

1. Solution

Let x represent a datum of interest. Let i represent that datum's index. Let ℓ represent that datum's percentile. Let n represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given $x = 21.349$. This means $i = 4$. We know $n = 11$. Determine the percentile ℓ .

$$\ell = \frac{4}{11}$$

$$\ell = 0.364$$

So, the percentile rank is $\boxed{0.364}$, or 36.4th percentile.

(b) We are given $\ell = 0.818$. We can use algebra to solve for i .

$$\ell = \frac{i}{n}$$

Multiply both sides by n .

$$n \cdot (\ell) = n \cdot \left(\frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate i .

$$i = (11)(0.818)$$

$$i = 9$$

Determine the x associated with $i = 9$.

$$x = \boxed{29.714}$$

(c) The mean: $\bar{x} = \frac{272.081}{11} = \boxed{24.735}$

(d) If n is odd, then median is $x_{i=\frac{n+1}{2}}$, the value of x when $i = \frac{n+1}{2}$. Otherwise, if n is even, the median is mean of $x_{i=\frac{n}{2}}$ and $x_{i=\frac{n}{2}+1}$. In this case, $n = 11$ and so n is odd.

$$\text{median} = x_{(11+1)/2} = x_6$$

So, median = $\boxed{21.941}$.

2. Solution

Let x represent a datum of interest. Let i represent that datum's index. Let ℓ represent that datum's percentile. Let n represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given $x = 85.313$. This means $i = 25$. We know $n = 56$. Determine the percentile ℓ .

$$\ell = \frac{25}{56}$$

$$\ell = 0.446$$

So, the percentile rank is $\boxed{0.446}$, or 44.6th percentile.

(b) We are given $\ell = 0.839$. We can use algebra to solve for i .

$$\ell = \frac{i}{n}$$

Multiply both sides by n .

$$n \cdot (\ell) = n \cdot \left(\frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate i .

$$i = (56)(0.839)$$

$$i = 47$$

Determine the x associated with $i = 47$.

$$x = \boxed{88.578}$$

(c) The mean: $\bar{x} = \frac{4781.671}{56} = \boxed{85.387}$

(d) If n is odd, then median is $x_{i=\frac{n+1}{2}}$, the value of x when $i = \frac{n+1}{2}$. Otherwise, if n is even, the median is mean of $x_{i=\frac{n}{2}}$ and $x_{i=\frac{n}{2}+1}$. In this case, $n = 56$ and so n is even.

$$\text{median} = \frac{x_{28} + x_{29}}{2} = \frac{85.612 + 85.665}{2}$$

So, median = $\boxed{85.6385}$.