



**DataCamp**

*Learning by doing*

# Introduction

- In this lecture, 4 tests, each compare means
  - z-test
  - t-test (single sample)
  - t-test (dependent)
  - t-test (independent)

# Introduction

- $z = (\text{Observed} - \text{Expected}) / \text{SE}$
- $t = (\text{Observed} - \text{Expected}) / \text{SE}$ 
  - SE: Standard error

# When to use z and t?

- z-test
  - When comparing a sample mean to a population mean and the standard deviation of the population is known
- Single sample t-test
  - When comparing a sample mean to a population mean and the standard deviation of the population is not known

# When to use z and t?

- Dependent t-test
  - When evaluating the difference between two related samples
- Independent t-test
  - When evaluating the difference between two independent samples

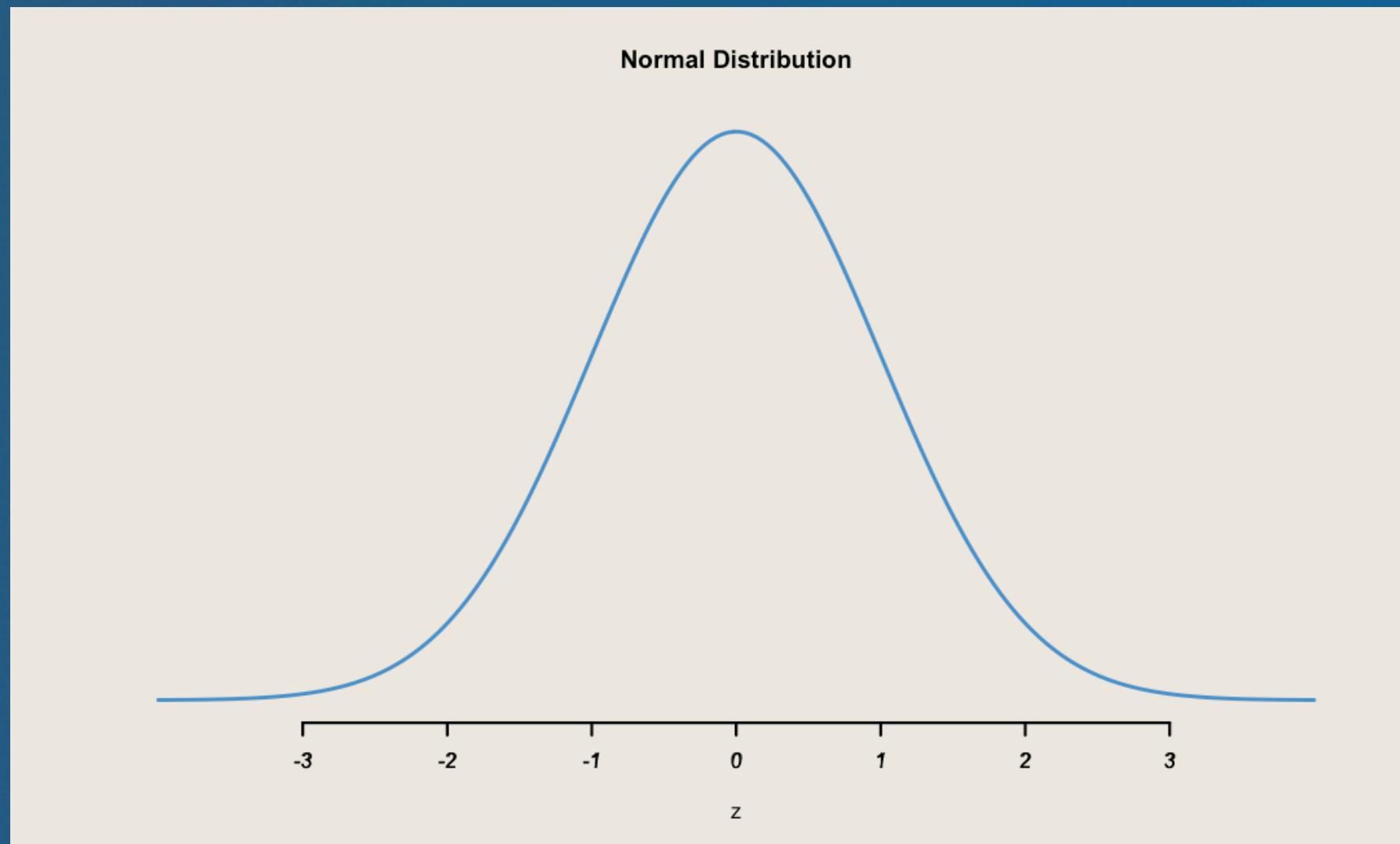
# Observed, Expected, and SE

	Observed	Expected	SE
z	Sample mean	Population mean	SE of the mean
t (single sample)	Sample mean	Population mean	SE of the mean
t (dependent)	Sample mean of difference scores	Population mean of difference scores	SE of the mean difference
t (independent)	Difference between two sample means	Difference between two population means	SE of the difference between Ms

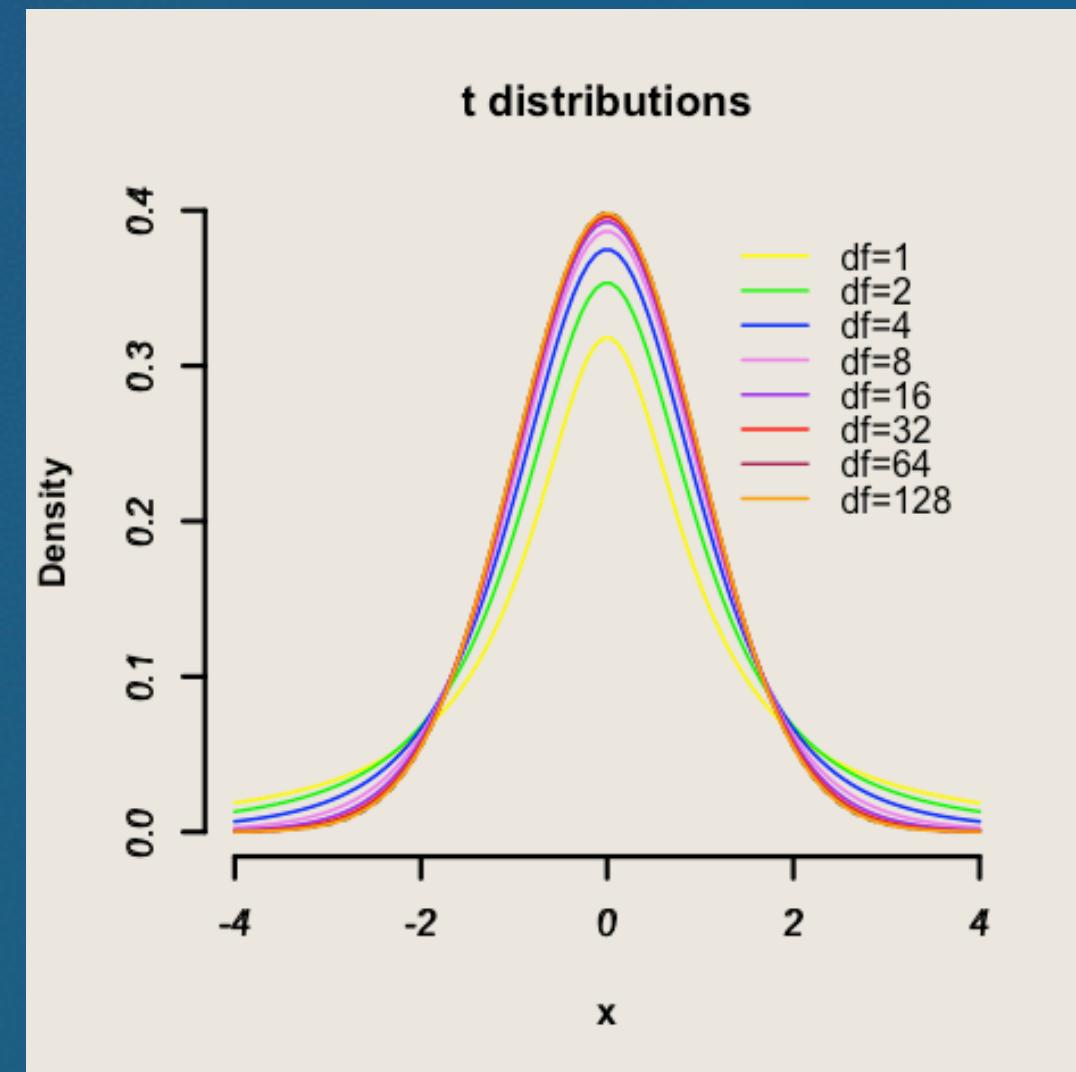
# p-values for z and t

- Exact p-value depends on:
  - Directional or non-directional test
  - Degrees of freedom (df)
    - Different t-distributions for different sample sizes

# z distribution



# Family of t distributions



# Degrees of freedom (df)

	<b>df</b>
z	NA
t (single sample)	N-1
t (dependent)	N-1
t (independent)	$(N_1 - 1) + (N_2 - 1)$

# Segment summary

- $z = (\text{Observed} - \text{Expected}) / \text{SE}$
- $t = (\text{Observed} - \text{Expected}) / \text{SE}$ 
  - SE: Standard error

# Dependent t-test

- Also known as paired samples t-test
  - Appropriate when the same subjects are being compared
    - For example, pre/post design
  - Or when two samples are matched at the level of individual subjects
    - Allowing for a difference score to be calculated

# Dependent t-test

- A thorough analysis will include
  - t-value
  - p-value
  - Cohen's d (effect size)
  - Confidence interval (interval estimate)

# Dependent t-test

- t-value
  - $t = (\text{Observed} - \text{Expected}) / \text{SE}$
  - $t = (M - 0) / \text{SE} = M / \text{SE}$

# Dependent t-test

- p-value
  - Based on t-value and the t-distribution
  - Directional or non-directional test

# Dependent t-test

- Cohen's d
  - $d = M / SD$

# Dependent t-test

- Confidence interval
  - Upper bound =  $M + t (SE)$
  - Lower bound =  $M - t (SE)$
  - t-value depends on level of confidence and t-distribution