

Chapter 4 Homework

4.1 From $S \rightarrow aS \mid bS \mid B$ $S' \rightarrow S$ $S' \rightarrow S \mid \lambda$
 $B \rightarrow bb \mid C \mid \lambda$ $S \rightarrow aS \mid bS \mid B$ $S \rightarrow aS \mid bS \mid a \mid b \mid B$
 $C \rightarrow cC \mid \lambda$ $B \rightarrow bb \mid C \mid \lambda$ $B \rightarrow bb \mid C$
 $C \rightarrow cC \mid \lambda$ $C \rightarrow cC \mid \lambda$ $C \rightarrow cC \mid c$

$$L(G) = (aS \cup bS)^* bb \cup (aS \cup bS)^* c^* = (aS \cup bS)^* (bb \cup c^*)$$

4.3 From $S \rightarrow BSA \mid A$ $S' \rightarrow S$ $S' \rightarrow S \mid \lambda$
 $A \rightarrow aA \mid \lambda$ $S \rightarrow BSA \mid A$ $S \rightarrow BSA \mid SA \mid BS \mid BA \mid S \mid A \mid B$
 $B \rightarrow Bba \mid \lambda$ $A \rightarrow aA \mid \lambda$ $A \rightarrow aA \mid a$
 $B \rightarrow Bba \mid \lambda$ $B \rightarrow Bba \mid \lambda$ $B \rightarrow Bba \mid ba$

$S \rightarrow A: a^+$ $S \rightarrow B: (ba)^+$ $S \rightarrow BA: (ba)^+ a^+$ $S: (a^+ \cup (ba)^+ \cup (ba)^+ a^+)$
 $SA \mid BS: a^+ \cup (ba)^+ S$ $BSA: (ba)^+ a^+$
 $L(G) = ((ba)^+ \cup \lambda) (a^+ \cup (ba)^+ \cup (ba)^+ a^+) (\lambda \cup a^+)$

4.7 From $S \rightarrow AS \mid A$ $S \rightarrow AS \mid aA \mid bB \mid cC \mid b$
 $A \rightarrow aA \mid bB \mid C$ $A \rightarrow aA \mid bB \mid cC \mid b$
 $B \rightarrow bB \mid b$ $B \rightarrow bB \mid b$
 $C \rightarrow cC \mid B$ $C \rightarrow cC \mid bB \mid b$
 $bB = bb^+$ $cC = c^+(bb^+ \cup b) \cup b$ $b = b$
 $aA = a(a^+(bb^+ \cup c^+(bb^+ \cup b) \cup b) \cup b)$ $A^+ = (a^+(bb^+ \cup c^+(bb^+ \cup b) \cup b) \cup b)^+$
 $L(G) = A^+(aA \cup bB \cup cC \cup b) \cup aA \cup bB \cup cC \cup b = (A^+ \cup \lambda)(aA \cup bB \cup cC \cup b)$

4.8 From $S \rightarrow A \mid B \mid C$ $S \rightarrow aa \mid bb \mid cc$
 $A \rightarrow aa \mid B$ $A \rightarrow aa \mid bb \mid cc$
 $B \rightarrow bb \mid C$ $B \rightarrow aa \mid bb \mid cc$
 $C \rightarrow cc \mid A$ $C \rightarrow aa \mid bb \mid cc$

$$L(G) = aa \cup bb \cup cc$$

4.11 From $S \rightarrow S' \rightarrow S \mid \lambda$ $S' \rightarrow aS \mid bS \mid a \mid b \mid bb \mid cC \mid c \mid \lambda$
 $S \rightarrow aS \mid bS \mid a \mid b \mid B$ $S \rightarrow aS \mid bS \mid a \mid b \mid bb \mid cC \mid c$
 $B \rightarrow bb \mid C$ $B \rightarrow bb \mid cC \mid c$
 $C \rightarrow cC \mid c$ $C \rightarrow cC \mid c$

$$L(G) = (aS \cup bS)^* bb \cup (aS \cup bS)^* c^* = (aS \cup bS)^* (bb \cup c^*)$$

4.14 From $S \rightarrow AA \mid CD \mid bB$ $S_T \rightarrow AA$ $S_U \rightarrow AA$
 $A \rightarrow aA \mid a$ $A \rightarrow aA \mid a$ $A \rightarrow aA \mid a$
 $B \rightarrow bB \mid bC$ $D \rightarrow dD \mid d$
 $C \rightarrow cB$
 $D \rightarrow dD \mid d$
 $L(G) = aa^+$

4.16 From $S \rightarrow ACH \mid BB$ $S_T \rightarrow BB$ $S_U \rightarrow BB$
 $A \rightarrow aA \mid aF$ $A \rightarrow aA \mid aF$ $B \rightarrow b$
 $B \rightarrow CFH \mid b$ $B \rightarrow b$
 $C \rightarrow aC \mid DH$ $F \rightarrow bB \mid b$
 $D \rightarrow aD \mid BD \mid Ca$ $H \rightarrow dH \mid d$
 $F \rightarrow bB \mid b$
 $H \rightarrow dH \mid d$

$$L(G) = bb$$

4.17 From $S \rightarrow A \mid CB$ $S \rightarrow cC \mid c \mid dD \mid d \mid CB$
 $A \rightarrow C \mid D$ $A \rightarrow cC \mid c \mid dD \mid d$
 $B \rightarrow bB \mid b$ $B \rightarrow bB \mid b$
 $C \rightarrow cC \mid c$ $C \rightarrow cC \mid c$
 $D \rightarrow dD \mid d$ $D \rightarrow dD \mid d$

$$V = TERM = \{B, C, D, S, A\} = REACH = \{S, A, C, B, D\}$$

From $S \rightarrow cC \mid c \mid dD \mid d \mid CB$ $S_T \rightarrow cC \mid c \mid dD \mid d \mid CB$ $S_U \rightarrow cC \mid c \mid dD \mid d \mid CB$
 $A \rightarrow cC \mid c \mid dD \mid d$ $A \rightarrow cC \mid c \mid dD \mid d$ $B \rightarrow bB \mid b$
 $B \rightarrow bB \mid b$ $B \rightarrow bB \mid b$ $C \rightarrow cC \mid c$
 $C \rightarrow cC \mid c$ $C \rightarrow cC \mid c$ $D \rightarrow dD \mid d$
 $D \rightarrow dD \mid d$ $D \rightarrow dD \mid d$

4.19 From $S \rightarrow aAbB \mid ABC \mid a$ $S \rightarrow A'T_1 \mid AT_2 \mid a$
 $A \rightarrow aA \mid a$ $T_1 \rightarrow AT_3$
 $B \rightarrow bBcC \mid b$ $T_2 \rightarrow BC$
 $C \rightarrow abc$ $T_3 \rightarrow B'B$
 $A \rightarrow A'A \mid a$
 $B \rightarrow B'T_4 \mid b$
 $T_4 \rightarrow BT_5$
 $T_5 \rightarrow C'C$
 $T_6 \rightarrow A'T_7$
 $T_7 \rightarrow B'C'$
 $A' \rightarrow a'$
 $B' \rightarrow b'$
 $C' \rightarrow c'$

4.26 From $S \rightarrow AX \mid AY \mid a$

$X \rightarrow AX \mid a$

$Y \rightarrow BY \mid a$

$A \rightarrow a$

$B \rightarrow b$

CYK for string **abaaa**

Derivation	Rule
$S \Rightarrow AY$	$S \rightarrow AY$
$\Rightarrow aY$	$A \rightarrow a$
$\Rightarrow aBY$	$Y \rightarrow BY$
$\Rightarrow abY$	$B \rightarrow b$
$\Rightarrow aba$	$Y \rightarrow a$

X_{11} {S, X, Y, A}	X_{12} Φ	X_{13} {S}	X_{14} Φ	X_{15} Φ
a	X_{22} {B}	X_{23} {Y}	X_{24} Φ	X_{25} Φ
	b	X_{33} {S, X, Y, A}	X_{34} {S, X}	X_{35} {S, X}
		a	X_{44} {S, X, Y, A}	X_{45} {S, X}
			a	X_{55} {S, X, Y, A}
				a

27 Construct an equivalent grammar with leftmost derivations removed

$S \rightarrow A \mid B$

$A \rightarrow aaB \mid Aab \mid Aba$

$B \rightarrow bB \mid Bb \mid aba$

$S' \rightarrow A \mid B$

$A \rightarrow aaBY \mid aaB$

$Y \rightarrow abY \mid baY \mid ab \mid ba$

$B \rightarrow bB \mid abaZ \mid aba$

$Z \rightarrow bZ \mid b$

$B = aba \cup abab^+ \cup b^+aba \cup b^+abab^+$

$aaB = aa(aba \cup abab^+ \cup b^+aba \cup b^+abab^+)$

$aaBY = aa(aba \cup abab^+ \cup b^+aba \cup b^+abab^+)(ab \cup ba)^+$

4.28 From $S \rightarrow A \mid C$

$A \rightarrow AaB \mid AaC \mid B \mid a$

$B \rightarrow Bb \mid Cb$

$C \rightarrow cC \mid c$

$S \rightarrow A \mid C$

$A \rightarrow BY \mid aY \mid B \mid a$

$Y \rightarrow aBY \mid aCY \mid aB \mid aC$

$B \rightarrow CbZ \mid Cb$

$Z \rightarrow bZ \mid b$

$C \rightarrow cC \mid c$

Leftmost derivation for string **aaccacb**

Derivation	Rule
$S \Rightarrow A$	$S \rightarrow A$
$\Rightarrow aY$	$A \rightarrow aY$
$\Rightarrow aaCY$	$Y \rightarrow aCY$
$\Rightarrow aaccY$	$C \rightarrow cC$
$\Rightarrow aaccaY$	$C \rightarrow c$
$\Rightarrow aaccaB$	$Y \rightarrow aB$
$\Rightarrow aaccaCb$	$B \rightarrow Cb$
$\Rightarrow aaccacb$	$C \rightarrow c$