

# Bunker Hill Community College

Final Statistics Exam 2019-05-02

Exam ID 003

**Name:** \_\_\_\_\_

This take-home exam is due **Wednesday, May 8**, at the beginning of class.

You may use any notes, textbook, or online tools; however, you may not request help from any other human.

You will show your work on the pages with questions. When you are sure of your answers, you will **put those answers in the boxes** on the first few pages.

Unless you have an objection to doing so, please **copy the honor-code text below and sign**.

*I understand that outside help is NOT allowed on this exam. On my honor, the work herein is my own.*

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**Signature:** \_\_\_\_\_

1. (a)
- (b)
- (c)
- (d)
- (e)
- (f)
2.
3.
4. (a)
- (b)
5.
6. (a)
- (b)
- (c)
- (d)
- (e)
- (f)
- (g)
7. (a)
- (b)

8. (a)
- (b)
- (c)
- (d)
- (e)
- (f)
- (g)

1. In a deck of strange cards, there are 1253 cards. Each card has an image and a color. The amounts are shown in the table below.

	blue	indigo	orange	red	violet
flower	14	67	47	40	10
pig	52	98	48	51	20
shovel	53	41	90	55	27
tree	70	88	73	21	35
wheel	36	61	62	78	16

- (a) What is the probability a random card is both a wheel and orange?
- (b) What is the probability a random card is blue?
- (c) What is the probability a random card is a tree?
- (d) What is the probability a random card is a pig given it is red?
- (e) What is the probability a random card is indigo given it is a tree?
- (f) What is the probability a random card is either a wheel or orange (or both)?

2. In a deck of strange cards, each card has an image and a color. The chance of drawing a cat is 38.3%. If a cat is drawn, there is a 82.7% chance that it is green. If a card that is not a cat is drawn, there is a 61.9% chance that it is green.

Now, someone draws a random card and reveals it is not green. What is the chance the card is a cat?

3. In a very large pile of toothpicks, the mean length is 66.87 millimeters and the standard deviation is 1.79 millimeters. If you randomly sample 175 toothpicks, what is the chance the sample mean is between 66.76 and 66.99 millimeters?

4. In a game, there is a 20% chance to win a round. You will play 180 rounds.
- (a) What is the probability of winning exactly 37 rounds?
  - (b) What is the probability of winning at least 38 but at most 48 rounds?

5. As an ornithologist, you wish to determine the average body mass of *Porzana carolina*. You randomly sample 27 adults of *Porzana carolina*, resulting in a sample mean of 66.97 grams and a sample standard deviation of 9.8 grams. Determine a 95% confidence interval of the true population mean.



6. A treatment group of size 21 has a mean of 108 and standard deviation of 18.3. A control group of size 20 has a mean of 96.8 and standard deviation of 20.4. If you decided to use a significance level of 0.04, is there sufficient evidence to conclude the treatment causes an effect?

By using the Welch-Satterthwaite equation, I've calculated the degrees of freedom should be 38.

- (a) State the null hypothesis.
- (b) State the alternative hypothesis.
- (c) Evaluate the critical value. (The critical value is either  $z^*$  or  $t^*$ . Determine its value.)
- (d) Determine the standard error of the relevant sampling distribution.
- (e) Evaluate the absolute value of the test statistic. (The test statistic is either  $z_{\text{obs}}$  or  $t_{\text{obs}}$ . Determine its absolute value.)
- (f) If possible, evaluate the  $p$ -value. Otherwise, describe an interval containing the  $p$ -value.
- (g) Do we reject or retain the null?

7. From a very large population, a random sample of 59000 individuals was taken. In that sample, 10.1% were asleep. Determine a 98% confidence interval of the population proportion.
- (a) Find the lower bound of the confidence interval.
  - (b) Find the upper bound of the confidence interval.

8. An experiment is run with a treatment group of size 235 and a control group of size 268. The results are summarized in the table below.

	treatment	control
cold	19	11
not cold	216	257

Using a significance level of 0.1, determine whether the treatment causes an effect on the proportion of cases that are cold.

- (a) State the null hypothesis.
- (b) State the alternative hypothesis.
- (c) Evaluate the critical value. (The critical value is either  $z^*$  or  $t^*$ . Determine its value.)
- (d) Determine the standard error of the relevant sampling distribution.
- (e) Evaluate the absolute value of the test statistic. (The test statistic is either  $z_{\text{obs}}$  or  $t_{\text{obs}}$ . Determine its absolute value.)
- (f) If possible, evaluate the  $p$ -value. Otherwise, describe an interval containing the  $p$ -value.
- (g) Do we reject or retain the null?