

# Bunker Hill Community College

Final Statistics Exam 2019-05-02

Exam ID 010

**Name:** \_\_\_\_\_

This take-home exam is due **Wednesday, May 8**, at the beginning of class.

You may use any notes, textbook, or online tools; however, you may not request help from any other human.

You will show your work on the pages with questions. When you are sure of your answers, you will **put those answers in the boxes** on the first few pages.

Unless you have an objection to doing so, please **copy the honor-code text below and sign**.

*I understand that outside help is NOT allowed on this exam. On my honor, the work herein is my own.*

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**Signature:** \_\_\_\_\_

1. (a)
- (b)
- (c)
- (d)
- (e)
- (f)
2.
3.
4. (a)
- (b)
5.
6. (a)
- (b)
- (c)
- (d)
- (e)
- (f)
- (g)
7. (a)
- (b)

8. (a)
- (b)
- (c)
- (d)
- (e)
- (f)
- (g)

1. In a deck of strange cards, there are 1387 cards. Each card has an image and a color. The amounts are shown in the table below.

	black	orange	pink	violet	white
dog	41	16	32	24	68
flower	67	85	43	77	10
horn	79	97	63	96	76
tree	52	56	29	14	60
wheel	38	72	86	45	61

- (a) What is the probability a random card is both a wheel and violet?
- (b) What is the probability a random card is violet?
- (c) What is the probability a random card is either a tree or black (or both)?
- (d) What is the probability a random card is a horn given it is pink?
- (e) What is the probability a random card is pink given it is a tree?
- (f) What is the probability a random card is a flower?

2. In a deck of strange cards, each card has an image and a color. The chance of drawing a horn is 42.2%. If a horn is drawn, there is a 18.5% chance that it is teal. If a card that is not a horn is drawn, there is a 80.1% chance that it is teal.

Now, someone draws a random card and reveals it is teal. What is the chance the card is a horn?

3. In a very large pile of toothpicks, the mean length is 67.57 millimeters and the standard deviation is 2.91 millimeters. If you randomly sample 121 toothpicks, what is the chance the sample mean is between 66.88 and 67.91 millimeters?

4. In a game, there is a 62% chance to win a round. You will play 163 rounds.
- (a) What is the probability of winning exactly 103 rounds?
  - (b) What is the probability of winning at least 87 but at most 105 rounds?

5. As an ornithologist, you wish to determine the average body mass of *Piranga olivacea*. You randomly sample 30 adults of *Piranga olivacea*, resulting in a sample mean of 39.2 grams and a sample standard deviation of 5.49 grams. Determine a 90% confidence interval of the true population mean.



6. A treatment group of size 16 has a mean of 1060 and standard deviation of 85.8. A control group of size 22 has a mean of 1000 and standard deviation of 110. If you decided to use a significance level of 0.1, is there sufficient evidence to conclude the treatment causes an effect?

By using the Welch-Satterthwaite equation, I've calculated the degrees of freedom should be 35.

- (a) State the null hypothesis.
- (b) State the alternative hypothesis.
- (c) Evaluate the critical value. (The critical value is either  $z^*$  or  $t^*$ . Determine its value.)
- (d) Determine the standard error of the relevant sampling distribution.
- (e) Evaluate the absolute value of the test statistic. (The test statistic is either  $z_{\text{obs}}$  or  $t_{\text{obs}}$ . Determine its absolute value.)
- (f) If possible, evaluate the  $p$ -value. Otherwise, describe an interval containing the  $p$ -value.
- (g) Do we reject or retain the null?

7. From a very large population, a random sample of 4900 individuals was taken. In that sample, 44.6% were tasty. Determine a 80% confidence interval of the population proportion.
- (a) Find the lower bound of the confidence interval.
  - (b) Find the upper bound of the confidence interval.

8. An experiment is run with a treatment group of size 258 and a control group of size 226. The results are summarized in the table below.

	treatment	control
happy	170	166
not happy	88	60

Using a significance level of 0.1, determine whether the treatment causes an effect on the proportion of cases that are happy.

- (a) State the null hypothesis.
- (b) State the alternative hypothesis.
- (c) Evaluate the critical value. (The critical value is either  $z^*$  or  $t^*$ . Determine its value.)
- (d) Determine the standard error of the relevant sampling distribution.
- (e) Evaluate the absolute value of the test statistic. (The test statistic is either  $z_{\text{obs}}$  or  $t_{\text{obs}}$ . Determine its absolute value.)
- (f) If possible, evaluate the  $p$ -value. Otherwise, describe an interval containing the  $p$ -value.
- (g) Do we reject or retain the null?