

1. Solution

Let x represent a datum of interest. Let i represent that datum's index. Let ℓ represent that datum's percentile. Let n represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given $x = 21.563$. This means $i = 1$. We know $n = 6$. Determine the percentile ℓ .

$$\ell = \frac{1}{6}$$

$$\ell = 0.167$$

So, the percentile rank is $\boxed{0.167}$, or 16.7th percentile.

(b) We are given $\ell = 0.333$. We can use algebra to solve for i .

$$\ell = \frac{i}{n}$$

Multiply both sides by n .

$$n \cdot (\ell) = n \cdot \left(\frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate i .

$$i = (6)(0.333)$$

$$i = 2$$

Determine the x associated with $i = 2$.

$$x = \boxed{27.973}$$

(c) The mean: $\bar{x} = \frac{171.605}{6} = \boxed{28.601}$

(d) If n is odd, then median is $x_{i=\frac{n+1}{2}}$, the value of x when $i = \frac{n+1}{2}$. Otherwise, if n is even, the median is mean of $x_{i=\frac{n}{2}}$ and $x_{i=\frac{n}{2}+1}$. In this case, $n = 6$ and so n is even.

$$\text{median} = \frac{x_3 + x_4}{2} = \frac{29.211 + 30.211}{2}$$

So, median = $\boxed{29.711}$.

2. Solution

Let x represent a datum of interest. Let i represent that datum's index. Let ℓ represent that datum's percentile. Let n represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given $x = 51.558$. This means $i = 11$. We know $n = 28$. Determine the percentile ℓ .

$$\ell = \frac{11}{28}$$

$$\ell = 0.393$$

So, the percentile rank is $\boxed{0.393}$, or 39.3th percentile.

(b) We are given $\ell = 0.786$. We can use algebra to solve for i .

$$\ell = \frac{i}{n}$$

Multiply both sides by n .

$$n \cdot (\ell) = n \cdot \left(\frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate i .

$$i = (28)(0.786)$$

$$i = 22$$

Determine the x associated with $i = 22$.

$$x = \boxed{54.293}$$

(c) The mean: $\bar{x} = \frac{1469.418}{28} = \boxed{52.479}$

(d) If n is odd, then median is $x_{i=\frac{n+1}{2}}$, the value of x when $i = \frac{n+1}{2}$. Otherwise, if n is even, the median is mean of $x_{i=\frac{n}{2}}$ and $x_{i=\frac{n}{2}+1}$. In this case, $n = 28$ and so n is even.

$$\text{median} = \frac{x_{14} + x_{15}}{2} = \frac{52.13 + 52.179}{2}$$

So, median = $\boxed{52.1545}$.