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1 Introduction

2 Problem 1

Exercise 17, section 2.5.

$$\lim_{x \rightarrow 1} \frac{2-x}{(x-1)^2} = \frac{1}{0^+} = \infty$$

3 Problem 2

Exercise 21, section 2.5:

$$\lim_{x \rightarrow \infty} \frac{x^3 + 5x}{2x^3 - x^2 + 4} = \lim_{x \rightarrow \infty} \frac{1 + \frac{5x}{x^3}}{2 - \frac{x^2}{x^3} + \frac{4}{x^3}} = \frac{1}{2}$$

Three other similar examples:

$$\lim_{x \rightarrow \infty} \frac{x^2 + 5x}{2x^3 - x^2 + 4} = \lim_{x \rightarrow \infty} \frac{\frac{1}{x} + \frac{5x}{x^3}}{2 - \frac{x^2}{x^3} + \frac{4}{x^3}} = 0$$

$$\lim_{x \rightarrow \infty} \frac{x^4 + 5x}{2x^3 - x^2 + 4} = \lim_{x \rightarrow \infty} \frac{x + \frac{5x}{x^3}}{2 - \frac{x^2}{x^3} + \frac{4}{x^3}} = +\infty$$

$$\lim_{x \rightarrow \infty} \frac{x^4 + 5x}{-2x^3 - x^2 + 4} = \lim_{x \rightarrow \infty} \frac{x + \frac{5x}{x^3}}{-2 - \frac{x^2}{x^3} + \frac{4}{x^3}} = -\infty$$

4 Problem 3

Exercise 25.

$$\begin{aligned} \lim_{x \rightarrow \infty} \left(\sqrt{9x^2 + x} - 3x \right) &= \lim_{x \rightarrow \infty} \left(\sqrt{9x^2 + x} - 3x \right) \frac{\sqrt{9x^2 + x} + 3x}{\sqrt{9x^2 + x} + 3x} = \lim_{x \rightarrow \infty} \frac{(9x^2 + x) - 9x^2}{\sqrt{9x^2 + x} + 3x} = \\ &= \lim_{x \rightarrow \infty} \frac{x}{\sqrt{9x^2 + x} + 3x} = \lim_{x \rightarrow \infty} \frac{1}{\frac{\sqrt{9x^2 + x}}{x} + 3} = \lim_{x \rightarrow \infty} \frac{1}{\sqrt{9 + \frac{1}{x}} + 3} = \frac{1}{\sqrt{9} + 3} = \frac{1}{6} \end{aligned}$$

5 Problem 4

Similar to the Exercise 8, section 2.6.

$$y = x^3$$

Calculate the slope of the tangent line at the point $x = a$. The slope at the point a is defined as

$$m = \lim_{h \rightarrow 0} \frac{y(a+h) - y(a)}{h}$$

So we get:

$$m = \lim_{h \rightarrow 0} \frac{y(a+h) - y(a)}{h} = \lim_{h \rightarrow 0} \frac{(a+h)^3 - a^3}{h} = \lim_{h \rightarrow 0} \frac{3a^2h + O(h^2)}{h} = \lim_{h \rightarrow 0} (3a^2 + O(h)) = 3a^2$$

6 Quizzes

We did Quiz 5 & 6.