

# Bunker Hill Community College

Final Statistics Exam 2019-05-02

Exam ID 021

**Name:** \_\_\_\_\_

This take-home exam is due **Wednesday, May 8**, at the beginning of class.

You may use any notes, textbook, or online tools; however, you may not request help from any other human.

You will show your work on the pages with questions. When you are sure of your answers, you will **put those answers in the boxes** on the first few pages.

Unless you have an objection to doing so, please **copy the honor-code text below and sign**.

*I understand that outside help is NOT allowed on this exam. On my honor, the work herein is my own.*

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**Signature:** \_\_\_\_\_

1. (a)
- (b)
- (c)
- (d)
- (e)
- (f)
2.
3.
4. (a)
- (b)
5.
6. (a)
- (b)
- (c)
- (d)
- (e)
- (f)
- (g)
7. (a)
- (b)

8. (a)
- (b)
- (c)
- (d)
- (e)
- (f)
- (g)

1. In a deck of strange cards, there are 809 cards. Each card has an image and a color. The amounts are shown in the table below.

	black	gray	violet
bike	57	94	50
dog	78	91	65
flower	12	99	95
gem	88	67	13

- (a) What is the probability a random card is both a gem and violet?
- (b) What is the probability a random card is gray?
- (c) What is the probability a random card is either a flower or violet (or both)?
- (d) What is the probability a random card is gray given it is a bike?
- (e) What is the probability a random card is a bike?
- (f) What is the probability a random card is a dog given it is black?

2. In a deck of strange cards, each card has an image and a color. The chance of drawing a bike is 19.4%. If a bike is drawn, there is a 35.3% chance that it is orange. If a card that is not a bike is drawn, there is a 83% chance that it is orange.

Now, someone draws a random card and reveals it is not orange. What is the chance the card is a bike?

3. In a very large pile of toothpicks, the mean length is 67.14 millimeters and the standard deviation is 2.61 millimeters. If you randomly sample 150 toothpicks, what is the chance the sample mean is between 66.95 and 67.67 millimeters?

4. In a game, there is a 87% chance to win a round. You will play 103 rounds.
- (a) What is the probability of winning exactly 90 rounds?
  - (b) What is the probability of winning at least 86 but at most 94 rounds?

5. As an ornithologist, you wish to determine the average body mass of *Setophaga ruticilla*. You randomly sample 30 adults of *Setophaga ruticilla*, resulting in a sample mean of 9.18 grams and a sample standard deviation of 1.39 grams. Determine a 80% confidence interval of the true population mean.



6. A treatment group of size 13 has a mean of 106 and standard deviation of 10.3. A control group of size 38 has a mean of 101 and standard deviation of 9.99. If you decided to use a significance level of 0.1, is there sufficient evidence to conclude the treatment causes an effect?

By using the Welch-Satterthwaite equation, I've calculated the degrees of freedom should be 20.

- (a) State the null hypothesis.
- (b) State the alternative hypothesis.
- (c) Evaluate the critical value. (The critical value is either  $z^*$  or  $t^*$ . Determine its value.)
- (d) Determine the standard error of the relevant sampling distribution.
- (e) Evaluate the absolute value of the test statistic. (The test statistic is either  $z_{\text{obs}}$  or  $t_{\text{obs}}$ . Determine its absolute value.)
- (f) If possible, evaluate the  $p$ -value. Otherwise, describe an interval containing the  $p$ -value.
- (g) Do we reject or retain the null?

7. From a very large population, a random sample of 71000 individuals was taken. In that sample, 31.4% were floating. Determine a 98% confidence interval of the population proportion.
- (a) Find the lower bound of the confidence interval.
  - (b) Find the upper bound of the confidence interval.

8. An experiment is run with a treatment group of size 195 and a control group of size 179. The results are summarized in the table below.

	treatment	control
special	168	163
not special	27	16

Using a significance level of 0.2, determine whether the treatment causes an effect on the proportion of cases that are special.

- (a) State the null hypothesis.
- (b) State the alternative hypothesis.
- (c) Evaluate the critical value. (The critical value is either  $z^*$  or  $t^*$ . Determine its value.)
- (d) Determine the standard error of the relevant sampling distribution.
- (e) Evaluate the absolute value of the test statistic. (The test statistic is either  $z_{\text{obs}}$  or  $t_{\text{obs}}$ . Determine its absolute value.)
- (f) If possible, evaluate the  $p$ -value. Otherwise, describe an interval containing the  $p$ -value.
- (g) Do we reject or retain the null?