

**1. Solution**

Let  $x$  represent a datum of interest. Let  $i$  represent that datum's index. Let  $\ell$  represent that datum's percentile. Let  $n$  represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given  $x = 22.017$ . This means  $i = 11$ . We know  $n = 11$ . Determine the percentile  $\ell$ .

$$\ell = \frac{11}{11}$$

$$\ell = 1$$

So, the answer is 1, or 100%.

(b) We are given  $\ell = 0.364$ . We can use algebra to solve for  $i$ .

$$\ell = \frac{i}{n}$$

Multiply both sides by  $n$ .

$$n \cdot (\ell) = n \cdot \left( \frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate  $i$ .

$$i = (11)(0.364)$$

$$i = 4$$

Determine the  $x$  associated with  $i = 4$ .

$$x = 21.364$$

(c) The mean is  $\frac{236.519}{11} = 21.5017273$

(d) If  $n$  is odd, then median is  $x_{\frac{n+1}{2}}$ , the value of  $x$  when  $i = \frac{n+1}{2}$ . Otherwise median is mean of  $x_{\lfloor \frac{n+1}{2} \rfloor}$  and  $x_{\lceil \frac{n+1}{2} \rceil}$ . So, median = 21.463.

**2. Solution**

Let  $x$  represent a datum of interest. Let  $i$  represent that datum's index. Let  $\ell$  represent that datum's percentile. Let  $n$  represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given  $x = 41.753$ . This means  $i = 35$ . We know  $n = 40$ . Determine the percentile  $\ell$ .

$$\ell = \frac{35}{40}$$

$$\ell = 0.875$$

So, the answer is 0.875, or 87.5%.

(b) We are given  $\ell = 0.3$ . We can use algebra to solve for  $i$ .

$$\ell = \frac{i}{n}$$

Multiply both sides by  $n$ .

$$n \cdot (\ell) = n \cdot \left( \frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate  $i$ .

$$i = (40)(0.3)$$

$$i = 12$$

Determine the  $x$  associated with  $i = 12$ .

$$x = 41.357$$

(c) The mean is  $\frac{1658.932}{40} = 41.473$

(d) If  $n$  is odd, then median is  $x_{\frac{n+1}{2}}$ , the value of  $x$  when  $i = \frac{n+1}{2}$ . Otherwise median is mean of  $x_{\lfloor \frac{n+1}{2} \rfloor}$  and  $x_{\lceil \frac{n+1}{2} \rceil}$ . So, median = 41.469.