



Keras

Example 4 – Keras for regression

Example 4 – Boston dataset

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
```

```
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import StandardScaler
```

```
import tensorflow as tf
import random as python_random
```

```
from keras.models import Sequential
from keras.layers import Dense
```

Example 4 – Boston dataset

```
df0 = pd.read_csv( 'Boston.csv' )
df0.shape
```

```
(506, 14)
```

```
df0[:5]
```

| | crim | zn | indus | chas | nox | rm | age | dis | rad | tax | ptratio | black | lstat | medv |
|---|---------|------|-------|------|-------|-------|------|--------|-----|-----|---------|--------|-------|------|
| 0 | 0.00632 | 18.0 | 2.31 | 0 | 0.538 | 6.575 | 65.2 | 4.0900 | 1 | 296 | 15.3 | 396.90 | 4.98 | 24.0 |
| 1 | 0.02731 | 0.0 | 7.07 | 0 | 0.469 | 6.421 | 78.9 | 4.9671 | 2 | 242 | 17.8 | 396.90 | 9.14 | 21.6 |
| 2 | 0.02729 | 0.0 | 7.07 | 0 | 0.469 | 7.185 | 61.1 | 4.9671 | 2 | 242 | 17.8 | 392.83 | 4.03 | 34.7 |
| 3 | 0.03237 | 0.0 | 2.18 | 0 | 0.458 | 6.998 | 45.8 | 6.0622 | 3 | 222 | 18.7 | 394.63 | 2.94 | 33.4 |
| 4 | 0.06905 | 0.0 | 2.18 | 0 | 0.458 | 7.147 | 54.2 | 6.0622 | 3 | 222 | 18.7 | 396.90 | 5.33 | 36.2 |

Example 4 – Boston dataset

```
df = df0.values  
X = df[:,0:13]  
y = df[:,13]
```

```
# Reserve test set for performance evaluation
```

```
X_train,X_test,y_train,y_test = train_test_split(X,y,random_state=7,  
                                                test_size = 0.20)
```

```
scaler = StandardScaler()  
scaler.fit(X_train)
```

```
Xtrain_scaled = scaler.transform(X_train)  
Xtest_scaled = scaler.transform(X_test)
```

```
X_train.shape
```

```
(404, 13)
```

Example 4 – Boston dataset

```
# to have reproducible results
```

```
j = 999  
# for starting Numpy generated random numbers  
np.random.seed(j)  
# for starting core Python generated random numbers  
python_random.seed(j)  
# for starting tensorflow random number generation  
tf.random.set_seed(j)
```

```
# An input layer with 13 nodes (one for each predictor)  
# two hidden layers with 64 nodes  
# try 10 epochs, then will increase to 50  
# for regression problems, use output layer with one node, always
```

```
model = Sequential()  
model.add(Dense(64,activation = 'relu', input_shape=(13,)))  
model.add(Dense(64,activation = 'relu'))  
model.add(Dense(1))  
model.compile(optimizer = 'rmsprop', loss = 'mse', metrics=['mae'])  
model.fit(Xtrain_scaled,y_train,epochs =10, batch_size = 1);
```

Example 4 – Boston dataset

```
model = Sequential()
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model.fit(Xtrain_scaled,y_train,epochs =10, batch_size = 1)
```

```
Epoch 1/10
404/404 [=====] - 1s 1ms/step - loss: 165.145
5 - mae: 9.1668
Epoch 2/10
404/404 [=====] - 0s 1ms/step - loss: 21.1889
- mae: 3.1907
Epoch 3/10
404/404 [=====] - 1s 2ms/step - loss: 15.6568
- mae: 2.7467
```

...

```
mse, mae = model.evaluate(Xtest_scaled,y_test,verbose=0)
print(mse, ', ', mae)
```

```
27.150823985829074 , 3.0409677028656006
```

Example 4 – Boston dataset

```

model = Sequential()
model.add(Dense(64, activation = 'relu', input_shape=(13,)))
model.add(Dense(64, activation = 'relu'))
model.add(Dense(1))
model.compile(optimizer = 'rmsprop', loss = 'mse', metrics=['mae'])
model.fit(Xtrain_scaled, y_train, epochs = 10, batch_size = 1)

```

Annotations in the original image:

- 1 input layer (pointing to `input_shape=(13,)`)
- 2 hidden layers (pointing to the two `Dense(64, ...)` layers)
- 1 output layer (pointing to `Dense(1)`)

```

Epoch 1/10
404/404 [=====] - 1s 1ms/step - loss: 165.145
5 - mae: 9.1668
Epoch 2/10
404/404 [=====] - 0s 1ms/step - loss: 21.1889
- mae: 3.1907
Epoch 3/10
404/404 [=====] - 1s 2ms/step - loss: 15.6568
- mae: 2.7467

```

```

...
mse, mae = model.evaluate(Xtest_scaled, y_test, verbose=0)
print(mse, ', ', mae)

```

```

27.150823985829074 , 3.0409677028656006

```


Example 4 – Boston dataset

```
model = Sequential()  
model.add(Dense(64,activation = 'relu', input_shape=(13,)))  
model.add(Dense(64,activation = 'relu'))  
model.add(Dense(1))  
model.compile(optimizer = 'rmsprop', loss = 'mse', metrics=['mae'])  
model.fit(Xtrain_scaled,y_train,epochs =50, batch_size = 1,verbose = 0)
```

```
mse, mae = model.evaluate(Xtest_scaled,y_test,verbose=0)  
print(mse, ', ', mae)
```

```
22.646251933247434 , 2.7271087169647217
```

Example 4 – K-fold Cross Validation

```
def build_model():  
    model = Sequential()  
    model.add(Dense(64, activation = 'relu', input_shape=(13,)))  
    model.add(Dense(64, activation = 'relu'))  
    model.add(Dense(1))  
    model.compile(optimizer = 'rmsprop', loss = 'mse', metrics=['mae'])  
    return model
```

```
# use 4 folds
```

```
k = 4
```

```
# number of observations per fold
```

```
n = len(Xtrain_scaled)//k
```

round down

```
n
```

Example 4 – K-fold Cross Validation

| fold i | Validation set | Train set | | fold 1 | fold 2 | fold 3 | fold 4 |
|----------|----------------|---------------------|------|-----------|-----------|-----------|-----------|
| 0 | $[0, n)$ | $[n, 4n]$ | 0 | | | | |
| 1 | $[n, 2n)$ | $[0, n), [2n, 4n]$ | n | | | | |
| 2 | $[2n, 3n)$ | $[0, 2n), [3n, 4n]$ | $2n$ | | | | |
| 3 | $[3n, 4n)$ | $[0, 3n)$ | $3n$ | | | | |
| | | | $4n$ | | | | |

Example 4 – K-fold Cross Validation

$n = 101$

```
for i in range(k):  
    print ('processing fold #', i)  
  
    # Select ith fold test set  
    X_val = Xtrain_scaled[i*n:(i+1)*n]  
    y_val = y_train[i*n:(i+1)*n]
```

| fold i | Validation set |
|----------|----------------|
| 0 | $[0, n)$ |
| 1 | $[n, 2n)$ |
| 2 | $[2n, 3n)$ |
| 3 | $[3n, 4n)$ |

Example 4 – K-fold Cross Validation

`n = 101`

```
for i in range(k):
```

```
    # Train ith fold
```

```
    model.fit(X_fold,y_fold, epochs = 50, batch_size = 1,verbose = 0)
```

```
    # Test ith fold
```

```
    mse, mae = model.evaluate(X_val,y_val,verbose = 0)
```

```
    scores.append(mae)
```

Example 4 – K-fold Cross Validation

`n = 101`

```
for i in range(k):
    print ('processing fold #', i)

    # Select ith fold test set
    X_val = Xtrain_scaled[i*n:(i+1)*n]
    y_val = y_train[i*n:(i+1)*n]

    # Create ith fold train set
    X_fold = np.concatenate([Xtrain_scaled[:i*n],
                              Xtrain_scaled[(i+1)*n:]], axis = 0)
    y_fold = np.concatenate([y_train[:i*n],
                              y_train[(i+1)*n:]], axis = 0)
    model = build_model()

    # Train ith fold
    model.fit(X_fold,y_fold, epochs = 50, batch_size = 1,verbose = 0)
    # Test ith fold
    mse, mae = model.evaluate(X_val,y_val,verbose = 0)
    scores.append(mae)
```

Example 4 – K-fold Cross Validation

```
scores
```

```
[2.194908380508423, 2.8107619285583496, 2.281386613845825, 2.33  
918335]
```

```
np.mean(scores)
```

```
2.404637038707733
```

```
# On average we are off by 2404 dollars
```


Example 4 – K-fold Cross Validation

```
all_scores = []
```

modify the for loop to record MAE values after each epoch

```
for i in range(k):
    print ('processing fold #', i)

    # Select ith fold test set
    X_val = Xtrain_scaled[i*n:(i+1)*n]
    y_val = y_train[i*n:(i+1)*n]

    # Create ith fold train set
    X_fold = np.concatenate([Xtrain_scaled[:i*n],
                              Xtrain_scaled[(i+1)*n:]], axis = 0)
    y_fold = np.concatenate([y_train[:i*n],
                              y_train[(i+1)*n:]], axis = 0)

    model = build_model()
    # Train ith fold
    output = model.fit(X_fold, y_fold, validation_data=(X_val, y_val),
                       epochs = 100, batch_size = 1, verbose = 0)
    mae_history = output.history['val_mae']
    all_scores.append(mae_history)
```

Example 4 – Tuning the n. of epochs

```
len(all_scores)
```

4

```
len(all_scores[0])
```

100

a list of 4 lists, each with 100 MAE values

```
array1 = np.vstack(all_scores).T  
array1[:5]
```

```
array([[4.0470109 , 5.44161797, 4.56757212, 4.26246643],  
       [3.16702819, 3.82390976, 3.25191021, 3.51601124],  
       [2.53141928, 3.29371619, 2.86713576, 2.63695264],  
       [3.05941558, 3.74093485, 2.81018758, 2.5811286 ],  
       [2.25084043, 2.91507649, 2.56233144, 2.67849207]])
```

100 x 4

Example 4 – Tuning the n. of epochs

```
cols = range(1,5)
df2 = pd.DataFrame(array1, columns = cols)
df2.columns.name = 'fold'
df2.index.name = 'epoch'
df2
```

| | fold | 1 | 2 | 3 | 4 |
|-------|----------|----------|----------|----------|-----|
| epoch | | | | | |
| 0 | 4.047011 | 5.441618 | 4.567572 | 4.262466 | |
| 1 | 3.167028 | 3.823910 | 3.251910 | 3.516011 | |
| 2 | 2.531419 | 3.293716 | 2.867136 | 2.636953 | |
| 3 | 3.059416 | 3.740935 | 2.810188 | 2.581129 | |
| 4 | 2.250840 | 2.915076 | 2.562331 | 2.678492 | |
| ... | ... | ... | ... | ... | ... |
| 95 | 2.432788 | 2.733259 | 2.579102 | 2.264670 | |
| 96 | 2.847583 | 2.804327 | 2.272040 | 2.197043 | |
| 97 | 3.012051 | 2.857696 | 2.186508 | 2.146194 | |
| 98 | 2.552628 | 2.961175 | 2.283123 | 2.696445 | |
| 99 | 3.035638 | 2.684096 | 2.433445 | 2.279399 | |

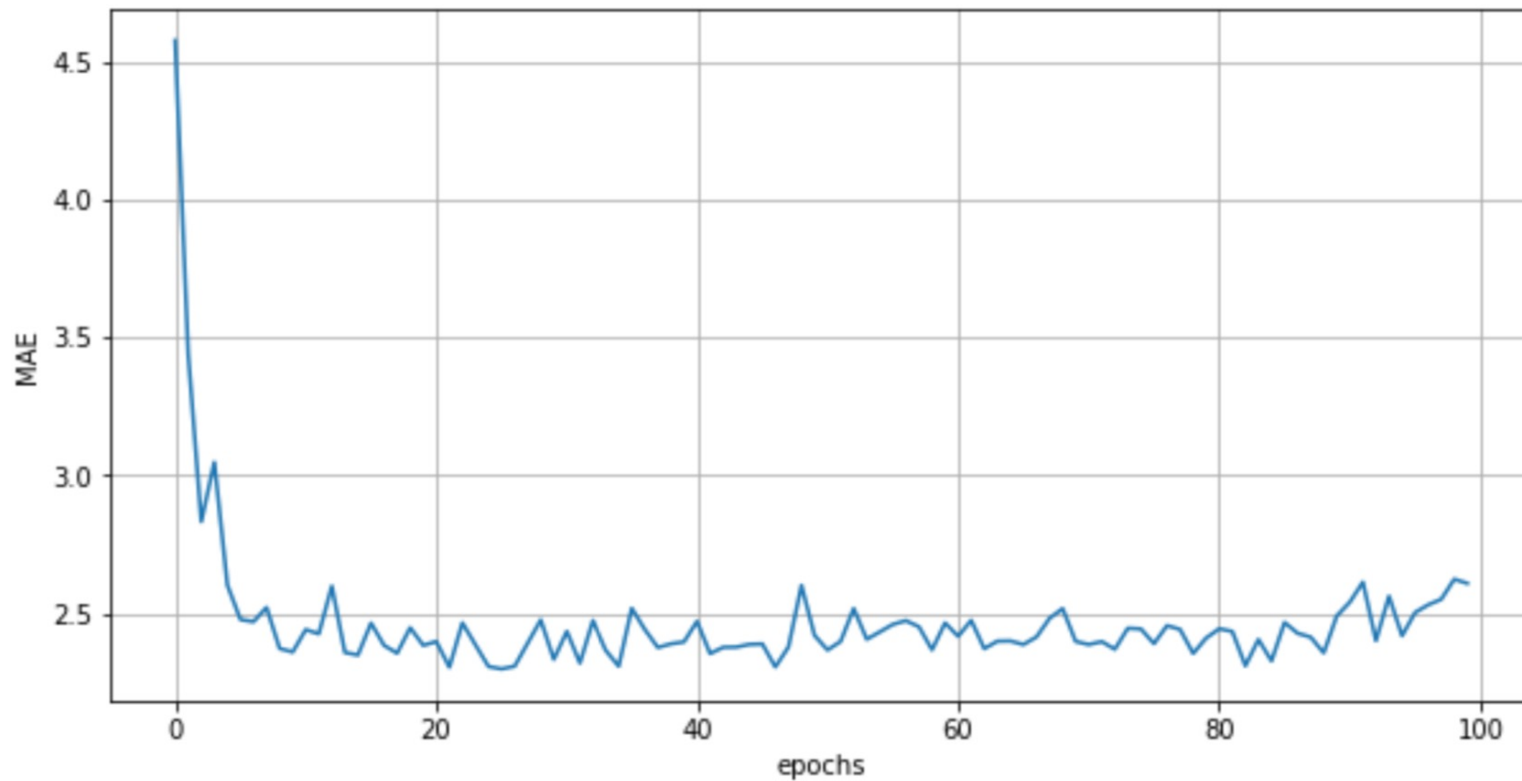
```
df3 = df2.copy()
df3['means'] = df3.mean(axis=1)
df3[:5]
```

| | fold | 1 | 2 | 3 | 4 | row means |
|-------|----------|----------|----------|----------|----------|-----------|
| epoch | | | | | | |
| 0 | 4.047011 | 5.441618 | 4.567572 | 4.262466 | 4.579667 | |
| 1 | 3.167028 | 3.823910 | 3.251910 | 3.516011 | 3.439715 | |
| 2 | 2.531419 | 3.293716 | 2.867136 | 2.636953 | 2.832306 | |
| 3 | 3.059416 | 3.740935 | 2.810188 | 2.581129 | 3.047917 | |
| 4 | 2.250840 | 2.915076 | 2.562331 | 2.678492 | 2.601685 | |

```
means = df3.means
```

Example 4 – Tuning the n. of epochs

```
xaxis = range(100)
plt.figure(figsize=(10,5))
plt.plot(xaxis,means)
plt.xlabel('epochs')
plt.ylabel('MAE')
```



Example 4 – Tuning the n. of epochs

```
means = df3.means
means
```

epoch

| | |
|-----|----------|
| 0 | 4.579667 |
| 1 | 3.439715 |
| 2 | 2.832306 |
| 3 | 3.047917 |
| 4 | 2.601685 |
| ... | |
| 95 | 2.502455 |
| 96 | 2.530248 |
| 97 | 2.550612 |
| 98 | 2.623343 |
| 99 | 2.608145 |

```
mavg[mavg == mavg.min()]
```

epoch

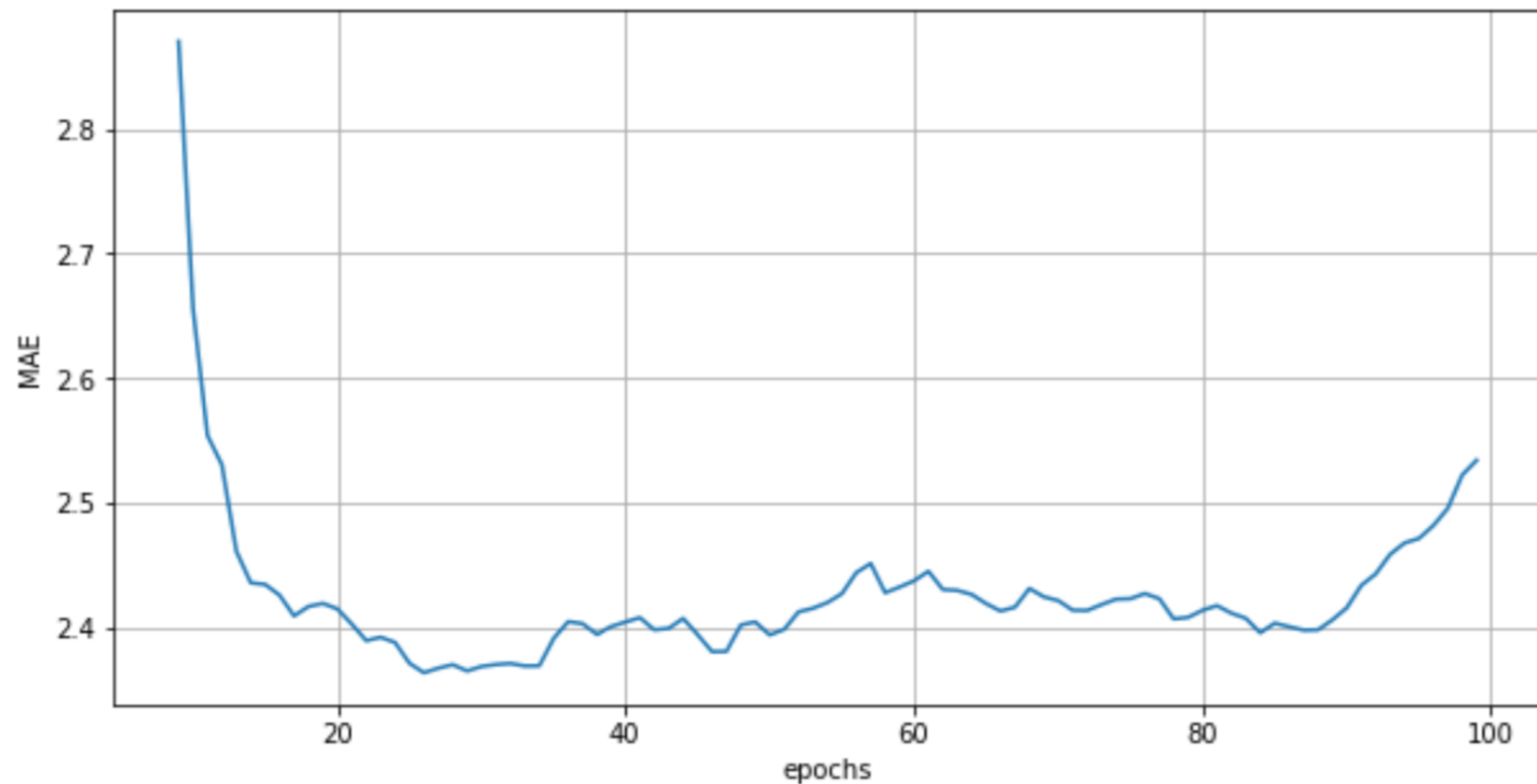
| | |
|----|----------|
| 26 | 2.364716 |
|----|----------|

smallest average MAE
found in epoch 26

Example 4 – Tuning the n. of epochs

```
plt.figure(figsize =(10,5))  
plt.plot(xaxis,mavg)  
plt.xlabel('epochs')  
plt.ylabel('MAE')  
plt.grid()
```

NN starts overfitting after 26 epochs



Example 4 – Tuning the n. of epochs

```
model = Sequential()  
model.add(Dense(64,activation = 'relu', input_shape=(13,)))  
model.add(Dense(64,activation = 'relu'))  
model.add(Dense(1))  
model.compile(optimizer = 'rmsprop', loss = 'mse', metrics=['mae'])  
model.fit(Xtrain_scaled,y_train,epochs = 26, batch_size = 1,verbose = 0);
```

```
mse, mae = model.evaluate(Xtest_scaled,y_test)  
print(mse, ', ', mae)
```

```
102/102 [=====] - 0s 344us/step  
22.878724850860298 , 2.7827768325805664
```

```
# predictions are off by about 2800 dollars
```