

Behavior of weakly adsorbing protein impurities in flow-through ion-exchange chromatography

Chase E. Herman^a, Xuankuo Xu^b, Steven J. Traylor^b, Sanchayita Ghose^b,
Zheng Jian Li^b, Abraham M. Lenhoff^{a,*}

^a*Department of Chemical and Biomolecular Engineering, University of
Delaware, Newark, DE, USA*

^b*Biologics Process Development, Bristol Myers Squibb, Devens, MA, USA*

Abstract

Flow-through ion-exchange chromatography is frequently used in polishing biotherapeutics, but the factors that contribute to impurity persistence are incompletely understood. A large number of dilute impurities may be encountered that exhibit physicochemical diversity, making the flow-through separation performance highly sensitive to process conditions. The analysis presented in this work develops two novel correlations that offer transferable insights into the chromatographic behavior of weakly adsorbing impurities. The first, based on column simulations and validated experimentally, delineates the relative contributions of thermodynamic, transport, and geometric properties in dictating the initial breakthrough volume of dilute species. The Graetz number for mass transfer was found to generalize the transport contributions, enabling estimation of a threshold in the equilibrium constant below which impurity persistence is expected. Impurity adsorption equilibria are needed to use this correlation, but such data are not typically available. The

*Corresponding author

E-mail address: lenhoff@udel.edu (A.M. Lenhoff).

second relationship presented in this work may be used to reduce the experimental burden of estimating adsorption equilibria as a function of ionic strength. A correlation between stoichiometric displacement model parameters was found by consolidating isocratic retention data for over 200 protein-pH-resin combinations from the extant literature. Coupled with Yamamoto’s analysis of linear gradient elution data, this correlation may be used to estimate retentivity approximately from a single experimental measurement, which could prove useful in predicting host-cell protein chromatographic behavior.

Keywords: Flow-through, Ion-exchange, Impurity, Clearance, Breakthrough, Stoichiometric displacement model

1. Introduction

The biopharmaceutical market has grown substantially over the past few decades, with over 300 biologics having received regulatory approval and hundreds more in development pipelines [1, 2]. Monoclonal antibodies (mAbs) comprise the majority of these biologics, partly because platform purification processes have enabled their rapid development [3, 4]. One stage in a typical platform process is polishing, where trace impurities such as host-cell proteins (HCPs) are removed prior to product formulation using one or more chromatographic operations [5]. Despite their low concentrations, some of these impurities may pose a risk to therapeutic safety and stability, and polishing operations are designed to remove them completely [6, 7].

Polishing may be performed using ion-exchange (IEX), hydrophobic interaction or multimodal resins. Since the majority of secreted HCPs are more

14 acidic than the typical mAb [8], anion-exchange (AEX) resins are more natu-
15 rally suited to flow-through operations [9], in which impurities are intended to
16 adsorb to the resin, but they may be used in bind-and-elute mode as well [10].
17 The inverse is true of cation-exchange (CEX) stationary phases. The flow-
18 through operational mode offers the advantage of relatively high throughput;
19 as a heuristic, 1 g of mAb usually requires 1 ml of resin in flow-through IEX
20 [11]. For mAb concentrations on the order of 20 mg/ml, this corresponds to
21 an apparent processing capacity on the order of 50 column volumes (CV).
22 Such large capacities can enable high productivity operations with relatively
23 small columns. If convective media are used instead of resin particles, there
24 is the potential to increase productivity beyond the limitations inherently
25 associated with packed column flow rate constraints [¹][12, 13]. These
26 process intensification benefits have led to an increasing consideration of
27 flow-through operations for applications outside of polishing, particularly in
28 the development of continuous downstream processes [11, 14, 15].

29 Despite the utility of flow-through IEX steps, relatively few studies have
30 systematically investigated their development and limitations. This is partly
31 because impurity behavior is essential to understanding flow-through separa-
32 tions, but it is difficult to interrogate experimentally. Total HCP concentra-
33 tions encountered in mAb polishing are usually on the order of 1000 ppm [16],
34 rendering in-line detection and quantification infeasible [17, 18]. Hundreds
35 of HCPs may be present, and their biophysical diversity leads to heteroge-
36 neous chromatographic behavior. Although process conditions are tuned to

¹removed: [12]

37 maximize HCP adsorption, they are generally less conducive to strong reten-
38 tion than in bind-and-elute mode. This may make impurity clearance highly
39 sensitive to the mobile phase composition and the resin.

40 Coupled with the plethora of available resins, the high sensitivity of sep-
41 aration performance typically necessitates screening studies during process
42 development. Commercial IEX resins are available that differ in particle
43 size, pore size and morphology, base matrix, ligand chemistry, ionic capac-
44 ity, and surface functionalization [19, 20]. Screening studies to determine
45 the best resin among several alternatives can provide valuable application-
46 specific data, and perhaps furnish general resin retentivity heuristics [21], but
47 they offer limited transferable insights into individual HCP chromatographic
48 retention and capacity. Column modeling has therefore been suggested as a
49 complementary technique to elucidate the factors that contribute to impurity
50 persistence [17, 18]. A better understanding of this phenomenon could po-
51 tentially improve flow-through process design, expedite development, reduce
52 costs, and increase consistency with quality by design principles. It could also
53 help direct future *in silico* optimization efforts, which to date have focused
54 primarily on product molecules rather than impurities.

55 Two HCP persistence mechanisms have been hypothesized for flow-through
56 processes: product association and weak adsorption [5]. The relative im-
57 portance of these mechanisms remains unclear. Product association is ex-
58 pected to vary mechanistically with the therapeutic molecule and the impu-
59 rity species, which may hinder a general understanding of the phenomenon.
60 However, it may be tractable to analyze generally the breakthrough of weakly
61 adsorbing impurities. Two attributes of the flow-through process simplify the

analysis, namely that the process is isocratic, and that the adsorption equilibria of weakly adsorbing species are expected to be approximately linear and independent. Assuming HCP concentrations on the order of 1000 ppm, column capacities on the order of 100 mg/ml, and the load heuristic of 1 g mAb/ml of column, only $\sim 1\%$ of the column is expected to saturate with HCPs. The majority of the column is therefore available for weakly retained HCPs to adsorb with negligible competition for the IEX surface.

This work focuses on developing transferable insights into the breakthrough of weakly adsorbing impurities in flow-through IEX. We placed emphasis on understanding contributions to the initial breakthrough volume, as the goal of flow-through polishing is the complete removal of trace impurities. To maintain generalizability across diverse sets of HCPs, we simulated the chromatographic behavior of dilute species with a variety of transport and thermodynamic properties. Simulated initial breakthrough volumes were analytically related to the Graetz number for mass transfer, and this relationship was validated experimentally. Transport and thermodynamic parameters need to be estimated to use this relationship, but HCP adsorption equilibrium constants are usually unknown. To gain a better understanding of IEX adsorption equilibria, we consolidated dilute isocratic retention data from the extant literature on model species. From these data, a correlation was observed between stoichiometric displacement model (SDM) parameters that are commonly used to relate the adsorption equilibrium constant to ionic strength [22]. This thermodynamic correlation was corroborated by linear gradient elution data, suggesting a way to estimate SDM parameters approximately from one experimental measurement. These relationships pro-

87 vide novel insights into properties that contribute to flow-through impurity
 88 clearance.

89 2. Theory and simulation

90 2.1. Column chromatography model

91 The 1D general rate model of column chromatography was used in this
 92 work, which describes the transport of solutes within the column interstitial
 93 volume as [20, 23, 24]:

$$\frac{\partial c}{\partial t} + v \frac{\partial c}{\partial z} = D_{ax} \frac{\partial^2 c}{\partial z^2} - \frac{3}{r_p} \left(\frac{1 - \varepsilon_c}{\varepsilon_c} \right) k_f \left(c - c_p|_{r=r_p} \right) \quad (1a)$$

94 with Danckwerts' boundary conditions:

$$v (c_{in} - c|_{z=0}) = -D_{ax} \frac{\partial c}{\partial z} \Big|_{z=0} \quad (1b)$$

95

$$\frac{\partial c}{\partial z} \Big|_{z=L_{col}} = 0 \quad (1c)$$

96 where c is the solute concentration in the interstitial volume, c_p is the solute
 97 concentration in the resin bead pore space, t is time, z is the column axial
 98 coordinate, r is the resin bead radial coordinate, c_{in} is the column inlet
 99 concentration, L_{col} is the column length, r_p is the resin bead radius, v is the
 100 interstitial velocity, D_{ax} is the axial dispersion coefficient, k_f is the film mass
 101 transfer coefficient, and ε_c is the [\[.2 \]interstitial column porosity \(i.e., the bed](#)
 102 [void fraction\)](#). Solute transport within the resin beads is described by:

$$\varepsilon_p \frac{\partial c_p}{\partial t} + (1 - \varepsilon_p) \frac{\partial q}{\partial t} = \varepsilon_p D_p \left(\frac{\partial^2 c_p}{\partial r^2} + \frac{1}{r} \frac{\partial c_p}{\partial r} \right) + (1 - \varepsilon_p) D_s \left(\frac{\partial^2 q}{\partial r^2} + \frac{1}{r} \frac{\partial q}{\partial r} \right) \quad (2a)$$

²removed: column porosity

103 with boundary conditions of spherical symmetry at the bead center and a
 104 mass balance at the bead edge, respectively:

$$\left. \frac{\partial c_p}{\partial r} \right|_{r=0} = 0, \quad \left. \frac{\partial q}{\partial r} \right|_{r=0} = 0 \quad (2b)$$

105

$$\varepsilon_p D_p \left. \frac{\partial c_p}{\partial r} \right|_{r=r_p} + (1 - \varepsilon_p) D_s \left. \frac{\partial q}{\partial r} \right|_{r=r_p} = k_f \left(c - c_p|_{r=r_p} \right) \quad (2c)$$

106 where q is the adsorbed solute concentration, ε_p is the resin bead porosity
 107 accessible to the solute, D_p is pore diffusivity, and D_s is surface diffusivity.
 108 Typically, the relevant initial conditions are:

$$c|_{t=0} = 0, \quad c_p|_{t=0} = 0, \quad q|_{t=0} = 0 \quad (3)$$

109 An isotherm relating q to c_p is needed to complete the column model,
 110 along with a description of the adsorption kinetics. Since adsorption and
 111 desorption steps are usually much faster than the other transport processes,
 112 instantaneous equilibration was assumed in this work. [\[.3 \]Although a linear](#)
 113 [isotherm was assumed for comparison with experimental data \(section 2.2\), in](#)
 114 [general the](#) Langmuir isotherm was used:

$$q = q_{max} \left(\frac{K_L c_p}{K_L c_p + 1} \right) \quad (4)$$

115 where q_{max} is the resin saturation capacity and K_L is a thermodynamic pa-
 116 rameter (equal to the ratio of the adsorption and desorption rate constants,
 117 k_a/k_d). The adsorption equilibrium constant, K_{eq} , is defined by the initial
 118 isotherm slope, which for the Langmuir model is:

$$K_{eq} \equiv \lim_{c_p \rightarrow 0} \frac{q}{c_p} = q_{max} K_L \quad (5)$$

³removed: The

119 Dimensions of volume concentration were used for q in this work (as opposed
120 to excess surface concentration), making K_{eq} a dimensionless parameter.

121 Column model equations were solved with the Chromatography Analysis
122 and Design Toolkit (CADET, versions 4.1.0 and 4.2.0) [25].

123 2.2. Simulations for analyzing breakthrough volumes

124 To ascertain qualitative differences between the breakthrough of concen-
125 trated and dilute species, simulations were performed for single-component
126 systems with load concentrations between 10 mg/ml and 1 μ g/ml with q_{max}
127 fixed at 100 mg/ml of packed column, K_{eq} varied from 1 to 10000, and trans-
128 port parameters selected from representative calibrations to model species.
129 Exploratory simulations were then performed for a load concentration of 1
130 μ g/ml at variable v , D_p , L_{col} , and r_p . D_{ax} was estimated as a function of
131 v from correlations for beds packed with solid particles [26], using a dilute
132 solution diffusivity of 7.5×10^{-11} m²/s to represent general protein behavior
133 [27]. Film mass transfer was assumed [..⁴]not to be rate-limiting, and k_f
134 was consequently set to 1×10^{-3} m/s [..⁵]to remove this degree of freedom
135 from all simulations. D_s was estimated as a function of K_{eq} using results
136 reported for a mAb of the form $D_s = aK_{eq}^b$, where the power law [..⁶]coef-
137 ficients $a = 1.66 \times 10^{-12}$ m²/s and $b = -0.24$ [28]. All simulation parameters
138 are summarized in Supplementary Table S1.

139 Results from these simulations were correlated to relate breakthrough
140 volume with system parameters, making use of an effective intraparticle dif-

⁴removed: to be relatively fast

⁵removed: for

⁶removed: coefficient

141 fusivity (D_{eff}) to describe the combined effects of pore and surface diffusion
 142 [29]:

$$D_{eff} \equiv D_p + \left(\frac{1 - \varepsilon_p}{\varepsilon_p} \right) K_{eq} D_s \quad (6)$$

143 This expression may be derived from Equation 2a by assuming instantaneous
 144 equilibration and linear chromatographic conditions, as given by:

$$q = K_{eq} c_p \quad (7)$$

145 A linear isotherm was used for comparing simulations with experimental
 146 data, and the extra-column volume, which consisted of valves and 0.75 mm
 147 ID tubing, was described as a continuously stirred tank reactor (CSTR) in
 148 series with a dispersed plug flow reactor (PFR) [30]. The fraction of the
 149 extra-column volume allocated to the CSTR was fit as a function of flow
 150 rate, and the PFR axial dispersion coefficient was set to 1×10^{-12} m²/s.

151 2.3. Models for ion-exchange adsorption equilibria

152 A number of models have been proposed to relate protein IEX adsorp-
 153 tion equilibria to solution conditions, with perhaps the simplest and most
 154 commonly cited being the stoichiometric displacement model (SDM), which
 155 describes adsorption as a strict ion-exchange process [22]. From the law of
 156 mass action, the adsorption equilibrium constant is related to ionic strength,
 157 I , as:

$$K_{eq} = \alpha I^{-\nu} \quad (8)$$

158 where α is a measure of adsorption strength and ν is the protein charac-
 159 teristic charge, which represents the stoichiometry of ion exchange. These
 160 parameters are commonly estimated by fitting isocratic retention data at

different ionic strengths or regressing linear gradient elution data according to Yamamoto's method [31]. The fundamental equation of ideal linear chromatography predicts that retention factors should also exhibit a power law dependence on ionic strength [23]:

$$k' = \phi K_{eq} = \phi \alpha I^{-\nu} \quad (9)$$

where $k' = (V_R - V_0)/V_0$ is the retention factor for the solute and solution conditions of interest, V_R is the retention volume, and V_0 is the ⁷retention volume under non-adsorbing conditions. For dimensionless K_{eq} , $\phi = (1 - \varepsilon_t)/\varepsilon_t$ is a dimensionless phase ratio where ⁸ $\varepsilon_t = \varepsilon_c + (1 - \varepsilon_c)\varepsilon_p = V_0/V_{column}$ represents the total column porosity.

More sophisticated colloidal models that are based on statistical thermodynamics have also been proposed for estimating K_{eq} from the free energy change of molecular adsorption, ΔF , using some form of the general expression [32]:

$$K_{eq}(I, \text{pH}) = \int_{\Omega} \int_{z_0}^{\infty} (e^{-\Delta F(z, \Omega, I, \text{pH})/k_B T} - 1) dz d\Omega \quad (10)$$

where Ω represents the protein orientation with respect to the resin and z is the separation distance. Previous models have used continuum electrostatics and van der Waals equations to estimate ΔF , often making use of mean-field approximations [33, 34]. Notably, the K_{eq} estimates from these models are quite sensitive to ΔF due to the Boltzmann weighting.

⁷removed: flow-through

⁸removed: $\varepsilon_t = \varepsilon_c + (1 - \varepsilon_c)\varepsilon_p$

179 **3. Materials and methods**

180 *3.1. Chemicals and buffers*

181 Sodium hydroxide, hydrochloric acid, sodium chloride, monobasic sodium
182 phosphate, dibasic sodium phosphate, acetic acid, sodium acetate, boric
183 acid, and sodium bicarbonate were purchased from Fisher (Fair Lawn, NJ).
184 Sodium carbonate, ethanolamine, and 2000 kDa blue dextran were pur-
185 chased from Sigma (St. Louis, MO). Fluorescein isothiocyanate (FITC) and
186 dimethylformamide were purchased from Thermo Scientific (Rockford, IL).
187 All chemicals were used without any further purification.

188 Buffer solutions were prepared to the desired constituent concentrations
189 at room temperature with deionized water from an EMD Millipore Milli-Q
190 system ($> 18.2 \text{ M}\Omega \text{ cm}$). Low and high ionic strength buffers were prepared
191 with 0 and 1 M added NaCl, respectively. Buffer pH and conductivity were
192 measured with a Cole-Parmer PC200 meter, and pH adjustments were made
193 with concentrated sodium hydroxide and hydrochloric acid solutions. Prior
194 to use, buffer solutions were filtered with Fisher 0.2 μm aPES membranes
195 (Pittsburgh, PA).

196 *3.2. Proteins*

197 Lyophilized hen egg white lysozyme was purchased from Sigma (St. Louis,
198 MO). A mAb sample was obtained from the protein A eluate pool of a
199 manufacturing process at Bristol Myers Squibb (Devens, MA). The mAb
200 was supplied at 35 mg/ml and stored at -80°C . It was thawed prior to use
201 and exchanged into the desired buffer using a GE Sephadex G25 desalting

column, and protein solution concentrations were measured with a Thermo Scientific NanoDrop Lite spectrophotometer.

3.3. Resins and chromatography equipment

All chromatographic measurements were performed using an Amersham Biosciences Äkta Explorer equipped with a P-960 sample pump, fraction collector, 10 mm UV flow cell, and in-line pH and conductivity meters. SP Sepharose FF, a strong cation-exchanger with a nominal particle diameter of 90 μm , was purchased from GE Healthcare (Uppsala, Sweden). It was exchanged three times into a pH 7.0 (25 mM sodium phosphate) buffer by centrifugation and decantation prior to slurry packing (50%) into a 0.5 \times 10 cm Waters AP chromatography column to a final bed volume of 2.0 ml. Column packing was validated at pH 7.0 by injecting a 100 μl pulse of a 1 M NaCl buffer and verifying that the conductivity trace asymmetry fell within commonly accepted limits [19].

3.4. Linear gradient elution

The retention of lysozyme on SP Sepharose FF was measured with linear gradient elution at pH 5.0, 7.0, and 9.0 (in 75 mM sodium acetate, 25 mM sodium phosphate, and 25 mM ethanolamine buffers, respectively) at a superficial velocity of 300 cm/h. Feed solutions were prepared by dissolving lysozyme in the appropriate low ionic strength buffer at ~ 20 mg/ml, and lyophilized excipients were removed with three buffer exchange cycles using EMD Millipore Amicon centrifugal filter units (Cork, Ireland). Lysozyme solutions were filtered using Thermo Scientific 0.2 μm PVDF membranes (Rockwood, TN) and diluted to ≤ 10 mg/ml prior to use. The SP Sepharose

226 FF column was equilibrated in the relevant low ionic strength buffer for 5 [..⁹
227]column volumes (CV), and gradient elution from 0 to 1 M NaCl began shortly
228 after a 100 μ l sample injection. The gradient elution volume was varied from
229 10 to 50 CV in increments of 10 CV, and the conductivity at peak elution
230 was determined. This was used with a correlation for the instrument’s con-
231 ductivity response to estimate the peak elution ionic strength. Columns were
232 regenerated at least once every five runs via 15 minutes of contact with 0.5
233 M NaOH.

234 3.5. Breakthrough measurements during isocratic elution

235 To validate corresponding simulation results, frontal loading chromatog-
236 raphy was performed with dilute lysozyme solutions on SP Sepharose FF
237 at pH 7.0 (20 mM sodium phosphate) under conditions of weak to moder-
238 ate retention. The requisite ionic strength for such retention was estimated
239 from linear gradient elution measurements and tuned empirically to target
240 a breakthrough volume of \sim 10 CV. A feedstock of 10 μ g/ml lysozyme was
241 used to mimic the low impurity concentrations encountered in flow-through
242 polishing, and outlet concentrations were estimated from the absorbance at
243 215 nm with a computed extinction coefficient [35]. At such low protein con-
244 centrations, appreciable variability in component separation was observed
245 between replicate feedstock preparations. For this reason, feedstock batches
246 were prepared at the desired ionic strength in sufficient volume to service
247 the entire set of measurements, and a batch exhibiting minimal component
248 separation was selected for use. For each measurement, a 10 CV equilibra-

⁹removed: CV

tion period preceded a 20 CV load through the Äkta's sample pump, after which the column was washed as described previously. This was performed at superficial velocities ranging from 30 to 305 cm/h in a randomized order, and comparable breakthrough measurements were made under non-adsorbing conditions (at high ionic strength).

To qualitatively validate simulated trends under conditions of greater relevance to flow-through polishing, breakthrough behavior was also demonstrated with fluorescently labelled lysozyme in the presence of a mAb. Lysozyme was conjugated with FITC according to the manufacturer's protocol, producing a complex product mixture with different label ratios and conjugation sites. A fraction of the conjugation products exhibiting relatively homogeneous chromatographic behavior was required to effectively represent the breakthrough of an individual impurity. The conjugation product mixture was therefore subjected to repeated fractionation on SP Sepharose FF at pH 9.5 (20 mM sodium carbonate) using shallow ionic strength steps during elution. Average label ratios and FITC-lysozyme concentrations in the collected fractions were estimated from the absorbance profiles at 280 and 495 nm. Once a sufficiently homogeneous fraction was obtained, it was spiked to $\sim 10 \mu\text{g/ml}$ in a mAb solution at pH 9.5, where the mAb was observed to have negligible retention on SP Sepharose FF. As with lysozyme breakthrough measurements, an ionic strength was identified to achieve weak to moderate FITC-lysozyme retention, and breakthrough profiles were acquired over a range of superficial velocities in randomized order. The mAb concentration was dilute due to material constraints, and the eluate absorbance at 495 nm was used to distinguish FITC-lysozyme breakthrough from the mAb

274 flow-through.

275 3.6. Parameter estimation for test simulations

276 The breakthrough of lysozyme fed in dilute solution on SP Sepharose FF
277 was simulated in CADET as described in Section 2.2. Sequential parameter
278 estimation was used to reduce the dimensionality of the optimization space
279 when fitting the experimental data. Duplicate column bypass profiles were
280 acquired with lysozyme at each flow rate used in breakthrough measurements.
281 These were fit with a trust region optimization algorithm interfaced by the
282 `Scipy least_squares` function to determine the extra-column volume (which
283 is invariant with flow rate) and the fraction of that volume allocated to the
284 CSTR in the system model (which varies with flow rate). Triplicate blue
285 dextran pulses, monitored with the absorbance at 280 nm, were then passed
286 through the column to measure ε_c . Peak tailing was observed, which is
287 attributable to size heterogeneity in the blue dextran tracer. For this reason,
288 the average peak mode was used instead of the average first moment to
289 estimate ε_c .

290 Duplicate lysozyme pulses under non-adsorbing conditions (high ionic
291 strength) were then passed through the column at each flow rate. Retention
292 volumes under non-adsorbing conditions were computed from the first mo-
293 ment of the absorbance profiles and used to estimate ε_p . These profiles were
294 then fit to estimate D_p (which is invariant with flow rate) and D_{ax} (which
295 varies with flow rate). An evolutionary algorithm interfaced by the `Scipy`
296 `differential_evolution` function was used to estimate D_p and a coarse
297 dependence of D_{ax} on flow rate. The estimated value of D_p was retained,
298 and the coarse D_{ax} estimates were refined using the `least_squares` func-

tion. Without further refinement, the estimated parameters were validated by modeling dilute lysozyme breakthrough profiles under non-adsorbing conditions (at high ionic strength). Dilute breakthrough profiles under adsorbing conditions (at lower ionic strength) were then simulated by fitting K_{eq} and D_s (which are invariant with flow rate) using the `differential_evolution` function.

4. Results and discussion

4.1. Breakthrough volume correlation

In the context of polishing operations, the value of flow-through IEX is its ability to completely remove as many trace HCPs as possible from a mAb solution. Challenges inherent in this task may not be readily apparent because it is difficult to study the chromatographic behavior of dilute solutes empirically. A column simulation was therefore used to investigate differences between the breakthrough of overloaded products and dilute impurities. An initial set of single-component simulations were performed at different feed concentrations and K_{eq} values. Transport and geometric parameters were held fixed, and a Langmuir isotherm with constant $q_{max} = 100$ mg/ml of column was used. Results for [\[¹⁰\]](#) 10 mg/ml and 1 μ g/ml feed concentrations are juxtaposed in Figure 1, [\[¹¹\]](#) corresponding to separation factors that are $\ll 1$ (highly favorable) and ~ 1 (near-linear), respectively [36], while results for [intermediate feed](#) concentrations are shown in Supplementary Figure S1.

¹⁰removed: extreme

¹¹removed: and analogous plots for intermediate

320 As may be expected for the system with a 10 mg/ml feed [¹²](separation
 321 factor $\ll 1$), retention increases with K_{eq} until the column [¹³]saturates, and
 322 breakthrough profiles [¹⁴]become sharper as column saturation [¹⁵]is ap-
 323 proached. This self-sharpening behavior [¹⁶]does not occur for the 1 μ g/ml
 324 feed (near-linear conditions) over the volume scale simulated, revealing dilute
 325 solute breakthrough profiles to become more diffuse as retention increases
 326 due to the essentially linear isotherm. An order-of-magnitude difference can
 327 be observed between the load volumes corresponding to the initial break-
 328 through and the inflection point in the more strongly retained profiles. This
 329 illustrates an appreciable challenge; even if trace impurities exhibit strong
 330 to moderate retention, their diffuse distribution on the column may lead to
 331 relatively early breakthrough and preclude adequate clearance.

332 To better understand this challenge, the load volume corresponding to
 333 1% breakthrough was identified and plotted against K_{eq} (Figure 2). A cou-
 334 ple of trends may be observed. When column saturation is not approached,
 335 the breakthrough volume appears to scale linearly with K_{eq} . [¹⁷]A limit-
 336 ing estimate of the K_{eq} dependence may be [¹⁸]obtained as $CV_{breakthrough} =$
 337 $\varepsilon_t + (1 - \varepsilon_t)K_{eq}$ based on the fundamental equation of ideal linear chromatog-
 338 raphy. As shown, the slope of the dilute solute series differs markedly from
 339 the ideal limit, due largely to finite transport rates that limit the system's

¹²removed: , retention increased

¹³removed: saturated

¹⁴removed: became

¹⁵removed: was

¹⁶removed: did

¹⁷removed: An ideal limit on

¹⁸removed: roughly estimated

approach to equilibrium. The discrepancy between the observed and ideal behavior therefore suggests that transport rate optimization may provide a useful means of improving impurity clearance in flow-through processes.

[¹⁹] The simulation data show that the slope of the $CV_{1\%}$ vs. K_{eq} curve for dilute solutes varies with transport and geometric parameters, and the curve approaches an intercept between ε_c and ε_t at $K_{eq} = 0$. This observation indicates that the initial breakthrough volume may be approximately described as:

$$CV[²⁰]_{1\%} = $\varepsilon[²¹] + (1 - \varepsilon_t)K_{eq}f_{1\%}$ (11)$$

where [²²] $\varepsilon_c < \varepsilon < \varepsilon_t$ and $f_{1\%}$ is a function of transport parameters that modifies the breakthrough volume dependence on K_{eq} , with [²³] $0 \leq f_{1\%} \leq 1$. The form of this relationship has two implications: it suggests that thermodynamic and transport contributions to impurity breakthrough may be independent, and that transport contributions may be described by a single factor, which can presumably be expressed generally in terms of a dimensionless group.

Based on this rationale, a second set of simulations were performed for a 1 $\mu\text{g}/\text{ml}$ feed [²⁴] with a variety of thermodynamic, transport, and geometric parameters [²⁵]. $f_{1\%}$ was computed from the results by rearranging Equation 11 [²⁶] and substituting ε_c for ε , because ε_c [²⁷] was observed to

¹⁹removed: Further simulations showed

²²removed: f

²³removed: $0 \leq f \leq 1$

²⁴removed: . A

²⁵removed: were used, and f

²⁶removed: . However,

²⁷removed: was used in place of the ε_t intercept when computing f from Equation 11

359 [..²⁸] generally describe the simulated breakthrough volumes better than ε_t in
 360 the limit of $K_{eq} \rightarrow 0$ [..²⁹]; this may be attributable to finite transport rates
 361 limiting the solute exploration of intraparticle void volumes. As was done for the
 362 dynamic binding capacity correlation presented by Chen et al. [37], [..³⁰] $f_{1\%}$
 363 is plotted in Figure 3 against [..³¹]

$$[..^{32}]$$

364 [..³³] a Graetz number for mass transfer [..³⁴]:

$$Gz_{eff} = \frac{vd_{part}^2}{D_{eff}L_{col}} \quad (12)$$

365 This is often written as $Gz_{eff} = (d_{part}/L_{col}) P\acute{e}_{p-eff}$, where the particle Péclet
 366 number [..³⁵] $P\acute{e}_{p-eff} = vd_{part}/D_{eff}$ represents a ratio of characteristic times
 367 for diffusive and convective transport on the length scale of the resin particle [..³⁶
 368]. However, it is more directly meaningful as a ratio of [..³⁷] the characteristic
 369 times for intraparticle diffusion, d_{part}^2/D_{eff} , and convection along the column,
 370 L_{col}/v .

because this

²⁸removed: better

²⁹removed: . Based on

³⁰removed: f

³¹removed: the dimensionless group:

³³removed: which represents

³⁴removed: , written as a product of two dimensionless subgroups. The first is

³⁵removed: , which represents the ratio of convective to diffusive transport rates

³⁶removed: , when D_{eff} is used to describe the diffusional transport. The second

subgroup is

³⁷removed: characteristic length scales, namely the resin particle diameter and the column length

Figure 3 indicates that Equation 11 [..³⁸] may be written more specifically
as:

$$CV_{\%} = \varepsilon_c + (1 - \varepsilon_t)K_{eq}f_{\%}([..³⁹]Gz_{eff}) \quad (13)$$

where $CV_{\%}$ is the load volume at a given percent breakthrough threshold,
and $f_{\%}$ is the corresponding function of [..⁴⁰]the Graetz number. Rearranging
Equation 13 reveals this function to be approximately the ratio of dynamic to
static binding capacities under linear adsorption conditions when $CV_{\%} \gg \varepsilon_c$.
Figure 3 shows two series for illustrative breakthrough thresholds, but any ar-
bitrary threshold could be selected. Some noise is apparent, but it is largely
attributable to the approximation that $CV_{\%}$ is invariant with transport pa-
rameters when $K_{eq} = 0$. Within the noise, it is clear that $CV_{\%}$ decays
monotonically with the value of the Graetz number.

To maximize the load volume before breakthrough, which is approxi-
mated by $CV_{1\%}$, the Graetz number should be minimized. Unfortunately,
doing so comes at a cost to throughput if v is reduced or an increase in
column pressure drop if d_{part} is decreased or L_{col} is increased. This corre-
lation [..⁴¹]therefore does not suggest a free way of improving flow-through
processing. What it does quantify, however, is the inherent balance between
separation performance and throughput. Notably, the initial breakthrough
volume decays much more quickly with the Graetz number than the interme-
diate breakthrough volume. The benefit of optimizing the system geometry
and transport rates is expected to be only marginal for typical process con-

³⁸removed: with a modified intercept

⁴⁰removed: transport and geometric parameters. Shown are

⁴¹removed: does therefore

392 ditions, which correspond to Graetz numbers on the flat part of the 1%
 393 breakthrough curve in Figure 3. However, if the Graetz number could be
 394 decreased below ~ 5 , the benefit would become much more pronounced.

395 An interesting subtlety that is implicit in this correlation is the effect
 396 of thermodynamics on intraparticle transport rates, which is described by
 397 the dependence of D_{eff} on K_{eq} . D_{eff} captures the combined effects of pore
 398 and surface diffusion in the dilute solute limit by describing the effective
 399 intraparticle diffusivity as a weighted sum, where K_{eq} weights the relative
 400 importance of surface diffusion. IEX surface diffusivities have been shown
 401 to follow a power law of the form $D_s = aK_{eq}^b$ [..⁴²][28], where the empiri-
 402 cal power law coefficients a and b are expected to be on the order of D_p and
 403 -0.5 , respectively, with $b < 0$ [..⁴³][38, 39]. This leads to competing effects:
 404 increasing K_{eq} decreases the surface diffusivity but simultaneously increases
 405 the driving force for surface diffusion, with the effect that dominates being
 406 determined by whether [..⁴⁴] $b > -1$. If this is the case, increasing K_{eq}
 407 leads to an increase in D_{eff} and a reduction in the Graetz number, meaning
 408 that both thermodynamic and transport contributions to delaying impurity
 409 breakthrough are improved simultaneously.

410 Equation 13 also enables estimation of the problematic K_{eq} threshold
 411 below which impurities will persist via weak adsorption. To gain a sense for
 412 the threshold's order of magnitude, an illustrative calculation was performed
 413 with a spline fit to the $f_{1\%}$ curve shown in Figure 3. Results for a 20 cm

⁴²removed: , where

⁴³removed: [28]

⁴⁴removed: the power law exponent

column with a 6 minute residence time are shown in Figure 4 as a function of load volume using $\varepsilon_c = 0.35$, $\varepsilon_p = 0.5$, $d_{part} = 50 \mu\text{m}$, $D_p = 10^{-11} \text{ m}^2/\text{s}$, and D_s estimated from the power law discussed previously. The results show that, for load volumes on the order of 100 CV, HCPs with $K_{eq} < \sim 400$ are liable to break through before the end of loading. This would be equivalent to a retention factor of ~ 200 for an input feed pulse under identical conditions.

4.2. Validation of the breakthrough volume correlation

To validate the breakthrough volume correlation that was developed from simulation results, frontal loading chromatography was performed [..⁴⁵] as described in Section 3.5. Using a highly pure feedstock was found to be essential for demonstrating the behavior of individual species in the dilute limit. Various model proteins were tested with AEX and CEX resins, but only lysozyme was found to be readily prepared in sufficient purity. It was therefore used with SP Sepharose FF, despite the fact that most mAb flow-through purification processes are performed with AEX resins. Figure 5 shows breakthrough profiles acquired by loading lysozyme onto SP Sepharose FF at $10 \mu\text{g}/\text{ml}$ under high and low ionic strength conditions. The flow rate was varied to change the value of the Graetz number, and an increase in breakthrough volume was observed at lower flow rates. Equation 13 indicates that transport parameters should have a more pronounced effect on the initial breakthrough volume when retention is stronger, due to the K_{eq} weighting of $f\%$. This is consistent with the observed behavior at low ionic strength, where K_{eq} is higher. Column models with fit parameters showed excellent agreement at high ionic strength.

⁴⁵removed: using dilute feeds

437 Although not perfect, the agreement was also quantitatively close at low
 438 ionic strength. Discrepancies from simulation under these conditions may
 439 be attributable to feedstock component separation, as well as inaccuracies
 440 in describing extra-column effects with the simplified model of a CSTR in
 441 series with a PFR, which are more pronounced at low flow rates.

442 The breakthrough volume correlation was also qualitatively validated us-
 443 ing FITC-lysozyme in the presence of a mAb. As with lysozyme measure-
 444 ments, the flow rate was varied to change the value of the correlation variable
 445 under conditions of weak FITC-lysozyme retention. Figure 6 shows break-
 446 through profiles that were computed from absorbance measurements at 495
 447 and 280 nm, using the average FITC-lysozyme label ratio estimated during
 448 fractionation of the conjugation products. Appreciable measurement noise
 449 is apparent in the FITC-lysozyme profiles due to the low load concentra-
 450 tion of $\sim 10 \mu\text{g/ml}$. Nonetheless, the observed trend is consistent with the
 451 previous results: using lower flow rates delayed the onset of FITC-lysozyme
 452 breakthrough. This was not modeled explicitly due to the multicomponent
 453 nature of the FITC-lysozyme conjugation products, but it does support the
 454 breakthrough volume correlation qualitatively.

455 4.3. Correlation of SDM parameters

456 A knowledge of phenomenological properties is required to estimate break-
 457 through volumes using Equation 13, specifically values of D_p , D_s , and K_{eq} .
 458 However, such information is typically unknown for impurities such as HCPs
 459 on IEX resins. Methods of estimating these properties could therefore be
 460 useful, and some heuristics already exist for estimating the two intraparti-
 461 cle diffusivities. For instance, D_s is typically an order of magnitude smaller

than D_p under the relevant conditions of weak adsorption, and D_p should theoretically scale with the free solution diffusivity, D_0 , according to [19]:

$$D_p = \frac{\varepsilon_p \psi_p}{\tau_p} D_0 \quad (14)$$

where ψ_p and τ_p are the diffusional hindrance coefficient and the resin tortuosity factor, respectively. If a putative weakly adsorbing HCP has been identified, its molar mass may be used with the Stokes-Einstein equation or correlations to estimate D_0 [27]. Appreciable uncertainty surrounds the value of ψ_p/τ_p , but 0.2 appears to be representative of its order of magnitude [40]. Assuming a value like this enables rough estimation of D_p and D_s based on protein mass.

This leaves the estimation of K_{eq} , which varies with the solution conditions, as the main obstacle to applying the breakthrough volume correlation in practice. It is expected that K_{eq} will follow a power law in ionic strength of the SDM form, but the dependence on pH is less well defined. Several electrostatics models have been proposed for describing this behavior, but doing so predictively remains an open problem. In the absence of such predictive tools, insights may be drawn from experimental data on the retention of model proteins. To facilitate observation of system-independent trends, isocratic k' measurements at different ionic strengths were consolidated from the extant literature on 230 protein-pH-resin combinations, as shown in Supplementary Figure S2 [and the accompanying spreadsheet](#) [21, 30, 41–48]. These data were regressed according to Equation 9 to extract the SDM parameter ν and the quasi-SDM parameter $\phi\alpha$, which are plotted against each other in Figure 7 and observed to follow a significant intrinsically linear correlation (as determined by regressor t-tests).

486 This previously unobserved correlation is expected to be a consequence of
 487 adsorption thermodynamics rather than resin morphology, so the true rela-
 488 tionship represented in Figure 7 is suspected to be between ν and α . Inverse
 489 size exclusion chromatography data are unavailable for the majority of the
 490 resins studied, which precludes estimation of ϕ values that are specific to
 491 protein-resin pairs. However, all phase ratios are expected to be of compara-
 492 ble magnitude, and α may span several orders of magnitude, so the inclusion
 493 of ϕ is not expected to introduce much noise in the correlation. The fact
 494 that $\phi\alpha$ spans several orders of magnitude makes the prediction interval ap-
 495 preciable broad in terms of absolute values, and explaining some of the noise
 496 with additional factors would be advantageous. The ion-exchange type was
 497 tested for this purpose, and a significant difference was found between the
 498 correlations for AEX and CEX isocratic data (by including an interaction
 499 with the categorical variable). The mechanisms underlying this difference
 500 are not understood.

501 The utility of these relationships lies in their ability to remove one degree
 502 of freedom from the analysis of retention data. A series of measurements
 503 are usually performed to estimate SDM parameters, either from isocratic
 504 retention at different ionic strengths or elution peak ionic strength under
 505 linear gradient salt elutions of different volumes. The identified correlation
 506 could potentially enable the estimation of SDM parameters from only one
 507 experimental measurement. This concept is illustrated in Figure 8, which
 508 shows linear gradient elution data for lysozyme on SP Sepharose FF, collected
 509 as part of this study, plotted in the regression space for Yamamoto’s GH
 510 analysis [31]. Juxtaposed with these data are predictions from the correlation

511 of isocratic CEX SDM parameters. Close agreement is observed between
 512 predictions and experiment at each of the pH values tested. One point in each
 513 series would be sufficient to estimate roughly the value of ν , and therefore
 514 that of $\phi\alpha$ when using the correlation. However, because the uncertainty in
 515 $\phi\alpha$ is with respect to its order of magnitude, the absolute value of its estimate
 516 needs to be interpreted with caution.

517 The linear gradient elution data were regressed according to Yamamoto's
 518 method, and the SDM parameters are plotted in Figure 7. Analogous CEX
 519 gradient elution data for a mAb and its aggregates that had relatively large
 520 SDM parameters were also obtained from the literature and included in Fig-
 521 ure 7 [49]. Both sets of gradient elution data are consistent with the correla-
 522 tion of isocratic CEX data within the 95% prediction interval. This confirms
 523 the correlation's utility in removing a degree of freedom from the analysis of
 524 retention data. Unfortunately, it does not eliminate the need for some ex-
 525 perimental data in estimating K_{eq} , but it may reduce the burden of doing so.
 526 As proteomic techniques advance, it may become possible to quantitatively
 527 measure HCP retention. This would foreseeably be an expensive operation,
 528 and it may be essential to minimize the number of requisite measurements.
 529 The SDM parameter correlation may be useful in such an application.

530 From an intuitive perspective, the essential features of this correlation ap-
 531 pear to be broadly consistent with theory. If the characteristic charge indeed
 532 represents the number of attractive point charge interactions between the
 533 protein and the IEX resin, it seems reasonable to hypothesize that increas-
 534 ing this number at constant ionic strength would result in an approximately
 535 proportional increase in the adsorption free energy. This would result in an

536 order-of-magnitude increase in K_{eq} , which at the unit concentration of ionic
 537 strength is equivalent to α ; such an argument may rationalize the positive
 538 and log-linear correlation between ν and $\phi\alpha$. The reality is necessarily more
 539 complex, however, as the adsorption free energy would theoretically be a
 540 function of the pH, resin, protein, and the protein's adsorbed orientation.
 541 These are incorporated in a statistical thermodynamic calculation of K_{eq} in
 542 Equation 10, albeit implicitly with respect to the resin and protein species.
 543 Perhaps the dependence on all four variables can be generalized approxi-
 544 mately by the characteristic charge, but this would require evaluation and
 545 proof using a rigorous biophysical model. Developing that proof, or at least
 546 exhibiting behavior that is consistent with the empirical SDM parameter cor-
 547 relation (Figure 7), may provide a good validity test for molecular adsorption
 548 models.

549 **5. Conclusions**

550 Unlike concentrated solutes, the approximately linear chromatographic
 551 behavior of dilute impurities can lead to diffuse breakthrough. This can
 552 make it challenging to remove flow-through impurities completely, but it
 553 also enables breakthrough volumes to be analytically related to phenomeno-
 554 logical properties. Specifically, the Graetz number can describe transport
 555 contributions to dilute solute breakthrough volumes generally when an effec-
 556 tive intraparticle diffusivity is used. Knowledge of this relationship enables
 557 a problematic equilibrium constant threshold to be estimated, which is on
 558 the order of 400 for typical process conditions. However, for this to be used
 559 in practice, the IEX adsorption equilibria of impurities of interest must be

560 known. The correlation of SDM model parameters may be useful in estimat-
561 ing such data approximately from one linear gradient elution measurement,
562 and it may serve as a validity test for molecular adsorption models as well.

563 **Acknowledgements**

564 We thank Bristol Myers Squibb for providing materials and financial sup-
565 port. We also thank the CADET developers for making their work free and
566 open source, and for providing pedagogical support.

567 **Declaration of competing interest**

568 The authors declare that they have no known competing financial inter-
569 ests or personal relationships that could have appeared to influence the work
570 reported in this paper.

571 **CRedit authorship contribution statement**

572 **Chase E. Herman:** Conceptualization, Data curation, Formal analy-
573 sis, Investigation, Methodology, Validation, Visualization, Writing - origi-
574 nal draft. **Xuankuo Xu:** Conceptualization, Funding acquisition, Project
575 administration, Resources. **Steven J. Traylor:** Conceptualization, Re-
576 sources. **Sanchayita Ghose:** Resources. **Zheng Jian Li:** Resources.
577 **Abraham M. Lenhoff:** Conceptualization, Formal analysis, Funding ac-
578 quisition, Project administration, Supervision, Writing - review & editing.

579 **ORCID**

Chase E. Herman: <https://orcid.org/0000-0002-9989-9604>

Xuankuo Xu: <https://orcid.org/0000-0002-5557-0284>

580 **Steven Traylor:** <https://orcid.org/0000-0002-9433-0048>

Zheng Jian Li: <https://orcid.org/0000-0002-1941-4145>

Abraham M. Lenhoff: <https://orcid.org/0000-0002-7831-219X>

581 **Supplementary material**

582 Supplementary material is associated with this article.

583 **References**

584 [1] G. Walsh, Biopharmaceutical benchmarks 2018, Nature biotechnology
585 36 (12) (2018) 1136–1145. doi:10.1038/nbt.4305.

586 [2] R.-M. Lu, Y.-C. Hwang, I.-J. Liu, C.-C. Lee, H.-Z. Tsai, H.-J. Li,
587 H.-C. Wu, Development of therapeutic antibodies for the treatment
588 of diseases, Journal of Biomedical Science 27 (1) (2020) 1–30. doi:
589 10.1186/s12929-019-0592-z.

590 [3] L. Allen, The Evolution of Platform Technologies for the Downstream
591 Processing of Antibodies, in: U. Gottschalk (Ed.), Process Scale Purifi-
592 cation of Antibodies, 2nd Edition, John Wiley & Sons, Inc., Hoboken,
593 NJ, USA, 2017, pp. 365–389. doi:10.1002/9781119126942.ch17.

594 [4] A. A. Shukla, L. S. Wolfe, S. S. Mostafa, C. Norman, Evolving trends
595 in mAb production processes, Bioengineering & Translational Medicine
596 2 (1) (2017) 58–69. doi:10.1002/btm2.10061.

- 597 [5] N. E. Levy, K. N. Valente, K. H. Lee, A. M. Lenhoff, Host cell pro-
598 tein impurities in chromatographic polishing steps for monoclonal an-
599 tibody purification, *Biotechnology and Bioengineering* 113 (6) (2016)
600 1260–1272. doi:10.1002/bit.25882.
- 601 [6] M. Jones, N. Palackal, F. Wang, G. Gaza-Bulseco, K. Hurkmans,
602 Y. Zhao, C. Chitikila, S. Clavier, S. Liu, E. Menesale, N. S. Scho-
603 nenbach, S. Sharma, P. Valax, T. Waerner, L. Zhang, T. Connolly,
604 High-risk host cell proteins (HCPs): A multi-company collaborative
605 view, *Biotechnology and Bioengineering* 118 (8) (2021) 2870–2885.
606 doi:10.1002/bit.27808.
- 607 [7] R. Molden, M. Hu, S. Yen E., D. Saggese, J. Reilly, J. Mattila, H. Qiu,
608 G. Chen, H. Bak, N. Li, Host cell protein profiling of commercial
609 therapeutic protein drugs as a benchmark for monoclonal antibody-
610 based therapeutic protein development, *mAbs* 13 (1) (2021) e1955811.
611 doi:10.1080/19420862.2021.1955811.
- 612 [8] M. Jin, N. Szapiel, J. Zhang, J. Hickey, S. Ghose, Profiling of host cell
613 proteins by two-dimensional difference gel electrophoresis (2D-DIGE):
614 Implications for downstream process development, *Biotechnology and*
615 *Bioengineering* 105 (2) (2009) 306–316. doi:10.1002/bit.22532.
- 616 [9] B. D. Kelley, S. A. Tobler, P. Brown, J. L. Coffman, R. Godavarti,
617 T. Iskra, M. Switzer, S. Vunnum, Weak partitioning chromatography
618 for anion exchange purification of monoclonal antibodies, *Biotechnology*
619 *and Bioengineering* 101 (3) (2008) 553–566. doi:10.1002/bit.21923.

- [10] H. F. Liu, J. Ma, C. Winter, R. Bayer, Recovery and purification process development for monoclonal antibody production, *mAbs* 2 (5) (2010) 480–499. doi:10.4161/mabs.2.5.12645.
- [11] T. Ichihara, T. Ito, Y. Kurisu, K. Galipeau, C. Gillespie, Integrated flow-through purification for therapeutic monoclonal antibodies processing, *mAbs* 10 (2) (2018) 325–334. doi:10.1080/19420862.2017.1417717.
- [12] J. Schwellenbach, S. Zobel, F. Taft, L. Villain, J. Strube, Purification of monoclonal antibodies using a fiber based cation-exchange stationary phase: Parameter determination and modeling, *Bioengineering* 3 ([.46]24) (2016) 1–20. doi:10.3390/bioengineering3040024.
- [13] H. Trnovec, T. Doles, G. Hribar, N. Furlan, A. Podgornik, Characterization of membrane adsorbers used for impurity removal during the continuous purification of monoclonal antibodies, *Journal of Chromatography A* 1609 (460518) (2020) 1–13. doi:10.1016/j.chroma.2019.460518.
- [14] T. Ichihara, T. Ito, C. Gillespie, Polishing approach with fully connected flow-through purification for therapeutic monoclonal antibody, *Engineering in Life Sciences* 19 (2019) 31–36. doi:10.1002/elsc.201800123.
- [15] O. Khanal, A. M. Lenhoff, Developments and opportunities in continuous biopharmaceutical manufacturing, *mAbs* 13 (1) (2021) 1903664. doi:10.1080/19420862.2021.1903664.

⁴⁶removed: 4

- [16] Q. Zhang, A. M. Goetze, H. Cui, J. Wylie, S. Trimble, A. Hewig, G. C. Flynn, Comprehensive tracking of host cell proteins during monoclonal antibody purifications using mass spectrometry, *mAbs* 6 (3) (2014) 659–670. doi:10.4161/mabs.28120.
- [17] S. Hasegawa, C.-S. Chen, N. Yoshimoto, S. Yamamoto, Accelerated method for designing flow-through chromatography of proteins, *Journal of Chemical Engineering of Japan* 53 (5) (2020) 206–213. doi:10.1252/jcej.20we002.
- [18] S. Hasegawa, C.-S. Chen, N. Yoshimoto, S. Yamamoto, Optimization of flow-through chromatography of proteins, *Journal of Chemical Engineering of Japan* 53 (5) (2020) 214–221. doi:10.1252/jcej.20we003.
- [19] G. Carta, A. Jungbauer, Protein chromatography: Process development and scale-up, WILEY-VCH Verlag GmbH & Co. KGaA, Weinheim, Germany, 2010.
- [20] H. Schmidt-Traub, M. Schulte, A. Seidel-Morgenstern (Eds.), Preparative Chromatography, 2nd Edition, WILEY-VCH Verlag GmbH & Co. KGaA, Weinheim, Germany, 2012.
- [21] P. DePhillips, A. M. Lenhoff, Determinants of protein retention characteristics on cation-exchange adsorbents, *Journal of Chromatography A* 933 (2001) 57–72. doi:10.1016/S0021-9673(01)01275-4.
- [22] N. K. Boardman, S. M. Partridge, Separation of Neutral Proteins on Ion-Exchange Resins, *Biochemical Journal* 59 (1955) 543–552. doi:10.1038/171208a0.

- 664 [23] G. Guiochon, A. Felinger, D. G. Shirazi, A. M. Katti, Fundamentals of
665 Preparative and Nonlinear Chromatography, Elsevier Academic Press,
666 San Diego, CA, USA, 2006.
- 667 [24] V. Kumar, A. M. Lenhoff, Mechanistic Modeling of Preparative Col-
668 umn Chromatography for Biotherapeutics, Annual Review of Chemi-
669 cal and Biomolecular Engineering 11 (2020) 235–255. doi:10.1146/
670 annurev-chembioeng-102419-125430.
- 671 [25] S. Leweke, E. von Lieres, Chromatography analysis and design toolkit
672 (CADET), Computers and Chemical Engineering 113 (2018) 274–294.
673 doi:10.1016/j.compchemeng.2018.02.025.
- 674 [26] N. Han, J. Bhakta, R. G. Carbonell, Longitudinal and lateral dispersion
675 in packed beds: Effect of column length and particle size distribution,
676 AIChE Journal 31 (2) (1985) 277–288. doi:10.1002/aic.690310215.
- 677 [27] M. E. Young, P. A. Carroad, R. L. Bell, Estimation of diffusion co-
678 efficients of proteins, Biotechnology and Bioengineering 22 (5) (1980)
679 947–955. doi:10.1002/bit.260220504.
- 680 [28] O. Khanal, V. Kumar, F. Schlegel, A. M. Lenhoff, Estimating and
681 leveraging protein diffusion on ion-exchange resin surfaces, Proceed-
682 ings of the National Academy of Sciences 117 (13) (2020) 7004–7010.
683 doi:10.1073/pnas.1921499117.
- 684 [29] H. Yoshida, M. Yoshikawa, T. Kataoka, Parallel transport of BSA by
685 surface and pore diffusion in strongly basic chitosan, AIChE Journal
686 40 (12) (1994) 2034–2044. doi:10.1002/aic.690401213.

- 687 [30] V. Kumar, S. Leweke, E. von Lieres, A. S. Rathore, Mechanistic model-
688 ing of ion-exchange process chromatography of charge variants of mon-
689 oclonal antibody products, *Journal of Chromatography A* 1426 (2015)
690 140–153. doi:10.1016/j.chroma.2015.11.062.
- 691 [31] S. Yamamoto, M. Nomura, Y. Sano, Adsorption chromatography of
692 proteins: Determination of optimum conditions, *AIChE Journal* 33 (9)
693 (1987) 1426–1434. doi:10.1002/aic.690330903.
- 694 [32] D. Asthagiri, A. M. Lenhoff, Influence of Structural Details in Modeling
695 Electrostatically Driven Protein Adsorption, *Langmuir* 13 (25) (1997)
696 6761–6768. doi:10.1021/la970608u.
- 697 [33] B. Guélat, G. Ströhlein, M. Lattuada, L. Delegrange, P. Valax, M. Mor-
698 bidelli, Simulation model for overloaded monoclonal antibody variants
699 separations in ion-exchange chromatography, *Journal of Chromatogra-*
700 *phy A* 1253 (2012) 32–43. doi:10.1016/j.chroma.2012.06.081.
- 701 [34] T. Briskot, T. Hahn, T. Huuk, J. Hubbuch, Adsorption of colloidal
702 proteins in ion-exchange chromatography under consideration of charge
703 regulation, *Journal of Chromatography A* 1611 (2020) 460608. doi:
704 10.1016/j.chroma.2019.460608.
- 705 [35] B. J. Kuipers, H. Gruppen, Prediction of molar extinction coefficients
706 of proteins and peptides using UV absorption of the constituent amino
707 acids at 214 nm to enable quantitative reverse phase high-performance
708 liquid chromatography-mass spectrometry analysis, *Journal of Agricul-*

- 709 tural and Food Chemistry 55 (14) (2007) 5445–5451. doi:10.1021/
710 jf0703371.
- 711 [36] M. D. LeVan, G. Carta, C. M. Yon, Adsorption and ion exchange, in: R. H.
712 Perry, D. W. Green, J. O. Maloney (Eds.), Perry's chemical engineers' hand-
713 book, 7th Edition, McGraw-Hill, New York, NY, USA, 1997, pp. 16–15.
- 714 [37] C.-S. Chen, N. Yoshimoto, S. Yamamoto, Prediction of the performance
715 of capture chromatography processes of proteins and its application to
716 the repeated cyclic operation optimization, Journal of Chemical Engi-
717 neering of Japan 53 (11) (2020) 689–697. doi:10.1252/JCEJ.20WE116.
- 718 [38] J. A. Wesselingh, J. C. Bosma, Protein ion-exchange adsorption kinetics,
719 AIChE Journal 47 (7) (2001) 1571–1580. doi:10.1002/aic.690470710.
- 720 [39] A. M. Lenhoff, Multiscale modeling of protein uptake patterns in chromato-
721 graphic particles, Langmuir 24 (12) (2008) 5991–5995. doi:10.1021/
722 la8004163.
- 723 [40] J. M. Angelo, A. M. Lenhoff, Determinants of protein elution rates
724 from preparative ion-exchange adsorbents, Journal of Chromatography
725 A 1440 (2016) 94–104. doi:10.1016/j.chroma.2016.02.048.
- 726 [41] A. Staby, I. H. Jensen, I. Møllerup, Comparison of chromatographic ion-
727 exchange resins I. Strong anion-exchange resins, Journal of Chromatog-
728 raphy A 897 (2000) 99–111. doi:10.1016/S0021-9673(00)00780-9.
- 729 [42] A. Staby, I. H. Jensen, Comparison of chromatographic ion-exchange
730 resins II. More strong anion-exchange resins, Journal of Chromatogra-
731 phy A 908 (2001) 149–161. doi:10.1016/S0021-9673(00)00999-7.

- 732 [43] A. Staby, M.-B. Sand, R. G. Hansen, J. H. Jacobsen, L. A. Andersen,
733 M. Gerstenberg, U. K. Bruus, I. H. Jensen, Comparison of chromato-
734 graphic ion-exchange resins: III. Strong cation-exchange resins, Jour-
735 nal of Chromatography A 1034 (2004) 85–97. doi:10.1016/j.chroma.
736 2004.01.026.
- 737 [44] A. Staby, M.-B. Sand, R. G. Hansen, J. H. Jacobsen, L. A. Andersen,
738 M. Gerstenberg, U. K. Bruus, I. H. Jensen, Comparison of chromato-
739 graphic ion-exchange resins: IV. Strong and weak cation-exchange resins
740 and heparin resins, Journal of Chromatography A 1069 (2005) 65–77.
741 doi:10.1016/j.chroma.2004.11.094.
- 742 [45] A. Staby, J. H. Jacobsen, R. G. Hansen, U. K. Bruus, I. H. Jensen,
743 Comparison of chromatographic ion-exchange resins. V. Strong and
744 weak cation-exchange resins, Journal of Chromatography A 1118 (2006)
745 168–179. doi:10.1016/j.chroma.2006.03.116.
- 746 [46] A. Staby, R. H. Jensen, M. Bensch, J. Hubbuch, D. L. Dünweber,
747 J. Krarup, J. Nielsen, M. Lund, S. Kidal, T. B. Hansen, I. H. Jensen,
748 Comparison of chromatographic ion-exchange resins. VI. Weak anion-
749 exchange resins, Journal of Chromatography A 1164 (2007) 82–94.
750 doi:10.1016/j.chroma.2007.06.048.
- 751 [47] P. DePhillips, A. M. Lenhoff, Relative retention of the fibroblast growth
752 factors FGF-1 and FGF-2 on strong cation-exchange sorbents, Journal of
753 Chromatography A 1036 (2004) 51–60. doi:10.1016/j.chroma.2004.
754 01.012.

- 755 [48] J. Z. Bai, Characterization of protein retention and transport in an-
756 ion exchange chromatography, Master's thesis, University of Delaware,
757 Newark, DE, USA (1999).
- 758 [49] D. Saleh, G. Wang, B. Müller, F. Rischawy, S. Kluters, J. Studts, J. Hub-
759 buch, Straightforward method for calibration of mechanistic cation ex-
760 change chromatography models for industrial applications, *Biotechnol-
761 ogy Progress* 36 (4) (2020) e2984. doi:10.1002/btpr.2984.