

1. Solution

Let x represent a datum of interest. Let i represent that datum's index. Let ℓ represent that datum's percentile. Let n represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given $x = 85.727$. This means $i = 5$. We know $n = 6$. Determine the percentile ℓ .

$$\ell = \frac{5}{6}$$

$$\ell = 0.833$$

So, the percentile rank is $\boxed{0.833}$, or 83.3th percentile.

(b) We are given $\ell = 0.667$. We can use algebra to solve for i .

$$\ell = \frac{i}{n}$$

Multiply both sides by n .

$$n \cdot (\ell) = n \cdot \left(\frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate i .

$$i = (6)(0.667)$$

$$i = 4$$

Determine the x associated with $i = 4$.

$$x = \boxed{85.302}$$

(c) The mean: $\bar{x} = \frac{510.91}{6} = \boxed{85.152}$

(d) If n is odd, then median is $x_{i=\frac{n+1}{2}}$, the value of x when $i = \frac{n+1}{2}$. Otherwise, if n is even, the median is mean of $x_{i=\frac{n}{2}}$ and $x_{i=\frac{n}{2}+1}$. In this case, $n = 6$ and so n is even.

$$\text{median} = \frac{x_3 + x_4}{2} = \frac{84.999 + 85.302}{2}$$

So, median = $\boxed{85.1505}$.

2. Solution

Let x represent a datum of interest. Let i represent that datum's index. Let ℓ represent that datum's percentile. Let n represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given $x = 150.606$. This means $i = 52$. We know $n = 63$. Determine the percentile ℓ .

$$\ell = \frac{52}{63}$$

$$\ell = 0.825$$

So, the percentile rank is $\boxed{0.825}$, or 82.5th percentile.

(b) We are given $\ell = 0.905$. We can use algebra to solve for i .

$$\ell = \frac{i}{n}$$

Multiply both sides by n .

$$n \cdot (\ell) = n \cdot \left(\frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate i .

$$i = (63)(0.905)$$

$$i = 57$$

Determine the x associated with $i = 57$.

$$x = \boxed{152.768}$$

(c) The mean: $\bar{x} = \frac{8879.005}{63} = \boxed{140.94}$

(d) If n is odd, then median is $x_{i=\frac{n+1}{2}}$, the value of x when $i = \frac{n+1}{2}$. Otherwise, if n is even, the median is mean of $x_{i=\frac{n}{2}}$ and $x_{i=\frac{n}{2}+1}$. In this case, $n = 63$ and so n is odd.

$$\text{median} = x_{(63+1)/2} = x_{32}$$

So, median = $\boxed{141.371}$.