Programming Language Concepts Type Systems

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Outline

- 1 Type Systems
- 2 Polymorphism
 - Inclusion Polymorphism

- Parametric Polymorphism
- 3 Overloading
 - Coercion
- 5 Type Inference

Design choices for types:

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- monomorphic vs polymorphic type system.
- overloading allowed?
- coercion(auto type conversion) applied, how?
- type relations and subtypes exist?

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 - 3 Parametric polymorphism: Functions that are general and can operate identically on different types



Subtyping

C types:

$$char \subseteq short \subseteq int \subseteq long$$

- Need to define arithmetic operators on them separately?
- Consider all strings, alphanumeric strings, all strings from small letters, all strings from decimal digits. Ned to define special concatenation on those types?
- $\blacksquare f: T \to V$, $U \subseteq T \Rightarrow f: U \to V$
- Most languages have arithmetic operators operating on different precisions of numerical values.



Inheritance

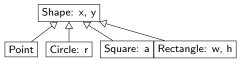
```
■ struct Point { int x, y; };
  struct Circle { int x, y, r; };
  struct Square { int x, y, a; };
  struct Rectangle { int x, y, w, h; };
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■ void move (Point p, int nx, int ny) {
             p.x=nx; p.y=ny;}
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- void move (Point p, int nx, int ny) { p.x=nx; p.y=ny;
- Moving a circle or any other shape is too different?



Haskell extensible records (only works for Hugs and in 98 mode!!):

```
import Hugs. Trex: -- Only in -98 mode!!!
type Shape = Rec (x::Int, y::Int)
type Circle = Rec (x::Int, y::Int, r::Int)
type Square = Rec (x::Int, y::Int, w::Int)
type Rectangle = Rec (x::Int, y::Int, w::Int, h::Int)
move (x=\_,v=\_|rest) b c = (x=b,v=c|rest)
(a::Shape)=(x=12,y=24)
(b:: Circle) = (x=12, y=24, r=10)
(c::Square)=(x=12,y=24,w=4)
(d::Rectangle)=(x=12,y=24,w=10,h=5)
Main > move b 4 5
(r = 10, x = 4, y = 5)
Main > move c 4 5
(w = 4, x = 4, y = 5)
Main> move d 4 5
(h = 5, w = 10, x = 4, y = 5)
```

Haskell Classes

- Subtyping hierarchy based on classes
- An instance implements interface functions of the class
- Functions operating on classes (using interface functions) can be defined

DataStr: insert, get, isempty

<uses>>

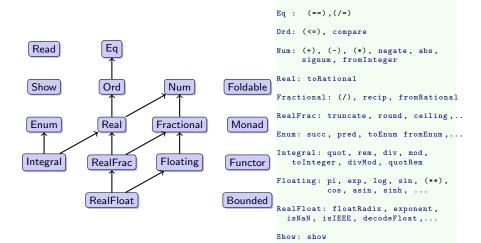
Stack

Queue

Iistinsert

■ Called interface in OO programming

Haskell Default Class Hieararchy





```
class DataStr a where
    insert :: (a v) -> v -> (a v)
    get :: (a v)-> Maybe (v,(a v))
    isempty :: (a v) -> Bool
instance DataStr Stack where
    insert \times v = push v \times
    get x = pop x
    isempty Empty = True
    isempty _ = False
instance DataStr Queue where
    insert \times v = enqueue v \times
    get \times = dequeue \times
    isempty EmptyQ = True
    isempty _ = False
insertlist :: DataStr a \Rightarrow (a v) \rightarrow [v] \rightarrow (a v)
insertlist \times \Pi = x
insertlist x (el:rest) = insertlist (insert x el) rest
data Stack a = Empty | St [a] deriving Show
data Queue a = EmptyQ | Qu [a] deriving Show
```

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- identity x = x function. type: $\alpha \to \alpha$ identity 4: 4, identity "ali": "ali", identity (5,"abc"): (5,"abc") int \to int, String \to String, int \times String \to int \times String

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- compose f g x = f (g x) function type: $(\beta \to \gamma) \to (\alpha \to \beta) \to \alpha \to \gamma$ compose square double 3:36, $(int \to int) \to (int \to int) \to int \to int$. compose listsum reverse [1,2,3,4]:10 $([int] \to int) \to ([int] \to [int]) \to [int] \to int$



- filter f [] = []

 filter f (x:r) = if (f x) then x:(filter f r) else (filter r) $(\alpha \to Bool) \to [\alpha] \to [\alpha]$ filter ((<) 3) [1,2,3,4,5,6] : [4,5,6] $(int \to Bool) \to [int] \to [int]$ filter identity [True, False, True, False] :

 [True,True] $(Bool \to Bool) \to [Bool] \to [Bool]$
- Operations are same, types are different.
- Types with type variables: polytypes
- Most functional languages are polymorphic
- Object oriented languages provide polymorphism through inheritance, run time binding and generics

Polymorphism in C++ and Java

- Inheritence provides subtyping polymorphism
- C++ virtual methods, and all methods in Java implements late binding to improve polymorphism through inheritence.
- Generic abstractions, C++ templates and Java generics provide polymorphic classes and functions.

```
template <typename T>
void sort(T arr[], int n) {
   // ... your favorite sort algorithm here
class Test { //Java requires functions be in a class
void <T> sort(T[] arr) {
```

■ C++ templates use compile time binding. Java generics binds at run time.

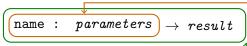


Overloading

- Overloading: Using same identifier for multiple places in same scope
- Example: Two different functions, two distinct types, same name.
- Polymorphic function: one function that can process multiple types.
- C++ allows overloading of functions and operators.

```
typedef struct Comp { double x, y; } Complex;
double mult(double a, double b) { return a*b; }
Complex mult(Complex s, Complex u) {
    Complex t;
    t.x = s.x*u.x - s.y*u.y;
    t.v = s.x*u.v + s.v*u.x;
   return t;
Complex a,b; double x,y; ...; a=mult(a,b); x=mult(y,2.1);
```

- Binding is more complicated. not only according to name but according to name and type
- Function type:



- Context dependent overloading: ______
 Overloading based on function name, parameter type and return type.
- Context independent overloading : Overloading based on function name and parameter type. No return type!

Which

type does the expression calling the function expects (context)?

```
int f(double a) { ....(1) }
int f(int a) { .... ② }
double f(int a) { .... ③ }
double x,y;
int a,b;
```

```
\blacksquare a=f(x);
  a=f(a):
  x=f(a):
  x=2.4+f(a):
  a=f(f(x)):
  a=f(f(a)):
```

Problem gets more complicated. (even forget about coercion)

Which

```
int f(double a) { ....(1) }
int f(int a) { .... ② }
double f(int a) { .... 3 }
double x,y;
int a,b;
```

- a=f(x); (1)(x double) a=f(a): x=f(a): x=2.4+f(a): a=f(f(x)): a=f(f(a)):
- Problem gets more complicated. (even forget about coercion)

Which

```
int f(double a) { ....① }
int f(int a) { ....② }
double f(int a) { ....③ }
double x,y;
int a,b;
```

- a=f(x); 1(x double)
 a=f(a); 2(a int, assign int)
 x=f(a);
 x=2.4+f(a);
 a=f(f(x));
 a=f(f(a)):
- Problem gets more complicated. (even forget about coercion)



Which

```
int f(double a) { ....(1) }
int f(int a) { ....(2) }
double f(int a) { .... ③ }
double x,y;
int a,b;
```

- a=f(x); (1)(x double) a=f(a); (2) (a int, assign int) x=f(a); (3) (a int, assign double) x=2.4+f(a): a=f(f(x)): a=f(f(a)):
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int f(double a) { ....(1) }
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double f(int a) { .... ③ }
double x,y;
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- a=f(x); (1)(x double) a=f(a); (2) (a int, assign int) x=f(a); (3) (a int, assign double) x=2.4+f(a); (3) (a int, mult double) a=f(f(x)): a=f(f(a)):
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Which

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int f(double a) { ....(1) }
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double x,y;
int a,b;
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- Problem gets more complicated. (even forget about coercion)



Which

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int f(double a) { ....(1) }
int f(int a) { ....(2) }
double f(int a) { .... ③ }
double x,y;
int a,b;
```

- a=f(x); (1)(x double) a=f(a); (2) (a int, assign int) x=f(a); (3) (a int, assign double) x=2.4+f(a); (3) (a int, mult double) a=f(f(x)); (2(1)) (x double, f(x):int, assign int)a=f(f(a)); (2)(2) or (1)(3)???
- Problem gets more complicated. (even forget about coercion)

Type Systems Polymorphism Overloading Coercion Type Inference

Context independent overloading

- Context dependent overloading is more expensive.
- Complex and confusing. Useful as much?
- Most overloading languages are context independent.
- Context independent overloading forbids ② and ③ functions defined together.
- parameters" part should be unique in "name: parameters \rightarrow result", in the same scope
- Overloading is not much useful. So languages avoid it.

Use carefully:

Overloading is useful only for functions doing same operations. Two functions with different purposes should not be given same names. Confuses programmer and causes errors

■ Is variable overloading possible? What about same name for two types?





- lacktriangle C makes $int \leftrightarrow double$ coercions and pointer coercions (with warning)
- \blacksquare Are other type of coercions are possible? (like A * \to A, A \to A *). Useful?
- May cause programming errors: x=k=3.25 : x becomes 3.0
- Coercion + Overloading: too complex.
- Most newer languages quit coercion completely (Strict type checking)



Type Inference

- Type system may force user to declare all types (C and most compiled imperative languages), or
- Language processor infers types. How?
- Each expression position provide information (put a constraint) on type inference:
 - Equality $e = x, x :: \alpha, y :: \beta \Rightarrow \alpha \equiv \beta$
 - Expressions $e = a + f \times + :: Num \rightarrow Num \rightarrow Num \rightarrow Num$ a :: Num, $f :: \alpha \rightarrow Num, e :: Num$
 - Function application $e = f \times \Rightarrow e :: \beta, x :: \alpha, f :: (\alpha \to \beta)$
 - Type constructors $f(x:r) = t \Rightarrow x :: \alpha, t :: \beta, f :: ([\alpha] \rightarrow \beta)$
- Inference of all values start from the most general type (i.e. any type α)
- Type inference finds the most general type satisfying the constraints.



Inferring Type from Initializers

- C++11 auto type specifier gets type from initializer or return expression.
- \blacksquare C++11 decltype (varexp) gets type same as the variables declared type

```
auto f(int a) {
  return a/3.0; // double, function becomes double
struct P { double x, y;} *pptr;
decltype(pptr->x) xval; // double since pptr->x is double
auto v = (P)(\{ 2.0, 4.0\}); // initializer is P typed
auto t = f(3); // f(3) returns double so t is double
```

■ GCC has typeof(expr), some other dialects have __typeof__ (expr) macro having a similar mechanism in C.



Summary

- Monomorphic vs Polymorphic types
- Subtyping
- Inheritence
- Overloading
- Parametric polymorphism
- Coercion
- Type Inference

