

$$NML = V_{il} - V_{ol}$$

Part 1

$$k_p' \left(\frac{W_p}{L_p} \right) = k_n' \left(\frac{W_n}{L_n} \right)$$

$$W_p = \frac{k_n' W_n L_p}{k_p' L_n} = \frac{432 \cdot 2 \cdot 0.1}{108 \cdot 0.1} = 8 \mu m$$

$$\frac{k_n' W_n}{2 L_n} (V_{GS} - V_{TN})^2 (1 - \lambda_n (V_{DS} - V_{DSSAT})) = \frac{k_p' W_p}{2 L_p} (V_{GS} + V_{TP})^2 (1 - \lambda_p (V_{SD} - V_{SPSAT}))$$

$$432 \cdot 2 (V_{th} - 0.4)^2 = 108 \cdot 8 (1.2 - V_{th} - 0.4)^2$$

$$V_{th} = 0.6$$

$$k_n' W_n (V_{th} - 0.4)^2 = k_p' W_p \cdot 2 (1.2 - V_{th} - 0.4)^2$$

$$V_{th} = 0.634 \mu m$$

As you decrease K_n , V_{th} goes up

Part 2

$$t_{rise} = t_{fall}$$

$$t_{fall} = \frac{C_L \Delta V}{I_{DN_{avg}}} = \frac{25 \times 10^{-12} \cdot (0.8(1.2))}{I_{DN_{avg}}} = 13.59 ns$$

$$k_n' \frac{W_n}{L_n} \left[\left((V_{GS} - V_{TN}) V_{DS} - \frac{V_{DS}^2}{2} \right) + \frac{k_n' W_n}{2 L_n} (V_{GS} - V_{TN})^2 \right]$$

$$432 \cdot \frac{2}{0.1} \left[(1.2 - 0.4) 0.12 - \frac{0.12^2}{2} \right] + \frac{432 \cdot 2}{2 \cdot 0.1} (1.2 - 0.4)^2$$

$$I_{DN_{avg}} = 1.766 \times 10^{-15}$$

Part 3

$$T = 2 \tau_p F O n$$

Period delay fanout number of inverter stages

$$\Delta t \propto C$$

$$\Delta t_1 = K C_{eff} = t_{delay(NL)}$$

$$\Delta t_2 = K(C_{eff} + C_{ext}) = t_{delay(L)}$$

$$\frac{t_{load}}{t_{no load}} = \frac{C_{left} + C_{ext}}{C_{left}}$$

$$t_{no load} (C_{eff} + C_{ext}) = t_{load} (C_{eff})$$

$$t_{no load} C_{eff} + t_{no load} C_{ext} = t_{load} C_{eff}$$

$$t_{no load} C_{ext} = t_{load} C_{eff} - t_{no load} C_{eff}$$

$$C_{eff} = \frac{t_{no load} C_{ext}}{t_{load} - t_{no load}}$$