This chapter describes how you can perform the conversions required by the IEEE standard using MathLib C functions. For each type of conversion, this chapter lists the functions you can use to perform that conversion. It shows the declarations of these functions, describes what they do, describes when they raise floating-point exceptions, and gives examples of how to use them. For a description of the conversions required by the IEEE standard and the details of how each conversion is performed in PowerPC Numerics, see Chapter 5, "Conversions." All of the conversion function declarations appear in the file fp.h.

Converting Floating-Point to Integer Formats

In C, the default method of converting floating-point numbers to integers is to simply discard the fractional part (truncate). MathLib provides two functions that convert floating-point numbers to integers using methods other than the default C method and that return the integers in integer types.

rinttol(x) Returns the nearest integer to x in the current rounding direction as an

integer type.

roundtol(x) Adds 1/2 to the magnitude of x, chops to an integer, and returns the

value as an integer type.

rinttol

You can use the rinttol function to round a real number to the nearest integer in the current rounding direction.

```
long int rinttol (double_t x);
```

x Any floating-point number.

DESCRIPTION

The rinttol function rounds its argument to the nearest integer in the current rounding direction and places the result in a long int type. The available rounding directions are upward, downward, to nearest, and toward zero.

The rinttol function provides the floating-point to integer conversion as described in the IEEE standard. It differs from rint (described on page 6-13) in that it returns the value in an integer type; rint returns the value in a floating-point type.

EXCEPTIONS

When x is finite and nonzero, either the result of rinttol(x) is exact or it raises one of the following exceptions:

- inexact (if *x* is not an integer)
- invalid (if the integer result is outside the range of the long int type)

SPECIAL CASES

Table 9-1 shows the results when the argument to the rinttol function is a zero, a NaN, or an Infinity.

 Table 9-1
 Special cases for the rinttol function

Operation	Result	Exceptions raised
rinttol(+0)	+0	None
rinttol(-0)	-0	None
rinttol(NaN)	Undefined	None [*]
$rinttol(+\infty)$	Undefined	Invalid
rinttol(-∞)	Undefined	Invalid

^{*} If the NaN is a signaling NaN, the invalid exception is raised.

EXAMPLES

roundtol

You can use the roundtol function to round a real number to the nearest integer value by adding 1/2 to the magnitude and truncating.

long int roundtol (double_t x);

x Any floating-point number.

DESCRIPTION

The roundtol function adds 1/2 to the magnitude of its argument and chops to integer, returning the answer in long int type.

The result is returned in an integer data type. (The return type is the difference between the roundtol function and the round function, described on page 9-10.)

This function is not affected by the current rounding direction. Notice that the roundtol function rounds halfway cases (1.5, 2.5, and so on) away from 0. With the default rounding direction, rinttol (described on page 9-3) rounds halfway cases to the even integer.

EXCEPTIONS

When x is finite and nonzero, either the result of roundtol(x) is exact or it raises one of the following exceptions:

- \blacksquare inexact (if x is not an integer)
- invalid (if the integer result is outside the range of the long int type)

SPECIAL CASES

Table 9-2 shows the results when the argument to the roundtol function is a zero, a NaN, or an Infinity.

Table 9-2 Special cases for the roundtol function

Operation	Result	Exceptions raised
roundtol(+0)	+0	None
roundtol(-0)	-0	None
roundtol(NaN)	Undefined	None*
$roundtol(+\infty)$	Undefined	Invalid
$roundtol(-\infty)$	Undefined	Invalid

^{*} If the NaN is a signaling NaN, the invalid exception is raised.

EXAMPLES

Rounding Floating-Point Numbers to Integers

MathLib provides six functions that convert floating-point numbers to integers and return the integer in a floating-point type. The first is the rint function, which performs the round-to-integer operation as described in Chapter 6, "Numeric Operations and Functions." The other functions either round in a specific direction or perform a variation of the rint operation.

ceil(x)	Returns the nearest integer not less than x .
floor(x)	Returns the nearest integer not greater than x .
nearbyint(x)	Returns the nearest integer to x in the current rounding direction.
round(x)	Adds $1/2$ to the magnitude of x and chops to an integer.
trunc(x)	Truncates the fractional part of <i>x</i> .

ceil

You can use the ceil function to round a real number upward to the nearest integer value.

DESCRIPTION

The ceil function rounds its argument upward. This is an ANSI standard C library function. The result is returned in a floating-point data type.

This function is the same as performing the following code sequence:

EXCEPTIONS

When x is finite and nonzero, the result of ceil(x) is exact.

SPECIAL CASES

Table 9-3 shows the results when the argument to the ceil function is a zero, a NaN, or an Infinity.

 Table 9-3
 Special cases for the ceil function

	Resul	
Operation	t	Exceptions raised
ceil(+0)	+0	None
ceil(-0)	-0	None
ceil(NaN)	NaN	None*
ceil(+∞)	+∞	None
ceil(-∞)	-∞	None

^{*} If the NaN is a signaling NaN, the invalid exception is raised.

EXAMPLES

```
z = ceil(+INFINITY); /* z = +INFINITY because +INFINITY is already an integer value by definition. */ z = ceil(300.1); /* z = 301.0 */ z = ceil(-300.1); /* z = -300.0 */
```

floor

You can use the floor function to round a real number downward to the next integer value.

```
double_t floor (double_t x);
```

x Any floating-point number.

DESCRIPTION

The floor function rounds its argument downward. This is an ANSI standard C library function. The result is returned in a floating-point data type.

This function is the same as performing the following code sequence:

EXCEPTIONS

When x is finite and nonzero, the result of floor(x) is exact.

SPECIAL CASES

Table 9-4 shows the results when the argument to the floor function is a zero, a NaN, or an Infinity.

 Table 9-4
 Special cases for the floor function

Operation	Resul t	Exceptions raised
floor(+0)	+0	None
floor(-0)	-0	None
floor(NaN)	NaN	None*
floor(+∞)	+∞	None
floor(-∞)	-∞	None

^{*} If the NaN is a signaling NaN, the invalid exception is raised.

EXAMPLES

```
z = floor(+INFINITY); /* z = +INFINITY because +\infty is already an integer value by definition. */

z = floor(300.1); /* z = 300.0 */

z = floor(-300.1); /* z = -301.0 */
```

nearbyint

You can use the nearbyint function to round a real number to the nearest integer in the current rounding direction.

DESCRIPTION

The nearbyint function rounds its argument to the nearest integer in the current rounding direction. The available rounding directions are upward, downward, to nearest, and toward zero.

The nearbyint function provides the floating-point to integer conversion described in the IEEE Standard 854. It differs from rint (described on page 6-13) only in that it does not raise the inexact flag when the argument is not already an integer.

EXCEPTIONS

When x is finite and nonzero, the result of nearbyint(x) is exact.

SPECIAL CASES

Table 9-5 shows the results when the argument to the nearbyint function is a zero, a NaN, or an Infinity.

 Table 9-5
 Special cases for the nearbyint function

Operation	Resul t	Exceptions raised
nearbyint(+0)	+0	None
nearbyint(-0)	-0	None
nearbyint(NaN)	NaN	None*
$nearbyint(+\infty)$	+∞	None
$nearbyint(-\infty)$	-∞	None

^{*} If the NaN is a signaling NaN, the invalid exception is raised.

EXAMPLES

round

You can use the round function to round a real number to the integer value obtained by adding 1/2 to the magnitude and truncating.

DESCRIPTION

The round function adds 1/2 to the magnitude of its argument and chops to integer. The result is returned in a floating-point data type.

This function is not affected by the current rounding direction. Notice that the round function rounds halfway cases (1.5, 2.5, and so on) away from 0. With the default rounding direction, rint (described on page 6-13) rounds halfway cases to the even integer.

EXCEPTIONS

When x is finite and nonzero, either the result of round(x) is exact or it raises the following exception:

■ inexact (if *x* is not an integer value)

SPECIAL CASES

Table 9-6 shows the results when the argument to the round function is a zero, a NaN, or an Infinity.

Table 9-6 Special cases for the round function

Operation	Resul t	Exceptions raised
round(+0)	+0	None
round(-0)	-0	None
round(NaN)	NaN	None*
$round(+\infty)$	+∞	None
round(-∞)	-∞	None

^{*} If the NaN is a signaling NaN, the invalid exception is raised.

EXAMPLES

```
 z = \text{round(+INFINITY)}; \qquad /* \ z = +\text{INFINITY because} \ +\infty \ \text{is already an integer value by definition.} \ */ \\ z = \text{round(0.5)}; \qquad /* \ z = 1.0 \ \text{because} \ |0.5| \ + 0.5 = 1.0. \ \text{The inexact exception is raised.} \ */ \\ z = \text{round(-0.9)}; \qquad /* \ z = -1.0 \ \text{because} \ |-0.9| \ + 0.5 = 1.4. \\ \text{The inexact exception is raised.} \ */
```

trunc

You can use the trunc function to truncate the fractional part of a real number so that just the integer part remains.

```
double_t trunc (double_t x);
x Any floating-point number.
```

DESCRIPTION

The trunc function chops off the fractional part of its argument. This is an ANSI standard C library function.

This function is the same as performing the following code sequence:

EXCEPTIONS

When x is finite and nonzero, the result of trunc(x) is exact.

SPECIAL CASES

Table 9-7 shows the results when the argument to the trunc function is a zero, a NaN, or an Infinity.

 Table 9-7
 Special cases for the trunc function

Operation	Resul t	Exceptions raised
trunc(+0)	+0	None
trunc(-0)	-0	None
trunc(NaN)	NaN	None*
trunc(+∞)	+∞	None
trunc(-∞)	-∞	None

^{*} If the NaN is a signaling NaN, the invalid exception is raised.

EXAMPLES

Converting Integers to Floating-Point Formats

In the C programming language, conversions from integers stored in an integer format to floating-point formats are automatic when you assign an integer to a floating-point variable.

Converting Between Floating-Point Formats

In the C programming language, conversions between floating-point formats are automatic when you assign a floating-point number of one type to a variable of another type.

Converting Between Binary and Decimal Numbers

MathLib provides two functions that let you manually convert between binary and decimal formats.

```
dec2num Converts a decimal number to a binary number.
num2dec Converts a binary number to a decimal number.
```

Conversions between binary floating-point numbers and decimal numbers use structures of type decimal. The decimal structure is defined in the header file fp.h as

The significand. String sig.text contains the significand as a decimal integer in the form of a string, that is, with the string length in the zeroth byte (sig.length) and the initial character of the string in the first byte (sig.text[0] to sig.text[SIGDIGLEN - 1]).

The value represented is

```
(-1)^{sgn} \times sig \times 10^{exp}
```

For example, if sgn equals 1, exp equals -3, and sig equals "85" (string length sig.length equals 2, not shown), then the number represented is -0.085.

Note

The maximum length of the string sig is implementation dependent. The limit is 36 characters. Also, the representations of 0 and 1 in the 16-bit word sgn are implementation dependent. ◆

Conversions from binary to decimal use a decimal format structure to specify how the number should look in decimal. The decform structure is defined in the header file fp.h as

Note

Formatting details, such as the representations of 0 and 1 in the 16-bit style word, are implementation dependent. •

If the style field of the decform structure equals 0 (in C, f.style == FLOATDECIMAL), the output is formatted in floating style, with the digits field specifying the number of significant digits required. Output in floating style is represented in the following format; Table 9-8 defines its components.

```
[- \mid ]m[.nnn]e[+ \mid -]dddd
```

Table 9-8 Format of decimal output string in floating style

Component	Description
Minus sign (–) or space	Minus sign if $sgn = 1$; space if $sgn = 0$
m	Single digit, 0 only if value represented is 0
Point (.)	Present if digits > 1
nnn	String of digits; present if digits > 1
е	The letter e
Plus sign (+) or minus sign (-)	Plus sign if $\exp \ge 0$; minus sign if $\exp < 0$.
dddd	One to four exponent digits

If the style field of the decform structure equals 1 (in C, f.style == FIXEDDECIMAL), the output is formatted in fixed style, with the digits field specifying the number of digits to follow the decimal point. All output in fixed style is represented in the following format; Table 9-9 defines its components.

[-]*mmm*[.*nnn*]

 Table 9-9
 Format of decimal output string in fixed style

Component	Description
Minus sign (–)	Present if sgn = 1
mmm	String of digits; at least one digit but no superfluous leading zeros
Point (.)	Present if $digits > 0$
nnn	String of digits of length equal to digits; present if digits > 0

Note that if sgn equals 0, then floating-style output begins with a space but fixed-style output does not.

Double-double values being converted to decimal strings are first rounded to 113 bits (if they in fact span more than that number of bits in their significands) and then converted to the decimal string of the desired length.

dec2num

You can use the dec2num function to convert a decimal number to a binary floating-point number.

```
float dec2f (const decimal *d);
double_t dec2num (const decimal *d);
long double dec2numl (const decimal *d);
short int dec2s (const decimal *d);
long int dec2l (const decimal *d);
```

The decimal structure to be converted. See page 9-13 for the definition of the decimal structure.

DESCRIPTION

The dec2num function converts a decimal number in a decimal structure to a double format floating-point number. Conversions from the decimal structure type handle any sig string of length 36 or less (with an implicit decimal point at the right end).

There are three versions of this function that convert to a floating-point type: dec2f converts the decimal number to the float type, dec2num converts to the double type, and dec2numl converts to the long double type. The other two versions of this function, dec2s and dec2l, convert to the short and long integer types, respectively.

IMPORTANT

When you create a decimal structure, you must set sig.length to the size of the string you place in sig.text. You cannot leave the length field undefined. ▲

Before using this function, you can use the numeric formatter (str2dec, described on page 9-21) to convert a decimal string to a decimal structure suitable for input to the dec2num function.

EXCEPTIONS

When the sig string is longer than 36 characters, the result is undefined.

SPECIAL CASES

The following special cases apply:

■ If sig.text[0] is "0" (zero), the decimal structure is converted to zero. For example, a decimal structure with sig = "0913" is converted to zero.

- If sig.text[0] is "N", the decimal structure is converted to a NaN. The succeeding characters of sig are interpreted as a hexadecimal representation of the result's significand: if fewer than four characters follow the N, then they are right aligned in the high-order 15 bits of the field f illustrated in the section "Formats" in Chapter 2, "Floating-Point Data Formats"; if four or more characters follow the N, then they are left aligned in the result's significand.
- If sig.text[0] is "I", the decimal structure is converted to an Infinity.

EXAMPLES

num2dec

You can use the num2dec function to convert a binary floating-point number to a decimal number.

```
void num2dec (const decform *f, double_t x, decimal *d); void num2decl (const decform *f, long double x, decimal *d);
```

- f A decform structure that describes how the number should look in decimal. See page 9-14 for a description of the decform structure.
- x The floating-point number to be converted.
- d Upon return, a pointer to the decimal structure containing the number. See page 9-13 for a description of the decimal structure.

DESCRIPTION

The num2dec function converts a floating-point number to a decimal number. The decimal number is contained in a decimal structure. Each conversion to a decimal structure d is controlled by a decform structure f. All implementations allow 36 digits to be returned in the sig field of the decimal structure. The implied decimal point is at the right end of sig, with exp set accordingly.

After using the num2dec function, you can use the dec2str function to convert the decimal structure to a character string.

IMPORTANT

Use the same decimal format structure settings for dec2str as you used for num2dec; otherwise, the results are unspecified. \blacktriangle

EXCEPTIONS

When the number of digits specified in a decform structure exceeds an implementation maximum (which is 36), the result is undefined.

A number might be too large to represent in a chosen fixed style. For instance, if the implementation's maximum length for sig is 36, then 10^{35} (which requires 33 digits to the left of the point in fixed-style representations) is too large for a fixed-style representation specifying more than two digits to the right of the point. If a number is too large for a chosen fixed style, then (depending on the numeric implementation) one of two results is returned: an implementation might return the most significant digits of the number in sig and set exp so that the decimal structure contains a valid floating-style approximation of the number; alternatively, an implementation might simply set sig to the string "?". Note that in any implementation, the following test determines whether a nonzero finite number is too large for the chosen fixed style.

```
decimal d;
decform f;
int too_big; /* Boolean */
too_big = (-d.exp != f.digits) || (d.sig.text[0] == "?");
```

For fixed-point formatting, PowerPC Numerics treats a negative value for digits as a specification for rounding to the left of the decimal point; for example, digits = -2 means to round to hundreds. For floating-point formatting, a negative value for digits gives unspecified results.

SPECIAL CASES

- For zeros, the character "0" is placed in sig.text[0].
- For NaNs, The character "N" is placed in sig.text[0]. The character "N" might be followed by a hexadecimal representation of the input significand. The third and fourth hexadecimal digits following the "N" give the NaN code. For example, "N402100000000000" has NaN code 0x21.
- For Infinities, the character "I" is placed in sig.text[0].

In all three of these cases, exp is undefined.

EXAMPLES

Converting Between Decimal Formats

MathLib provides a scanner for converting from decimal strings to decimal structures and a formatter for converting from decimal structures to decimal strings.

dec2str Converts decimal structures to decimal strings. The PowerPC Numerics

formatter.

str2dec Converts decimal strings to decimal structures. The PowerPC Numerics

scanner.

dec2str

You can use the dec2str function to convert a number in a decimal structure to a decimal string.

void dec2str (const decform *f, const decimal *d, char *s);

- f A decform structure that describes how the number should look in decimal. See page 9-14 for a description of the decform structure.
- d The decimal structure to be converted. See page 9-13 for the definition of the decimal structure.
- s On return, a string representing the number in decimal.

DESCRIPTION

The dec2str function is the PowerPC Numerics formatter. It takes a number from a decimal structure and converts it to a string. You can use the num2dec function to convert a binary floating-point number to a decimal structure appropriate for input to the dec2str function.

IMPORTANT

Use the same decimal format structure settings for dec2str as you used for num2dec; otherwise, results are unspecified. •

The numeric formatter is controlled by a decform structure f. With floating style, numbers formatted using the same value for f.digits have aligning decimal points and e's. To ensure that numbers have the same width also, pad the exponent-digits field with spaces to a width of 4. For example, if f.digits = 12, then pad 12 + 8 - length(s) spaces on the right of the result string s. The value 8 accounts for the sign, point, letter e, exponent sign, and four exponent digits. Note that this scheme gives the correct field width for NaNs and Infinities too.

With fixed style, numbers formatted using the same value for f.digits have aligning decimal points if enough leading spaces are added to the result string s to attain a fixed width, which must be no narrower than the widest s.

IMPORTANT

When you create a decimal structure, you must set sig.length to the size of the string you place in sig.text. You cannot leave the length field undefined. ▲

EXCEPTIONS

The formatter is always exact and signals no exceptions.

SPECIAL CASES

For fixed-point formatting, dec2str treats a negative value for digits as a specification for rounding to the left of the decimal point; for example, digits = -2 means to round to hundreds. For floating-point formatting, values for digits less than 1 are treated as 1.

NaNs are formatted as NAN; Infinities are formatted as INF. A leading sign or space is included according to the style convention.

The formatter never returns fewer significant digits than are contained in sig. However, if the decform structure calls for more significant digits than are contained in sig, then the formatter pads with zeros as needed.

If more than 80 characters are required to honor digits, then the formatter returns the string "?".

EXAMPLES

Suppose you have an accounting program that computes exact values using binary numbers of pennies and prints outputs in dollars and cents. If you simply divide the number of pennies by 100 to get dollars, you incur errors because hundredths are not exact in binary. One way to print out exact values in dollars and cents is to convert the number of pennies to a decimal structure, perform the division by adjusting the exponent, and print the result, as shown in Listing 9-1.

Listing 9-1 Accounting program

```
#include <fp.h>
   decform
               df;
   double
                           /* This is the input value */
               pennies;
   decimal
               dpennies;
                           /* decimal value for pennies */
   char *
               dollars;
                            /* string to print as $$$.¢¢ */
{
   df.style = FIXEDDECIMAL;
   df.digits = 0;
                     /* start with 0 digits after decimal point */
   num2dec(&df, pennies, &dpennies);
                                              /* decimal pennies */
                                              /* divide by 100 */
   dpennies.exp = dpennies.exp - 2;
                         /* request 2 digits after decimal point */
   df.digits = 2;
   dec2str(&df, &dpennies, dollars);
   /* dollar string to print */
}
```

str2dec

You can use the str2dec function to convert a decimal string to a decimal structure.

void str2dec (const char *s, short *ix, decimal *d, short *vp);

```
The character string containing the number to be converted.

On entry, the starting position in the string. On return, one greater than the position of the last character in the string that was parsed if the entire string was not converted successfully.
```

- d On return, a pointer to the decimal structure containing the decimal number. See page 9-13 for a description of the decimal structure.
- vp On return, a Boolean argument indicating the success of the function. If the entire string was parsed, vp is true. If part of the string was parsed, vp is false and ix indicates where the function stopped parsing.

DESCRIPTION

The str2dec function is the PowerPC Numerics scanner, which is designed for use both with fixed strings and with strings being received interactively character by character. The scanner parses the longest possible numeric substring; if no numeric substring is recognized, then the value of ix remains unchanged.

To convert floating-point strings embedded in text, parse to the beginning of a floating-point string ($[+ \mid -] digit$) and pass the current scan location as the index into the text. The conversion routine will return the value scanned and a new value of the index for continued parsing.

You might need to distinguish those numeric ASCII strings that represent values of an integer format. You can do this by scanning the source, looking for integer syntax. You can handle integers yourself and send to the numeric scanner any strings with floating-point syntax (that is, containing a period (.), an E, or an e). You might also want to pass along to the scanner any strings that cause integer overflow.

EXCEPTIONS

The scanner signals no exceptions. It faithfully converts all values within range that are representable in the decimal structure format.

SPECIAL CASES

To convert a zero, NaN, or Infinity, use one of the following as input:

```
-0 +0 0 -INF Inf NAN -NaN() nan
```

EXAMPLES

Listing 9-2 shows an example of how to scan decimal strings into an application and then convert the strings to binary floating-point numbers using MathLib functions. Table 9-10 shows some sample inputs to the loop shown in Listing 9-2 and the results after each string has been converted to a decimal structure using str2dec.

Listing 9-2 Scanning algorithm

```
s = "";  /* initialize string */

/* loop until string is not a valid prefix*/
do
  {
    /* code to get next character and append to string goes here */
    /* scan string */
    ix = 0;
    str2dec(s, &ix, &d, &vp);
    }
while (vp = false);
/* convert from decimal to numeric-format result */
result = dec2num(d);
```

 Table 9-10
 Examples of conversions to decimal structures

Input	In	dex	Output	
string	In	Out	value	Valid prefix
12	0	2	12	True
12E	0	2	12	True
12E-	0	2	12	True
12E-3	0	5	12E-3	True
12E-X	0	2	12	False
12E-3X	0	5	12E-3	False
x12E-3	1	6	12E-3	True
IN	0	0	NAN	True
INF	0	3	INF	True

Conversions Summary

This section summarizes the C constants, macros, functions, and type definitions associated with converting floating-point values.

C Summary

Constants

```
#define SIGDIGLEN 36 /* significant decimal digits */
#define DECSTROUTLEN 80 /* max length for dec2str output */
#define FLOATDECIMAL ((char)(0))
#define FIXEDDECIMAL ((char)(1))
```

Data Types

```
struct decimal
                                           /* sign 0 for +, 1 for - */
   char sgn;
  char unused;
                                           /* decimal exponent */
   short exp;
   struct
      unsigned char length;
      unsigned char text[SIGDIGLEN];
                                           /* significant digits */
      unsigned char unused;
   } sig;
};
typedef struct decimal decimal;
struct decform
   char style;
                                        /* FLOATDECIMAL or FIXEDDECIMAL */
   char unused;
   short digits;
typedef struct decform decform;
```

Conversion Routines

Converting Floating-Point Formats to Integer Formats

Rounding Floating-Point Numbers to Integers

Converting Decimal Numbers to Binary Numbers

```
float dec2f (const decimal *d);
double_t dec2num (const decimal *d);
long double dec2numl (const decimal *d);
short int dec2s (const decimal *d);
long int dec2l (const decimal *d);
```

Converting Binary Numbers to Decimal Numbers

Converting Between Decimal Formats