

1. Solution

Let x represent a datum of interest. Let i represent that datum's index. Let ℓ represent that datum's percentile. Let n represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given $x = 62.667$. This means $i = 2$. We know $n = 7$. Determine the percentile ℓ .

$$\ell = \frac{2}{7}$$

$$\ell = 0.286$$

So, the percentile rank is 0.286, or 28.6th percentile.

(b) We are given $\ell = 0.143$. We can use algebra to solve for i .

$$\ell = \frac{i}{n}$$

Multiply both sides by n .

$$n \cdot (\ell) = n \cdot \left(\frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate i .

$$i = (7)(0.143)$$

$$i = 1$$

Determine the x associated with $i = 1$.

$$x = \text{62.532}$$

(c) The mean: $\bar{x} = \frac{446.397}{7} = \text{63.771}$

(d) If n is odd, then median is $x_{i=\frac{n+1}{2}}$, the value of x when $i = \frac{n+1}{2}$. Otherwise, if n is even, the median is mean of $x_{i=\frac{n}{2}}$ and $x_{i=\frac{n}{2}+1}$. In this case, $n = 7$ and so n is odd.

$$\text{median} = x_{(7+1)/2} = x_4$$

So, median = 63.999.

2. Solution

Let x represent a datum of interest. Let i represent that datum's index. Let ℓ represent that datum's percentile. Let n represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given $x = 40.078$. This means $i = 3$. We know $n = 50$. Determine the percentile ℓ .

$$\ell = \frac{3}{50}$$

$$\ell = 0.06$$

So, the percentile rank is 0.06, or 6th percentile.

(b) We are given $\ell = 0.2$. We can use algebra to solve for i .

$$\ell = \frac{i}{n}$$

Multiply both sides by n .

$$n \cdot (\ell) = n \cdot \left(\frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate i .

$$i = (50)(0.2)$$

$$i = 10$$

Determine the x associated with $i = 10$.

$$x = \text{41.288}$$

(c) The mean: $\bar{x} = \frac{2494.625}{50} = \text{49.892}$

(d) If n is odd, then median is $x_{i=\frac{n+1}{2}}$, the value of x when $i = \frac{n+1}{2}$. Otherwise, if n is even, the median is mean of $x_{i=\frac{n}{2}}$ and $x_{i=\frac{n}{2}+1}$. In this case, $n = 50$ and so n is even.

$$\text{median} = \frac{x_{25} + x_{26}}{2} = \frac{51.862 + 51.893}{2}$$

So, median = 51.8775.