# The Parma Polyhedra Library C Language Interface User's Manual\* (version 0.10.2)

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All the declarations needed for using the PPL's C interface (preprocessor symbols, data types, variables and functions) are collected in the header file ppl\_c.h. This file, which is designed to work with pre-ANSI and ANSI C compilers as well as C99 and C++ compilers, should be included, either directly or via some other header file, with the directive

```
#include <ppl_c.h>
```

If this directive does not work, then your compiler is unable to find the file ppl\_c.h. So check that the library is installed (if it is not installed, you may want to make install, perhaps with root privileges) in the right place (if not you may want to reconfigure the library using the appropriate pathname for the -prefix option); and that your compiler knows where it is installed (if not you should add the path to the directory where ppl\_c.h is located to the compiler's include file search path; this is usually done with the -I option).

The name space of the PPL's C interface is PPL\_\* for preprocessor symbols, enumeration values and variables; and ppl\_\*\* for data types and function names. The interface systematically uses *opaque data types* (generic pointers that completely hide the internal representations from the client code) and provides all required access functions. By using just the interface, the client code can exploit all the functionalities of the library yet avoid directly manipulating the library's data structures. The advantages are that (1) applications do not depend on the internals of the library (these may change from release to release), and (2) the interface invariants can be thoroughly checked (by the access functions).

The PPL's C interface is initialized by means of the ppl\_initialize function. This function must be called *before using any other interface of the library*. The application can release the resources allocated by the library by calling the ppl\_finalize function. After this function is called *no other interface of the library may be used* until the interface is re-initialized using ppl\_initialize.

Any application using the PPL should make sure that only the intended version(s) of the library are ever used. The version used can be checked at compile-time thanks to the macros PPL\_VERSION\_MAJOR,

PPL\_VERSION\_MINOR, PPL\_VERSION\_REVISION and PPL\_VERSION\_BETA, which give, respectively major, minor, revision and beta numbers of the PPL version. This is an example of their use:

```
#if PPL_VERSION_MAJOR == 0 && PPL_VERSION_MINOR < 6
# error "PPL version 0.6 or following is required"
#endif</pre>
```

Compile-time checking, however, is not normally enough, particularly in an environment where there is dynamic linking. Run-time checking can be performed by means of the functions ppl\_version\_major, ppl\_version\_minor, ppl\_version\_revision, and ppl\_version\_beta. The PPL's C interface also provides functions ppl\_version, returning character string containing the full version number, and ppl\_banner, returning a string that, in addition, provides (pointers to) other useful information for the library user.

All programs using the PPL's C interface must link with the following libraries: <code>libppl\_c</code> (PPL's C interface), <code>libppl</code> (PPL's core), <code>libgmpxx</code> (GMP's C++ interface), and <code>libgmp</code> (GMP's library core). On most Unix-like systems, this is done by adding <code>-lppl\_c</code>, <code>-lppl</code>, <code>-lgmpxx</code>, and <code>-lgmp</code> to the compiler's or linker's command line. For example:

```
gcc myprogram.o -lppl_c -lppl -lgmpxx -lgmp
```

If this does not work, it means that your compiler/linker is not finding the libraries where it expects. Again, this could be because you forgot to install the library or you installed it in a non-standard location. In the latter case you will need to use the appropriate options (usually -L) and, if you use shared libraries, some sort of run-time path selection mechanisms. Consult your compiler's documentation for details. Notice that the PPL is built using Libtool and an application can exploit this fact to significantly simplify the linking phase. See Libtool's documentation for details. Those working under Linux can find a lot of useful information on how to use program libraries (including static, shared, and dynamically loaded libraries) in the Program Library HOWTO.

For examples on how to use the functions provided by the C interface, you are referred to the directory demos/ppl\_lpsol/ in the source distribution. It contains a *Mixed Integer (Linear) Programming* solver written in C. In order to use this solver you will need to install GLPK (the GNU Linear Programming Kit): this is used to read linear programs in MPS format.

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Version 3, 29 June 2007

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# 4 Module Index

#### 4.1 Modules

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# 5.1 Class List

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# 6 Module Documentation

# **6.1** C Language Interface

The Parma Polyhedra Library comes equipped with an interface for the C language.

# 6.2 Library Initialization and Finalization

# **Functions**

- int ppl\_initialize (void)

  Initializes the Parma Polyhedra Library. This function must be called before any other function.
- int ppl\_finalize (void)

  Finalizes the Parma Polyhedra Library. This function must be called after any other function.
- int ppl\_set\_rounding\_for\_PPL (void)

  Sets the FPU rounding mode so that the PPL abstractions based on floating point numbers work correctly.
- int ppl\_restore\_pre\_PPL\_rounding (void)

  Sets the FPU rounding mode as it was before initialization of the PPL.

# 6.2.1 Detailed Description

Functions for initialization/finalization of the library, as well as setting/resetting of floating-point rounding mode.

#### 6.2.2 Function Documentation

# 6.2.2.1 int ppl\_initialize (void)

Initializes the Parma Polyhedra Library. This function must be called before any other function.

#### **Returns:**

PPL ERROR INVALID ARGUMENT if the library was already initialized.

# 6.2.2.2 int ppl\_finalize (void)

Finalizes the Parma Polyhedra Library. This function must be called after any other function.

# **Returns:**

PPL\_ERROR\_INVALID\_ARGUMENT if the library was already finalized.

#### 6.2.2.3 int ppl\_set\_rounding\_for\_PPL (void)

Sets the FPU rounding mode so that the PPL abstractions based on floating point numbers work correctly.

This is performed automatically at initialization-time. Calling this function is needed only if restore\_pre\_-PPL\_rounding() has been previously called.

# 6.2.2.4 int ppl\_restore\_pre\_PPL\_rounding (void)

Sets the FPU rounding mode as it was before initialization of the PPL.

After calling this function it is absolutely necessary to call set\_rounding\_for\_PPL() before using any PPL abstractions based on floating point numbers. This is performed automatically at finalization-time.

# **6.3** Version Checking

#### **Defines**

- #define PPL\_VERSION "0.10.2"
   A string containing the PPL version.
- #define PPL\_VERSION\_MAJOR 0
   The major number of the PPL version.
- #define PPL\_VERSION\_MINOR 10

  The minor number of the PPL version.
- #define PPL\_VERSION\_REVISION 2
   The revision number of the PPL version.

• #define PPL\_VERSION\_BETA 0

The beta number of the PPL version. This is zero for official releases and nonzero for development snapshots.

#### **Functions**

- int ppl\_version\_major (void)

  Returns the major number of the PPL version.
- int ppl\_version\_minor (void)

  Returns the minor number of the PPL version.
- int ppl\_version\_revision (void)

  Returns the revision number of the PPL version.
- int ppl\_version\_beta (void)

  Returns the beta number of the PPL version.
- int ppl\_version (const char \*\*p)

  Writes to \*p a pointer to a character string containing the PPL version.
- int ppl\_banner (const char \*\*p)

  Writes to \*p a pointer to a character string containing the PPL banner.

# **6.3.1 Detailed Description**

Symbolic constants and functions related to library version checking.

#### 6.3.2 Define Documentation

# 6.3.2.1 #define PPL\_VERSION "0.10.2"

A string containing the PPL version.

Let M and m denote the numbers associated to PPL\_VERSION\_MAJOR and PPL\_VERSION\_MINOR, respectively. The format of PPL\_VERSION is M "." m if both PPL\_VERSION\_REVISION (r) and PPL\_VERSION\_BETA (b)are zero, M "." m "pre" b if PPL\_VERSION\_REVISION is zero and PPL\_VERSION\_BETA is not zero, M "." m "." r if PPL\_VERSION\_REVISION is not zero and PPL\_VERSION\_BETA is zero, M "." m "." r "pre" b if neither PPL\_VERSION\_REVISION nor PPL\_VERSION\_BETA are zero.

#### **6.3.3** Function Documentation

# 6.3.3.1 int ppl\_banner (const char \*\*p)

Writes to \*p a pointer to a character string containing the PPL banner.

The banner provides information about the PPL version, the licensing, the lack of any warranty whatsoever, the C++ compiler used to build the library, where to report bugs and where to look for further information.

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# 6.4 Error Handling

#### **Enumerations**

• enum ppl\_enum\_error\_code {

PPL\_ERROR\_OUT\_OF\_MEMORY, PPL\_ERROR\_INVALID\_ARGUMENT, PPL\_ERROR\_DOMAIN\_ERROR, PPL\_ERROR\_LENGTH\_ERROR,

PPL\_ARITHMETIC\_OVERFLOW, PPL\_STDIO\_ERROR, PPL\_ERROR\_INTERNAL\_ERROR, PPL\_ERROR\_UNKNOWN\_STANDARD\_EXCEPTION,

PPL\_ERROR\_UNEXPECTED\_ERROR }

Defines the error codes that any function may return.

#### **Functions**

• int ppl\_set\_error\_handler (void(\*h)(enum ppl\_enum\_error\_code code, const char \*description))

Installs the user-defined error handler pointed at by h.

#### 6.4.1 Detailed Description

Symbolic constants and functions related to error reporting/handling.

# **6.4.2** Enumeration Type Documentation

#### 6.4.2.1 enum ppl\_enum\_error\_code

Defines the error codes that any function may return.

#### **Enumerator:**

- **PPL\_ERROR\_OUT\_OF\_MEMORY** The virtual memory available to the process has been exhausted.
- PPL ERROR INVALID ARGUMENT A function has been invoked with an invalid argument.
- PPL\_ERROR\_DOMAIN\_ERROR A function has been invoked outside its domain of definition.
- **PPL\_ERROR\_LENGTH\_ERROR** The construction of an object that would exceed its maximum permitted size was attempted.
- **PPL\_ARITHMETIC\_OVERFLOW** An arithmetic overflow occurred and the computation was consequently interrupted. This can *only* happen in library's incarnations using bounded integers as coefficients.
- **PPL\_STDIO\_ERROR** An error occurred during a C input/output operation. A more precise indication of what went wrong is available via erro.
- **PPL\_ERROR\_INTERNAL\_ERROR** An internal error that was diagnosed by the PPL itself. This indicates a bug in the PPL.
- **PPL\_ERROR\_UNKNOWN\_STANDARD\_EXCEPTION** A standard exception has been raised by the C++ run-time environment. This indicates a bug in the PPL.
- **PPL\_ERROR\_UNEXPECTED\_ERROR** A totally unknown, totally unexpected error happened. This indicates a bug in the PPL.

#### 6.4.3 Function Documentation

# 6.4.3.1 int ppl\_set\_error\_handler (void(\*)(enum ppl\_enum\_error\_code code, const char \*description) h)

Installs the user-defined error handler pointed at by h.

The error handler takes an error code and a textual description that gives further information about the actual error. The C string containing the textual description is read-only and its existence is not guaranteed after the handler has returned.

# **6.5** Library Datatypes

Typedefs for the library datatypes and related symbolic constants.

# **Typedefs**

- typedef size\_t ppl\_dimension\_type

  An unsigned integral type for representing space dimensions.
- typedef const char \* ppl\_io\_variable\_output\_function\_type (ppl\_dimension\_type var)

  The type of output functions used for printing variables.
- typedef struct ppl\_Coefficient\_tag \* ppl\_Coefficient\_t
   Opaque pointer.
- typedef struct ppl\_Coefficient\_tag const \* ppl\_const\_Coefficient\_t
   Opaque pointer to const object.
- typedef struct ppl\_Linear\_Expression\_tag const \* ppl\_const\_Linear\_Expression\_t
   Opaque pointer to const object.
- typedef struct ppl\_Constraint\_tag \* ppl\_Constraint\_t
   Opaque pointer.
- typedef struct ppl\_Constraint\_tag const \* ppl\_const\_Constraint\_t
   Opaque pointer to const object.

- typedef struct ppl\_Constraint\_System\_const\_iterator\_tag \* ppl\_Constraint\_System\_const\_iterator\_t

  Opaque pointer.

typedef struct ppl\_Constraint\_System\_const\_iterator\_tag const \* ppl\_const\_Constraint\_System\_const\_iterator\_t

Opaque pointer to const object.

- typedef struct ppl\_Generator\_System\_const\_iterator\_tag \* ppl\_Generator\_System\_const\_iterator\_t Opaque pointer.
- typedef struct ppl\_Generator\_System\_const\_iterator\_tag const \* ppl\_const\_Generator\_System\_const\_iterator\_t

Opaque pointer to const object.

- typedef struct ppl\_Congruence\_System\_const\_iterator\_tag \* ppl\_Congruence\_System\_const\_iterator\_t

Opaque pointer.

• typedef struct ppl\_Congruence\_System\_const\_iterator\_tag const \* ppl\_const\_Congruence\_-System\_const\_iterator\_t

Opaque pointer to const object.

- typedef struct ppl\_Grid\_Generator\_tag \* ppl\_Grid\_Generator\_t Opaque pointer.
- typedef struct ppl\_Grid\_Generator\_System\_tag \* ppl\_Grid\_Generator\_System\_t

Opaque pointer.

- typedef struct ppl\_Grid\_Generator\_System\_const\_iterator\_tag \* ppl\_Grid\_Generator\_System\_const\_iterator\_t

Opaque pointer.

• typedef struct ppl\_Grid\_Generator\_System\_const\_iterator\_tag const \* ppl\_const\_Grid\_Generator\_ System\_const\_iterator\_t

Opaque pointer to const object.

- typedef struct ppl\_MIP\_Problem\_tag \* ppl\_MIP\_Problem\_t
   Opaque pointer.

- typedef struct ppl\_Polyhedron\_tag const \* ppl\_const\_Polyhedron\_t
   Opaque pointer to const object.
- $\bullet \ \ typedef \ struct \ ppl\_Pointset\_Powerset\_C\_Polyhedron\_tag * ppl\_Pointset\_Powerset\_C\_Polyhedron\_t$

Opaque pointer.

• typedef struct ppl\_Pointset\_Powerset\_C\_Polyhedron\_tag const \* ppl\_const\_Pointset\_Powerset\_C\_-Polyhedron\_t

Opaque pointer to const object.

 typedef struct ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_tag \* ppl\_Pointset\_Powerset\_C\_-Polyhedron\_iterator\_t

Opaque pointer.

• typedef struct ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_tag const \* ppl\_const\_Pointset\_-Powerset\_C\_Polyhedron\_iterator\_t

Opaque pointer to const object.

• typedef struct ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_tag \* ppl\_Pointset\_Powerset\_-C\_Polyhedron\_const\_iterator\_t

Opaque pointer.

• typedef struct ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_tag const \* ppl\_const\_-Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_t

Opaque pointer to const object.

#### **Enumerations**

enum ppl\_enum\_Constraint\_Type {
 PPL\_CONSTRAINT\_TYPE\_LESS\_THAN, PPL\_CONSTRAINT\_TYPE\_LESS\_OR\_EQUAL,
 PPL\_CONSTRAINT\_TYPE\_EQUAL, PPL\_CONSTRAINT\_TYPE\_GREATER\_OR\_EQUAL,
 PPL\_CONSTRAINT\_TYPE\_GREATER\_THAN }

Describes the relations represented by a constraint.

enum ppl\_enum\_Generator\_Type { PPL\_GENERATOR\_TYPE\_LINE, PPL\_GENERATOR\_TYPE\_RAY, PPL\_GENERATOR\_TYPE\_POINT, PPL\_GENERATOR\_TYPE\_CLOSURE\_POINT }

Describes the different kinds of generators.

enum ppl\_enum\_Grid\_Generator\_Type { PPL\_GRID\_GENERATOR\_TYPE\_LINE, PPL\_GRID\_GENERATOR\_TYPE\_PARAMETER, PPL\_GRID\_GENERATOR\_TYPE\_POINT }

Describes the different kinds of grid generators.

#### **Functions**

- int ppl\_max\_space\_dimension (ppl\_dimension\_type \*m)

  Writes to m the maximum space dimension this library can handle.
- int ppl\_not\_a\_dimension (ppl\_dimension\_type \*m)

  Writes to m a value that does not designate a valid dimension.
- int ppl\_io\_print\_variable (ppl\_dimension\_type var)

  \*Pretty-prints var to stdout.
- int ppl\_io\_fprint\_variable (FILE \*stream, ppl\_dimension\_type var)

  Pretty-prints var to the given output stream.
- int ppl\_io\_asprint\_variable (char \*\*strp, ppl\_dimension\_type var)

  Pretty-prints var to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_io\_set\_variable\_output\_function (ppl\_io\_variable\_output\_function\_type \*p)

  Sets the output function to be used for printing variables to p.
- int ppl\_io\_get\_variable\_output\_function (ppl\_io\_variable\_output\_function\_type \*\*pp)

  Writes a pointer to the current variable output function to pp.
- char \* ppl\_io\_wrap\_string (const char \*src, unsigned indent\_depth, unsigned preferred\_first\_line\_length, unsigned preferred\_line\_length)

 ${\it Utility function for the wrapping of lines of text.}$ 

#### Variables

unsigned int PPL\_COMPLEXITY\_CLASS\_POLYNOMIAL
 Code of the worst-case polynomial complexity class.

• unsigned int PPL\_COMPLEXITY\_CLASS\_SIMPLEX

Code of the worst-case exponential but typically polynomial complexity class.

unsigned int PPL COMPLEXITY CLASS ANY

Code of the universal complexity class.

unsigned int PPL\_POLY\_CON\_RELATION\_IS\_DISJOINT

Individual bit saying that the polyhedron and the set of points satisfying the constraint are disjoint.

• unsigned int PPL\_POLY\_CON\_RELATION\_STRICTLY\_INTERSECTS

Individual bit saying that the polyhedron intersects the set of points satisfying the constraint, but it is not included in it.

• unsigned int PPL\_POLY\_CON\_RELATION\_IS\_INCLUDED

Individual bit saying that the polyhedron is included in the set of points satisfying the constraint.

• unsigned int PPL\_POLY\_CON\_RELATION\_SATURATES

Individual bit saying that the polyhedron is included in the set of points saturating the constraint.

• unsigned int PPL\_POLY\_GEN\_RELATION\_SUBSUMES

Individual bit saying that adding the generator would not change the polyhedron.

# **6.5.1 Detailed Description**

Typedefs for the library datatypes and related symbolic constants.

The datatypes provided by the library should be manipulated by means of the corresponding opaque pointer types and the functions working on them.

#### Note:

To simplify the detection of common programming mistakes, we provide both pointer-to-const and pointer-to-nonconst opaque pointers, with implicit conversions mapping each pointer-to-nonconst to the corresponding pointer-to-const when needed. The user of the C interface is therefore recommended to adopt the pointer-to-const type whenever read-only access is meant.

#### **6.5.2** Typedef Documentation

# 6.5.2.1 typedef const char\* ppl\_io\_variable\_output\_function\_type(ppl\_dimension\_type var)

The type of output functions used for printing variables.

An output function for variables must write a textual representation for var to a character buffer, null-terminate it, and return a pointer to the beginning of the buffer. In case the operation fails, 0 should be returned and perhaps errno should be set in a meaningful way. The library does nothing with the buffer, besides printing its contents.

# 6.5.3 Enumeration Type Documentation

# 6.5.3.1 enum ppl\_enum\_Constraint\_Type

Describes the relations represented by a constraint.

# **Enumerator:**

```
PPL\_CONSTRAINT\_TYPE\_LESS\_THAN The constraint is of the form e < 0. PPL\_CONSTRAINT\_TYPE\_LESS\_OR\_EQUAL The constraint is of the form e \le 0. PPL\_CONSTRAINT\_TYPE\_EQUAL The constraint is of the form e = 0. PPL\_CONSTRAINT\_TYPE\_GREATER\_OR\_EQUAL The constraint is of the form e \ge 0. PPL\_CONSTRAINT\_TYPE\_GREATER\_THAN The constraint is of the form e > 0.
```

# 6.5.3.2 enum ppl\_enum\_Generator\_Type

Describes the different kinds of generators.

#### **Enumerator:**

```
PPL_GENERATOR_TYPE_LINE The generator is a line.
PPL_GENERATOR_TYPE_RAY The generator is a ray.
PPL_GENERATOR_TYPE_POINT The generator is a point.
PPL_GENERATOR_TYPE_CLOSURE_POINT The generator is a closure point.
```

# 6.5.3.3 enum ppl\_enum\_Grid\_Generator\_Type

Describes the different kinds of grid generators.

# **Enumerator:**

```
PPL_GRID_GENERATOR_TYPE_LINE The grid generator is a line.
PPL_GRID_GENERATOR_TYPE_PARAMETER The grid generator is a parameter.
PPL_GRID_GENERATOR_TYPE_POINT The grid generator is a point.
```

# **6.5.4** Function Documentation

# 6.5.4.1 char\* ppl\_io\_wrap\_string (const char \* src, unsigned indent\_depth, unsigned preferred\_first\_line\_length, unsigned preferred\_line\_length)

Utility function for the wrapping of lines of text.

#### **Parameters:**

```
src The source string holding the text to wrap.indent_depth The indentation depth.preferred_first_line_length The preferred length for the first line of text.preferred_line_length The preferred length for all the lines but the first one.
```

# Returns:

The wrapped string in a malloc-allocated buffer.

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# 7 Class Documentation

# 7.1 ppl\_Coefficient\_tag Interface Reference

Types and functions for coefficients.

```
#include <ppl_c_header.h>
```

#### **Related Functions**

(Note that these are not member functions.)

# Constructors, Assignment and Destructor

int ppl\_new\_Coefficient (ppl\_Coefficient\_t \*pc)
 Creates a new coefficient with value 0 and writes a handle for the newly created coefficient at address pc.

• int ppl\_new\_Coefficient\_from\_mpz\_t (ppl\_Coefficient\_t \*pc, mpz\_t z)

Creates a new coefficient with the value given by the GMP integer z and writes a handle for the newly created coefficient at address pc.

- int ppl\_new\_Coefficient\_from\_Coefficient (ppl\_Coefficient\_t \*pc, ppl\_const\_Coefficient\_t c)

  Builds a coefficient that is a copy of c; writes a handle for the newly created coefficient at address pc.
- int ppl\_assign\_Coefficient\_from\_mpz\_t (ppl\_Coefficient\_t dst, mpz\_t z)

  Assign to dst the value given by the GMP integer z.
- int ppl\_assign\_Coefficient\_from\_Coefficient (ppl\_Coefficient\_t dst, ppl\_const\_Coefficient\_t src)

  Assigns a copy of the coefficient src to dst.
- int ppl\_delete\_Coefficient (ppl\_const\_Coefficient\_t c)

  Invalidates the handle c: this makes sure the corresponding resources will eventually be released.

#### **Read-Only Accessor Functions**

- int ppl\_Coefficient\_to\_mpz\_t (ppl\_const\_Coefficient\_t c, mpz\_t z)

  Sets the value of the GMP integer z to the value of c.
- int ppl\_Coefficient\_OK (ppl\_const\_Coefficient\_t c)

  Returns a positive integer if c is well formed i.e. if it satisfies all its imit

Returns a positive integer if c is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if c is broken. Useful for debugging purposes.

• int ppl\_Coefficient\_is\_bounded (void)

Returns a positive integer if coefficients are bounded; returns 0 otherwise.

• int ppl\_Coefficient\_min (mpz\_t min)

Returns a positive integer if coefficients are bounded, in which case min is set to their minimum value; returns 0 otherwise.

• int ppl Coefficient max (mpz t max)

Returns a positive integer if coefficients are bounded, in which case max is set to their maximum value; returns 0 otherwise.

#### I/O Functions

- int ppl\_io\_print\_Coefficient (ppl\_const\_Coefficient\_t x)

  \*Prints x to stdout.
- int ppl\_io\_fprint\_Coefficient (FILE \*stream, ppl\_const\_Coefficient\_t x)

  Prints x to the given output stream.
- int ppl\_io\_asprint\_Coefficient (char \*\*strp, ppl\_const\_Coefficient\_t x)

  Prints x to a malloc-allocated string, a pointer to which is returned via strp.

# 7.1.1 Detailed Description

Types and functions for coefficients.

The types and functions for coefficients provide an interface towards *Coefficient*. Depending on configuration, the PPL coefficients may be implemented by the unbounded precision integers provided by GMP (default), or by bounded precision integers (with checks for overflows).

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.2 ppl\_Congruence\_System\_const\_iterator\_tag Interface Reference

Types and functions for iterating on congruence systems.

```
#include <ppl_c_header.h>
```

#### **Related Functions**

(Note that these are not member functions.)

# Constructors, Assignment and Destructor

int ppl\_new\_Congruence\_System\_const\_iterator (ppl\_Congruence\_System\_const\_iterator\_t \*pcit)

Builds a new 'const iterator' and writes a handle to it at address poit.

• int ppl\_new\_Congruence\_System\_const\_iterator\_from\_Congruence\_System\_const\_iterator (ppl\_Congruence\_System\_const\_iterator\_t \*pcit, ppl\_const\_Congruence\_System\_const\_iterator\_t cit)

Builds a const iterator that is a copy of cit; writes an handle for the newly created const iterator at address pcit.

• int ppl\_assign\_Congruence\_System\_const\_iterator\_from\_Congruence\_System\_const\_iterator (ppl\_Congruence\_System\_const\_iterator\_t dst, ppl\_const\_Congruence\_System\_const\_iterator\_t src)

Assigns a copy of the const iterator src to dst.

• int ppl\_delete\_Congruence\_System\_const\_iterator (ppl\_const\_Congruence\_System\_const\_iterator t cit)

Invalidates the handle cit: this makes sure the corresponding resources will eventually be released.

#### **Dereferencing, Incrementing and Equality Testing**

• int ppl\_Congruence\_System\_const\_iterator\_dereference (ppl\_const\_Congruence\_System\_const\_iterator\_t cit, ppl\_const\_Congruence\_t \*pc)

Dereference cit writing a const handle to the resulting congruence at address pc.

int ppl\_Congruence\_System\_const\_iterator\_increment (ppl\_Congruence\_System\_const\_iterator\_t cit)

Increment cit so that it "points" to the next congruence.

• int ppl\_Congruence\_System\_const\_iterator\_equal\_test (ppl\_const\_Congruence\_System\_const\_iterator\_t x, ppl\_const\_Congruence\_System\_const\_iterator\_t y)

Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.

# 7.2.1 Detailed Description

Types and functions for iterating on congruence systems.

The types and functions for congruence systems iterators provide read-only access to the elements of a congruence system by interfacing *Congruence\_System::const\_iterator*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.3 ppl\_Congruence\_System\_tag Interface Reference

Types and functions for congruence systems.

```
#include <ppl_c_header.h>
```

#### **Related Functions**

(Note that these are not member functions.)

# Constructors, Assignment and Destructor

- int ppl\_new\_Congruence\_System (ppl\_Congruence\_System\_t \*pcs)

  Builds an empty system of congruences and writes a handle to it at address pcs.
- int ppl\_new\_Congruence\_System\_zero\_dim\_empty (ppl\_Congruence\_System\_t \*pcs)

  Builds a zero-dimensional, unsatisfiable congruence system and writes a handle to it at address pcs.

• int ppl\_new\_Congruence\_System\_from\_Congruence (ppl\_Congruence\_System\_t \*pcs, ppl\_const\_Congruence\_t c)

Builds the singleton congruence system containing only a copy of congruence c; writes a handle for the newly created system at address pcs.

• int ppl\_new\_Congruence\_System\_from\_Congruence\_System (ppl\_Congruence\_System\_t \*pcs, ppl\_const\_Congruence\_System\_t cs)

Builds a congruence system that is a copy of cs; writes a handle for the newly created system at address pcs.

• int ppl\_assign\_Congruence\_System\_from\_Congruence\_System (ppl\_Congruence\_System\_t dst, ppl\_const\_Congruence\_System\_t src)

Assigns a copy of the congruence system src to dst.

• int ppl\_delete\_Congruence\_System (ppl\_const\_Congruence\_System\_t cs)

Invalidates the handle cs: this makes sure the corresponding resources will eventually be released.

#### Functions that Do Not Modify the Congruence System

• int ppl\_Congruence\_System\_space\_dimension (ppl\_const\_Congruence\_System\_t cs, ppl\_dimension\_type \*m)

Writes to m the dimension of the vector space enclosing cs.

- int ppl\_Congruence\_System\_empty (ppl\_const\_Congruence\_System\_t cs)

  Returns a positive integer if cs contains no (non-trivial) congruence; returns 0 otherwise.
- int ppl\_Congruence\_System\_begin (ppl\_const\_Congruence\_System\_t cs, ppl\_Congruence\_System\_const\_iterator\_t cit)

Assigns to cit a const iterator "pointing" to the beginning of the congruence system cs.

• int ppl\_Congruence\_System\_end (ppl\_const\_Congruence\_System\_t cs, ppl\_Congruence\_System\_const\_iterator\_t cit)

Assigns to cit a const iterator "pointing" past the end of the congruence system cs.

• int ppl\_Congruence\_System\_OK (ppl\_const\_Congruence\_System\_t cs)

Returns a positive integer if cs is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if cs is broken. Useful for debugging purposes.

# **Functions that May Modify the Congruence System**

- int ppl\_Congruence\_System\_clear (ppl\_Congruence\_System\_t cs)

  Removes all the congruences from the congruence system cs and sets its space dimension to 0.
- int ppl\_Congruence\_System\_insert\_Congruence (ppl\_Congruence\_System\_t cs, ppl\_const\_-Congruence\_t c)

Inserts a copy of the congruence c into cs; the space dimension is increased, if necessary.

# **Input/Output Functions**

• int ppl\_io\_print\_Congruence\_System (ppl\_const\_Congruence\_System\_t x)

Prints x to stdout.

- int ppl\_io\_fprint\_Congruence\_System (FILE \*stream, ppl\_const\_Congruence\_System\_t x)

  \*Prints x to the given output stream.
- int ppl\_io\_asprint\_Congruence\_System (char \*\*strp, ppl\_const\_Congruence\_System\_t x)

  Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_Congruence\_System\_ascii\_dump (ppl\_const\_Congruence\_System\_t x, FILE \*stream)

  Dumps an ascii representation of x on stream.
- int ppl\_Congruence\_System\_ascii\_load (ppl\_Congruence\_System\_t x, FILE \*stream)

  Loads an ascii representation of x from stream.

# 7.3.1 Detailed Description

Types and functions for congruence systems.

The types and functions for congruence systems provide an interface towards Congruence\_System.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.4 ppl\_Congruence\_tag Interface Reference

Types and functions for congruences.

```
#include <ppl_c_header.h>
```

#### **Related Functions**

(Note that these are not member functions.)

# Constructors, Assignment and Destructor

• int ppl\_new\_Congruence (ppl\_Congruence\_t \*pc, ppl\_const\_Linear\_Expression\_t le, ppl\_const\_-Coefficient\_t m)

Creates the new congruence  $le = 0 \pmod{m}$  and writes a handle for it at address pc. The space dimension of the new congruence is equal to the space dimension of le.

- int ppl\_new\_Congruence\_zero\_dim\_false (ppl\_Congruence\_t \*pc)

  Creates the unsatisfiable (zero-dimension space) congruence 0 = 1 (mod 0) and writes a handle for it at address pc.
- int ppl\_new\_Congruence\_zero\_dim\_integrality (ppl\_Congruence\_t \*pc)

  Creates the true (zero-dimension space) congruence 0 = 1 (mod 1), also known as integrality congruence. A handle for the newly created congruence is written at address pc.
- int ppl\_new\_Congruence\_from\_Congruence (ppl\_Congruence\_t \*pc, ppl\_const\_Congruence\_t c)

Builds a congruence that is a copy of c; writes a handle for the newly created congruence at address pc.

• int ppl\_assign\_Congruence\_from\_Congruence (ppl\_Congruence\_t dst, ppl\_const\_Congruence\_t src)

Assigns a copy of the congruence src to dst.

• int ppl\_delete\_Congruence (ppl\_const\_Congruence\_t c)

Invalidates the handle c: this makes sure the corresponding resources will eventually be released.

#### **Functions that Do Not Modify the Congruence**

- int ppl\_Congruence\_space\_dimension (ppl\_const\_Congruence\_t c, ppl\_dimension\_type \*m)

  Writes to m the space dimension of c.
- int ppl\_Congruence\_coefficient (ppl\_const\_Congruence\_t c, ppl\_dimension\_type var, ppl\_Coefficient\_t n)

Copies into n the coefficient of variable var in congruence c.

- int ppl\_Congruence\_inhomogeneous\_term (ppl\_const\_Congruence\_t c, ppl\_Coefficient\_t n)

  Copies into n the inhomogeneous term of congruence c.
- int ppl\_Congruence\_modulus (ppl\_const\_Congruence\_t c, ppl\_Coefficient\_t m)

  Copies into m the modulus of congruence c.
- int ppl\_Congruence\_OK (ppl\_const\_Congruence\_t c)

  Returns a positive integer if c is well formed, i.e., if it satisfies all its implementation invariants; returns

  0 and perhaps makes some noise if c is broken. Useful for debugging purposes.

# **Input/Output Functions**

- int ppl\_io\_print\_Congruence (ppl\_const\_Congruence\_t x)

  \*Prints x to stdout.
- int ppl\_io\_fprint\_Congruence (FILE \*stream, ppl\_const\_Congruence\_t x)

  Prints x to the given output stream.
- int ppl\_io\_asprint\_Congruence (char \*\*strp, ppl\_const\_Congruence\_t x)

  Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_Congruence\_ascii\_dump (ppl\_const\_Congruence\_t x, FILE \*stream)

  Dumps an ascii representation of x on stream.
- int ppl\_Congruence\_ascii\_load (ppl\_Congruence\_t x, FILE \*stream)

  Loads an ascii representation of x from stream.

# 7.4.1 Detailed Description

Types and functions for congruences.

The types and functions for congruences provide an interface towards *Congruence*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.5 ppl\_Constraint\_System\_const\_iterator\_tag Interface Reference

Types and functions for iterating on constraint systems.

```
#include <ppl_c_header.h>
```

#### **Related Functions**

(Note that these are not member functions.)

#### Constructors, Assignment and Destructor

- int ppl\_new\_Constraint\_System\_const\_iterator (ppl\_Constraint\_System\_const\_iterator\_t \*pcit)

  Builds a new 'const iterator' and writes a handle to it at address pcit.
- int ppl\_new\_Constraint\_System\_const\_iterator\_from\_Constraint\_System\_const\_iterator (ppl\_Constraint\_System\_const\_iterator\_t \*pcit, ppl\_const\_Constraint\_System\_const\_iterator\_t cit)

  Builds a const iterator that is a copy of cit; writes an handle for the newly created const iterator at address pcit.
- int ppl\_assign\_Constraint\_System\_const\_iterator\_from\_Constraint\_System\_const\_iterator (ppl\_Constraint\_System\_const\_iterator\_t dst, ppl\_const\_Constraint\_System\_const\_iterator\_t src)

  Assigns a copy of the const iterator src to dst.
- int ppl\_delete\_Constraint\_System\_const\_iterator (ppl\_const\_Constraint\_System\_const\_iterator\_t cit)

Invalidates the handle cit: this makes sure the corresponding resources will eventually be released.

# **Dereferencing, Incrementing and Equality Testing**

• int ppl\_Constraint\_System\_const\_iterator\_dereference (ppl\_const\_Constraint\_System\_const\_iterator\_t cit, ppl\_const\_Constraint\_t \*pc)

Dereference cit writing a const handle to the resulting constraint at address pc.

int ppl\_Constraint\_System\_const\_iterator\_increment (ppl\_Constraint\_System\_const\_iterator\_t cit)

Increment cit so that it "points" to the next constraint.

• int ppl\_Constraint\_System\_const\_iterator\_equal\_test (ppl\_const\_Constraint\_System\_const\_iterator t x, ppl\_const\_Constraint\_System\_const\_iterator t y)

Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.

# 7.5.1 Detailed Description

Types and functions for iterating on constraint systems.

The types and functions for constraint systems iterators provide read-only access to the elements of a constraint system by interfacing *Constraint\_System::const\_iterator*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

## 7.6 ppl\_Constraint\_System\_tag Interface Reference

Types and functions for constraint systems.

```
#include <ppl_c_header.h>
```

#### **Related Functions**

(Note that these are not member functions.)

#### Constructors, Assignment and Destructor

- int ppl\_new\_Constraint\_System (ppl\_Constraint\_System\_t \*pcs)

  Builds an empty system of constraints and writes a handle to it at address pcs.
- int ppl\_new\_Constraint\_System\_zero\_dim\_empty (ppl\_Constraint\_System\_t \*pcs)

  Builds a zero-dimensional, unsatisfiable constraint system and writes a handle to it at address pcs.
- int ppl\_new\_Constraint\_System\_from\_Constraint (ppl\_Constraint\_System\_t \*pcs, ppl\_const\_-Constraint\_t c)

Builds the singleton constraint system containing only a copy of constraint c; writes a handle for the newly created system at address pcs.

• int ppl\_new\_Constraint\_System\_from\_Constraint\_System (ppl\_Constraint\_System\_t \*pcs, ppl\_const\_Constraint\_System\_t cs)

Builds a constraint system that is a copy of cs; writes a handle for the newly created system at address pcs.

• int ppl\_assign\_Constraint\_System\_from\_Constraint\_System (ppl\_Constraint\_System\_t dst, ppl\_const\_Constraint\_System\_t src)

Assigns a copy of the constraint system src to dst.

• int ppl\_delete\_Constraint\_System (ppl\_const\_Constraint\_System\_t cs)

Invalidates the handle cs: this makes sure the corresponding resources will eventually be released.

## Functions that Do Not Modify the Constraint System

int ppl\_Constraint\_System\_space\_dimension (ppl\_const\_Constraint\_System\_t cs, ppl\_dimension\_type \*m)

Writes to m the dimension of the vector space enclosing cs.

- int ppl\_Constraint\_System\_empty (ppl\_const\_Constraint\_System\_t cs)

  Returns a positive integer if cs contains no (non-trivial) constraint; returns 0 otherwise.
- int ppl\_Constraint\_System\_has\_strict\_inequalities (ppl\_const\_Constraint\_System\_t cs)

  Returns a positive integer if cs contains any (non-trivial) strict inequality; returns 0 otherwise.
- int ppl\_Constraint\_System\_begin (ppl\_const\_Constraint\_System\_t cs, ppl\_Constraint\_System\_-const\_iterator\_t cit)

Assigns to cit a const iterator "pointing" to the beginning of the constraint system cs.

 int ppl\_Constraint\_System\_end (ppl\_const\_Constraint\_System\_t cs, ppl\_Constraint\_System\_const\_iterator\_t cit) Assigns to cit a const iterator "pointing" past the end of the constraint system cs.

• int ppl\_Constraint\_System\_OK (ppl\_const\_Constraint\_System\_t cs)

Returns a positive integer if cs is well formed, i.e., if it satisfies all its implementation invariants; returns
0 and perhaps makes some noise if cs is broken. Useful for debugging purposes.

### **Functions that May Modify the Constraint System**

- int ppl\_Constraint\_System\_clear (ppl\_Constraint\_System\_t cs)

  Removes all the constraints from the constraint system cs and sets its space dimension to 0.
- int ppl\_Constraint\_System\_insert\_Constraint (ppl\_Constraint\_System\_t cs, ppl\_const\_-Constraint\_t c)

*Inserts a copy of the constraint* c *into* cs; *the space dimension is increased, if necessary.* 

### **Input/Output Functions**

- int ppl\_io\_print\_Constraint\_System (ppl\_const\_Constraint\_System\_t x)

  \*\*Prints x to stdout.\*\*
- int ppl\_io\_fprint\_Constraint\_System (FILE \*stream, ppl\_const\_Constraint\_System\_t x)

  Prints x to the given output stream.
- int ppl\_io\_asprint\_Constraint\_System (char \*\*strp, ppl\_const\_Constraint\_System\_t x)

  Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_Constraint\_System\_ascii\_dump (ppl\_const\_Constraint\_System\_t x, FILE \*stream)

  Dumps an ascii representation of x on stream.
- int ppl\_Constraint\_System\_ascii\_load (ppl\_Constraint\_System\_t x, FILE \*stream)

  Loads an ascii representation of x from stream.

### 7.6.1 Detailed Description

Types and functions for constraint systems.

The types and functions for constraint systems provide an interface towards Constraint\_System.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

### 7.7 ppl\_Constraint\_tag Interface Reference

Types and functions for constraints.

```
#include <ppl_c_header.h>
```

#### **Related Functions**

(Note that these are not member functions.)

#### Constructors, Assignment and Destructor

• int ppl\_new\_Constraint (ppl\_Constraint\_t \*pc, ppl\_const\_Linear\_Expression\_t le, enum ppl\_enum\_Constraint\_Type rel)

Creates the new constraint 'le rel 0' and writes a handle for it at address pc. The space dimension of the new constraint is equal to the space dimension of le.

• int ppl\_new\_Constraint\_zero\_dim\_false (ppl\_Constraint\_t \*pc)

Creates the unsatisfiable (zero-dimension space) constraint 0=1 and writes a handle for it at address pc.

• int ppl\_new\_Constraint\_zero\_dim\_positivity (ppl\_Constraint\_t \*pc)

Creates the true (zero-dimension space) constraint  $0 \le 1$ , also known as positivity constraint. A handle for the newly created constraint is written at address pc.

- int ppl\_new\_Constraint\_from\_Constraint (ppl\_Constraint\_t \*pc, ppl\_const\_Constraint\_t c)

  Builds a constraint that is a copy of c; writes a handle for the newly created constraint at address pc.
- int ppl\_assign\_Constraint\_from\_Constraint (ppl\_Constraint\_t dst, ppl\_const\_Constraint\_t src)

  Assigns a copy of the constraint src to dst.
- int ppl\_delete\_Constraint (ppl\_const\_Constraint\_t c)

  Invalidates the handle c: this makes sure the corresponding resources will eventually be released.

#### **Functions that Do Not Modify the Constraint**

- int ppl\_Constraint\_space\_dimension (ppl\_const\_Constraint\_t c, ppl\_dimension\_type \*m)

  Writes to m the space dimension of c.
- int ppl\_Constraint\_type (ppl\_const\_Constraint\_t c)

  Returns the type of constraint c.
- int ppl\_Constraint\_coefficient (ppl\_const\_Constraint\_t c, ppl\_dimension\_type var, ppl\_Coefficient\_t n)

Copies into n the coefficient of variable var in constraint c.

- int ppl\_Constraint\_inhomogeneous\_term (ppl\_const\_Constraint\_t c, ppl\_Coefficient\_t n)

  Copies into n the inhomogeneous term of constraint c.
- int ppl\_Constraint\_OK (ppl\_const\_Constraint\_t c)

Returns a positive integer if c is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if c is broken. Useful for debugging purposes.

### **Input/Output Functions**

• int ppl\_io\_print\_Constraint (ppl\_const\_Constraint\_t x)

\*Prints x to stdout.

- int ppl\_io\_fprint\_Constraint (FILE \*stream, ppl\_const\_Constraint\_t x)

  Prints x to the given output stream.
- int ppl\_io\_asprint\_Constraint (char \*\*strp, ppl\_const\_Constraint\_t x)

  Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_Constraint\_ascii\_dump (ppl\_const\_Constraint\_t x, FILE \*stream)

  Dumps an ascii representation of x on stream.
- int ppl\_Constraint\_ascii\_load (ppl\_Constraint\_t x, FILE \*stream)

  Loads an ascii representation of x from stream.

#### 7.7.1 Detailed Description

Types and functions for constraints.

The types and functions for constraints provide an interface towards Constraint.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.8 ppl\_Generator\_System\_const\_iterator\_tag Interface Reference

Types and functions for iterating on generator systems.

```
#include <ppl_c_header.h>
```

#### **Related Functions**

(Note that these are not member functions.)

## Constructors, Assignment and Destructor

- int ppl\_new\_Generator\_System\_const\_iterator (ppl\_Generator\_System\_const\_iterator\_t \*pgit)

  Builds a new 'const iterator' and writes a handle to it at address pgit.
- int ppl\_new\_Generator\_System\_const\_iterator\_from\_Generator\_System\_const\_iterator (ppl\_Generator\_System\_const\_iterator\_t \*pgit, ppl\_const\_Generator\_System\_const\_iterator\_t git)

  Builds a const iterator that is a copy of git; writes an handle for the newly created const iterator at address pgit.
- int ppl\_assign\_Generator\_System\_const\_iterator\_from\_Generator\_System\_const\_iterator (ppl\_Generator\_System\_const\_iterator\_t dst, ppl\_const\_Generator\_System\_const\_iterator\_t src)

  Assigns a copy of the const iterator src to dst.
- int ppl\_delete\_Generator\_System\_const\_iterator (ppl\_const\_Generator\_System\_const\_iterator\_t git)

Invalidates the handle git: this makes sure the corresponding resources will eventually be released.

### **Dereferencing, Incrementing and Equality Testing**

• int ppl\_Generator\_System\_const\_iterator\_dereference (ppl\_const\_Generator\_System\_const\_iterator\_t git, ppl\_const\_Generator\_t \*pg)

Dereference git writing a const handle to the resulting generator at address pg.

• int ppl\_Generator\_System\_const\_iterator\_increment (ppl\_Generator\_System\_const\_iterator\_t git)

*Increment* git so that it "points" to the next generator.

• int ppl\_Generator\_System\_const\_iterator\_equal\_test (ppl\_const\_Generator\_System\_const\_iterator\_t x, ppl\_const\_Generator\_System\_const\_iterator\_t y)

Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.

#### 7.8.1 Detailed Description

Types and functions for iterating on generator systems.

The types and functions for generator systems iterators provide read-only access to the elements of a generator system by interfacing *Generator\_System::const\_iterator*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

## 7.9 ppl Generator System tag Interface Reference

Types and functions for generator systems.

```
#include <ppl_c_header.h>
```

#### **Related Functions**

(Note that these are not member functions.)

# Constructors, Assignment and Destructor

- int ppl\_new\_Generator\_System (ppl\_Generator\_System\_t \*pgs)

  Builds an empty system of generators and writes a handle to it at address pgs.
- int ppl\_new\_Generator\_System\_from\_Generator (ppl\_Generator\_System\_t \*pgs, ppl\_const\_-Generator\_t g)

Builds the singleton generator system containing only a copy of generator g; writes a handle for the newly created system at address pgs.

• int ppl\_new\_Generator\_System\_from\_Generator\_System (ppl\_Generator\_System\_t \*pgs, ppl\_const\_Generator\_System\_t gs)

Builds a generator system that is a copy of gs; writes a handle for the newly created system at address pgs.

• int ppl\_assign\_Generator\_System\_from\_Generator\_System (ppl\_Generator\_System\_t dst, ppl\_const\_Generator\_System\_t src)

Assigns a copy of the generator system src to dst.

• int ppl\_delete\_Generator\_System (ppl\_const\_Generator\_System\_t gs)

Invalidates the handle gs: this makes sure the corresponding resources will eventually be released.

#### Functions that Do Not Modify the Generator System

• int ppl\_Generator\_System\_space\_dimension (ppl\_const\_Generator\_System\_t gs, ppl\_dimension\_type \*m)

Writes to m the dimension of the vector space enclosing qs.

- int ppl\_Generator\_System\_empty (ppl\_const\_Generator\_System\_t gs)

  Returns a positive integer if qs contains no generators; returns 0 otherwise.
- int ppl\_Generator\_System\_begin (ppl\_const\_Generator\_System\_t gs, ppl\_Generator\_System\_-const\_iterator\_t git)

Assigns to git a const iterator "pointing" to the beginning of the generator system gs.

 int ppl\_Generator\_System\_end (ppl\_const\_Generator\_System\_t gs, ppl\_Generator\_System\_const\_iterator\_t git)

Assigns to git a const iterator "pointing" past the end of the generator system gs.

• int ppl\_Generator\_System\_OK (ppl\_const\_Generator\_System\_t gs)

Returns a positive integer if gs is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if gs is broken. Useful for debugging purposes.

#### **Functions that May Modify the Generator System**

- int ppl\_Generator\_System\_clear (ppl\_Generator\_System\_t gs)

  Removes all the generators from the generator system gs and sets its space dimension to 0.
- int ppl\_Generator\_System\_insert\_Generator (ppl\_Generator\_System\_t gs, ppl\_const\_-Generator t g)

Inserts a copy of the generator g into gs; the space dimension is increased, if necessary.

#### **Input/Output Functions**

- int ppl\_io\_print\_Generator\_System (ppl\_const\_Generator\_System\_t x)

  \*Prints x to stdout.
- int ppl\_io\_fprint\_Generator\_System (FILE \*stream, ppl\_const\_Generator\_System\_t x)

  Prints x to the given output stream.
- int ppl\_io\_asprint\_Generator\_System (char \*\*strp, ppl\_const\_Generator\_System\_t x)

  Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_Generator\_System\_ascii\_dump (ppl\_const\_Generator\_System\_t x, FILE \*stream)

  Dumps an ascii representation of x on stream.
- int ppl\_Generator\_System\_ascii\_load (ppl\_Generator\_System\_t x, FILE \*stream)

  Loads an ascii representation of x from stream.

## 7.9.1 Detailed Description

Types and functions for generator systems.

The types and functions for generator systems provide an interface towards Generator\_System.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.10 ppl\_Generator\_tag Interface Reference

Types and functions for generators.

```
#include <ppl_c_header.h>
```

#### **Related Functions**

(Note that these are not member functions.)

#### Constructors, Assignment and Destructor

• int ppl\_new\_Generator (ppl\_Generator\_t \*pg, ppl\_const\_Linear\_Expression\_t le, enum ppl\_enum\_Generator\_Type t, ppl\_const\_Coefficient\_t d)

Creates a new generator of direction le and type t. If the generator to be created is a point or a closure point, the divisor d is applied to le. For other types of generators d is simply disregarded. A handle for the new generator is written at address pg. The space dimension of the new generator is equal to the space dimension of le.

- int ppl\_new\_Generator\_zero\_dim\_point (ppl\_Generator\_t \*pg)

  Creates the point that is the origin of the zero-dimensional space  $\mathbb{R}^0$ . Writes a handle for the new generator at address pg.
- int ppl\_new\_Generator\_zero\_dim\_closure\_point (ppl\_Generator\_t \*pg)

  Creates, as a closure point, the point that is the origin of the zero-dimensional space  $\mathbb{R}^0$ . Writes a handle for the new generator at address pg.
- int ppl\_new\_Generator\_from\_Generator (ppl\_Generator\_t \*pg, ppl\_const\_Generator\_t g)

  Builds a generator that is a copy of g; writes a handle for the newly created generator at address pg.
- int ppl\_assign\_Generator\_from\_Generator (ppl\_Generator\_t dst, ppl\_const\_Generator\_t src)

  Assigns a copy of the generator src to dst.
- int ppl\_delete\_Generator (ppl\_const\_Generator\_t g)

  Invalidates the handle g: this makes sure the corresponding resources will eventually be released.

#### **Functions that Do Not Modify the Generator**

- int ppl\_Generator\_space\_dimension (ppl\_const\_Generator\_t g, ppl\_dimension\_type \*m)

  Writes to m the space dimension of g.
- int ppl\_Generator\_type (ppl\_const\_Generator\_t g)

  Returns the type of generator g.

• int ppl\_Generator\_coefficient (ppl\_const\_Generator\_t g, ppl\_dimension\_type var, ppl\_-Coefficient\_t n)

Copies into n the coefficient of variable var in generator g.

- int ppl\_Generator\_divisor (ppl\_const\_Generator\_t g, ppl\_Coefficient\_t n)

  If g is a point or a closure point assigns its divisor to n.
- int ppl\_Generator\_OK (ppl\_const\_Generator\_t g)

Returns a positive integer if g is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if g is broken. Useful for debugging purposes.

## **Input/Output Functions**

- int ppl\_io\_print\_Generator (ppl\_const\_Generator\_t x)

  \*Prints x to stdout.
- int ppl\_io\_fprint\_Generator (FILE \*stream, ppl\_const\_Generator\_t x)

  Prints x to the given output stream.
- int ppl\_io\_asprint\_Generator (char \*\*strp, ppl\_const\_Generator\_t x)

  Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_Generator\_ascii\_dump (ppl\_const\_Generator\_t x, FILE \*stream)

  Dumps an ascii representation of x on stream.
- int ppl\_Generator\_ascii\_load (ppl\_Generator\_t x, FILE \*stream)

  Loads an ascii representation of x from stream.

### 7.10.1 Detailed Description

Types and functions for generators.

The types and functions for generators provide an interface towards *Generator*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

### 7.11 ppl Grid Generator System const iterator tag Interface Reference

Types and functions for iterating on grid generator systems.

```
#include <ppl c header.h>
```

### **Related Functions**

(Note that these are not member functions.)

## Constructors, Assignment and Destructor

• int ppl\_new\_Grid\_Generator\_System\_const\_iterator (ppl\_Grid\_Generator\_System\_const\_iterator\_t \*pgit)

Builds a new 'const iterator' and writes a handle to it at address pgit.

• int ppl\_new\_Grid\_Generator\_System\_const\_iterator\_from\_Grid\_Generator\_System\_const\_iterator (ppl\_Grid\_Generator\_System\_const\_iterator\_t \*pgit, ppl\_const\_Grid\_Generator\_System\_const\_iterator\_t git)

Builds a const iterator that is a copy of git; writes an handle for the newly created const iterator at address pgit.

• int ppl\_assign\_Grid\_Generator\_System\_const\_iterator\_from\_Grid\_Generator\_System\_const\_iterator (ppl\_Grid\_Generator\_System\_const\_iterator\_t dst, ppl\_const\_Grid\_Generator\_System\_const\_iterator\_t src)

Assigns a copy of the const iterator src to dst.

• int ppl\_delete\_Grid\_Generator\_System\_const\_iterator (ppl\_const\_Grid\_Generator\_System\_const\_iterator\_t git)

Invalidates the handle git: this makes sure the corresponding resources will eventually be released.

#### **Dereferencing, Incrementing and Equality Testing**

• int ppl\_Grid\_Generator\_System\_const\_iterator\_dereference (ppl\_const\_Grid\_Generator\_-System\_const\_iterator\_t git, ppl\_const\_Grid\_Generator\_t \*pg)

Dereference git writing a const handle to the resulting grid generator at address pg.

• int ppl\_Grid\_Generator\_System\_const\_iterator\_increment (ppl\_Grid\_Generator\_System\_const\_iterator\_t git)

*Increment* git so that it "points" to the next grid generator.

• int ppl\_Grid\_Generator\_System\_const\_iterator\_equal\_test (ppl\_const\_Grid\_Generator\_-System\_const\_iterator\_t x, ppl\_const\_Grid\_Generator\_System\_const\_iterator\_t y)

Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.

#### 7.11.1 Detailed Description

Types and functions for iterating on grid generator systems.

The types and functions for grid generator systems iterators provide read-only access to the elements of a grid generator system by interfacing *Grid\_Generator\_System::const\_iterator*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

### 7.12 ppl\_Grid\_Generator\_System\_tag Interface Reference

Types and functions for grid generator systems.

```
#include <ppl_c_header.h>
```

#### **Related Functions**

(Note that these are not member functions.)

#### Constructors, Assignment and Destructor

- int ppl\_new\_Grid\_Generator\_System (ppl\_Grid\_Generator\_System\_t \*pgs)

  Builds an empty system of grid generators and writes a handle to it at address pgs.
- int ppl\_new\_Grid\_Generator\_System\_from\_Grid\_Generator (ppl\_Grid\_Generator\_System\_t \*pgs, ppl\_const\_Grid\_Generator\_t g)

Builds the singleton grid generator system containing only a copy of generator g; writes a handle for the newly created system at address pgs.

• int ppl\_new\_Grid\_Generator\_System\_from\_Grid\_Generator\_System (ppl\_Grid\_Generator\_System\_t \*pgs, ppl\_const\_Grid\_Generator\_System\_t gs)

Builds a grid generator system that is a copy of gs; writes a handle for the newly created system at address pgs.

• int ppl\_assign\_Grid\_Generator\_System\_from\_Grid\_Generator\_System (ppl\_Grid\_Generator\_System\_t dst, ppl\_const\_Grid\_Generator\_System\_t src)

Assigns a copy of the grid generator system src to dst.

• int ppl\_delete\_Grid\_Generator\_System (ppl\_const\_Grid\_Generator\_System\_t gs)

Invalidates the handle gs: this makes sure the corresponding resources will eventually be released.

# Functions that Do Not Modify the Grid Generator System

• int ppl\_Grid\_Generator\_System\_space\_dimension (ppl\_const\_Grid\_Generator\_System\_t gs, ppl\_dimension\_type \*m)

Writes to m the dimension of the vector space enclosing gs.

- int ppl\_Grid\_Generator\_System\_empty (ppl\_const\_Grid\_Generator\_System\_t gs)

  Returns a positive integer if gs contains no generator; returns 0 otherwise.
- int ppl\_Grid\_Generator\_System\_begin (ppl\_const\_Grid\_Generator\_System\_t gs, ppl\_Grid\_-Generator\_System\_const\_iterator\_t git)

Assigns to git a const iterator "pointing" to the beginning of the grid generator system gs.

• int ppl\_Grid\_Generator\_System\_end (ppl\_const\_Grid\_Generator\_System\_t gs, ppl\_Grid\_-Generator\_System\_const\_iterator\_t git)

Assigns to git a const iterator "pointing" past the end of the grid generator system gs.

• int ppl\_Grid\_Generator\_System\_OK (ppl\_const\_Grid\_Generator\_System\_t gs)

Returns a positive integer if gs is well formed, i.e., if it satisfies all its implementation invariants; returns
0 and perhaps makes some noise if gs is broken. Useful for debugging purposes.

### **Functions that May Modify the Grid Generator System**

• int ppl\_Grid\_Generator\_System\_clear (ppl\_Grid\_Generator\_System\_t gs)

Removes all the generators from the grid generator system gs and sets its space dimension to 0.

• int ppl\_Grid\_Generator\_System\_insert\_Grid\_Generator (ppl\_Grid\_Generator\_System\_t gs, ppl\_const\_Grid\_Generator\_t g)

Inserts a copy of the grid generator g into gs; the space dimension is increased, if necessary.

#### **Input/Output Functions**

- int ppl\_io\_print\_Grid\_Generator\_System (ppl\_const\_Grid\_Generator\_System\_t x)

  \*Prints x to stdout.
- int ppl\_io\_fprint\_Grid\_Generator\_System (FILE \*stream, ppl\_const\_Grid\_Generator\_System\_t x)

*Prints* x *to the given output* stream.

• int ppl\_io\_asprint\_Grid\_Generator\_System (char \*\*strp, ppl\_const\_Grid\_Generator\_System\_t x)

*Prints* x *to a malloc-allocated string, a pointer to which is returned via* strp.

• int ppl\_Grid\_Generator\_System\_ascii\_dump (ppl\_const\_Grid\_Generator\_System\_t x, FILE \*stream)

Dumps an ascii representation of x on stream.

• int ppl\_Grid\_Generator\_System\_ascii\_load (ppl\_Grid\_Generator\_System\_t x, FILE \*stream)

Loads an ascii representation of x from stream.

### 7.12.1 Detailed Description

Types and functions for grid generator systems.

The types and functions for grid generator systems provide an interface towards *Grid\_Generator\_System*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.13 ppl\_Grid\_Generator\_tag Interface Reference

Types and functions for grid generators.

```
#include <ppl_c_header.h>
```

### Related Functions

(Note that these are not member functions.)

#### Constructors, Assignment and Destructor

• int ppl\_new\_Grid\_Generator (ppl\_Grid\_Generator\_t \*pg, ppl\_const\_Linear\_Expression\_t le, enum ppl\_enum\_Grid\_Generator\_Type t, ppl\_const\_Coefficient\_t d)

Creates a new grid generator of direction le and type t. If the grid generator to be created is a point or a parameter, the divisor d is applied to le. If it is a line, d is simply disregarded. A handle for the new grid generator is written at address pg. The space dimension of the new grid generator is equal to the space dimension of le.

- int ppl\_new\_Grid\_Generator\_zero\_dim\_point (ppl\_Grid\_Generator\_t \*pg)

  Creates the point that is the origin of the zero-dimensional space  $\mathbb{R}^0$ . Writes a handle for the new grid generator at address pg.
- int ppl\_new\_Grid\_Generator\_from\_Grid\_Generator (ppl\_Grid\_Generator\_t \*pg, ppl\_const\_-Grid\_Generator\_t g)

Builds a grid generator that is a copy of g; writes a handle for the newly created grid generator at address pg.

• int ppl\_assign\_Grid\_Generator\_from\_Grid\_Generator (ppl\_Grid\_Generator\_t dst, ppl\_const\_-Grid\_Generator\_t src)

Assigns a copy of the grid generator src to dst.

• int ppl\_delete\_Grid\_Generator (ppl\_const\_Grid\_Generator\_t g)

Invalidates the handle g: this makes sure the corresponding resources will eventually be released.

#### **Functions that Do Not Modify the Grid Generator**

• int ppl\_Grid\_Generator\_space\_dimension (ppl\_const\_Grid\_Generator\_t g, ppl\_dimension\_type \*m)

Writes to m the space dimension of g.

- int ppl\_Grid\_Generator\_type (ppl\_const\_Grid\_Generator\_t g)

  \*Returns the type of grid generator g.
- int ppl\_Grid\_Generator\_coefficient (ppl\_const\_Grid\_Generator\_t g, ppl\_dimension\_type var, ppl\_Coefficient\_t n)

Copies into n the coefficient of variable var in grid generator q.

- int ppl\_Grid\_Generator\_divisor (ppl\_const\_Grid\_Generator\_t g, ppl\_Coefficient\_t n)

  If g is a point or a parameter assigns its divisor to n.
- int ppl\_Grid\_Generator\_OK (ppl\_const\_Grid\_Generator\_t g)

  Returns a positive integer if g is well formed, i.e., if it satisfies all its implementation invariants; returns

  0 and perhaps makes some noise if g is broken. Useful for debugging purposes.

# **Input/Output Functions**

- int ppl\_io\_print\_Grid\_Generator (ppl\_const\_Grid\_Generator\_t x)

  \*Prints x to stdout.
- int ppl\_io\_fprint\_Grid\_Generator (FILE \*stream, ppl\_const\_Grid\_Generator\_t x)

  Prints x to the given output stream.
- int ppl\_io\_asprint\_Grid\_Generator (char \*\*strp, ppl\_const\_Grid\_Generator\_t x)

  Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_Grid\_Generator\_ascii\_dump (ppl\_const\_Grid\_Generator\_t x, FILE \*stream)

  Dumps an ascii representation of x on stream.
- int ppl\_Grid\_Generator\_ascii\_load (ppl\_Grid\_Generator\_t x, FILE \*stream)

  Loads an ascii representation of x from stream.

## 7.13.1 Detailed Description

Types and functions for grid generators.

The types and functions for grid generators provide an interface towards *Grid\_Generator*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.14 ppl\_Linear\_Expression\_tag Interface Reference

Types and functions for linear expressions.

```
#include <ppl_c_header.h>
```

#### **Related Functions**

(Note that these are not member functions.)

### Constructors, Assignment and Destructor

• int ppl\_new\_Linear\_Expression (ppl\_Linear\_Expression\_t \*ple)

Creates a new linear expression corresponding to the constant 0 in a zero-dimensional space; writes a handle for the new linear expression at address ple.

• int ppl\_new\_Linear\_Expression\_with\_dimension (ppl\_Linear\_Expression\_t \*ple, ppl\_dimension\_type d)

Creates a new linear expression corresponding to the constant 0 in a d-dimensional space; writes a handle for the new linear expression at address ple.

• int ppl\_new\_Linear\_Expression\_from\_Linear\_Expression (ppl\_Linear\_Expression\_t \*ple, ppl\_const\_Linear\_Expression\_t le)

Builds a linear expression that is a copy of le; writes a handle for the newly created linear expression at address ple.

• int ppl\_new\_Linear\_Expression\_from\_Constraint (ppl\_Linear\_Expression\_t \*ple, ppl\_const\_-Constraint\_t c)

Builds a linear expression corresponding to constraint c; writes a handle for the newly created linear expression at address ple.

• int ppl\_new\_Linear\_Expression\_from\_Generator (ppl\_Linear\_Expression\_t \*ple, ppl\_const\_-Generator\_t g)

Builds a linear expression corresponding to generator g; writes a handle for the newly created linear expression at address ple.

• int ppl\_new\_Linear\_Expression\_from\_Congruence (ppl\_Linear\_Expression\_t \*ple, ppl\_const\_-Congruence\_t c)

Builds a linear expression corresponding to congruence c; writes a handle for the newly created linear expression at address ple.

• int ppl\_new\_Linear\_Expression\_from\_Grid\_Generator (ppl\_Linear\_Expression\_t \*ple, ppl\_const\_Grid\_Generator\_t g)

Builds a linear expression corresponding to grid generator g; writes a handle for the newly created linear expression at address ple.

• int ppl\_assign\_Linear\_Expression\_from\_Linear\_Expression (ppl\_Linear\_Expression\_t dst, ppl\_const\_Linear\_Expression\_t src)

Assigns a copy of the linear expression src to dst.

• int ppl\_delete\_Linear\_Expression (ppl\_const\_Linear\_Expression\_t le)

Invalidates the handle le: this makes sure the corresponding resources will eventually be released.

#### **Functions that Do Not Modify the Linear Expression**

• int ppl\_Linear\_Expression\_space\_dimension (ppl\_const\_Linear\_Expression\_t le, ppl\_dimension\_type \*m)

Writes to m the space dimension of le.

• int ppl\_Linear\_Expression\_coefficient (ppl\_const\_Linear\_Expression\_t le, ppl\_dimension\_type var, ppl\_Coefficient\_t n)

Copies into n the coefficient of variable var in the linear expression le.

• int ppl\_Linear\_Expression\_inhomogeneous\_term (ppl\_const\_Linear\_Expression\_t le, ppl\_-Coefficient t n)

Copies into n the inhomogeneous term of linear expression le.

• int ppl\_Linear\_Expression\_OK (ppl\_const\_Linear\_Expression\_t le)

Returns a positive integer if l = is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if l = is broken. Useful for debugging purposes.

#### **Functions that May Modify the Linear Expression**

• int ppl\_Linear\_Expression\_add\_to\_coefficient (ppl\_Linear\_Expression\_t le, ppl\_dimension\_type var, ppl\_const\_Coefficient\_t n)

Adds n to the coefficient of variable var in the linear expression le. The space dimension is set to be the maximum between var + 1 and the old space dimension.

• int ppl\_Linear\_Expression\_add\_to\_inhomogeneous (ppl\_Linear\_Expression\_t le, ppl\_const\_-Coefficient\_t n)

Adds n to the inhomogeneous term of the linear expression le.

• int ppl\_add\_Linear\_Expression\_to\_Linear\_Expression (ppl\_Linear\_Expression\_t dst, ppl\_const\_Linear\_Expression\_t src)

Adds the linear expression src to dst.

• int ppl\_subtract\_Linear\_Expression\_from\_Linear\_Expression (ppl\_Linear\_Expression\_t dst, ppl\_const\_Linear\_Expression\_t src)

Subtracts the linear expression src from dst.

• int ppl\_multiply\_Linear\_Expression\_by\_Coefficient (ppl\_Linear\_Expression\_t le, ppl\_const\_-Coefficient\_t n)

Multiply the linear expression dst by n.

## **Input/Output Functions**

- int ppl\_io\_print\_Linear\_Expression (ppl\_const\_Linear\_Expression\_t x)

  Prints x to stdout.
- int ppl\_io\_fprint\_Linear\_Expression (FILE \*stream, ppl\_const\_Linear\_Expression\_t x)

  Prints x to the given output stream.
- int ppl\_io\_asprint\_Linear\_Expression (char \*\*strp, ppl\_const\_Linear\_Expression\_t x)

  Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_Linear\_Expression\_ascii\_dump (ppl\_const\_Linear\_Expression\_t x, FILE \*stream)

  Dumps an ascii representation of x on stream.
- int ppl\_Linear\_Expression\_ascii\_load (ppl\_Linear\_Expression\_t x, FILE \*stream)

  Loads an ascii representation of x from stream.

#### 7.14.1 Detailed Description

Types and functions for linear expressions.

The types and functions for linear expression provide an interface towards *Linear\_Expression*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.15 ppl\_MIP\_Problem\_tag Interface Reference

Types and functions for MIP problems.

```
#include <ppl_c_header.h>
```

### **Related Functions**

(Note that these are not member functions.)

#### **Symbolic Constants**

- int PPL\_OPTIMIZATION\_MODE\_MAXIMIZATION Code of the "maximization" optimization mode.
- int PPL\_OPTIMIZATION\_MODE\_MINIMIZATION Code of the "minimization" optimization mode.
- int PPL\_MIP\_PROBLEM\_STATUS\_UNFEASIBLE Code of the "unfeasible MIP problem" status.
- int PPL\_MIP\_PROBLEM\_STATUS\_UNBOUNDED Code of the "unbounded MIP problem" status.
- int PPL\_MIP\_PROBLEM\_STATUS\_OPTIMIZED

Code of the "optimized MIP problem" status.

- int PPL\_MIP\_PROBLEM\_CONTROL\_PARAMETER\_NAME\_PRICING Code for the MIP problem's "pricing" control parameter name.
- int PPL\_MIP\_PROBLEM\_CONTROL\_PARAMETER\_PRICING\_TEXTBOOK Code of MIP problem's "textbook" pricing method.
- int PPL MIP PROBLEM CONTROL PARAMETER PRICING STEEPEST EDGE EXACT

Code of MIP problem's "exact steepest-edge" pricing method.

• int PPL\_MIP\_PROBLEM\_CONTROL\_PARAMETER\_PRICING\_STEEPEST\_EDGE\_FLOAT Code of MIP problem's "float steepest-edge" pricing method.

#### Constructors, Assignment and Destructor

int ppl\_new\_MIP\_Problem\_from\_space\_dimension (ppl\_MIP\_Problem\_t \*pmip, ppl\_dimension\_type d)

Builds a trivial MIP problem of dimension d and writes an handle to it at address pmip.

• int ppl\_new\_MIP\_Problem (ppl\_MIP\_Problem\_t \*pmip, ppl\_dimension\_type d, ppl\_const\_-Constraint\_System\_t cs, ppl\_const\_Linear\_Expression\_t le, int m)

Builds an MIP problem of space dimension d having feasible region cs, objective function le and optimization mode m; writes a handle to it at address pmip.

• int ppl\_new\_MIP\_Problem\_from\_MIP\_Problem (ppl\_MIP\_Problem\_t \*pmip, ppl\_const\_MIP\_-Problem\_t mip)

Builds an MIP problem that is a copy of mip; writes a handle for the newly created system at address pmip.

• int ppl\_assign\_MIP\_Problem\_from\_MIP\_Problem (ppl\_MIP\_Problem\_t dst, ppl\_const\_MIP\_Problem\_t src)

Assigns a copy of the MIP problem src to dst.

• int ppl\_delete\_MIP\_Problem (ppl\_const\_MIP\_Problem\_t mip)

Invalidates the handle mip: this makes sure the corresponding resources will eventually be released.

### Functions that Do Not Modify the MIP\_Problem

• int ppl\_MIP\_Problem\_space\_dimension (ppl\_const\_MIP\_Problem\_t mip, ppl\_dimension\_type \*m)

Writes to m the dimension of the vector space enclosing mip.

• int ppl\_MIP\_Problem\_number\_of\_integer\_space\_dimensions (ppl\_const\_MIP\_Problem\_t mip, ppl\_dimension\_type \*m)

Writes to m the number of integer space dimensions of mip.

• int ppl\_MIP\_Problem\_integer\_space\_dimensions (ppl\_const\_MIP\_Problem\_t mip, ppl\_dimension\_type ds[])

Writes in the first positions of the array ds all the integer space dimensions of problem mip. If the array is not big enough to hold all of the integer space dimensions, the behavior is undefined.

int ppl\_MIP\_Problem\_number\_of\_constraints (ppl\_const\_MIP\_Problem\_t mip, ppl\_dimension\_type \*m)

Writes to m the number of constraints defining the feasible region of mip.

• int ppl\_MIP\_Problem\_constraint\_at\_index (ppl\_const\_MIP\_Problem\_t mip, ppl\_dimension\_type i, ppl\_const\_Constraint\_t \*pc)

Writes at address pc a const handle to the i-th constraint defining the feasible region of the MIP problem mip.

• int ppl\_MIP\_Problem\_objective\_function (ppl\_const\_MIP\_Problem\_t mip, ppl\_const\_Linear\_-Expression\_t \*ple)

Writes a const handle to the linear expression defining the objective function of the MIP problem mip at address ple.

- int ppl\_MIP\_Problem\_optimization\_mode (ppl\_const\_MIP\_Problem\_t mip)

  Returns the optimization mode of the MIP problem mip.
- int ppl\_MIP\_Problem\_OK (ppl\_const\_MIP\_Problem\_t mip)

Returns a positive integer if mip is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if mip is broken. Useful for debugging purposes.

#### Functions that May Modify the MIP\_Problem

- int ppl\_MIP\_Problem\_clear (ppl\_MIP\_Problem\_t mip)

  Resets the MIP problem to be a trivial problem of space dimension 0.
- int ppl\_MIP\_Problem\_add\_space\_dimensions\_and\_embed (ppl\_MIP\_Problem\_t mip, ppl\_dimension\_type d)

Adds d new dimensions to the space enclosing the MIP problem mip and to mip itself.

• int ppl\_MIP\_Problem\_add\_to\_integer\_space\_dimensions (ppl\_MIP\_Problem\_t mip, ppl\_dimension\_type ds[], size\_t n)

Sets the space dimensions that are specified in first n positions of the array ds to be integer dimensions of problem mip. The presence of duplicates in ds is a waste but an innocuous one.

- int ppl\_MIP\_Problem\_add\_constraint (ppl\_MIP\_Problem\_t mip, ppl\_const\_Constraint\_t c)

  Modifies the feasible region of the MIP problem mip by adding a copy of the constraint c.
- int ppl\_MIP\_Problem\_add\_constraints (ppl\_MIP\_Problem\_t mip, ppl\_const\_Constraint\_-System t cs)

Modifies the feasible region of the MIP problem mip by adding a copy of the constraints in cs.

• int ppl\_MIP\_Problem\_set\_objective\_function (ppl\_MIP\_Problem\_t mip, ppl\_const\_Linear\_-Expression\_t le)

Sets the objective function of the MIP problem mip to a copy of le.

• int ppl\_MIP\_Problem\_set\_optimization\_mode (ppl\_MIP\_Problem\_t mip, int mode)

Sets the optimization mode of the MIP problem mip to mode.

# Computing the Solution of the MIP\_Problem

- int ppl\_MIP\_Problem\_is\_satisfiable (ppl\_const\_MIP\_Problem\_t mip)

  Returns a positive integer if mip is satisfiable; returns 0 otherwise.
- int ppl\_MIP\_Problem\_solve (ppl\_const\_MIP\_Problem\_t mip)

  Solves the MIP problem mip, returning an exit status.
- int ppl\_MIP\_Problem\_evaluate\_objective\_function (ppl\_const\_MIP\_Problem\_t mip, ppl\_const\_-Generator\_t g, ppl\_Coefficient\_t num, ppl\_Coefficient\_t den)

  Evaluates the objective function of mip on point g.
- int ppl\_MIP\_Problem\_feasible\_point (ppl\_const\_MIP\_Problem\_t mip, ppl\_const\_Generator\_t \*pg)

Writes a const handle to a feasible point for the MIP problem mip at address pg.

 int ppl\_MIP\_Problem\_optimizing\_point (ppl\_const\_MIP\_Problem\_t mip, ppl\_const\_-Generator\_t \*pg)

Writes a const handle to an optimizing point for the MIP problem mip at address pg.

• int ppl\_MIP\_Problem\_optimal\_value (ppl\_const\_MIP\_Problem\_t mip, ppl\_Coefficient\_t num, ppl\_Coefficient\_t den)

Returns the optimal value for mip.

#### **Querying/Setting Control Parameters**

- int ppl\_MIP\_Problem\_get\_control\_parameter (ppl\_const\_MIP\_Problem\_t mip, int name)

  Returns the value of control parameter name in problem mip.
- int ppl\_MIP\_Problem\_set\_control\_parameter (ppl\_MIP\_Problem\_t mip, int value) Sets control parameter value in problem mip.

#### **Input/Output Functions**

- int ppl\_io\_print\_MIP\_Problem (ppl\_const\_MIP\_Problem\_t x)

  \*Prints x to stdout.
- int ppl\_io\_fprint\_MIP\_Problem (FILE \*stream, ppl\_const\_MIP\_Problem\_t x)

  Prints x to the given output stream.
- int ppl\_io\_asprint\_MIP\_Problem (char \*\*strp, ppl\_const\_MIP\_Problem\_t x)

  Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_MIP\_Problem\_ascii\_dump (ppl\_const\_MIP\_Problem\_t x, FILE \*stream)

  Dumps an ascii representation of x on stream.
- int ppl\_MIP\_Problem\_ascii\_load (ppl\_MIP\_Problem\_t x, FILE \*stream)

  Loads an ascii representation of x from stream.

#### 7.15.1 Detailed Description

Types and functions for MIP problems.

The types and functions for MIP problems provide an interface towards MIP\_Problem.

#### 7.15.2 Friends And Related Function Documentation

### 7.15.2.1 int ppl\_MIP\_Problem\_solve (ppl\_const\_MIP\_Problem\_t mip) [related]

Solves the MIP problem mip, returning an exit status.

#### **Returns:**

PPL\_MIP\_PROBLEM\_STATUS\_UNFEASIBLE if the MIP problem is not satisfiable; PPL\_MIP\_PROBLEM\_STATUS\_UNBOUNDED if the MIP problem is satisfiable but there is no finite bound to the value of the objective function; PPL\_MIP\_PROBLEM\_STATUS\_OPTIMIZED if the MIP problem admits an optimal solution.

# 7.15.2.2 int ppl\_MIP\_Problem\_evaluate\_objective\_function (ppl\_const\_MIP\_Problem\_t mip, ppl\_const\_Generator\_t g, ppl\_Coefficient\_t num, ppl\_Coefficient\_t den) [related]

Evaluates the objective function of mip on point g.

#### **Parameters:**

```
mip The MIP problem defining the objective function;
```

g The generator on which the objective function will be evaluated;

**num** Will be assigned the numerator of the objective function value;

**den** Will be assigned the denominator of the objective function value;

# 7.15.2.3 int ppl\_MIP\_Problem\_optimal\_value (ppl\_const\_MIP\_Problem\_t mip, ppl\_Coefficient\_t num, ppl\_Coefficient\_t den) [related]

Returns the optimal value for mip.

#### **Parameters:**

mip The MIP problem;

num Will be assigned the numerator of the optimal value;

den Will be assigned the denominator of the optimal value.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 

Types and functions for iterating on the disjuncts of a const ppl\_Pointset\_Powerset\_C\_Polyhedron\_tag.

#### **Related Functions**

(Note that these are not member functions.)

### **Construction, Initialization and Destruction**

• int \_\_ppl\_new\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator \_\_(ppl\_Pointset\_Powerset\_C\_-Polyhedron\_const\_iterator\_t \*pit)

Builds a new 'const iterator' and writes a handle to it at address pit.

• int ppl\_new\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_from\_const\_iterator (ppl\_-Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_t \*pit, ppl\_const\_Pointset\_Powerset\_C\_-Polyhedron\_const\_iterator\_t y)

Builds a copy of y and writes a handle to it at address pit.

- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_begin (ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_t ps, ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_t psit)

  Assigns to psit a const iterator "pointing" to the beginning of the sequence of disjuncts of ps.
- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_end (ppl\_const\_Pointset\_Powerset\_-C\_Polyhedron\_t ps, ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_t psit)

  Assigns to psit a const iterator "pointing" past the end of the sequence of disjuncts of ps.
- int ppl\_delete\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator (ppl\_const\_Pointset\_Powerset\_-C\_Polyhedron\_const\_iterator\_t it)

Invalidates the handle it: this makes sure the corresponding resources will eventually be released.

### **Dereferencing, Increment, Decrement and Equality Testing**

- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_dereference (ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_t it, ppl\_const\_Polyhedron\_t \*d)

  \*\*Dereferences it writing a const handle to the resulting disjunct at address d.\*\*
- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_increment (ppl\_Pointset\_Powerset\_C\_-Polyhedron\_const\_iterator\_t it)

*Increments* it so that it "points" to the next disjunct.

• int ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_decrement (ppl\_Pointset\_Powerset\_-C\_Polyhedron\_const\_iterator\_t it)

Decrements it so that it "points" to the previous disjunct.

int ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_equal\_test (ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_t x, ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_t y)

Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.

### 7.16.1 Detailed Description

Types and functions for iterating on the disjuncts of a const ppl\_Pointset\_Powerset\_C\_Polyhedron\_tag.

# 7.16.2 Friends And Related Function Documentation

7.16.2.1 int ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_dereference (ppl\_const\_-Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_t it, ppl\_const\_Polyhedron\_t \* d) [related]

Dereferences it writing a const handle to the resulting disjunct at address d.

#### Warning:

On exit, the disjunct d is still owned by the powerset object: any function call on the owning powerset object may invalidate it. Moreover, d should **not** be deleted directly: its resources will be released when deleting the owning powerset.

The documentation for this interface was generated from the following file:

· C interface.dox

# 7.17 ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_tag Interface Reference

Types and functions for iterating on the disjuncts of a ppl\_Pointset\_Powerset\_C\_Polyhedron\_tag.

#### **Related Functions**

(Note that these are not member functions.)

#### **Construction, Initialization and Destruction**

- - Builds a new 'iterator' and writes a handle to it at address pit.
- int ppl\_new\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_from\_iterator (ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_t \*pit, ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_t y)

  Builds a copy of y and writes a handle to it at address pit.
- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_begin (ppl\_Pointset\_Powerset\_C\_-Polyhedron\_t ps, ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_t psit)

  Assigns to psit an iterator "pointing" to the beginning of the sequence of disjuncts of ps.
- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_end (ppl\_Pointset\_Powerset\_C\_Polyhedron\_t ps, ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_t psit)

  Assigns to psit an iterator "pointing" past the end of the sequence of disjuncts of ps.
- int ppl\_delete\_Pointset\_Powerset\_C\_Polyhedron\_iterator (ppl\_const\_Pointset\_Powerset\_C\_-Polyhedron\_iterator\_t it)

Invalidates the handle it: this makes sure the corresponding resources will eventually be released.

#### **Dereferencing, Increment, Decrement and Equality Testing**

- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_dereference (ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_t it, ppl\_const\_Polyhedron\_t \*d)
   Dereferences it writing a const handle to the resulting disjunct at address d.
- int \_\_ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_increment \_\_(ppl\_Pointset\_Powerset\_C\_-Polyhedron\_iterator\_t it)

*Increments* it so that it "points" to the next disjunct.

• int \_\_ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_decrement \_\_(ppl\_Pointset\_Powerset\_C\_-Polyhedron\_iterator\_t it) Decrements it so that it "points" to the previous disjunct.

• int ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_equal\_test (ppl\_const\_Pointset\_Powerset\_-C\_Polyhedron\_iterator\_t x, ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_t y)

Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.

#### 7.17.1 Detailed Description

Types and functions for iterating on the disjuncts of a ppl\_Pointset\_Powerset\_C\_Polyhedron\_tag.

#### 7.17.2 Friends And Related Function Documentation

7.17.2.1 int ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_dereference (ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_t it, ppl\_const\_Polyhedron\_t \*d) [related]

Dereferences it writing a const handle to the resulting disjunct at address d.

#### Note:

Even though it is an non-const iterator, dereferencing it results in a handle to a **const** disjunct. This is because mutable iterators are meant to allow for the modification of the sequence of disjuncts (e.g., by dropping elements), while preventing direct modifications of the disjuncts they point to.

#### Warning:

On exit, the disjunct d is still owned by the powerset object: any function call on the owning powerset object may invalidate it. Moreover, d should **not** be deleted directly: its resources will be released when deleting the owning powerset.

The documentation for this interface was generated from the following file:

• C\_interface.dox

## 7.18 ppl\_Pointset\_Powerset\_C\_Polyhedron\_tag Interface Reference

Types and functions for the Pointset\_Powerset of C\_Polyhedron objects.

#### **Related Functions**

(Note that these are not member functions.)

#### Ad Hoc Functions for Pointset Powerset domains

• int ppl\_Pointset\_Powerset\_C\_Polyhedron\_omega\_reduce (ppl\_const\_Pointset\_Powerset\_C\_-Polyhedron t ps)

Drops from the sequence of disjuncts in ps all the non-maximal elements so that ps is non-redundant.

int ppl\_Pointset\_Powerset\_C\_Polyhedron\_size (ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_t ps, size\_t \*sz)

Writes to sz the number of disjuncts in ps.

• int ppl\_Pointset\_Powerset\_C\_Polyhedron\_geometrically\_covers\_Pointset\_Powerset\_C\_-Polyhedron (ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_t x, ppl\_const\_Pointset\_Powerset\_-C\_Polyhedron\_t y)

Returns a positive integer if powerset x geometrically covers powerset y; returns 0 otherwise.

• int ppl\_Pointset\_Powerset\_C\_Polyhedron\_geometrically\_equals\_Pointset\_Powerset\_C\_-Polyhedron (ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_t x, ppl\_const\_Pointset\_Powerset\_-C\_Polyhedron\_t y)

Returns a positive integer if powerset x is geometrically equal to powerset y; returns 0 otherwise.

- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_add\_disjunct (ppl\_Pointset\_Powerset\_C\_-Polyhedron\_t ps, ppl\_const\_Polyhedron\_t d)

  \*\*Adds to ps a copy of disjunct d.\*\*
- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_drop\_disjunct (ppl\_Pointset\_Powerset\_C\_-Polyhedron\_t ps, ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_t cit, ppl\_Pointset\_-Powerset\_C\_Polyhedron\_iterator\_t it)

Drops from ps the disjunct pointed to by cit, assigning to it an iterator to the disjunct following cit.

• int ppl\_Pointset\_Powerset\_C\_Polyhedron\_drop\_disjuncts (ppl\_Pointset\_Powerset\_C\_-Polyhedron\_t ps, ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_t first, ppl\_const\_-Pointset\_Powerset\_C\_Polyhedron\_iterator\_t last)

Drops from ps all the disjuncts from first to last (excluded).

• int \_\_ppl\_Pointset\_Powerset\_C\_Polyhedron\_pairwise\_reduce \_\_(ppl\_Pointset\_Powerset\_C\_-Polyhedron\_t ps)

Modifies ps by (recursively) merging together the pairs of disjuncts whose upper-bound is the same as their set-theoretical union.

### 7.18.1 Detailed Description

Types and functions for the Pointset\_Powerset of C\_Polyhedron objects.

The powerset domains can be instantiated by taking as a base domain any fixed semantic geometric description (C and NNC polyhedra, BD and octagonal shapes, boxes and grids). An element of the powerset domain represents a disjunctive collection of base objects (its disjuncts), all having the same space dimension

Besides the functions that are available in all semantic geometric descriptions (whose documentation is not repeated here), the powerset domain also provides several ad hoc functions. In particular, the iterator types allow for the examination and manipulation of the collection of disjuncts.

#### 7.18.2 Friends And Related Function Documentation

7.18.2.1 int ppl\_Pointset\_Powerset\_C\_Polyhedron\_size (ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_t ps, size\_t \* sz) [related]

Writes to sz the number of disjuncts in ps.

#### Note:

If present, Omega-redundant elements will be counted too.

The documentation for this interface was generated from the following file:

• C\_interface.dox

# 7.19 ppl\_Polyhedron\_tag Interface Reference

Types and functions for the domains of C and NNC convex polyhedra.

#### **Related Functions**

(Note that these are not member functions.)

#### Constructors and Assignment for C\_Polyhedron

• int ppl\_new\_C\_Polyhedron\_from\_space\_dimension (ppl\_Polyhedron\_t \*pph, ppl\_dimension\_type d, int empty)

Builds a C polyhedron of dimension d and writes an handle to it at address pph. If empty is different from zero, the newly created polyhedron will be empty; otherwise, it will be a universe polyhedron.

• int ppl\_new\_C\_Polyhedron\_from\_C\_Polyhedron (ppl\_Polyhedron\_t \*pph, ppl\_const\_-Polyhedron\_t ph)

Builds a C polyhedron that is a copy of ph; writes a handle for the newly created polyhedron at address pph.

- int ppl\_new\_C\_Polyhedron\_from\_C\_Polyhedron\_with\_complexity (ppl\_Polyhedron\_t \*pph, ppl\_const\_Polyhedron\_t ph, int complexity)
  - Builds a C polyhedron that is a copy of ph; writes a handle for the newly created polyhedron at address pph.
- int ppl\_new\_C\_Polyhedron\_from\_Constraint\_System (ppl\_Polyhedron\_t \*pph, ppl\_const\_-Constraint\_System\_t cs)

Builds a new C polyhedron from the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_C\_Polyhedron\_recycle\_Constraint\_System (ppl\_Polyhedron\_t \*pph, ppl\_-Constraint\_System\_t cs)

Builds a new C polyhedron recycling the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_C\_Polyhedron\_from\_Congruence\_System (ppl\_Polyhedron\_t \*pph, ppl\_const\_-Congruence\_System\_t cs)

Builds a new C polyhedron from the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_C\_Polyhedron\_recycle\_Congruence\_System (ppl\_Polyhedron\_t \*pph, ppl\_-Congruence\_System\_t cs)

Builds a new C polyhedron recycling the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_assign\_C\_Polyhedron\_from\_C\_Polyhedron (ppl\_Polyhedron\_t dst, ppl\_const\_-Polyhedron\_t src)

Assigns a copy of the C polyhedron src to the C polyhedron dst.

#### Constructors and Assignment for NNC\_Polyhedron

• int ppl\_new\_NNC\_Polyhedron\_from\_space\_dimension (ppl\_Polyhedron\_t \*pph, ppl\_dimension\_type d, int empty)

Builds an NNC polyhedron of dimension d and writes an handle to it at address pph. If empty is different from zero, the newly created polyhedron will be empty; otherwise, it will be a universe polyhedron.

• int ppl\_new\_NNC\_Polyhedron\_from\_NNC\_Polyhedron (ppl\_Polyhedron\_t \*pph, ppl\_const\_-Polyhedron\_t ph)

Builds an NNC polyhedron that is a copy of ph; writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_NNC\_Polyhedron\_from\_NNC\_Polyhedron\_with\_complexity (ppl\_Polyhedron\_t \*pph, ppl\_const\_Polyhedron\_t ph, int complexity)

Builds an NNC polyhedron that is a copy of ph; writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_NNC\_Polyhedron\_from\_Constraint\_System (ppl\_Polyhedron\_t \*pph, ppl\_const\_-Constraint System t cs)

Builds a new NNC polyhedron from the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_NNC\_Polyhedron\_recycle\_Constraint\_System (ppl\_Polyhedron\_t \*pph, ppl\_Constraint\_System\_t cs)

Builds a new NNC polyhedron recycling the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_NNC\_Polyhedron\_from\_Congruence\_System (ppl\_Polyhedron\_t \*pph, ppl\_const\_-Congruence System t cs)

Builds a new NNC polyhedron from the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_NNC\_Polyhedron\_recycle\_Congruence\_System (ppl\_Polyhedron\_t \*pph, ppl\_-Congruence\_System\_t cs)

Builds a new NNC polyhedron recycling the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_assign\_NNC\_Polyhedron\_from\_NNC\_Polyhedron (ppl\_Polyhedron\_t dst, ppl\_const\_-Polyhedron t src)

Assigns a copy of the NNC polyhedron src to the NNC polyhedron dst.

### **Constructors Behaving as Conversion Operators**

Besides the conversions listed here below, the library also provides conversion operators that build a semantic geometric description starting from any other semantic geometric description (e.g., ppl\_new\_Grid\_from\_C\_Polyhedron, ppl\_new\_C\_Polyhedron\_from\_BD\_Shape\_mpq\_class, etc.). Clearly, the conversion operators are only available if both the source and the target semantic geometric descriptions have been enabled when configuring the library. The conversions also taking as argument a complexity class sometimes provide non-trivial precision/efficiency trade-offs.

• int ppl\_new\_C\_Polyhedron\_from\_NNC\_Polyhedron (ppl\_Polyhedron\_t \*pph, ppl\_const\_-Polyhedron\_t ph)

Builds a C polyhedron that is a copy of the topological closure of the NNC polyhedron ph; writes a handle for the newly created polyhedron at address pph.

- int ppl\_new\_C\_Polyhedron\_from\_NNC\_Polyhedron\_with\_complexity (ppl\_Polyhedron\_t \*pph, ppl\_const\_Polyhedron\_t ph, int complexity)
  - Builds a C polyhedron that approximates NNC\_Polyhedron ph, using an algorithm whose complexity does not exceed complexity; writes a handle for the newly created polyhedron at address pph.
- int ppl\_new\_NNC\_Polyhedron\_from\_C\_Polyhedron (ppl\_Polyhedron\_t \*pph, ppl\_const\_-Polyhedron\_t ph)

Builds an NNC polyhedron that is a copy of the C polyhedron ph; writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_NNC\_Polyhedron\_from\_C\_Polyhedron\_with\_complexity (ppl\_Polyhedron\_t \*pph, ppl\_const\_Polyhedron\_t ph, int complexity)

Builds an NNC polyhedron that approximates C\_Polyhedron ph, using an algorithm whose complexity does not exceed complexity; writes a handle for the newly created polyhedron at address pph.

### Destructor for (C or NNC) Polyhedra

• int ppl\_delete\_Polyhedron (ppl\_const\_Polyhedron\_t ph)

Invalidates the handle ph: this makes sure the corresponding resources will eventually be released.

#### Functions that Do Not Modify the Polyhedron

- int ppl\_Polyhedron\_space\_dimension (ppl\_const\_Polyhedron\_t ph, ppl\_dimension\_type \*m)

  Writes to m the dimension of the vector space enclosing ph.
- int ppl\_Polyhedron\_affine\_dimension (ppl\_const\_Polyhedron\_t ph, ppl\_dimension\_type \*m)

  Writes to m the affine dimension of ph (not to be confused with the dimension of its enclosing vector space) or 0, if ph is empty.
- int ppl\_Polyhedron\_relation\_with\_Constraint (ppl\_const\_Polyhedron\_t ph, ppl\_const\_-Constraint\_t c)

Checks the relation between the polyhedron ph and the constraint c.

• int ppl\_Polyhedron\_relation\_with\_Generator (ppl\_const\_Polyhedron\_t ph, ppl\_const\_-Generator\_t g)

Checks the relation between the polyhedron ph and the generator g.

 int ppl\_Polyhedron\_get\_constraints (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Constraint\_-System\_t \*pcs)

Writes a const handle to the constraint system defining the polyhedron ph at address pcs.

• int ppl\_Polyhedron\_get\_congruences (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Congruence\_-System\_t \*pcs)

Writes at address pcs a const handle to a system of congruences approximating the polyhedron ph.

• int ppl\_Polyhedron\_get\_minimized\_constraints (ppl\_const\_Polyhedron\_t ph, ppl\_const\_-Constraint\_System\_t \*pcs)

Writes a const handle to the minimized constraint system defining the polyhedron ph at address pcs.

• int ppl\_Polyhedron\_get\_minimized\_congruences (ppl\_const\_Polyhedron\_t ph, ppl\_const\_-Congruence\_System\_t \*pcs) Writes at address pcs a const handle to a system of minimized congruences approximating the polyhedron ph.

- int ppl\_Polyhedron\_is\_empty (ppl\_const\_Polyhedron\_t ph)

  Returns a positive integer if ph is empty; returns 0 if ph is not empty.
- int ppl\_Polyhedron\_is\_universe (ppl\_const\_Polyhedron\_t ph)

  Returns a positive integer if ph is a universe polyhedron; returns 0 if it is not.
- int ppl\_Polyhedron\_is\_bounded (ppl\_const\_Polyhedron\_t ph)

  Returns a positive integer if ph is bounded; returns 0 if ph is unbounded.
- int ppl\_Polyhedron\_contains\_integer\_point (ppl\_const\_Polyhedron\_t ph)

  Returns a positive integer if ph contains at least one integer point; returns 0 otherwise.
- int ppl\_Polyhedron\_is\_topologically\_closed (ppl\_const\_Polyhedron\_t ph)

  Returns a positive integer if ph is topologically closed; returns 0 if ph is not topologically closed.
- int ppl\_Polyhedron\_is\_discrete (ppl\_const\_Polyhedron\_t ph)

  Returns a positive integer if ph is a discrete set; returns 0 if ph is not a discrete set.
- int ppl\_Polyhedron\_constrains (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var)

  Returns a positive integer if ph constrains var; returns 0 if ph does not constrain var.
- int ppl\_Polyhedron\_bounds\_from\_above (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Linear\_-Expression\_t le)

Returns a positive integer if le is bounded from above in ph; returns 0 otherwise.

• int ppl\_Polyhedron\_bounds\_from\_below (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Linear\_-Expression\_t le)

*Returns a positive integer if* le *is bounded from below in* ph; *returns 0 otherwise.* 

• int ppl\_Polyhedron\_maximize\_with\_point (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Linear\_-Expression\_t le, ppl\_Coefficient\_t sup\_n, ppl\_Coefficient\_t sup\_d, int \*pmaximum, ppl\_-Generator\_t point)

Returns a positive integer if ph is not empty and le is bounded from above in ph, in which case the supremum value and a point where le reaches it are computed.

• int ppl\_Polyhedron\_maximize (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Linear\_Expression\_t le, ppl\_Coefficient\_t sup\_n, ppl\_Coefficient\_t sup\_d, int \*pmaximum)

The same as ppl\_Polyhedron\_maximize\_with\_point, but without the output argument for the location where the supremum value is reached.

• int ppl\_Polyhedron\_minimize\_with\_point (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Linear\_-Expression\_t le, ppl\_Coefficient\_t inf\_n, ppl\_Coefficient\_t inf\_d, int \*pminimum, ppl\_-Generator\_t point)

Returns a positive integer if ph is not empty and le is bounded from below in ph, in which case the infimum value and a point where le reaches it are computed.

• int ppl\_Polyhedron\_minimize\_with\_point (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Linear\_-Expression\_t le, ppl\_Coefficient\_t inf\_n, ppl\_Coefficient\_t inf\_d, int \*pminimum)

The same as ppl\_Polyhedron\_minimize\_with\_point, but without the output argument for the location where the infimum value is reached.

• int ppl\_Polyhedron\_contains\_Polyhedron (ppl\_const\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y)

Returns a positive integer if x contains or is equal to y; returns 0 if it does not.

• int ppl\_Polyhedron\_strictly\_contains\_Polyhedron (ppl\_const\_Polyhedron\_t x, ppl\_const\_-Polyhedron\_t y)

Returns a positive integer if x strictly contains y; returns 0 if it does not.

• int ppl\_Polyhedron\_is\_disjoint\_from\_Polyhedron (ppl\_const\_Polyhedron\_t x, ppl\_const\_-Polyhedron\_t y)

Returns a positive integer if x and y are disjoint; returns 0 if they are not.

- int ppl\_Polyhedron\_equals\_Polyhedron (ppl\_const\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y)

  Returns a positive integer if x and y are the same polyhedron; returns 0 if they are different.
- int ppl\_Polyhedron\_OK (ppl\_const\_Polyhedron\_t ph)

  Returns a positive integer if ph is well formed, i.e., if it satisfies all its implementation invariants; returns

  0 and perhaps makes some noise if ph is broken. Useful for debugging purposes.
- int ppl\_Polyhedron\_external\_memory\_in\_bytes (ppl\_const\_Polyhedron\_t ph, size\_t \*sz) Writes to sz a lower bound to the size in bytes of the memory managed by ph.
- int ppl\_Polyhedron\_total\_memory\_in\_bytes (ppl\_const\_Polyhedron\_t ph, size\_t \*sz) Writes to sz a lower bound to the size in bytes of the memory managed by ph.

#### Space Dimension Preserving Functions that May Modify the Polyhedron

- int ppl\_Polyhedron\_add\_constraint (ppl\_Polyhedron\_t ph, ppl\_const\_Constraint\_t c)

  Adds a copy of the constraint c to the system of constraints of ph.
- int ppl\_Polyhedron\_add\_congruence (ppl\_Polyhedron\_t ph, ppl\_const\_Congruence\_t c)

  \*Adds a copy of the congruence c to polyhedron of ph.
- int ppl\_Polyhedron\_add\_constraints (ppl\_Polyhedron\_t ph, ppl\_const\_Constraint\_System\_t cs)

  Adds a copy of the system of constraints cs to the system of constraints of ph.
- int ppl\_Polyhedron\_add\_congruences (ppl\_Polyhedron\_t ph, ppl\_const\_Congruence\_System\_t cs)

Adds a copy of the system of congruences cs to the polyhedron ph.

• int ppl\_Polyhedron\_add\_recycled\_constraints (ppl\_Polyhedron\_t ph, ppl\_Constraint\_System\_t cs)

Adds the system of constraints cs to the system of constraints of ph.

 int ppl\_Polyhedron\_add\_recycled\_congruences (ppl\_Polyhedron\_t ph, ppl\_Congruence\_-System\_t cs)

Adds the system of congruences cs to the polyhedron ph.

- int ppl\_Polyhedron\_refine\_with\_constraint (ppl\_Polyhedron\_t ph, ppl\_const\_Constraint\_t c) \*Refines ph using constraint c.
- int ppl\_Polyhedron\_refine\_with\_congruence (ppl\_Polyhedron\_t ph, ppl\_const\_Congruence\_t c) Refines ph using congruence c.

• int ppl\_Polyhedron\_refine\_with\_constraints (ppl\_Polyhedron\_t ph, ppl\_const\_Constraint\_-System\_t cs)

Refines ph using the constraints in cs.

• int ppl\_Polyhedron\_refine\_with\_congruences (ppl\_Polyhedron\_t ph, ppl\_const\_Congruence\_-System\_t cs)

Refines ph using the congruences in cs.

- int ppl\_Polyhedron\_intersection\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y)

  Intersects x with polyhedron y and assigns the result to x.
- int ppl\_Polyhedron\_upper\_bound\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y)

  Assigns to x an upper bound of x and y.
- int ppl\_Polyhedron\_difference\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y) Same as ppl\_Polyhedron\_poly\_difference\_assign(x, y).
- int ppl\_Polyhedron\_simplify\_using\_context\_assign (ppl\_Polyhedron\_t x, ppl\_const\_-Polyhedron\_t y)

Assigns to x the meet-preserving simplification of x with respect to context y. Returns a positive integer if x and y have a nonempty intersection; returns 0 if they are disjoint.

- int ppl\_Polyhedron\_time\_elapse\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y)

  Assigns to x the time-elapse between the polyhedra x and y.
- int ppl\_Polyhedron\_topological\_closure\_assign (ppl\_Polyhedron\_t ph)

  Assigns to ph its topological closure.
- int ppl\_Polyhedron\_unconstrain\_space\_dimension (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var)

Modifies ph by unconstraining the space dimension var.

• int ppl\_Polyhedron\_unconstrain\_space\_dimensions (ppl\_Polyhedron\_t ph, ppl\_dimension\_type ds[], size\_t n)

Modifies ph by unconstraining the space dimensions that are specified in the first n positions of the array ds. The presence of duplicates in ds is a waste but an innocuous one.

• int ppl\_Polyhedron\_affine\_image (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, ppl\_const\_ Linear\_Expression\_t le, ppl\_const\_Coefficient\_t d)

Transforms the polyhedron ph, assigning an affine expression to the specified variable.

• int ppl\_Polyhedron\_affine\_preimage (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, ppl\_const\_ Linear\_Expression\_t le, ppl\_const\_Coefficient\_t d)

Transforms the polyhedron ph, substituting an affine expression to the specified variable.

- int ppl\_Polyhedron\_bounded\_affine\_image (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, ppl\_const\_Linear\_Expression\_t lb, ppl\_const\_Linear\_Expression\_t ub, ppl\_const\_Coefficient\_t d) Assigns to ph the image of ph with respect to the generalized affine transfer relation  $\frac{\text{lb}}{\text{d}} \leq \text{var}' \leq \frac{\text{ub}}{\text{d}}$ .
- int ppl\_Polyhedron\_bounded\_affine\_preimage (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, ppl\_const\_Linear\_Expression\_t lb, ppl\_const\_Linear\_Expression\_t ub, ppl\_const\_Coefficient\_t d)

Assigns to ph the preimage of ph with respect to the generalized affine transfer relation  $\frac{lb}{d} \leq var' \leq \frac{ub}{d}$ .

• int ppl\_Polyhedron\_generalized\_affine\_image (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, enum ppl\_enum\_Constraint\_Type relsym, ppl\_const\_Linear\_Expression\_t le, ppl\_const\_Coefficient t d)

Assigns to ph the image of ph with respect to the generalized affine transfer relation  $\operatorname{var}'\bowtie\frac{\operatorname{le}}{\operatorname{d}}$ , where  $\bowtie$  is the relation symbol encoded by relsym.

• int ppl\_Polyhedron\_generalized\_affine\_preimage (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, enum ppl\_enum\_Constraint\_Type relsym, ppl\_const\_Linear\_Expression\_t le, ppl\_const\_Coefficient t d)

Assigns to ph the preimage of ph with respect to the generalized affine transfer relation  $\operatorname{var}'\bowtie \frac{\operatorname{le}}{\operatorname{d}}$ , where  $\bowtie$  is the relation symbol encoded by relsym.

• int ppl\_Polyhedron\_generalized\_affine\_image\_lhs\_rhs (ppl\_Polyhedron\_t ph, ppl\_const\_-Linear\_Expression\_t lhs, enum ppl\_enum\_Constraint\_Type relsym, ppl\_const\_Linear\_-Expression\_t rhs)

Assigns to ph the image of ph with respect to the generalized affine transfer relation  $lhs' \bowtie rhs$ , where  $\bowtie$  is the relation symbol encoded by relsym.

• int ppl\_Polyhedron\_generalized\_affine\_preimage\_lhs\_rhs (ppl\_Polyhedron\_t ph, ppl\_const\_ Linear\_Expression\_t lhs, enum ppl\_enum\_Constraint\_Type relsym, ppl\_const\_Linear\_ Expression t rhs)

Assigns to ph the preimage of ph with respect to the generalized affine transfer relation lhs'  $\bowtie$  rhs, where  $\bowtie$  is the relation symbol encoded by relsym.

#### Functions that May Modify the Dimension of the Vector Space

- int ppl\_Polyhedron\_concatenate\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y)

  Seeing a polyhedron as a set of tuples (its points), assigns to x all the tuples that can be obtained by concatenating, in the order given, a tuple of x with a tuple of y.
- int ppl\_Polyhedron\_add\_space\_dimensions\_and\_embed (ppl\_Polyhedron\_t ph, ppl\_dimension\_type d)

Adds d new dimensions to the space enclosing the polyhedron ph and to ph itself.

• int ppl\_Polyhedron\_add\_space\_dimensions\_and\_project (ppl\_Polyhedron\_t ph, ppl\_dimension\_type d)

Adds d new dimensions to the space enclosing the polyhedron ph.

• int ppl\_Polyhedron\_remove\_space\_dimensions (ppl\_Polyhedron\_t ph, ppl\_dimension\_type ds[], size t n)

Removes from the vector space enclosing ph the space dimensions that are specified in first n positions of the array ds. The presence of duplicates in ds is a waste but an innocuous one.

• int ppl\_Polyhedron\_remove\_higher\_space\_dimensions (ppl\_Polyhedron\_t ph, ppl\_dimension\_type d)

Removes the higher dimensions from the vector space enclosing ph so that, upon successful return, the new space dimension is d.

• int ppl\_Polyhedron\_map\_space\_dimensions (ppl\_Polyhedron\_t ph, ppl\_dimension\_type maps[], size t n)

Remaps the dimensions of the vector space according to a partial function. This function is specified by means of the maps array, which has n entries.

• int ppl\_Polyhedron\_expand\_space\_dimension (ppl\_Polyhedron\_t ph, ppl\_dimension\_type d, ppl\_dimension\_type m)

Expands the *d-th dimension of the vector space enclosing* ph to m new space dimensions.

• int ppl\_Polyhedron\_fold\_space\_dimensions (ppl\_Polyhedron\_t ph, ppl\_dimension\_type ds[], size\_t n, ppl\_dimension\_type d)

Modifies ph by folding the space dimensions contained in the first n positions of the array ds into dimension d. The presence of duplicates in ds is a waste but an innocuous one.

#### **Input/Output Functions**

- int ppl\_io\_print\_Polyhedron (ppl\_const\_Polyhedron\_t x)

  \*Prints x to stdout.
- int ppl\_io\_fprint\_Polyhedron (FILE \*stream, ppl\_const\_Polyhedron\_t x)

  Prints x to the given output stream.
- int ppl\_io\_asprint\_Polyhedron (char \*\*strp, ppl\_const\_Polyhedron\_t x)

  Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_Polyhedron\_ascii\_dump (ppl\_const\_Polyhedron\_t x, FILE \*stream)

  Dumps an ascii representation of x on stream.
- int ppl\_Polyhedron\_ascii\_load (ppl\_Polyhedron\_t x, FILE \*stream)

  Loads an ascii representation of x from stream.

#### Ad Hoc Functions for (C or NNC) Polyhedra

The functions listed here below, being specific of the polyhedron domains, do not have a correspondence in other semantic geometric descriptions.

- int ppl\_new\_C\_Polyhedron\_from\_Generator\_System (ppl\_Polyhedron\_t \*pph, ppl\_const\_-Generator\_System\_t gs)
  - Builds a new C polyhedron from the system of generators gs and writes a handle for the newly created polyhedron at address pph.
- int ppl\_new\_C\_Polyhedron\_recycle\_Generator\_System (ppl\_Polyhedron\_t \*pph, ppl\_-Generator\_System\_t gs)

Builds a new C polyhedron recycling the system of generators gs and writes a handle for the newly created polyhedron at address pph.

- int ppl\_new\_NNC\_Polyhedron\_from\_Generator\_System (ppl\_Polyhedron\_t \*pph, ppl\_const\_-Generator\_System\_t gs)
  - Builds a new NNC polyhedron from the system of generators gs and writes a handle for the newly created polyhedron at address pph.
- int ppl\_new\_NNC\_Polyhedron\_recycle\_Generator\_System (ppl\_Polyhedron\_t \*pph, ppl\_-Generator\_System\_t gs)

Builds a new NNC polyhedron recycling the system of generators gs and writes a handle for the newly created polyhedron at address pph.

int ppl\_Polyhedron\_get\_generators (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Generator\_System\_t \*pgs)

Writes a const handle to the generator system defining the polyhedron ph at address pgs.

• int ppl\_Polyhedron\_get\_minimized\_generators (ppl\_const\_Polyhedron\_t ph, ppl\_const\_-Generator System t \*pgs)

Writes a const handle to the minimized generator system defining the polyhedron ph at address pqs.

- int ppl\_Polyhedron\_add\_generator (ppl\_Polyhedron\_t ph, ppl\_const\_Generator\_t g)

  Adds a copy of the generator g to the system of generators of ph.
- int ppl\_Polyhedron\_add\_generators (ppl\_Polyhedron\_t ph, ppl\_const\_Generator\_System\_t gs)

  Adds a copy of the system of generators gs to the system of generators of ph.
- int ppl\_Polyhedron\_add\_recycled\_generators (ppl\_Polyhedron\_t ph, ppl\_Generator\_System\_-t gs)

Adds the system of generators gs to the system of generators of ph.

- int ppl\_Polyhedron\_poly\_hull\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y)

  Assigns to x the poly-hull of x and y.
- int ppl\_Polyhedron\_poly\_difference\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y)

  Assigns to x the poly-difference of x and y.
- int ppl\_Polyhedron\_BHRZ03\_widening\_assign\_with\_tokens (ppl\_Polyhedron\_t x, ppl\_const\_-Polyhedron\_t y, unsigned \*tp)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the BHRZ03-widening of x and y. If tp is not the null pointer, the widening with tokens delay technique is applied with \*tp available tokens.

• int ppl\_Polyhedron\_H79\_widening\_assign\_with\_tokens (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y, unsigned \*tp)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the H79-widening of x and y. If tp is not the null pointer, the widening with tokens delay technique is applied with \*tp available tokens.

• int ppl\_Polyhedron\_BHRZ03\_widening\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the BHRZ03-widening of x and y.

- int ppl\_Polyhedron\_H79\_widening\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y)

  If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the H79-widening of x and y.
- int ppl\_Polyhedron\_limited\_BHRZ03\_extrapolation\_assign\_with\_tokens (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y, ppl\_const\_Constraint\_System\_t cs, unsigned \*tp)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the BHRZ03-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x. If tp is not the null pointer, the widening with tokens delay technique is applied with \*tp available tokens.

• int ppl\_Polyhedron\_limited\_H79\_extrapolation\_assign\_with\_tokens (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y, ppl\_const\_Constraint\_System\_t cs, unsigned \*tp)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the H79-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x. If tp is not the null pointer, the widening with tokens delay technique is applied with tp available tokens.

• int ppl\_Polyhedron\_limited\_BHRZ03\_extrapolation\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y, ppl\_const\_Constraint\_System\_t cs)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the BHRZ03-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x.

• int ppl\_Polyhedron\_limited\_H79\_extrapolation\_assign (ppl\_Polyhedron\_t x, ppl\_const\_-Polyhedron\_t y, ppl\_const\_Constraint\_System\_t cs)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the H79-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x.

• int ppl\_Polyhedron\_bounded\_BHRZ03\_extrapolation\_assign\_with\_tokens (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y, ppl\_const\_Constraint\_System\_t cs, unsigned \*tp)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the BHRZ03-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x, further intersected with all the constraints of the form  $\pm v \le r$  and  $\pm v < r$ , with  $r \in \mathbb{Q}$ , that are satisfied by all the points of x. If tp is not the null pointer, the widening with tokens delay technique is applied with tp available tokens.

• int ppl\_Polyhedron\_bounded\_H79\_extrapolation\_assign\_with\_tokens (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y, ppl\_const\_Constraint\_System\_t cs, unsigned \*tp)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the H79-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x, further intersected with all the constraints of the form  $\pm v \leq r$  and  $\pm v < r$ , with  $r \in \mathbb{Q}$ , that are satisfied by all the points of x. If tp is not the null pointer, the widening with tokens delay technique is applied with tp available tokens.

• int ppl\_Polyhedron\_bounded\_BHRZ03\_extrapolation\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y, ppl\_const\_Constraint\_System\_t cs)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the BHRZ03-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x, further intersected with all the constraints of the form  $\pm v \leq r$  and  $\pm v < r$ , with  $r \in \mathbb{Q}$ , that are satisfied by all the points of x.

• int ppl\_Polyhedron\_bounded\_H79\_extrapolation\_assign (ppl\_Polyhedron\_t x, ppl\_const\_-Polyhedron\_t y, ppl\_const\_Constraint\_System\_t cs)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the H79-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x, further intersected with all the constraints of the form  $\pm v \leq r$  and  $\pm v < r$ , with  $r \in \mathbb{Q}$ , that are satisfied by all the points of x.

# 7.19.1 Detailed Description

Types and functions for the domains of C and NNC convex polyhedra.

The types and functions for convex polyhedra provide a single interface for accessing both topologically closed (C) and not necessarily closed (NNC) convex polyhedra. The distinction between C and NNC polyhedra need only be explicitly stated when *creating* or *assigning* a polyhedron object, by means of one of the functions ppl\_new\_\* and ppl\_assign\_\*.

Having a single datatype does not mean that C and NNC polyhedra can be freely interchanged: as specified in the main manual, most library functions require their arguments to be topologically and/or space-dimension compatible.

#### 7.19.2 Friends And Related Function Documentation

# 7.19.2.1 int ppl\_new\_C\_Polyhedron\_from\_C\_Polyhedron\_with\_complexity (ppl\_Polyhedron\_t \* pph, ppl\_const\_Polyhedron\_t ph, int complexity) [related]

Builds a C polyhedron that is a copy of ph; writes a handle for the newly created polyhedron at address pph.

#### Note:

The complexity argument is ignored.

# 7.19.2.2 int ppl\_new\_C\_Polyhedron\_from\_Constraint\_System (ppl\_Polyhedron\_t \* pph, ppl\_const\_Constraint\_System\_t cs) [related]

Builds a new C polyhedron from the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

# 7.19.2.3 int ppl\_new\_C\_Polyhedron\_recycle\_Constraint\_System (ppl\_Polyhedron\_t \* pph, ppl\_Constraint\_System\_t cs) [related]

Builds a new C polyhedron recycling the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

### Warning:

This function modifies the constraint system referenced by cs: upon return, no assumption can be made on its value.

# 7.19.2.4 int ppl\_new\_C\_Polyhedron\_from\_Congruence\_System (ppl\_Polyhedron\_t \* pph, ppl\_const\_Congruence\_System\_t cs) [related]

Builds a new C polyhedron from the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

# 7.19.2.5 int ppl\_new\_C\_Polyhedron\_recycle\_Congruence\_System (ppl\_Polyhedron\_t \* pph, ppl\_Congruence\_System\_t cs) [related]

Builds a new C polyhedron recycling the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

## Warning:

This function modifies the congruence system referenced by cs: upon return, no assumption can be made on its value.

# 7.19.2.6 int ppl\_new\_NNC\_Polyhedron\_from\_NNC\_Polyhedron\_with\_complexity (ppl\_Polyhedron\_t \* pph, ppl\_const\_Polyhedron\_t ph, int complexity) [related]

Builds an NNC polyhedron that is a copy of ph; writes a handle for the newly created polyhedron at address pph.

#### Note:

The complexity argument is ignored.

# 7.19.2.7 int ppl\_new\_NNC\_Polyhedron\_from\_Constraint\_System (ppl\_Polyhedron\_t \* pph, ppl\_const\_Constraint\_System\_t cs) [related]

Builds a new NNC polyhedron from the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

# 7.19.2.8 int ppl\_new\_NNC\_Polyhedron\_recycle\_Constraint\_System (ppl\_Polyhedron\_t \* pph, ppl\_Constraint\_System\_t cs) [related]

Builds a new NNC polyhedron recycling the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

#### Warning:

This function modifies the constraint system referenced by cs: upon return, no assumption can be made on its value.

# 7.19.2.9 int ppl\_new\_NNC\_Polyhedron\_from\_Congruence\_System (ppl\_Polyhedron\_t \* pph, ppl\_const\_Congruence\_System\_t cs) [related]

Builds a new NNC polyhedron from the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

# 7.19.2.10 int ppl\_new\_NNC\_Polyhedron\_recycle\_Congruence\_System (ppl\_Polyhedron\_t \* pph, ppl\_Congruence\_System\_t cs) [related]

Builds a new NNC polyhedron recycling the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

#### Warning:

This function modifies the congruence system referenced by cs: upon return, no assumption can be made on its value.

# 7.19.2.11 int ppl\_new\_C\_Polyhedron\_from\_NNC\_Polyhedron\_with\_complexity (ppl\_Polyhedron\_t \* pph, ppl\_const\_Polyhedron\_t ph, int complexity) [related]

Builds a C polyhedron that approximates NNC\_Polyhedron ph, using an algorithm whose complexity does not exceed complexity; writes a handle for the newly created polyhedron at address pph.

#### Note:

The complexity argument, which can take values PPL\_COMPLEXITY\_CLASS\_POLYNOMIAL, PPL\_COMPLEXITY\_CLASS\_SIMPLEX and PPL\_COMPLEXITY\_CLASS\_ANY, is ignored since the exact constructor has polynomial complexity.

# 7.19.2.12 int ppl\_new\_NNC\_Polyhedron\_from\_C\_Polyhedron\_with\_complexity (ppl\_Polyhedron\_t \* pph, ppl\_const\_Polyhedron\_t ph, int complexity) [related]

Builds an NNC polyhedron that approximates C\_Polyhedron ph, using an algorithm whose complexity does not exceed complexity; writes a handle for the newly created polyhedron at address pph.

#### Note:

The complexity argument, which can take values PPL\_COMPLEXITY\_CLASS\_POLYNOMIAL, PPL\_COMPLEXITY\_CLASS\_SIMPLEX and PPL\_COMPLEXITY\_CLASS\_ANY, is ignored since the exact constructor has polynomial complexity.

# 7.19.2.13 int ppl\_Polyhedron\_relation\_with\_Constraint (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Constraint\_t c) [related]

Checks the relation between the polyhedron ph and the constraint c.

If successful, returns a non-negative integer that is obtained as the bitwise or of the bits (chosen among PPL\_POLY\_CON\_RELATION\_IS\_DISJOINT PPL\_POLY\_CON\_RELATION\_STRICTLY\_INTERSECTS, PPL\_POLY\_CON\_RELATION\_IS\_INCLUDED, and PPL\_POLY\_CON\_RELATION\_SATURATES) that describe the relation between ph and c.

# 7.19.2.14 int ppl\_Polyhedron\_relation\_with\_Generator (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Generator\_t g) [related]

Checks the relation between the polyhedron ph and the generator g.

If successful, returns a non-negative integer that is obtained as the bitwise or of the bits (only PPL\_POLY\_-GEN\_RELATION\_SUBSUMES, at present) that describe the relation between ph and q.

# 7.19.2.15 int ppl\_Polyhedron\_maximize\_with\_point (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Linear\_Expression\_t le, ppl\_Coefficient\_t sup\_n, ppl\_Coefficient\_t sup\_d, int \* pmaximum, ppl\_Generator\_t point) [related]

Returns a positive integer if ph is not empty and le is bounded from above in ph, in which case the supremum value and a point where le reaches it are computed.

### Parameters:

**ph** The polyhedron constraining le;

le The linear expression to be maximized subject to ph;

sup\_n Will be assigned the numerator of the supremum value;

sup\_d Will be assigned the denominator of the supremum value;

**pmaximum** Will store 1 in this location if the supremum is also the maximum, will store 0 otherwise; **point** Will be assigned the point or closure point where le reaches the extremum value.

If ph is empty or le is not bounded from above, 0 will be returned and sup\_n, sup\_d, \*pmaximum and point will be left untouched.

# 7.19.2.16 int ppl\_Polyhedron\_minimize\_with\_point (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Linear\_Expression\_t le, ppl\_Coefficient\_t inf\_n, ppl\_Coefficient\_t inf\_d, int \* pminimum, ppl\_Generator\_t point) [related]

Returns a positive integer if ph is not empty and le is bounded from below in ph, in which case the infimum value and a point where le reaches it are computed.

#### **Parameters:**

**ph** The polyhedron constraining le;

le The linear expression to be minimized subject to ph;

*inf\_n* Will be assigned the numerator of the infimum value;

*inf\_d* Will be assigned the denominator of the infimum value;

**pminimum** Will store 1 in this location if the infimum is also the minimum, will store 0 otherwise; **point** Will be assigned the point or closure point where le reaches the extremum value.

If ph is empty or le is not bounded from below, 0 will be returned and sup\_n, sup\_d, \*pmaximum and point will be left untouched.

# 7.19.2.17 int ppl\_Polyhedron\_equals\_Polyhedron (ppl\_const\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y) [related]

Returns a positive integer if x and y are the same polyhedron; returns 0 if they are different.

Note that x and y may be topology- and/or dimension-incompatible polyhedra: in those cases, the value 0 is returned.

# 7.19.2.18 int ppl\_Polyhedron\_add\_recycled\_constraints (ppl\_Polyhedron\_t ph, ppl\_Constraint\_System\_t cs) [related]

Adds the system of constraints cs to the system of constraints of ph.

#### Warning:

This function modifies the constraint system referenced by cs: upon return, no assumption can be made on its value.

# 7.19.2.19 int ppl\_Polyhedron\_add\_recycled\_congruences (ppl\_Polyhedron\_t ph, ppl\_Congruence\_System\_t cs) [related]

Adds the system of congruences cs to the polyhedron ph.

#### Warning:

This function modifies the congruence system referenced by cs: upon return, no assumption can be made on its value.

# 7.19.2.20 int ppl\_Polyhedron\_upper\_bound\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y) [related]

Assigns to x an upper bound of x and y.

For the domain of polyhedra, this is the same as ppl\_Polyhedron\_poly\_hull\_assign(x, y).

# 7.19.2.21 int ppl\_Polyhedron\_affine\_image (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, ppl\_const\_Linear\_Expression\_t le, ppl\_const\_Coefficient\_t d) [related]

Transforms the polyhedron ph, assigning an affine expression to the specified variable.

#### **Parameters:**

- **ph** The polyhedron that is transformed;
- var The variable to which the affine expression is assigned;
- le The numerator of the affine expression;
- **d** The denominator of the affine expression.

# 7.19.2.22 int ppl\_Polyhedron\_affine\_preimage (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, ppl\_const\_Linear\_Expression\_t le, ppl\_const\_Coefficient\_t d) [related]

Transforms the polyhedron ph, substituting an affine expression to the specified variable.

#### **Parameters:**

- **ph** The polyhedron that is transformed;
- var The variable to which the affine expression is substituted;
- le The numerator of the affine expression;
- **d** The denominator of the affine expression.

# 7.19.2.23 int ppl\_Polyhedron\_bounded\_affine\_image (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, ppl\_const\_Linear\_Expression\_t lb, ppl\_const\_Linear\_Expression\_t ub, ppl\_const\_Coefficient\_t d) [related]

Assigns to ph the image of ph with respect to the generalized affine transfer relation  $\frac{\text{lb}}{\text{d}} \leq \text{var}' \leq \frac{\text{ub}}{\text{d}}$ .

#### **Parameters:**

- **ph** The polyhedron that is transformed;
- var The variable bounded by the generalized affine transfer relation;
- *lb* The numerator of the lower bounding affine expression;
- *ub* The numerator of the upper bounding affine expression;
- d The (common) denominator of the lower and upper bounding affine expressions.

7.19.2.24 int ppl\_Polyhedron\_bounded\_affine\_preimage (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, ppl\_const\_Linear\_Expression\_t lb, ppl\_const\_Linear\_Expression\_t ub, ppl\_const\_Coefficient\_t d) [related]

Assigns to ph the preimage of ph with respect to the generalized affine transfer relation  $\frac{lb}{d} \leq var' \leq \frac{ub}{d}$ .

#### **Parameters:**

- **ph** The polyhedron that is transformed;
- var The variable bounded by the generalized affine transfer relation;
- *lb* The numerator of the lower bounding affine expression;
- *ub* The numerator of the upper bounding affine expression;
- d The (common) denominator of the lower and upper bounding affine expressions.

# 7.19.2.25 int ppl\_Polyhedron\_generalized\_affine\_image (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, enum ppl\_enum\_Constraint\_Type relsym, ppl\_const\_Linear\_Expression\_t le, ppl\_const\_Coefficient\_t d) [related]

Assigns to ph the image of ph with respect to the *generalized affine transfer relation*  $\operatorname{var}' \bowtie \frac{\operatorname{le}}{\operatorname{d}}$ , where  $\bowtie$  is the relation symbol encoded by relsym.

#### **Parameters:**

- **ph** The polyhedron that is transformed;
- var The left hand side variable of the generalized affine transfer relation;
- *relsym* The relation symbol;
- le The numerator of the right hand side affine expression;
- d The denominator of the right hand side affine expression.

# 7.19.2.26 int ppl\_Polyhedron\_generalized\_affine\_preimage (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, enum ppl\_enum\_Constraint\_Type relsym, ppl\_const\_Linear\_Expression\_t le, ppl\_const\_Coefficient\_t d) [related]

Assigns to ph the preimage of ph with respect to the *generalized affine transfer relation*  $var' \bowtie \frac{le}{d}$ , where  $\bowtie$  is the relation symbol encoded by relsym.

#### **Parameters:**

- **ph** The polyhedron that is transformed;
- var The left hand side variable of the generalized affine transfer relation;
- *relsym* The relation symbol;
- le The numerator of the right hand side affine expression;
- d The denominator of the right hand side affine expression.

7.19.2.27 int ppl\_Polyhedron\_generalized\_affine\_image\_lhs\_rhs (ppl\_Polyhedron\_t ph, ppl\_const\_Linear\_Expression\_t lhs, enum ppl\_enum\_Constraint\_Type relsym, ppl\_const\_Linear\_Expression\_t rhs) [related]

Assigns to ph the image of ph with respect to the *generalized affine transfer relation* lhs'  $\bowtie$  rhs, where  $\bowtie$  is the relation symbol encoded by relsym.

#### **Parameters:**

```
ph The polyhedron that is transformed;lhs The left hand side affine expression;relsym The relation symbol;rhs The right hand side affine expression.
```

# 7.19.2.28 int ppl\_Polyhedron\_generalized\_affine\_preimage\_lhs\_rhs (ppl\_Polyhedron\_t ph, ppl\_const\_Linear\_Expression\_t lhs, enum ppl\_enum\_Constraint\_Type relsym, ppl\_const\_Linear\_Expression t rhs) [related]

Assigns to ph the preimage of ph with respect to the *generalized affine transfer relation* lhs'  $\bowtie$  rhs, where  $\bowtie$  is the relation symbol encoded by relsym.

#### **Parameters:**

```
ph The polyhedron that is transformed;lhs The left hand side affine expression;relsym The relation symbol;rhs The right hand side affine expression.
```

# 7.19.2.29 int ppl\_Polyhedron\_map\_space\_dimensions (ppl\_Polyhedron\_t ph, ppl\_dimension\_type maps[], size\_t n) [related]

Remaps the dimensions of the vector space according to a *partial function*. This function is specified by means of the maps array, which has n entries.

The partial function is defined on dimension i if i < n and maps [i] != ppl\_not\_a\_dimension; otherwise it is undefined on dimension i. If the function is defined on dimension i, then dimension i is mapped onto dimension maps [i].

The result is undefined if maps does not encode a partial function with the properties described in the *specification of the mapping operator*.

# 7.19.2.30 int ppl\_new\_C\_Polyhedron\_from\_Generator\_System (ppl\_Polyhedron\_t \*pph, ppl\_const\_Generator\_System\_t gs) [related]

Builds a new C polyhedron from the system of generators gs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of gs.

# 7.19.2.31 int ppl\_new\_C\_Polyhedron\_recycle\_Generator\_System (ppl\_Polyhedron\_t \* pph, ppl\_Generator\_System\_t gs) [related]

Builds a new C polyhedron recycling the system of generators gs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of gs.

#### Warning:

This function modifies the generator system referenced by gs: upon return, no assumption can be made on its value.

# 7.19.2.32 int ppl\_new\_NNC\_Polyhedron\_from\_Generator\_System (ppl\_Polyhedron\_t \* pph, ppl\_const\_Generator\_System\_t gs) [related]

Builds a new NNC polyhedron from the system of generators gs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of gs.

# 7.19.2.33 int ppl\_new\_NNC\_Polyhedron\_recycle\_Generator\_System (ppl\_Polyhedron\_t \* pph, ppl\_Generator\_System\_t gs) [related]

Builds a new NNC polyhedron recycling the system of generators gs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of qs.

### Warning:

This function modifies the generator system referenced by gs: upon return, no assumption can be made on its value.

# 7.19.2.34 int ppl\_Polyhedron\_add\_recycled\_generators (ppl\_Polyhedron\_t ph, ppl\_Generator\_System\_t gs) [related]

Adds the system of generators gs to the system of generators of ph.

#### Warning:

This function modifies the generator system referenced by gs: upon return, no assumption can be made on its value.

The documentation for this interface was generated from the following file:

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