

**1. Solution**

Let  $x$  represent a datum of interest. Let  $i$  represent that datum's index. Let  $\ell$  represent that datum's percentile. Let  $n$  represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given  $x = 148.486$ . This means  $i = 4$ . We know  $n = 6$ . Determine the percentile  $\ell$ .

$$\ell = \frac{4}{6}$$

$$\ell = 0.667$$

So, the percentile rank is  $\boxed{0.667}$ , or 66.7th percentile.

(b) We are given  $\ell = 0.5$ . We can use algebra to solve for  $i$ .

$$\ell = \frac{i}{n}$$

Multiply both sides by  $n$ .

$$n \cdot (\ell) = n \cdot \left( \frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate  $i$ .

$$i = (6)(0.5)$$

$$i = 3$$

Determine the  $x$  associated with  $i = 3$ .

$$x = \boxed{129.095}$$

(c) The mean:  $\bar{x} = \frac{817.856}{6} = \boxed{136.31}$

(d) If  $n$  is odd, then median is  $x_{i=\frac{n+1}{2}}$ , the value of  $x$  when  $i = \frac{n+1}{2}$ . Otherwise, if  $n$  is even, the median is mean of  $x_{i=\frac{n}{2}}$  and  $x_{i=\frac{n}{2}+1}$ . In this case,  $n = 6$  and so  $n$  is even.

$$\text{median} = \frac{x_3 + x_4}{2} = \frac{129.095 + 148.486}{2}$$

So, median =  $\boxed{138.7905}$ .

**2. Solution**

Let  $x$  represent a datum of interest. Let  $i$  represent that datum's index. Let  $\ell$  represent that datum's percentile. Let  $n$  represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given  $x = 51.711$ . This means  $i = 7$ . We know  $n = 12$ . Determine the percentile  $\ell$ .

$$\ell = \frac{7}{12}$$

$$\ell = 0.583$$

So, the percentile rank is 0.583, or 58.3th percentile.

(b) We are given  $\ell = 0.25$ . We can use algebra to solve for  $i$ .

$$\ell = \frac{i}{n}$$

Multiply both sides by  $n$ .

$$n \cdot (\ell) = n \cdot \left( \frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate  $i$ .

$$i = (12)(0.25)$$

$$i = 3$$

Determine the  $x$  associated with  $i = 3$ .

$$x = \text{50.441}$$

(c) The mean:  $\bar{x} = \frac{624.382}{12} = \text{52.032}$

(d) If  $n$  is odd, then median is  $x_{i=\frac{n+1}{2}}$ , the value of  $x$  when  $i = \frac{n+1}{2}$ . Otherwise, if  $n$  is even, the median is mean of  $x_{i=\frac{n}{2}}$  and  $x_{i=\frac{n}{2}+1}$ . In this case,  $n = 12$  and so  $n$  is even.

$$\text{median} = \frac{x_6 + x_7}{2} = \frac{51.334 + 51.711}{2}$$

So, median = 51.5225.