Programming Language Concepts Syntax and Parsing

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■ if-then-else ambiguity

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Introduction

- Syntax: the form and structure of a program.
- Semantics: meaning of a program
- Language definitions are used by:
 - Programmers
 - Implementors of the language processors
 - Language designers

Definitions

- A sentence is a string of characters over some alphabet
- A language is a set of sentences
- A lexeme is the lowest level syntactic unit of the language (i.e. ++, int, total)
- A token is a category of lexemes (i.e. *identifier*)

Definitions

- syntax recognition: read input strings of the language and verify the input belonging to the language
- syntax generation: generate sentences of the language (i.e. from a given data structure)
- Compilers and interpreters recognize syntax and convert it into machine understandable form.

Backus-Naur Form and CFGs

- CFG's introduced by Noam Chomsky (mid 1950s)
- Programming languages are usually in context free language class
- BNF introduced by John Bakus and modified by Peter Naur for describing Algol language
- BNF is equivalent to CFGs. It is a meta-language that decribes other languages
- Extended BNF improves readability of BNF

A Grammar Rule

```
\langle \mathsf{while\_stmt} 
angle \; 	o \; \mathtt{while} \; ( \; \langle \mathsf{logic\_expr} 
angle \; ) \; \langle \mathsf{stmt} 
angle
```

- LHS is a non-terminal denoting an intermediate phrase
- LHS can be defined (rewritten) as the RHS sequence which can contain terminals (lexems and tokens) of the language and other non-terminals
- Non-terminals are denoted as strings enclosed in angle brackets.
- ::= may be used in BNF notation instead of the arrow
- is used to combine multiple rules with same LHS in a single rule

```
\langle lgc\_cons\rangle ::= \texttt{true} \quad \equiv \quad \langle lgc\_cons\rangle ::= \texttt{true} \mid \texttt{false} \langle lgc\_cons\rangle ::= \texttt{false}
```



Context Free Grammar

- A grammar G is defined as $G = (N, \Sigma, R, S)$:
 - N, finite set of non terminals
 - \blacksquare Σ , finite set of terminals
 - R is a set of grammar rules. A relation from N to $(N \cup \Sigma)^*$.
 - $S \in N$ the start symbol
- Application of a rule maps one sentential form into the other by replacing a non-terminal element in sentential form with its right handside seuqence in the rule, $u \mapsto v$.
- lacksquare Language of a grammar $L(G) = \left\{ w \mid w \in \Sigma^*, S \stackrel{*}{\mapsto} w
 ight\}$



 Recursive or list like structures can be represented using recursion

```
\begin{array}{l} \langle expr\_list \rangle \ \rightarrow \ \langle expr \rangle \ \ , \ \ \langle expr\_list \rangle \\ \langle btree \rangle \ \rightarrow \ \langle head \rangle \ \ ( \ \ \langle btree \rangle \ \ , \ \ \langle btree \rangle \ \ ) \end{array}
```

- A derivation starts with a starting non-terminal and rules are applied repeteadly to end with a sentence containing only terminal symbols.
- leftmost derivation: always leftmost non-terminal is chosen for replacement
- rightmost derivation: always rightmost non-terminal is chosen for replacement
- Same sentence can be derived using leftmost, rightmost, or other derivaionts.

Sample Grammar

```
\langle \mathsf{stmt} \rangle \to \langle \mathsf{id} \rangle = \langle \mathsf{expr} \rangle
\langle expr \rangle \rightarrow \langle expr \rangle \langle op \rangle \langle expr \rangle \mid \langle id \rangle
\langle \mathsf{op} \rangle \to + \mid *
\langle id \rangle \rightarrow a \mid b \mid c
```

Leftmost derivation of a = a * b :

$$\begin{array}{lll} \langle \textbf{stmt} \rangle \mapsto \langle \textbf{id} \rangle = \langle \textbf{expr} \rangle & \mapsto & \textbf{a} = \langle \textbf{expr} \rangle \\ \mapsto & \textbf{a} = \langle \textbf{id} \rangle \; \langle \textbf{op} \rangle \; \langle \textbf{expr} \rangle & \mapsto & \textbf{a} = \textbf{a} \; \langle \textbf{op} \rangle \; \langle \textbf{expr} \rangle \\ \mapsto & \textbf{a} = \textbf{a} \; * \; \langle \textbf{expr} \rangle & \mapsto & \textbf{a} = \textbf{a} \; * \; \langle \textbf{id} \rangle & \mapsto & \textbf{a} = \textbf{a} \; * \; \textbf{b} \end{array}$$

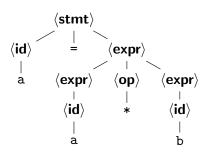
Rightmost derivation of a = a * b : $\langle \mathsf{stmt} \rangle \mapsto \langle \mathsf{id} \rangle = \langle \mathsf{expr} \rangle \quad \mapsto \quad \langle \mathsf{id} \rangle = \langle \mathsf{expr} \rangle \langle \mathsf{op} \rangle \langle \mathsf{expr} \rangle$ \mapsto $\langle id \rangle = \langle expr \rangle \langle op \rangle \langle id \rangle \mapsto \langle id \rangle = \langle expr \rangle \langle op \rangle b$ \mapsto $\langle id \rangle = \langle expr \rangle * b \mapsto \langle id \rangle = \langle id \rangle * b$ \mapsto $\langle id \rangle = a * b \mapsto a = a * b$

Parse Tree

- Steps of a derivation gives the structure of the sentence. This structure can be represented as a tree.
- All non-terminals used in derivation are intermediate nodes. Each grammar rule replaces the non-terminal node with is children. Root node is the start symbol.
- Terminal nodes are the leaf nodes.
- preorder traversal of leaf nodes gives the resulting sentence.
- leftmost and rightmos derivations can be retrieved by traversal of the tree.

Parse Tree Example

$$a = a * b$$

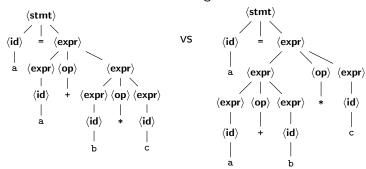


Parse Tree Generation

- A parse tree gives the structure of the program so semantics of the program is related to this structure.
- For example local scopes, evaluation order of expressions etc.
- During compilation, parse trees might be required for code generation, semantic analysis and optimization phases.
- After a parse tree generated, it can be traversed to do various tasks of compilation.
- The processing of parse tree takes too long, so creation of parse trees is usually avoided.
- Approaches like syntax directed translation combines parsing with code generation, semantic analysis etc..

Ambigous Grammars

■ Consider a = a + b * c in our grammar:



■ Both can be derived by the grammar!

- A grammar is called ambigous if same sentence can be derived by following different set of rules, thus resulting in a different parse tree
- If structure changes semantic meaning of the program, ambiguity is a serious problem.
- Even if not, which one is the result?
- i.e. Precedence of operators affects the value of the expression.
- Programming languages enforces precedence rules to resolv ambiguity.
- Solution:
 - 1 design grammar not to be ambigous, or
 - 2 during parsing, choose rules to generate the correct parse tree

Precedence and Grammar

- Operators with different precedence levels should be treated differently
- Higher precedence operations should be deep in the parse tree
 → their rules should be applied later.
- Lower precedence operations should be closer to root \rightarrow applied earlier in derivation.
- For each precedence level, define a non-terminal
- One rewritten on the other based on the precedence lower to higher

Rewritten Grammar

$$\begin{split} \langle stmt \rangle &\rightarrow \langle id \rangle = \langle expr \rangle \\ \langle expr \rangle &\rightarrow \langle expr \rangle + \langle term \rangle \mid \langle term \rangle \\ \langle term \rangle &\rightarrow \langle term \rangle * \langle factor \rangle \mid \langle factor \rangle \\ \langle factor \rangle &\rightarrow \langle id \rangle \mid (\langle expr \rangle) \\ \langle id \rangle &\rightarrow \text{a} \mid \text{b} \mid \text{c} \end{split}$$

- ⟨**term**⟩ and ⟨**expr**⟩ has different precedence.
- Once inside of $\langle term \rangle$, there is no way to derive +
- Only one parse possible



Associativity

■ Associativity of operators is another issue

$$a - b - c \equiv (a - b) - c$$
 or $a - (b - c)$

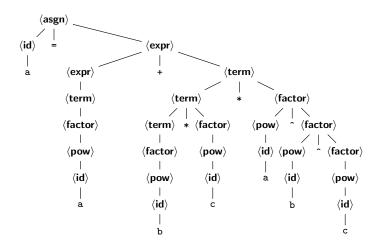
- Recursion of grammar defines how tree is constructed for operators in the same level.
- If left recursive, later operators in the sentence will be closer to root, if right recursive earlier operators will be closer to root
- left recursion implies left associativity, right recursion implies right associativity.

Sample Grammar

```
\langle \mathsf{asgn} 
angle \, 	o \, \langle \mathsf{id} 
angle \, = \, \langle \mathsf{asgn} 
angle \, \, | \, \, \langle \mathsf{id} 
angle \, = \, \langle \mathsf{expr} 
angle
 \langle expr \rangle \rightarrow \langle expr \rangle + \langle term \rangle \mid \langle term \rangle
\langle term \rangle \rightarrow \langle term \rangle * \langle factor \rangle \mid \langle factor \rangle
\langle factor \rangle \rightarrow \langle pow \rangle \hat{\ } \langle factor \rangle | \langle pow \rangle
\langle pow \rangle \rightarrow \langle id \rangle \mid (\langle expr \rangle)
\langle id \rangle \rightarrow a \mid b \mid c
```

- (asgn) is right recursive like right associative C assignments.
- (expr) and (term) are left recursive, * and + left associative
- (factor) is right recursive for power operation ^ to be right associative.
- \blacksquare precedence order is (...) \prec $^{\land}$ \prec * \prec + \prec =

$$a = a + b * c * a ^ b ^ c$$



if-then-else ambiguity

■ Following grammar is ambigous:

```
\begin{array}{c} \langle \mathsf{stmt} \rangle \to \langle \mathsf{if\text{-}stmt} \rangle \\ \langle \mathsf{if\text{-}stmt} \rangle \to \mathsf{if} \ \langle \mathsf{logic\text{-}expr} \rangle \ \mathsf{then} \ \langle \mathsf{stmt} \rangle \ | \\ \qquad \qquad \qquad \qquad \mathsf{if} \ \langle \mathsf{logic\text{-}expr} \rangle \ \mathsf{then} \ \langle \mathsf{stmt} \rangle \ \mathsf{else} \ \langle \mathsf{stmt} \rangle \end{array}
```

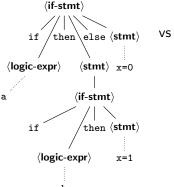
■ Consider if a then if b then x=1 else x=0:

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```

 \blacksquare Consider if a then if b then x=1 else x=0:

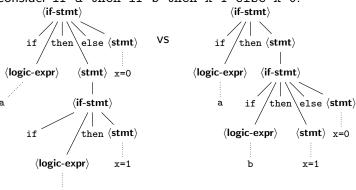


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```

 \blacksquare Consider if a then if b then x=1 else x=0:



Solution

Distinguish categories of statements. if's matched with else and unmatched:

```
\begin{tabular}{ll} $\langle stmt \rangle \to \langle matched \rangle & | \langle unmatched \rangle \\ \langle matched \rangle \to & if \langle logic-expr \rangle & then \langle matched \rangle & else \langle matched \rangle & | \\ \langle other-stmt \rangle & | \\ \langle unmatched \rangle \to & if \langle logic-expr \rangle & then \langle stmt \rangle & | \\ & if \langle logic-expr \rangle & then \langle matched \rangle & else \langle unmatched \rangle & | \\ \end{tabular}
```

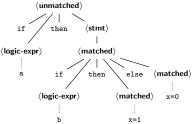
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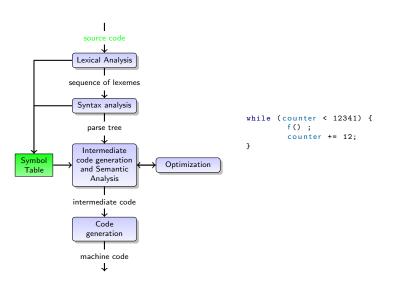
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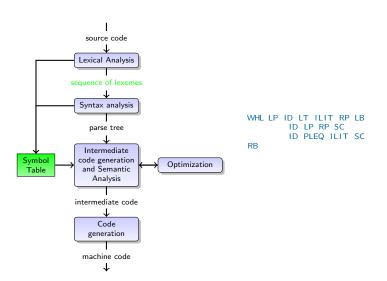
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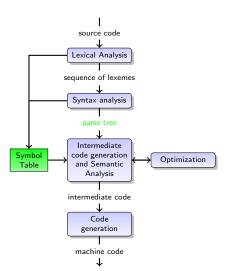
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```

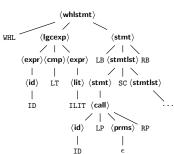
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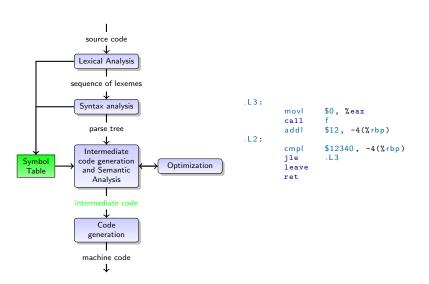


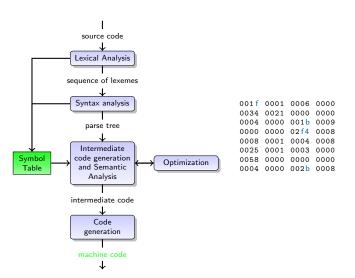












Lexical Analysis

- input: sequence of characters, source code.
- output: sequence of lexemes
- Worst case complexity of parsing is $\mathcal{O}(n^3)$. Depending on algorithm type, recursion type and number of grammar rules, this might change. n is the length of the string.
- Regular language processing complexity is $\mathcal{O}(n)$. Grammars can be defined in terms of lexemes.
- # of chars vs # of lexemes?
- Lexical analysis convert character sequences into lexemes. Identifiers registered on symbol table

Parsing

- input: sequence of lexemes (output of lexical analysis) or characters.
- output: parse tree, intermediate code, translated code, or sometimes only if document is valid or not.
- Two main classes of parser:
 - Top down parsing
 - Tottom up parsing

Top-down Parsing

■ Start from the starting non-terminal, apply grammar rules to reach the input sentence

- Simplest form gives leftmost derivation of a grammar processing input from left to right.
- Left recursion in grammar is a problem. Elimination of left recursion needed.
- Deterministic parsing: Look at input symbols to choose next rule to apply.
- recursive descent parsers, LL family parsers are top-down parsers

Recursive Descent Parser

```
typedef enum {ident, number, lparen, rparen, times,
        slash, plus, minus} Symbol;
int accept(Symbol s) { if (sym == s) { next(); return 1; }
        return 0:
void factor(void) {
   if (accept(ident));
    else if (accept(number));
    else if (accept(|paren)) { expression(); expect(rparen);}
    else { error("factor:usyntaxuerroruatu",currsym); next(); }
void term(void) {
   factor();
    while (accept(times) || accept(slash))
        factor();
void expression(void) {
   term():
    while (accept(plus) || accept(minus))
        term();
```

- Each non-terminal realized as a parsing function
- Parsing functions calls the right handside functions in sequence
- Rule choices are based on the current input symbol. accept checks a terminal and consumes if matches.
- Cannot handle direct or indirect left recursion. A function has to call itself before anything else.
- Hand coded, not flexible.

LL Parsers

- First L is 'left to right input processing', second is 'leftmost derivation'
- Checks next *N* input symbols to decide on which rule to apply: LL(N) parsing.
- For example LL(1) checks the next input symbol only.
- LL(N) parsing table: A table for $V \times \Sigma^N \mapsto R$
- for expanding a nonterminal $NT \in V$, looking at this table and the next N input symbols, LL(N) parser chooses the grammar rule $r \in R$ to apply in the next step.

■ Grammar and lookup table for a LL(1) parser:

1
$$S \rightarrow E$$

$$2 \quad S \rightarrow -E$$

$$3 \quad E \rightarrow N+E$$

4
$$E \rightarrow (E)$$

$$5 \quad \textit{N} \rightarrow \texttt{a}$$

6
$$N \rightarrow b$$

	a	b	-	(
S	1	1	2	1
Е	3	3		4
N	5	6		

- What if we add $E \rightarrow N$ to grammar?
- You need an LL(2) grammar. What if N is recursive?

■ Grammar and lookup table for a LL(1) parser:

1	S-	\rightarrow	Ε	
2	C			⊏

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- What if we add $E \rightarrow N$ to grammar?
- You need an LL(2) grammar. What if N is recursive? see LL(*) parser

Bottom-up Parsing

 Start from input sentence and merge parts of sentential form matching RHS of a rule into LHS at each step. Try to reach the starting non-terminal. reach the input sentence

$$\begin{array}{llll} a=a+b*a & \mapsto & a=\left\langle \mathit{fact}\right\rangle +b*a & \mapsto & a=\left\langle \mathit{term}\right\rangle +b*a & \mapsto \\ a=\left\langle \mathit{expr}\right\rangle +b*a & \mapsto & a=\left\langle \mathit{expr}\right\rangle +\left\langle \mathit{fact}\right\rangle *a & \mapsto \\ a=\left\langle \mathit{expr}\right\rangle +\left\langle \mathit{term}\right\rangle *a & \mapsto & a=\left\langle \mathit{expr}\right\rangle +\left\langle \mathit{term}\right\rangle *\left\langle \mathit{fact}\right\rangle & \mapsto \\ a=\left\langle \mathit{expr}\right\rangle +\left\langle \mathit{term}\right\rangle & \mapsto & a=\left\langle \mathit{expr}\right\rangle & \mapsto \left\langle \mathit{assign}\right\rangle \end{array}$$

- Simplest form gives rightmost derivation of a grammar (in reverse) processing input from left to right.
- Shift-reduce parsers are bottom-up:
 - shift: take a symbol from input and push to stack.
 - reduce: match and pop a RHS from stack and reduce into LHS.



Shift-Reduce Parser in Prolog

```
% Grammar is E \rightarrow E - T/E + T/T T \rightarrow a/b
rule(e,[e,-,t]).
rule(e,[e,+,t]).
rule(e,[t]).
rule(t,[a]).
rule(t,[b]).
parse([],[S]): - S = e . % starting symbol alone in the stack
% reduce: find RHS of a rule on stack, reduce it to LHS
parse(Input, Stack) :- match(LHS, Stack, Remainder),
                        parse(Input,[LHS|Remainder]).
% shift: nonterminals are removed from input added on stack
parse([H|Input], Stack) :- member(X,[a,b,-,+]),
                            parse(Input,[H|Stack]).
% check if RSH of a rule is a prefix of Stack (reversed).
match (LHS, List, L) :- rule (LHS, RHS), reverse (RHS, NRHS),
                       prefix (NRHS, List, L).
```

- Shift reduce parser tries all non-deterministic shift combinations to get all parses.
- For deterministic parsing states based on input lookahead or precedence required
- Deterministic bottom up parsers: LALR, SLR(1).