

# Time Series Analysis: Citibike NYC

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Stat 715: Professor Dana Sylvan

May 13, 2019





# OUTLINE

## ◎ INTRODUCTION

1. History

2. Data

3. Plot Time Series/Transformations/Auto Correlation Structure

## ◎ METHODS

1. Model Specification

2. Model Fitting

3. Model Diagnostics

4. Forecasting

## ◎ CONCLUSION

# INTRODUCTION: HISTORY

**1967** Amsterdam: Witte Fietse



**1995** Copenhagen: Bycyklen

**1996** Portsmouth UK: Bikeabout

**2007** Paris, France: Vélib & Barcelona, Spain: Bicing



**2008** Washington DC: SmartBike DC

**2013** NYC: Citibike  
Launches w/ 6000 bikes  
in Manhattan and BK

**2019** As of Feb, Citibike has:  
+750 stations  
+62K rides/day  
+12K bikes

Total revenue for month~\$4.7 mill

# INTRODUCTION: HISTORY

## Why are Bike Sharing Systems Beneficial?

### © Environmental

1. In Shanghai (2018), bike sharing systems cut down CO2 by 25,240 tons. A number big enough to consider as a component when meeting China's Paris Accord greenhouse emissions requirements

### © Economic

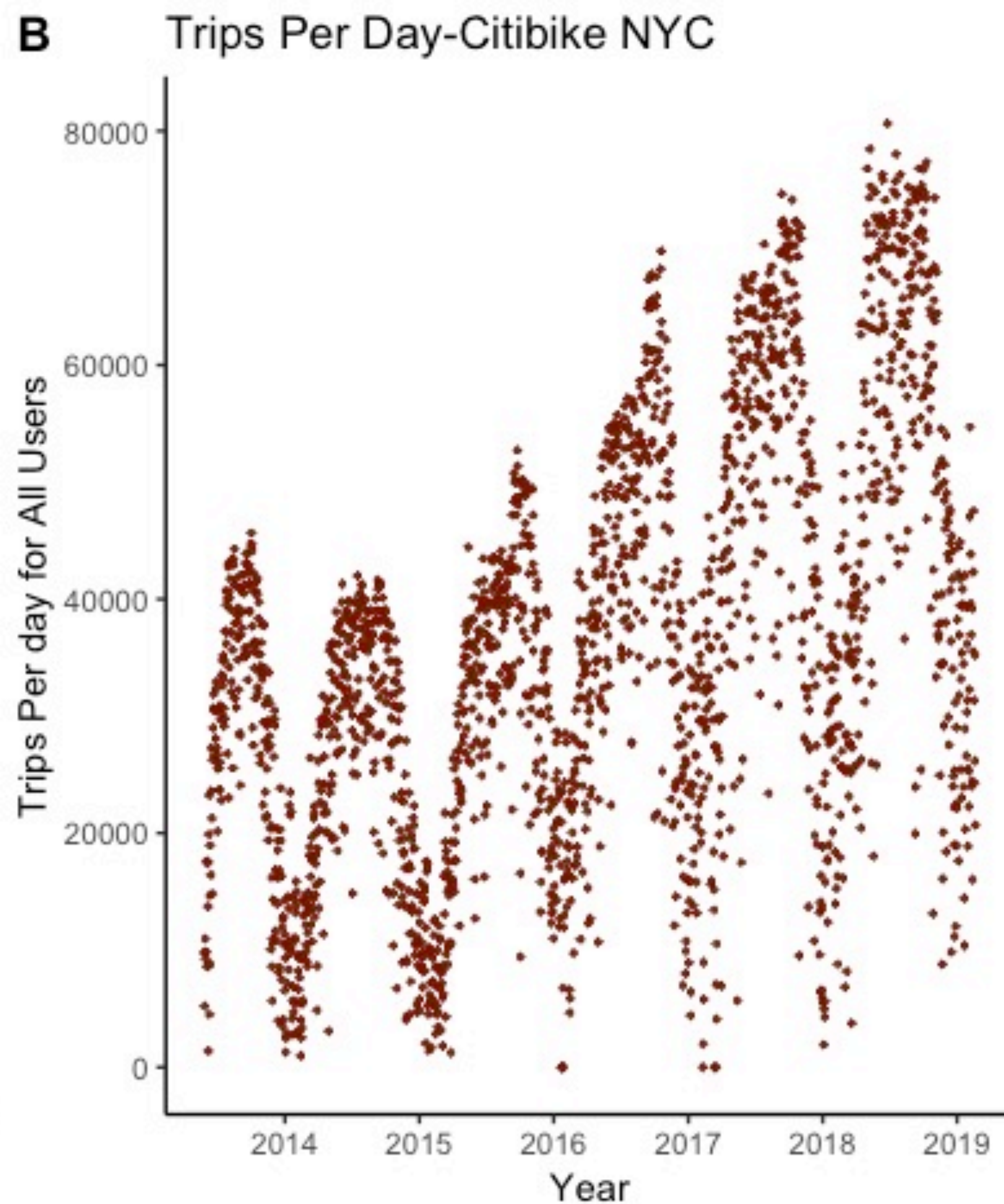
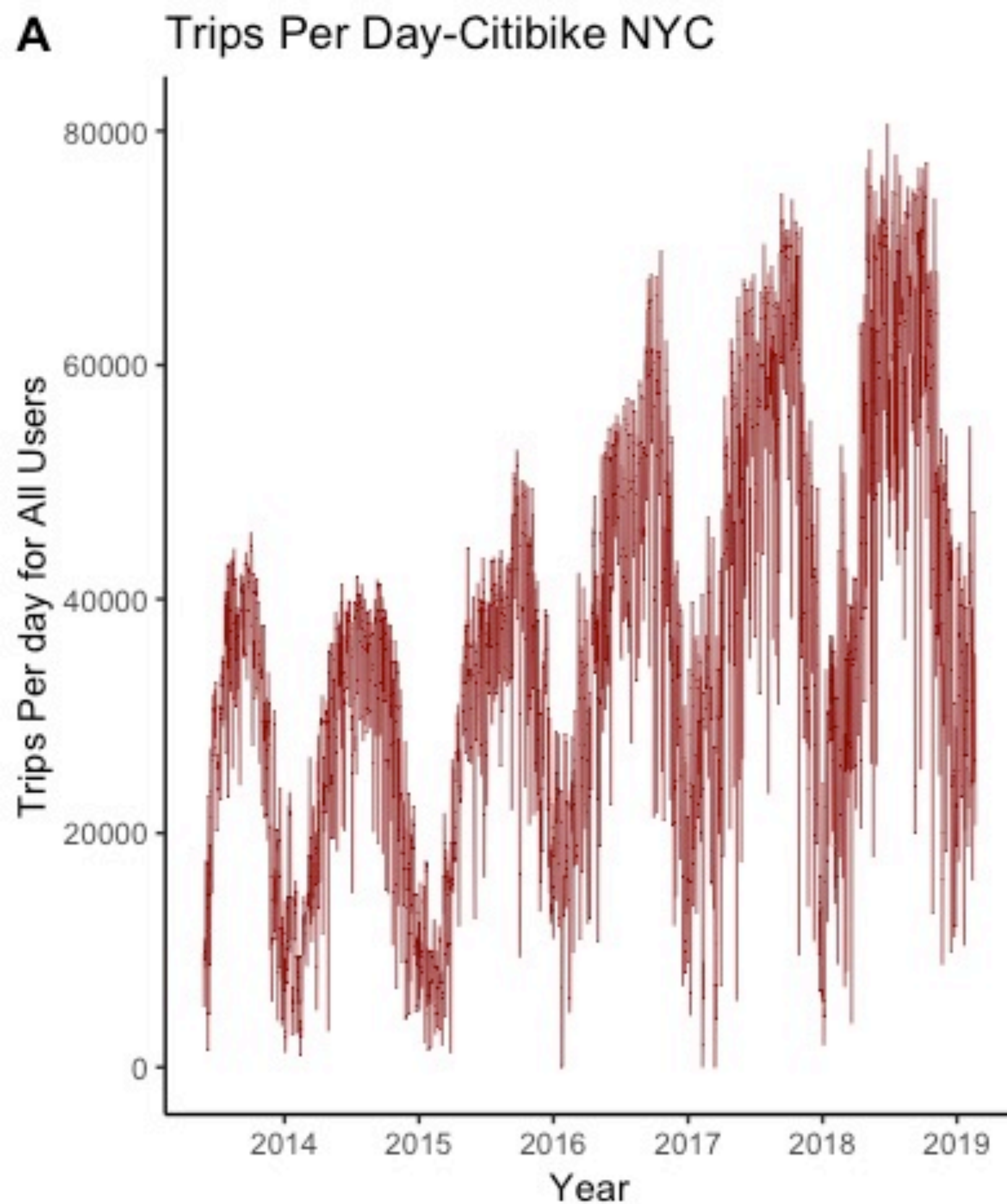
2. If all Bike Sharing trips replaced car trips in 12 major cities in Europe, 73.25 deaths could be avoided each year (225 million Euros saving)

# INTRODUCTION: DATA

- ◎ Online Citibike System Data Repository
- ◎ Python: Cleaning, wrangling and exploratory analysis
- ◎ R: Statical application
- ◎ 2096 observations from 05/27/2013-02/15/2019
  - \* "Date" "Trips\_per\_24hrs"
- ◎ Hypothesis
  - \*  $H_0$  = Trips per day (for All Users) increase in the summer months



# INTRODUCTION: PLOT TS



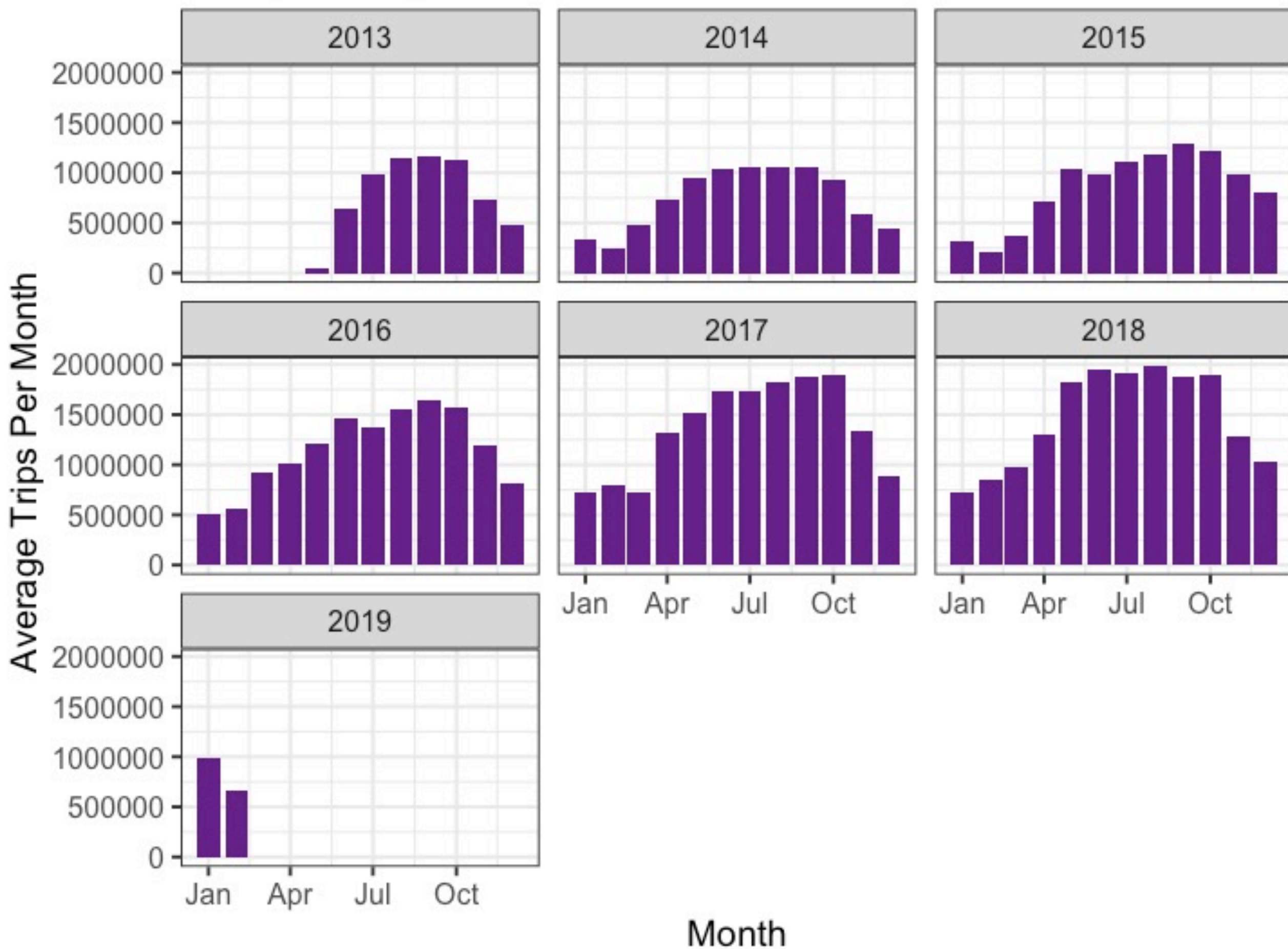


# INTRODUCTION: PLOT TS

C

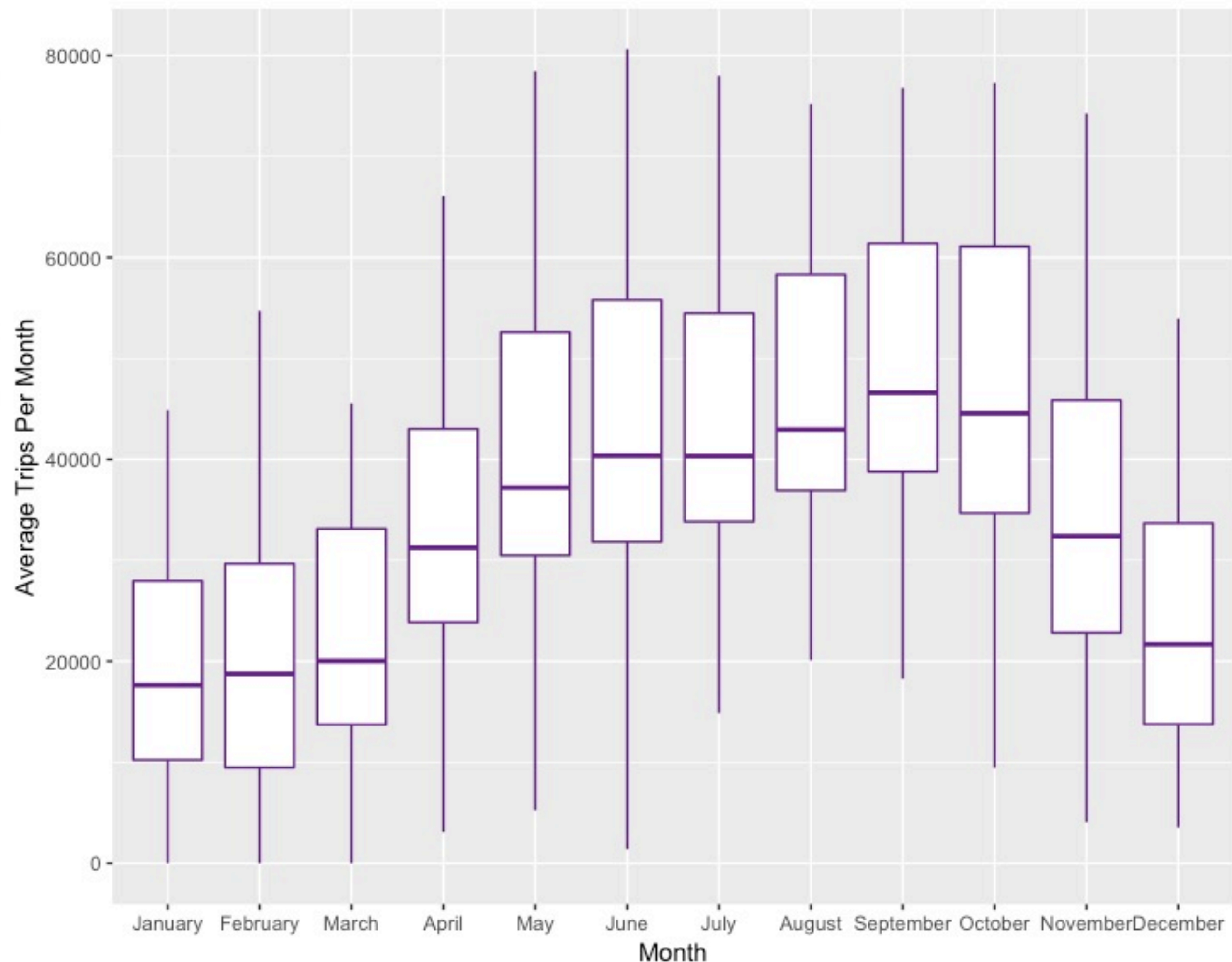
Average Trips Per Month- Citibike NYC

Data plotted by month



D

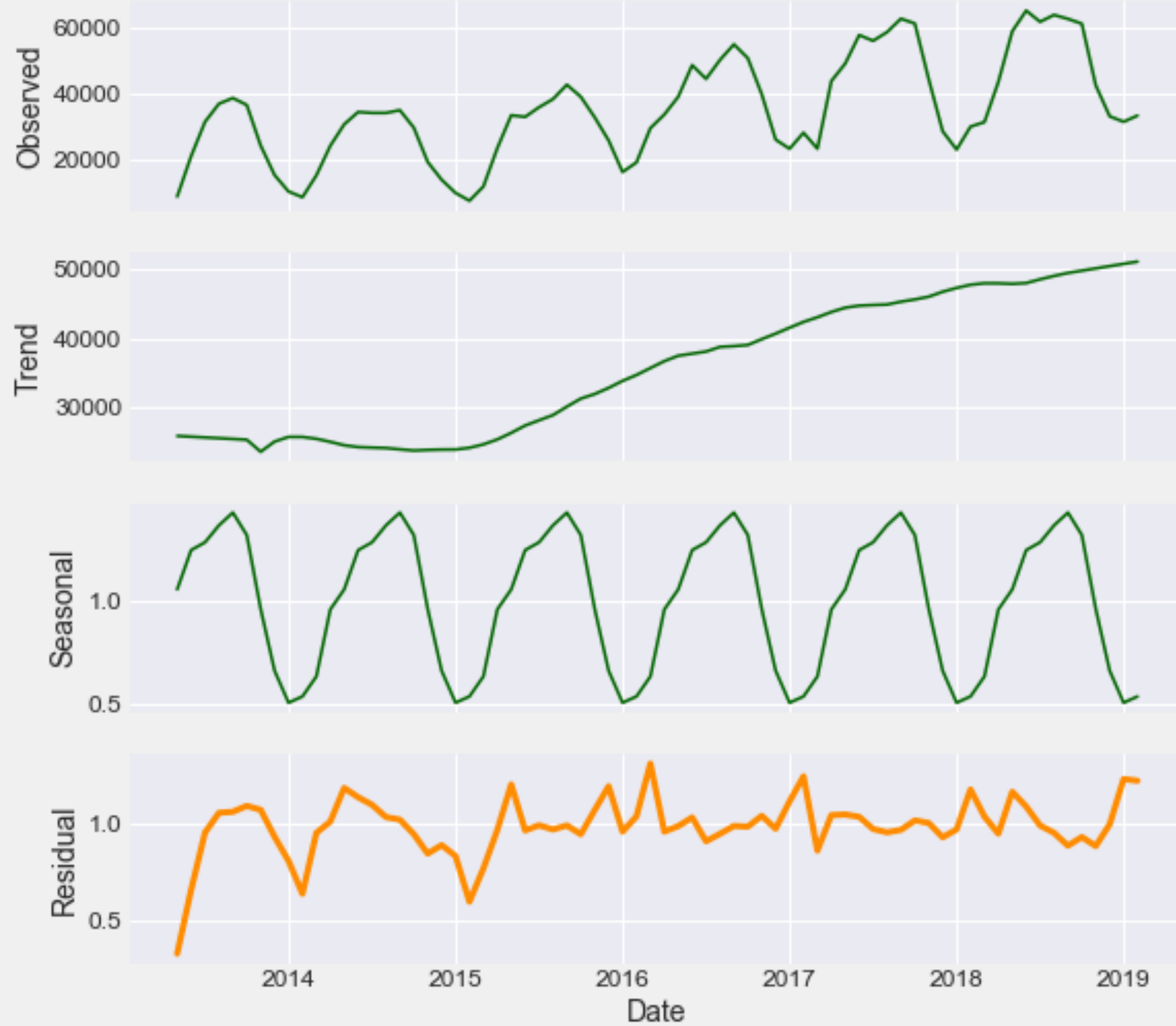
Average Trips Per Month-Citibike NYC



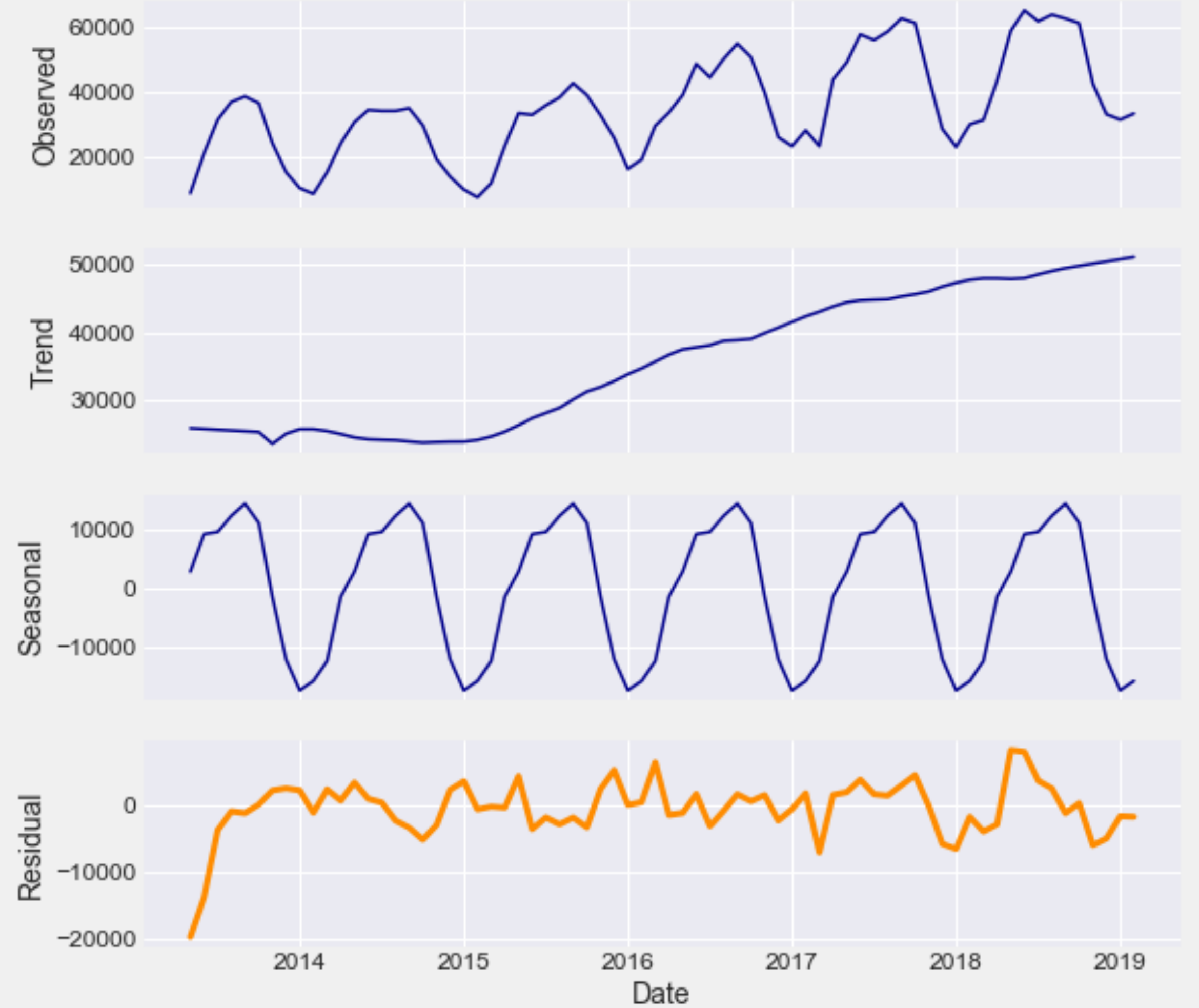
# INTRODUCTION: PLOT TS

E

Multiplicative Decomposition Plots for Average Daily Trips



Additive Decomposition Plots for Average Daily Trips

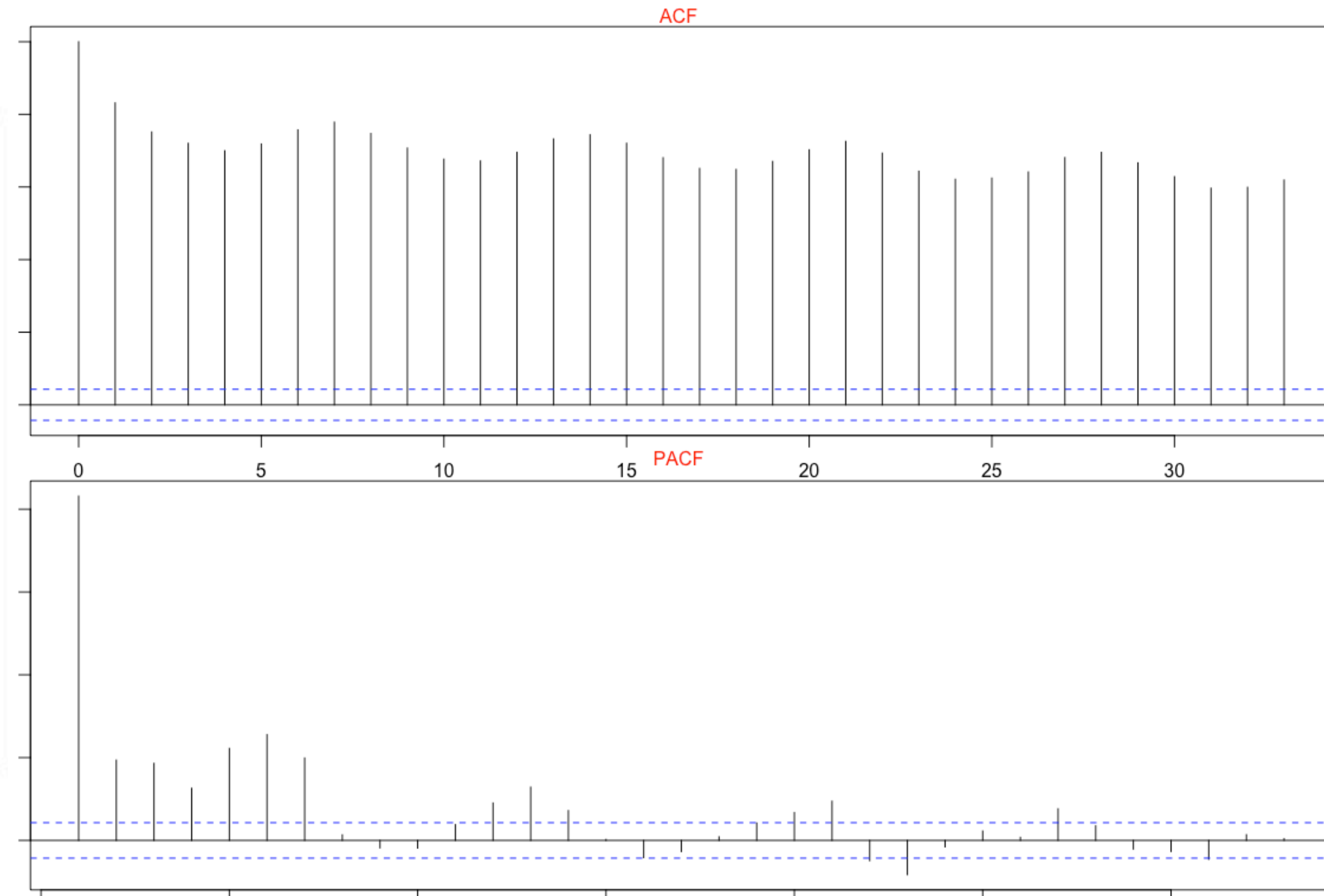
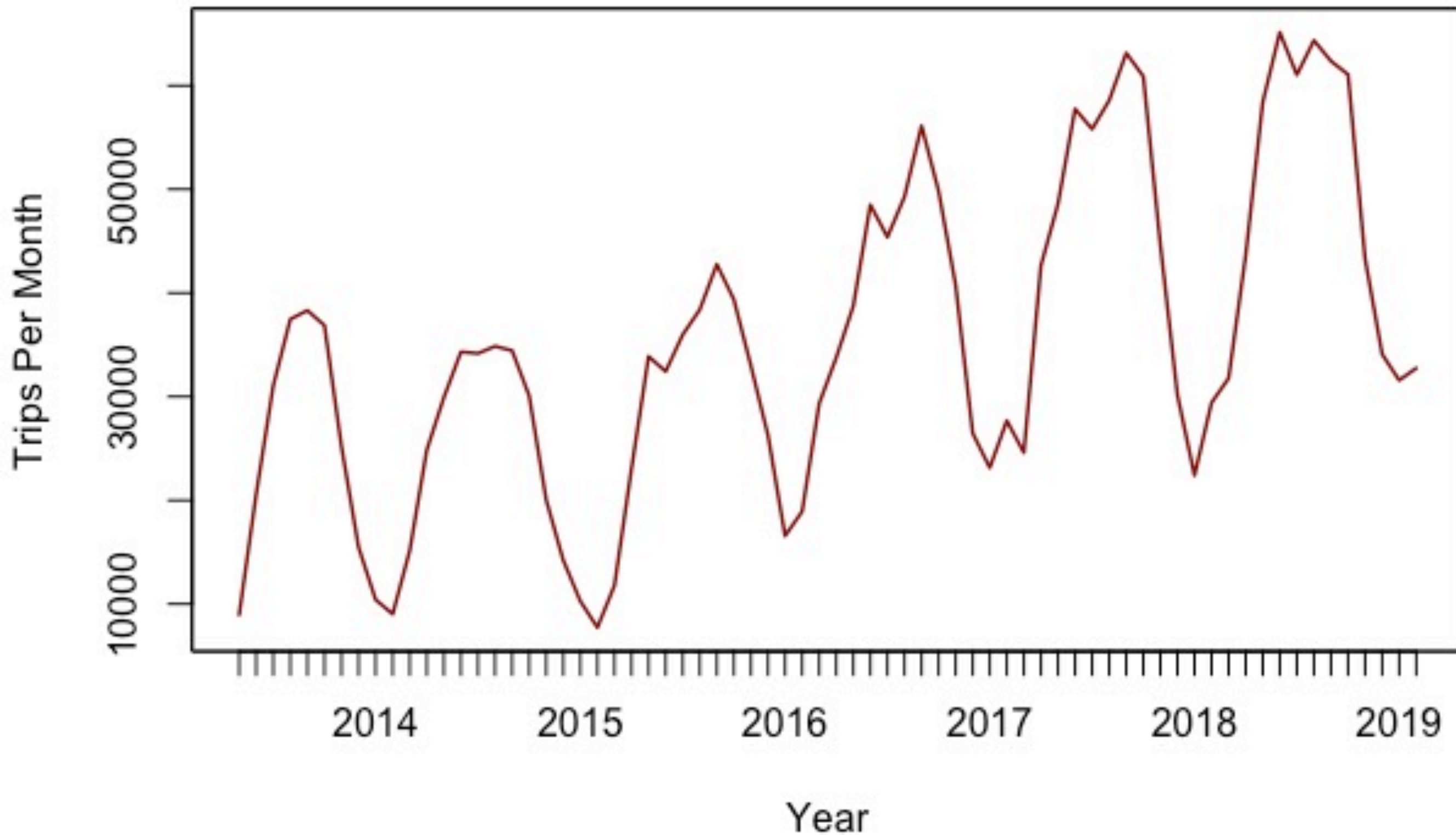




# INTRODUCTION: PLOT TS

F

Average Trips Per Month



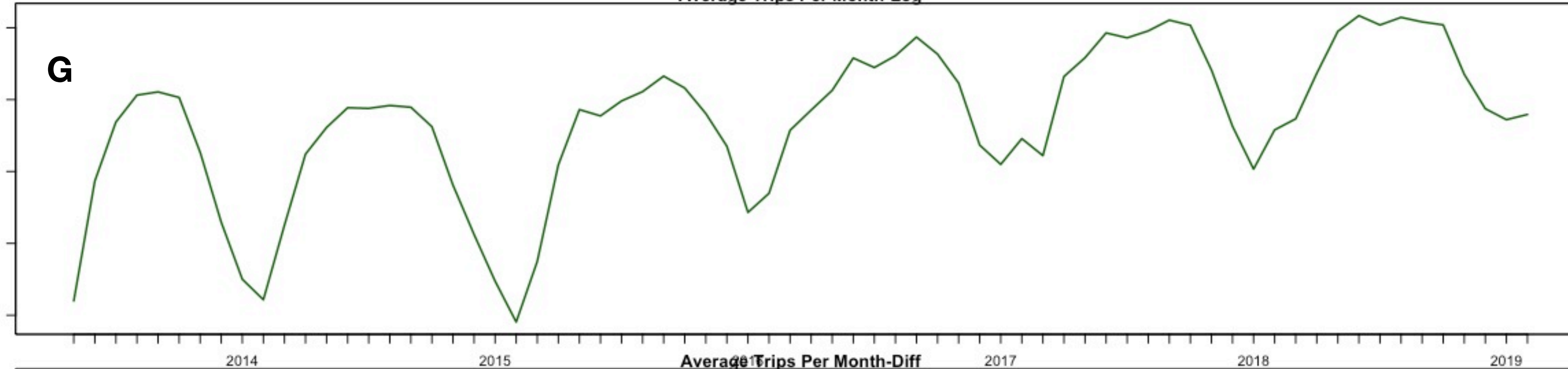
Augmented Dickey-Fuller Test

```
data: z
Dickey-Fuller = -3.2223, Lag order = 12, p-value = 0.08406
alternative hypothesis: stationary
```

# INTRODUCTION: TRANSFORMATIONS

G

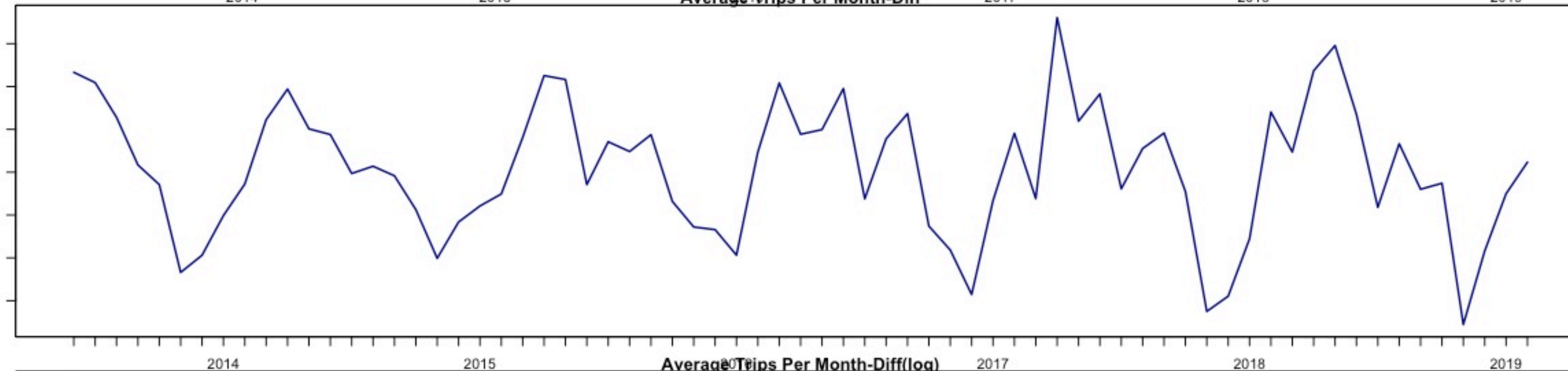
Average Trips Per Month-Log



Augmented Dickey-Fuller Test

```
data: df_trips.mo.log
Dickey-Fuller = -5.4888, Lag order = 4, p-value = 0.01
alternative hypothesis: stationary
```

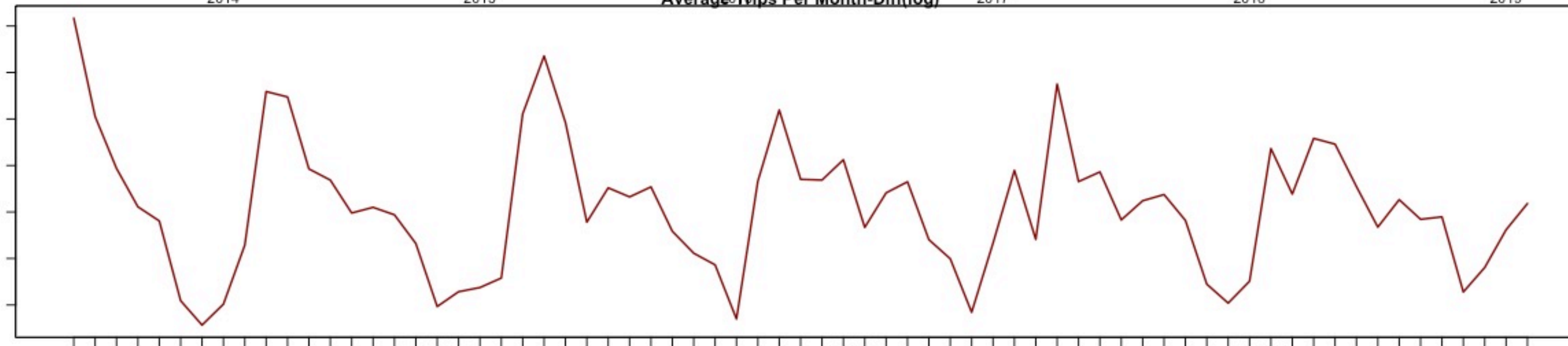
Average Trips Per Month-Diff



Augmented Dickey-Fuller Test

```
data: df_trips.mo.diff
Dickey-Fuller = -5.731, Lag order = 4, p-value = 0.01
alternative hypothesis: stationary
```

Average Trips Per Month-Diff(log)



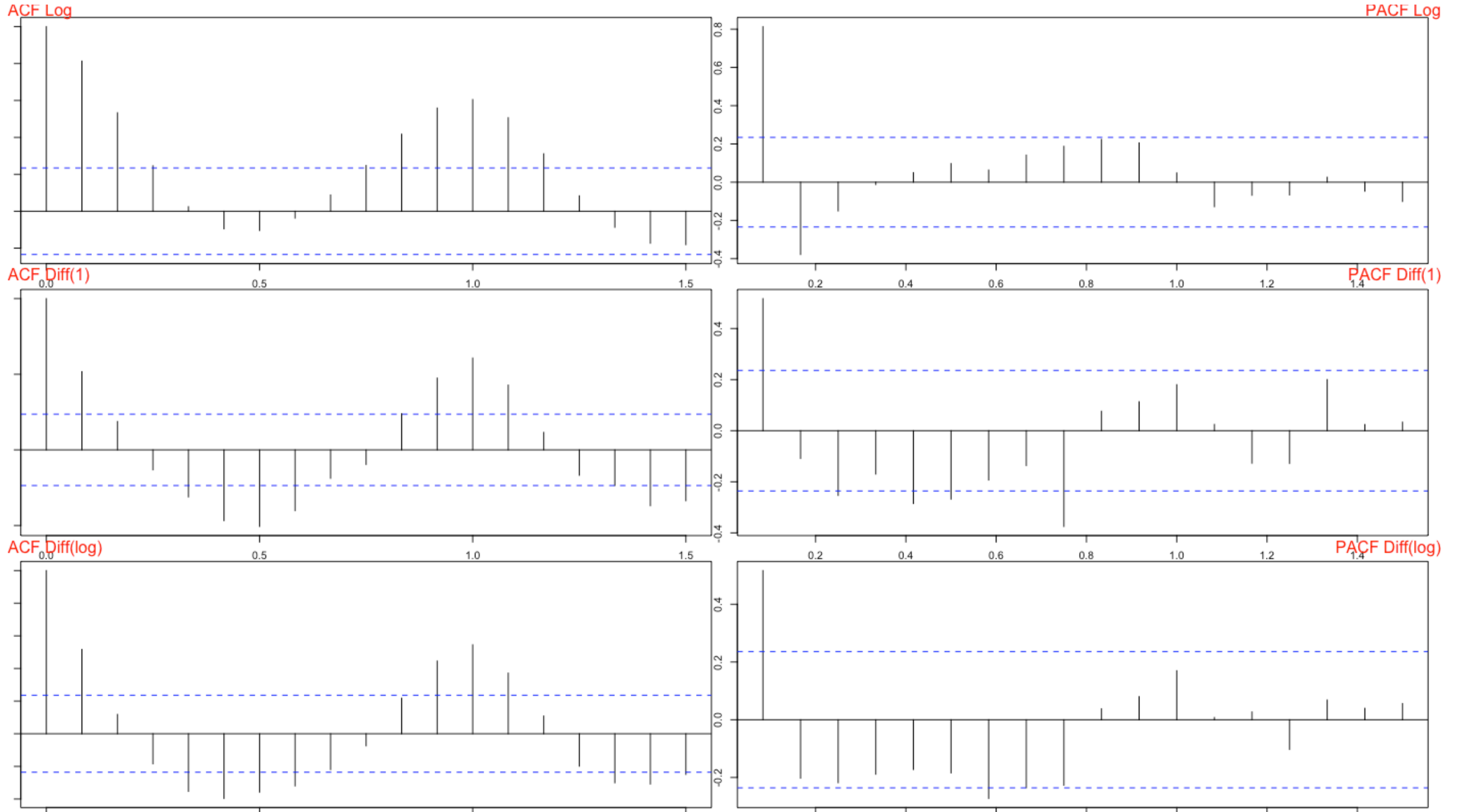
Augmented Dickey-Fuller Test

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data: df_trips.mo.diff_log
Dickey-Fuller = -5.345, Lag order = 4, p-value = 0.01
alternative hypothesis: stationary
```



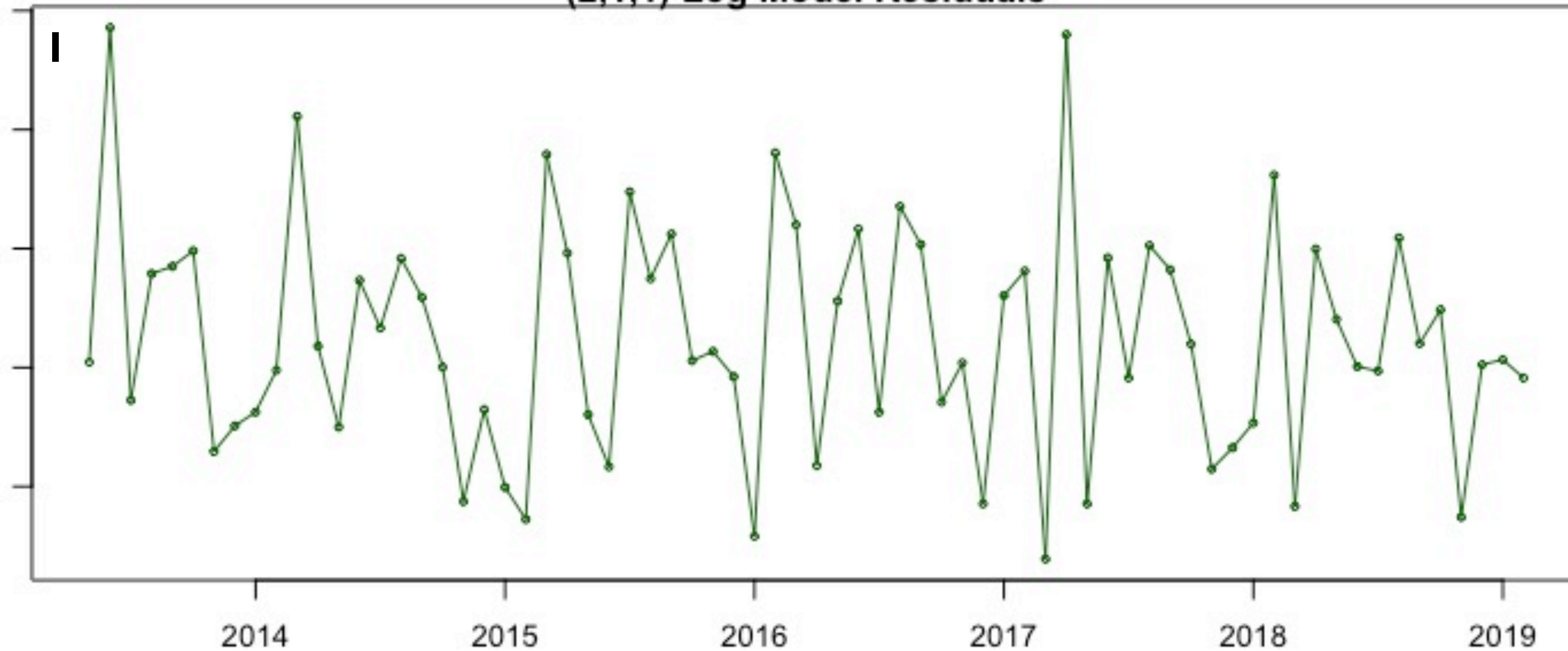
# INTRODUCTION: ACF STRUCTURES

H



# METHODS: MODEL SPECIFICATION

(2,1,1) Log Model Residuals

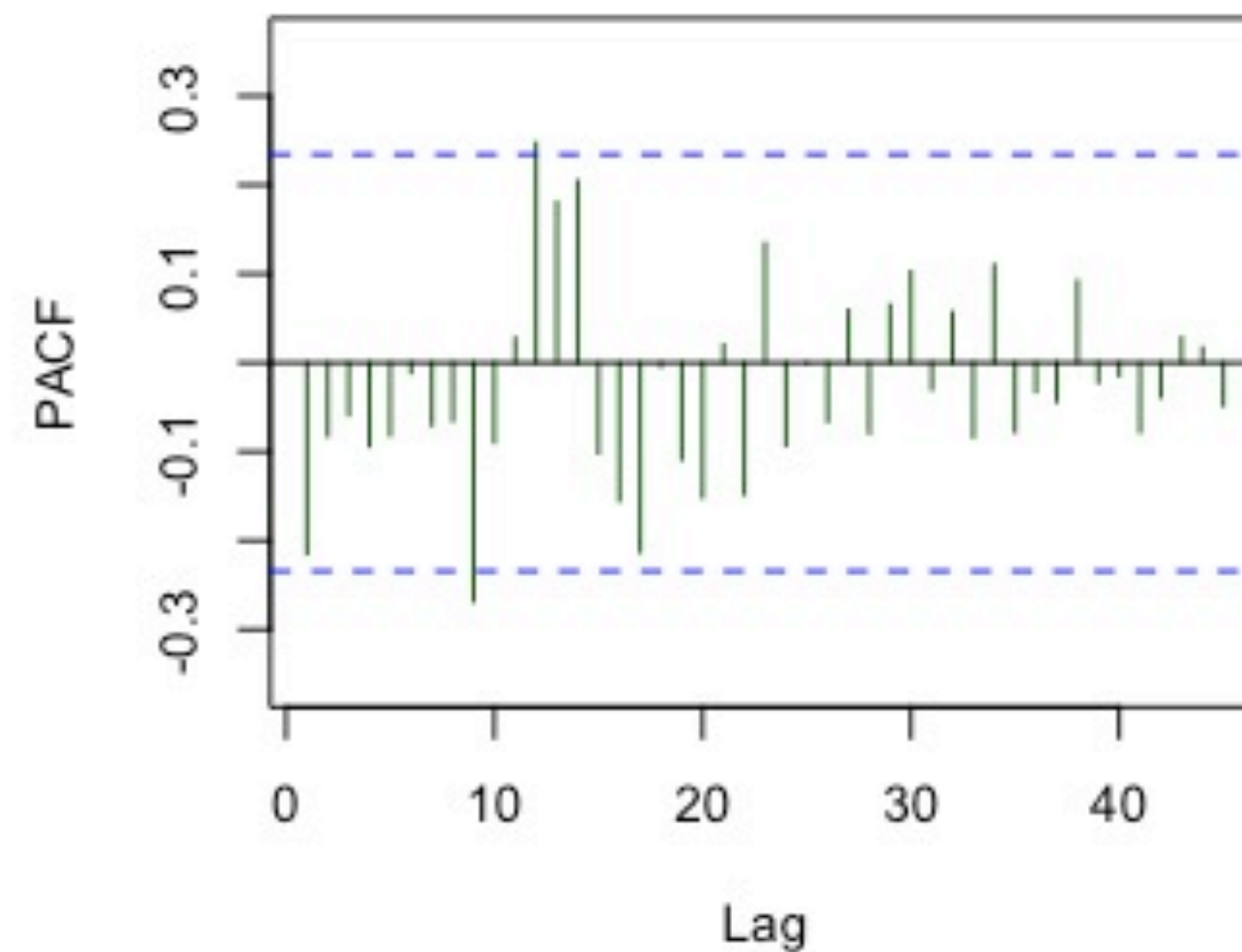
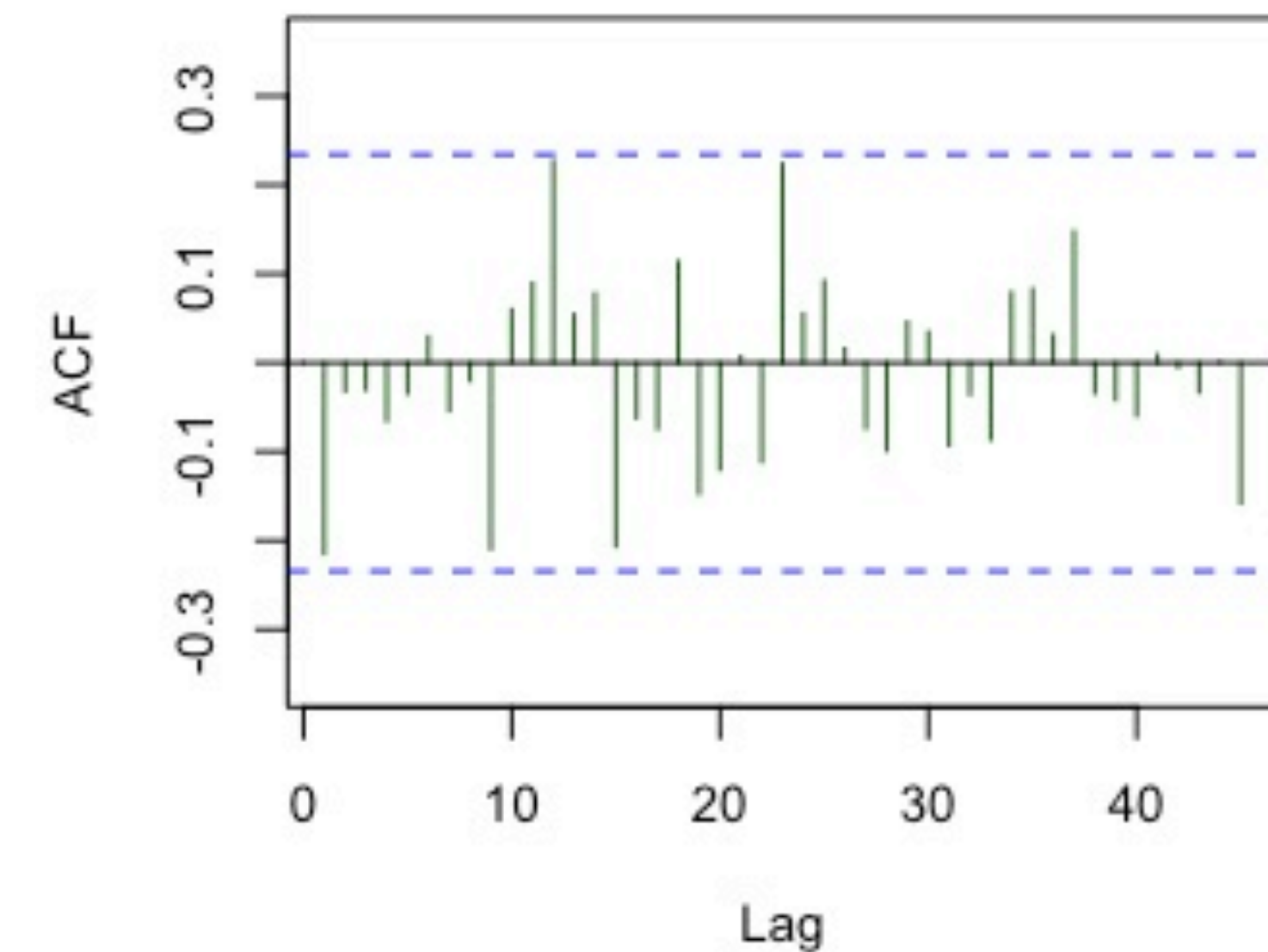


Series: df\_trips.mo.log  
ARIMA(2,1,1)

Coefficients:

	ar1	ar2	ma1
	1.3995	-0.7231	-0.8854
s.e.	0.0920	0.0890	0.0488

sigma<sup>2</sup> estimated as 0.04215: log likelihood=11.94  
AIC=-15.88 AICc=-15.26 BIC=-6.94



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Training set error measures:

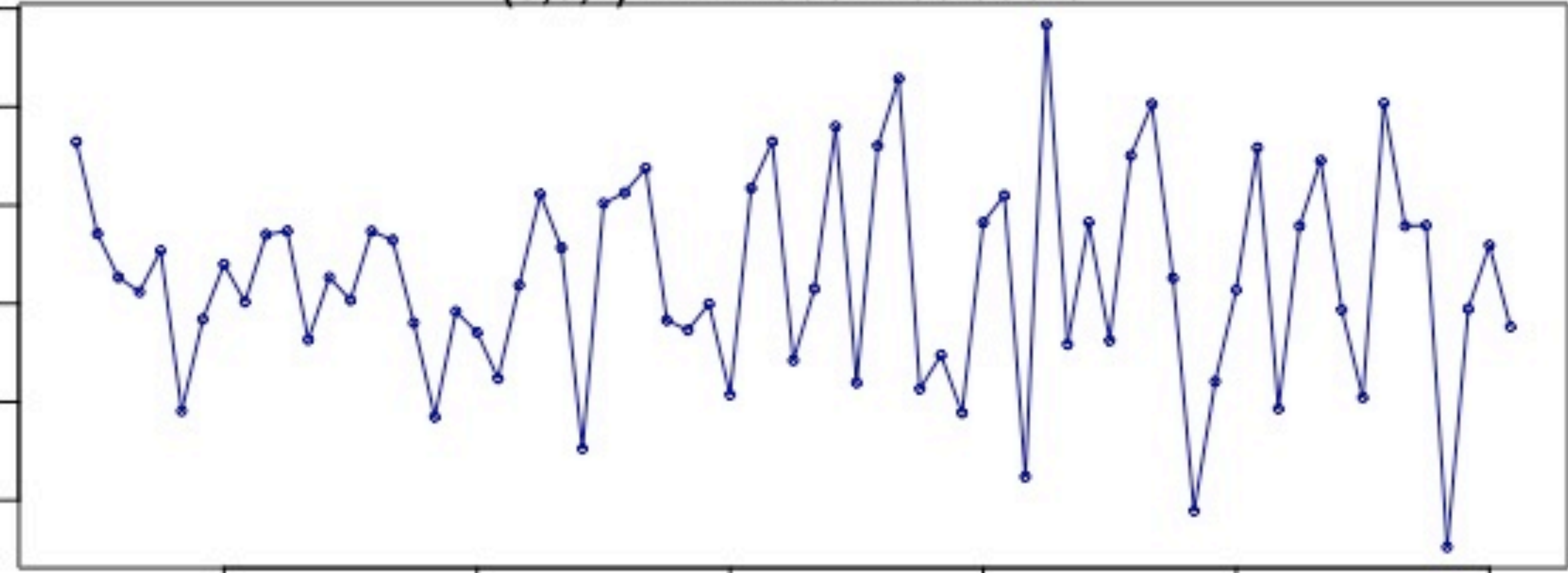
	ME	RMSE	MAE	MPE	MAPE	MASE	ACF
Training set	0.04874772	0.1993619	0.1565437	0.454322	1.523958	0.6844499	-0.214706



# METHODS: MODEL SPECIFICATION

J

(3,0,1) Diff Model Residuals



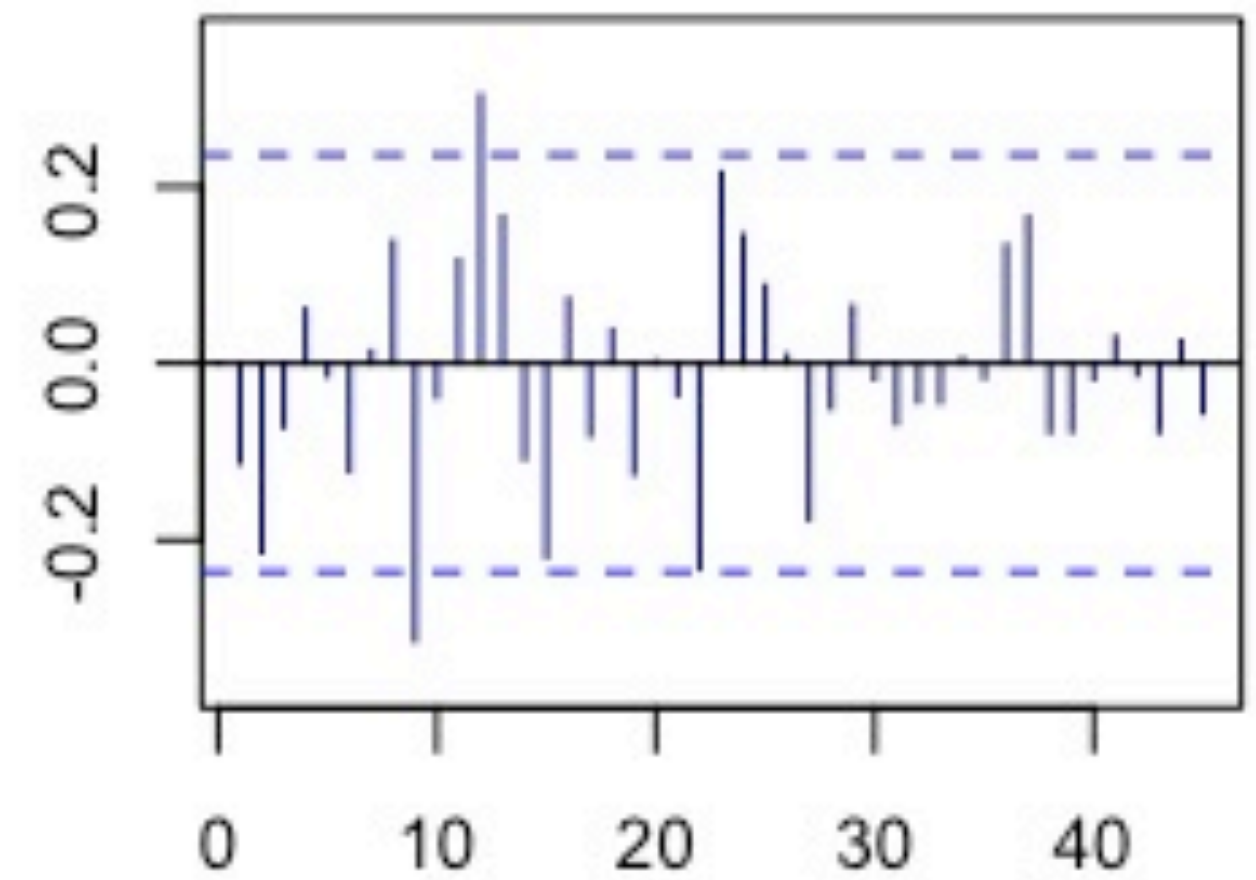
Series: df\_trips.mo.diff  
ARIMA(3,0,1) with zero mean

Coefficients:

	ar1	ar2	ar3	ma1
	1.1520	-0.2535	-0.3063	-0.8573
s.e.	0.1197	0.1801	0.1191	0.0520

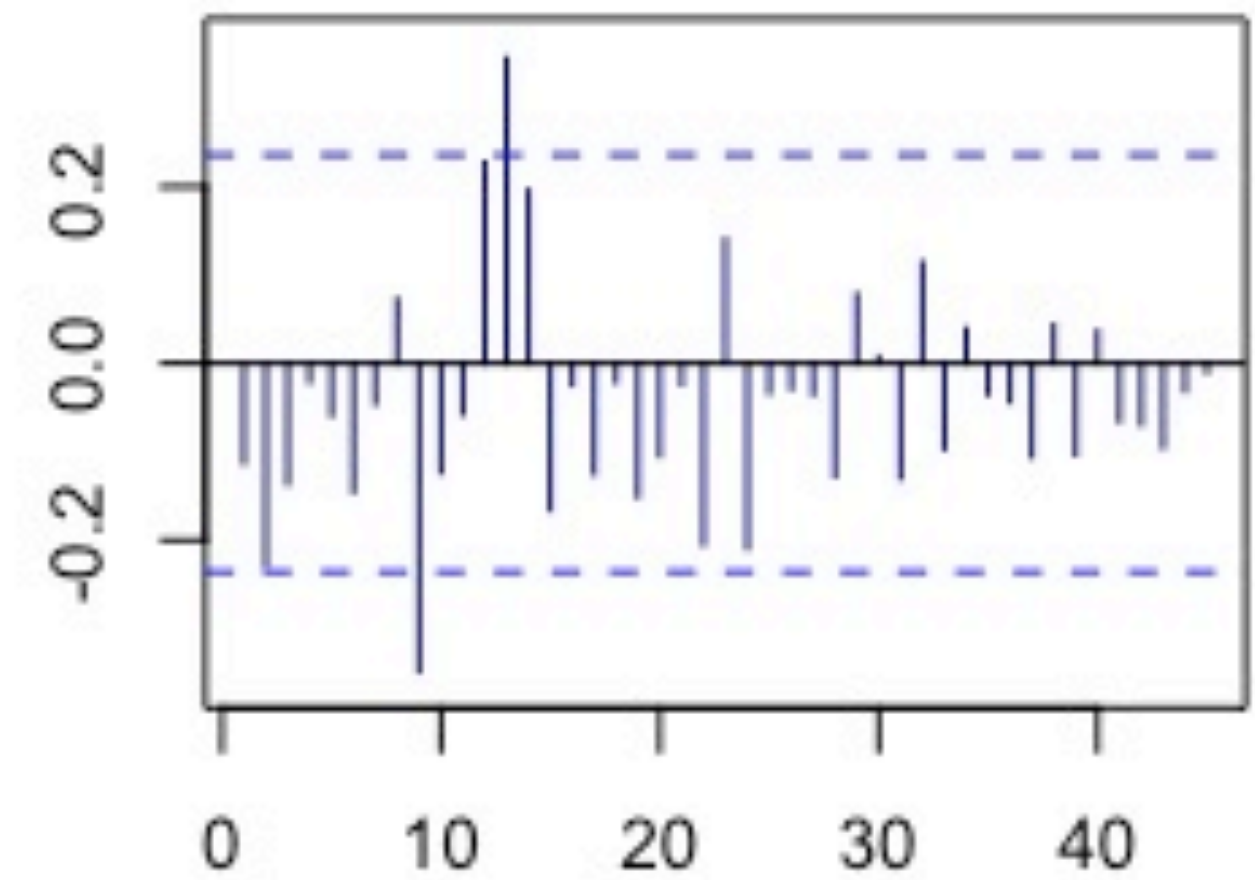
sigma^2 estimated as 31277961: log likelihood=-692.27  
AIC=1394.54 AICc=1395.5 BIC=1405.71

ACF



Lag

PACF



Lag

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sigma^2 estimated as 31277961: log likelihood=-692.27  
AIC=1394.54 AICc=1395.5 BIC=1405.71

Training set error measures:

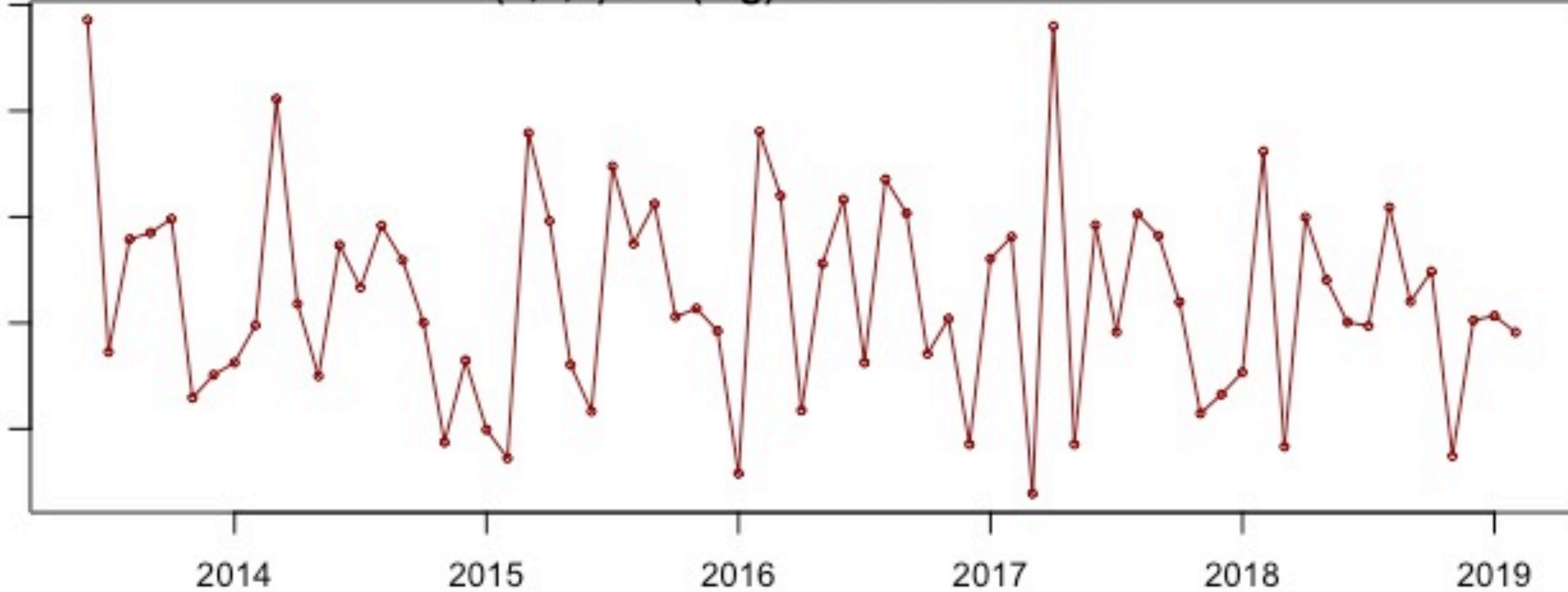
	ME	RMSE	MAE	MPE	MAPE	MASE	ACF1
Training set	1250.249	5428.144	4315.528	43.436	112.9727	1.014973	-0.1126688



# METHODS: MODEL SPECIFICATION

K

(2,0,1) Diff(log) Model Residuals

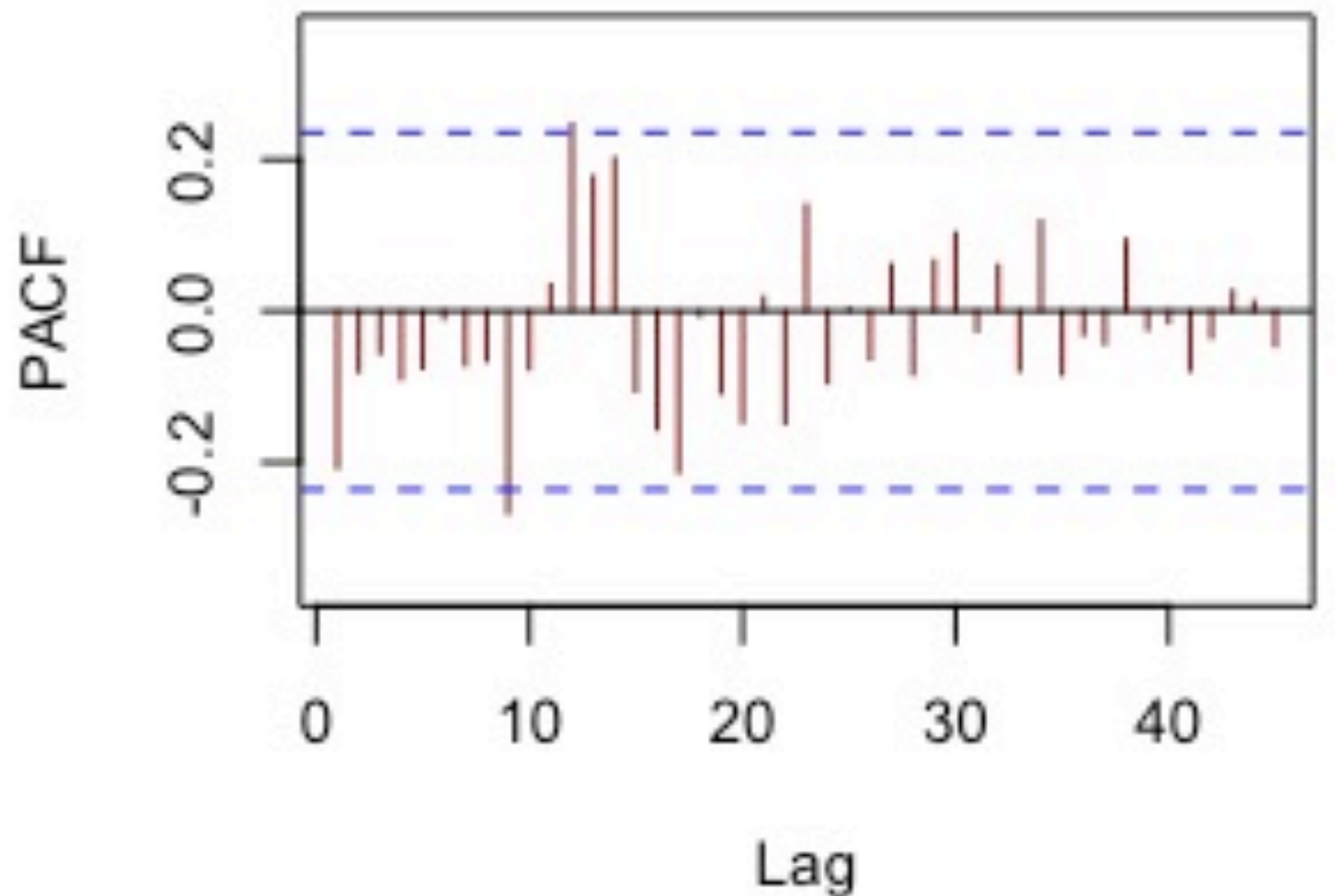
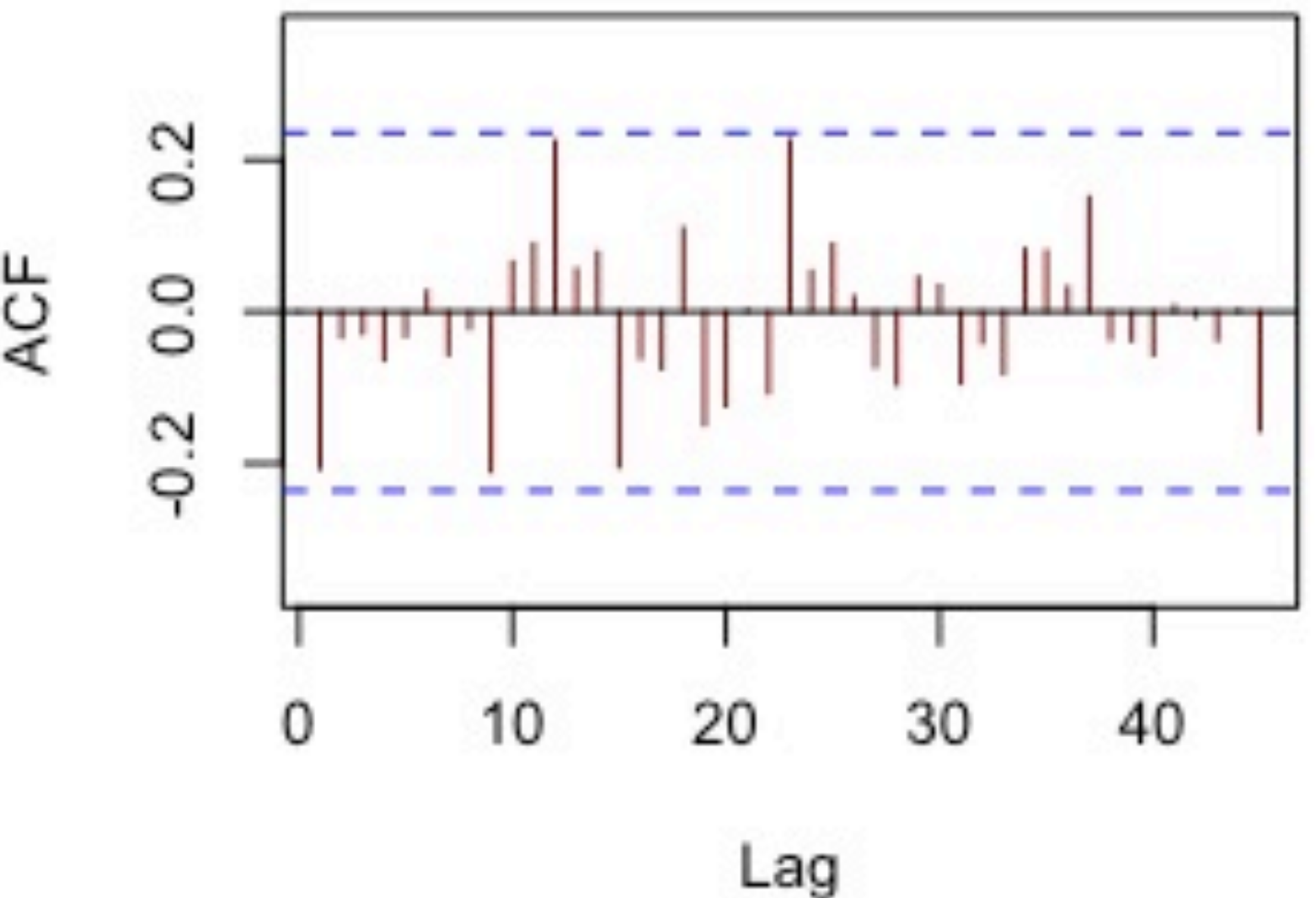


Series: df\_trips.mo.diff\_log  
ARIMA(2,0,1) with zero mean

Coefficients:

	ar1	ar2	ma1
	1.3995	-0.7231	-0.8854
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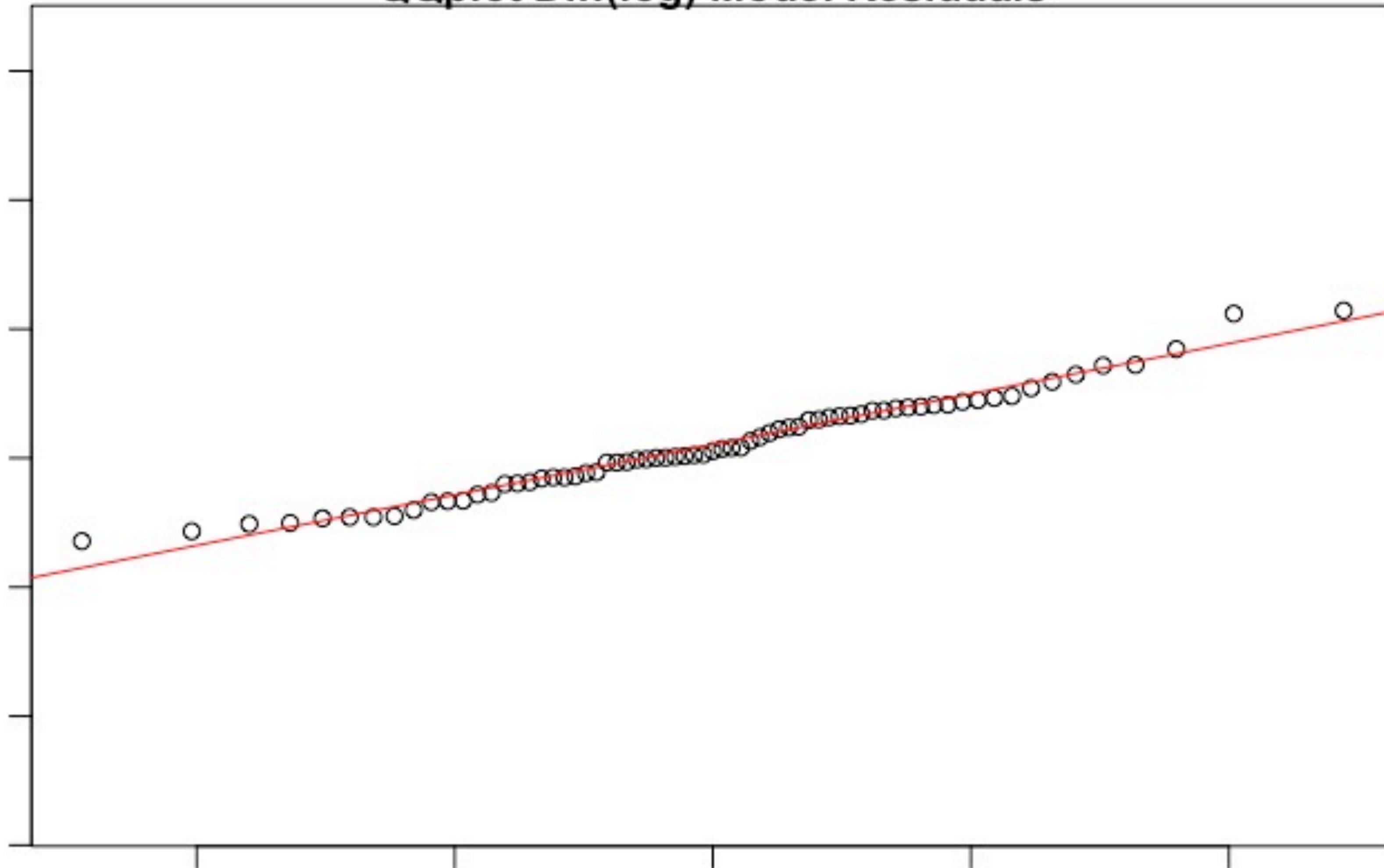
Training set error measures:

	ME	RMSE	MAE	MPE	MAPE	MASE	ACF
Training set	0.04932225	0.2007986	0.1586807	33.86179	166.8318	1.043891	-0.206810



# METHODS: MODEL DIAGNOSTICS

QQplot Diff(log) Model Residuals



Ljung-Box test

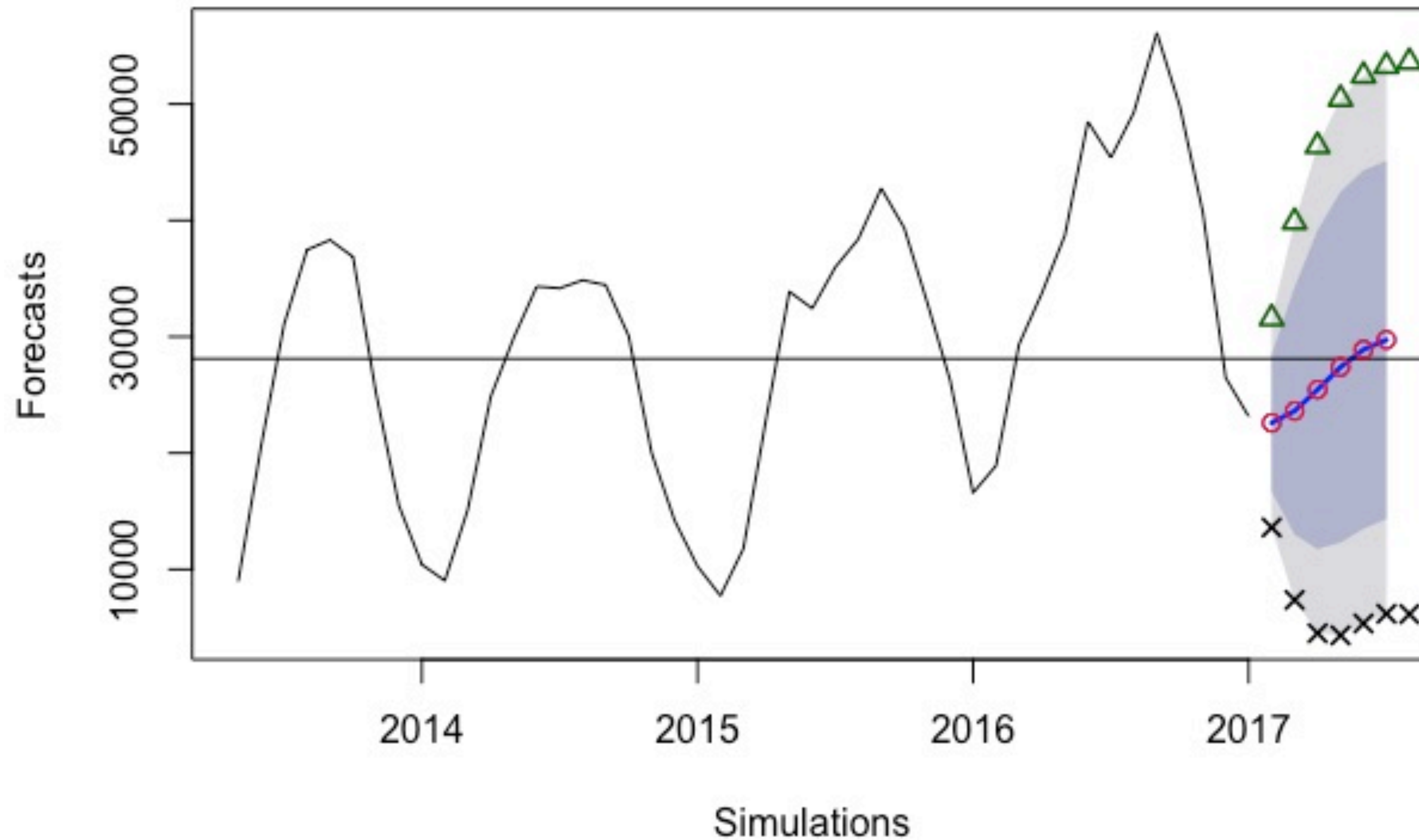
data: Residuals from ARIMA(2,0,1) with zero mean  
 $Q^* = 13.77$ ,  $df = 11$ ,  $p\text{-value} = 0.246$

Model df: 3. Total lags used: 14

# METHODS: FORECASTING

M

Forecasts for Simulated AR(2,0,1)





# CONCLUSION

- ◎ Trips per Day is a Seasonal TS
- ◎ AR(2,0,1) of Diff(log) was best model
  1. Best ACF/PACF plots
  2. Lowest RMSE
- ◎ Forecast of Trips per Day confirmed proper selection of model
  - ◎ Test values found in lower and upper 95%

# REFERENCES

1. “The Real Story Behind the Global Bike-Share Boom.” CityLab, [www.citylab.com/city-makers-connections/bike-share/](http://www.citylab.com/city-makers-connections/bike-share/).
2. Motivate International, Inc. “Citi Bike System Data.” *Citi Bike NYC*, [www.citibikenyc.com/system-data](http://www.citibikenyc.com/system-data).
3. Zhang, Yongping, and Zhifu Mi. “Environmental Benefits of Bike Sharing: A Big Data-Based Analysis.” *Applied Energy*, vol. 220, 2018, pp. 296–301., doi:10.1016/j.apenergy.2018.03.101.
4. Otero, I., et al. “Health Impacts of Bike Sharing Systems in Europe.” *Environment International*, vol. 115, 2018, pp. 387–394., doi:10.1016/j.envint.2018.04.014.
5. Motivate International, Inc. “Citi Bike System Data.” *Citi Bike NYC*, [www.citibikenyc.com/system-data](http://www.citibikenyc.com/system-data).
6. Citibike Image: “Lined up Rental Citibank Bikes in Lower Manhattan. New York , NY , USA -.” *Shutterstock.com*, 2 Oct. 2018, [www.shutterstock.com/image-photo/lined-rental-citibank-bikes-lower-manhattan-1192959820](http://www.shutterstock.com/image-photo/lined-rental-citibank-bikes-lower-manhattan-1192959820).