

1. Problem

Let random variable W have mean $\mu_W = 11$ and standard deviation $\sigma_W = 2$. Let random variable X represent the **sum** of $n = 169$ instances of W .

- (a) Determine the expected value of X . $\mu_X = ?$
- (b) Determine the standard deviation of X . $\sigma_X = ?$
- (c) Using normal approximation, determine $P(X < 1884.74)$.
- (d) Using normal approximation, determine $P(X > 1878.76)$.
- (e) Using normal approximation, determine $P(|X - \mu_X| < 11.96)$.
- (f) Using normal approximation, determine $P(|X - \mu_X| > 4.42)$.

2. Problem

Let random variable W have mean $\mu_W = 22$ and standard deviation $\sigma_W = 3$. Let random variable X represent the **sum** of $n = 81$ instances of W .

- (a) Determine the expected value of X . $\mu_X = ?$
- (b) Determine the standard deviation of X . $\sigma_X = ?$
- (c) Using normal approximation, determine $P(X < 1773.63)$.
- (d) Using normal approximation, determine $P(X > 1762.02)$.
- (e) Using normal approximation, determine $P(|X - \mu_X| < 29.43)$.
- (f) Using normal approximation, determine $P(|X - \mu_X| > 33.21)$.

3. Problem

Let random variable W have mean $\mu_W = 39$ and standard deviation $\sigma_W = 9$. Let random variable X represent the **average** of $n = 196$ instances of W .

- (a) Determine the expected value of X . $\mu_X = ?$
- (b) Determine the standard deviation of X . $\sigma_X = ?$
- (c) Using normal approximation, determine $P(X < 38.93)$.
- (d) Using normal approximation, determine $P(X > 39.35)$.
- (e) Using normal approximation, determine $P(|X - \mu_X| < 0.2636)$.
- (f) Using normal approximation, determine $P(|X - \mu_X| > 0.18)$.

4. Problem

Let random variable W have mean $\mu_W = 45$ and standard deviation $\sigma_W = 14$. Let random variable X represent the **average** of $n = 100$ instances of W .

- (a) Determine the expected value of X . $\mu_X = ?$
- (b) Determine the standard deviation of X . $\sigma_X = ?$
- (c) Using normal approximation, determine $P(X < 46.3)$.
- (d) Using normal approximation, determine $P(X > 45.71)$.
- (e) Using normal approximation, determine $P(|X - \mu_X| < 2.282)$.
- (f) Using normal approximation, determine $P(|X - \mu_X| > 1.246)$.

5. Problem

Let random variable W have mean $\mu_W = 11$ and standard deviation $\sigma_W = 2$. Let random variable X represent the **sum** of $n = 225$ instances of W .

- (a) Determine the expected value of X . $\mu_X = ?$
- (b) Determine the standard deviation of X . $\sigma_X = ?$
- (c) Using normal approximation, determine $P(X < 2452.8)$.
- (d) Using normal approximation, determine $P(X > 2521.8)$.
- (e) Using normal approximation, determine $P(|X - \mu_X| < 20.4)$.
- (f) Using normal approximation, determine $P(|X - \mu_X| > 27)$.

6. Problem

Let random variable W have mean $\mu_W = 58$ and standard deviation $\sigma_W = 19$. Let random variable X represent the **average** of $n = 225$ instances of W .

- (a) Determine the expected value of X . $\mu_X = ?$
- (b) Determine the standard deviation of X . $\sigma_X = ?$
- (c) Using normal approximation, determine $P(X < 59.79)$.
- (d) Using normal approximation, determine $P(X > 58.09)$.
- (e) Using normal approximation, determine $P(|X - \mu_X| < 0.5573)$.
- (f) Using normal approximation, determine $P(|X - \mu_X| > 0.722)$.

7. Problem

Let random variable W have mean $\mu_W = 9$ and standard deviation $\sigma_W = 2$. Let random variable X represent the **average** of $n = 36$ instances of W .

- (a) Determine the expected value of X . $\mu_X = ?$
- (b) Determine the standard deviation of X . $\sigma_X = ?$
- (c) Using normal approximation, determine $P(X < 8.56)$.
- (d) Using normal approximation, determine $P(X > 9.07)$.
- (e) Using normal approximation, determine $P(|X - \mu_X| < 0.2467)$.
- (f) Using normal approximation, determine $P(|X - \mu_X| > 0.2167)$.

8. Problem

Let random variable W have mean $\mu_W = 57$ and standard deviation $\sigma_W = 17$. Let random variable X represent the **sum** of $n = 169$ instances of W .

- (a) Determine the expected value of X . $\mu_X = ?$
- (b) Determine the standard deviation of X . $\sigma_X = ?$
- (c) Using normal approximation, determine $P(X < 9535.76)$.
- (d) Using normal approximation, determine $P(X > 9593.22)$.
- (e) Using normal approximation, determine $P(|X - \mu_X| < 112.71)$.
- (f) Using normal approximation, determine $P(|X - \mu_X| > 316.03)$.

9. Problem

Let random variable W have mean $\mu_W = 57$ and standard deviation $\sigma_W = 13$. Let random variable X represent the **average** of $n = 49$ instances of W .

- (a) Determine the expected value of X . $\mu_X = ?$
- (b) Determine the standard deviation of X . $\sigma_X = ?$
- (c) Using normal approximation, determine $P(X < 55.83)$.
- (d) Using normal approximation, determine $P(X > 56.05)$.
- (e) Using normal approximation, determine $P(|X - \mu_X| < 1.0214)$.
- (f) Using normal approximation, determine $P(|X - \mu_X| > 0.7243)$.

10. Problem

Let random variable W have mean $\mu_W = 40$ and standard deviation $\sigma_W = 2$. Let random variable X represent the **sum** of $n = 81$ instances of W .

- (a) Determine the expected value of X . $\mu_X = ?$
- (b) Determine the standard deviation of X . $\sigma_X = ?$
- (c) Using normal approximation, determine $P(X < 3245.04)$.
- (d) Using normal approximation, determine $P(X > 3236.4)$.
- (e) Using normal approximation, determine $P(|X - \mu_X| < 13.86)$.
- (f) Using normal approximation, determine $P(|X - \mu_X| > 12.96)$.

11. Problem

Let random variable W have mean $\mu_W = 59$ and standard deviation $\sigma_W = 17$. Let random variable X represent the **average** of $n = 64$ instances of W .

- (a) Determine the expected value of X . $\mu_X = ?$
- (b) Determine the standard deviation of X . $\sigma_X = ?$
- (c) Using normal approximation, determine $P(X < 56.2)$.
- (d) Using normal approximation, determine $P(X > 58.72)$.
- (e) Using normal approximation, determine $P(|X - \mu_X| < 0.17)$.
- (f) Using normal approximation, determine $P(|X - \mu_X| > 0.9775)$.

12. Problem

Let random variable W have mean $\mu_W = 27$ and standard deviation $\sigma_W = 5$. Let random variable X represent the **sum** of $n = 144$ instances of W .

- (a) Determine the expected value of X . $\mu_X = ?$
- (b) Determine the standard deviation of X . $\sigma_X = ?$
- (c) Using normal approximation, determine $P(X < 3886.2)$.
- (d) Using normal approximation, determine $P(X > 3895.2)$.
- (e) Using normal approximation, determine $P(|X - \mu_X| < 54)$.
- (f) Using normal approximation, determine $P(|X - \mu_X| > 95.4)$.

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|-------------|-------------|--------------|
| 1. (a) 1859 | 5. (a) 2475 | 9. (a) 57 |
| (b) 26 | (b) 30 | (b) 1.8571 |
| (c) 0.8389 | (c) 0.2296 | (c) 0.2643 |
| (d) 0.2236 | (d) 0.0594 | (d) 0.7357 |
| (e) 0.3545 | (e) 0.5035 | (e) 0.4177 |
| (f) 0.865 | (f) 0.3681 | (f) 0.6965 |
| 2. (a) 1782 | 6. (a) 58 | 10. (a) 3240 |
| (b) 27 | (b) 1.2667 | (b) 18 |
| (c) 0.3783 | (c) 0.9207 | (c) 0.6103 |
| (d) 0.7704 | (d) 0.0793 | (d) 0.5793 |
| (e) 0.7243 | (e) 0.3401 | (e) 0.5587 |
| (f) 0.2187 | (f) 0.5687 | (f) 0.4715 |
| 3. (a) 39 | 7. (a) 9 | 11. (a) 59 |
| (b) 0.6429 | (b) 0.3333 | (b) 2.125 |
| (c) 0.4562 | (c) 0.0951 | (c) 0.0934 |
| (d) 0.5438 | (d) 0.9049 | (d) 0.9066 |
| (e) 0.3182 | (e) 0.5407 | (e) 0.0638 |
| (f) 0.7795 | (f) 0.5157 | (f) 0.6455 |
| 4. (a) 45 | 8. (a) 9633 | 12. (a) 3888 |
| (b) 1.4 | (b) 221 | (b) 60 |
| (c) 0.8238 | (c) 0.33 | (c) 0.488 |
| (d) 0.1762 | (d) 0.5714 | (d) 0.4522 |
| (e) 0.8969 | (e) 0.3899 | (e) 0.6319 |
| (f) 0.3735 | (f) 0.1527 | (f) 0.1118 |