# Homework 1

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2024-02-07

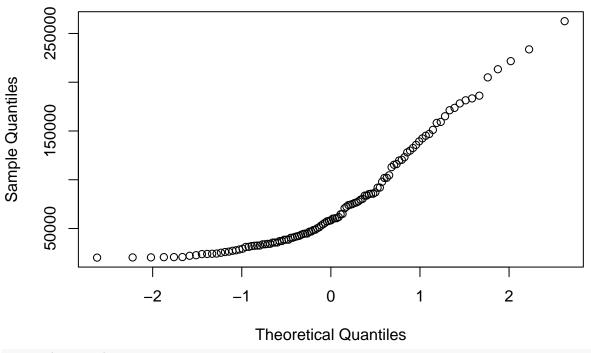
### Question 1

```
# load data
data <- read.csv("HW1P1.csv")
```

#### Part a:

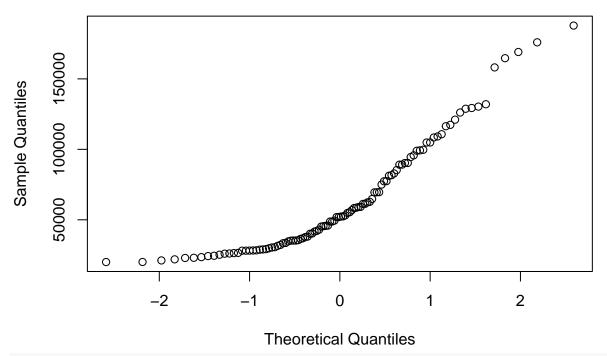
```
# make a new column that is the difference between the two
male_vec <- data$Males
fem_vec <- na.omit(data$Females)
# check normality of the difference
qqnorm(male_vec)</pre>
```

# Normal Q-Q Plot



qqnorm(fem\_vec)

# Normal Q-Q Plot



# let H\_alt be mu > 0 with 99% confidence
# run student t.test
t.test(male\_vec,fem\_vec, alternative = "greater", paired = F, conf.level = .99)

The selected  $\alpha = 0.01$  and here p-value is greater that 0.01. Thus we fail to reject the null hypothesis.

conclusion: There is not sufficient sample evidence to support the claim that "males are making more than females."

#### part b.

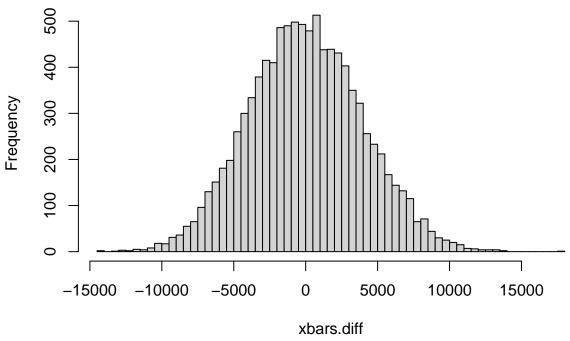
```
# find population mean
BS.male_vec <- male_vec - mean(male_vec)
BS.fem_vec <- fem_vec - mean(fem_vec)
BS.pop.mean <- mean(male_vec) - mean(fem_vec)

# bootstrapping

xbars.diff <- rep(0,10000)
for (i in 1:10000){
    sampleM <- sample(BS.male_vec,300, replace = T)
    sampleF <- sample(BS.fem_vec,300, replace = T)
    xbars.diff[i] <- mean(sampleM - sampleF)
}

# render histogram
hist(xbars.diff, breaks = 80)</pre>
```

# Histogram of xbars.diff



```
# finding a p-value
pval <- length(xbars.diff[xbars.diff > BS.pop.mean])/10000
pval
```

## [1] 1e-04

The histogram suggests we can follow a normally distributed data set with our bootstrapped data; this suggested we could create a p-value. It would be necessary

#### Question 2

```
#generate observations
obs <- rnorm(100000)</pre>
```

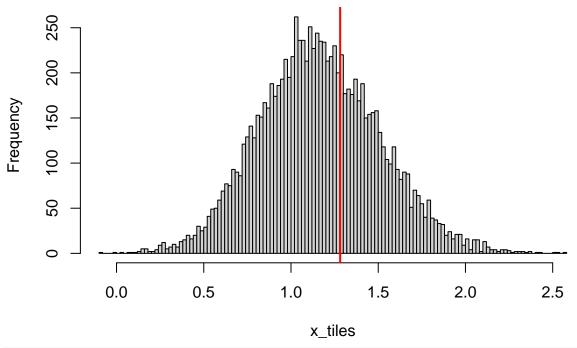
#### part a.

```
x_tiles <- rep(0,10000)
true_90th <- quantile(obs, .9)

for (i in 1:10000){
   samp <- sample(obs,20,replace = T)</pre>
```

```
x_tiles[i] <- quantile(samp, .9)
}
hist(x_tiles, breaks = 160)
abline(v = true_90th,col = "red", lwd = 2)</pre>
```

# Histogram of x\_tiles

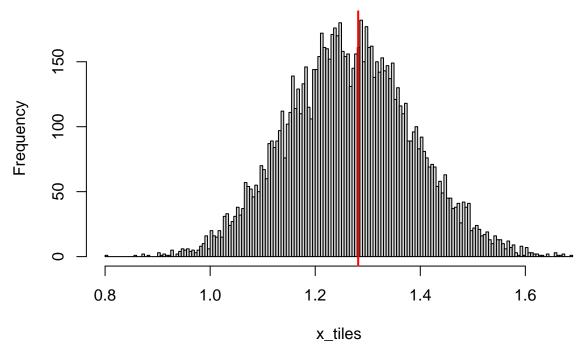


```
# bootstrap now but with a larger sample size in each iteration

for (i in 1:10000){
    samp <- sample(obs,200,replace = T)
    x_tiles[i] <- quantile(samp, .9)
}

hist(x_tiles, breaks = 160)
abline(v = true_90th,col = "red", lwd = 2)</pre>
```

# Histogram of x\_tiles



Using only a sample size of 20 is biased as when I highered the sample size in the second graphic, the true 90% tile got closer to median.

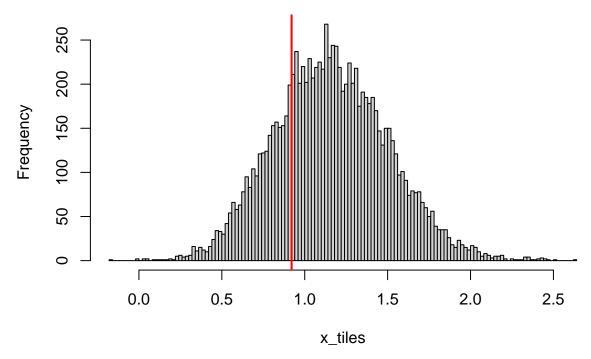
#### part b.

```
single.samp.90 <- quantile(sample(obs,20,replace = T),.9)

for (i in 1:10000){
   samp <- sample(obs,20,replace = T)
   x_tiles[i] <- quantile(samp, .9)
}

hist(x_tiles, breaks = 160)
abline(v = single.samp.90,col = "red", lwd = 2)</pre>
```

# Histogram of x\_tiles



This doesn't seem as biased as our last example as the single sampled 90th quantile is about at the median/mean when we present our graphic.

I think to a degree we can possibly quantify the amount of bias

#### part c.