

**1. Solution**

Let  $x$  represent a datum of interest. Let  $i$  represent that datum's index. Let  $\ell$  represent that datum's percentile. Let  $n$  represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given  $x = 86.975$ . This means  $i = 3$ . We know  $n = 10$ . Determine the percentile  $\ell$ .

$$\ell = \frac{3}{10}$$

$$\ell = 0.3$$

So, the percentile rank is  $\boxed{0.3}$ , or 30th percentile.

(b) We are given  $\ell = 0.4$ . We can use algebra to solve for  $i$ .

$$\ell = \frac{i}{n}$$

Multiply both sides by  $n$ .

$$n \cdot (\ell) = n \cdot \left( \frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate  $i$ .

$$i = (10)(0.4)$$

$$i = 4$$

Determine the  $x$  associated with  $i = 4$ .

$$x = \boxed{88.376}$$

(c) The mean:  $\bar{x} = \frac{982.643}{10} = \boxed{98.264}$

(d) If  $n$  is odd, then median is  $x_{i=\frac{n+1}{2}}$ , the value of  $x$  when  $i = \frac{n+1}{2}$ . Otherwise, if  $n$  is even, the median is mean of  $x_{i=\frac{n}{2}}$  and  $x_{i=\frac{n}{2}+1}$ . In this case,  $n = 10$  and so  $n$  is even.

$$\text{median} = \frac{x_5 + x_6}{2} = \frac{88.744 + 90.028}{2}$$

So, median =  $\boxed{89.386}$ .

**2. Solution**

Let  $x$  represent a datum of interest. Let  $i$  represent that datum's index. Let  $\ell$  represent that datum's percentile. Let  $n$  represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given  $x = 13.209$ . This means  $i = 1$ . We know  $n = 28$ . Determine the percentile  $\ell$ .

$$\ell = \frac{1}{28}$$

$$\ell = 0.0357$$

So, the percentile rank is 0.0357, or 3.57th percentile.

(b) We are given  $\ell = 0.321$ . We can use algebra to solve for  $i$ .

$$\ell = \frac{i}{n}$$

Multiply both sides by  $n$ .

$$n \cdot (\ell) = n \cdot \left( \frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate  $i$ .

$$i = (28)(0.321)$$

$$i = 9$$

Determine the  $x$  associated with  $i = 9$ .

$$x = \text{14.687}$$

(c) The mean:  $\bar{x} = \frac{423.481}{28} = \text{15.124}$

(d) If  $n$  is odd, then median is  $x_{i=\frac{n+1}{2}}$ , the value of  $x$  when  $i = \frac{n+1}{2}$ . Otherwise, if  $n$  is even, the median is mean of  $x_{i=\frac{n}{2}}$  and  $x_{i=\frac{n}{2}+1}$ . In this case,  $n = 28$  and so  $n$  is even.

$$\text{median} = \frac{x_{14} + x_{15}}{2} = \frac{14.999 + 15.176}{2}$$

So, median = 15.0875.