Choose the **best** model!

Test if the model is correct!

(model checking)

Choose the best model!

Test if the model is correct!

(model checking)

Existing methods can say:

"If the model is true it produces such data extremely rarely."

Or

"If the model is true it produces such data extremely rarely."

Choose the **best** model!

What is best?

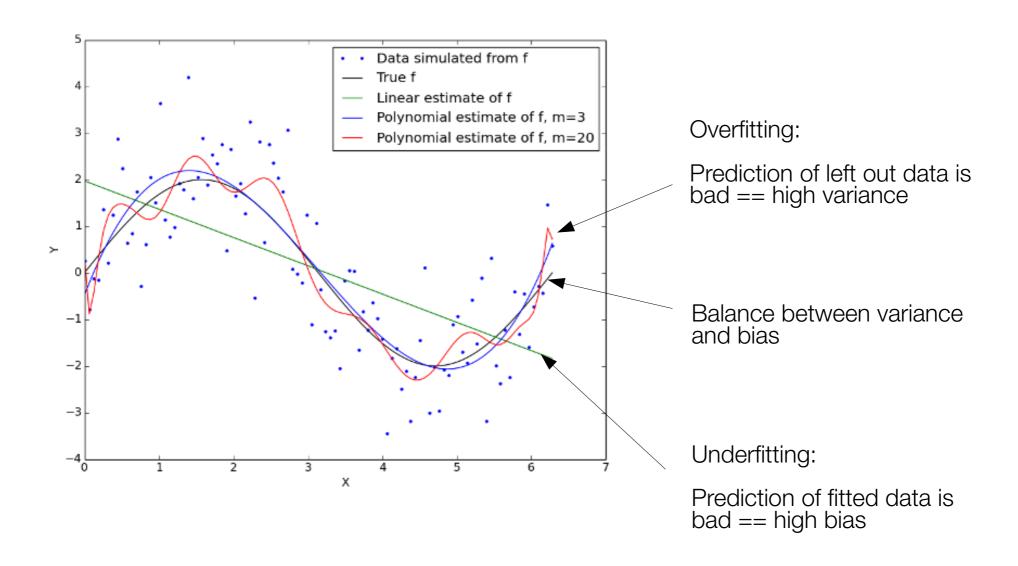
- If it fits the data!

Create a model that equals the data

→ fits perfectly

different styles of model comparison

Bias-variance trade-off



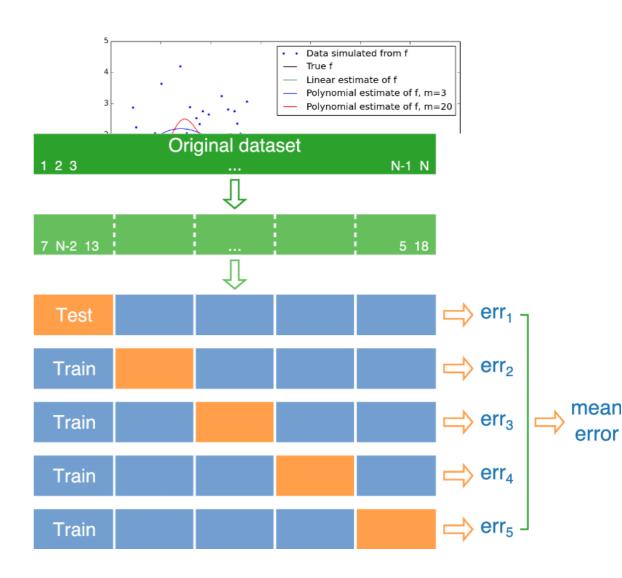
Empirical models

- Polynomials, splines, ...
- Capture effective behaviour
- Prediction quality of left-out data

K-folding Boot-strapping

leave-one-out, LOO Jackknife

Problem-dependent how to split



Common in machine learning!

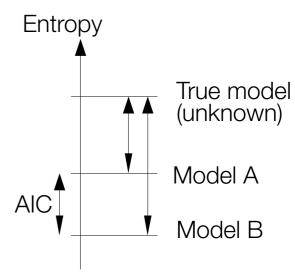
Best = predicts unseen data from the same pool of data

Information theory

- Store data into the fitted model
- Measure entropy, loss of information
- KL divergence between model result and true model
- Akaike information criterion:

Beware: derived in the limit of high-data

Best = retains information in the data



Variations

DIC: Deviance information criterion "effective" number of parameters

AICc: correction for few

<u>WAIC</u>: uses the likelihood contribution from each data point

Effect size

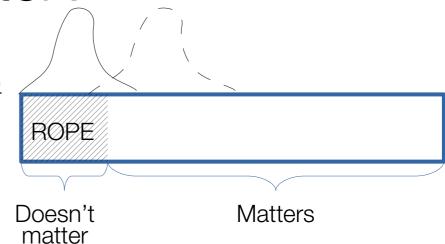
 Model B = Model A + some effect (e.g., a line, process)

Does the effect matter?

Define

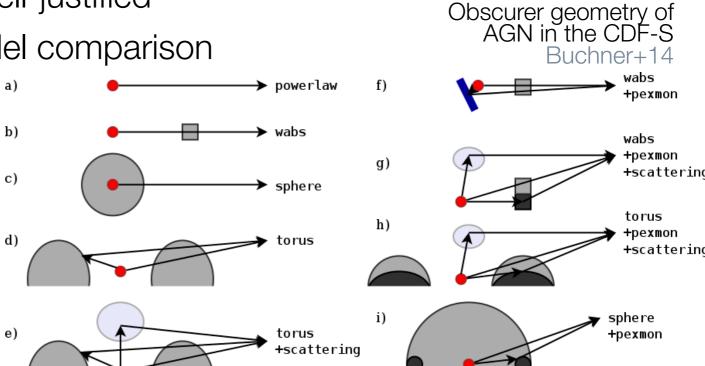
Region of practical equivalence (ROPE)

between the models



• Is parameter posterior contained in ROPE? (parameter estimation)

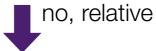
- Empirical models
 - Information content
 - Prediction quality
- Physical effects
 - Priors often well-justified
 - Bayesian model comparison



Test model in isolation?



Posterior predictive checks (PPC)
Parametric bootstrap



Compare physical models or empirical descriptions?





Information content (AIC)
Prediction quality (Cross validation)



Additive component



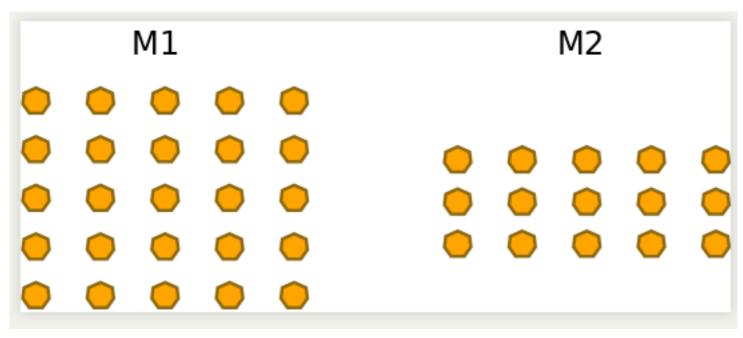
Parameter estimation Region of equivalence Bayesian model comparison

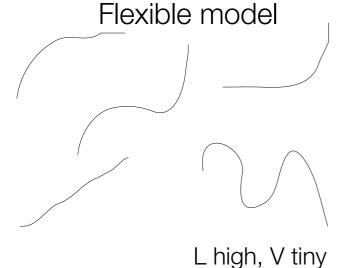


Bayesian model comparison

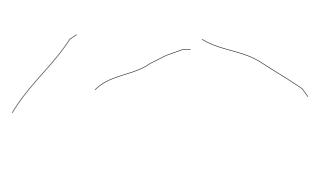
Punishing prediction diversity

(not number of parameters)





Inflexible model



L medium, V medium

Data

What to do with Z

• Z1, Z2

$$rac{p(M1|D)}{p(M2|D)} = rac{Z1 \cdot p(M1)}{Z2 \cdot p(M2)}$$

Posterior odds ratio

Bayes factor

Prior odds ratio

What to do with Z

• Z1, Z2

$$rac{p(M1|D)}{p(M2|D)} = rac{Z1 \cdot p(M1)}{Z2 \cdot p(M2)}$$

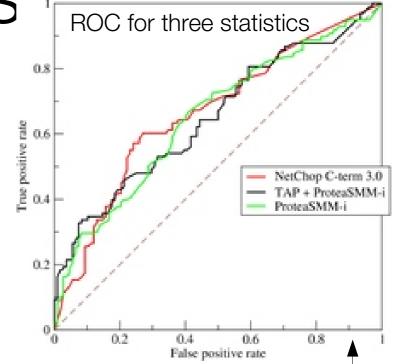
model priors: leave to reader or motivated by theory

ullet Does $rac{p(M1|D)}{p(M2|D)}=3/1$ mean M2 is correct in a quarter of the cases?

Comparing selection methods

 You have a <u>statistic</u> (a indicator) – (signal strength, likelihood ratio, Bayes factor, classifier probability)

- If you apply threshold:
 - if above → select model A
 - if below → select model B
- There will be
 - cases where you will be right
 - cases where you will be wrong
- determine the rates with simulations from model A and model B.
- Plot the rates as a function of threshold: ROC curve

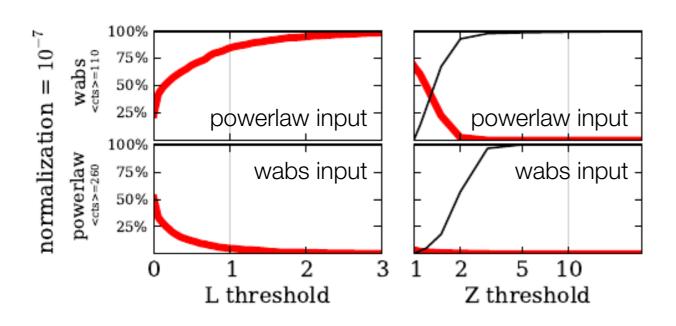


Predicted class Actual class	Cat	Dog
Cat	6	2
→ Dog	1	3

Calibrating model decisions

- Model probabilities → decisions
- False decision rate (false positives/negatives)
 - Monte Carlo simulations (parametric bootstrap)

Calibrating model decisions



Buchner+14

False negatives Non-decisions

Advantages:

- Get rid of parameter prior dependences
- Have frequentist properties of Bayesian method
 Completely Bayesian treatment + decisions

Disadvantages:

- Can be computationally expensive

Exercise

- Create a Bayes factor distribution
 P(model A|D) / P(model B|D)
- from simulations from the simpler model

→ example-sine-modelcomparison.ipynb