

Bunker Hill Community College

Final Statistics Exam 2019-05-02

Exam ID 027

Name: _____

This take-home exam is due **Wednesday, May 8**, at the beginning of class.

You may use any notes, textbook, or online tools; however, you may not request help from any other human.

You will show your work on the pages with questions. When you are sure of your answers, you will **put those answers in the boxes** on the first few pages.

Unless you have an objection to doing so, please **copy the honor-code text below and sign**.

I understand that outside help is NOT allowed on this exam. On my honor, the work herein is my own.

Signature: _____

1. (a)
- (b)
- (c)
- (d)
- (e)
- (f)
2.
3.
4. (a)
- (b)
5.
6. (a)
- (b)
- (c)
- (d)
- (e)
- (f)
- (g)
7. (a)
- (b)

8. (a)
- (b)
- (c)
- (d)
- (e)
- (f)
- (g)

1. In a deck of strange cards, there are 795 cards. Each card has an image and a color. The amounts are shown in the table below.

	blue	green	indigo	pink
flower	49	86	30	35
gem	16	54	41	88
horn	10	68	27	44
tree	99	69	48	31

- (a) What is the probability a random card is indigo given it is a gem?
- (b) What is the probability a random card is a gem given it is blue?
- (c) What is the probability a random card is both a tree and blue?
- (d) What is the probability a random card is green?
- (e) What is the probability a random card is either a flower or indigo (or both)?
- (f) What is the probability a random card is a gem?

2. In a deck of strange cards, each card has an image and a color. The chance of drawing a flower is 44.2%. If a flower is drawn, there is a 64.3% chance that it is teal. If a card that is not a flower is drawn, there is a 75.1% chance that it is teal.

Now, someone draws a random card and reveals it is teal. What is the chance the card is a flower?

3. In a very large pile of toothpicks, the mean length is 73.52 millimeters and the standard deviation is 3.5 millimeters. If you randomly sample 120 toothpicks, what is the chance the sample mean is between 73.15 and 74.28 millimeters?

4. In a game, there is a 15% chance to win a round. You will play 83 rounds.
- (a) What is the probability of winning exactly 10 rounds?
 - (b) What is the probability of winning at least 12 but at most 21 rounds?

5. As an ornithologist, you wish to determine the average body mass of *Vermivora peregrina*. You randomly sample 27 adults of *Vermivora peregrina*, resulting in a sample mean of 12.91 grams and a sample standard deviation of 1.26 grams. Determine a 80% confidence interval of the true population mean.

6. A treatment group of size 20 has a mean of 1140 and standard deviation of 151. A control group of size 12 has a mean of 998 and standard deviation of 143. If you decided to use a significance level of 0.01, is there sufficient evidence to conclude the treatment causes an effect?

By using the Welch-Satterthwaite equation, I've calculated the degrees of freedom should be 24.

- (a) State the null hypothesis.
- (b) State the alternative hypothesis.
- (c) Evaluate the critical value. (The critical value is either z^* or t^* . Determine its value.)
- (d) Determine the standard error of the relevant sampling distribution.
- (e) Evaluate the absolute value of the test statistic. (The test statistic is either z_{obs} or t_{obs} . Determine its absolute value.)
- (f) If possible, evaluate the p -value. Otherwise, describe an interval containing the p -value.
- (g) Do we reject or retain the null?

7. From a very large population, a random sample of 71000 individuals was taken. In that sample, 29.6% were purple. Determine a 99.5% confidence interval of the population proportion.
- (a) Find the lower bound of the confidence interval.
 - (b) Find the upper bound of the confidence interval.

8. An experiment is run with a treatment group of size 139 and a control group of size 157. The results are summarized in the table below.

	treatment	control
special	106	133
not special	33	24

Using a significance level of 0.1, determine whether the treatment causes an effect on the proportion of cases that are special.

- (a) State the null hypothesis.
- (b) State the alternative hypothesis.
- (c) Evaluate the critical value. (The critical value is either z^* or t^* . Determine its value.)
- (d) Determine the standard error of the relevant sampling distribution.
- (e) Evaluate the absolute value of the test statistic. (The test statistic is either z_{obs} or t_{obs} . Determine its absolute value.)
- (f) If possible, evaluate the p -value. Otherwise, describe an interval containing the p -value.
- (g) Do we reject or retain the null?