Algorithm 1 Shims heuristic at the node π_k

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1: procedure SolveNode(Shims, \pi_k, G, time)
            T_{begin} \leftarrow \text{current system time}
 2:
            Let G(M \cup N_{\pi_k} \cup Q_{\pi_k}, E_{Q_{\pi_k}})
 3:
            Sort M by |D_i^{long}| in non-descending order
 4:

    An empty set of pallet-item edges

 5:
            \tau_{\pi_k} \leftarrow 0
                                                                                                                                                             \triangleright Torque at the node \pi_k
 6:
            \tau_{max} \leftarrow W_{max} \times limit_{long}^{CG}
                                                                                                                                                        ▶ Maximum aircraft torque
 7:
            vol_i \leftarrow 0, \ 1 \le i \le m
 8:
            limit \leftarrow 0.92
 9:
10:
            for i \leftarrow 1 to m
                   for q \leftarrow 1 to m_{\pi_k}
11:
                          \begin{aligned} \textbf{if} \ (i,q) &\in E_{Q_{\pi_k}} \\ vol_i &\leftarrow vol_i + v_q \end{aligned} 
12:
13:
                               \tau_{\pi_k} \leftarrow \tau_{\pi_k} + \hat{v_q \times D_i^{long}}
14:
                  Let E be an array of n_{\pi_k} possibles edges of the pallet i sorted by \theta_{ij}^{\pi_k} in non-ascending order
15:
                  \eta_1 \leftarrow 1
16:
                  repeat
17:
                                                                                                               \triangleright e_{ij} is the allocation of the item j to the pallet i
                         e_{ij} \leftarrow E_{n_1}
18:
                         if (E_{N_{\pi_k}} \cup \{e_{ij}\}) is feasible) and (vol_i \leq V_i \times limit) and (|\tau_{\pi_k} + w_j \times D_i^{long}| \leq W_{max} \times limit_{long}^{CG})
19:
                               E_{N_{\pi_k}} \leftarrow E_{N_{\pi_k}} \cup \{e_{ij}\}
vol_i \leftarrow vol_i + v_j
20:
21:
                               \begin{array}{l} \boldsymbol{\tau_{\pi_k}} \leftarrow \boldsymbol{\tau_{\pi_k}} + \boldsymbol{w_j} \times \boldsymbol{D_i^{long}} \\ \boldsymbol{\eta_1} \leftarrow \boldsymbol{\eta_1} + \boldsymbol{1} \end{array}
22:
23:
                   until (vol_i > V_i \times limit) or (\eta_1 > n_{\pi_k})
                                                                                                                                                             ▶ End of the first phase
24:
                   slack_i \leftarrow V_i - vol_i
25:
26:
                   \eta_2 \leftarrow \eta_1
                   while (\eta_2 \leq n_{\pi_k}) and (vol_i < (1 + 3 \times (1 - limit)) \times V_i))
27:
28:
                         e_{ij} \leftarrow E_{\eta_2}
                         vol_i \leftarrow vol_i + v_i
29:
                                                                                                                                                          ▶ End of the second phase
30:
                         \eta_2 \leftarrow \eta_2 + 1
                   vol \leftarrow 0, b \leftarrow 1, shims_b \leftarrow \emptyset, Set \leftarrow \{shims_b\}
31:
                   for x \leftarrow \eta_1 to \eta_2
32:
                         if T_{current} - T_{begin} > time
33:
                               break
                                                                                                                                                                 ▶ Time limit exceeded
34:
                         NewShims \leftarrow \mathbf{True}
35:
36:
                         e_{ij} \leftarrow E_x
                         for shims \in Set
37:
                               if (e_{ij} \notin (E_{N_{\pi_{l}}} \cup shims)) and (e_{ij} \text{ is feasible}) and ((v_j + vol) \leq slack_i)
38:
                                      shims \leftarrow \ddot{s}hims \cup \{e_{ij}\}
39:
                                      vol \leftarrow vol + v_i
40:
                                      NewShims \leftarrow False
41:
42:
                                      break
                         if NewShims
43:
                               vol \leftarrow 0
44:
                               b \leftarrow b + 1
45:
                               shims_b \leftarrow \{\ \}
46:
                               shims_b \leftarrow shims_b \cup \{e_{ij}\}
47:
                               Set \leftarrow Set \cup \{ shims_b \}
48:
                  sh_w \leftarrow shims, where shims \in Set and \sum_{e_{ab} \in shims} w_b is maximum sh_v \leftarrow shims, where shims \in Set and \sum_{e_{ab} \in shims} v_b is maximum sh_{best} \leftarrow shims, where shims \in \{sh_w, sh_v\} and \sum_{e_{ab} \in x} s_b is maximum
49:
50:
51:
                                                                                                                                                             ▷ End of the third phase
                   E_{N_{\pi_{k}}} \leftarrow E_{N_{\pi_{k}}} \cup sh_{best}
52:
            return G(M \cup N_{\pi_k} \cup Q_{\pi_k}, E_{Q_{\pi_k}} \cup E_{N_{\pi_k}})
53:
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Initially, Q_{π_k} (line 3) corresponds to the packed contents that remain on board. It is important to remember that $E_{Q_{\pi_k}}$ and M were modified by $UpdatePacked(M, Q_{\pi_k}, \pi_k)$ and $SetPalletsDestinations(M, \pi_k)$. Then, the pallets i are considered in non-descending order of $|D_i^{long}|$.

For each pallet i, its n_{π_k} possible edges $e_{ij}^{\pi_k}$ are considered in non-increasing order of $\theta_{ij}^{\pi_k}$:

• In the greedy phase (lines 4-24), a partial solution for each pallet i is constructed by edges inclusion, until its volume $V_i \times limit$ is reached. The value limit = 0.92 (line 9) was empirically determined by the iRace tool [?].

From lines 9 to 24, as items are inserted, the value of η_1 is incremented and stops when the pallet volume reaches 92% of its capacity.

When it stops, this is the initial value of η_2 , line 26. η_2 , then it is incremented until the volume exceeds the pallet capacity with a factor of 1 + (2 x [1 - limit]). This factor of was obtained empirically, through many test with different problem instances. Higher values can improve the solution, but at the expense of performance. So we tried to keep it as low as possible, a trade-off between quality and performance.

• In the *composition phase* (lines 25-30), a set of shims named Set is created for each pallet i, where each shim is formed by a set of edges in the range $[\eta_1, \eta_2]$, whose total volume is limited by $slack_i$.

After the η_2 index, there may be items with little probability of being in the optimal solution because their low value of $\theta_{ij}^{\pi_k}$, being not considered for inclusion.

In line 31 the initial *Shim* and *Set* are created.

In this phase, the heuristic that provided the best results, both in terms of time and quality, is based on $First-Fit\ Decreasing$, which is an approximation algorithm for the $Bin\ Packing\ Problem\ [?]$. Basically, shims are created by accumulating the following edges, taking $slack_i$ as a limit.

• In the selection phase (lines 31-52), the best shim in Set is chosen. Initially, two shims are found: sh_w with larger weight, and sh_v with larger volume. Between the two, the one with the highest score will be chosen and its edges are inserted into $E_{N_{\pi_b}}$.