

1. **A.** The points of inflection are at  $x = 2, x = 4, x = 6$  because the tangent slope of the tangent lines at these points are  $0 \rightarrow f''(x) = 0$ . That means that the graph of  $f$  changes its concavity at these points.  
**B.** The function  $f$  has has relative maximum at  $x = 7$  because there is a critical point  $f'(7) = 0$  and  $f''(7) < 0$ .  
**C.** The graph is concave up on  $0 < x < 2$  and  $4 < x < 6$  because  $f''(x) > 0$  for those intervals.
2. **A.** To identify the relative extrema of  $g$  we need to find the critical points. We know that  $f'(x) = 0$  or  $DNE$  at those points.

$$f'(x) = 3x^2 - 12$$

Now we need to set it equal to zero

$$x = \pm 2$$

We know that the critical point of  $g$  is at  $x = \pm 2$ . Now we need to look at the function  $g''$  to determine wether it is maximum, minimum or neither of those.

$$g''(x) = 6x$$

If we plug the x-coordinates of the critical points into the second derivative we'll know that  $g''(-2) < 0$  and  $g''(2) > 0$ . We now know that there's maximum at  $x = -2$  where  $g(-2) = 16$  and there's a minimum at  $x = 2$  where  $g(2) = -16$ .

**B.** To determine the concavity of the function we need to find the inflection points ( $g''(x) = 0$ ) which will split the function into concave up and concave down areas.

$$0 = 6x$$

$$x = 0$$

The point of inflection of  $g$  is at  $x = 0$ . From the previous part we know that for  $x < 0$   $g''(x) < 0$  and for  $x > 0$   $g''(x) > 0$ . The function is concave down for  $x < 0$  and concave up for  $x > 0$ .