

**1. Solution**

Let  $x$  represent a datum of interest. Let  $i$  represent that datum's index. Let  $\ell$  represent that datum's percentile. Let  $n$  represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given  $x = 76.29$ . This means  $i = 5$ . We know  $n = 6$ . Determine the percentile  $\ell$ .

$$\ell = \frac{5}{6}$$

$$\ell = 0.833$$

So, the percentile rank is 0.833, or 83.3th percentile.

(b) We are given  $\ell = 1$ . We can use algebra to solve for  $i$ .

$$\ell = \frac{i}{n}$$

Multiply both sides by  $n$ .

$$n \cdot (\ell) = n \cdot \left( \frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate  $i$ .

$$i = (6)(1)$$

$$i = 6$$

Determine the  $x$  associated with  $i = 6$ .

$$x = \text{79.444}$$

(c) The mean:  $\bar{x} = \frac{390.534}{6} = \text{65.089}$

(d) If  $n$  is odd, then median is  $x_{i=\frac{n+1}{2}}$ , the value of  $x$  when  $i = \frac{n+1}{2}$ . Otherwise, if  $n$  is even, the median is mean of  $x_{i=\frac{n}{2}}$  and  $x_{i=\frac{n}{2}+1}$ . In this case,  $n = 6$  and so  $n$  is even.

$$\text{median} = \frac{x_3 + x_4}{2} = \frac{67.358 + 74.857}{2}$$

So, median = 71.1075.

**2. Solution**

Let  $x$  represent a datum of interest. Let  $i$  represent that datum's index. Let  $\ell$  represent that datum's percentile. Let  $n$  represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given  $x = 44.077$ . This means  $i = 32$ . We know  $n = 56$ . Determine the percentile  $\ell$ .

$$\ell = \frac{32}{56}$$

$$\ell = 0.571$$

So, the percentile rank is  $\boxed{0.571}$ , or 57.1th percentile.

(b) We are given  $\ell = 0.804$ . We can use algebra to solve for  $i$ .

$$\ell = \frac{i}{n}$$

Multiply both sides by  $n$ .

$$n \cdot (\ell) = n \cdot \left( \frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate  $i$ .

$$i = (56)(0.804)$$

$$i = 45$$

Determine the  $x$  associated with  $i = 45$ .

$$x = \boxed{44.594}$$

(c) The mean:  $\bar{x} = \frac{2440.719}{56} = \boxed{43.584}$

(d) If  $n$  is odd, then median is  $x_{i=\frac{n+1}{2}}$ , the value of  $x$  when  $i = \frac{n+1}{2}$ . Otherwise, if  $n$  is even, the median is mean of  $x_{i=\frac{n}{2}}$  and  $x_{i=\frac{n}{2}+1}$ . In this case,  $n = 56$  and so  $n$  is even.

$$\text{median} = \frac{x_{28} + x_{29}}{2} = \frac{43.916 + 43.927}{2}$$

So, median =  $\boxed{43.9215}$ .