Notes on Consensus Protocols

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Consensus. A set of n distributed nodes want to agree on a single value proposed by one of them. In the context of blockchains, consensus often means agreement on a sequence of values similar to an atomic broadcast [CV17]. A consensus protocol generally provides the following properties:

- Agreement: All honest nodes agree on the same message.
- Validity: All honest nodes decide on the the input of some honest node.
- Integrity: Every honest node decides on at most one value which is the input of some node.
- *Termination:* All honest nodes decide on some value.

Byzantine Faults. A node that can deviate arbitrarily from the protocol. Byzantine nodes can vote for both a statement and its contradiction, i.e., make different statements to different nodes to put honest nodes into inconsistent states. When consensus is performed in such a setting, it is often called Byzantine consensus/agreement.

Interactive Consistency (IC) [PSL80]. Each participant has an initial value. All honest participants must agree on a vector of values, one for each participant. More formally:

- Agreement: All honest parties output the same array of values $A[v_1,...,v_n]$.
- *Validity*: If party i is honest and its input is v_i , then all honest parties agree on v_i for A[i]. If party i is faulty, then honest parties can agree on any value for A[i].
- *Termination*: Each honest party must eventually decide on *A*.

Byzantine Generals Problem [LSP82]. Consider a group of parties, where one of them, called the *leader* (or *source* or *dealer*), holds an initial value. A Byzantine generals protocol satisfies the following properties:

- *Agreement*: All honest parties output the same value.
- *Validity*: If the leader is honest, then all honest parties output the value proposed by the leader.
- Termination: Each honest party must eventually decide on a value.

Byzantine Agreement Problem [LSP82]. In the distributed computing literature, the term "Byzantine agreement" has been used to refer to multiple problems (*e.g.*, compare [DFF⁺82, LLR02]). Here we adopt the definition used more frequently as in [LLR02, KS16]. Consider a group of parties each holding an initial value. A Byzantine agreement protocol satisfies the following properties:

- *Agreement*: All honest parties output the same value.
- Validity: If all honest parties start with the same initial value v, then all honest parties output v.
- Termination: Each honest party must eventually decide on a value.

Equivalence of Consensus Variants. If any of the consensus variants (Byzantine agreement, consensus, and interactive consistency) has a solution, then all of them have a solution. For example, IC can be achieved from BA by run BA n times, one with each participant as the leader. Also, consensus can be achieved from IC by running IC, then outputting the first element of the vector.

Safety and Liveness Guarantees. *Safety* means that all honest nodes agree on the same outcome. *Liveness* means that the honest nodes will make progress during the course of the protocol. Safety can be trivially achieved by making no forward progress at all from an initial state. Liveness can be trivially achieved by making progress unsafely by just letting each node decide on arbitrary outcomes. Neither of these guarantees are useful by themselves.

Consensus Termination. A consensus protocol terminates when all honest participants have terminated. If all honest participants terminate in the same round, then we call they have achieved an *immediate agreement*. Otherwise, we call they have achieved an *eventual agreement* [Fis83]. Pease *et al.* [?] show that at most t < n/2 nodes can be faulty for the Byzantine agreement to be solvable. Also, they show that if messages are not authenticated using a digital signature scheme, then at most t < n/3 nodes can be faulty.

CAP Theorem. It is impossible for a distributed data store to simultaneously provide more than two out of the following three properties:

- **Consistency:** Every read receives the most recent write or an error.
- Availability: Every request receives a (non-error) response.
- **Partition Tolerance:** The system works even if an arbitrary number of messages being dropped (or delayed).

In other words, in the presence of a network partition, the system can only guarantee either consistency or availability. Existing decentralized systems (such as cryptocurrencies) work by compromising between availability and consistency.

Authenticated Byzantine Agreement. When messages exchanged between the participants are signed using a digital signature scheme, the protocol is called authenticated Byzantine agreement. This assumption requires that the author of a signed message be determined by anyone holding the message, regardless of where it came from (this is often called the *non-repudiation* property). Therefore, message authentication codes (MACs) cannot be solely used to provide authenticated BA. Such an assumption makes synchronous Byzantine agreement solvable when f < n/2 [RNAD17]. The intuition behind this is that corrupted nodes can no longer simulate the actions of honest nodes because the use of digital signatures prevents impersonations.

Dolev and Strong [DS83] show that t + 1 rounds are necessary and sufficient for *deterministic* BA protocols even in the authenticated setting. They show that this can be achieved by exchanging O(nt) messages using the following algorithm:

Failure type	Syn- chronous	Asyn-chronous	Partially syn- chronous com- munication and synchronous processors	Partially syn- chronous communica- tion and pro- cessors	Partially syn- chronous pro- cessors and synchronous communica- tion
Fail-stop	t	∞	2t + 1	2t + 1	t
Omission	t	00	2t + 1	2t + 1	[2t, 2t + 1]
Authenticated Byzantine	t	œ	3t + 1	3t + 1	2t + 1
Byzantine	3t + 1	∞	3t + 1	3t + 1	3t + 1

Figure 1: Smallest number of nodes for which *t*-resilient consensus protocol exists [DLS88].

- 1. In each round, each node signs the value and sends it to only the participants who have not signed it yet.
- 2. After t rounds, each message has t signatures on it. Hence, each correct value has been seen by all the correct participants after t + 1 rounds.

Message and Round Impossibilities of BA. For deterministic protocols, it is shown that t + 1 rounds are needed for both unauthenticated and authenticated BA [FL81, DS82]. Also, any (deterministic) authenticated BA requires exchanging $\Omega(nt)$ messages [DR82].

FLP Impossibility [FLP85]. Deterministic consensus in the asynchronous setting is impossible even with one crash failure. This is because it is impossible to distinguish a failed process from a very slow one, so processes remain ambivalent when deciding. To avoid this impossibility and/or to achieve practicality, the protocol may be allowed to provide probabilistic safety or liveness guarantees. In the latter case, the protocol is said to provide *eventual liveness* (or *eventual consistency*) since nodes can decide on a value with probability one but with no time bound.

Bracha-Toueg Impossibility [BT83]. There is no (probabilistic) asynchronous consensus protocol resilient to $t \ge n/3$ malicious nodes. See Figure 1.

Broadcast Channel. If a broadcast channel is available, then the Byzantine agreement problem is trivial for t < n/2: Each player simply broadcasts their value and then honest players decide on the majority value.

Authenticated Broadcast. Unlike Byzantine agreement which is only solvable in the honest majority (*i.e.*, t < n/2) setting, Byzantine broadcast is solvable for any t < n. Dolev and Strong [DS83] show that t + 1 rounds are necessary and sufficient for *deterministic* authenticated broadcast protocols. Pease et al. [29, 24] construct an authenticated broadcast protocol for any t < n, and Dolev and Strong [DS83] propose a polynomial-time broadcast protocol for this setting. A dishonest majority broadcast protocol can be used to achieve unanimous abort [GL02] and partial fairness [GVZ06].

Atomic Broadcast. A set of distributed nodes agree on a sequence of values [HT93]. Consensus and atomic broadcast are equivalent because a sequence of consensus instances provides atomic broadcast. An atomic broadcast protocol generally provides the following properties:

- Agreement: All honest nodes eventually receive the same message.
- Validity: If an honest node broadcasts a message, then all honest nodes eventually receive it.
- Integrity: All honest nodes receive the same message exactly once.
- *Total Order:* An honest node receives m_1 before m_2 if and only if the sender sends m_1 before m_2 .

State-Machine Replication. A protocol that runs among a set of nodes to agree on a sequence of requests based on a deterministic state machine that implements the logic of a service to be replicated among the nodes.

Eventual Synchrony. Introduced by Dwork [DLS88], it models an asynchronous network that may delay messages among honest nodes arbitrarily, but eventually behaves synchronously delivering all messages within a *fixed* but *unknown* time bound. It is widely accepted as a realistic model for designing robust distributed systems [CV17].

Partial Synchrony. Similar to eventual synchrony but with probabilistic network behavior over time [DLS88].

View-Change Protocols. Some consensus protocols such as Paxos [Lam98], Raft [OO14], and PBFT [CL99] proceed in *epochs* (a.k.a., *views*), where a *leader* (a.k.a., the *primary*) is responsible for the progress of the protocol. When a node (a.k.a., a *replicate* or *backup*) suspects that the leader is faulty, the node broadcasts a View-Change message to replace the leader. The new leader has to gather at least 2f + 1 signed View-Change messages, to broadcast a New-View message. A Byzantine leader cannot violate safety (*i.e.*, cause inconsistencies) but can violate liveness (*i.e.*, prevent progress) by not proposing. In PBFT [CL99], every honest participant monitors the current leader, and if a new message is not proposed after some time, the honest participant requests a new leader.

Byzantine Generals Problem. A commanding general orders its lieutenant generals to attack or to surrender. Some of the generals are traitors. The goal is:

- All loyal lieutenants obey the same order, or
- If the commanding general is loyal, then every loyal lieutenant obeys the order he sends.

Why is consensus among generals important? Because, halfhearted attack by a few generals would be worse than a coordinated attack or a coordinated retreat. Pease et al. [?] prove 3f + 1 parties are necessary to achieve agreement in this problem.

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