

**1. Solution**

Let  $x$  represent a datum of interest. Let  $i$  represent that datum's index. Let  $\ell$  represent that datum's percentile. Let  $n$  represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given  $x = 69.795$ . This means  $i = 8$ . We know  $n = 8$ . Determine the percentile  $\ell$ .

$$\ell = \frac{8}{8}$$

$$\ell = 1$$

So, the percentile rank is 1, or 100th percentile.

(b) We are given  $\ell = 0.25$ . We can use algebra to solve for  $i$ .

$$\ell = \frac{i}{n}$$

Multiply both sides by  $n$ .

$$n \cdot (\ell) = n \cdot \left( \frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate  $i$ .

$$i = (8)(0.25)$$

$$i = 2$$

Determine the  $x$  associated with  $i = 2$ .

$$x = \text{54.699}$$

(c) The mean:  $\bar{x} = \frac{502.48}{8} = \text{62.81}$

(d) If  $n$  is odd, then median is  $x_{i=\frac{n+1}{2}}$ , the value of  $x$  when  $i = \frac{n+1}{2}$ . Otherwise, if  $n$  is even, the median is mean of  $x_{i=\frac{n}{2}}$  and  $x_{i=\frac{n}{2}+1}$ . In this case,  $n = 8$  and so  $n$  is even.

$$\text{median} = \frac{x_4 + x_5}{2} = \frac{63.148 + 67.5}{2}$$

So, median = 65.324.

**2. Solution**

Let  $x$  represent a datum of interest. Let  $i$  represent that datum's index. Let  $\ell$  represent that datum's percentile. Let  $n$  represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given  $x = 38.895$ . This means  $i = 54$ . We know  $n = 64$ . Determine the percentile  $\ell$ .

$$\ell = \frac{54}{64}$$

$$\ell = 0.844$$

So, the percentile rank is  $\boxed{0.844}$ , or 84.4th percentile.

(b) We are given  $\ell = 0.766$ . We can use algebra to solve for  $i$ .

$$\ell = \frac{i}{n}$$

Multiply both sides by  $n$ .

$$n \cdot (\ell) = n \cdot \left( \frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate  $i$ .

$$i = (64)(0.766)$$

$$i = 49$$

Determine the  $x$  associated with  $i = 49$ .

$$x = \boxed{38.031}$$

(c) The mean:  $\bar{x} = \frac{2213.214}{64} = \boxed{34.581}$

(d) If  $n$  is odd, then median is  $x_{i=\frac{n+1}{2}}$ , the value of  $x$  when  $i = \frac{n+1}{2}$ . Otherwise, if  $n$  is even, the median is mean of  $x_{i=\frac{n}{2}}$  and  $x_{i=\frac{n}{2}+1}$ . In this case,  $n = 64$  and so  $n$  is even.

$$\text{median} = \frac{x_{32} + x_{33}}{2} = \frac{35.453 + 35.59}{2}$$

So, median =  $\boxed{35.5215}$ .