

- As an ornithologist, you wish to determine the average body mass of *Seiurus noveboracensis*. You randomly capture 31 adults of *Seiurus noveboracensis*, resulting in a sample mean of 20.47 grams and a sample standard deviation of 3.53 grams. You decide to report a 95% confidence interval.
  - Determine the lower bound of the confidence interval.
  - Determine the upper bound of the confidence interval.
- A teacher has 6 students who have each taken two quizzes. Perform a two-tail test with significance level 0.04 to determine whether students' performance changed on average.

	student1	student2	student3	student4	student5	student6
quiz 1:	62.9	83.4	55.8	57.7	85.9	62.3
quiz 2:	48.8	78.3	49.1	52.3	88.8	53.9

- State the null hypothesis.
  - State the alternative hypothesis.
  - Evaluate the critical value. (The critical value is either  $z^*$  or  $t^*$ . Determine its value.)
  - Determine the standard error of the relevant sampling distribution.
  - Evaluate the absolute value of the test statistic. (The test statistic is either  $z_{\text{obs}}$  or  $t_{\text{obs}}$ . Determine its absolute value.)
  - If possible, evaluate the  $p$ -value. Otherwise, describe an interval containing the  $p$ -value.
  - Do we reject or retain the null?
- You are interested in whether a treatment causes an effect on a continuously measurable attribute. You use a treatment group with 5 cases and a control group with 5 cases. You decide to run a hypothesis test with a significance level of 0.04. Your data is below. Please use 5 for the degrees of freedom (calculated with the Welch-Satterthwaite equation).

treatment	control
14.8	13.4
12.3	12.2
15.1	10.8
13.4	13
17.7	10.6

- State the null hypothesis.
- State the alternative hypothesis.
- Evaluate the critical value. (The critical value is either  $z^*$  or  $t^*$ . Determine its value.)
- Determine the standard error of the relevant sampling distribution.

- (e) Evaluate the absolute value of the test statistic. (The test statistic is either  $z_{\text{obs}}$  or  $t_{\text{obs}}$ . Determine its absolute value.)
  - (f) If possible, evaluate the  $p$ -value. Otherwise, describe an interval containing the  $p$ -value.
  - (g) Do we reject or retain the null?
4. From a very large population, a random sample of 1300 individuals was taken. In that sample, 81% were blue. Determine a 95% confidence interval of the population proportion.
- (a) Find the lower bound of the confidence interval.
  - (b) Find the upper bound of the confidence interval.
5. Your boss wants to know what proportion of a very large population is glowing. She also wants to guarantee that the margin of error of a 99% confidence interval will be less than 0.01 (which is 1 percentage points). How large of a sample is needed? Please round up, using only 2 significant digits.
6. An experiment is run with a treatment group of size 290 and a control group of size 248. The results are summarized in the table below.

	treatment	control
omnivorous	217	171
not omnivorous	73	77

Using a significance level of 0.2, determine whether the treatment causes an effect on the proportion of cases that are omnivorous.

- (a) State the null hypothesis.
- (b) State the alternative hypothesis.
- (c) Evaluate the critical value. (The critical value is either  $z^*$  or  $t^*$ . Determine its value.)
- (d) Determine the standard error of the relevant sampling distribution.
- (e) Evaluate the absolute value of the test statistic. (The test statistic is either  $z_{\text{obs}}$  or  $t_{\text{obs}}$ . Determine its absolute value.)
- (f) If possible, evaluate the  $p$ -value. Otherwise, describe an interval containing the  $p$ -value.
- (g) Do we reject or retain the null?

1. (a) LB = 19.2  
(b) UB = 21.8
2. (a)  $H_0 : \mu_{\text{diff}} = 0$   
(b)  $H_A : \mu_{\text{diff}} \neq 0$   
(c)  $t^* = 2.76$   
(d)  $SE = 1.78$   
(e)  $|t_{\text{obs}}| = 2.724$   
(f)  $0.04 < p\text{-value} < 0.05$   
(g) retain
3. (a)  $H_0 : \mu_2 - \mu_1 = 0$   
(b)  $H_0 : \mu_2 - \mu_1 \neq 0$   
(c)  $t^* = 2.76$   
(d)  $SE = 1.07$   
(e)  $|t_{\text{obs}}| = 2.52$   
(f)  $0.05 < p\text{-value} < 0.1$   
(g) retain
4. (a) LB of p CI = 0.789 or 78.9%  
(b) UB of p CI = 0.831 or 83.1%
5.  $n \approx 17000$
6. (a)  $H_0 : p_2 - p_1 = 0$   
(b)  $H_A : p_2 - p_1 \neq 0$   
(c)  $z^* = 1.28$   
(d)  $SE = 0.039$   
(e)  $|z_{\text{obs}}| = 1.49$   
(f)  $p\text{-value} = 0.1362$   
(g) reject