

# Digital Circuits Assignment 3 / 2013 Güz

①

		c			
		00	01	11	10
00			1		
01	1		1	1	1
11	1	1	1		1
10	1	1			1

a | b

$$\bar{c}d, b\bar{c}, \bar{a}b, a\bar{c}, a\bar{d}, b\bar{d}$$

Symbol	Prime Implicant	Covered points	Cost
A	$\bar{c}d$	1, 9, 13	5
B	$b\bar{c}$	4, 12, 13	5
C	$\bar{a}b$	4, 6, 7	5
D	$a\bar{c}$	8, 9, 12, 13	5
E	$a\bar{d}$	8, 12, 14	5
F	$b\bar{d}$	4, 6, 12, 14	5

distinguished points

	1	4	6	7	8	9	12	13	14	Cost
✓ A	X					X		X		5
B		X					X	X		5
✓ C		X	X	X						5
D					X	X	X	X		5
E					X		X		X	5
F		X	X				X		X	5

Step 1:  
1 and 7 are distinguished points. So, A and C have to be in the final result.  
(mark them and can remove the rows and columns they cover.)

	8	12	14	Cost
B		X		5
D	X	X		5
E	X	X	X	5
F		X	X	5

Step 2:

Column 12 covers column 8 and column 14. So, I can remove column 12.

(Bu adım olmadan da E direkt seçilebilir!)

	8	14	Cost
D	X		5
✓ E	X	X	5
F		X	5

Step 3

E covers both 8 and 14.  
So, F have to be in the final result.

$$\text{So result with minimum cost} = A + C + E = \bar{c}d + \bar{a}b + a\bar{d}$$

$$\Rightarrow \text{min Cost} = 5 + 5 + 5 = 15$$

Sonuç : ~~XXXXXXXXXX~~  $\bar{a}b + \bar{c}d + a\bar{d}$

