

1. Solution

Let x represent a datum of interest. Let i represent that datum's index. Let ℓ represent that datum's percentile. Let n represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given $x = 32.482$. This means $i = 5$. We know $n = 7$. Determine the percentile ℓ .

$$\ell = \frac{5}{7}$$

$$\ell = 0.714$$

So, the percentile rank is 0.714, or 71.4th percentile.

(b) We are given $\ell = 0.286$. We can use algebra to solve for i .

$$\ell = \frac{i}{n}$$

Multiply both sides by n .

$$n \cdot (\ell) = n \cdot \left(\frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate i .

$$i = (7)(0.286)$$

$$i = 2$$

Determine the x associated with $i = 2$.

$$x = \text{31.82}$$

(c) The mean: $\bar{x} = \frac{225.8}{7} = \text{32.257}$

(d) If n is odd, then median is $x_{i=\frac{n+1}{2}}$, the value of x when $i = \frac{n+1}{2}$. Otherwise, if n is even, the median is mean of $x_{i=\frac{n}{2}}$ and $x_{i=\frac{n}{2}+1}$. In this case, $n = 7$ and so n is odd.

$$\text{median} = x_{(7+1)/2} = x_4$$

So, median = 32.336.

2. Solution

Let x represent a datum of interest. Let i represent that datum's index. Let ℓ represent that datum's percentile. Let n represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given $x = 128.807$. This means $i = 2$. We know $n = 18$. Determine the percentile ℓ .

$$\ell = \frac{2}{18}$$

$$\ell = 0.111$$

So, the percentile rank is 0.111, or 11.1th percentile.

(b) We are given $\ell = 0.389$. We can use algebra to solve for i .

$$\ell = \frac{i}{n}$$

Multiply both sides by n .

$$n \cdot (\ell) = n \cdot \left(\frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate i .

$$i = (18)(0.389)$$

$$i = 7$$

Determine the x associated with $i = 7$.

$$x = \text{148.462}$$

(c) The mean: $\bar{x} = \frac{2752.595}{18} = \text{152.92}$

(d) If n is odd, then median is $x_{i=\frac{n+1}{2}}$, the value of x when $i = \frac{n+1}{2}$. Otherwise, if n is even, the median is mean of $x_{i=\frac{n}{2}}$ and $x_{i=\frac{n}{2}+1}$. In this case, $n = 18$ and so n is even.

$$\text{median} = \frac{x_9 + x_{10}}{2} = \frac{160.95 + 162.854}{2}$$

So, median = 161.902.