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IVP Assignment 3

```
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```

Creating a new environment

```
clc;
clear all;
close all;
```

Functions Created: sharpening_with_laplacian_filter

```
% Function that sharpens the image using Laplacian via the Frequency
Domain

function [img] = sharpening_with_laplacian_filter(image)
    % image: We assume that it is a grayscale image.

    dft_image = fftshift(fft2(image));
    [row, col] = size(dft_image);
    mid_row = (1 + row) / 2;
    mid_col = (1 + col) / 2;
    filter = zeros(size(dft_image));

    % Creates the laplacian filter for image sharpening.
    for i = 1:row
```

```

        for j = 1:col
            filter(i, j) = 1 + 4*pi^2*((mid_row - i)^2 + (mid_col-
j)^2);
        end
    end

    % ifftshift shifts the fft2d back and then perform the idft.
    img = real(ifft2(ifftshift(filter .* double(dft_image))));

```

Functions Created: low_pass_gaussian_filter_smoothering

```

% Function that smoothes the image using a low pass gaussian filter

function [img] = low_pass_gaussian_filter_smoothering(image, var)
    % image: We assume that it is a grayscale image.
    % var: Gives the variance of the 2D gaussian distribution.

    dft_image = fftshift(fft2(image));
    [row, col] = size(dft_image);
    mid_row = (1 + row) / 2;
    mid_col = (1 + col) / 2;
    filter = zeros(size(dft_image));

    % Creates the low pass gaussian filter for smothering.
    for i = 1:row
        for j = 1:col
            filter(i, j) = exp(-((mid_row - i)^2 + (mid_col-j)^2) / (2
* var^2));
        end
    end

    % ifftshift shifts the fft2d back and then perform the idft.
    img = real(ifft2(ifftshift(filter .* dft_image)));

```

Functions Created: high_pass_gaussian_filter_sharpening

```

% Function that sharpens the image using a high pass gaussian filter

function [img] = high_pass_gaussian_filter_sharpening(image, var)
    % image: We assume that it is a grayscale image.
    % var: Gives the variance of the 2D gaussian distribution.

```

```

dft_image = fftshift(fft2(image));
[row, col] = size(dft_image);
mid_row = (1 + row) / 2;
mid_col = (1 + col) / 2;
filter = zeros(size(dft_image));

% Creates the high pass gaussian filter for sharpening.
for i = 1:row
    for j = 1:col
        filter(i, j) = 1- exp(-((mid_row - i)^2 + (mid_col-
j)^2) ...
                        / (2 * var^2));
    end
end

% ifftshift shifts the fft2d back and then perform the idft.
img = real(ifft2(ifftshift(filter .* dft_image)));

```

Functions Created: erosion

```

% Function that performs the morphological operation erosion and
% returns
% the processed image.

function [img] = erosion(image, struct_elem)
    % image: Contains the binary image
    % struct_elem: Contains the structuring element upon which the
    % morphological operation is being done. The assumption is that
    the
    % struct_elem is odd.

    % The logic is that if we take the structuring element and
    multiply it
    % with the same window of the original image (element wise) and if
    the
    % sum of that is equal to the sum of all the values in the
    structuring
    % element then it means A intersection B is true for the entire
    region.
    % Else it is false

    img = uint8(zeros(size(image)));
    [row_img, col_img] = size(image);
    [row_struct_elem, col_struct_elem] = size(struct_elem);

    mid_row = double(uint8((row_struct_elem + 1) / 2));
    mid_col = double(uint8((col_struct_elem + 1) / 2));
    sum_struct_elem = sum(sum(struct_elem));

```

```

        for i = 1:(row_img - row_struct_elem + 1)
            for j = 1:(col_img - col_struct_elem + 1)
                sum_ = image(i:(i+row_struct_elem-1), j:(j
+col_struct_elem-1)) ...
                    .* struct_elem;
                sum_ = sum(sum(sum_));
                if (sum_ == sum_struct_elem)
                    img((i+mid_row-1), (j+mid_col-1)) = 1;
                end
            end
        end
    end
end

```

Functions Created: dilation

```

% Function that performs the morphological operation dilation and
% returns
% the processed image.

function [img] = dilation(image, struct_elem)
    % image: Contains the binary image
    % struct_elem: Contains the structuring element upon which the
    % morphological operation is being done. The assumption is that
    the
    % struct_elem is odd.

    % The logic is that if we take the structuring element and
    multiply it
    % with the same window of the original image (element wise) and if
    the
    % sum of that is greater than 0, then it means that A intersection
    B
    % lies in A.

    img = zeros(size(image));
    [row_img, col_img] = size(image);
    [row_struct_elem, col_struct_elem] = size(struct_elem);

    mid_row = double(uint8((row_struct_elem + 1) / 2));
    mid_col = double(uint8((col_struct_elem + 1) / 2));

    for i = 1:(row_img - row_struct_elem + 1)
        for j = 1:(col_img - col_struct_elem + 1)
            sum_ = image(i:i+row_struct_elem-1, j:j
+col_struct_elem-1) ...
                .* struct_elem;
            sum_ = sum(sum(sum_));
            if (sum_ > 0)
                img(i+mid_row-1, j+mid_col-1) = 1;
            end
        end
    end
end

```

```
        end
    end
end

end
```

Image Imports

```
lena = imread('C:\Chanakya\Projects\ivp-assignments
\Assignment-3\images\lena_gray_256.tif');
orig_fingerprint = rgb2gray(imread('C:\Chanakya\Projects\ivp-
assignments\Assignment-3\images\fingerprint.jpg'));
```

Sharpening using the Laplacian Filter

The image can be sharpened in both the time domain and the frequency domain. In this case we convert the Laplacian to the frequency domain sharpen it and then convert it back to the time domain via the inverse dft transform. We use the following in the frequency domain:

$$H(u, v) = (1 + 4 * \pi^2 * (u^2 + v^2))(F(u, v))$$

```
% Calling the sharpening_with_laplacian_filter function
sharpened_lena_laplacian = sharpening_with_laplacian_filter(lena);

% Plotting the images
figure('Name', 'Sharpening using Laplacian Filter', 'units', ...
    'normalized', 'outerposition', [0 0 1 1]);

subplot(1,2,1)
imshow(lena);
title('Original Image');

subplot(1,2,2)
imshow((mat2gray(uint8(sharpened_lena_laplacian))));
title('Sharpening using the Laplacian Filter');
```



Smoothing using the Low Pass Gaussian Filter

The images can be blurred via the frequency domain via the Low Pass Gaussian Filter. The smoothed image can be obtained via the IDFT after filtration.

$$H(u, v) = \exp \frac{-D(u, v)^2}{2 \cdot D_0^2} * F(u, v)$$

```
% Calling the low_pass_gaussian_filter_smoothing function
smoothened_lena = low_pass_gaussian_filter_smoothing(lena, 10);

% Plotting the images
figure('Name', 'Smoothing using LPG Filter', 'units', ...
      'normalized', 'outerposition', [0 0 1 1]);

subplot(1,2,1)
imshow(lena);
title('Original Image');

subplot(1,2,2)
imshow((mat2gray(uint8(smoothened_lena))));
title('Smoothing using the LPG Filter');
```



Sharpening Using the High Pass Gaussian Filter

The images can be sharpened via the frequency domain via the High Pass Gaussian Filter. The smoothed image can be obtained via the IDFT after filtration.

$$H(u, v) = (1 - \exp^{\frac{-D(u,v)^2}{2 \cdot D_0^2}}) * F(u, v)$$

```
% Calling the high_pass_gaussian_filter_sharpening function
sharpened_lena_hpg = high_pass_gaussian_filter_sharpening(lena, 10);

% Plotting the images
figure('Name', 'Sharpening using HPG Filter', 'units', ...
      'normalized', 'outerposition', [0 0 1 1]);

subplot(1,2,1)
imshow(lena);
title('Original Image');

subplot(1,2,2)
imshow((mat2gray(uint8(sharpened_lena_hpg))));
title('Sharpening using the HPG Filter');
```



Removing the noise using Opening: Erosion followed by dilation

Erosion and Dilation are operations that are done for basically removing unnecessary protrusions and filling in holes. Closing is used for filling in holes and then resizing the it back to the original image. Opening is used for removing protrusions and resizing the images back to the original images. The equations for opening and closing are as follows:

$$A \circ B = (A \ominus B) \oplus B$$

$$A \bullet B = (A \oplus B) \ominus B$$

```
% Creating the structuring element
struct_elem = uint8([0, 1, 0; 1, 1, 1; 0, 1, 0]);

% Making the fingerprint image a binary image
fingerprint = uint8(orig_fingerprint>128);

% Calling the erosion and dilation function
eroded_image = erosion(fingerprint, struct_elem);
dilated_image = dilation(fingerprint, struct_elem);

% Closing and Dilation
% Erosion and Dilation and are defined opposite here. That's because
the
% fingerprint is black and the outer region is white. Therefore, we
have to
% consider the opposite.
opening = dilation(uint8(erosion(fingerprint, struct_elem)),
    struct_elem);
closing = erosion(uint8(dilation(fingerprint, struct_elem)),
    struct_elem);
```

```
% Plotting the images
figure('Name', 'Erosion and Dilation', 'units', ...
      'normalized','outerposition', [0 0 1 1]);

subplot(2,3,1)
imshow(orig_fingerprint);
title('Original Image');

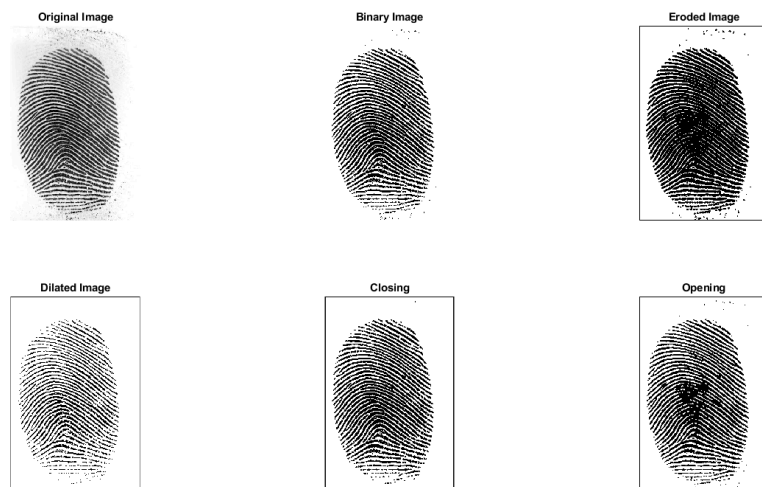
subplot(2,3,2)
imshow(mat2gray(fingerprint));
title('Binary Image');

subplot(2,3,3)
imshow((mat2gray(uint8(eroded_image))));
title('Eroded Image');

subplot(2,3,4)
imshow((mat2gray(uint8(dilated_image))));
title('Dilated Image');

subplot(2,3,5)
imshow((mat2gray(uint8(closing))));
title('Closing');

subplot(2,3,6)
imshow((mat2gray(uint8(opening))));
title('Opening');
```



Conclusion

From these experiments we can see that we can perform smoothening as well as sharpening via the frequency domain. We can observe that sometimes it is easier to process the image in the frequency domain. Moreover, we can also see that we can use operations like opening and closing to embellish the images.

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