

1. Problem

From a very large population, a small sample of measurements was taken.

| | | | | |
|-----|-----|-----|-----|-----|
| 110 | 117 | 120 | 115 | 112 |
|-----|-----|-----|-----|-----|

Please calculate the average absolute deviation using the following formula:

$$AAD = \frac{\sum |x - \bar{x}|}{n}$$

Solution

We fill out the table column by column.

| x | $x - \bar{x}$ | $ x - \bar{x} $ |
|-------------------|--------------------|-----------------------------|
| 110 | -4.8 | 4.8 |
| 117 | 2.2 | 2.2 |
| 120 | 5.2 | 5.2 |
| 115 | 0.2000000000000003 | 0.2 |
| 112 | -2.8 | 2.8 |
| ===== | ===== | ===== |
| $\sum x = 574$ | | $\sum x - \bar{x} = 15.2$ |
| $\bar{x} = 114.8$ | | |

We are ready for the formula.

$$s = \frac{\sum |x - \bar{x}|}{n}$$

$$= \frac{15.2}{5}$$

$$= \boxed{3.04}$$

2. Problem

From a very large population, a small sample of measurements was taken.

| | | | | |
|----|----|----|----|----|
| 65 | 67 | 67 | 65 | 66 |
|----|----|----|----|----|

Please calculate the (Bessel corrected) sample standard deviation using the following formula:

$$s = \sqrt{\frac{\sum (x - \bar{x})^2}{n - 1}}$$

Solution

We fill out the table column by column.

| x | $x - \bar{x}$ | $(x - \bar{x})^2$ |
|----------------|---------------|----------------------------|
| 65 | -1 | 1 |
| 67 | 1 | 1 |
| 67 | 1 | 1 |
| 65 | -1 | 1 |
| 66 | 0 | 0 |
| <hr/> | | |
| $\sum x = 330$ | | $\sum (x - \bar{x})^2 = 4$ |
| $\bar{x} = 66$ | | |

We are ready for the formula.

$$s = \sqrt{\frac{\sum (x - \bar{x})^2}{n - 1}}$$

$$= \sqrt{\frac{4}{5 - 1}}$$

$$= \sqrt{1}$$

$$= \boxed{1}$$