

## CHAPTER 4

# EVALUATION OF NPS RETURN FLOW TO THE RIVER USING A WATER BALANCE MODEL

### 4.1. WATER BALANCE MODEL APPLIED TO THE LARV

#### *Water Balance Model Equation.*

The purpose of the water balance model is to determine the volume of unaccounted for water in each reach. We begin with a basic water balance model as describe in most  
5 hydrology texts — (Wanielista, Kersten, Eaglin, et al. 1997).

$$\text{change in storage} = \text{inputs} - \text{outputs}$$

Adding the variables, both known and unknown, present in the LARV we have the following equation:

$$\frac{\Delta S}{\Delta t} = Q_{in,US} + \sum Q_{in} + P + R + B - Q_{out,DS} - \sum Q_{out} - E - T - F \quad (1)$$

Where:

$\frac{\Delta S}{\Delta t}$  = Stored volume change between time steps.

$Q_{in,US}$  = Flow in the river entering the study reach at the upstream end.

$\sum Q_{in}$  = Flow gained by the river from tributaries and other gauged sources.

$P$  = Volume of water gained to the river due to precipitation falling directly on the river's surface.

$R$  = Volume of water gained to the river due to precipitation runoff from adjacent land.

$B$  = Volume of water gained to the river due to subsurface flow.

$Q_{out,DS}$  = Flow in the river leaving the study reach at the downstream end.

$\sum Q_{out}$  Flow lost from the river to canals and other gauged sinks.

$E$  = Volume of water lost from the river due to direct evaporation from the water's surface.

$T$  = Volume of water lost from the river due to plant transpiration.

$F$  = Volume of water lost from the river due to infiltration into the subsurface flow.

If we combine the terms that are unknown or unmeasured, we arrive at the following equation:

$$\frac{\Delta S}{\Delta t} = Q_{in,US} + \sum Q_{in} + P - Q_{out,DS} - \sum Q_{out} - E + Q_{NPS} \quad (2)$$

Where:

$Q_{UNPS}$  = The sum of gains from non-point sources and losses to non-point sinks

$$(Q_{NPS} = R + B - T - F + Q_{U,in} - Q_{U,out}).$$

5        There is no reasonable method for differentiating the components of  $Q_{UNPS}$ , therefore the abbreviation NPS in this thesis refers to both non-point sources and non-point sinks.  $Q_{UNPS}$  includes the non-point source gains from groundwater sources ( $B$ ), non-point source losses to groundwater sinks ( $F$ ), transpiration losses from plants in the river channel ( $T$ ), and gains from precipitation runoff from adjacent land ( $R$ ). Additionally, this term includes  
10    ungauged flows leaving and entering the river. Ungauged gains to the river ( $Q_{U,in}$ ) are suspected to be primarily in the form of irrigation drainage from adjacent farmland. Other sources could be due to errors in underestimating flows entering the river or overestimating flows leaving the river. Ungauged losses from the river ( $Q_{U,out}$ ) are suspected to be primarily in the form of minor or unauthorized withdrawals from the river channel. Of the

ungauged flows, irrigation drainage from adjacent farmlands is assumed to be the largest contributor.

The two groundwater components of  $Q_{UNPS}$  are suspected of being the largest components of  $Q_{UNPS}$ . Water transfer between the aquifer and river happens continually whereas  $Q_{U,in}$ ,  $Q_{U,out}$ ,  $R$ , and  $T$  are not continuous.  $Q_{U,in}$  and  $Q_{U,out}$  only occur periodically when individuals actively withdraw from the river or allow irrigation runoff to return to the river.  $R$  only occurs during rain events. Within the LARV, most rainwater is captured in irrigation canals. Only precipitation falling in the riparian zone is likely to reach the river.  $T$  only occurs during growing season. This value is also only considering the transpiration happening within the river channel and does not include the riparian zone. Any losses due to transpiration in the riparian zone are first considered river losses to the aquifer ( $F$ ).

Re-arranging equation (2) to solve for the unknown values produces equation 3. Due to the nearly identical method of calculating flow ( $Q$ ) and its associated error and uncertainty, these terms were associated with each other. Likewise, the precipitation ( $P$ ) and evaporation ( $E$ ) terms were associated with each other.

$$Q_{UNPS} = \left( Q_{out,DS} + \sum Q_{out} - Q_{in,US} - \sum Q_{in} \right) - \frac{\Delta S}{\Delta t} - (P + E) \quad (3)$$

A time step of one day was established for all models calculated in this thesis. Most of the data from agencies is readily available in average daily format. While most of the data could also be obtained in hourly or quarter-hourly format, it was assumed that the additional information would not improve model accuracy.

## 4.2. STOCHASTIC AND DETERMINISTIC MODELS

Deterministic and stochastic models are used in both the unaccounted for water and mass balance models. Deterministic models are fully determined by the input parameters or variables. Randomness of any kind is not included. Stochastic models extend deterministic  
5 models by including one or more random parameters. Given the same input parameter values, a stochastic model will produce different results with each iteration.

There are many recognized methods for solving stochastic models. Solutions to these models are not definite and the term "solve" must be taken loosely. Any individual solution from a stochastic model is one of a potentially infinite number of possible solutions. The  
10 Monte Carlo (MC) simulation technique was used to obtain solutions for all stochastic models in this thesis. The MC technique is conceptually simple. The stochastic model is repetitively solved in a series of iterations. The combined solutions from all iterations are used to define the solution statistics of the model.

The number of iterations performed is determined by calculating and analyzing a set  
15 of identifier statistic(s) after each run. Identifier statistic(s) are those that the modeler has determined to be of value in determining when to terminate the model. These statistics are monitored to identify when the change in the statistic has reached a predetermined threshold. It was determined that for the sake of simplicity, all of the models calculated in this thesis would use the same number of iterations. The USR mass balance model is the most  
20 complex model as it has the largest number of input variables and uncertainty terms. The identifier statistics used were the mean, variance, and skewness which are the first, second, and third moments of the probability density. These were calculated for each iteration. The threshold between the observed iteration and the previous iteration was fixed at 0.1%. The identifier statistics reached the threshold in the following order: mean, variance, and

skewness. Skewness reached its break point shortly before the 500th iteration. A judgment call was made to increase the factor of safety. Therefore, the number of stochastic model iterations was fixed at 5,000. The fourth moment, kurtosis, was also calculated and analyzed for each iteration. It was found to be too sensitive as it did not consistently stay within the  
5 accepted cutoff threshold of 0.1%. It is assumed that this sensitivity is due to the existence of a significant number of outliers that cause the distribution of results to be non-normal.

### 4.3. ERROR AND UNCERTAINTY.

Any problem that measures variable natural processes must account for parameter and model uncertainties (Vicens, Rodríguez-Iturbe, and Schaake 1975). Parameter uncer-  
10 tainty is derived from measurement error, spatial variability, and temporal variability (Hersch 2002). Measurement error is the difference between the true and measured values. Most of this error type is due to instrument measurement inaccuracies due to either error inherent in the instrument or from errors in calibration or measurement. Measurement errors inherent to the instrument are uncorrectable and cannot be accounted for within the  
15 model. Errors due to calibration or measurement deviations are only correctable at the time of measurement or calibration and cannot be accounted for within the model.

Spatial variability is the difference in the true value at different points when measured at the same time. Data collected at a single given point in space may not be representative of the area it is assumed to represent due to spatial variability. This can manifest itself even  
20 with very small distances between measurements. Temporal variability is the difference in the true value at the same point, but at different times. Data collected at a one time may not be representative of the time frame it is assumed to represent due to temporal variability (Gates and Al-Zahrani 1996). Again, this can be manifested even over small time differences. Due

to instrument error, the spatiotemporal variability of the measured object, and the inability to know the true value of the measurement, reported parameter values should be treated as random variables (C. T. Haan 1989; Charles Thomas Haan 2002).

Almost all of the data was obtained from outside agencies and was not collected  
 5 by the research team. These agencies have data uncertainty ranges that account for all parameter uncertainties. These uncertainties are expressed in accordance with the ISO Guide to Expression of Uncertainty in Measurement (GUM) (ISO 2008). While the GUM classifies uncertainty as either "Type A" or "Type B", the all of the data included in this thesis has uncertainty evaluations described as "Type B". Type B evaluations usually use  
 10 standard deviations and assumed probability distributions obtained from scientific judgment, available information, and possible variability of a measurement.

The data originators have provided uncertainty ranges which include instrument measurement random error and uncertainties due to temporal variations of the measured location. The root mean square method is used to estimate the uncertainty related to measurement  
 15 of water quantity and water quality values (Harmel and Smith 2007; ISO 2008). Harmel and Smith (2007) describe this measurement uncertainty as the probably error range, and quantify upper and lower uncertainty boundaries for measured data points as the following when attempting to specify an expected range of expected values.

$$\sigma^2 = \left( \frac{O_i - UO_i(l)}{3.9} \right)^2 \quad or \quad \sigma^2 = \left( \frac{UO_i(u) - O_i}{3.9} \right)^2 \quad (4)$$

Where:

$\sigma^2 =$  variance about measured data value  $O_i$ .

$O_i =$  measured value.

$UO_i =$  upper ( $u$ ) and lower ( $l$ ) uncertainty boundaries.

3.9 = number of standard deviations accounting for  $> 99.99\%$  of a normal probability distribution

The data collected for this thesis is assumed to represent the mean of a normal distribution of possible values. The upper and lower bounds of the distributions are given  
 5 as either a percent or value deviation from the mean. Equation 4 is re-written from the definition found in Harmel and Smith (2007) to that found in equation 5.

$$\sigma^2 = \left( \frac{\mu - (\mu - \mu p)}{3.9} \right)^2 \quad \text{or} \quad \sigma^2 = \left( \frac{(\mu + \mu p) - \mu}{3.9} \right)^2 \quad (5)$$

Where:

$\mu =$  the reported value (assumed to be the mean).

$p =$  the reported percent deviation from  $\mu$ .

Both of these equations in 5 simplify to equation 6. The standard deviation is shown  
 10 as the calculated result due to the requirements of the modeling software.

$$\sigma = \frac{\mu p}{3.9} \quad (6)$$

When the upper and lower bounds are defined as a fixed value deviation from the reported value, then equation 4 becomes:

$$\sigma^2 = \left( \frac{\mu - (\mu - v)}{3.9} \right)^2 \quad \text{or} \quad \sigma^2 = \left( \frac{(\mu + v) - \mu}{3.9} \right)^2 \quad (7)$$

Where:

$v =$  the reported value deviation from  $\mu$ .

In this case, both equations in 7 simplify to:

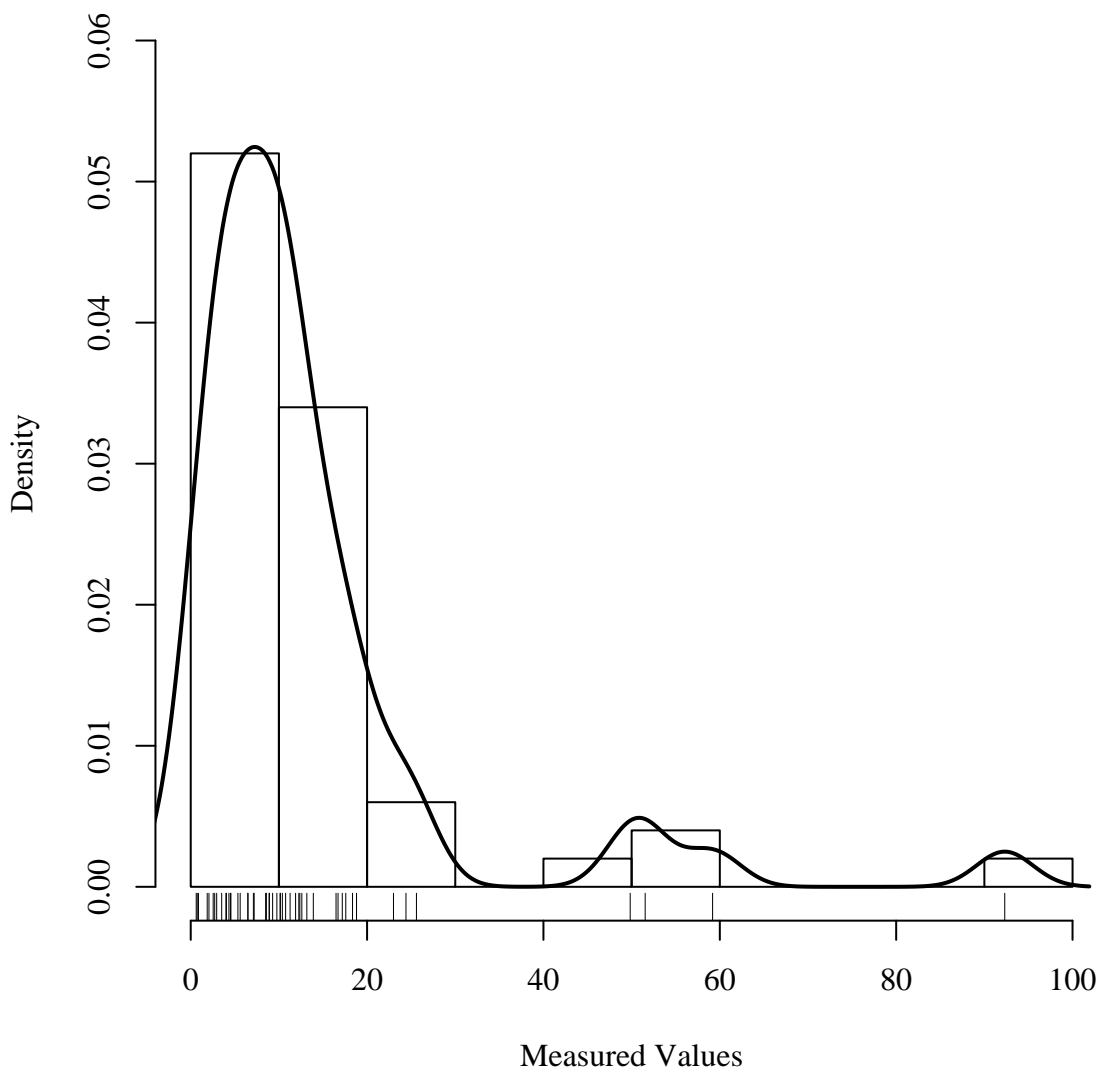
$$\sigma = \frac{v}{3.9} \quad (8)$$

The difference between a model's calculated or estimated value and the reported value is called a residual. The distribution of residuals is the model uncertainty. These distributions are uni-variate and do not have predefined shapes. There are a variety of statistical and graphical tools available to analyze unknown residual distributions to determine a best fit parametric distribution. The two graphical tools used in this thesis to analyze distributions are the histogram and the kernel density estimate.

Non-parametric distribution models are used as an aid for analyzing uni-variate data sets. Specifically, kernel density estimates (KDE) are used in conjunction with histograms to assist in visual analysis of the data. Figure 4.1 is an example of a random sample of one of the input data sets used in this thesis. The curve is the KDE. The short vertical lines between the histogram and the x-axis, called a rug, depict the data values. This figure adequately displays the resulting differences between histograms and KDE. KDEs can more accurately depict data groupings that are lost in histogram bins. The histogram leads us to believe that the data has a strong tendency to be near zero, while the KDE shows that the majority of the data is between 0-20. Histograms can more accurately depict extremes



or cut-off values. In the figure, there are no values less than zero. The histogram clearly shows this while the KDE shows that there are values less than zero. Both histograms and KDE are used throughout this thesis to assist in the description of distributions. A rug is also presented with the histogram whenever the quantity of data allows for adequate data  
5 presentation. A rug is not included when the data set is too large to allow for discreet identification of data values.



**Figure 4.1.** Example kernel density estimate. The data is a random sample of an input variable used in this thesis. The curve depicts the kernel density estimate. The short vertical lines between the histogram and the x-axis, called a rug, depict the data values.

Determining which parametric distribution best fits the uni-variate residual distribution requires the use of both the graphical and statistical tools. For each residual distribution, probable parametric distributions types were chosen for testing against the residual distribution. For each of these parametric distribution types, a best fit was generated using the maximum likely-hood estimator (MLE) method. These MLE results were then analyzed using Kolmogorov-Smirnov (K-S), Cramer-von Mises (CvM), and Anderson-Darling (A-D) goodness-of-fit tests to determine which distribution type best fit the uni-variate residual distribution. All three tests are non-parametric tests of continuous uni-variate probability distributions. The K-S and CvM tests calculate the difference between the empirical cumulative density function (ECDF) of the test data and the cumulative density function (CDF) of the tested reference distribution. The K-S and CvM tests use different algorithms to perform the calculation. Each of the goodness-of-fit tests has their own strength and weaknesses and as such, graphical tools are used to confirm or refute the statistical test results (D'Agostino and Stephens 1986; Delignette-Muller and Dutang 2014; Venables and Ripley 2002).

#### 4.4. RIVER STORAGE CHANGE

River reach estimated stored water volume changes ( $\frac{\Delta S}{\Delta t}$ ) from equation 1 are the sum of the river segment stored water volume changes for each reach (Equation 9). The storage change for each segment is calculated independent of adjacent segments.

$$\frac{\Delta S}{\Delta t} = \sum \frac{\Delta S_i}{\Delta t} \quad (9)$$

Where:

$\Delta S$  = Water storage change in the river reach.

$\Delta S_i$  = Water storage change in river segment  $i$ .

$\Delta t$  = Model time step = 1 day.

River reach volume changes are calculated between two consecutive time steps. Reach volume changes are calculated as the sum of the volume changes within the segments that compose the reach. River segment volume change between time steps is calculated as shown

in equation 10.

$$\frac{\Delta S_i}{\Delta t} = L_i \cdot \frac{\Delta A_i}{\Delta t} \quad (10)$$

Where:

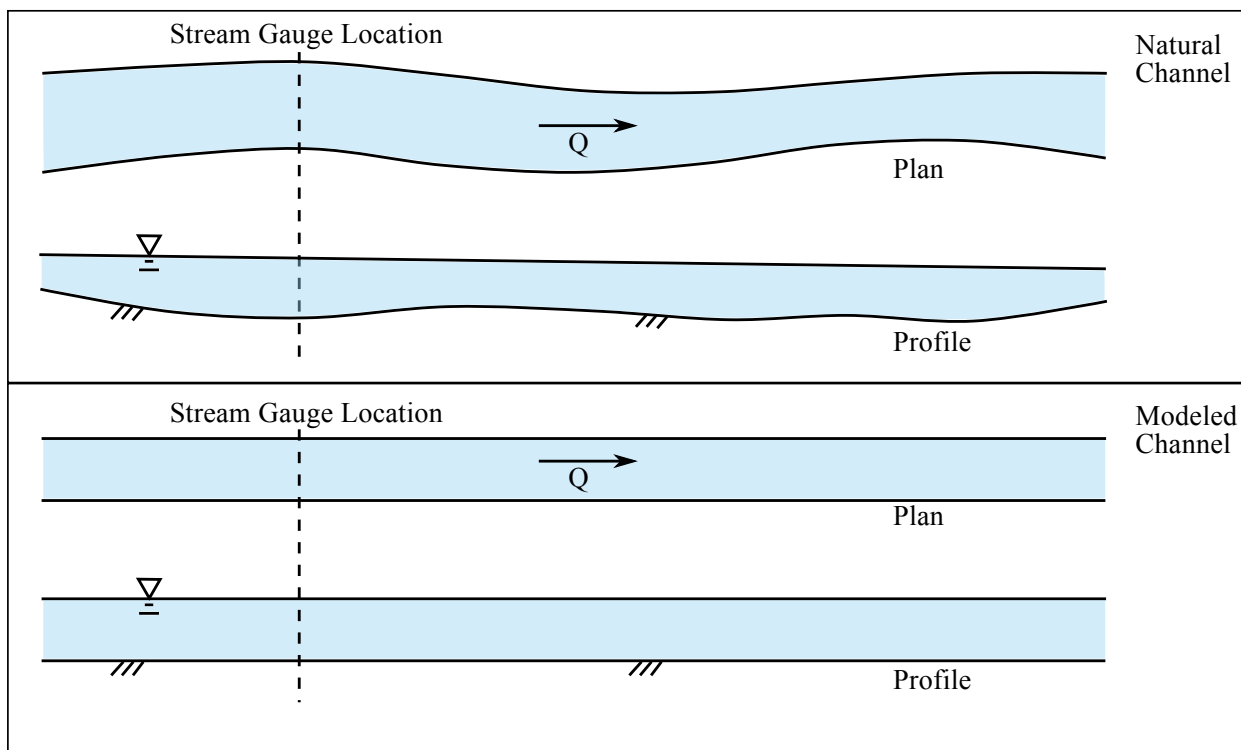
$\frac{\Delta S_i}{\Delta t}$  = Segment storage change.

$L_i$  = Segment length.

$\frac{\Delta A_i}{\Delta t}$  = Segment cross-section area change.

Figure 4.2 shows the difference between a simplified example of a natural channel and the modeled channel. Although the river is variable in width and depth along its entire lengths, it is modeled as a trapezoidal prism with a constant length and with a cross-section

that does not vary with respect to location. It was reasoned that this simplistic model would best approximate the average channel shape along the entire reach. The channel water surface elevation is assumed to be constant through each segment. This assumption is not true in nature, but we are not concerned with the water surface elevation, but with the flow depth. We are assuming that the flow depth remains relatively constant through a river segment. This assumes that all gains and losses to the river are accounted for either through flow gains and losses, evaporation, precipitation, or unaccounted for gains and losses as shown in equation 1.



**Figure 4.2.** River Segment Model.

Segment lengths, as reported in Table 4.2, are sufficiently short such that any surges due to irrigation canal gates changes, precipitation events, or other events pass through the segment in less than a day. The total travel time is approximately 2-3 days and 1-2 days in the USR and DSR, respectively, based on USGS reported average stream velocity

measurements taken in conjunction with stream gauge calibrations. River segment length ( $L_i$ ) was measured to the nearest 0.1 km using publicly available satellite imagery, USGS hydrography data, and geographical information system (GIS) software. River segment length was calculated as the length of the thalweg between the segment endpoints. When the USGS thalweg did not follow along the river channel as shown in the satellite imagery, a new thalweg was drawn. Rough validation of these measurements was performed in the field by comparing the GIS calculated length of adjacent roadways to the actual driven distance as reported by a vehicle odometer. River lengths are assumed to be constant throughout the study time frame. Individual and combined variations in the channel path along a river segment were assumed to be negligible.

**Table 4.2.** River Segment Lengths.

Study Reach	River Segment	Segment Length	
		km	mi
USR	A	12.5	7.8
	B	3.9	2.4
	C	30.7	19.1
	D	37.8	23.5
	E	14.3	8.9
DSR	F	37.6	23.4
	G	24.9	15.5

River segment cross-sectional area change ( $\frac{\Delta A_i}{\Delta t}$ ) calculation is based on the trapezoidal area that approximates the difference between the cross-sectional area at two different flow depths as depicted in Figures 4.3, 4.4 and in equation 11. While the cross sectional area difference isn't exactly a trapezoid, the difference for small differences in gauge height is insignificant.



14

Where:

$t$  = Current time step.

$t-1$  = Previous time step.

$\frac{\Delta A_i}{\Delta t}$  = Cross-section area change at river section  $i$  between time steps.

$\overline{Tw}$  = Average river top width.

$\Delta y$  = Change in flow depth from the previous time step.

$Tw$  = River top width.

$y$  = River flow depth.

Figure 4.3 shows a simplified river cross section at a stream gauge location. As previously discussed, stream gauges do not hold the channel bottom as their datum. They have an arbitrarily fixed datum that does not move unless reset by the gauge owner. The difference between the stream gauge datum and the channel bottom is corrected using a constant correction factor calculated from the river survey. The gauge datum does not have a known marker where the elevation could be directly measured. Instead, the surveyed water surface elevation was recorded at the gauge location on both sides of the channel. The flow depth value was calculated by finding the difference between the surveyed average water surface elevation and the surveyed channel bottom elevation. The flow depth was then compared to the stream gauge height reported for the same date and time as when the water surface elevation was surveyed. The difference between the reported value and the average of the surveyed values was taken as the correction factor for the gauge. This procedure was repeated for each gauge.

Flow depth values as reported by the USGS and CDWR are measured values with an associated probability range as calculated in equation 6. The uncertainties are applied

as shown in equation 12. A correction factor ( $C_i$ ) is applied to each reported gauge depth to correct for the difference between the gauge datum and the channel bottom as measured during the channel cross-section survey. Two separate uncertainties are applied.  $\varepsilon_{h1}$  is the uncertainty distribution as described by the gauge owner. This uncertainty is reported by both the USGS and CDWR as being normally distributed with extreme values at  $\pm 0.01$  ft ( $\pm 0.003$  m) (Cobb 1989). The second uncertainty term,  $\varepsilon_{h2}$ , is the result of personal observation of the river channel along its entire length. This term describes the variability in flow depth. It was observed that the channel depth did not vary greatly along most of its length. There were particular areas where there were deeper pools, but these areas were noted to be more prone to ponding during low flow. It is assumed that the average effective flow depth only varies within a normal distribution with limits of  $\pm 0.076$  m ( $\pm 0.25$  ft). There is the possibility that  $\varepsilon_{h1}$  could cause the storage change between the time steps to change from a storage gain to a storage loss, or vice versa. This is acceptable as it is within the measurement limits of the instruments. Once  $h + \varepsilon_{h1}$  has been calculated for the two successive time steps, the relationship between the two time steps is fixed. If the river segment flow depth rises between time steps after this calculation, then that relationship must continue throughout the rest of the volume change calculation. To facilitate this, it is assumed that  $\varepsilon_{h2}$  does not vary significantly within the study time frame and does not vary within a realization. The Arkansas River channel is sufficiently stable between consecutive days that this assumption is valid. A new  $\varepsilon_{h2}$  is drawn for each realization and remains constant for all time steps within the study time frame.

$$y_{i,t} = h_{i,t} + C_i + \varepsilon_{h1} + \varepsilon_{h2} \quad (12)$$



Where:

$y_{i,t}$  = Section  $i$  modeled average daily flow depth at time  $t$ .

$h_{i,t}$  = Section  $i$  reported average daily river gauge height at time  $t$ .

$C_i$  = Section  $i$  river gauge height to flow depth correction term.

$\varepsilon_{h1}$  = Reported river gauge height data uncertainty.

$\varepsilon_{h2}$  = Estimated flow depth uncertainty.

Since the two uncertainty terms are both normal and additive to flow depth, they were added to produce a new normal distribution with mean equal to the sum of the means of the two distributions and standard deviation equal to the sum of the standard deviations of the two distributions. This additional step was taken to improve model calculation speed and to reduce the possible error of producing a total flow depth error that would cause a flow depth outside of the accepted range of 0.153 m to 1.53 m (0.5 ft to 5 ft). The uncertainty distributions  $\varepsilon_{h1}$  and  $\varepsilon_{h2}$  are not dependent on location, therefore all flow depth calculations draw from the same distribution. The normal distribution resulting from the addition of the  $\varepsilon_{h1}$  and  $\varepsilon_{h2}$  has a mean of zero and standard deviation of 0.007 07 m (0.020 32 ft) (Equation 13).

$$y_{i,t} = h_{i,t} + C_i + \mathcal{N}(\mu = 0m, \sigma = 0.00707m) \quad (13)$$

River top width ( $Tw$ ) is calculated using equation 14. (Buhman, Gates, and Watson 2002; Gates and Al-Zahrani 1996). The river channel does not have a fixed cross-section along it's length, therefore, the fitting parameters,  $\beta_1$  and  $\beta_2$  are not constant, but are from distributions of  $\beta_1$  and  $\beta_2$ . Equation 14 and the data from each survey cross-section was used to calculate a best fit equation using non-linear least squares regression. Regression results

justify

for each cross-section are presented in Table 4.3. There are an insufficient number of cross sections within each river segment to provide a statistically significant sample. This means that there is insufficient data available to generate independent fitting equations for each river segment. Therefore, the  $\beta_1$  and  $\beta_2$  values from each cross-section were combined to  
5 determine the distribution of  $\beta_1$  and  $\beta_2$  for the entire river reach. The combined distributions were tested to determine the best fit parametric distribution using the previously described method. The best fit distributions for  $\beta_1$  and  $\beta_2$  are presented in table 4.4.  $\beta_1$  and  $\beta_2$  values were analyzed for correlation which was found to be insignificant with a Pearson R value of 0.17. Visual analysis of the data points showed that there was no distinguishable  
10 pattern. Future cross-section surveys will expand the data set and may show that there is a correlation between  $\beta_1$  and  $\beta_2$ , but the available data does not support that conclusion. Also presented in Table 4.4 is the best fit distribution for the residuals. These distributions and the distributions for  $\beta_1$  and  $\beta_2$  were analyzed to determine the best fit distribution using the methodology described in Section 4.3.

$$Tw_{i,t} = \beta_1 y_{i,t}^{\beta_2} + \varepsilon_{Tw} \quad (14)$$

Where:

$Tw_{i,t}$  = River segment  $i$  average daily top width at time step  $t$ .

$y_{i,t}$  = Calculated segment  $i$  average daily flow depth at time step  $t$  calculated  
15 using equation 12.

$\beta_1$  and  $\beta_2$  = fitting parameter distributions.

$\varepsilon_{Tw}$  = Calculated average daily flow depth uncertainty.

**Table 4.3.** Arkansas River segment top width estimating coefficients.

Study Region	River Segment	Cross- Section	Fitting Parameter		Root Mean Squared Error
			$\beta_1$	$\beta_2$	
USR	A	1	219.1	0.5098	21.57
		2	197.5	0.01573	0.07938
		3	205.2	0.7734	32.05
		4	211.5	0.008948	0.2069
	B	5	59.4	0.9835	0.5002
		6	202	0.1382	12.48
		7	53.99	1.197	2.412
	C	10	141	0.5465	10.92
		11	187.2	0.5697	7.784
		12	277.9	0.01398	0.2358
		13	116.5	1.536	27.5
		14	110	0.917	1.986
	D	16	49.37	1.115	1.5171
		17	57.68	1.288	1.469
		18	116.4	0.5197	17.42
		19	58.35	0.3868	6.382
		21	141	0.07095	0.7172
		22	63.82	0.6103	1.132
		23	109.3	0.07456	0.4762
	E	26	47.62	0.1682	0.5901
DSR	F	1	22.48	0.4006	0.8139
		2	41.61	1.390	3.953
		3	29.82	0.2265	1.821
		4	21.46	0.3801	2.541
		5	22.78	0.8004	5.715
		6	26.21	0.4153	1.681
		7	41.92	1.487	3.299
	G	8	23.49	1.504	2.344
		9	33.54	1.106	3.676
		10	28.03	0.5790	2.003
		11	24.16	0.2103	1.693
		12	24.74	0.8992	2.617
		13	52.68	1.1850	5.757
		14	24.18	0.4764	0.9259

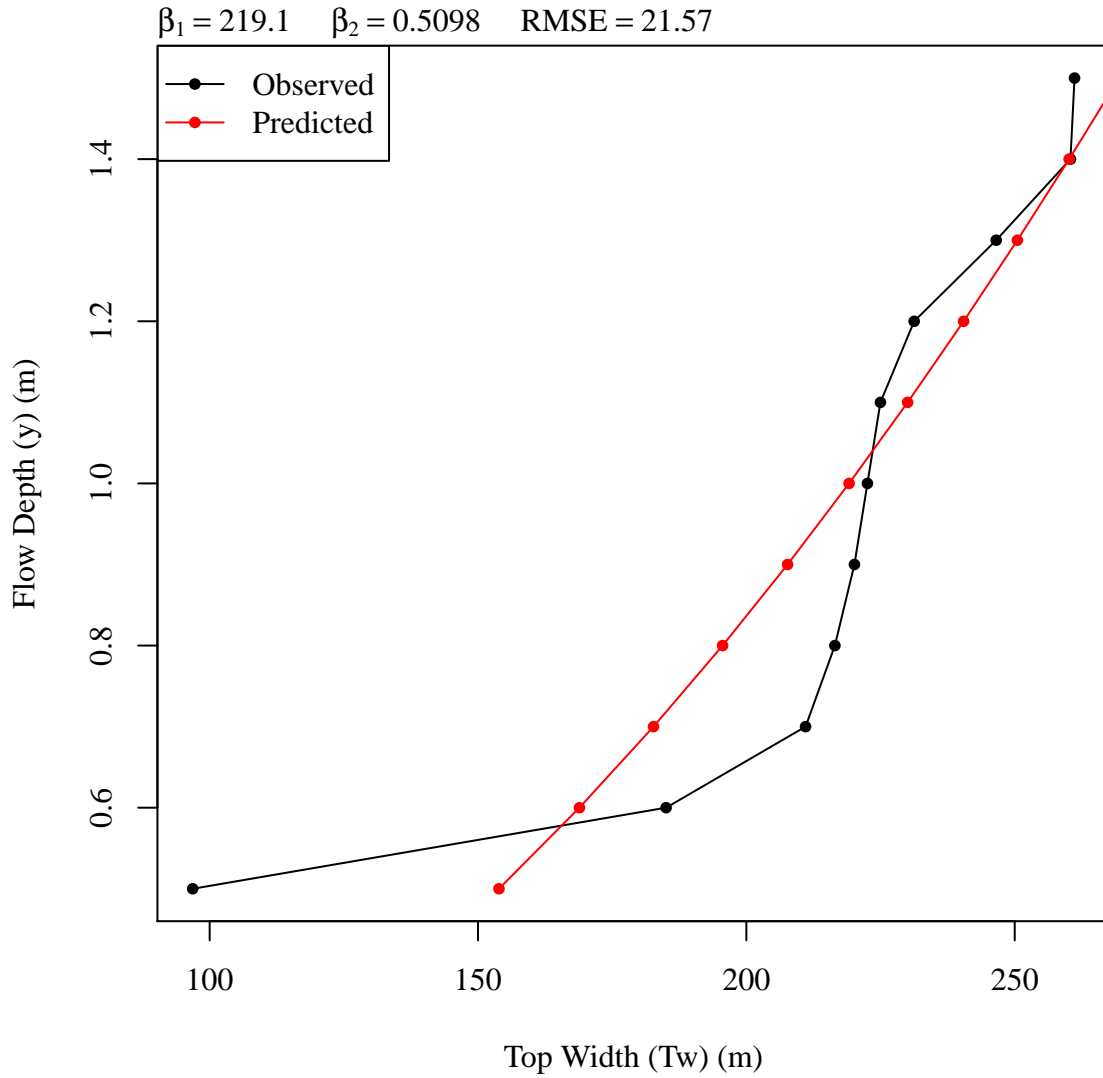
Non-linear regression models were used only when the specific model form, determined from known physical or geometrical relationships, was non-linear. R-squared values were not

used to determine goodness-of-fit for non-linear regression models since they can have valid R-squared values that are negative or greater than one (Spiess and Neumeyer 2010) and as such are outside of the boundary for comparing linear models. Pseudo or modified r-squared calculations are available, yet these computations result in values that are comparable to the r-squared value for linear models, but have slightly different interpretations . Since non-linear regression models were used only when specific model forms could be predetermined, there was no need to compare different model forms estimating the same result.

reference

Goodness-of-fit for non-linear regressions used in this thesis are purely for informational purposes. Since all non-linear models were based on known relationships, goodness-of-fit values only serve to show how well the data fits the model. In order to define non-linear regression model goodness-of-fit, the root mean squared error (RMSE) value was calculated. The RMSE represents the standard deviation of the differences between the predicted and observed values. The RMSE is scale dependent as the units are the same as the observed value. The RMSE is also known as the standard deviation. This would cause an issue if models for different observed value units and scales were compared against each other. In this study, non-linear regression models are only used to estimate the cross-sectional width of a river segment and to estimate the selenium concentration at one location. Since all cross-section analyses use the same measurement units, this allows us to compare the residual errors associated with the various cross sections without needing to consider scale or units.

The results of the top width equation for each cross-section, generated through non-linear regression, was compared to the observed results to visually compare the goodness-of-fit for each cross-section. Figure 4.5 is an example



**Figure 4.5.** Example Flow Depth vs. River Top Width Relationship. The non-linear best fit line of the form in Equation 14 is red. The values are the two non-linear regression fitting parameters ( $\beta_1$  and  $\beta_2$ ) and the residual standard error for the fitting equation ( $\sigma$ ). Similar figures for all cross-sections are found in the appendix.

Values  $\beta_1$  and  $\beta_2$  are drawn from probability distributions. Calculated flow depth and river top width data pairs were used to determine the distributions from which  $\beta_1$  and  $\beta_2$  in equation 14 were drawn. These distributions were developed using non-linear, least-squares regression. Values below 0.15 m (0.5 ft) were removed from the regression analysis. Flow

5 values below this depth are not common and it was determined that these points would not

**Table 4.4.** River top width fitting parameter distributions.

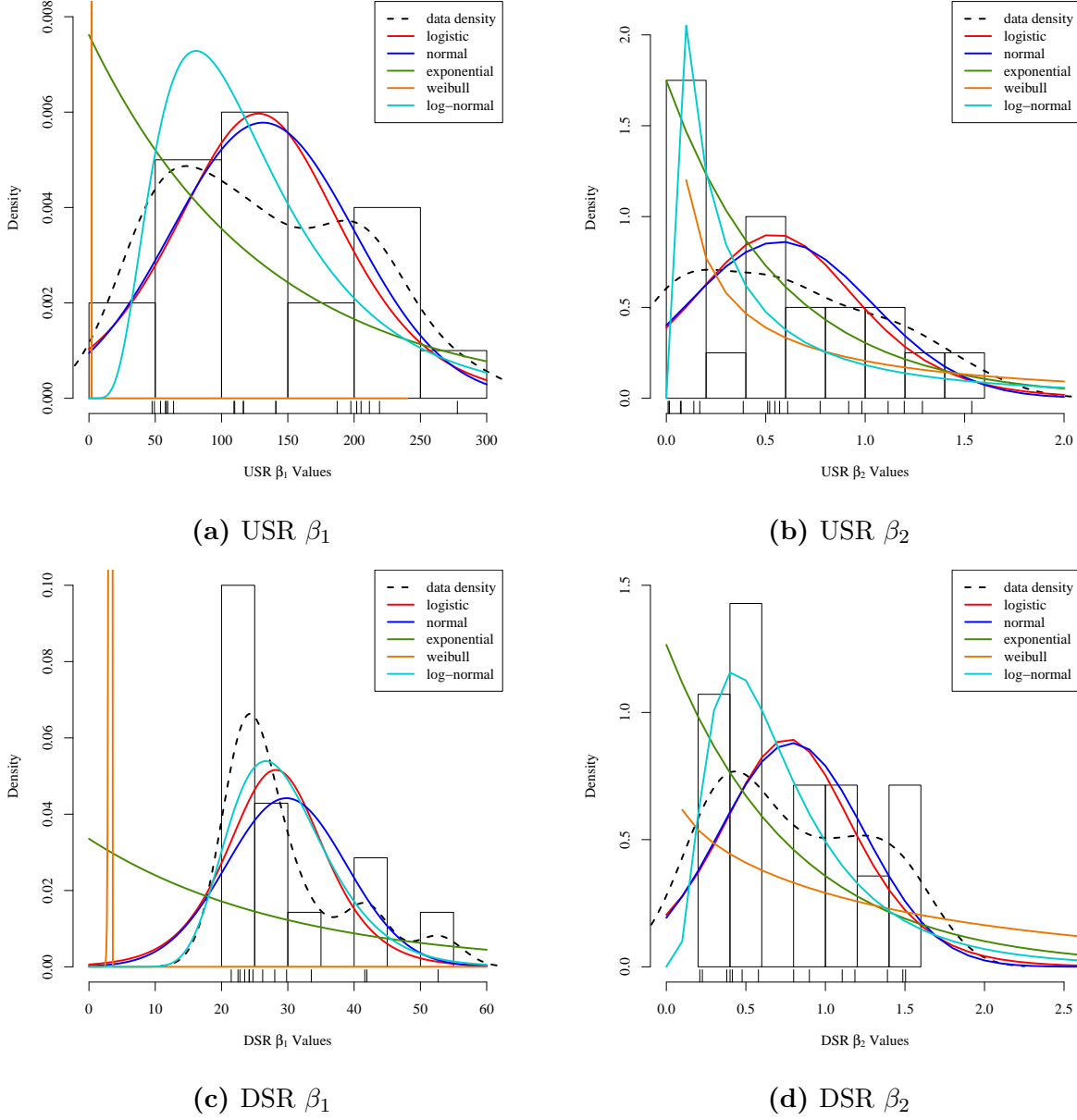
Study	Fitting Parameter	Best Fit Distribution		
		Dist. Shape	p1*	p2*
USR	$\beta_1$	logistic	16.8	7.53
	$\beta_2$	log-normal	-1.27	1.57
	Residual	logistic	1.99	0.99
DSR	$\beta_1$	logistic	28.2	4.84
	$\beta_2$	log-normal	-0.43	0.65
	Residual	log-normal	0.87	0.57

\* Distribution fitting parameters. For logistic, p1=location and p2=scale. For log-normal, p1=mean of the log scale and p2=standard dev. of the log scale

allow for an accurate representation of the flow depth to river top width relationship for the range of known flow depths. Values above 1.52 m (5.0 ft) were also removed from the regression analysis. Flow depths above this depth are above the banks of the primary river channel and are within the inner flood plain. Table 4.3 gives the resulting  $\beta_1$  and  $\beta_2$  values for each surveyed cross-section. Figure 4.5 is an example of the surveyed flow depth and river top width relationships and the derived non-linear relationship for cross-section 1 in river segment A of the USR. Similar relationship plots for the other surveyed cross-sections are found in the appendix.

Figure 4.6 shows the distributions of  $\beta_1$  and  $\beta_2$  values and the various best-fit distributions in both the USR and DSR. Logistic, normal, exponential, Weibull, and log-normal distributions were fitted to the data. Vertical tick marks in the x-axis margin are at the data values. Kernel density estimations were used as an alternative means to graphically represent the data density.

The resulting river shape parameter distributions are valid for the river reach for which they were calculated. Each river segment draws values from the shape parameter distributions independently. Only one pair of shape parameters is drawn for each realization.



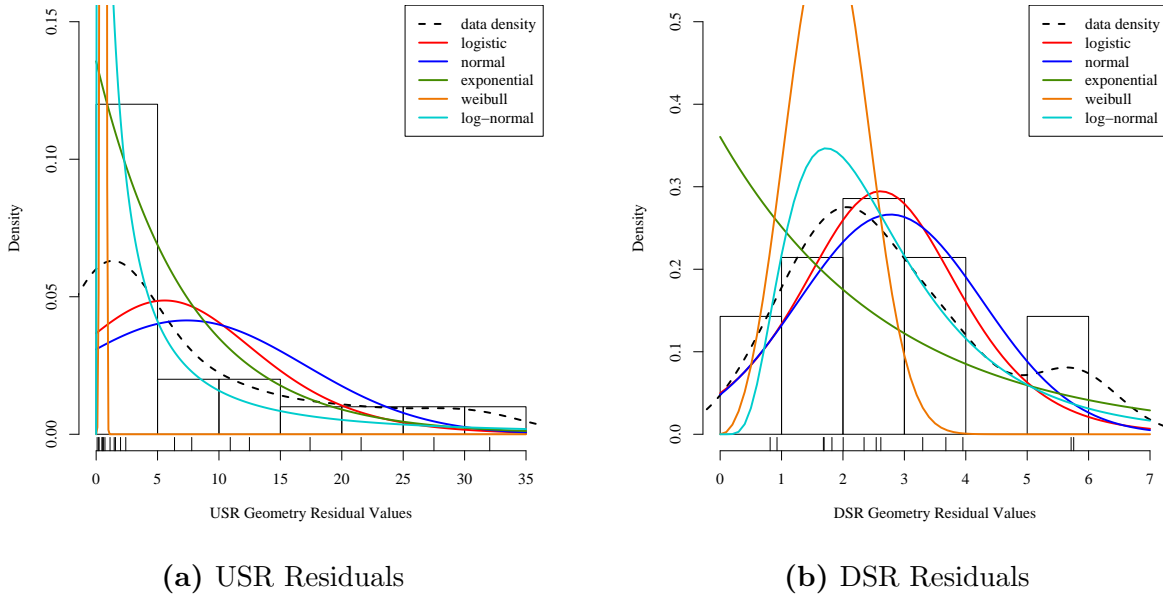
**Figure 4.6.**  $Tw$  Versus  $h$  Fitting Parameter  $\beta_1$  and  $\beta_2$  Distributions. The black dashed line is a kernel density plot representing a histogram where the bin size approaches zero. The colored curves are the best fit for the particular distribution type. Vertical tick marks in the x-axis are at the data values.

It is assumed that the river geometry does not significantly change within the study time frame. Channel variability is modeled between the realizations.

Residuals from the non-linear regression analyses were combined into a single data set for uncertainty analysis. Combining this data set was a logical step following the combination

of the data that generated the residuals. Residuals were tested using the same tools and techniques used to test the river shape parameter distributions. USR and DSR channel shape residuals were found to have a log-normal distribution. Figure 4.7 presents the residuals distribution analyses for the USR and DSR. These figures are of the same type as those used

5 to analyze the river shape parameter distributions, figure 4.6.



**Figure 4.7.**  $T_w$  versus  $H$  Residuals Distribution. The black dashed line is a kernel density plot representing a histogram where the bin size approaches zero. The colored curves are the best fit for the particular distribution type. Vertical tick marks in the x-axis are at the data values.

Residuals are the collection of the difference between the calculated regression model values and the measured values. Collectively, the distribution of the residuals describe the uncertainty of the regression model. In this case, the distribution of residuals describe the top width estimating uncertainty  $\varepsilon_{T_w}$ . Residuals should be tested for heteroskedasticity

10 to determine if the model does not adequately predict the data. Heteroskedasticity is the condition where the variability of a variable, in this case the residuals, is unequal across the range of the values and is usually indicative of under specification of the model. There are

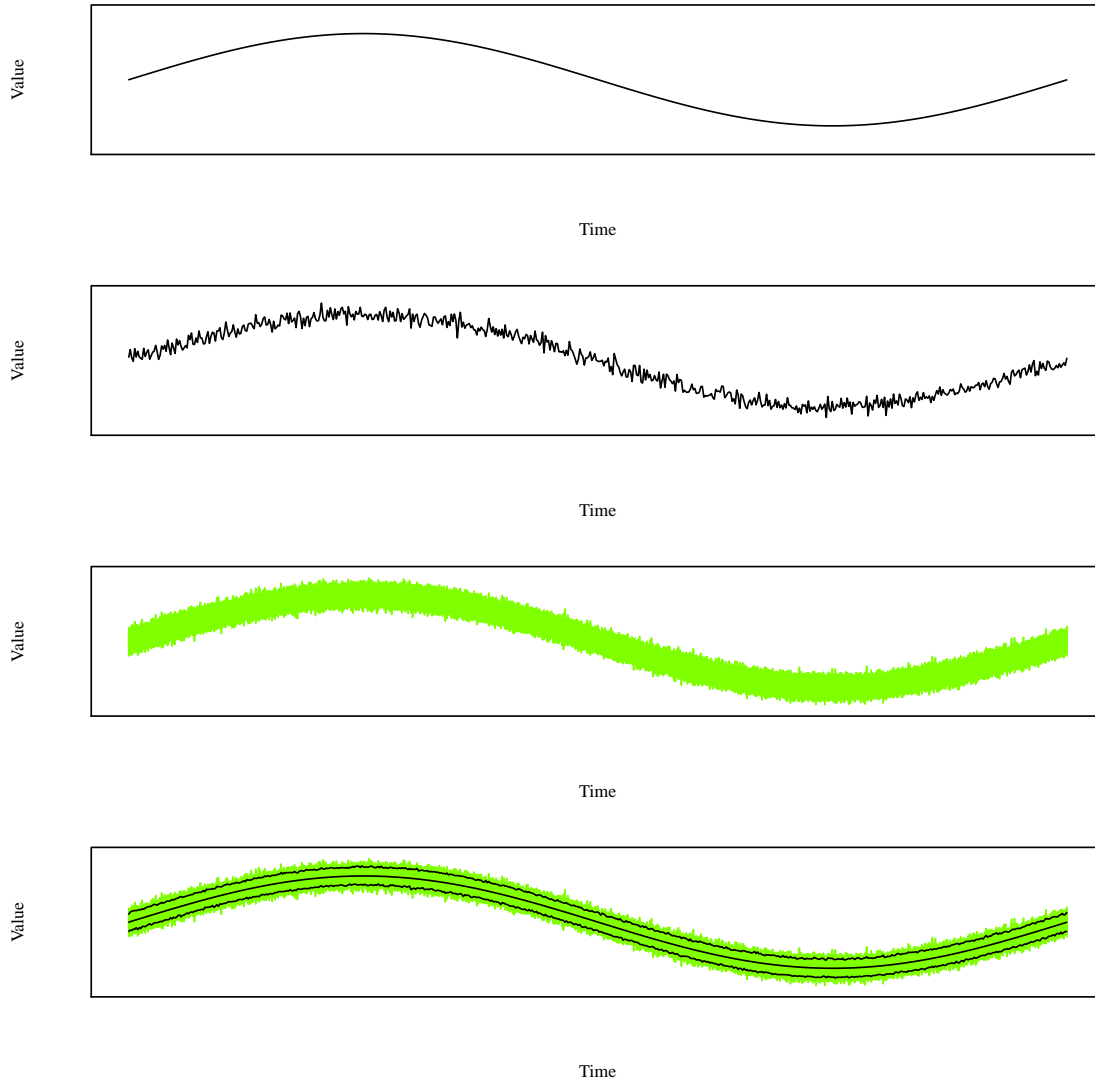


many tests for heteroskedasticity, but the most powerful is visual analysis of the plot of the residuals against the fitted, or calculated, values. When a small number of values is used to perform the regression, visual and computational analysis becomes difficult since patterns may appear that don't truly exist or patterns may not appear where they do exist. When  
5 heteroskedasticity was evident during model creation, the model was modified to remove the heteroskedasticity. Other methods are available to account for heteroskedasticity, but the most strongly recommended is model modification. Determining the parametric distribution that best fits the regressions is performed using the method described in section 4.3. Both visual and goodness-of-fit tests were applied to all residual regression analyses.

10 Results from the individual regression and residuals analyses are plotted with the source data to visually determine if the resulting best fit estimating equation or residuals distribution suitably fit the source data. An example of one of these figures is Figure 4.5 which plots a best fit regression equation alongside the source data. Figure 4.7 is representative of how the residual analysis results are visually analyzed. The best fit of several different  
15 distribution shapes are plotted over the histogram and KDE of the residuals or source data. These types of figures are used throughout the analysis to visually verify that the calculated regression models and best-fit distributions actually fit the data.

Results from deterministic and stochastic models are presented throughout this thesis. While both model types present results from the same source data, stochastic models, as  
20 previously discussed, also include uncertainty in many forms. Stochastic model results are complex. They are time-series models where each time step is an independent distribution of the results. Figure is a very simple representation of a time-series. The top sub-figure shows a sine curve which represents the deterministic model. The second sub-figure shows one realization of the stochastic model which is the deterministic model with uncertainty

added at each time step. For this example, the uncertainty is normally distributed within the time step. The third sub-figure is 500 independent realizations shown on top of each other. The fourth sub-figure shows the 500 realizations with three calculated lines representing stochastic model summary statistics time-series.



**Figure 4.8.** Stochastic model graphical results presentation description. The top sub-figure represents a simple deterministic time-series model. The second sub-figure represents a single stochastic time-series model. The third sub-figure represents 500 stochastic time-series. The fourth sub-figure shows the 500 stochastic time-series with the three stochastic model summary statistics time-series. The top line is the 97.5th percentile time-series, the middle line is the mean time-series, and the bottom line is the 2.5th percentile time-series.

The middle line is the time-series that represents the mean value calculated for each time-step. This is the stochastic model mean time-series. The top and bottom lines are the 97.5th and 2.5th percentile calculated for each time step. These are the stochastic model 97.5th percentile time-series and stochastic model 2.5th percentile time-series, respectively.

5 Collectively, these three time-series are called stochastic model summary statistics time-series. These three time-series show how the results and range of possible results vary with time. All stochastic time-series graphs present only the three stochastic model summary statistics time-series. Values outside of these are not plotted so as to improve understanding and readability of the graphical results

10 Presenting individual values for stochastic model results requires further summary statistics of the calculated stochastic model summary statistics time-series. Without this further reduction, results would contain large quantities of values which are very difficult to present. The mean, 97.5th percentile, and 2.5th percentile are calculated for each of the summary statistics time-series to provide more readable results. The summary statistics for  
15 each of the stochastic model summary statistics time-series indicate the most likely value and the range of possible values as presented in the example in Table 4.5. In this table, each row of the bottom portion of the table presents one of the stochastic model summary statistic time-series results. In this example, values ' $g$ ', ' $h$ ', and ' $i$ ' are the summary statistics for the stochastic model mean time-series.

20 Table 4.5 also includes the deterministic time-series summary statistics values. These values are the 2.5th percentile, mean, and 97.5th percentile calculated from the deterministic model results and are presented in the upper half of the table. The deterministic model time-series summary statistics should be approximately the same as the stochastic model mean time-series summary statistics, which are values  $g$ ,  $h$ , and  $i$  in the lower half of the

table. This statement should be true if the deterministic model is a possible realization of the stochastic model and if the distribution of the combined uncertainties in the stochastic model are approximately normally distributed.

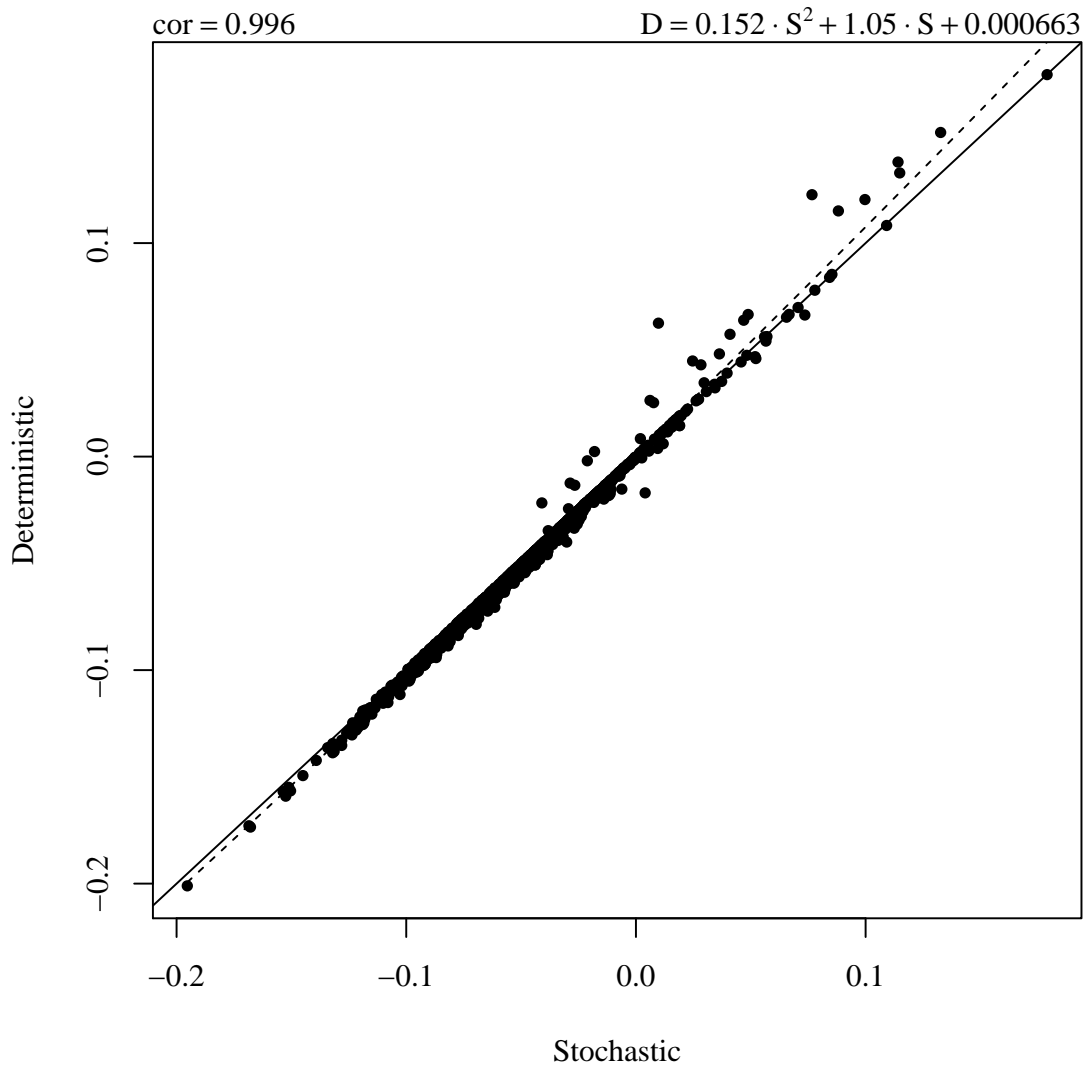
**Table 4.5.** Example deterministic and stochastic model numerical results. The single row on the deterministic model side presents the summary statistics for the deterministic model (values  $a$ ,  $b$ , and  $c$ ). Each row on the stochastic model side presents the results for a specific stochastic model summary time-series. All values are presented in common units. The Pearson Correlation value ( $m$ ) is calculated between the deterministic model time-series and the stochastic model mean time-series values at each time-step in the models.

Deterministic Model Time Series			
	2.5th Percentile	Mean	97.5th Percentile
	a	b	c
Stochastic Model Summary Statistics Time Series			
	2.5th Percentile	Mean	97.5th Percentile
97.5th Percentile	d	e	f
Mean	g	h	i
2.5th Percentile	j	k	l
Pearson Correlation = $m$			

One goal of stochastic modeling is to have a deterministic model that resides within  
5 the stochastic. If the deterministic model isnt a possible realization of the stochastic model,  
then there are significant stochastic model issues that need to be addressed. Ideally, the sto-  
chastic model mean time-series at each time step should be close to the deterministic model  
at that same time step. To determine if this relationship is true, the Pearson correlation  
between the stochastic model mean time-series and the deterministic model was calculated  
10 and is included at the bottom of Table 4.5. Calculating the Pearson correlation requires as-  
suming the two compared data sets are continuous and are linearly related. All input values  
and results in this thesis are continuous, either from zero to  $+\infty$  or between  $\pm\infty$ .

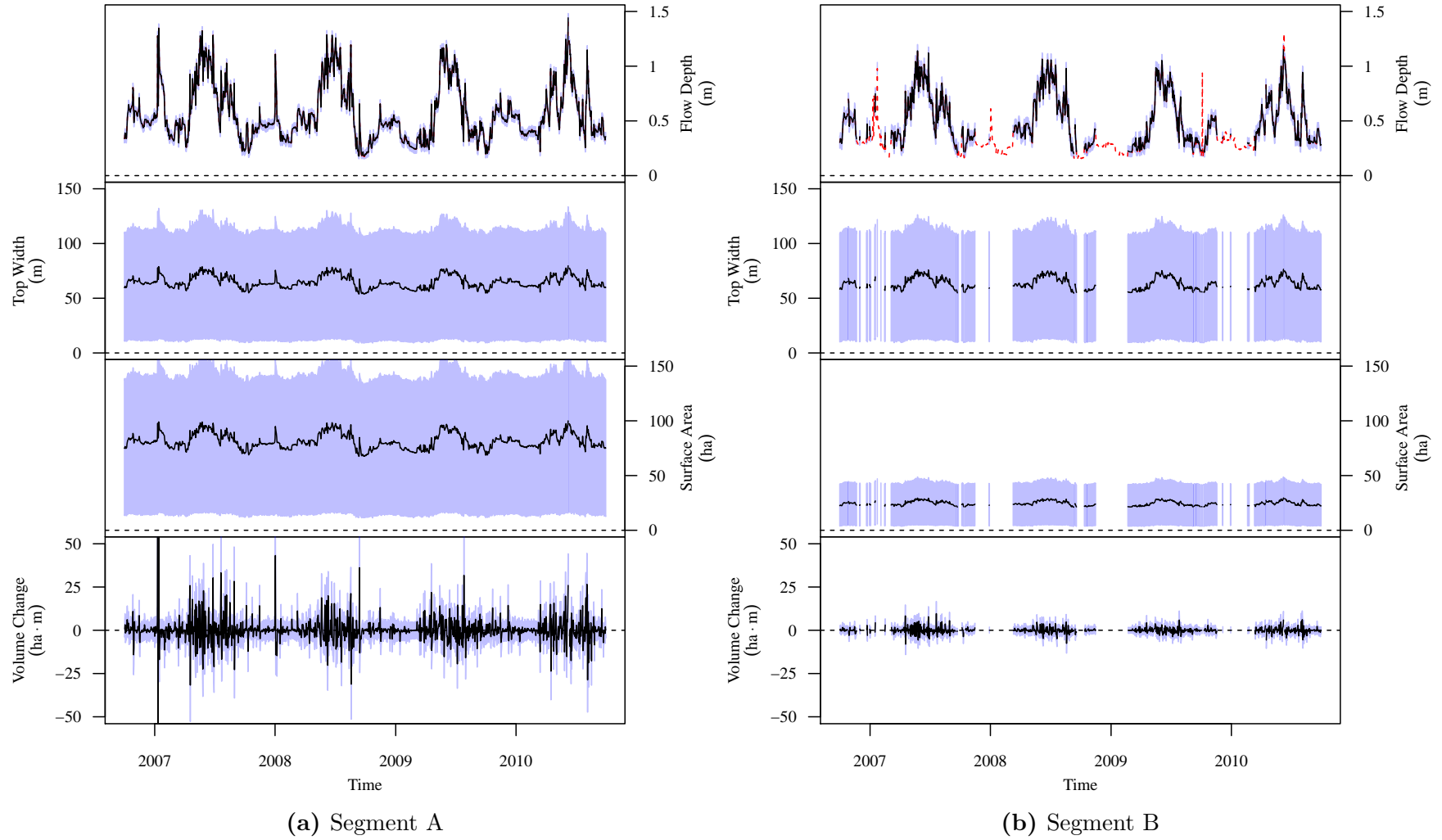
Correlation values only provides a numerical value to describe the relationship between two values or data sets. It does not imply causality or linearity. We can infer causality because the deterministic model is a subset of the stochastic model. In fact, the deterministic model was used to create the stochastic model. We cannot infer linearity. Figure attempts  
5 to answer the linearity issue through visual analysis. The black dots are the comparison of the stochastic mean time-series and the deterministic model. The red and blue dots are the comparison of the stochastic 97.5th and 2.5th percentile time-series as compared to the deterministic model, respectively. The solid black line follows the equation  $y=x$ . This is where all of the black dots should lie if the stochastic mean time-series and deterministic  
10 models were in perfect agreement. The dashed line is the quadratic best fit line through the stochastic mean time-series.

River segment B in the USR does not have a flow gauge within its boundaries and therefore has no reported flow depths. This segment has an additional irrigation diversion check structure within its boundaries, thereby sub-dividing segment B into two sub-segments,  
15 each with its own ungauged flow depth. Due to segment B being the shortest, composing only 3.9% of the USR's total length, and the additional variability of the possible flow depth, the average daily flow depth within segment B is taken as the mean of the reported flow depths in segment A and C. Top width and volume change calculation follows the previously described methodology.



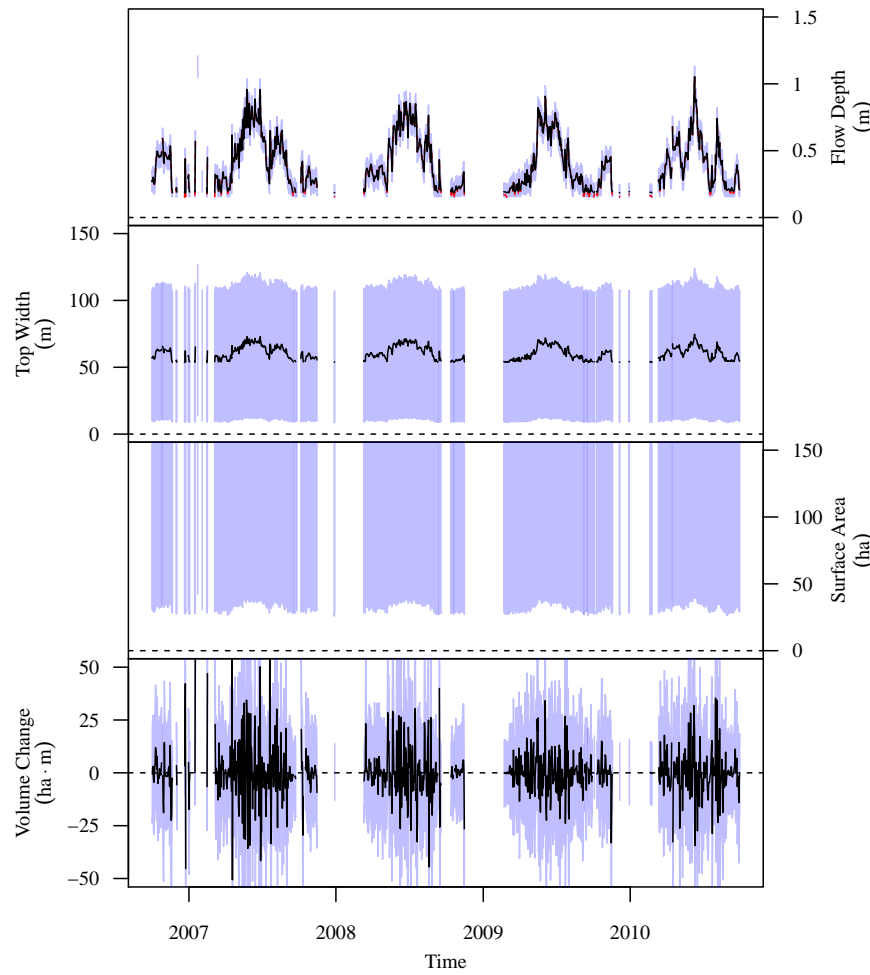
**Figure 4.9.** Example scatterplot comparing deterministic model time-series and stochastic model mean time-series results. The solid line is drawn such that  $y = x$ . The dashed line is the best-fit quadratic equation between the deterministic model time-series and the stochastic model mean time-series and the equation is in the top right. The Pearson Correlation is the top left number.

The time-series plots of all four stochastic geometric parameters for each study region river section segment is presented in Figures 4.10 and 4.11 for the USR and DSR, respectively. The black lines indicate the stochastic model mean time-series. The blue band indicates the 95% central inter-percentile range (CIR) of the stochastic values as defined by the stochastic model 2.5th percentile time-series and the stochastic model 97.5th percentile time-series. The red dashed line in the flow depth portion of the figure indicates the reported flow depth values. It is plotted under the stochastic model mean time-series line and as such is only visible when either the stochastic model mean time-series value was not calculated due to missing data or when the two values deviate.

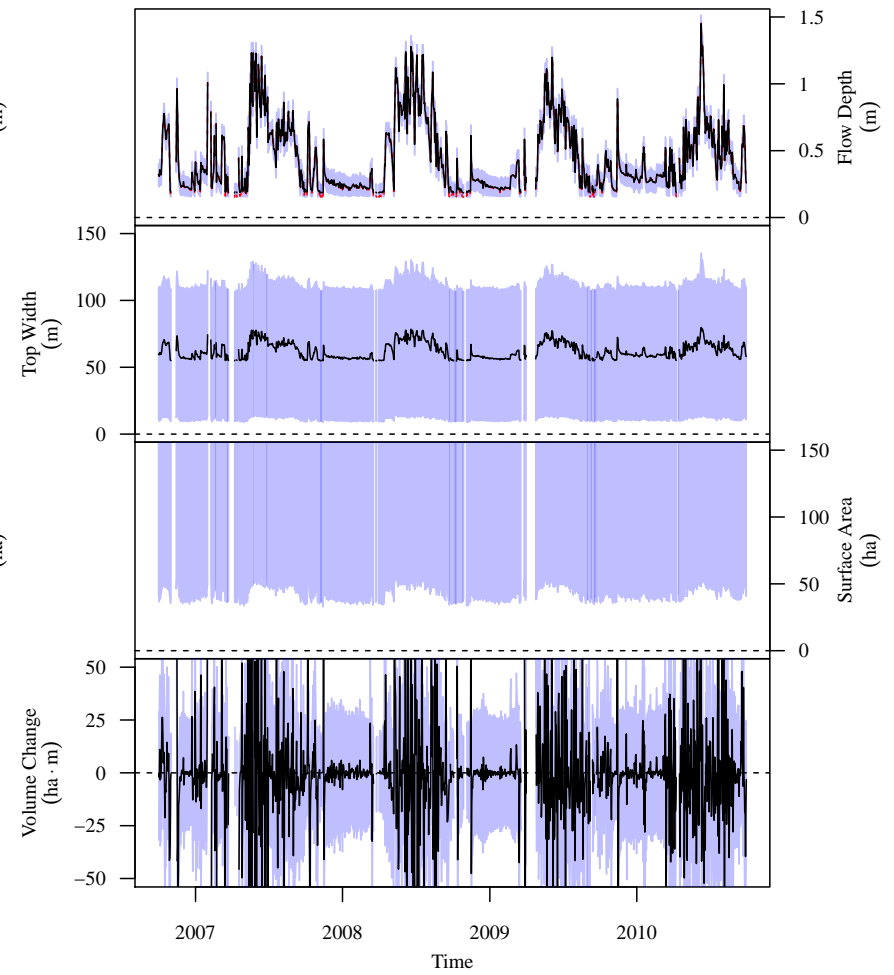


**Figure 4.10.** USR stochastic geometric parameter time-series. The black lines indicate the stochastic model mean time-series. The blue band indicates the 95% central inter-percentile range (CIR) of the stochastic values. The red dashed line in the flow depth portion of the figure indicates the reported flow depth values.



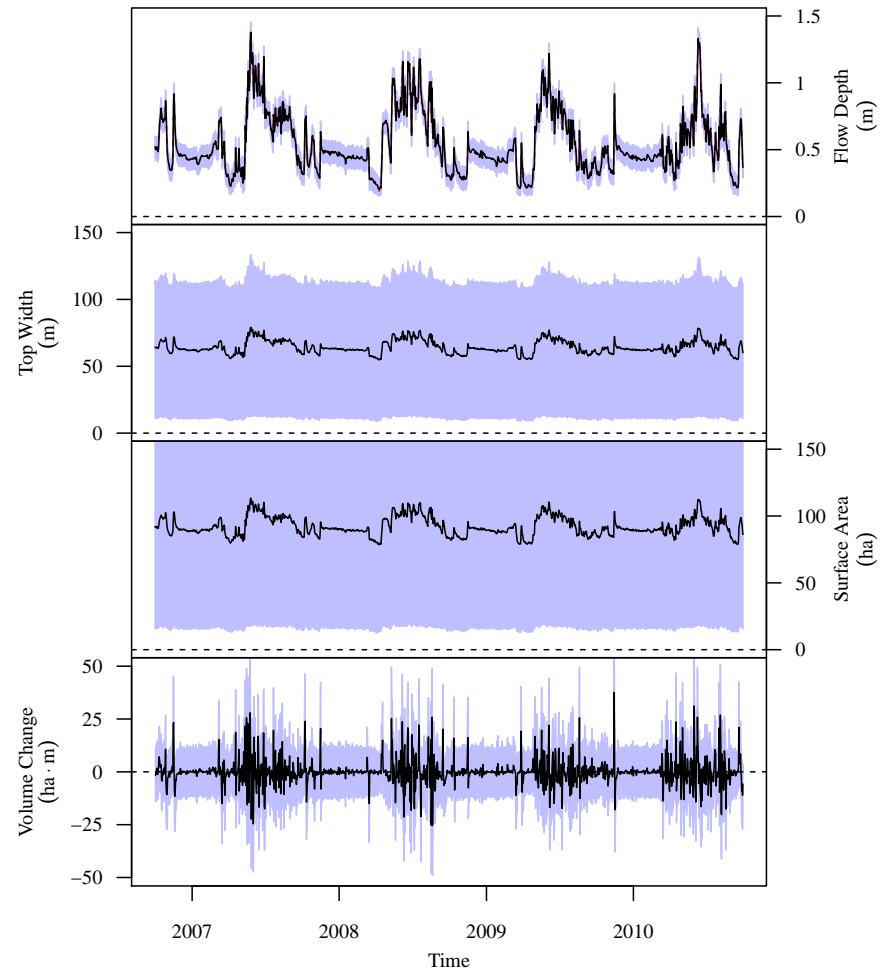


(a) Segment C



(b) Segment D

**Figure 4.10 (Cont).** Stochastic geometric parameter time-series.



(a) Segment E

**Figure 4.10 (Cont).** Stochastic geometric parameter time-series.



**Figure 4.11.** DSR stochastic geometric parameter time-series. The black lines indicate the stochastic model mean time-series. The blue band indicates the 95% central inter-percentile range (CIR) of the stochastic values. The red dashed line in the flow depth portion of the figure indicates the reported flow depth values.

Figures 4.10 and 4.11 were analyzed to verify that direct correlations existed between the flow depth and the calculated geometric parameters. Top width and surface area should increase and decrease in proportion with the increase and decrease in flow depth. Volume changes are based on two flow depth values and do not have a direct correlation to the flow depth displayed in the figure. All of the river sections show the correct correlations between flow depth and the calculated river geometric parameters.

Tables 4.6 and 4.7 present the river segment average daily surface area deterministic model time-series and stochastic model summary statistic time-series results for the USR and DSR, respectively. Summary results for river segment average daily flow depth and river segment average daily top width are not included as they are not direct precursors to the final model results. The surface area is directly used for precipitation and evaporation calculations.

Every one of these tables shows that the stochastic model tends to underestimate the river segment water surface area by approximately 38% in the USR and XX% in the DSR. The correlation values indicate that the deterministic model time-series and stochastic model mean time-series are highly correlated. The corresponding correlation scatter-plots show that the relationships are linear. This is due to the way the river section average daily top width was estimated for the deterministic models. Since  $\beta_1$  and  $\beta_2$  are drawn from distributions and the deterministic model requires that none of the input values are variable, the most likely values from the respective distributions were chosen as the fixed values. The  $\beta$  values from both study reaches are not normal, therefore the most likely value is not the mean and the values are not evenly distributed on either side of the likely value. The skewness of the  $\beta$  values is represented in the stochastic model. Calibrating the deterministic models to find the  $\beta$  values that approximate the stochastic model defeats the

**Table 4.6.** USR river segment surface area deterministic and stochastic model numerical results. Values are in hectares (ha) with values in parentheses in acres (ac).

USR river segment A			
<b>Deterministic Model Time Series</b>			
	2.5th Percentile	Mean	97.5th Percentile
	106.2 (262.4)	134.3 (331.9)	167.1 (412.9)
<b>Stochastic Model Summary Statistics Time Series</b>			
	2.5th Percentile	Mean	97.5th Percentile
97.5th Percentile	134.6 (332.6)	142.7 (352.6)	158.4 (391.4)
Mean	70.1 (173.2)	81.43 (201.2)	95.74 (236.6)
2.5th Percentile	12.05 (29.78)	14.8 (36.57)	17.52 (43.29)
Pearson Correlation = 0.9985			
USR river segment B			
<b>Deterministic Model Time Series</b>			
	2.5th Percentile	Mean	97.5th Percentile
	30.55 (75.49)	38.51 (95.16)	48.96 (121)
<b>Stochastic Model Summary Statistics Time Series</b>			
	2.5th Percentile	Mean	97.5th Percentile
97.5th Percentile	41.49 (102.5)	43.66 (107.9)	47.02 (116.2)
Mean	21.49 (53.1)	24.65 (60.91)	28.48 (70.38)
2.5th Percentile	3.739 (9.239)	4.548 (11.24)	5.408 (13.36)
Pearson Correlation = 0.9982			

purpose of the deterministic model, which is to estimate the most likely values. Sensitivity analysis which is discussed later, will show whether or not the river section average daily surface area values are significant enough to warrant the effort required to calibrate them to the stochastic model.

5        Tables 4.8 and 4.9 present the river segment average daily surface area deterministic model time-series and stochastic model summary statistic time-series results for the USR and DSR, respectively. Summary results for river segment average daily flow depth and

**Table 4.6 (Cont).** USR river segment surface area deterministic and stochastic model numerical results.

USR river segment C			
<b>Deterministic Model Time Series</b>			
	2.5th Percentile	Mean	97.5th Percentile
	237.2 (586.1)	300.9 (743.5)	372.1 (919.5)
<b>Stochastic Model Summary Statistics Time Series</b>			
	2.5th Percentile	Mean	97.5th Percentile
97.5th Percentile	326 (805.6)	341.2 (843.1)	363.2 (897.5)
Mean	165.9 (409.9)	187.4 (463.1)	216.8 (535.7)
2.5th Percentile	27.49 (67.93)	33.26 (82.19)	39.83 (98.42)
Pearson Correlation = 0.9959			
USR river segment D			
<b>Deterministic Model Time Series</b>			
	2.5th Percentile	Mean	97.5th Percentile
	290.3 (717.3)	373.7 (923.4)	497.8 (1230)
<b>Stochastic Model Summary Statistics Time Series</b>			
	2.5th Percentile	Mean	97.5th Percentile
97.5th Percentile	403.9 (998.1)	424.2 (1048)	470.9 (1164)
Mean	208.3 (514.7)	235.7 (582.4)	286.5 (708)
2.5th Percentile	35.28 (87.18)	43.12 (106.6)	54.18 (133.9)
Pearson Correlation = 0.9968			

river segment average daily top width are not included as they are not direct precursors to the final model results. The surface area is directly used for precipitation and evaporation calculations.

The mean of the deterministic model time-series and the mean of the stochastic  
 5 model mean time-series calculated average daily river segment water volume change are much closer to each other as reported in Tables 4.8 and 4.9. The stochastic model mean time-series underestimates the deterministic model time-series values by approximately 47%.

**Table 4.6 (Cont).** USR river segment surface area deterministic and stochastic model numerical results.

USR river segment E			
Deterministic Model Time Series			
	2.5th Percentile	Mean	97.5th Percentile
	121.1 (299.2)	152 (375.6)	187.5 (463.3)
Stochastic Model Summary Statistics Time Series			
	2.5th Percentile	Mean	97.5th Percentile
97.5th Percentile	155.1 (383.3)	162.8 (402.3)	178 (439.8)
Mean	80.04 (197.8)	92.11 (227.6)	107.7 (266.1)
2.5th Percentile	13.69 (33.83)	16.75 (41.39)	19.62 (48.48)
Pearson Correlation = 0.9983			

**Table 4.7.** DSR river segment surface area deterministic and stochastic model numerical results. Values are in hectares (ha) with values in parentheses in acres (ac).

DSR river segment F

DSR river segment G

The difference between the two models in terms of water volume is quite small, less than 1 ha m. The Pearson correlation values and their associated scatter-plots indicate that the results are strongly linearly related. The effects of uncertainty on river segment average river daily water volume change is much smaller than the effect on surface area. As with the surface area results, the significant portion of the difference between the deterministic model time-series and the stochastic model mean time-series is due to the estimation of the most likely values of  $\beta_1$  and  $\beta_2$  used in the deterministic models. At this point, adjusting or calibrating these values such that the results of the deterministic and stochastic models are more closely aligned seems unnecessary.

Figure 4.12 and 4.13 presents the river reach average daily river water storage change deterministic model time-series for the USR. The left-hand figure is the deterministic model

**Table 4.8.** USR river segment volume change deterministic and stochastic model numerical results. Values are in hectare-meters (ha m) and the values in parentheses are in acres (ac).

USR river segment A			
<b>Deterministic Model Time Series</b>			
	2.5th Percentile	Mean	97.5th Percentile
	-20.26 (-164.3)	0.02332 (0.1891)	24.24 (196.5)
<b>Stochastic Model Summary Statistics Time Series</b>			
	2.5th Percentile	Mean	97.5th Percentile
97.5th Percentile	-2.648 (-21.47)	6.181 (50.11)	26.71 (216.5)
Mean	-12.13 (-98.34)	0.01343 (0.1089)	14.6 (118.4)
2.5th Percentile	-22.79 (-184.8)	-6.302 (-51.09)	3.271 (26.52)
Pearson Correlation = 0.9996			
USR river segment B			
<b>Deterministic Model Time Series</b>			
	2.5th Percentile	Mean	97.5th Percentile
	-5.084 (-41.22)	-0.02081 (-0.1687)	5.571 (45.16)
<b>Stochastic Model Summary Statistics Time Series</b>			
	2.5th Percentile	Mean	97.5th Percentile
97.5th Percentile	-0.6022 (-4.882)	2.347 (19.03)	7.577 (61.43)
Mean	-3.259 (-26.42)	-0.0106 (-0.08594)	3.725 (30.2)
2.5th Percentile	-6.961 (-56.43)	-2.401 (-19.47)	0.7138 (5.787)
Pearson Correlation = 0.9995			

time-series. The right-hand figure is the stochastic model results with the black line representing the calculated stochastic model mean time-series and the blue band representing the space between the stochastic model 97.5th percentile time-series and the stochastic model 2.5th percentile time-series. The minimum and maximum range of values is not presented

5 in this figure.



**Table 4.8 (Cont).** USR river segment volume change deterministic and stochastic model numerical results.

USR river segment C			
<b>Deterministic Model Time Series</b>			
	2.5th Percentile	Mean	97.5th Percentile
	-39.47 (-320)	-0.07203 (-0.584)	44.95 (364.4)
<b>Stochastic Model Summary Statistics Time Series</b>			
	2.5th Percentile	Mean	97.5th Percentile
97.5th Percentile	-1.434 (-11.63)	24.14 (195.7)	63.41 (514.1)
Mean	-23.82 (-193.1)	-0.03093 (-0.2508)	26.82 (217.4)
2.5th Percentile	-59.67 (-483.8)	-24.43 (-198.1)	2.816 (22.83)
Pearson Correlation = 0.999			
USR river segment D			
<b>Deterministic Model Time Series</b>			
	2.5th Percentile	Mean	97.5th Percentile
	-83.35 (-675.7)	-0.2914 (-2.362)	108.8 (882.1)
<b>Stochastic Model Summary Statistics Time Series</b>			
	2.5th Percentile	Mean	97.5th Percentile
97.5th Percentile	-10.31 (-83.58)	31.77 (257.6)	126.7 (1027)
Mean	-49.74 (-403.2)	-0.1587 (-1.287)	65.4 (530.2)
2.5th Percentile	-105.4 (-854.5)	-32.74 (-265.4)	14.35 (116.3)
Pearson Correlation = 0.9994			

Table xx presents the deterministic model time-series summary statistics and the summary statistics for each of the stochastic model summary statistics time-series for the river reach average daily water storage change in the USR and DSR.

The figures show that there is a definite seasonal variation in the storage component. Stored water changes are smallest during the cold months and are increasingly larger during the growing season. This pattern is caused by irrigation practices in the Lower Arkansas River Basin (LARV). Stored irrigation water is released from reservoirs upstream of the

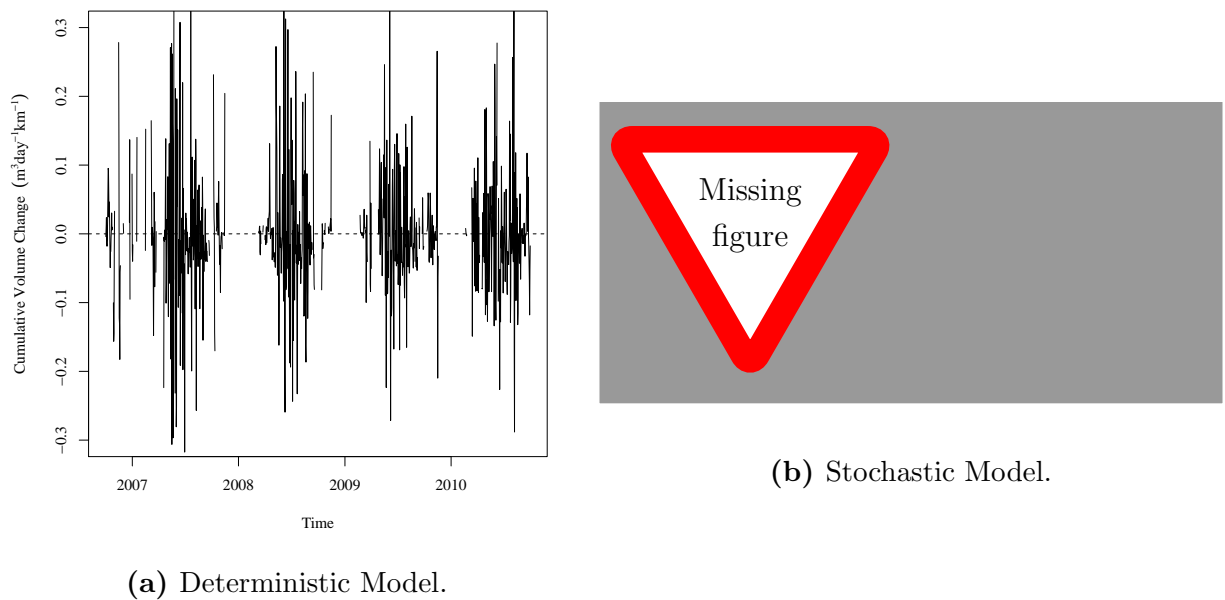
**Table 4.8 (Cont).** USR river segment volume change deterministic and stochastic model numerical results.

USR river segment E			
Deterministic Model Time Series			
	2.5th Percentile	Mean	97.5th Percentile
	-20.02 (-162.3)	-0.01768 (-0.1433)	27.2 (220.5)
Stochastic Model Summary Statistics Time Series			
	2.5th Percentile	Mean	97.5th Percentile
97.5th Percentile	-0.9003 (-7.299)	12.18 (98.74)	35.34 (286.5)
Mean	-11.67 (-94.61)	-0.01049 (-0.08504)	16.3 (132.1)
2.5th Percentile	-28.85 (-233.9)	-12.36 (-100.2)	2.657 (21.54)
Pearson Correlation = 0.9996			

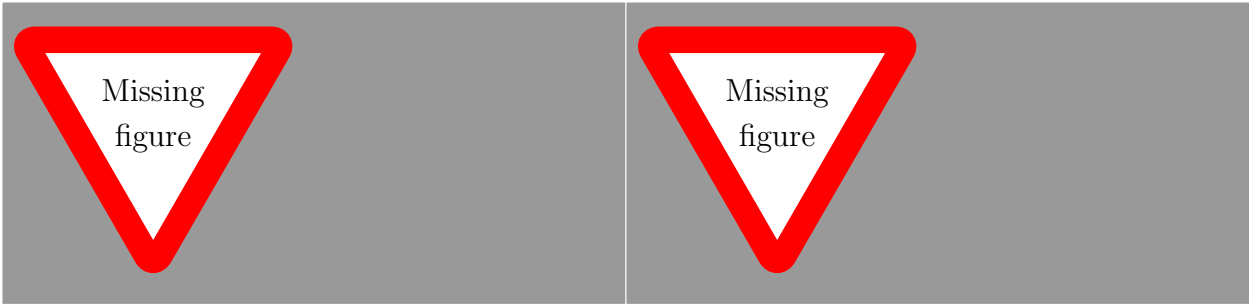
**Table 4.9.** DSR river segment volume change deterministic and stochastic model numerical results. Values are in hectare-meters (ha m) and the values in parentheses are in acres (ac).

DSR river segment F

DSR river segment G



**Figure 4.12.** USR Arkansas River water storage change contribution to the water model.



(a) Deterministic Model.

(b) Stochastic Model.

**Figure 4.13.** USR Arkansas River water storage change contribution to the water model.

(a) USR river reach average daily water storage change.

(b) USR river reach average daily water storage change.

**Table 4.10.** caption

5 LARV during the irrigation season as demands require. During the winter, there is very little to no irrigation occurring. This, combined with the low precipitation and no additional flow from snow-pack runoff, allow flows in the Arkansas R. to reach base flow level when the river is at a natural equilibrium.

This pattern is not as pronounced in the DSR. This is most likely due to required flow rates being maintained at the Colorado-Kansas border. With the constant required  
 5 flow, John Martin Reservoir releases only enough water to meet the required flow rate. This creates a flow regime that is nearly constant through most of the DSR.

Deviations are noted during peak irrigation season. These additional volume changes are most likely due to irrigation flows returning to the Arkansas R. from fields irrigated from canal systems that procure and store water upstream of John Martin Reservoir. The Fort  
 10 Lyon Storage Canal and Fort Lyon Canal are two examples of canal systems that perform this function. Water removed from the USR, stored, and added to the DSR is not included in this study.

**Table 4.11.** USGS Measured Field Parameter Accuracy Rating Table. This table was taken from the USGS annual water data report.

Measured field parameter	Ratings of accuracy (Based on combined fouling and calibration drift corrections applied to the record)			
	Excellent	Good	Fair	Poor
Water temperature	$\leq \pm 0.2\text{ }^{\circ}\text{C}$	$> \pm 0.2 - 0.5\text{ }^{\circ}\text{C}$	$> \pm 0.5 - 0.8\text{ }^{\circ}\text{C}$	$> \pm 0.8\text{ }^{\circ}\text{C}$
Specific conductance	$\leq \pm 3\%$	$> \pm 3 - 10\%$	$> \pm 10 - 15\%$	$> \pm 15\%$
Dissolved oxygen	$\leq \pm 0.3\text{ mg/L}$ or $\leq \pm 5\%$ , whichever is greater	$> \pm 0.3 - 0.5\text{ mg/L}$ or $> \pm 5 - 10\%$ , whichever is greater	$> \pm 0.5 - 0.8\text{ mg/L}$ or $> \pm 10 - 15\%$ , whichever is greater	$> \pm 0.8\text{ mg/L}$ or $> \pm 15\%$ , whichever is greater
pH	$\leq \pm 0.2\text{ units}$	$> \pm 0.2 - 0.5\text{ units}$	$> \pm 0.5 - 0.8\text{ units}$	$> \pm 0.8\text{ units}$
Turbidity	$\leq \pm 0.5\text{ turbidity units}$ or $\leq \pm 5\%$ , whichever is greater	$> \pm 0.5 - 1.0\text{ turbidity units}$ or $> \pm 5 - 10\%$ , whichever is greater	$> \pm 1.0 - 1.5\text{ turbidity units}$ or $> \pm 10 - 15\%$ , whichever is greater	$> \pm 1.5\text{ turbidity units}$ or $> \pm 15\%$ , whichever is greater

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