

**1. Problem**

A company needs to select a secretary, a manager, a CFO, and a president. Each position will be held by a different person. The company is considering the same pool of 10 applicants for each position. How many configurations are possible?

**2. Problem**

A company needs to select 4 members to be on a committee. The company is considering a pool of 12 applicants. How many committees are possible?

**3. Problem**

A traveller is packing shirts. She has 20 shirts to choose from, but will only bring 4 shirts. How many possibilities exist?

**4. Problem**

A committee is judging the performances of 24 different acrobats. The committee needs to assign 1st prize, 2nd prize, and 3rd prize. How many ways could the committee assign the prizes?

**5. Problem**

A team has 13 players. The coach needs to pick 3 starters. How many ways could the coach do this?

**6. Problem**

A basketball team has 12 players. The coach needs to pick players to fill 3 different positions. How many ways could the coach do this?

**7. Problem**

A team has 10 players. The coach will give out 2 different prizes. How many ways could the coach do this?

**8. Problem**

Joe is shopping for shirts. Joe likes 22 of the shirts, but will only buy 4 of them. How many different combinations of shirts are possible?

**9. Problem**

A landscape architect has 2 spots to plant 2 different trees. The landscape architect has 22 different trees available. How many configurations are possible?

**10. Problem**

A company needs to select 3 members to be on a committee. The company is considering a pool of 12 applicants. How many committees are possible?

**11. Problem**

A team has 11 players. The coach will give out 5 different prizes. How many ways could the coach do this?

**12. Problem**

A designer is choosing a color palette. There are 12 colors available, but the designer will only choose 5 colors for her palette. How many palettes are possible?

1. This scenario describes a permutations problem (order matters). We are considering the nonrepeating sequences of size 4 from a set of size 10.

$${}_nP_r = \frac{n!}{(n-r)!}$$

$$n = 10$$

$$r = 4$$

$${}_{10}P_4 = \frac{10!}{(10-4)!}$$

$$= \frac{10!}{6!}$$

$$= 10 \cdot 9 \cdot 8 \cdot 7$$

$$= \boxed{5040}$$

2. This scenario describes a combinations problem (order does not matter). We are considering the subsets of size 4 from a set of size 12.

$${}_nC_r = \frac{n!}{(n-r)! \cdot r!}$$

$$n = 12$$

$$r = 4$$

$${}_{12}C_4 = \frac{12!}{(12-4)! \cdot 4!}$$

$$= \frac{12!}{8! \cdot 4!}$$

$$= \frac{12 \cdot 11 \cdot 10 \cdot 9}{4 \cdot 3 \cdot 2 \cdot 1}$$

$$= \boxed{495}$$

3. This scenario describes a combinations problem (order does not matter). We are considering the subsets of size 4 from a set of size 20.

$${}_nC_r = \frac{n!}{(n-r)! \cdot r!}$$

$$n = 20$$

$$r = 4$$

$${}_{20}C_4 = \frac{20!}{(20-4)! \cdot 4!}$$

$$= \frac{20!}{16! \cdot 4!}$$

$$= \frac{20 \cdot 19 \cdot 18 \cdot 17}{4 \cdot 3 \cdot 2 \cdot 1}$$

$$= \boxed{4845}$$

4. This scenario describes a permutations problem (order matters). We are considering the nonrepeating sequences of size 3 from a set of size 24.

$${}_nP_r = \frac{n!}{(n-r)!}$$

$$n = 24$$

$$r = 3$$

$${}_{24}P_3 = \frac{24!}{(24-3)!}$$

$$= \frac{24!}{21!}$$

$$= 24 \cdot 23 \cdot 22$$

$$= \boxed{12144}$$



5. This scenario describes a combinations problem (order does not matter). We are considering the subsets of size 3 from a set of size 13.

$${}_nC_r = \frac{n!}{(n-r)! \cdot r!}$$

$$n = 13$$

$$r = 3$$

$${}_{13}C_3 = \frac{13!}{(13-3)! \cdot 3!}$$

$$= \frac{13!}{10! \cdot 3!}$$

$$= \frac{13 \cdot 12 \cdot 11}{3 \cdot 2 \cdot 1}$$

$$= \boxed{286}$$

6. This scenario describes a permutations problem (order matters). We are considering the nonrepeating sequences of size 3 from a set of size 12.

$${}_nP_r = \frac{n!}{(n-r)!}$$

$$n = 12$$

$$r = 3$$

$${}_{12}P_3 = \frac{12!}{(12-3)!}$$

$$= \frac{12!}{9!}$$

$$= 12 \cdot 11 \cdot 10$$

$$= \boxed{1320}$$

7. This scenario describes a permutations problem (order matters). We are considering the nonrepeating sequences of size 2 from a set of size 10.

$${}_nP_r = \frac{n!}{(n-r)!}$$

$$n = 10$$

$$r = 2$$

$${}_{10}P_2 = \frac{10!}{(10-2)!}$$

$$= \frac{10!}{8!}$$

$$= 10 \cdot 9$$

$$= \boxed{90}$$

8. This scenario describes a combinations problem (order does not matter). We are considering the subsets of size 4 from a set of size 22.

$${}_nC_r = \frac{n!}{(n-r)! \cdot r!}$$

$$n = 22$$

$$r = 4$$

$${}_{22}C_4 = \frac{22!}{(22-4)! \cdot 4!}$$

$$= \frac{22!}{18! \cdot 4!}$$

$$= \frac{22 \cdot 21 \cdot 20 \cdot 19}{4 \cdot 3 \cdot 2 \cdot 1}$$

$$= \boxed{7315}$$

9. This scenario describes a permutations problem (order matters). We are considering the nonrepeating sequences of size 2 from a set of size 22.

$${}_nP_r = \frac{n!}{(n-r)!}$$

$$n = 22$$

$$r = 2$$

$${}_{22}P_2 = \frac{22!}{(22-2)!}$$

$$= \frac{22!}{20!}$$

$$= 22 \cdot 21$$

$$= \boxed{462}$$

10. This scenario describes a combinations problem (order does not matter). We are considering the subsets of size 3 from a set of size 12.

$${}_nC_r = \frac{n!}{(n-r)! \cdot r!}$$

$$n = 12$$

$$r = 3$$

$${}_{12}C_3 = \frac{12!}{(12-3)! \cdot 3!}$$

$$= \frac{12!}{9! \cdot 3!}$$

$$= \frac{12 \cdot 11 \cdot 10}{3 \cdot 2 \cdot 1}$$

$$= \boxed{220}$$

11. This scenario describes a permutations problem (order matters). We are considering the nonrepeating sequences of size 5 from a set of size 11.

$${}_nP_r = \frac{n!}{(n-r)!}$$

$$n = 11$$

$$r = 5$$

$${}_{11}P_5 = \frac{11!}{(11-5)!}$$

$$= \frac{11!}{6!}$$

$$= 11 \cdot 10 \cdot 9 \cdot 8 \cdot 7$$

$$= \boxed{55440}$$

12. This scenario describes a combinations problem (order does not matter). We are considering the subsets of size 5 from a set of size 12.

$${}_nC_r = \frac{n!}{(n-r)! \cdot r!}$$

$$n = 12$$

$$r = 5$$

$${}_{12}C_5 = \frac{12!}{(12-5)! \cdot 5!}$$

$$= \frac{12!}{7! \cdot 5!}$$

$$= \frac{12 \cdot 11 \cdot 10 \cdot 9 \cdot 8}{5 \cdot 4 \cdot 3 \cdot 2 \cdot 1}$$

$$= \boxed{792}$$