

# Bunker Hill Community College

Final Statistics Exam 2019-05-02

Exam ID 007

**Name:** \_\_\_\_\_

This take-home exam is due **Wednesday, May 8**, at the beginning of class.

You may use any notes, textbook, or online tools; however, you may not request help from any other human.

You will show your work on the pages with questions. When you are sure of your answers, you will **put those answers in the boxes** on the first few pages.

Unless you have an objection to doing so, please **copy the honor-code text below and sign**.

*I understand that outside help is NOT allowed on this exam. On my honor, the work herein is my own.*

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**Signature:** \_\_\_\_\_

1. (a)
- (b)
- (c)
- (d)
- (e)
- (f)
2.
3.
4. (a)
- (b)
5.
6. (a)
- (b)
- (c)
- (d)
- (e)
- (f)
- (g)
7. (a)
- (b)

8. (a)
- (b)
- (c)
- (d)
- (e)
- (f)
- (g)

1. In a deck of strange cards, there are 628 cards. Each card has an image and a color. The amounts are shown in the table below.

	blue	indigo	white	yellow
flower	61	85	10	88
gem	23	40	28	81
horn	44	97	14	57

- (a) What is the probability a random card is white?
- (b) What is the probability a random card is a gem given it is blue?
- (c) What is the probability a random card is yellow given it is a horn?
- (d) What is the probability a random card is either a gem or yellow (or both)?
- (e) What is the probability a random card is both a gem and blue?
- (f) What is the probability a random card is a flower?

2. In a deck of strange cards, each card has an image and a color. The chance of drawing a horn is 22%. If a horn is drawn, there is a 55.5% chance that it is blue. If a card that is not a horn is drawn, there is a 35% chance that it is blue.

Now, someone draws a random card and reveals it is blue. What is the chance the card is not a horn?

3. In a very large pile of toothpicks, the mean length is 66.22 millimeters and the standard deviation is 3.19 millimeters. If you randomly sample 121 toothpicks, what is the chance the sample mean is between 65.96 and 66.74 millimeters?

4. In a game, there is a 73% chance to win a round. You will play 71 rounds.
- (a) What is the probability of winning exactly 51 rounds?
  - (b) What is the probability of winning at least 49 but at most 59 rounds?

5. As an ornithologist, you wish to determine the average body mass of *Agelaius Phoeniceus*. You randomly sample 25 adults of *Agelaius Phoeniceus*, resulting in a sample mean of 45.6 grams and a sample standard deviation of 5.6 grams. Determine a 99.5% confidence interval of the true population mean.



6. A treatment group of size 31 has a mean of 11 and standard deviation of 0.98. A control group of size 9 has a mean of 9.88 and standard deviation of 1.04. If you decided to use a significance level of 0.01, is there sufficient evidence to conclude the treatment causes an effect?

By using the Welch-Satterthwaite equation, I've calculated the degrees of freedom should be 12.

- (a) State the null hypothesis.
- (b) State the alternative hypothesis.
- (c) Evaluate the critical value. (The critical value is either  $z^*$  or  $t^*$ . Determine its value.)
- (d) Determine the standard error of the relevant sampling distribution.
- (e) Evaluate the absolute value of the test statistic. (The test statistic is either  $z_{\text{obs}}$  or  $t_{\text{obs}}$ . Determine its absolute value.)
- (f) If possible, evaluate the  $p$ -value. Otherwise, describe an interval containing the  $p$ -value.
- (g) Do we reject or retain the null?

7. From a very large population, a random sample of 4400 individuals was taken. In that sample, 9.5% were salty. Determine a 80% confidence interval of the population proportion.
- (a) Find the lower bound of the confidence interval.
  - (b) Find the upper bound of the confidence interval.

8. An experiment is run with a treatment group of size 16 and a control group of size 27. The results are summarized in the table below.

	treatment	control
sick	16	27
not sick	0	0

Using a significance level of 0.005, determine whether the treatment causes an effect on the proportion of cases that are sick.

- (a) State the null hypothesis.
- (b) State the alternative hypothesis.
- (c) Evaluate the critical value. (The critical value is either  $z^*$  or  $t^*$ . Determine its value.)
- (d) Determine the standard error of the relevant sampling distribution.
- (e) Evaluate the absolute value of the test statistic. (The test statistic is either  $z_{\text{obs}}$  or  $t_{\text{obs}}$ . Determine its absolute value.)
- (f) If possible, evaluate the  $p$ -value. Otherwise, describe an interval containing the  $p$ -value.
- (g) Do we reject or retain the null?