

# Bunker Hill Community College

Final Statistics Exam 2019-05-02

Exam ID 024

**Name:** \_\_\_\_\_

This take-home exam is due **Wednesday, May 8**, at the beginning of class.

You may use any notes, textbook, or online tools; however, you may not request help from any other human.

You will show your work on the pages with questions. When you are sure of your answers, you will **put those answers in the boxes** on the first few pages.

Unless you have an objection to doing so, please **copy the honor-code text below and sign**.

*I understand that outside help is NOT allowed on this exam. On my honor, the work herein is my own.*

---

---

---

**Signature:** \_\_\_\_\_

1. (a)
- (b)
- (c)
- (d)
- (e)
- (f)
2.
3.
4. (a)
- (b)
5.
6. (a)
- (b)
- (c)
- (d)
- (e)
- (f)
- (g)
7. (a)
- (b)

8. (a)
- (b)
- (c)
- (d)
- (e)
- (f)
- (g)

1. In a deck of strange cards, there are 713 cards. Each card has an image and a color. The amounts are shown in the table below.

	green	orange	red	yellow
dog	11	84	54	26
gem	99	34	83	57
tree	38	94	89	44

- (a) What is the probability a random card is yellow given it is a gem?
- (b) What is the probability a random card is both a dog and red?
- (c) What is the probability a random card is orange?
- (d) What is the probability a random card is either a dog or red (or both)?
- (e) What is the probability a random card is a dog given it is orange?
- (f) What is the probability a random card is a gem?

2. In a deck of strange cards, each card has an image and a color. The chance of drawing a cat is 43%. If a cat is drawn, there is a 81.6% chance that it is red. If a card that is not a cat is drawn, there is a 25.4% chance that it is red.

Now, someone draws a random card and reveals it is red. What is the chance the card is a cat?

3. In a very large pile of toothpicks, the mean length is 72.37 millimeters and the standard deviation is 1.36 millimeters. If you randomly sample 200 toothpicks, what is the chance the sample mean is between 72.13 and 72.47 millimeters?

4. In a game, there is a 9% chance to win a round. You will play 167 rounds.
- (a) What is the probability of winning exactly 12 rounds?
  - (b) What is the probability of winning at least 7 but at most 24 rounds?

5. As an ornithologist, you wish to determine the average body mass of *Protonotaria citrea*. You randomly sample 21 adults of *Protonotaria citrea*, resulting in a sample mean of 13.75 grams and a sample standard deviation of 1.64 grams. Determine a 99% confidence interval of the true population mean.



6. A treatment group of size 13 has a mean of 106 and standard deviation of 10.3. A control group of size 38 has a mean of 101 and standard deviation of 9.99. If you decided to use a significance level of 0.1, is there sufficient evidence to conclude the treatment causes an effect?

By using the Welch-Satterthwaite equation, I've calculated the degrees of freedom should be 20.

- (a) State the null hypothesis.
- (b) State the alternative hypothesis.
- (c) Evaluate the critical value. (The critical value is either  $z^*$  or  $t^*$ . Determine its value.)
- (d) Determine the standard error of the relevant sampling distribution.
- (e) Evaluate the absolute value of the test statistic. (The test statistic is either  $z_{\text{obs}}$  or  $t_{\text{obs}}$ . Determine its absolute value.)
- (f) If possible, evaluate the  $p$ -value. Otherwise, describe an interval containing the  $p$ -value.
- (g) Do we reject or retain the null?

7. From a very large population, a random sample of 71000 individuals was taken. In that sample, 31.4% were floating. Determine a 98% confidence interval of the population proportion.
- (a) Find the lower bound of the confidence interval.
  - (b) Find the upper bound of the confidence interval.

8. An experiment is run with a treatment group of size 104 and a control group of size 149. The results are summarized in the table below.

	treatment	control
sorry	35	37
not sorry	69	112

Using a significance level of 0.2, determine whether the treatment causes an effect on the proportion of cases that are sorry.

- (a) State the null hypothesis.
- (b) State the alternative hypothesis.
- (c) Evaluate the critical value. (The critical value is either  $z^*$  or  $t^*$ . Determine its value.)
- (d) Determine the standard error of the relevant sampling distribution.
- (e) Evaluate the absolute value of the test statistic. (The test statistic is either  $z_{\text{obs}}$  or  $t_{\text{obs}}$ . Determine its absolute value.)
- (f) If possible, evaluate the  $p$ -value. Otherwise, describe an interval containing the  $p$ -value.
- (g) Do we reject or retain the null?