

#### Gradient Descent

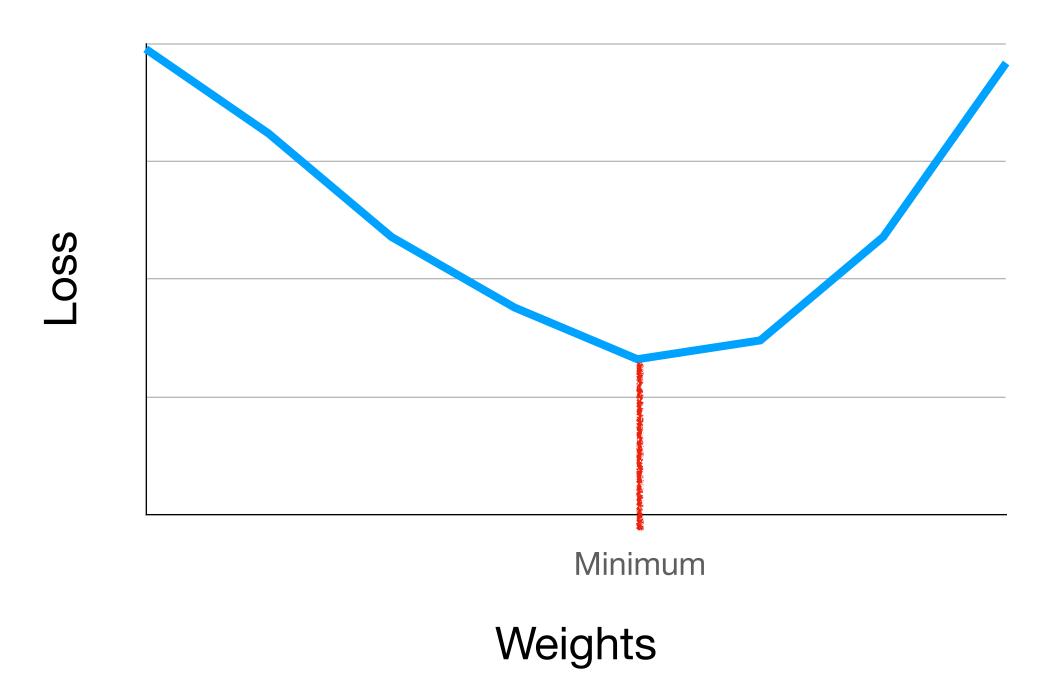
Finding the optimal weights



### Loss Functions

#### How do we find the lowest loss?

- Back Propagation is the process we use to update the individual weights or gradients
  - wx + b
- Our goal is finding the right value of weights where the loss is lowest
- The method by which we achieve this goal (i.e. updating all weights to lower the total loss) is called Gradient Descent
- It's the point at which we find the optimal weights such that loss is near lowest





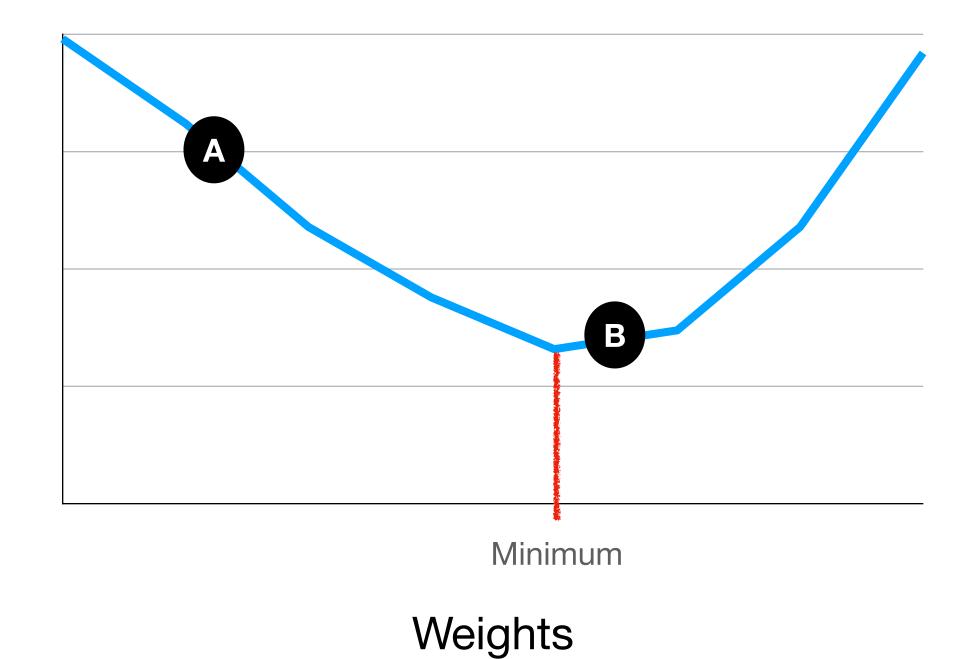
### Gradients

#### Gradients are the derivative of a function

• It tells us the rate of change of one variable with respect to the other e.g.

$$Gradient = \frac{dE}{dw}, \text{ where } E \text{ is the Error or Loss and } w \text{ is the weight}$$

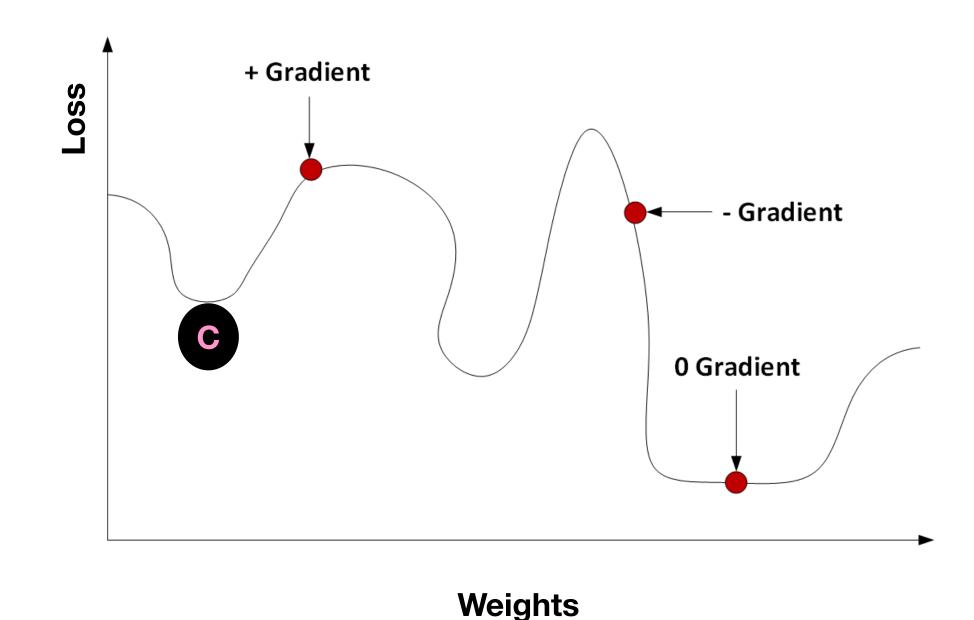
- A positive gradient means, loss increases if weights increase
- A negative gradient means, loss decreases if weights increase
- At point A, moving right increases our weights and decreases our loss, -ve
- A point B, moving right increases our weights and increases our loss, +ve
- Therefore, the negative of our gradient tells us the direction we should be moving





#### More on Gradients

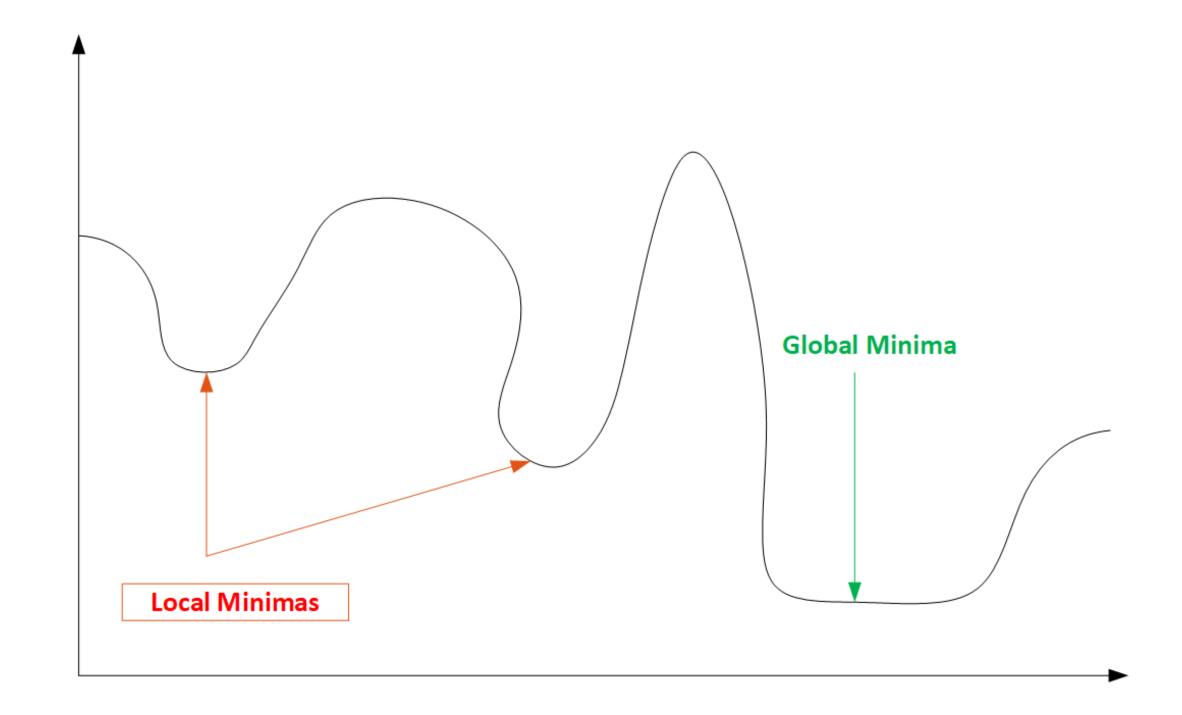
- The point at which a Gradient is zero means that small changes to the left or right don't change the loss
- In training Neural Networks this is good and bad
- At point, C, very small changes to the left or right don't change the Loss
- This means, our network gets stuck during training.
- This is called getting stuck in a Local Minima





## Local and Global Minimas

- We always want to find the Global Minima during training.
- That is the point where the combination of weights give the lowest loss





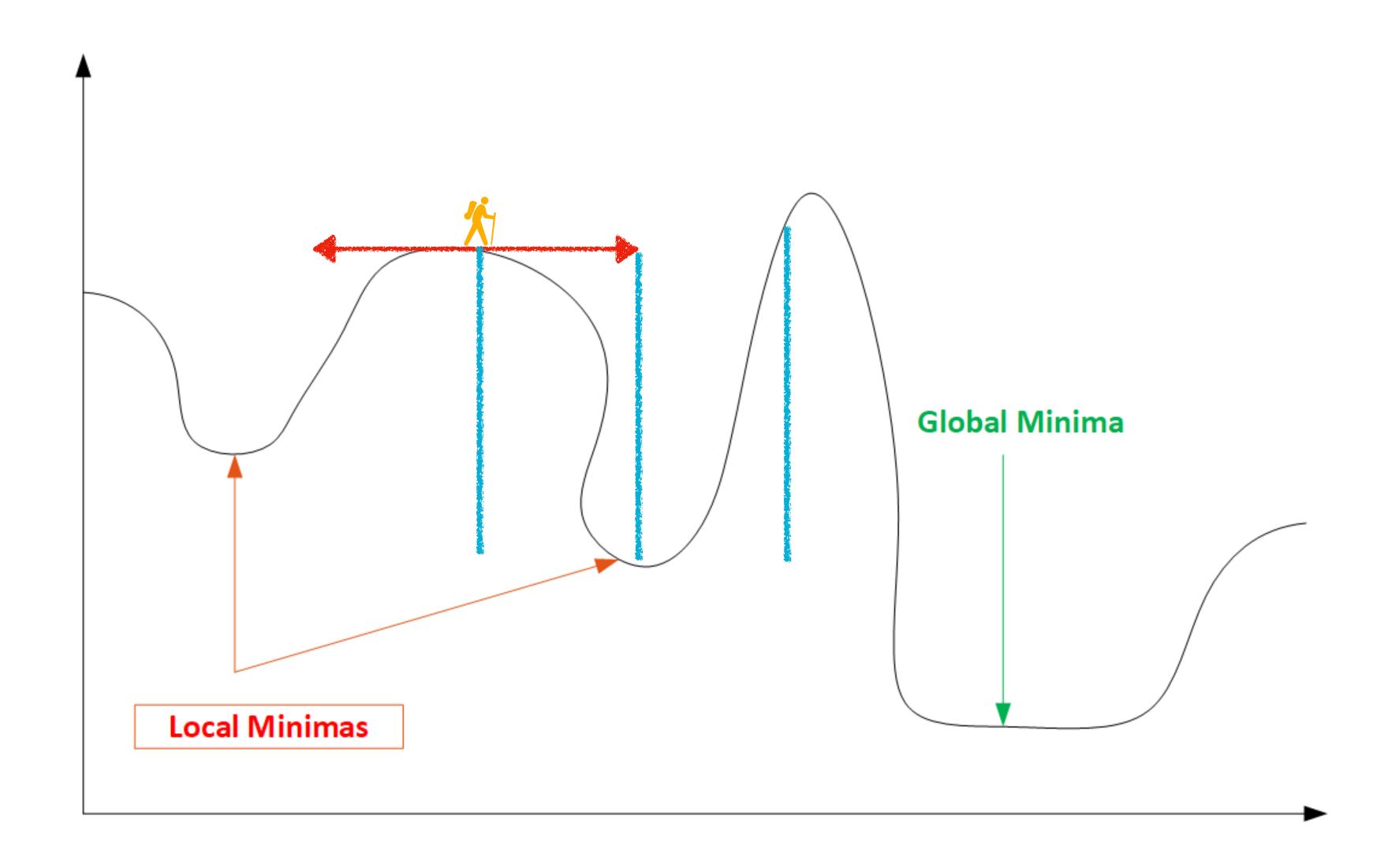
#### Gradient Descent

- Imagine being a really tiny person and you're traversing down the slope of this old, rough bowl.
- There'd be peaks, valleys, troughs etc.
- How do you know when you're truly at the bottom?
- Possibly take large steps so you don't get stuck in a valley
- But then you risk jumping over the Global Minima





## Step Size is Important





## Learning Rates

#### Recall our Back Propagation Weight Update Formula

$$W_5 = -\lambda \times \frac{dE_T}{dW_5}$$

- $\lambda$  is our learning rate
- Learning Rates allow us to adjust the magnitude of jumps in weights
- Finding an optimal value will avoid us finding Local Minimums and while preventing us from jumping over the Global Minimum.



### Gradient Descent Methods

- Naive Gradient Descent Passes the entire dataset through our network then updates the weights.
  - It is computationally expensive and slow.
- Stochastic Gradient Descent (SGD) Updates weights after each data sample (image) is forward propagated through our network.
  - This leads to noisy fluctuating loss values and is also slow to train
- Mini-Batch Gradient Descent Combines both methods, it takes a batch of data points (images) and forward propagates all, then updates the gradients.
  - This leads to faster training and convergence to the Global Minima
  - Batches are typically 8 to 256 in size

# Next...

**Optimisers** 

