1. Solution

Let x represent a datum of interest. Let i represent that datum's index. Let ℓ represent that datum's percentile. Let n represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given x = 92.56. This means i = 2. We know n = 6. Determine the percentile ℓ .

$$\ell = \frac{2}{6}$$

$$\ell = 0.333$$

So, the percentile rank is 0.333, or 33.3th percentile.

(b) We are given $\ell = 1$. We can use algebra to solve for i.

$$\ell = \frac{i}{n}$$

Multiply both sides by *n*.

$$n \cdot (\ell) = n \cdot \left(\frac{i}{n}\right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate i.

$$i = (6)(1)$$

$$i = 6$$

Determine the x associated with i = 6.

- (c) The mean: $\bar{x} = \frac{567.277}{6} = 94.546$
- (d) If n is odd, then median is $x_{i=\frac{n+1}{2}}$, the value of x when $i=\frac{n+1}{2}$. Otherwise, if n is even, the median is mean of $x_{i=\frac{n}{2}}$ and $x_{i=\frac{n}{2}+1}$. In this case, n=6 and so n is even.

$$median = \frac{x_3 + x_4}{2} = \frac{94.195 + 94.23}{2}$$

So, median = 94.2125

2. Solution

Let x represent a datum of interest. Let i represent that datum's index. Let ℓ represent that datum's percentile. Let n represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given x = 48.787. This means i = 11. We know n = 36. Determine the percentile ℓ .

$$\ell = \frac{11}{36}$$

$$\ell = 0.306$$

So, the percentile rank is 0.306, or 30.6th percentile.

(b) We are given $\ell = 0.694$. We can use algebra to solve for *i*.

$$\ell = \frac{i}{n}$$

Multiply both sides by *n*.

$$n\cdot (\ell)=n\cdot \left(\frac{i}{n}\right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate i.

$$i = (36)(0.694)$$

$$i = 25$$

Determine the x associated with i = 25.

$$x = 70.369$$

- (c) The mean: $\bar{x} = \frac{2141.341}{36} = \boxed{59.482}$
- (d) If n is odd, then median is $x_{i=\frac{n+1}{2}}$, the value of x when $i=\frac{n+1}{2}$. Otherwise, if n is even, the median is mean of $x_{i=\frac{n}{2}}$ and $x_{i=\frac{n}{2}+1}$. In this case, n=36 and so n is even.

$$\text{median} = \frac{x_{18} + x_{19}}{2} = \frac{62.632 + 62.762}{2}$$

So, median = 62.697