be contained inside the DisplayFrame. The purpose of the DisplayPanel is to contain the DisplayCanvas. The reason this class is used to contain the DisplayCanvas rather than using the top level DisplayFrame is because it gives the author much more control over dimensions and modification of layouts or contents.

### **2.4.2.3 DisplayCanvas**

The DisplayCanvas will be used to display the algorithms execution. This is the user interface element which will be painted and modified during the course of the algorithms execution.

### **2.4.2.4 UserInputPanel**

The UserInputPanel is used to represent the collection of text boxes and buttons which will be used by the user to directly modify the algorithms parameters and state of execution. This will be contained in the top level DisplayFrame.

## **2.4.3 Model**

### **2.4.3.1 AntColonyOptimisation**

The AntColonyOptimisation class is used to represent the high level behaviours of Ant Colony algorithms. This class will contain the current instance of the World as well as housing all relevant data such as current parameter values and ways to interact with such parameters (getters).

### **2.4.3.2 Ant Interface**

This interface will contain the necessary methods that every type of Ant (agent) has to have. This is by no means concrete, if there is only a need for one type of Ant then an interface is not strictly needed thus, it may be removed to reduce complexity.

### **2.4.3.3 Ant**

An instance of the Ant class will be used to represent an Ant (agent) in the world. As these are the agents which will be deployed on the world they will need to know about the World, whilst also

knowing information about themselves including where they have visited so far and how far have they travelled. This class will also contain the operations necessary in order for an Ant to be able to solve the current problem, this is main down the combination of knowing about the World and necessary details inside the move() method which will be used to select the Ants next location.

#### **2.4.3.4 World**

The World class is a representation of the current problem. This includes all information needed to model the graph and manipulating the current pheromone. The World will be in constant communication with the Ant instances in order to communicate the current state of World to each agent.

## **2.5 Interface Design**

### **2.5.1 Main User Interface**

The interface design must accommodate all the necessary elements required to allow user defined values for each of the algorithm parameters. The interface must also be able to visually represent the current algorithms state including the locations of the agents and nodes without impacting on the usability of the application (the interface must not freeze or be negatively affected by the algorithms execution).

The interface will use a very neutral colour scheme which will maximise the usability and reduce the risk of complications which may arise from users being subject to difficulties understanding or identifying certain colours. Every option for the user will be textually defined and will not rely on any sound or visual prompts in order to use. As a result in addition to the above, users with visual impairments will still be able to use the application as intended.

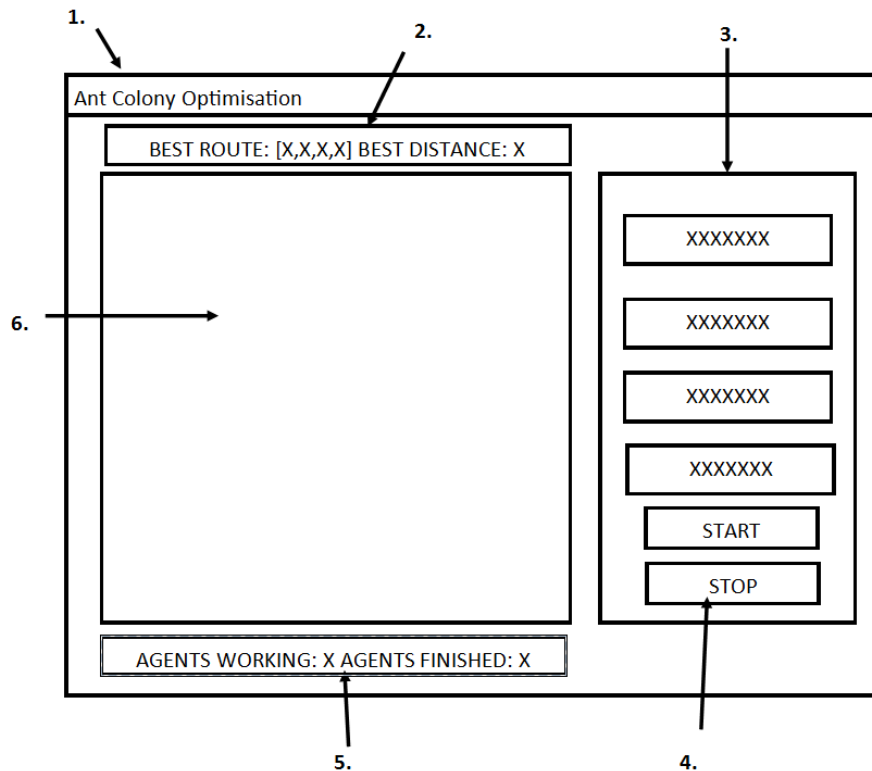


Figure B.5: Proposed design for the graphical user interface, showing the key elements in their planned locations.

**1.** in figure B.5 refers to the containing frame which will house the reset of the interface elements. This frame will not be resizable preventing complications such as the dynamic resizing of the interface having an impact on the observable range of the world. **2.** refers to a text view containing information relevant to the algorithms current state of execution. This text view will contain the current best distance as well as the order of nodes visited to traverse the current best path. This will only be populated during the algorithms execution and only if the best path has been initialised. **3.** refers to container which houses the interactive elements relating to the modification of the algorithms parameters. This will consist of several labels and text fields which can be modified informing the user of what they will be modifying as well as providing suitable error messages if the users enters an incorrect value for any of the parameters. **4.** refers to the start and stop buttons. These are here to conform to the expectation that a user expects a clear way to start and stop the application at their convenience, this is the simplest way to do this and requires no hidden menus or hidden key bindings. **5.** refers to a text view containing information relevant to the algorithms current state of execution. This text view will contain the number of agents currently working (which means the number of agents who haven't met their own stop conditions) as well as displaying the number of agents which are finished. **6.** refers to the main canvas area which will display the algorithms current state of execution to the user. The contents of this will reflect the user defined values (elements in: **3.**) as well as representing each agents current location, their movements between nodes and also the modelling of pheromone deposit and decay will be present in this canvas.

### 2.5.2 Error Message Feedback

As the Algorithm parameters will be user defined using the interface proposed in figure B.5 there must be measures in place to catch and inform the user of any illegal values. Not only must the user be told they have inputted illegal values the illegal parameter value will be identified and a range of legal values will be displayed to the user.

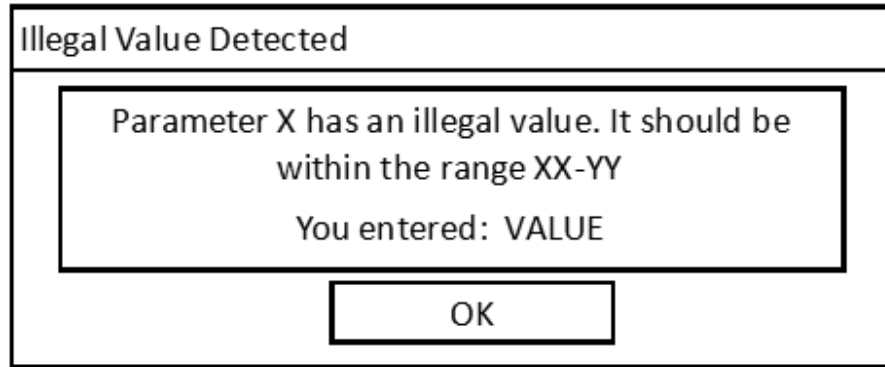


Figure B.6: Proposed design for the illegal parameter error message displayed to the user

As represented in figure B.6 the error message will contain all the information a user needs to identify the problem with their data input. The X value in figure B.6 represents which parameter has the illegal data input (i.e. Alpha, Beta). Range XX-YY represents the legal values for said parameter, and VALUE represents the value the user has specified for this parameter. The combination of these will provide the user with the knowledge of why this error message is being displayed and how they can resolve their issue.

This kind of error message will be composed using the `JOptionPane` and `JDialog` interfaces provided as default by the Java language specification. These views are very customisable and the styling will be handled by the languages underlying protocols which will reduce the codes complexity.

## 2.6 Algorithm

There are several adaptations of the Ant Colony Optimisation algorithm. Initially the project contain an implementation of Ant Colony Optimisation in its simplest form, without the presence of any enhancements such as using *Elitist Agents* or similar. Once a working implementation is in place the next step will be to adapt the algorithm in various ways to further aid the teaching potential of the project.

The general premise is that each Agent (Ant) embarks and a pseudo random walk through the state space. The Agents movements are influenced by pheromone deposits placed on edges between vertices. This pheromone is deposited by other Agents in accordance with the equations stated in section 2.6.2.2. The Agent's next move is influenced by the result of the equation stated in section 2.6.2.1. However; there is still the probability of the Agent moving to a less attractive point so the Agent does not always travel to the strongest pheromone concentration.

Overtime the pheromone deposit concentration on  $edge_{xy}$  is directly proportional to the quality



of the candidate solution, and ultimately the ants will converge to find the shorted route between two or more points.

There are several algorithm requirements;

- **Suitable problem representation** the World and Agents must be represented in a suitable and logical manner allowing the algorithm to execute as expected.
- **Pheromone manipulation metrics** there must exists adequate ways to access the pheromone matrix as well as manipulate (deposit/remove) the concentration of pheromone on a given edge in order to model decay and deposits.
- **Probabilistic movement functions** there must exist functions that calculate the probability of the Agent moving to a specific vertex. This is based on the pheromone concentration and the Agents location (see section 2.6.2.1).

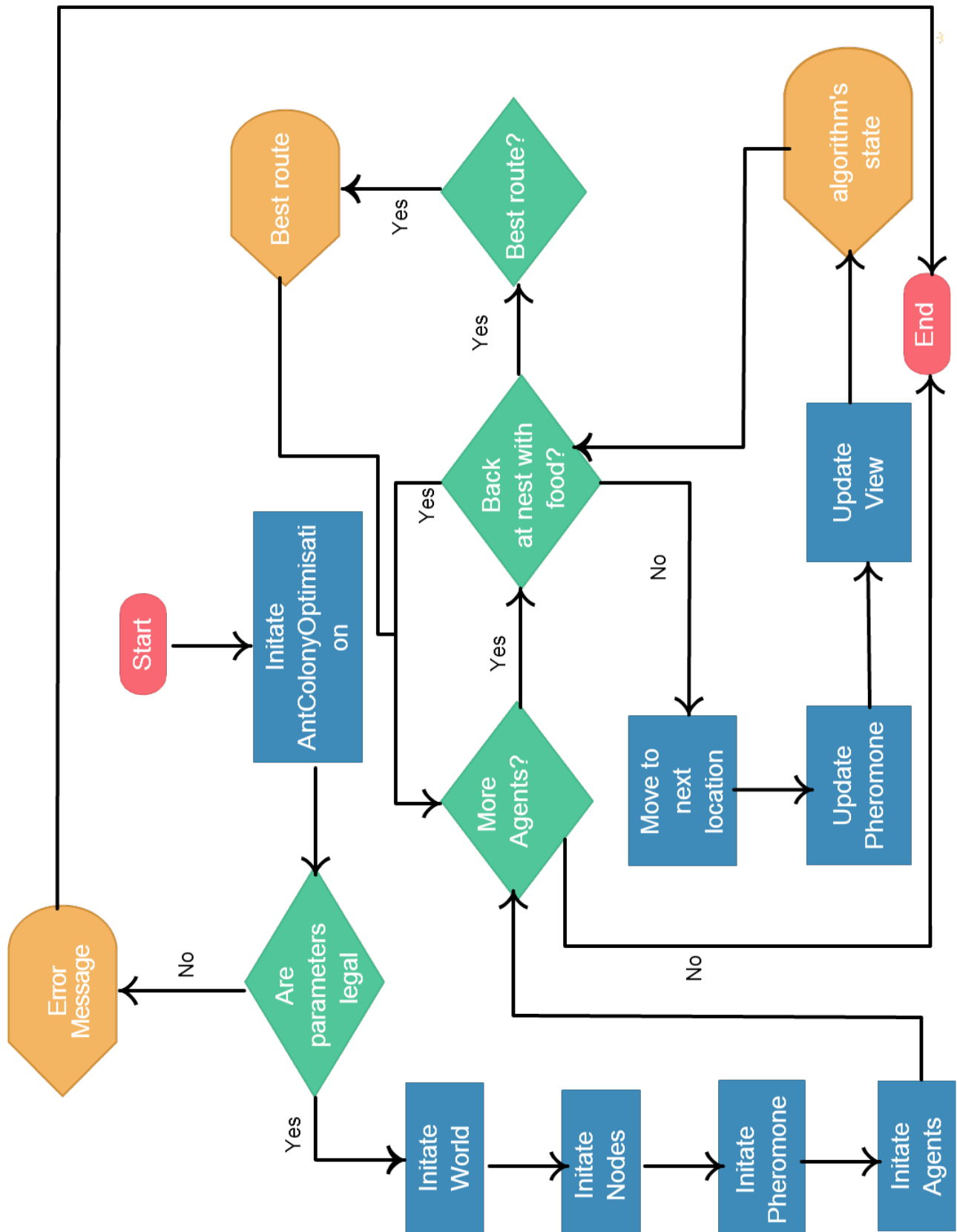


Figure B.7: High level flow diagram representing the pseudo code for Algorithm 5, section 2.6.1

### 2.6.1 Pseudo-code

---

**Algorithm 5** Pseudo-code for Ant Colony Optimisation
 

---

```

1: Initiate AntColonyOptimisation with defined parameters
2: if !parameters are legal then
3:   Display error message to user
4:   return
5: Initiate World with algorithm parameters
6: Initiate Nodes and graph
7: Initiate pheromone values
8: Initiate Agents
9: while !all agents finished do
10:  for all Agents do
11:    while !back at nest with food do
12:      Calculate next move using probabilistic function
13:      Add moved point to Agent's memory
14:      Calculate and deposit pheromone on the path
15:      Update the View
16:    end while
17:  end for
18: if local best solution < global best solution then
19:   globalbest = local best solution
20: end if
21: end while
22: output global best solution

```

---

Above is a somewhat simplified pseudo-code representation of the proposed Ant Colony Optimisation algorithm. The mathematical formulae required to achieve steps 7 and 10 are shown in section 2.6.2. The final algorithm may differ from the above depending on any additional feature present in the final release.

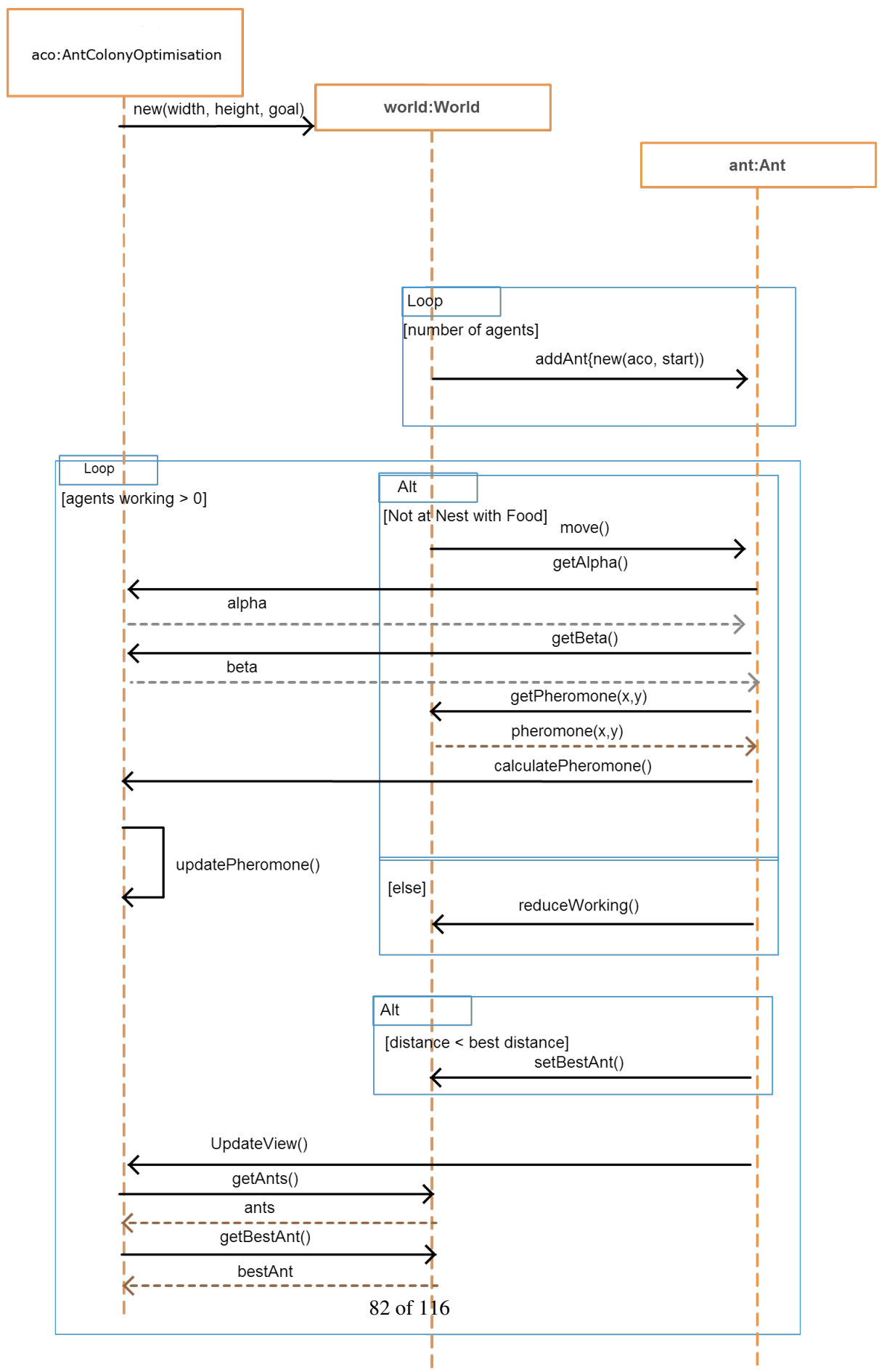


Figure B.8: Sequence diagram representing Algorithm 5, section 2.6.1

The sequence diagram shown in figure B.8 shows the high level interaction between the proposed main Model classes during the algorithms execution. The Ants are in constant communication with the AntColonyOptimisation and World instances during their movement through the graph to ensure the correct pheromone values are being parsed during the movement process. The View is also updated through the `updateView()` method in the AntColonyOptimisation instance which requires data about the current Ants and the current best Ant. This data is stored in and returned from the World instance.

## 2.6.2 Metrics

### 2.6.2.1 Probabilistic function

$$p_{xy}^k = \frac{(\tau_{xy}^\alpha)(\eta_{xy}^\beta)}{\sum (\tau_{xy}^\alpha)(\eta_{xy}^\beta)} \quad (1)$$

Figure B.9: Algebraic model of the probabilistic function used to calculate next move for any Agent [26]

The probability that an Agent moves to vertex  $xy$  is described using the above.  $p$  is the probability for any Agent  $k$  to move through vertex  $xy$ .  $\tau$  is the amount of pheromone deposited on vertex  $xy$ , which is raised to the exponent  $\alpha$ .  $\alpha$  is an heuristic value representing how greedy the algorithm is in its path finding [22]. The result for  $\tau_{xy}^\alpha$  is then multiplied by the edge  $xy$ 's evaluation( $\eta$ ). Generally  $\eta$  will be represented using  $\frac{1}{\text{Euclidean distance}_{xy}}$  [22] [20]. This will then be raised to the exponent  $\beta$  which like  $\alpha$  is an heuristic parameter however  $\beta$  describes the Agents path finding speed.  $\sum (\tau_{xy}^\alpha)(\eta_{xy}^\beta)$  is the sum of all possible solutions.

---

**Algorithm 6** Pseudo-code for Probabilistic function - Each Agent - figure B.9

---

- 1: read the *pheromone* level for vertex  $xy$
  - 2: raise the value from 1: to the exponent  $\alpha$
  - 3: Multiply the result of 2: by  $(\text{inverted distance}_{xy})^\beta$
  - 4: initiate a temporary double *columnTotal*
  - 5: **for all** non-visited vertex **do**
  - 6:      $\text{columnTotal} += (\text{read the pheromone level for vertex } xy)^\alpha \times (\text{inverted distance}_{xy})^\beta$
  - 7: **end for**
  - 8: divide the result of 3 : by the result of 5 : - 7 :
- 

### 2.6.2.2 Pheromone deposit

$$p_{xy}^k = (1 - \rho)\tau_{xy}^k + \Delta\tau_{xy}^k \quad (2)$$

Figure B.10: Algebraic model of the pheromone deposit function used to calculate the correct values for the pheromone matrix [27]

$\tau$  represents the pheromone deposit for an edge  $xy$  by Agent  $k$  [22].  $\rho$  is a value between 0 – 1 which represents the decay rate *decay*.  $1 - \rho$  is multiplied by the existing amount of pheromone at  $edge_{xy}$  to correctly account for decaying trails. The new amount of pheromone is then added using the equation from figure B.11.

$$\Delta\tau_{xy}^k = \begin{cases} Q/L_k & \text{if Agent } k \text{ uses curve } xy \text{ in its tour} \\ 0 & \text{otherwise} \end{cases} \quad (3)$$

Figure B.11: Algebraic model of the function used to calculate the how much new pheromone is deposited at  $xy$  [25]. Pheromone is only updated if the Agent  $k$  has visited point  $xy$ .

figure B.11 represents the new amount of pheromone to be added to the existing concentration at  $edge_{xy}$ . This can be read as change in  $\tau$  ( $\Delta\tau$ ).  $Q$  is simply another heuristic parameter which is divided by the distance *agentk* travelled to get to  $edge_{xy}$ . If the result of this is  $\leq 0$  return 0. This ensures that new *pheromone* is only added to the existing concentration at  $edge_{xy}$  is used by *agentk* in its tour.

---

**Algorithm 7** Pseudo-code for Pheromone function - figures B.10, B.11

---

```

1: if pheromoneDeposit = Q value/totalDistanceWalked ; 0 then
2:   pheromoneDeposit = 0
3: pheromonexy = (1 - algorithm decay rate) × currentPheromonexy +
   pheromoneDeposit
4: if pheromonexy ≥ 0 then
5:   pheromoneMatrixxy = pheromonexy
6: else
7:   pheromoneMatrixxy = 0
8: end if

```

---

## 2.7 Representation

### 2.7.1 World

The World class is used to model the graph that the Ants will traverse during the algorithms execution. The graph will be represented as a two-dimensional Array, with each element in said array representing a node in the graph itself. The two dimensional array will be composed of integer values with each element containing an integer value representing the terrain type at this index, this will also be used to set the nest and food locations.

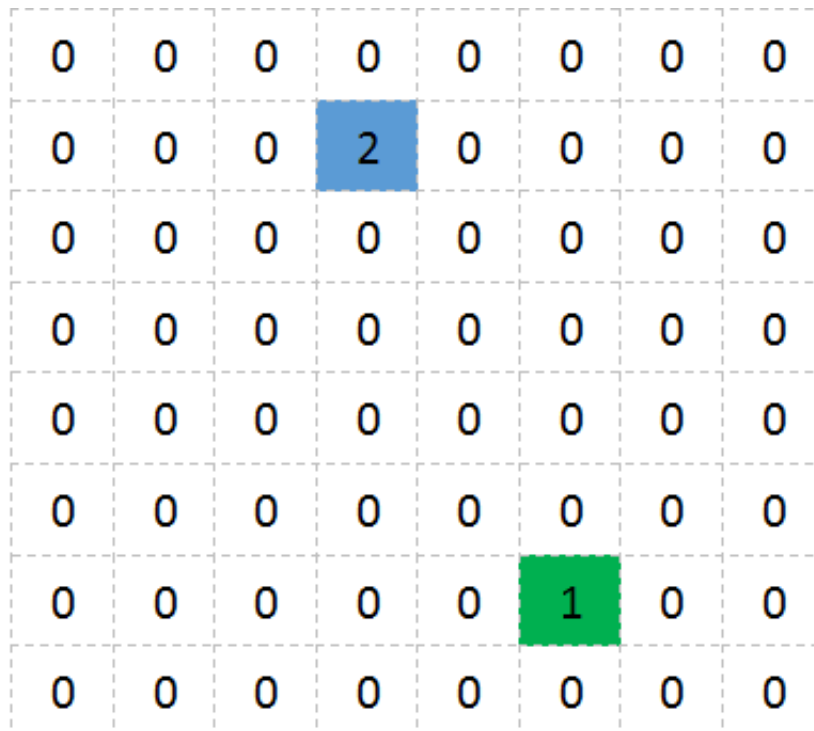


Figure B.12: Example World representation using a two-dimensional Integer Array

Figure B.12 shows how the proposed graph representation would be implemented. A '0' value represents normal terrain where the Ants can move to, '1' represents the nest location where the Ants will start and '2' represents the food location which is the initial target for the Ants. This is a simplistic way to model an environment for the Ants whilst also allowing a multitude of terrain options without having to modify the way the graph is stored.

### 2.7.2 Pheromone

The pheromone must be modelled in a way which is both easily accessible and modifiable. The data structure used to store the pheromone must also relate to the graph mentioned in 2.7.1 to allow for logical mapping between the representation of the Ants environment and the pheromone associated with each node in the graph. The pheromone will be stored as a two-dimensional Array of Doubles. Each element in the Array will represent the pheromone concentration for the corresponding Node in the graph for example, the double value at `pheromone[x][y]` will represent the pheromone concentration on edge `[x][y]` in the graph, thus there is a logical link between the two representations.

0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5
0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5
0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5
0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5
0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5
0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5
0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5
0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5

Figure B.13: Example Pheromone representation using a two-dimensional Double Array with default initial values

Figure B.13 demonstrates how a two-dimensional Double array can be effectively used to model the pheromone values for every node in the graph. The values in this figure are default initial values which will be user defined when the application is executed. As the Ants move through the graph the pheromone values at each index will correctly model the pheromone operations mentioned in section 2.6.2.2. As the values are stored in an array accessing or modifying the values is extremely simple and involves a simple getter or setter operation.

### 2.7.3 Visualisation

The data structures described in sections 2.7.1 and 2.7.2 must be visualised to the user in a manner that anybody can understand. Given that the graph will be stored as a two-dimension array it is perfectly logical to display this graph to the user in a grid format similar to that shown in figure B.12. The challenge with the visualisation process is visualising the pheromone deposit and decay operations as well as displaying the Ants moving between Nodes.

Given that the pheromone is stored in a two-dimensional array of doubles and the fact that accessing these values is extremely simple the value at each index can be used to directly influence how the user sees the pheromone. If each cell in the grid is coloured, and this colour's opacity is directly representational of the value at the corresponding index in the pheromone matrix then it becomes an accurate way of displaying the values of the pheromone to the user, which also allows the decay and deposit operations to be shown.



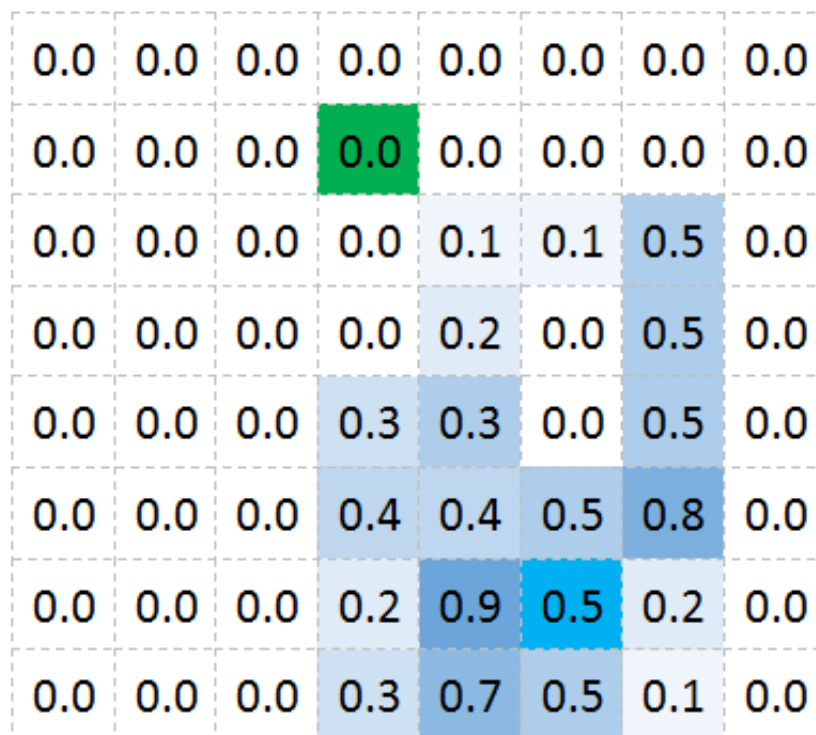


Figure B.14: Example Pheromone visualisation using the suggested visualisation method

Figure B.14 shows how the pheromone value for a given (x,y) co-ordinate has a direct influence on the opacity of the cells colour. In said figure the pheromone value at each index is multiplied by 100 to convert it to a percentage, which then becomes the opacity value for the given Node. However, if the pheromone values for each Node become extremely small during execution there must be a measure in place to covert the small values back into percentages using a larger scaling factor than 100.

## Appendix C

# Implemented Code

---

```
pheromone = new Pheromone[cities.size()][cities.size()];
for(int i = 0; i < pheromone.length; i++){
    for(int j = 0; j < pheromone[0].length; j++){
        pheromone[i][j] = new Pheromone(aco.getInitialPheromone());
    }
}
```

---

Figure C.1: Snippet of code used to initialise the pheromone Matrix. *cities* is a list of *City* objects. *aco* is the instance of the *AntColonyOptimisation* Class

---

```
distanceMatrix = new double[cities.size()][cities.size()];
for(int i = 0; i < distanceMatrix.length; i++){
    for(int j = 0; j < distanceMatrix[0].length; j++){
        distanceMatrix[i][j] =
            Globals.calculateEuclidianDistance(cities.get(i).getX(),
            cities.get(i).getY(), cities.get(j).getX(),
            cities.get(j).getY());
    }
}
```

---

Figure C.2: Snippet of code used to initialise the distance Matrix. *cities* is a list of *City* objects.

---

```

invertedMatrix = new
    double[distanceMatrix.length][distanceMatrix[0].length];
for(int i = 0; i < distanceMatrix.length; i++){
    for(int j = 0; j < distanceMatrix[0].length; j++){
        invertedMatrix[i][j] = invertValue(distanceMatrix[i][j]);
    }
}

```

---

Figure C.3: Snippet of code used to initialise the inverted distance Matrix. *cities* is a list of *City* objects. *invertValue**distanceMatrix[i][j]* returns  $\frac{1}{\text{distanceMatrix}[i][j]}$

---

```

cities = new ArrayList<City>();
Random r = new Random();
for(int i = 0; i < numberOfCities; i++){
    // the (+1) is to stop cities having the index '0' which would
    // cause them to half render out of view
    int x = r.nextInt(aco.getBoundaryX()) + 1;
    int y = r.nextInt(aco.getBoundaryY()) + 1;
    //make sure 2 cities can't spawn on top of each other
    for(City city: cities){
        if(x == city.getX() && y == city.getY()){
            x = r.nextInt(aco.getBoundaryX()) + 1;
            y = r.nextInt(aco.getBoundaryY()) + 1;
        }
    }
    cities.add(new City(x,y,i));
}

```

---

Figure C.4: Snippet of code used to initialise the collection of *City* objects.

---

```

Random r = new Random();
ants = new ArrayList<Ant>(numberOfAnts);
for(int i = 0; i < numberOfAnts; i++){
    int index = r.nextInt(cities.size());
    for(City c: cities){
        if(index == c.getIndex()){
            c.adjustAntsHere(1);
            break;
        }
    }
    ants.add(new Ant(this, index));
}

```

---

Figure C.5: Snippet of code used to initialise the collection of *Ant* objects. *this* refers to the current *World* Object.

---

```
for(int i = 0; i < pheromone.length; i++){
    for(int j = 0; j < pheromone[0].length; j++){
        updatePheromone(i, j, pheromone[i][j].getNewPhero());
        //reset the new phero values
        pheromone[i][j].resetNewPhero();
    }
}

public void updatePheromone(int x, int y, double newPheromone) {
    double phero =
        calculatePheromones(pheromone[x][y].getPheromoneValue(),
            newPheromone);
    //if phero is not negative then update the current concentration
    //if phero is negative then just set it as 0, you can't have
    //negative phero on an edge
    if (phero >= 0.0d) {
        pheromone[x][y].setPheromoneValue(phero);
    } else {
        pheromone[x][y].setPheromoneValue(0.0d);
    }
}

public double calculatePheromones(double current, double newPheromone)
{
    //we dont need to store the result in a temporary variable, just
    //return the equation in place
    return ((1 - aco.getDecayRate()) * current + newPheromone);
}
```

---

Figure C.6: Snippet of code used to update the pheromone values for every edge. *aco* is the current instance of the *AntColonyOptimisation* Class.

---

```

public final int getNextProbableNode(int y) {
    //This is an adapted version of a similar method provided by Thomas
    Jungblut found here: https://code.google.com/p/antcolonyopt/
    //create a location to store the probability for all next locations
    //this can then be easily accessed to return the next index for the
    ant's move
    //only do this if there is in fact locations to move to
    if (unvisited > 0) {
        int danglingUnvisited = -1;
        final double[] weights = new double[visited.length];
        double columnSum = 0.0d;
        for (int i = 0; i < visited.length; i++) {
            columnSum += calculateIndividualProbability(y, i);
        }
        //once we have the value for sum (which the sum off all solutions
        evaluation)
        double sum = 0.0d;
        for (int x = 0; x < visited.length; x++) {
            if (!visited[x]) {
                weights[x] = calculateTotalProbability(x, y, columnSum);
                sum += weights[x];
                danglingUnvisited = x;
            }
        }
        //if sum is 0 then return, as this will be used in a division it
        cannot be zero
        if (sum == 0.0d)
            return danglingUnvisited;
        /* We need to give each index of the probability weighting based
        on the result of calculateToalProbability
        * this result is then divided by the total sum of all
        probabilities (usually 1)
        * The result of this division is then put in the correct index
        in the matrix in order to get the probability weighting
        *
        */
        double pSum = 0.0d;
        for (int i = 0; i < visited.length; i++) {
            pSum += weights[i] / sum;
            weights[i] = pSum;
        }
        //nextDouble returns a value between 0 and 1, so this can be used
        to effectively select a 'random' index based on the weighted
        probability
        //provided virtually as is by Thomas Jungblut:
        https://code.google.com/p/antcolonyopt/
        //this is what makes the ant walk 'randomly'
        final double r = random.nextDouble();
        for (int i = 0; i < visited.length; i++) {
            if (!visited[i]) {
                if (r <= weights[i]) {
                    return i;
                }
            }
        }
    }
    return -1;
}

```

---

Figure C.7: Snippet of code used to select the Ants next location. This is a modifiedf version of the code provided by Thomas Jungblut [22]

---

```
boolean reset = false;
for(int i = 0; i < iterations; i++){
    aco.setCurrentIteration(i);
    if(aco.getRunning()){
        ArrayList<Ant> ants = (ArrayList<Ant>)aco.getWorld().getAnts();
        antsWorking = aco.getNoOfAgents();
        if(reset){
            //for the next iteration re-init the ants and go again
            for(City c: aco.getWorld().getCities()){
                c.resetAntCount();
            }
            aco.getWorld().initAnts();
            ants = (ArrayList<Ant>)aco.getWorld().getAnts();
            reset = false;
        }
        while(antsWorking > 0){
            for(Ant ant: ants){
                if(!aco.getRunning()){
                    return null;
                }
                if(!ant.getFinished()){
                    ant.move();
                    aco.reduceWorking();
                }else{
                    //if an ants is finished, decrease the counter
                    antsWorking--;
                }
            }
            aco.getWorld().decayPhero();
        }
        reset = true;
    }
}
```

---

Figure C.8: Snippet of code used to automatically execute the algorithm until completion. *aco* is the current instance of the *AntColonyOptimisation* Class.

---

```

stepIndex = 0;
if(currentIter < iterations){
    running = true;
    Ant ant = world.getAnts().get(stepIndex);
    if(!ant.getFinished()){
        ant.step();
        this.notifyCanvas();
        if(ant.getUnvisted() == 0){
            ant.setFinished(true);
        }
        else{
            reduceWorking();
            stepIndex++;
        }
        if(stepIndex >= world.getAnts().size()){
            //reset the ants and index
            world.initAnts();
            for(City c: world.getCities()){
                c.resetAntCount();
            }
            stepIndex = 0;
            agentsWorking = noOfAgents;
            currentIter++;
        }
    }
}

```

---

Figure C.9: Snippet of code used to execute the algorithm on a step by step basis

---

```

public static double linearInterpolateX(double x1, double x2, double
    mu) {
    return(x1*(1-mu)+x2*mu);
}

public static double linearInterpolateY(double y1, double y2, double
    mu) {
    return(y1*(1-mu)+y2*mu);
}

```

---

Figure C.10: Snippet of code determine the cordinate values for both  $x$  and  $y$  for a given  $\mu$  value.

---

```

City start = null;
City destination = null;
for(Ant ant: agents){
    if(!ant.getFinished()){
        for(City c: cities){
            if(ant.getCurrentIndex() == c.getIndex()){
                if(antImage != null){
                    g2.drawImage(antImage, (c.getX() * 20) - 15, (c.getY() *
                        20) - 9, null);
                }else{
                    g2.setColor(Color.GREEN);
                    g2.fillOval((c.getX() * 20) - 5, (c.getY() * 20) - 5,
                        10, 10);
                }
            }
        }
        if(ant.getMovementTracker()[0] !=
            ant.getMovementTracker()[1]){
            if(c.getIndex() == ant.getMovementTracker()[0]){
                start = c;
            }
            if(c.getIndex() == ant.getMovementTracker()[1]){
                destination = c;
            }
        }
        if(start != null && destination != null){
            g2.setColor(Color.CYAN);
            for(int i = 1; i < 5; i++){
                //cast to a double to stop integer behaviours rounding
                //down to 0
                double result = ((double)i)/5;
                //draw an ellipse2D every 1/5 the way along the line
                float y = (float)
                    (Globals.linearInterpolateY(start.getY(),
                        destination.getY(), result));
                float x = (float)
                    (Globals.linearInterpolateY(start.getX(),
                        destination.getX(), result));
                Ellipse2D movement = new Ellipse2D.Float((x * 20.0f) -
                    5, (y * 20.0f) - 5, 10, 10);
                g2.fill(movement);
                g2.draw(movement);
            }
        }
    }
}
//reset the values
start = null;
destination = null;

```

---

Figure C.11: Snippet of code used to visualise an Ants movement. *g2* is an instance of *Graphics2D*.



---

```

bestRoute = model.getWorld().getBestRoute();
if(bestRoute != null){
    for(int i = 0; i < bestRoute.size(); i++){
        for(City c: cities){
            if(bestRoute.get(i) == c.getIndex()){
                if(i + 1 < bestRoute.size()){
                    for(City c2: cities){
                        if(bestRoute.get(i + 1) == c2.getIndex()){
                            g2.setColor(Color.RED);
                            //make the best line slightly thicker than the rest
                            //so it stands out more
                            g2.setStroke(new BasicStroke(2));
                            g2.drawLine(c.getX() * 20, c.getY()*20, c2.getX() *
                                20, c2.getY() * 20);
                        }
                    }
                }
            }
        }
    }
}

```

---

Figure C.12: Snippet of code used to display the best route to the user.

---

```

for(EliteAntData data: eliteAnts){
    System.out.println(data.getEliteRoute());
    best = data.getEliteRoute();
    double e = (1/4) * numberOfCities;
    for(int i = 0; i < best.size(); i++){
        if(i + 1 < best.size()){
            pheromone[best.get(i)][best.get(i+1)].addToNewPhero
            (pheromone[best.get(i)][best.get(i+1)].getNewPhero() + e);
        }
    }
}

```

---

Figure C.13: Snippet of code used to deposit pheromone along the elite routes. An *EliteAntData* Object is used to represent an Elite route

---

```
Random r = new Random();
while(numberOfUphill > 0){
    int index = r.nextInt(cities.size());
    City temp = cities.get(index);
    index = r.nextInt(cities.size());
    if(!(temp.getUphilRoutes().contains(index)) && (index !=
        temp.getIndex())){
        temp.addToUphil(index);
        numberOfUphill--;
        distanceMatrix[temp.getIndex()][index] =
            (distanceMatrix[temp.getIndex()][index] * 2);
        invertedMatrix[temp.getIndex()][index] =
            1/distanceMatrix[temp.getIndex()][index];
    }
}
```

---

Figure C.14: Snippet of code used to generate uphill paths.

## Appendix D

# Testing

### 4.1 Test Code Examples

The test cases shown in this chapter are not fully representative of every application test, only a selection of code examples has been included.

---

```
@Test
public void testValidationRulesAllowLegalAlphaValues() {
    double[] values = new double[]{2.5, -2.1, 4.999999999,
        -4.999999999, 4, -2, -1.65, 5, -5, 3, -3.21};
    for(int i = 0; i < values.length; i++){
        assertTrue("validaite should return true alpha is legal",
            aco.validate(values[i], 2.5, 0.2, 0.2, 10, 15, 3, 3));
    }
}
```

---

Figure D.1: Code representing the automated testing process for checking mutliple alpha parameter values.

---

```
@Test
public void testValidationRulesAllowLegalBetaValues() {
    double[] values = new double[]{2.5, -2.1, 4.999999999,
        -4.999999999, 4, -2, -1.65, 5, -5, 3, -3.21};
    for(int i = 0; i < values.length; i++){
        assertTrue("validaite should return true Beta is legal",
            aco.validate(2, values[i], 0.2, 0.2, 10, 15, 3, 3));
    }
}
```

---

Figure D.2: Code representing the automated testing process for checking mutliple beta parameter values.

---

```
@Test
public void testValidationRulesAllowLegalAgentsValues() {
    int[] values = new int[]{25, 13, 19, 48, 29, 23, 11, 8, 2, 33, 40,
        39, 6};
    for(int i = 0; i < values.length; i++){
        assertTrue("validaite should return true number of agents is
            legal", aco.validate(2, 2.5, 0.2, 0.2, values[i], 15, 3, 3));
    }
}

@Test
public void testValidationRulesShouldNotAllowIllegalAgentsValues() {
    int[] values = new int[]{-1, -12, 55, 100, 87, 69, 52, 99, -72,
        -12, -5, 58, 60};
    for(int i = 0; i < values.length; i++){
        assertFalse("validaite should return true number of agents is
            illegal", aco.validate(2, 2.5, 0.2, 0.2, values[i], 15, 3, 3));
    }
}
```

---

Figure D.3: Code representing the automated testing process for checking mutliple agent parameter values.

---

```

@Test
public void testTotalProbabiliyIsCalculatedToEqualOne() {
    double value = 1.1275;
    double result = ((Math.pow(value, world.getAlpha())) *
        (Math.pow(value, world.getBeta())));
    assertEquals(1.82221,result, 0.0001);

    value = 3.1275;

    double result2 = ((Math.pow(value, world.getAlpha())) *
        (Math.pow(value, world.getBeta())));
    assertEquals(299.2172,result2, 0.0001);

    value = 2.1983;

    double result3 = ((Math.pow(value, world.getAlpha())) *
        (Math.pow(value, world.getBeta())));
    assertEquals(51.337509,result3, 0.0001);

    value = 0.0213;
    //test one with lower values 10^-9 is the result
    double result4 = ((Math.pow(value, world.getAlpha())) *
        (Math.pow(value, world.getBeta())));
    assertEquals(0.00000000438427,result4, 0.000000001);

    double totalSum = result + result2 + result3 + result4;

    assertEquals(352.376919, totalSum, 0.0001);

    double p1 = result/totalSum;
    double p2 = result2/totalSum;
    double p3 = result3/totalSum;
    double p4 = result4/totalSum;

    //check that total probability sums up to 1.0
    assertEquals(1.0, p1 + p2 + p3 + p4, 0.0001);
}

```

---

Figure D.4: Code representing the automated testing process for the probability function.

## 4.2 Black-box Testing

### 4.2.1 File Content Examples

The below figure D.5 contains an example of a valid problem configuration. Each line of content refers to a different specific value. A correct and valid file should contain values in this order and format;

- double, the alpha parameter value between must be in the range of  $-5.0$  to  $5.0$

- double, the double parameter value between must be in the range of  $-5.0$  to  $5.0$
- double, the decay rate value must be in the range of  $0$  to  $1$
- double, the initial edge pheromone value must be in the range of  $0$  to  $1$
- int, the number of agents must be between  $1$  and  $50$
- int, the number of cities must be between  $3$  and  $25$
- int. int, the X and Y coordinate for a City. There should be a line for the corresponding number of cities defined in the previous line
- int, the number of uphill routes to be generated this must be between  $0$  and  $15$
- int, the number of iterations this must be greater than  $0$
- EOF, signifies that this is the end of the configuration content

```

0.2
2.0
0.2
0.8
30
cities
15
36 6
30 1
19 1
25 22
8 7
2 20
26 19
19 3
24 23
7 9
12 6
18 27
2 24
35 23
21 27
7
5
EOF

```

Figure D.5: Contents of a legal problem representation stored in a file.

Below is an example of one of the test files used to ensure that only legal configurations are accepted. This file is rejected because the number of agents is specified as 30sffs which is not a

valid integer value. It is easier to reject this and tell the user to correct it than it is to extract the integer value from malformed data.

```
0.2
2.0
0.2
0.8
30sffs
cities
15
36 6
30 1
19 1
25 22
8 7
2 20
26 19
19 3
24 23
7 9
12 6
18 27
2 24
35 23
21 27
7
5
EOF
```

Figure D.6: Contents of an illegal problem representation stored in a file. The number of agents in line 5 is not an integer value (30sffs)

Below is another example of an illegal configuration. The contents of this file contains no value representing the number of agents.

```

0.2
2.0
0.2
0.8
cities
15
36 6
30 1
19 1
25 22
8 7
2 20
26 19
19 3
24 23
7 9
12 6
18 27
2 24
35 23
21 27
7
5
EOF

```

Figure D.7: Contents of an illegal problem representation stored in a file. The number of agents has not been defined.

#### 4.2.2 Acceptance Tests

Requirement	Test	Pass/Fail	Comment
<b>FR1</b>	Test that the application can be launches from the .jar file	Pass	This will be the default way to launch the application.
<b>FR16</b>	The user is able to exit the application whenever they wish	Pass	Click exit on the main JFrame container. This will exit the application regardless of what the application is currently doing.

Table D.1: A summary of the tests used to acceptance test against FR1 and FR16



Requirement	Test	Pass/Fail	Comment
<b>FR2</b>	A World can be randomly generated	Pass	Clicking 'start' will cause a random world to be generated.

Table D.2: A summary of the tests used to acceptance test against FR2

Requirement	Test	Pass/Fail	Comment
<b>FR3, FR5</b>	World visualisation: Cities are displayed in the correct location	Pass	The correct number of cities is displayed to the user and each city is shown at its own location. Occasionally two cities may render close to each other.
<b>FR3, FR5</b>	World visualisation: The paths between city locations are shown	Pass	The graph is a fully connected graph so a path is drawn from a city to every other city. This is not always clear as some paths may overlap.
<b>FR3, FR5</b>	World visualisation: The correct number of agents is shown	Pass	The correct number of agents is displayed to the user, As multiple agents can be shown at the same city index, there is a text based count which shows that the correct number of agents has been rendered.

Table D.3: A summary of the tests used to acceptance test against FR3 and FR5. These requirements are closely related thus they can be tested in parallel

Requirement	Test	Pass/Fail	Comment
<b>FR4</b>	Ensure that the user can define a value for the 'alpha' parameter	Pass	This is complete with error checking
<b>FR4</b>	Ensure that the user can define a value for the 'beta' parameter	Pass	This is complete with error checking
<b>FR4</b>	Ensure that the user can define a value for the 'decay rate' parameter	Pass	This is complete with error checking
<b>FR4</b>	Ensure that the user can define a value for the 'initial pheromone' parameter	Pass	This is complete with error checking
<b>FR4</b>	Ensure that the user can define the number of 'uphill' paths	Pass	This is complete with error checking
<b>FR4</b>	Ensure the user can define the number of agents	Pass	This is complete with error checking
<b>FR4</b>	Ensure the user can define the number of cities	Pass	This is complete with error checking
<b>FR4</b>	Ensure the user can specify the number of elite agents	Pass	This is complete with error checking
<b>FR4</b>	Ensure the user can specify the number of iterations	Pass	This is complete with error checking

Table D.4: A summary of the tests used to acceptance test against FR4

Requirement	Test	Pass/Fail	Comment
<b>FR6, FR13</b>	The opacity of the path is relative to the pheromone on each edge	Pass	Initially this will be the value specified by the 'initialPhero' parameter
<b>FR6, FR13</b>	Pheromone decay is correctly visualised	Pass	As the algorithm executed there is a clear representation of the pheromone decaying.

Table D.5: A summary of the tests used to acceptance test against FR6 and FR13

Requirement	Test	Pass/Fail	Comment
<b>FR7, FR12</b>	The agents can be displayed at any city location	Pass	Regardless of how many agents are at a city, only 1 image will be shown.
<b>FR7, FR12</b>	The path the agent took between cities will be highlighted	Pass	

Table D.6: A summary of the tests used to acceptance test against FR7 and FR12

Requirement	Test	Pass/Fail	Comment
<b>FR8</b>	Ensure the user can start the algorithms execution	Pass	Clicking the 'start' button will signal the algorithms execution to begin
<b>FR9</b>	Ensure the user can stop an already running algorithm	Pass	An algorithm can only be stopped if there is one already running.

Table D.7: A summary of the tests used to acceptance test against FR8 and FR9

Requirement	Test	Pass/Fail	Comment
<b>FR10</b>	Ensure the algorithm rejects an invalid alpha value	Pass	An error message is displayed to the user
<b>FR10</b>	Ensure the algorithm rejects an invalid beta value	Pass	An error message is displayed to the user
<b>FR10</b>	Ensure the algorithm rejects an invalid decay rate	Pass	An error message is displayed to the user
<b>FR10</b>	Ensure the algorithm rejects an invalid number of iterations	Pass	An error message is displayed to the user
<b>FR10</b>	Ensure the algorithm rejects an invalid number of uphill paths	Pass	An error message is displayed to the user
<b>FR10</b>	Ensure the algorithm rejects an invalid number of cities	Pass	An error message is displayed to the user
<b>FR10</b>	Ensure the algorithm rejects an invalid number of agents	Pass	An error message is displayed to the user
<b>FR10</b>	Ensure the algorithm rejects an invalid number of iterations	Pass	An error message is displayed to the user

Table D.8: A summary of the tests used to acceptance test against FR10

Requirement	Test	Pass/Fail	Comment
<b>FR11</b>	The best route is displayed to the user as a sequence of city indexes	Pass	This is displayed in addition to the visual route
<b>FR11</b>	The best route is shown as a red line between the cities along the best route	Pass	This line is thicker than the lines used to represent the regular paths so it is easy to see

Table D.9: A summary of the tests used to acceptance test against FR11

Requirement	Test	Pass/Fail	Comment
<b>FR14</b>	A problem configuration can be loaded from an external file	Pass	This test was performed with the knowledge that the files contents would enable the loading to complete as all values were legal
<b>FR15</b>	The current problem can be written to a file	Pass	This is only possible if a problem has been generated.

Table D.10: A summary of the tests used to acceptance test against FR14 and FR15

### 4.2.3 Interface Testing

The following tests are not directly related to the functional requirements however, they provide a huge increase in the overall quality of the application as proper error feedback is essential. The parameters and file IO have both been tested for boundary conditions during the unit test process. As a result the author is not concerned about the values tested below. The purpose of these tests is to solely ensure the view is performing as expected.

<b>Parameter Error feedback (1)</b>			
<b>Test</b>	<b>Expected Result</b>	<b>Pass/fail</b>	<b>Comments</b>
Input an alpha value that is too high	An error prompt should display informing the user of an illegal alpha value	Pass	
Input an alpha value that is too low	An error prompt should display informing the user of an illegal alpha value	Pass	
Input a non-double for the alpha value	An error prompt should display informing the user of an invalid data type	Pass	
Input a beta value that is too high	An error prompt should display informing the user of an illegal beta value	Pass	
Input a beta value that is too low	An error prompt should display informing the user of an illegal beta value	Pass	
Input a non-double for the beta value	An error prompt should display informing the user of an invalid data type	Pass	
Specify less than zero iterations	An error prompt should display informing the user of an illegal number of iterations	Pass	
Input a non integer value for the number of iterations	An error prompt should display informing the user of an invalid data type	Pass	
Input a decay rate that is too low	An error prompt should display informing the user of an illegal decay rate value	Pass	
Input a decay rate that is too high	An error prompt should display informing the user of an illegal decay rate value	Pass	
Input a non-double value for decay rate	An error prompt should display informing the user of an invalid data type	Pass	

Table D.11: A summary of the tests used to see if the error feedback is as expected(1).

<b>Parameter Error feedback (2)</b>			
<b>Test</b>	<b>Expected Result</b>	<b>Pass/fail</b>	<b>Comments</b>
Specify less than zero agents	An error prompt should display informing the user of an illegal number of agents	Fail	The prompt displayed when the agent value is illegal was incorrectly formatted. This has been fixed
Specify too many agents	An error prompt should display informing the user of an illegal number of agents	Fail	The prompt displayed when the agent value is illegal was incorrectly formatted. This has been fixed
Specify a non-integer value for the number of agents	An error prompt should display informing the user of an invalid data type	Pass	
Specify too few cities	An error prompt should display informing the user of an illegal number of cities	Pass	
Specify too many cities	An error prompt should display informing the user of an illegal number of cities	Pass	
Specify a non-integer value for the number of cities	An error prompt should display informing the user of an invalid data type	Pass	
Specify too few uphill paths	An error prompt should display informing the user of an illegal number of uphill paths	Pass	
Specify too many uphill paths	An error prompt should display informing the user of an illegal number of uphill paths	Pass	
Specify a non-integer value for the number of uphill paths	An error prompt should display informing the user of an invalid data type	Pass	

Table D.12: A summary of the tests used to see if the error feedback is as expected(2).

<b>File IO Error Feedback</b>			
<b>Test</b>	<b>Expected Result</b>	<b>Pass/fail</b>	<b>Comments</b>
Attempt to load whilst the algorithm is running	An error message should tell the user that the algorithm must be stopped or complete before loading	Pass	
Attempt to load an invalid file	An error message should be displayed informing the user than the problem configuration is invalid	Pass	The cause of the error is unimportant, checks have been done already in regards to catching illegal file content.
Attempt to save whilst the algorithm is running	An error message should tell the user that the algorithm must be stopped or complete before saving	Pass	
Attempt to save when there is nothing to save (no world exists)	The user should be informed that there is nothing to save and should be instructed how to create a world.	Pass	
A loaded problem should be automatically rendered	If the loading of a configuration completes, the configuration should be displayed to the user	Pass	The parameter text fields are also updated to reflect the values contained in such file

Table D.13: A summary of the tests used to see if the error feedback is as expected.

The tests below are designed to see if the algorithm handled general rendering tasks as expected. This does not includes the rendering of the problem or the movement of agents as this have been tested during the acceptance testing phase.



<b>General View Testing(1)</b>			
<b>Test</b>	<b>Expected Result</b>	<b>Pass/fail</b>	<b>Comments</b>
When step mode is enabled the view changes state	When step mode is enabled the 'start' button should now read 'step'	Pass	
When step mode is disabled the view changes state	When step mode is disabled the 'step' button should read 'start'	Pass	
The text values are correctly reset	When the user presses the 'reset values' button, the text fields are restored to default	Fail	The iterations field was not being reset. This has since been fixed.
When in step mode the user cant modify the algorithm	When the user is in step mode and has started the iteration process the text fields should become disabled until the algorithm completes or the user presses stop.	Pass	
When in step mode is complete the view should update	When step mode is complete, the text fields should become usable again	Pass	
When in step mode the algorithm should execute accordingly	When the user has enabled step mode, the algorithm should solve on a step-by-step basis and should not automatically execute until completion.	Pass	The user can stop this at any time.
The additional information should correctly update as the algorithm executed	As the algorithm executes these values should change from their defaults to correctly represent the current state of the algorithm	Pass	
The speed of execution can be changed freely	The user should be able to dynamically change the speed of which the algorithm executes	Pass	

Table D.14: A summary of the tests used to see if view renders elements as expected(1).

<b>General View Testing(2)</b>			
<b>Test</b>	<b>Expected Result</b>	<b>Pass/fail</b>	<b>Comments</b>
When uphill paths are disabled the view should update	When the user has disabled uphill path generation, the text field responsible for setting the number of uphill paths should be disabled	Pass	
When uphill paths are enabled the view should update	When the user has re-enabled the uphill path generation, the text field responsible for setting the number of uphill paths should no longer be disabled	Pass	

Table D.15: A summary of the tests used to see if view renders elements as expected(2).

# Annotated Bibliography

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Tom Blanchard’s dissertation, referenced pages contain relevant information and rationale about a suitable process which suited my development needs. Permission from Tom has been granted for the use and adaptation of his work.

- [4] c2.com, “eXtreme Programming for one, [online] Apr 2015,” Available: <http://c2.com/cgi/wiki?ExtremeProgrammingForOne>, accessed: 9th Apr 2015.

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An image mapping one solution to the Berlin52.tsp problem.

- [6] M. Dorigo, “Optimization, learning and natural algorithms (in Italian),” Ph.D. dissertation, Dipartimento di Elettronica, Politecnico di Milano, Milan, Italy, 1992.

Marco Dorigo PhD thesis containing information about Ant Colony methods. Marco first came up with this concept however this thesis is extremely detailed and too complicated for this project and is used merely as a reference point should a reader want further information. In addition it is difficult to find a good translation so it is not the best resource for the project however, out of respect to the author a reference to this work is provided.

- [7] E. Gamma, R. Helm, R. Johnson, and J. Vlissides, “Design Patterns: Elements of Reusable Object-Oriented Software,” Nov 1994, pp. 127-128, [Online]. Available: <http://www.worldcat.org/isbn/020163361>.

This book is a very good reference point for design patterns in general, providing concise descriptions, examples and use cases. The book examples are implemented using C++, as this will be a Java based project the main concepts are still relevant as the languages aren't too diss-similar. Pages 127-128 relate to the the Singleton pattern.

- [8] —, “Design Patterns: Elements of Reusable Object-Oriented Software,” Nov 1994, pp. 4-6, [Online]. Available: <http://www.worldcat.org/isbn/020163361>.

This book is a very good reference point for design patterns in general, providing concise descriptions, examples and use cases. The book examples are implemented using C++, as this will be a Java based project the main concepts are still relevant as the languages aren't too diss-similar. Pages 4-6 relate to the the Model-View-Controller pattern.

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An overview of Ant Colony Optimisation as a whole a simple explanations of the underlying functions and behaviours of each of the algorithm variations.

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Mono provide an open source implementation of the Microsoft .NET framework enabling the development of C Sharp across multiple platforms and environments. The Framework is based on ECMA standards for C Sharp so there is some reliability when developing C Sharp in different environments. However, based on research the implementation of certain features, specifically the newer features in the latest releases of the .NET framework do not always behave as expected. This causes development problems which can easily be avoided for this project.

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A Masters thesis looking into a hybrid Ant and Bee Colony algorithm for dynamic TSP problems. The thesis has some good concepts and background into the algorithm, however a lot of the information is highly theoretical.

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An image depicting the structure of the waterfall life cycle. This has been modified to properly show the process the author followed for this project.

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Simplistic explanations of each function required. A Break down of equations is also included in order to make them more digestible.

- [23] V. E. Sjoerd, ““Dynamic ant colony optimization for the travelling salesman problem,” Master’s thesis, Leiden University, The Netherlands, Leiden Institute of Advanced Computer Science (LIACS), Leiden University, Niels Bohrweg 1, 2333 CA Leiden, The Netherlands, Jul 2012, pp.11 [Online]. Available: <http://www.liacs.nl/assets/2012-08SjoerdvanEgmond.pdf>.

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Simple graphic representing the Double Bridge Experiment.

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Simple graphic representing the algebra representation of the pheromone function required to update the pheromone matrix.

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Simple graphic representing the algebra representation of the pheromone function required to select the Agents next movements.

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Simple graphic representing the algebra representation of the pheromone function required to update the pheromone matrix.