

# Bunker Hill Community College

Final Statistics Exam 2019-05-02

Exam ID 013

**Name:** \_\_\_\_\_

This take-home exam is due **Wednesday, May 8**, at the beginning of class.

You may use any notes, textbook, or online tools; however, you may not request help from any other human.

You will show your work on the pages with questions. When you are sure of your answers, you will **put those answers in the boxes** on the first few pages.

Unless you have an objection to doing so, please **copy the honor-code text below and sign**.

*I understand that outside help is NOT allowed on this exam. On my honor, the work herein is my own.*

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**Signature:** \_\_\_\_\_

1.
  - (a)
  - (b)
  - (c)
  - (d)
  - (e)
  - (f)
2.
3.
4.
  - (a)
  - (b)
5.
6.
  - (a)
  - (b)
  - (c)
  - (d)
  - (e)
  - (f)
  - (g)
7.
  - (a)
  - (b)

8. (a)
- (b)
- (c)
- (d)
- (e)
- (f)
- (g)

1. In a deck of strange cards, there are 752 cards. Each card has an image and a color. The amounts are shown in the table below.

	gray	green	orange	red
dog	61	76	81	24
horn	19	63	34	85
wheel	68	90	74	77

- (a) What is the probability a random card is orange given it is a dog?
- (b) What is the probability a random card is both a horn and gray?
- (c) What is the probability a random card is a horn given it is gray?
- (d) What is the probability a random card is a dog?
- (e) What is the probability a random card is gray?
- (f) What is the probability a random card is either a horn or red (or both)?

2. In a deck of strange cards, each card has an image and a color. The chance of drawing a cat is 36%. If a cat is drawn, there is a 87.9% chance that it is orange. If a card that is not a cat is drawn, there is a 64.8% chance that it is orange.

Now, someone draws a random card and reveals it is orange. What is the chance the card is a cat?

3. In a very large pile of toothpicks, the mean length is 70.4 millimeters and the standard deviation is 3.36 millimeters. If you randomly sample 225 toothpicks, what is the chance the sample mean is between 70.05 and 70.54 millimeters?

4. In a game, there is a 15% chance to win a round. You will play 188 rounds.
- (a) What is the probability of winning exactly 28 rounds?
  - (b) What is the probability of winning at least 33 but at most 40 rounds?

5. As an ornithologist, you wish to determine the average body mass of *Denrdoica magnolia*. You randomly sample 24 adults of *Denrdoica magnolia*, resulting in a sample mean of 9.62 grams and a sample standard deviation of 1.17 grams. Determine a 80% confidence interval of the true population mean.



6. A treatment group of size 27 has a mean of 1.02 and standard deviation of 0.066. A control group of size 23 has a mean of 1.05 and standard deviation of 0.0778. If you decided to use a significance level of 0.1, is there sufficient evidence to conclude the treatment causes an effect?

By using the Welch-Satterthwaite equation, I've calculated the degrees of freedom should be 43.

- (a) State the null hypothesis.
- (b) State the alternative hypothesis.
- (c) Evaluate the critical value. (The critical value is either  $z^*$  or  $t^*$ . Determine its value.)
- (d) Determine the standard error of the relevant sampling distribution.
- (e) Evaluate the absolute value of the test statistic. (The test statistic is either  $z_{\text{obs}}$  or  $t_{\text{obs}}$ . Determine its absolute value.)
- (f) If possible, evaluate the  $p$ -value. Otherwise, describe an interval containing the  $p$ -value.
- (g) Do we reject or retain the null?

7. From a very large population, a random sample of 440 individuals was taken. In that sample, 45.9% were tasty. Determine a 95% confidence interval of the population proportion.
- (a) Find the lower bound of the confidence interval.
  - (b) Find the upper bound of the confidence interval.

8. An experiment is run with a treatment group of size 49 and a control group of size 20. The results are summarized in the table below.

	treatment	control
green	9	10
not green	40	10

Using a significance level of 0.005, determine whether the treatment causes an effect on the proportion of cases that are green.

- (a) State the null hypothesis.
- (b) State the alternative hypothesis.
- (c) Evaluate the critical value. (The critical value is either  $z^*$  or  $t^*$ . Determine its value.)
- (d) Determine the standard error of the relevant sampling distribution.
- (e) Evaluate the absolute value of the test statistic. (The test statistic is either  $z_{\text{obs}}$  or  $t_{\text{obs}}$ . Determine its absolute value.)
- (f) If possible, evaluate the  $p$ -value. Otherwise, describe an interval containing the  $p$ -value.
- (g) Do we reject or retain the null?