## IN CLASS # 4

1. Consider a single crystal of some hypothetical metal that has the FCC crystal structure and is oriented such that a tensile stress is applied along a [102] direction. If slip occurs on a (111) plane and in a a [101] direction, compute the stress at which the crystal yields if its critical resolved shear stress is 3.42 MPa.

$$\theta = \cos^{-1} \left[ \frac{u_1 u_2 + v_1 v_2 + w_1 w_2}{\sqrt{(u_1^2 + v_1^2 + w_1^2)(u_2^2 + v_2^2 + w_2^2)}} \right] \quad \sigma_y = \frac{\tau_{crss}}{(\cos \phi \cos \lambda)_{max}}$$

First, it is necessary to determine the values of  $\phi$  and  $\lambda$ .

 $\lambda$  is the angle between [102] and [101].

Therefore, 
$$u_1 = -1$$
  $V_1 = 0$   $w_1 = 2$   $u_2 = -1$   $v_2 = 0$   $w_2 = 1$ 

$$\lambda = \cos^{-1} \left[ \frac{(-1)(-1) + (0)(0) + (2)(1)}{\int ((-1)^2 + (0)^2 + (2)^2) \cdot ((-1)^2 + (0)^2 + (1)^2)^{-1}} \right]$$

$$\lambda = \cos^{-1}\left(\frac{3}{\sqrt{10^{-1}}}\right) = 18.4^{\circ}$$

The normal to the (111) slip plane is [111] direction.

of is the angle between [102] and [111].

Therefore, 
$$U_1 = -1$$
  $V_1 = 0$   $W_1 = 2$   $U_2 = 1$   $V_2 = 1$   $W_2 = 1$ 

$$\phi = \cos^{-1} \left[ \frac{(-1)(1) + (0)(1) + (2)(1)}{\int ((-1)^2 + (0)^2 + (2)^2) \cdot ((1)^2 + (1)^2 + (1)^2)} \right]$$

$$\phi = \cos^{-1}\left(\frac{3}{\sqrt{15'}}\right) = 39.2^{\circ}$$

$$\overline{6y} = \frac{3.42 \text{ MPa}}{\left(\frac{3}{110'}\right) \left(\frac{3}{115'}\right)} = 4.65 \text{ MPa}$$

## IN CLASS # 4

2. The lower yield point for an iron that has an average grain diameter of  $5 \times 10^{-2}$  mm is 135 MPa. At a grain diameter of  $8 \times 10^{-3}$  mm, the yield point increases to 260 MPa. At what grain diameter will the lower yield point be 205 MPa?

$$\sigma_y = \sigma_0 + k_y d^{-1/2}$$

$$135 = 60 + 4.47.ky$$
  
 $260 = 60 + 11.18ky \rightarrow 60 = 260 - 11.18ky$ 

At a yield strength of 250 MPa;  

$$250 = 51.7 + 18.63.d^{-1/2}$$
  
 $J^{-1/2} = 8.23 \text{ mm}^{-1/2}$   
 $d = 1.48 \times 10^{-2} \text{ mm}$