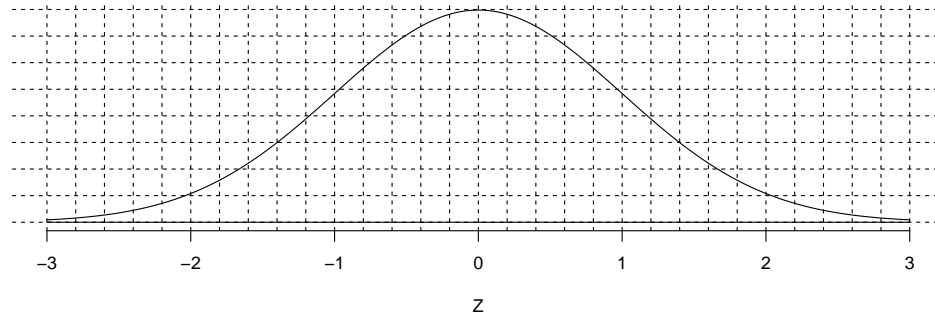


**1. Problem:**

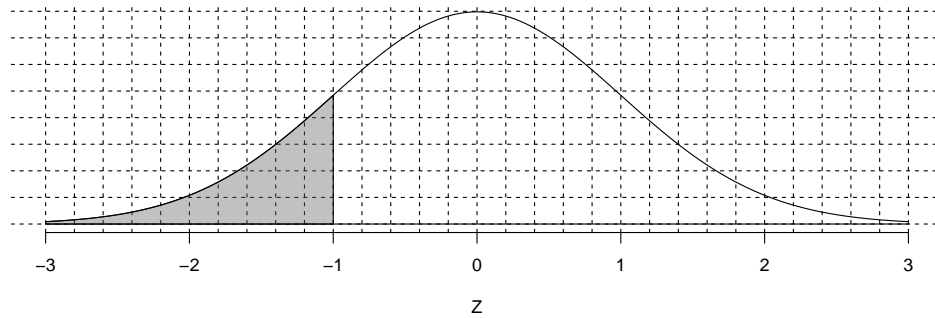
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(Z < -1)$  by shading and counting.
- (b) Determine  $P(Z < -1)$  by using the z-table.

**Solution:**

(a) The shaded region is shown below.

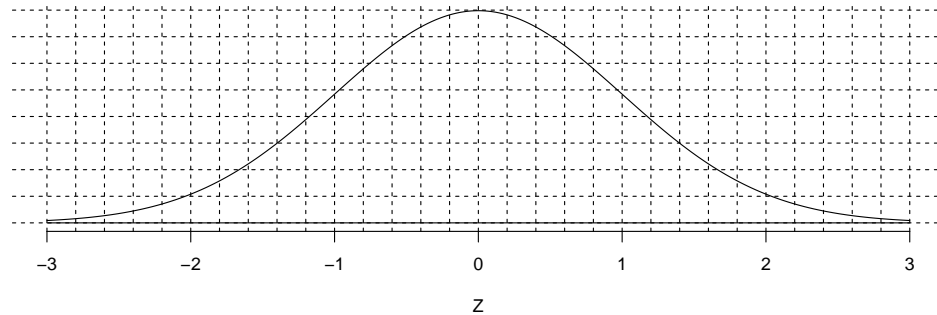


You should count about 16 shaded squares, giving a probability of about 0.16.

(b) The probability is 0.1587.

**2. Problem:**

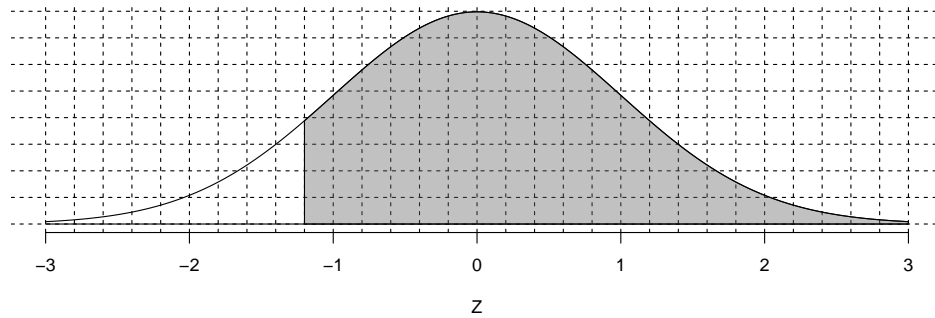
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(Z > -1.2)$  by shading and counting.
- (b) Determine  $P(Z > -1.2)$  by using the z-table.

**Solution:**

(a) The shaded region is shown below.

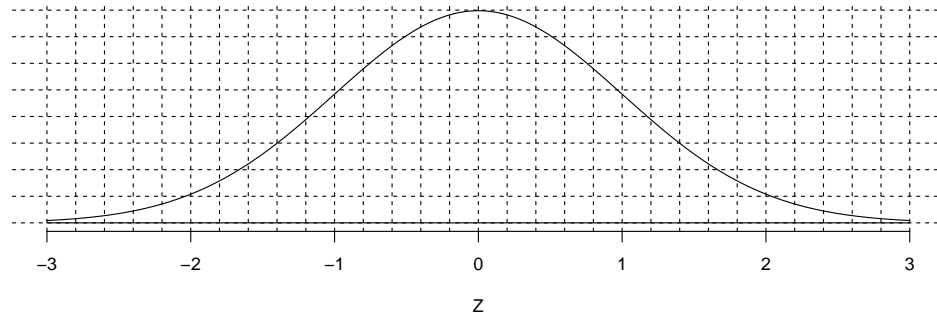


You should count about 88 shaded squares, giving a probability of about 0.88.

(b) The probability is 0.8849.

**3. Problem:**

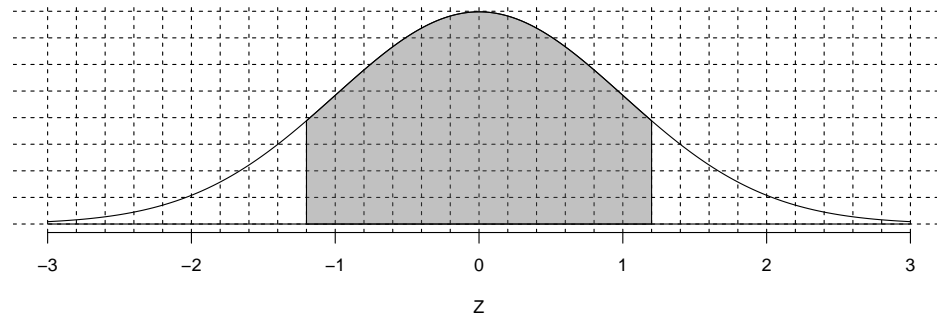
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(|Z| < 1.2)$  by shading and counting.
- (b) Determine  $P(|Z| < 1.2)$  by using the z-table.

**Solution:**

(a) The shaded region is shown below.

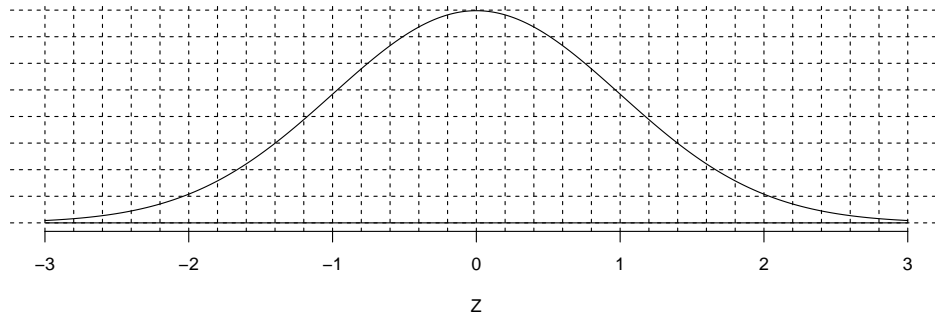


You should count about 77 shaded squares, giving a probability of about 0.77.

(b) The probability is 0.7699.

**4. Problem:**

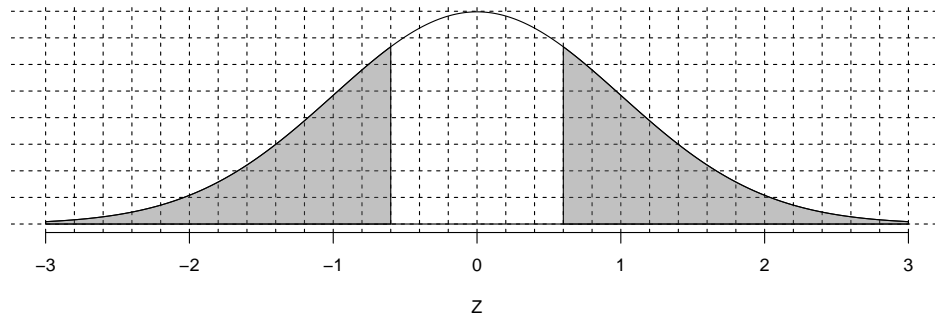
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(|Z| > 0.6)$  by shading and counting.
- (b) Determine  $P(|Z| > 0.6)$  by using the z-table.

**Solution:**

(a) The shaded regions are shown below.



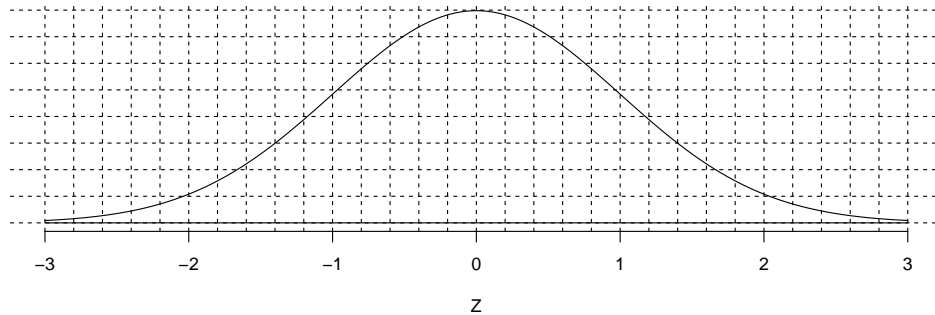
You should count about 55 shaded squares, giving a probability of about 0.55.

(b) The probability is 0.5485.



**5. Problem:**

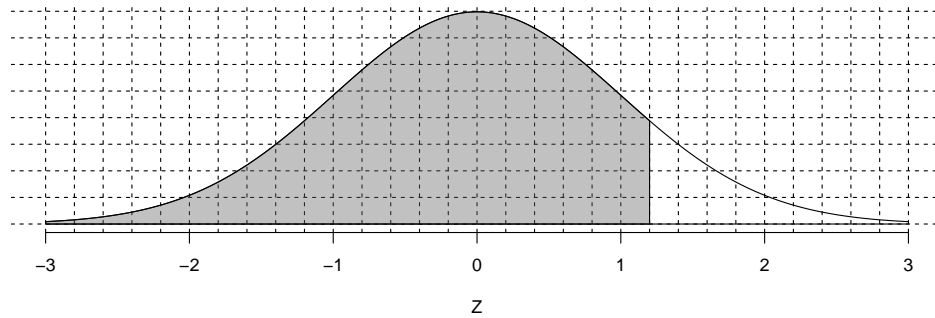
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(Z < z) = 0.88$  by shading and counting.
- (b) Determine  $z$  such that  $P(Z < z) = 0.88$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

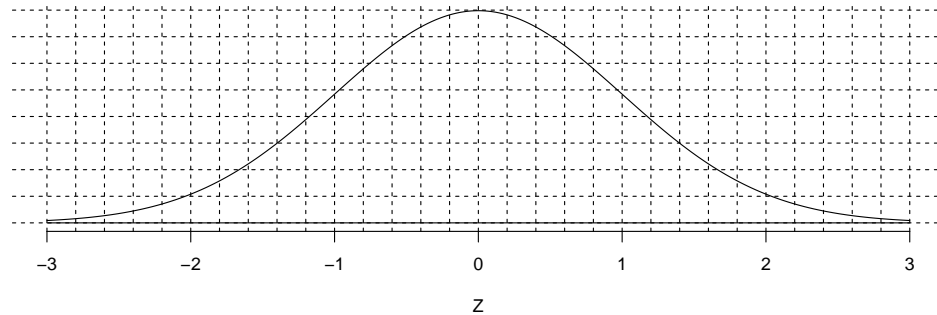


When you have shaded 88 squares, starting on the left, you should end around  $z = 1.2$ .

(b)  $z \approx 1.17$

**6. Problem:**

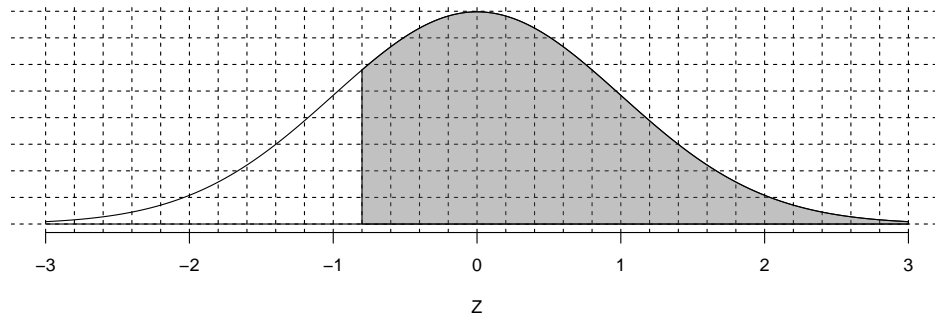
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(Z > z) = 0.79$  by shading and counting.
- (b) Determine  $z$  such that  $P(Z > z) = 0.79$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

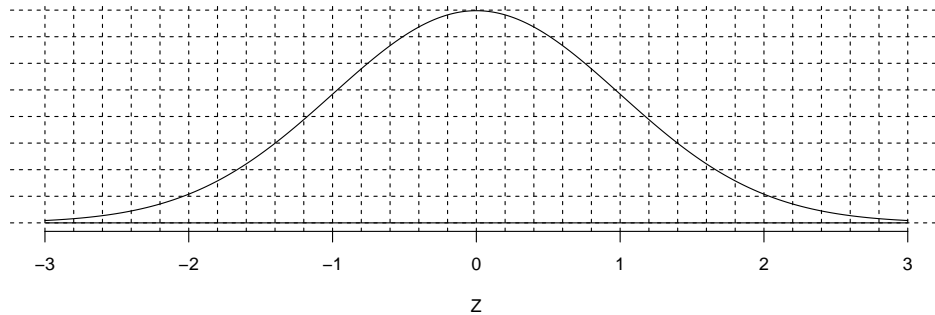


When you have shaded 79 squares, starting on the right, you should end around  $z = -0.8$ .

(b)  $z = 0.81$

**7. Problem:**

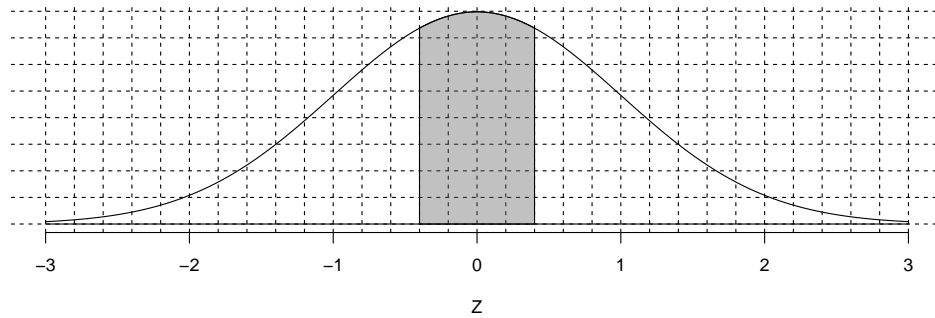
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(|Z| < z) = 0.31$  by shading and counting.
- (b) Determine  $z$  such that  $P(|Z| < z) = 0.31$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

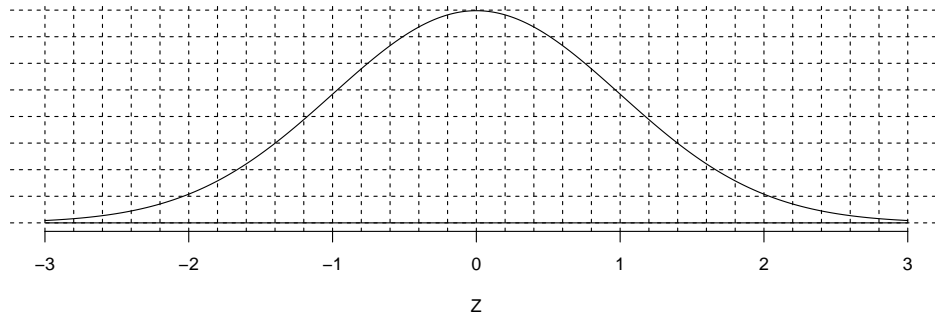


When you have shaded 31 squares, starting in the middle, you should end near  $z = 0.4$ .

(b)  $z = -0.5$

**8. Problem:**

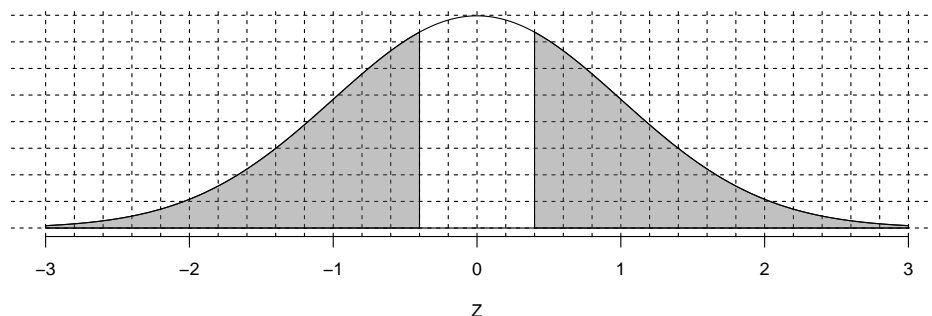
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(|Z| > z) = 0.69$  by shading and counting.
- (b) Determine  $z$  such that  $P(|Z| > z) = 0.69$  by using the  $z$ -table.

**Solution:**

- (a) The shaded regions are shown below.



When you have shaded 69 squares, starting at both tails, you should end near  $z = 0.4$ . Really, you want to shade 34.5 squares starting from the left and also 34.5 squares starting from the right.

- (b) Each tail has half the two-tail area. So each tail has an area of 0.345. We can find the  $z$  score with this left area...

$$z_{\text{left tail}} = -0.4$$

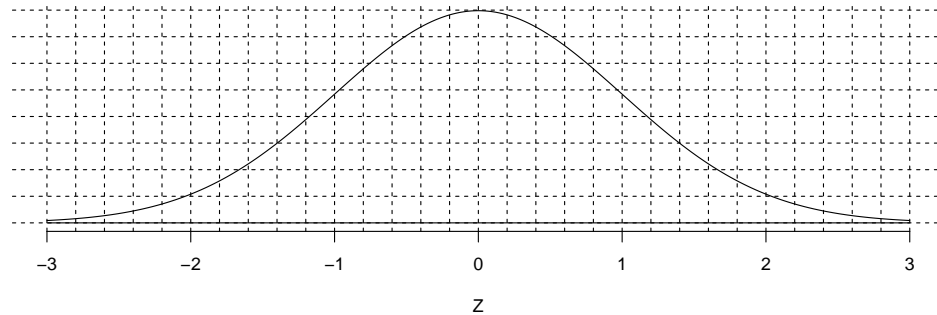
But, we want the positive value (the right tail's  $z$  boundary).

$$z = \boxed{0.4}$$



**9. Problem:**

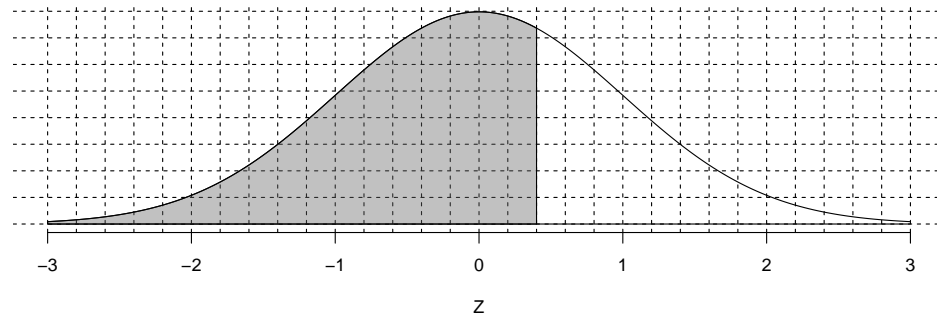
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(Z < z) = 0.66$  by shading and counting.
- (b) Determine  $z$  such that  $P(Z < z) = 0.66$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

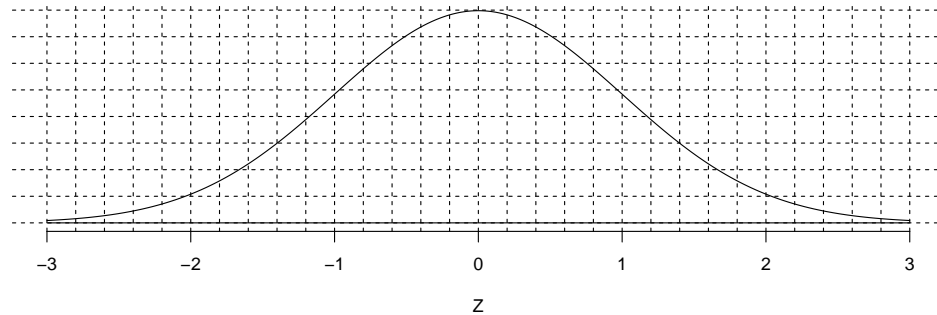


When you have shaded 66 squares, starting on the left, you should end around  $z = 0.4$ .

(b)  $z \approx 0.41$

10. **Problem:**

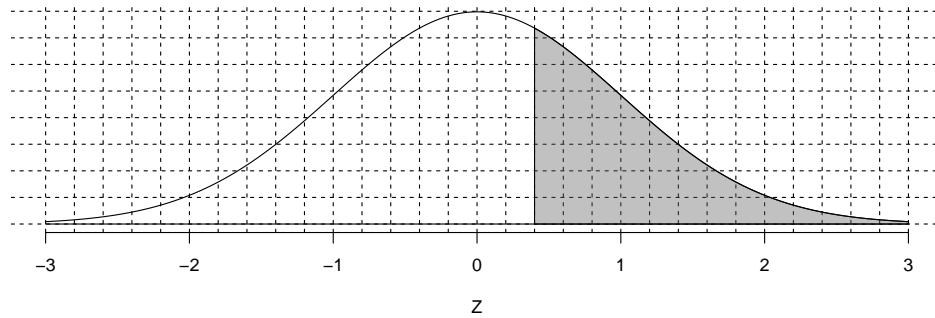
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(Z > z) = 0.34$  by shading and counting.
- (b) Determine  $z$  such that  $P(Z > z) = 0.34$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

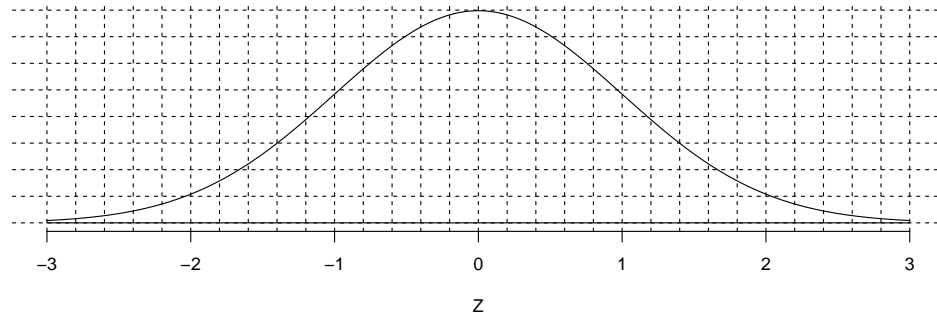


When you have shaded 34 squares, starting on the right, you should end around  $z = 0.4$ .

(b)  $z = -0.41$

11. **Problem:**

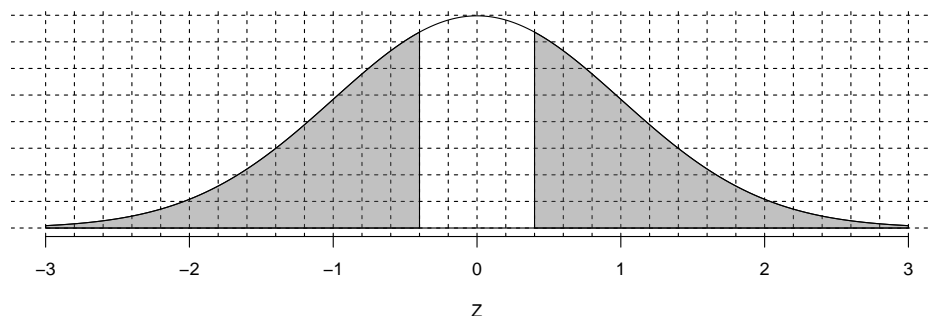
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(|Z| > z) = 0.69$  by shading and counting.
- (b) Determine  $z$  such that  $P(|Z| > z) = 0.69$  by using the  $z$ -table.

**Solution:**

- (a) The shaded regions are shown below.



When you have shaded 69 squares, starting at both tails, you should end near  $z = 0.4$ . Really, you want to shade 34.5 squares starting from the left and also 34.5 squares starting from the right.

- (b) Each tail has half the two-tail area. So each tail has an area of 0.345. We can find the  $z$  score with this left area. . .

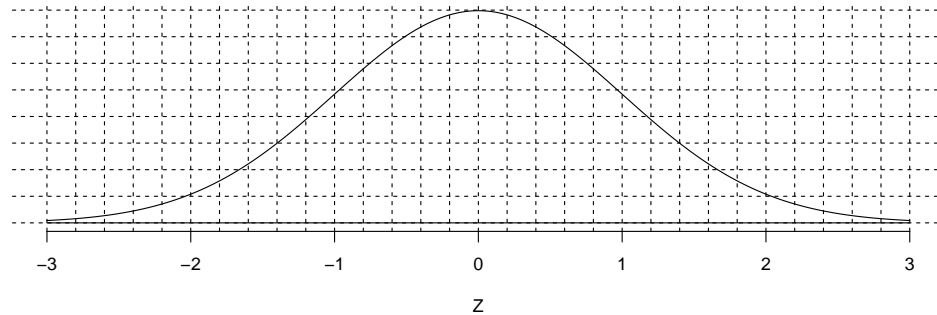
$$z_{\text{left tail}} = -0.4$$

But, we want the positive value (the right tail's  $z$  boundary).

$$z = \boxed{0.4}$$

**12. Problem:**

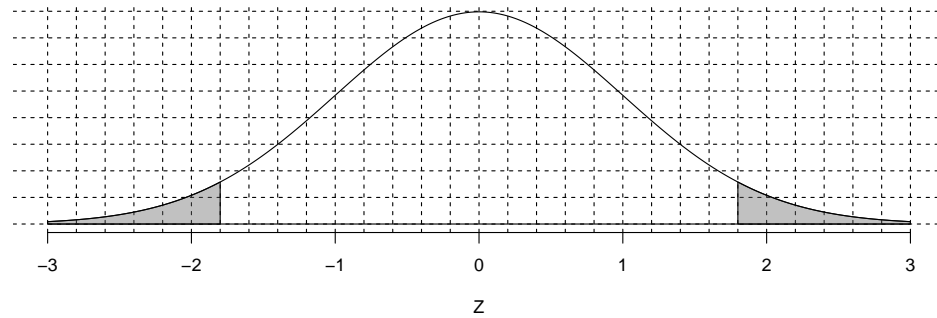
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(|Z| > 1.8)$  by shading and counting.
- (b) Determine  $P(|Z| > 1.8)$  by using the z-table.

**Solution:**

(a) The shaded regions are shown below.



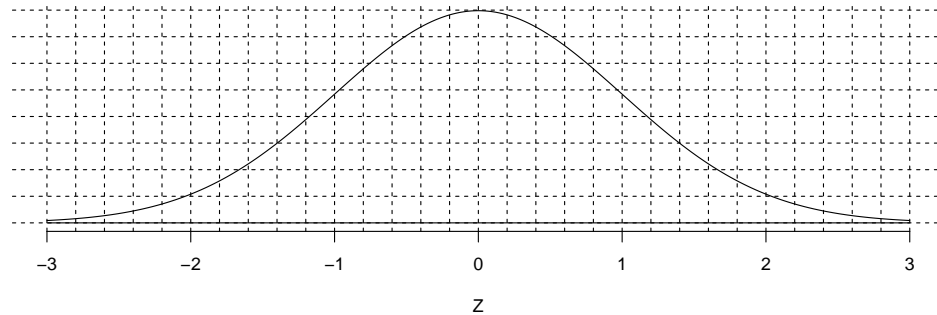
You should count about 7 shaded squares, giving a probability of about 0.07.

(b) The probability is 0.0719.



**13. Problem:**

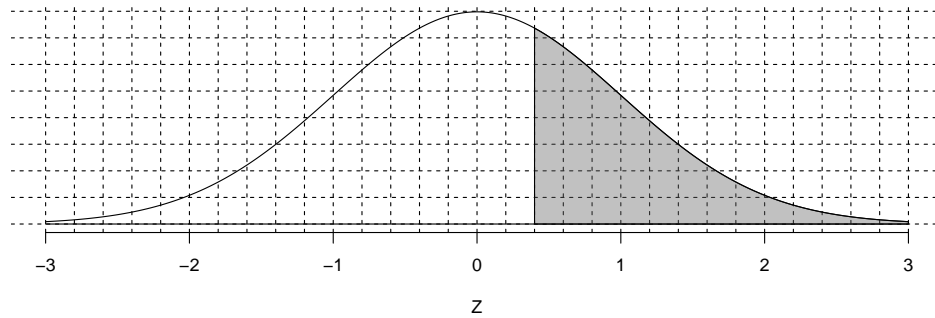
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(Z > z) = 0.34$  by shading and counting.
- (b) Determine  $z$  such that  $P(Z > z) = 0.34$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

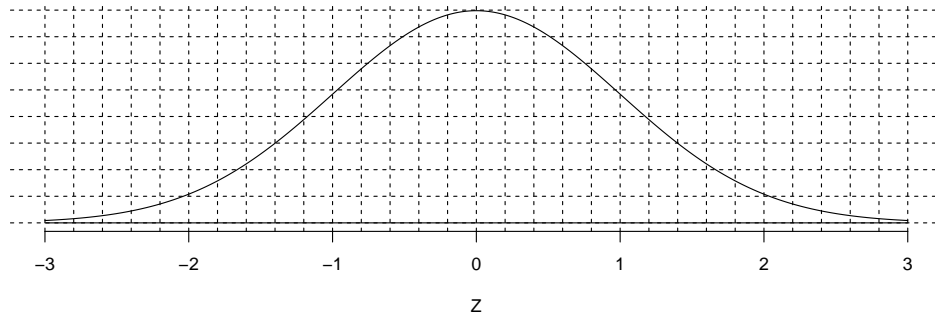


When you have shaded 34 squares, starting on the right, you should end around  $z = 0.4$ .

(b)  $z = -0.41$

**14. Problem:**

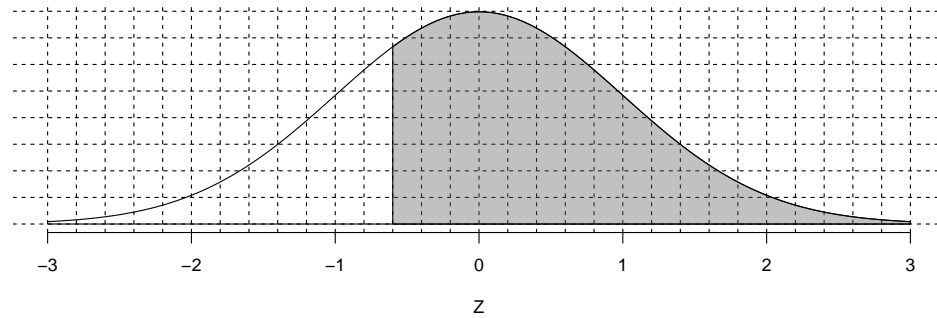
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(Z > z) = 0.73$  by shading and counting.
- (b) Determine  $z$  such that  $P(Z > z) = 0.73$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

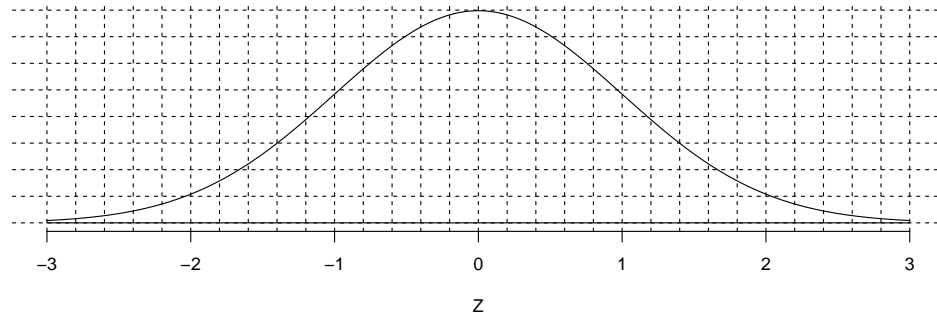


When you have shaded 73 squares, starting on the right, you should end around  $z = -0.6$ .

(b)  $z = 0.61$

**15. Problem:**

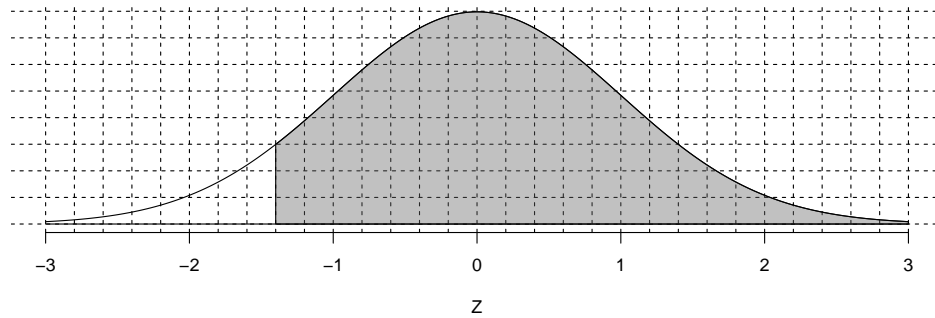
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(Z > z) = 0.92$  by shading and counting.
- (b) Determine  $z$  such that  $P(Z > z) = 0.92$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

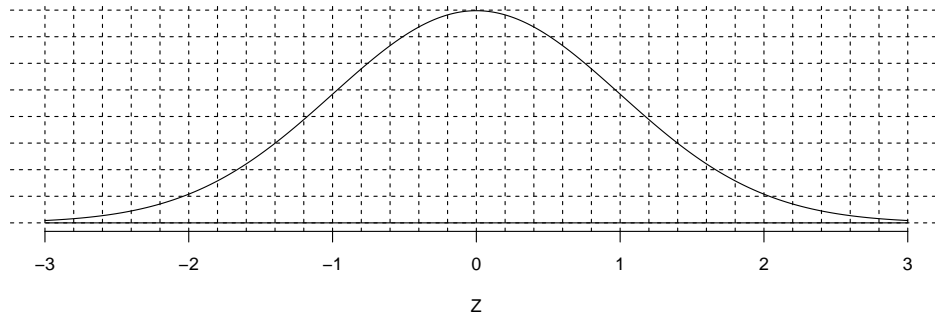


When you have shaded 92 squares, starting on the right, you should end around  $z = -1.4$ .

(b)  $z = 1.41$

**16. Problem:**

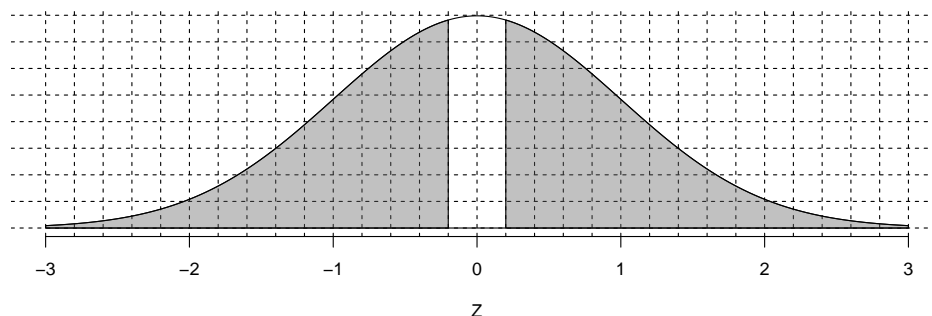
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(|Z| > z) = 0.84$  by shading and counting.
- (b) Determine  $z$  such that  $P(|Z| > z) = 0.84$  by using the  $z$ -table.

**Solution:**

(a) The shaded regions are shown below.



When you have shaded 84 squares, starting at both tails, you should end near  $z = 0.2$ . Really, you want to shade 42 squares starting from the left and also 42 squares starting from the right.

(b) Each tail has half the two-tail area. So each tail has an area of 0.42. We can find the  $z$  score with this left area. . .

$$z_{\text{left tail}} = -0.2$$

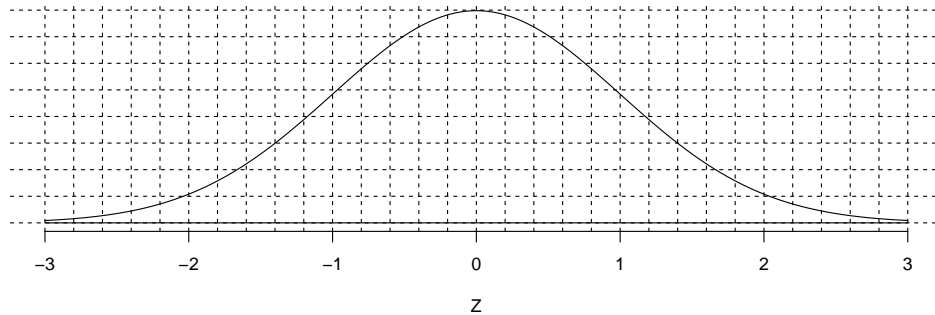
But, we want the positive value (the right tail's  $z$  boundary).

$$z = \boxed{0.2}$$



17. **Problem:**

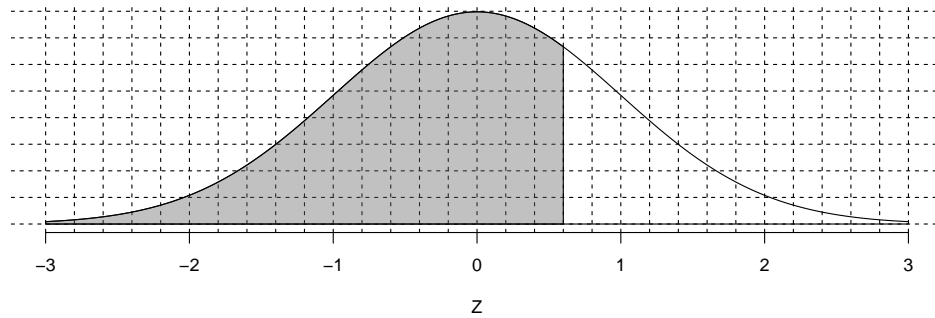
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(Z < 0.6)$  by shading and counting.
- (b) Determine  $P(Z < 0.6)$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

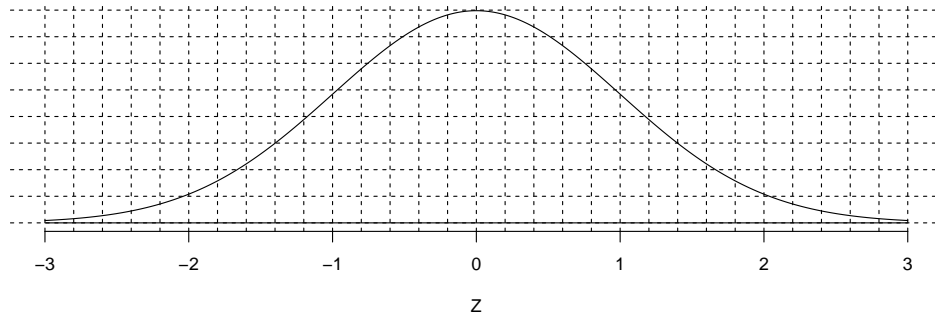


You should count about 73 shaded squares, giving a probability of about 0.73.

(b) The probability is 0.7257.

**18. Problem:**

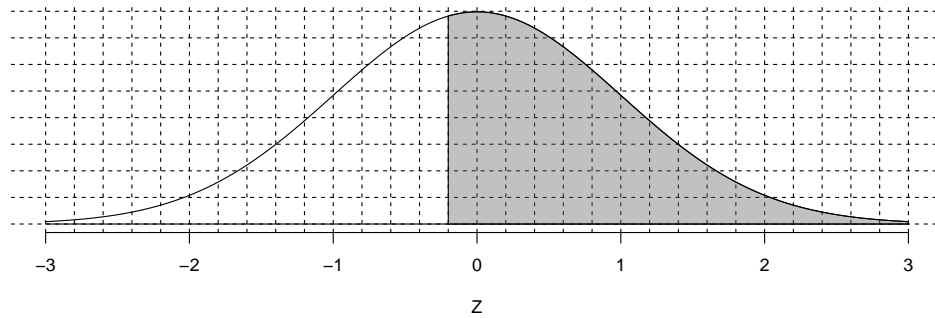
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(Z > -0.2)$  by shading and counting.
- (b) Determine  $P(Z > -0.2)$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

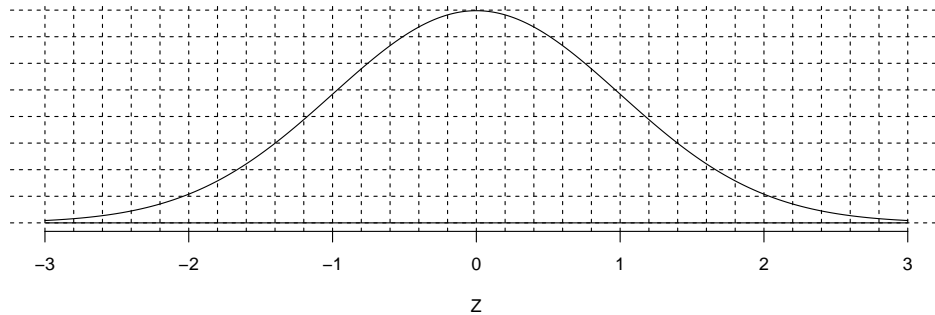


You should count about 58 shaded squares, giving a probability of about 0.58.

(b) The probability is 0.5793.

**19. Problem:**

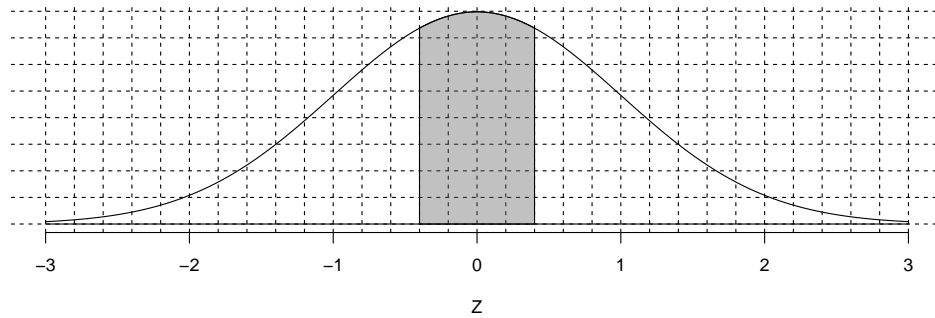
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(|Z| < z) = 0.31$  by shading and counting.
- (b) Determine  $z$  such that  $P(|Z| < z) = 0.31$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

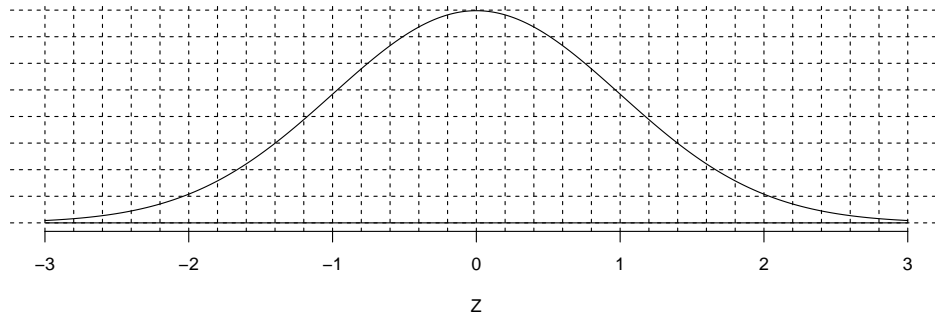


When you have shaded 31 squares, starting in the middle, you should end near  $z = 0.4$ .

(b)  $z = -0.5$

20. **Problem:**

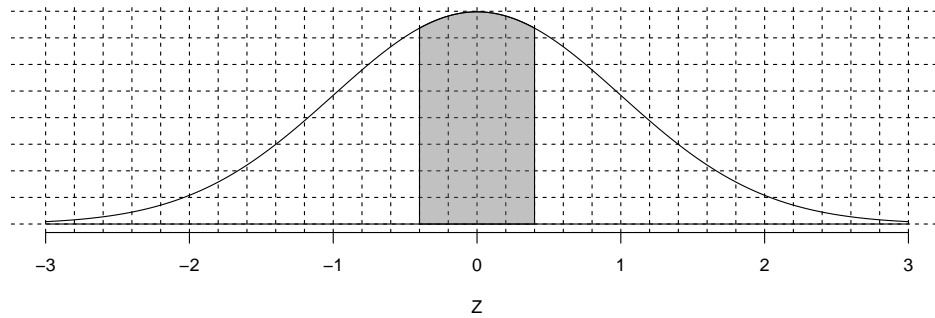
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(|Z| < 0.4)$  by shading and counting.
- (b) Determine  $P(|Z| < 0.4)$  by using the z-table.

**Solution:**

(a) The shaded region is shown below.



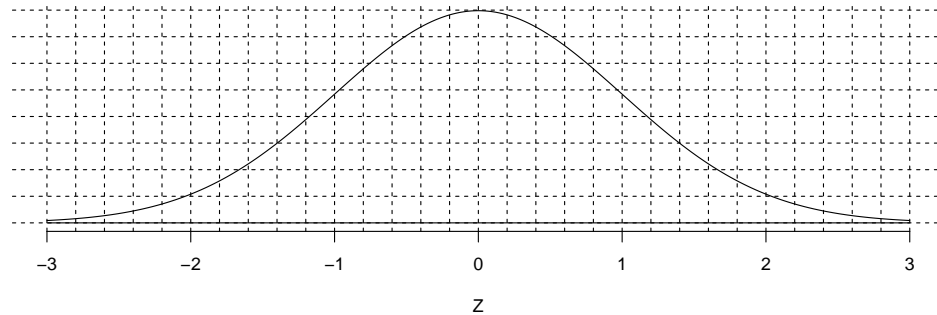
You should count about 31 shaded squares, giving a probability of about 0.31.

(b) The probability is 0.3108.



21. **Problem:**

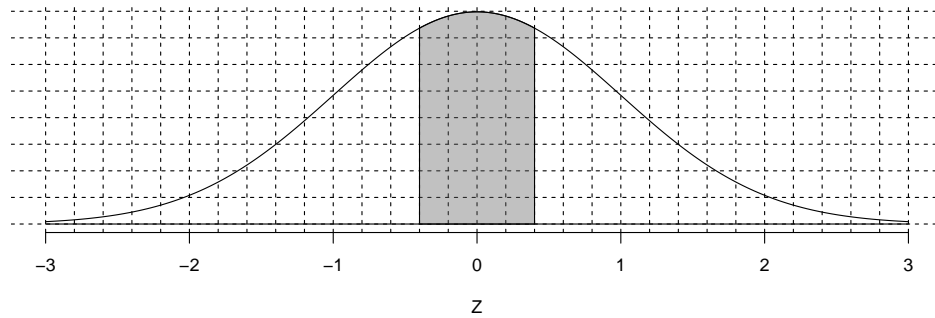
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(|Z| < 0.4)$  by shading and counting.
- (b) Determine  $P(|Z| < 0.4)$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

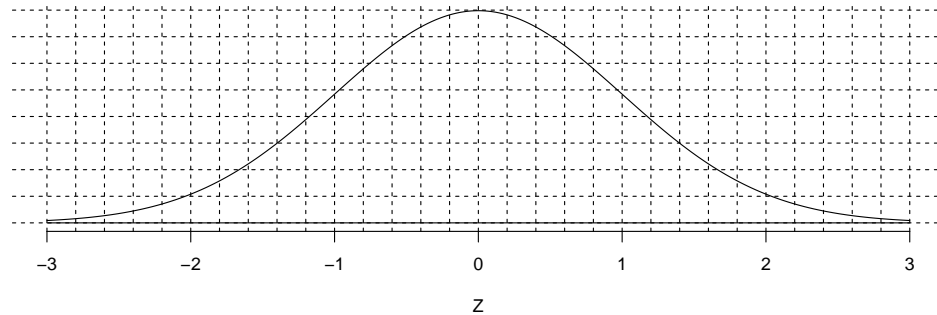


You should count about 31 shaded squares, giving a probability of about 0.31.

(b) The probability is 0.3108.

**22. Problem:**

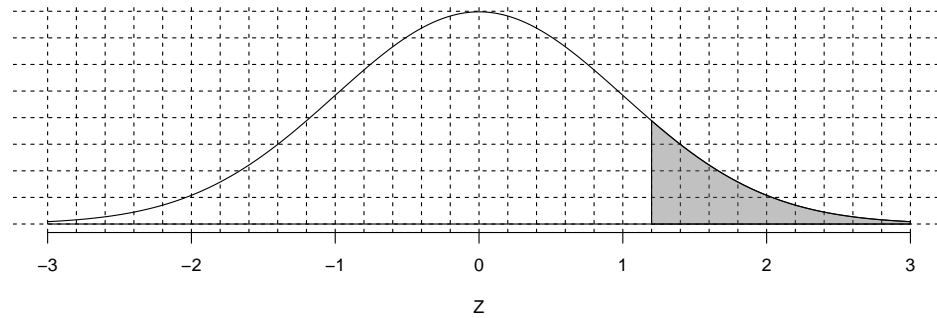
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(Z > 1.2)$  by shading and counting.
- (b) Determine  $P(Z > 1.2)$  by using the z-table.

**Solution:**

(a) The shaded region is shown below.

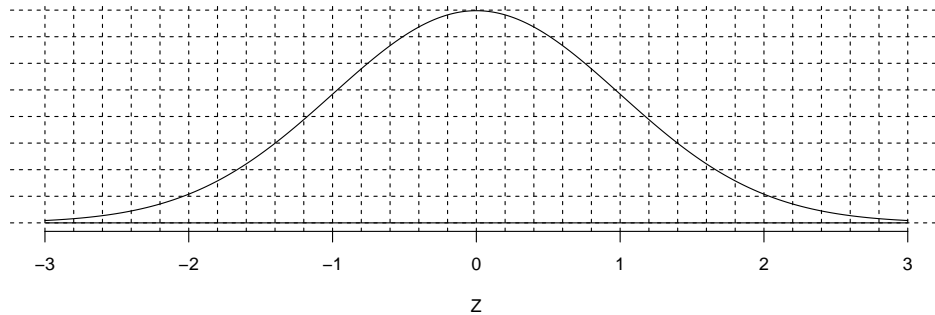


You should count about 12 shaded squares, giving a probability of about 0.12.

(b) The probability is 0.1151.

23. **Problem:**

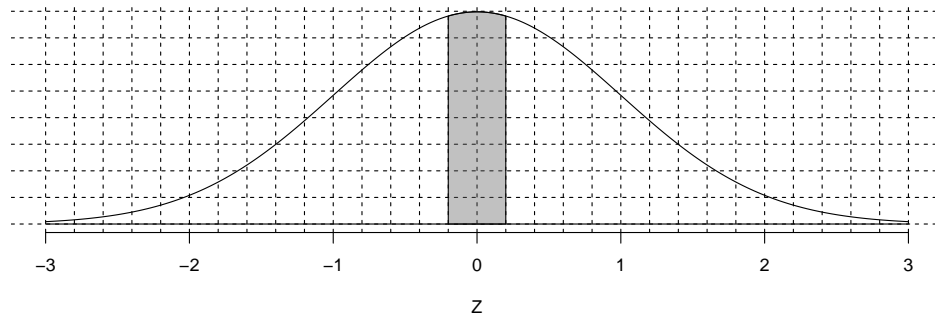
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(|Z| < z) = 0.16$  by shading and counting.
- (b) Determine  $z$  such that  $P(|Z| < z) = 0.16$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

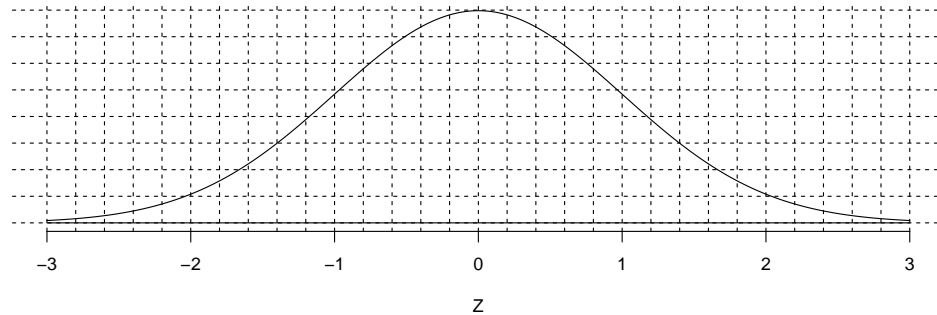


When you have shaded 16 squares, starting in the middle, you should end near  $z = 0.2$ .

(b)  $z = -0.99$

24. **Problem:**

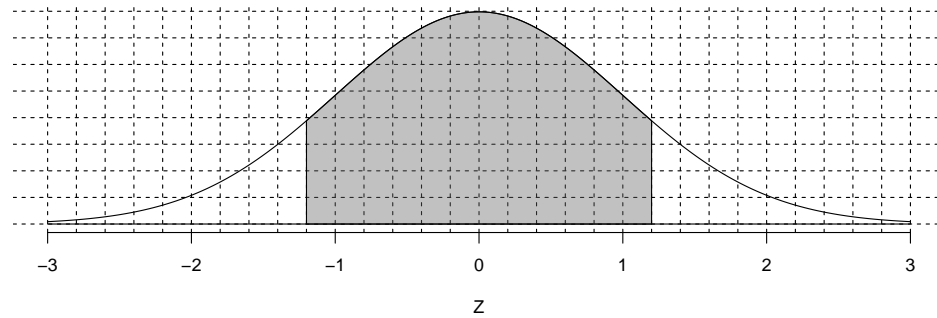
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(|Z| < z) = 0.77$  by shading and counting.
- (b) Determine  $z$  such that  $P(|Z| < z) = 0.77$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.



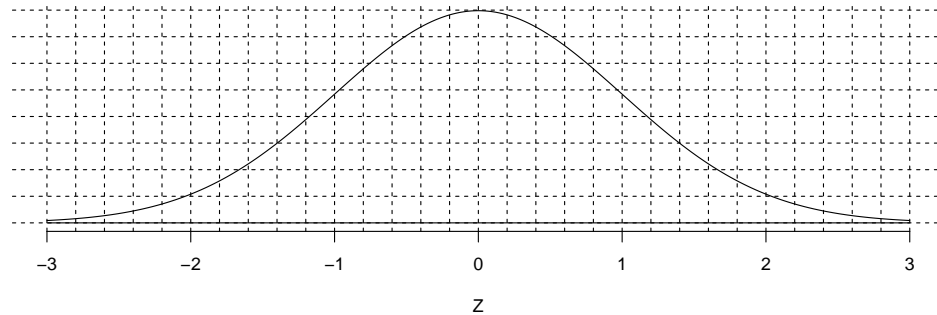
When you have shaded 77 squares, starting in the middle, you should end near  $z = 1.2$ .

(b)  $z = 0.74$



25. **Problem:**

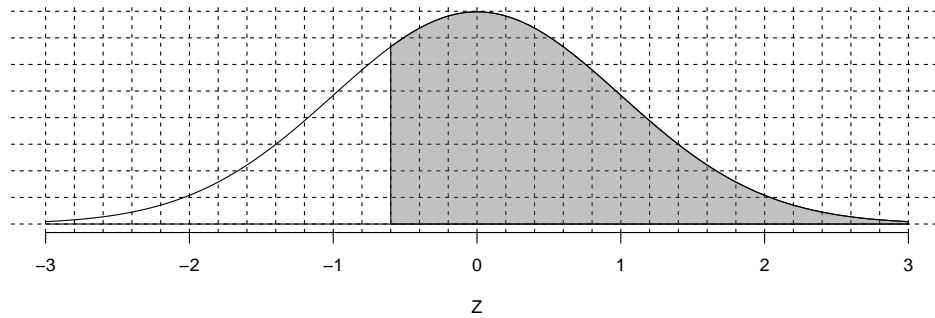
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(Z > z) = 0.73$  by shading and counting.
- (b) Determine  $z$  such that  $P(Z > z) = 0.73$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

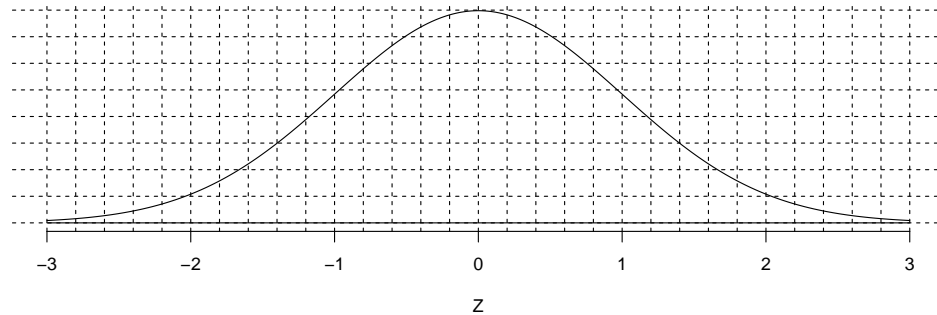


When you have shaded 73 squares, starting on the right, you should end around  $z = -0.6$ .

(b)  $z = 0.61$

26. **Problem:**

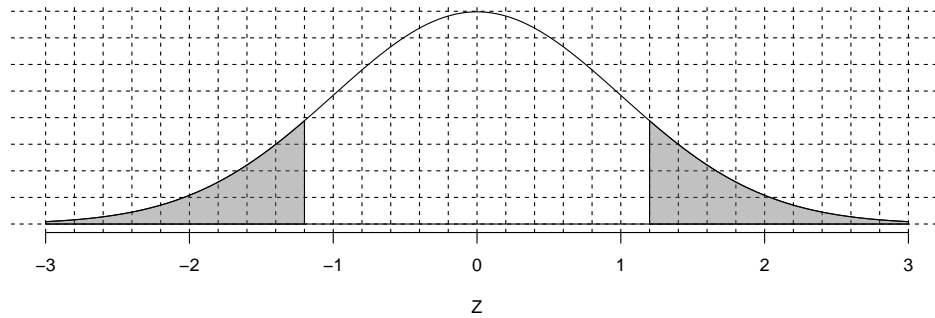
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(|Z| > 1.2)$  by shading and counting.
- (b) Determine  $P(|Z| > 1.2)$  by using the z-table.

**Solution:**

(a) The shaded regions are shown below.

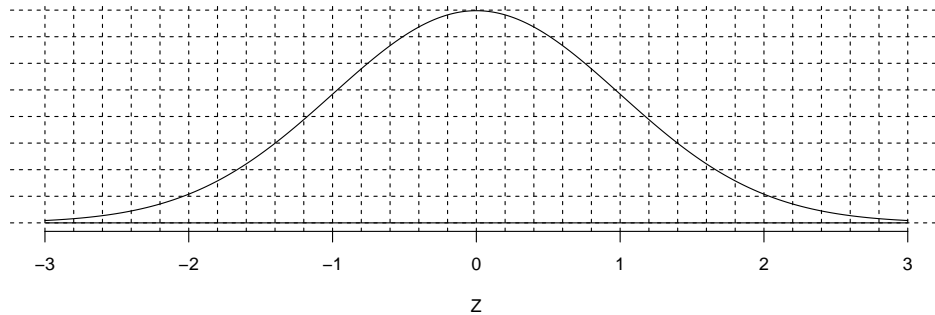


You should count about 23 shaded squares, giving a probability of about 0.23.

(b) The probability is 0.2301.

27. **Problem:**

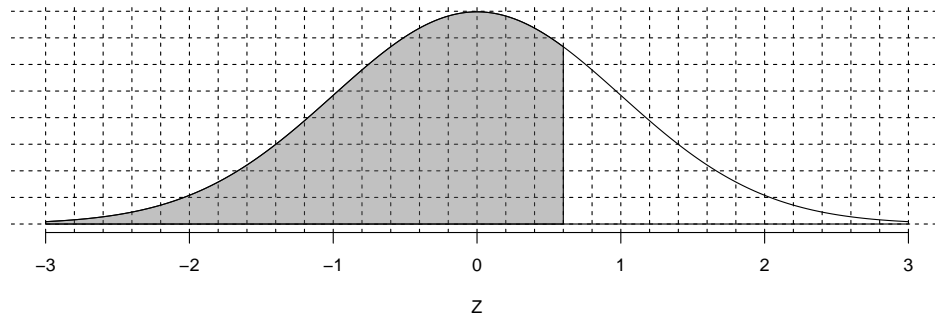
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(Z < z) = 0.73$  by shading and counting.
- (b) Determine  $z$  such that  $P(Z < z) = 0.73$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

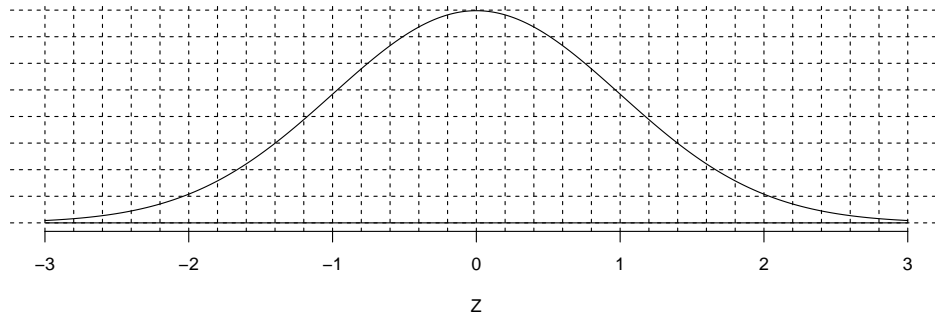


When you have shaded 73 squares, starting on the left, you should end around  $z = 0.6$ .

(b)  $z \approx 0.61$

28. **Problem:**

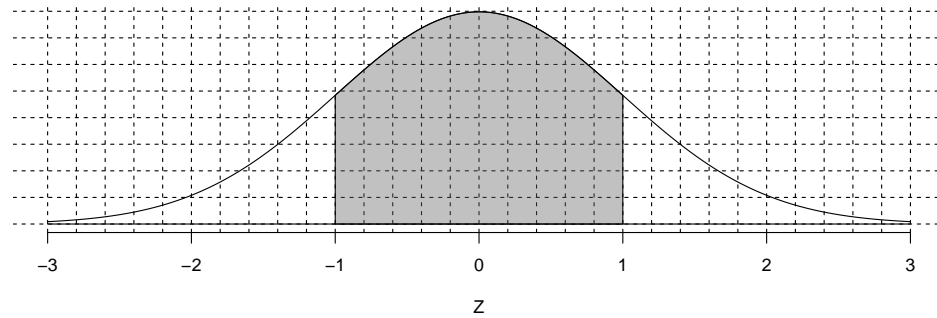
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(|Z| < z) = 0.68$  by shading and counting.
- (b) Determine  $z$  such that  $P(|Z| < z) = 0.68$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.



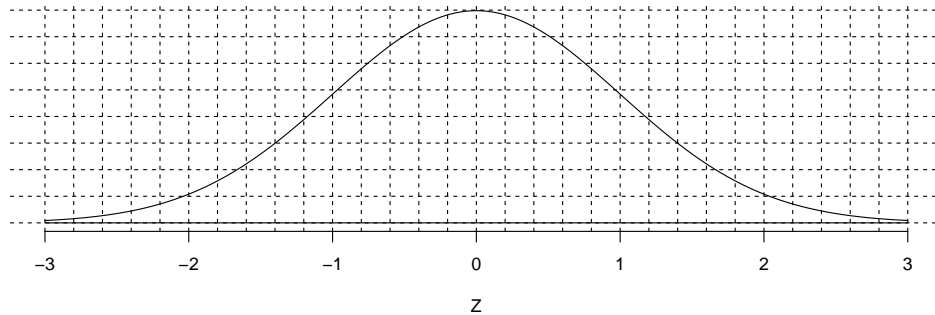
When you have shaded 68 squares, starting in the middle, you should end near  $z = 1$ .

(b)  $z = 0.47$



29. **Problem:**

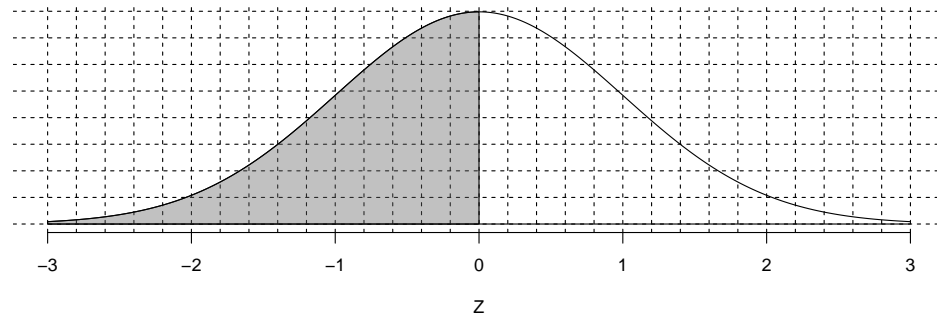
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(Z < 0)$  by shading and counting.
- (b) Determine  $P(Z < 0)$  by using the z-table.

**Solution:**

(a) The shaded region is shown below.

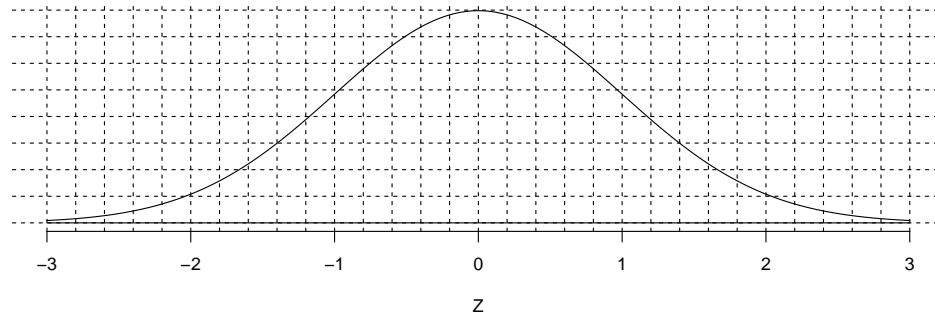


You should count about 50 shaded squares, giving a probability of about 0.5.

(b) The probability is 0.5.

30. **Problem:**

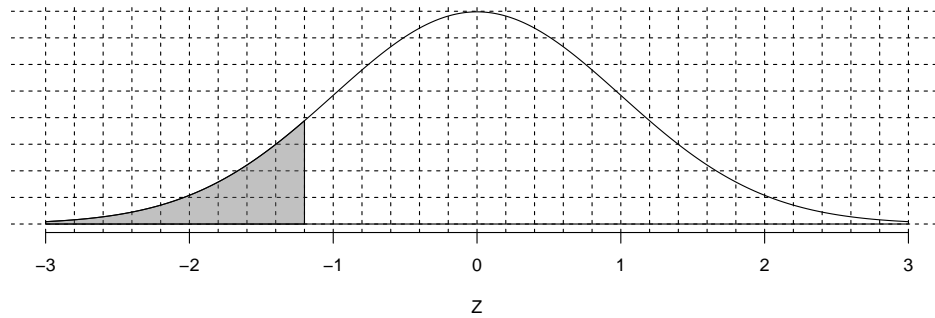
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(Z < z) = 0.12$  by shading and counting.
- (b) Determine  $z$  such that  $P(Z < z) = 0.12$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

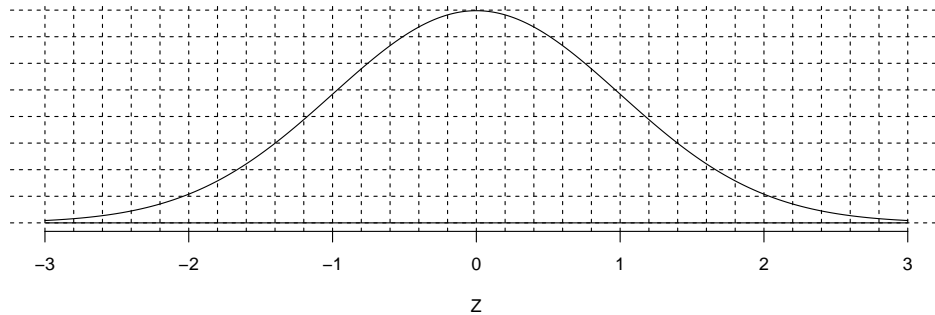


When you have shaded 12 squares, starting on the left, you should end around  $z = -1.2$ .

(b)  $z \approx -1.17$

31. **Problem:**

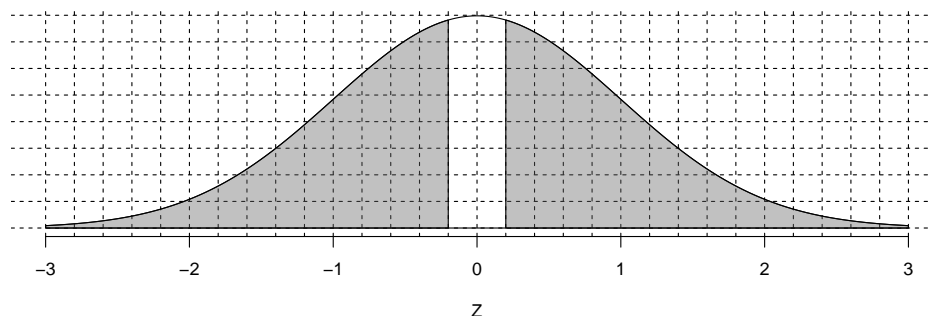
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(|Z| > z) = 0.84$  by shading and counting.
- (b) Determine  $z$  such that  $P(|Z| > z) = 0.84$  by using the  $z$ -table.

**Solution:**

(a) The shaded regions are shown below.



When you have shaded 84 squares, starting at both tails, you should end near  $z = 0.2$ . Really, you want to shade 42 squares starting from the left and also 42 squares starting from the right.

(b) Each tail has half the two-tail area. So each tail has an area of 0.42. We can find the  $z$  score with this left area. . .

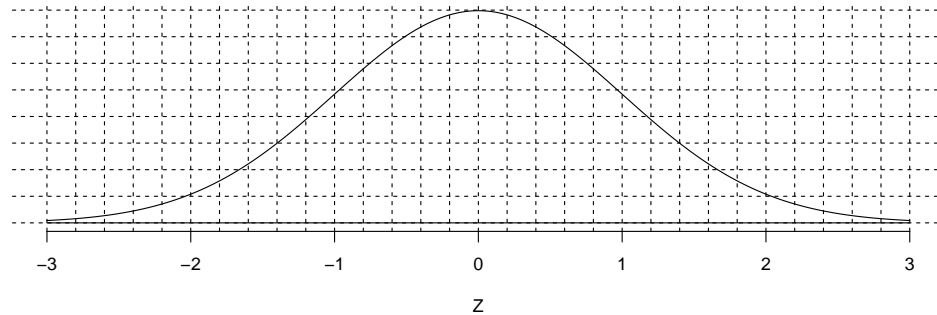
$$z_{\text{left tail}} = -0.2$$

But, we want the positive value (the right tail's  $z$  boundary).

$$z = \boxed{0.2}$$

32. **Problem:**

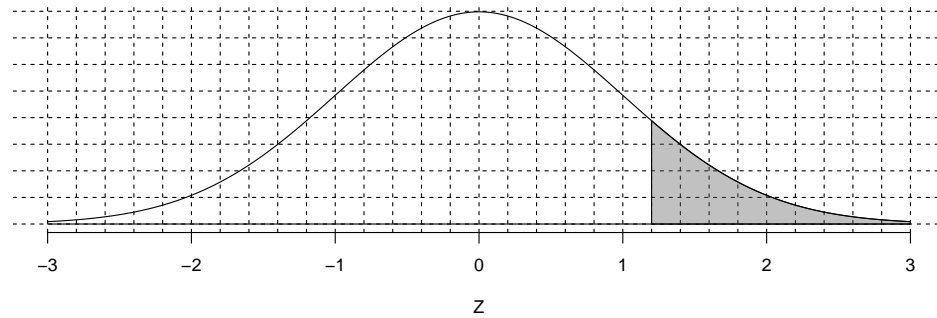
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(Z > z) = 0.12$  by shading and counting.
- (b) Determine  $z$  such that  $P(Z > z) = 0.12$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.



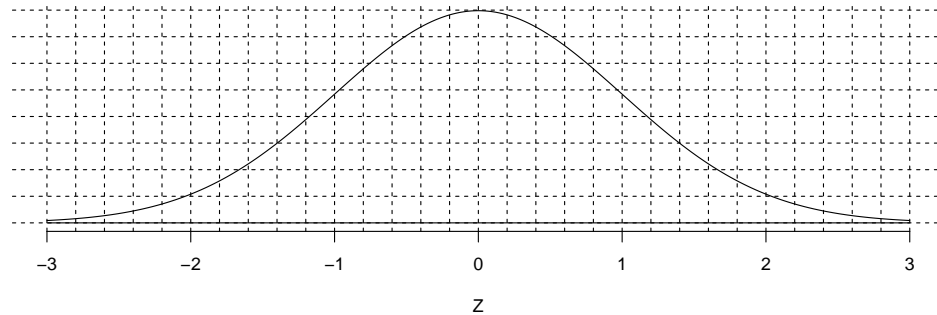
When you have shaded 12 squares, starting on the right, you should end around  $z = 1.2$ .

(b)  $z = -1.17$



33. **Problem:**

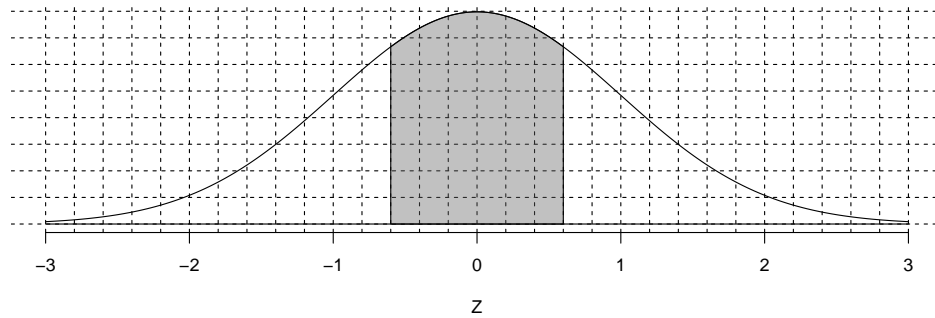
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(|Z| < z) = 0.45$  by shading and counting.
- (b) Determine  $z$  such that  $P(|Z| < z) = 0.45$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

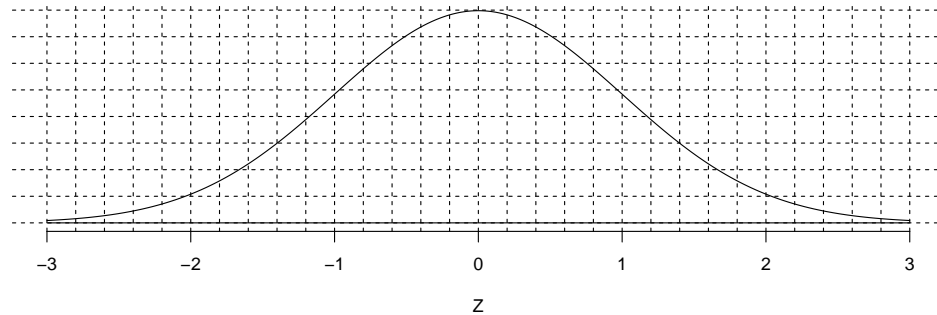


When you have shaded 45 squares, starting in the middle, you should end near  $z = 0.6$ .

(b)  $z = -0.13$

34. **Problem:**

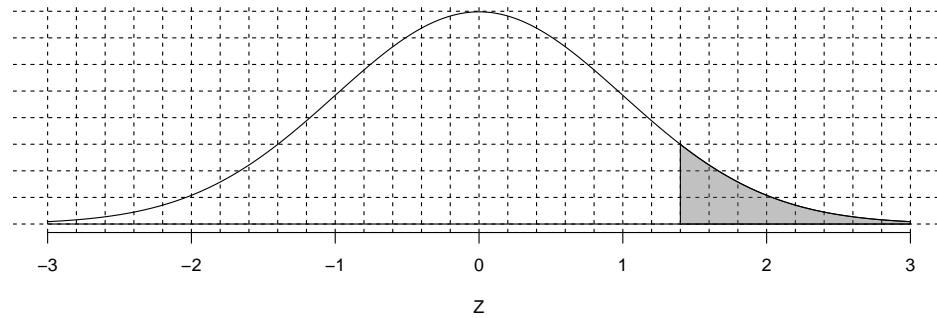
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(Z > 1.4)$  by shading and counting.
- (b) Determine  $P(Z > 1.4)$  by using the z-table.

**Solution:**

(a) The shaded region is shown below.

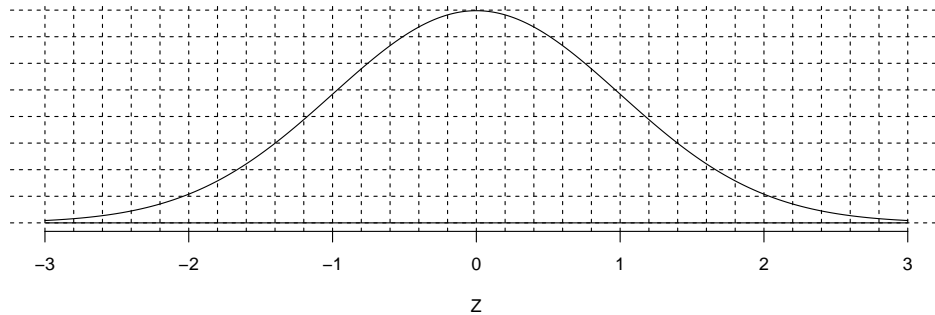


You should count about 8 shaded squares, giving a probability of about 0.08.

(b) The probability is 0.0808.

35. **Problem:**

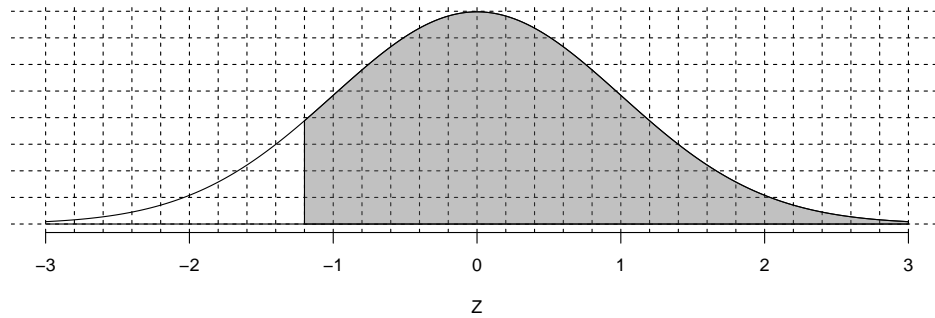
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(Z > -1.2)$  by shading and counting.
- (b) Determine  $P(Z > -1.2)$  by using the z-table.

**Solution:**

(a) The shaded region is shown below.

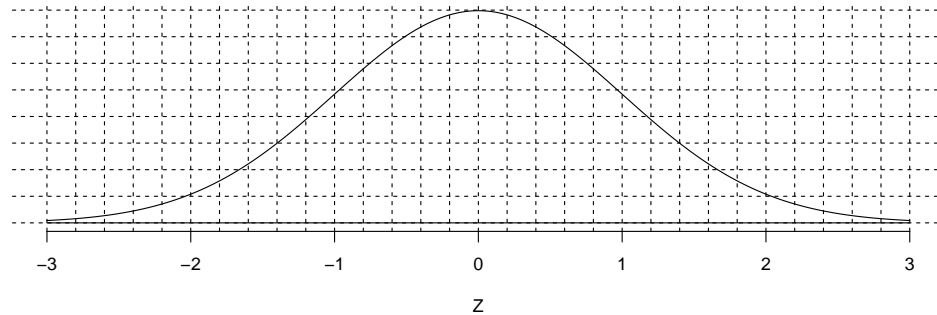


You should count about 88 shaded squares, giving a probability of about 0.88.

(b) The probability is 0.8849.

36. **Problem:**

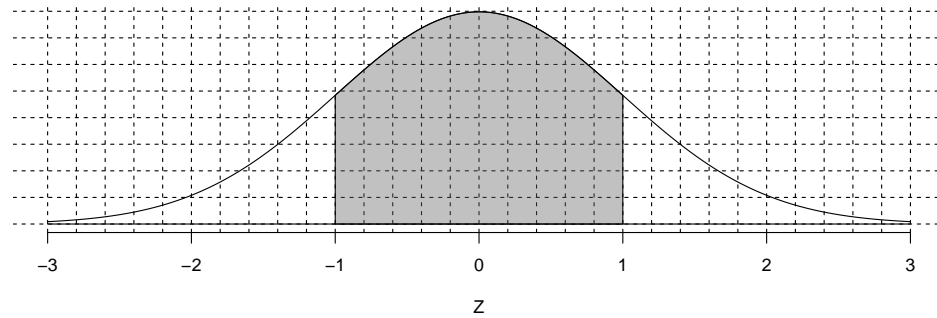
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(|Z| < 1)$  by shading and counting.
- (b) Determine  $P(|Z| < 1)$  by using the z-table.

**Solution:**

(a) The shaded region is shown below.



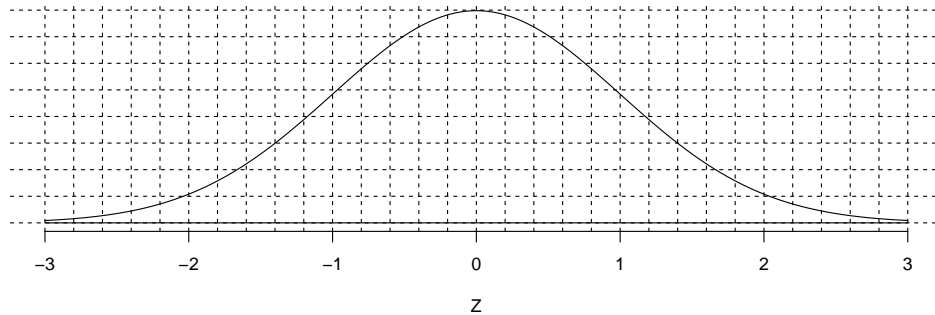
You should count about 68 shaded squares, giving a probability of about 0.68.

(b) The probability is 0.6827.



37. **Problem:**

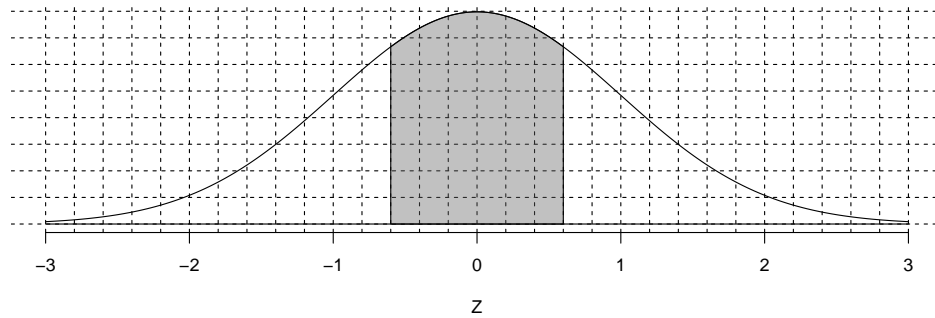
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(|Z| < 0.6)$  by shading and counting.
- (b) Determine  $P(|Z| < 0.6)$  by using the z-table.

**Solution:**

(a) The shaded region is shown below.

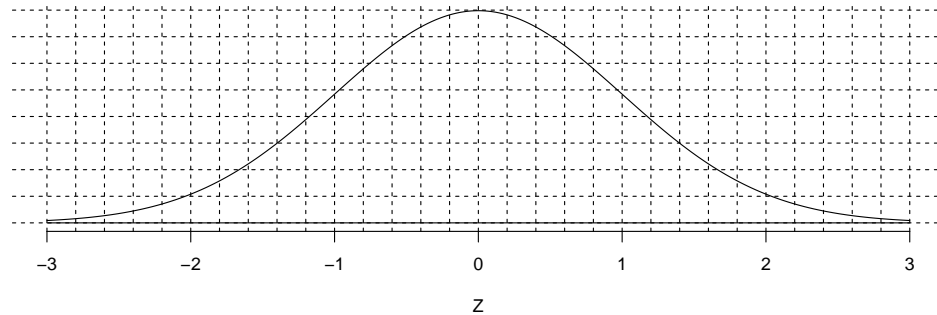


You should count about 45 shaded squares, giving a probability of about 0.45.

(b) The probability is 0.4515.

38. **Problem:**

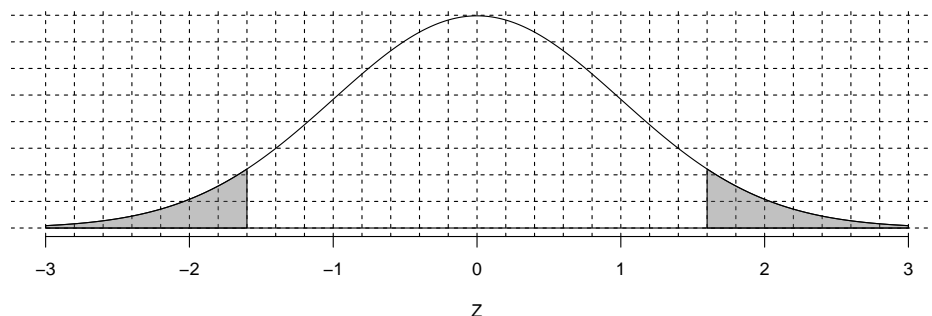
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(|Z| > z) = 0.11$  by shading and counting.
- (b) Determine  $z$  such that  $P(|Z| > z) = 0.11$  by using the  $z$ -table.

**Solution:**

(a) The shaded regions are shown below.



When you have shaded 11 squares, starting at both tails, you should end near  $z = 1.6$ . Really, you want to shade 5.5 squares starting from the left and also 5.5 squares starting from the right.

(b) Each tail has half the two-tail area. So each tail has an area of 0.055. We can find the  $z$  score with this left area. . .

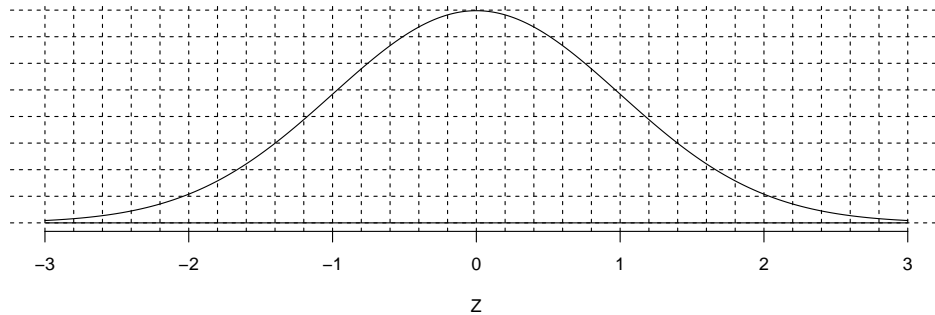
$$z_{\text{left tail}} = -1.6$$

But, we want the positive value (the right tail's  $z$  boundary).

$$z = \boxed{1.6}$$

39. **Problem:**

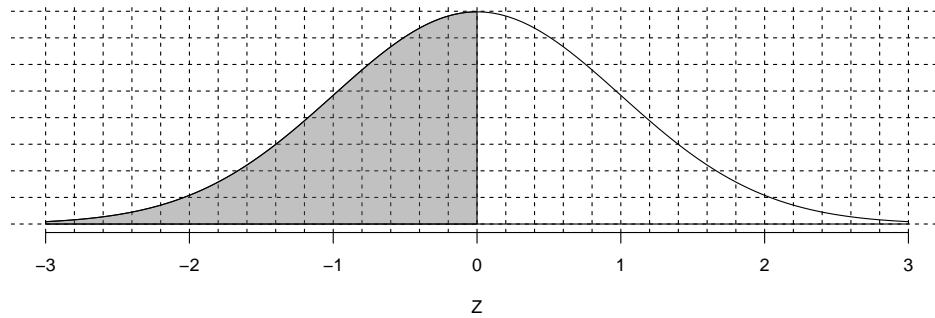
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(Z < z) = 0.5$  by shading and counting.
- (b) Determine  $z$  such that  $P(Z < z) = 0.5$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

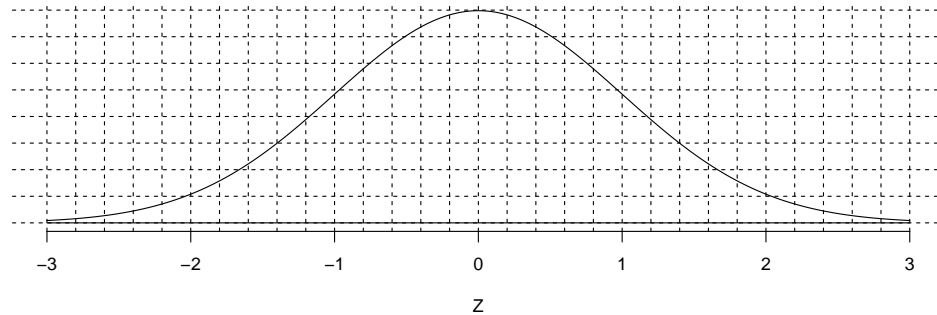


When you have shaded 50 squares, starting on the left, you should end around  $z = 0$ .

(b)  $z \approx 0$

40. **Problem:**

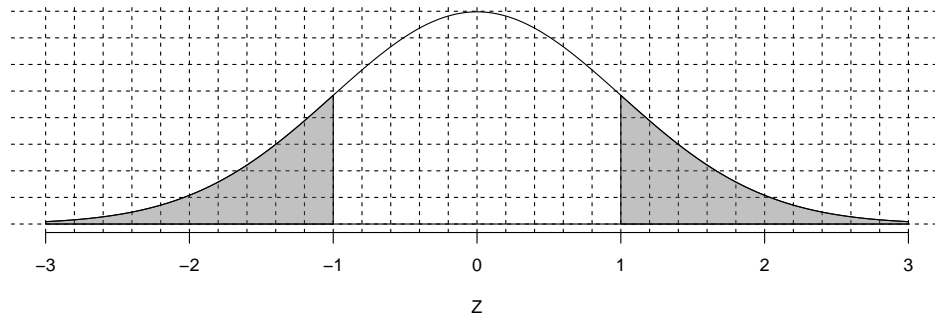
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(|Z| > 1)$  by shading and counting.
- (b) Determine  $P(|Z| > 1)$  by using the  $z$ -table.

**Solution:**

(a) The shaded regions are shown below.



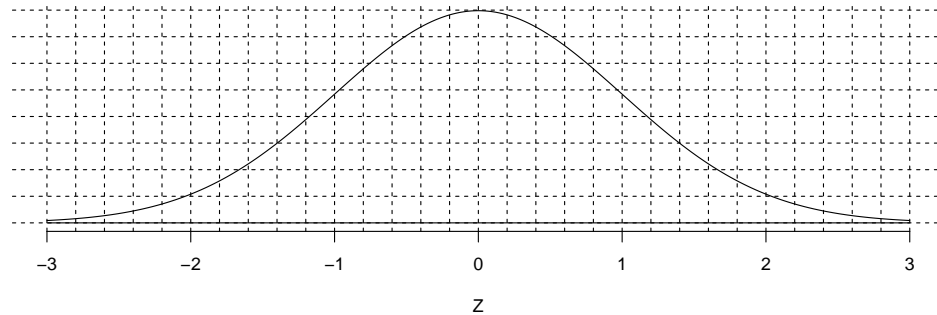
You should count about 32 shaded squares, giving a probability of about 0.32.

(b) The probability is 0.3173.



41. **Problem:**

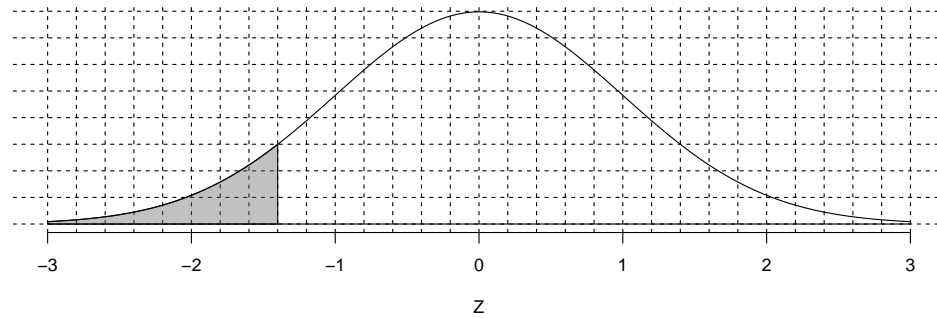
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(Z < -1.4)$  by shading and counting.
- (b) Determine  $P(Z < -1.4)$  by using the z-table.

**Solution:**

(a) The shaded region is shown below.

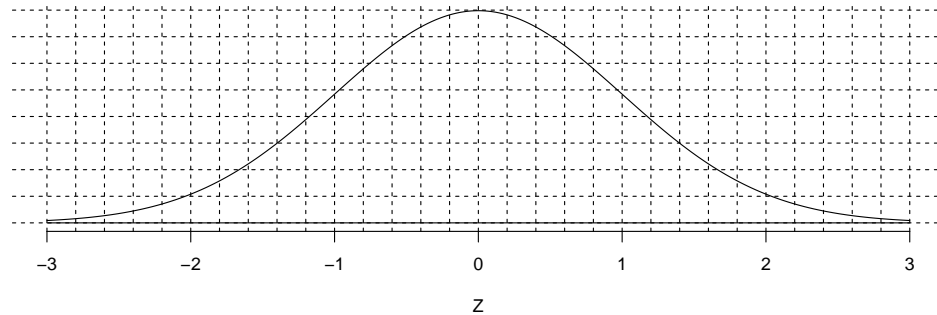


You should count about 8 shaded squares, giving a probability of about 0.08.

(b) The probability is 0.0808.

42. **Problem:**

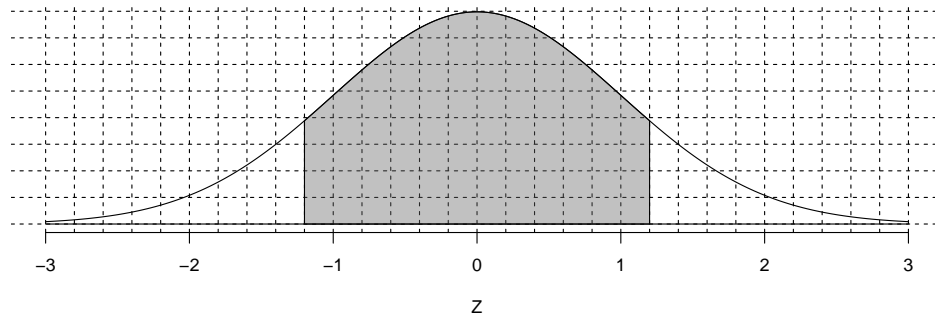
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(|Z| < z) = 0.77$  by shading and counting.
- (b) Determine  $z$  such that  $P(|Z| < z) = 0.77$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

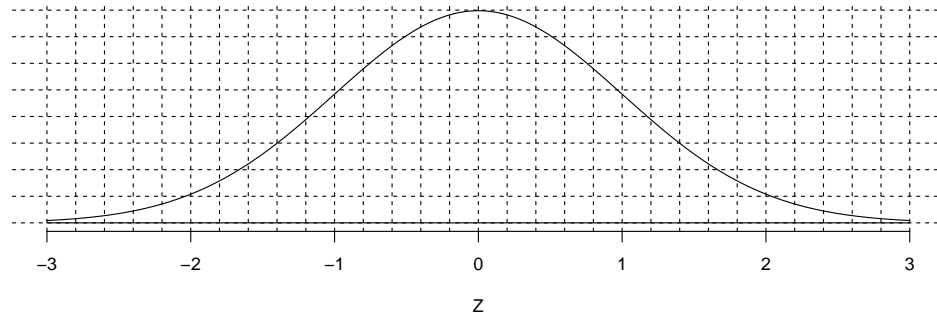


When you have shaded 77 squares, starting in the middle, you should end near  $z = 1.2$ .

(b)  $z = 0.74$

43. **Problem:**

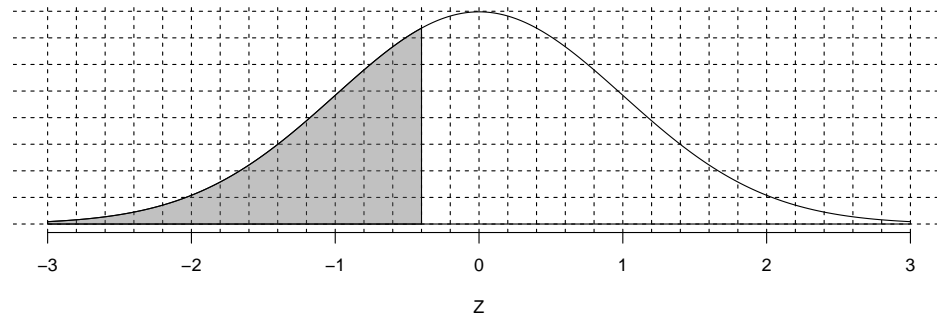
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(Z < -0.4)$  by shading and counting.
- (b) Determine  $P(Z < -0.4)$  by using the z-table.

**Solution:**

(a) The shaded region is shown below.

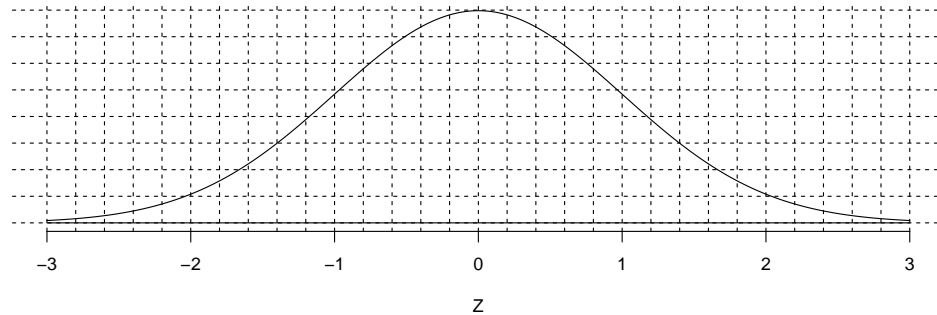


You should count about 34 shaded squares, giving a probability of about 0.34.

(b) The probability is 0.3446.

44. **Problem:**

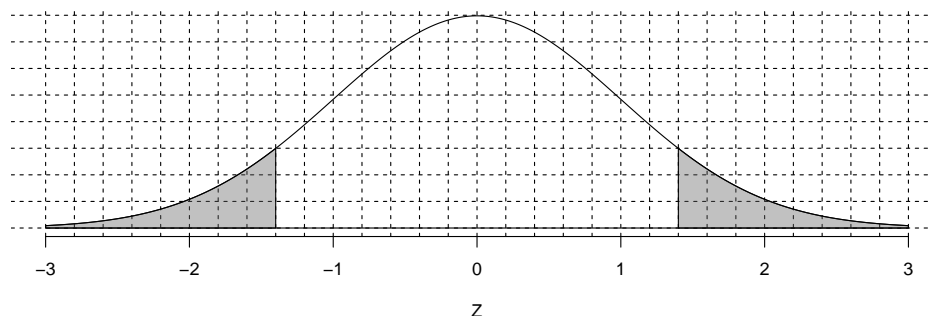
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(|Z| > z) = 0.16$  by shading and counting.
- (b) Determine  $z$  such that  $P(|Z| > z) = 0.16$  by using the  $z$ -table.

**Solution:**

(a) The shaded regions are shown below.



When you have shaded 16 squares, starting at both tails, you should end near  $z = 1.4$ . Really, you want to shade 8 squares starting from the left and also 8 squares starting from the right.

(b) Each tail has half the two-tail area. So each tail has an area of 0.08. We can find the  $z$  score with this left area. . .

$$z_{\text{left tail}} = -1.41$$

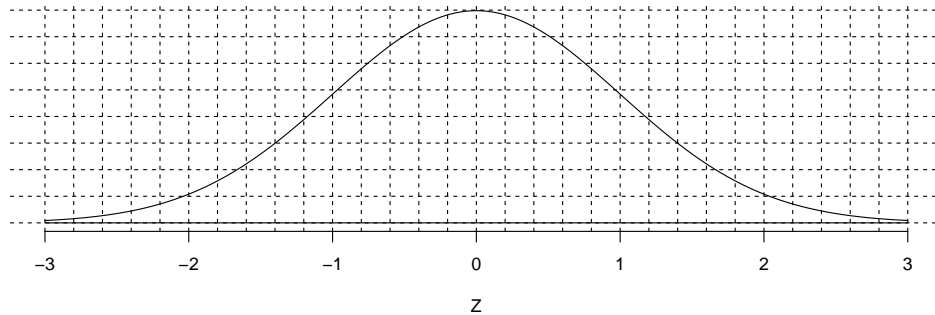
But, we want the positive value (the right tail's  $z$  boundary).

$$z = \boxed{1.41}$$



45. **Problem:**

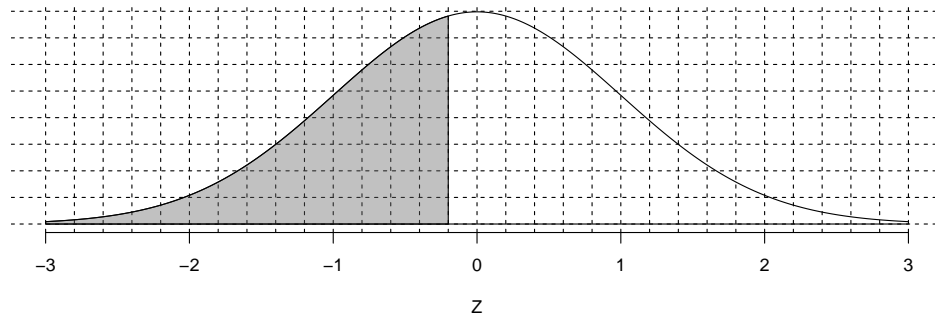
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(Z < z) = 0.42$  by shading and counting.
- (b) Determine  $z$  such that  $P(Z < z) = 0.42$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

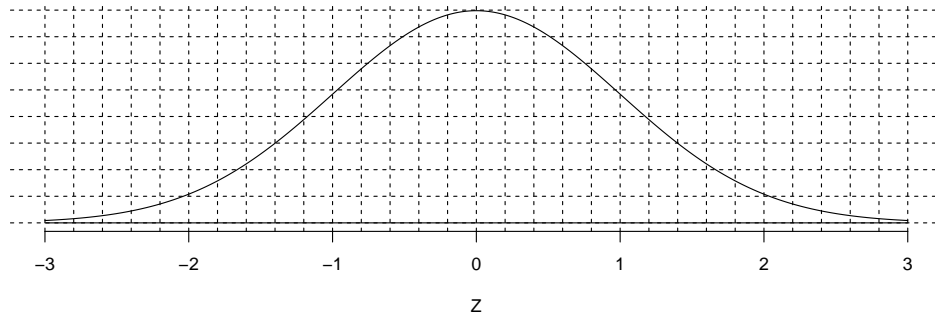


When you have shaded 42 squares, starting on the left, you should end around  $z = -0.2$ .

(b)  $z \approx -0.2$

46. **Problem:**

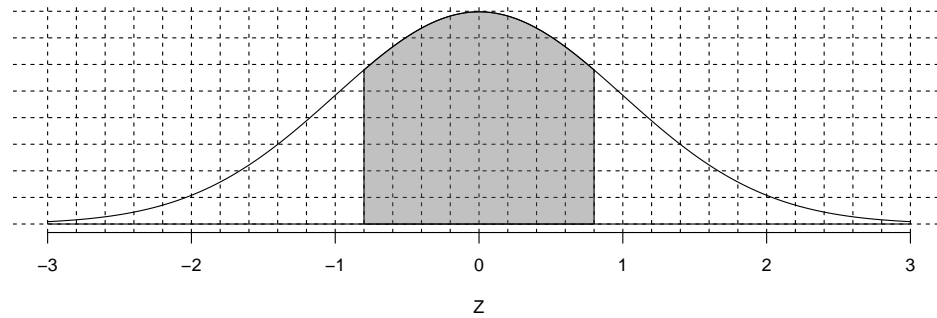
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(|Z| < 0.8)$  by shading and counting.
- (b) Determine  $P(|Z| < 0.8)$  by using the z-table.

**Solution:**

(a) The shaded region is shown below.

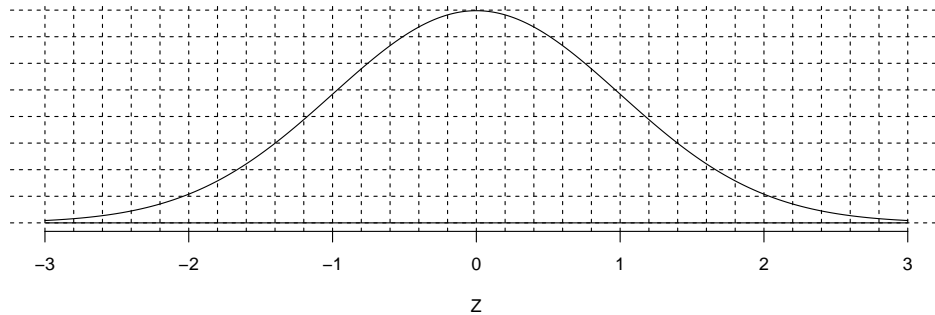


You should count about 58 shaded squares, giving a probability of about 0.58.

(b) The probability is 0.5763.

47. **Problem:**

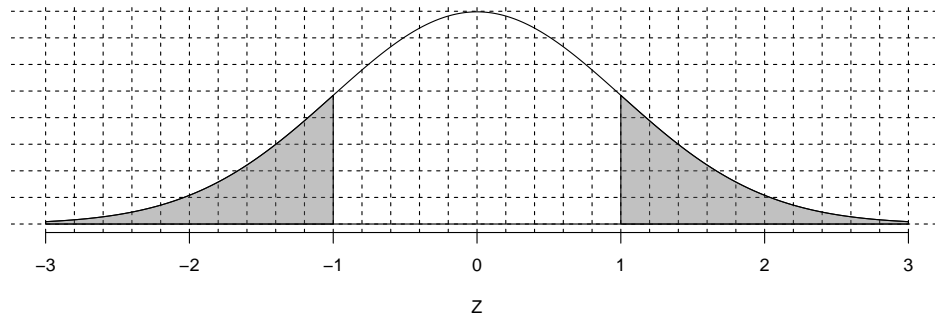
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(|Z| > 1)$  by shading and counting.
- (b) Determine  $P(|Z| > 1)$  by using the z-table.

**Solution:**

(a) The shaded regions are shown below.

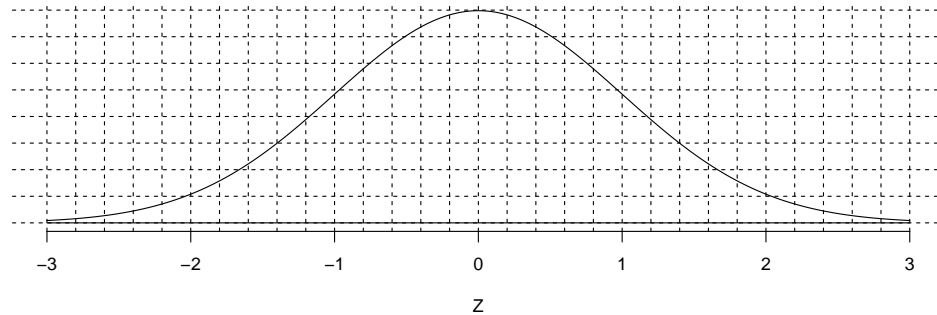


You should count about 32 shaded squares, giving a probability of about 0.32.

(b) The probability is 0.3173.

48. **Problem:**

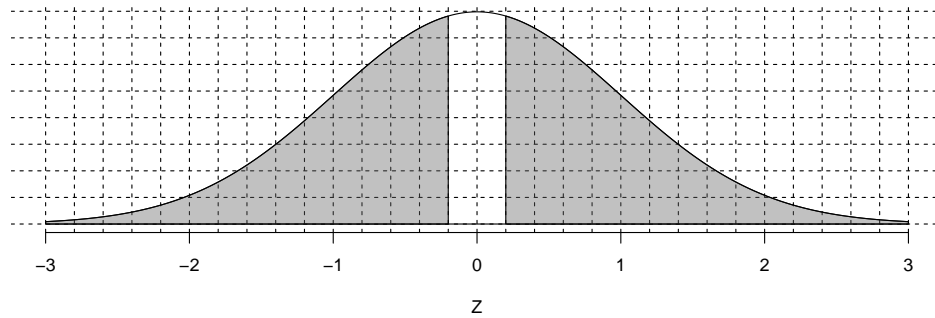
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(|Z| > 0.2)$  by shading and counting.
- (b) Determine  $P(|Z| > 0.2)$  by using the z-table.

**Solution:**

(a) The shaded regions are shown below.



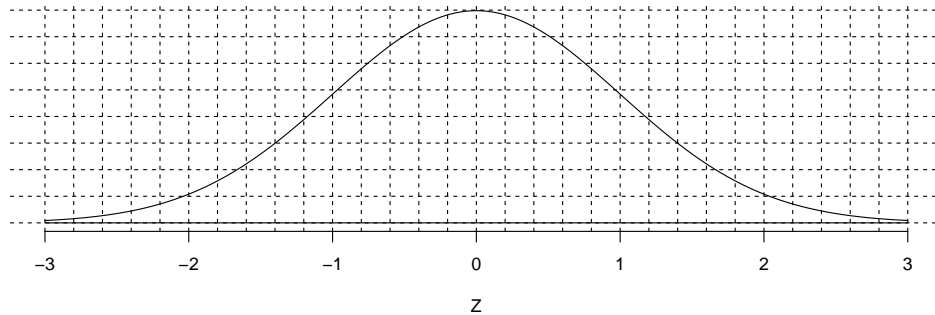
You should count about 84 shaded squares, giving a probability of about 0.84.

(b) The probability is 0.8415.



49. **Problem:**

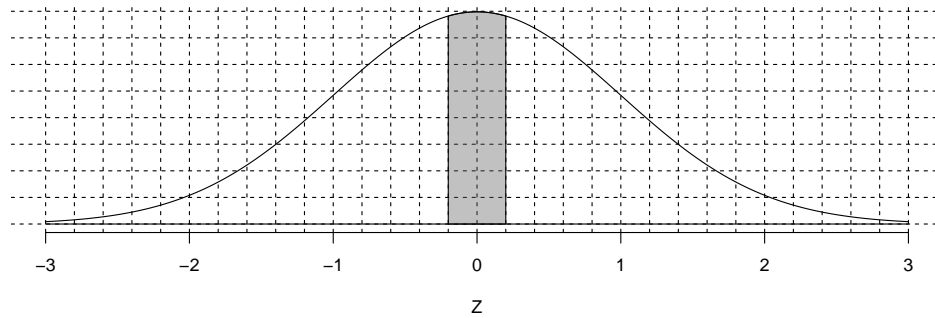
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(|Z| < 0.2)$  by shading and counting.
- (b) Determine  $P(|Z| < 0.2)$  by using the z-table.

**Solution:**

(a) The shaded region is shown below.

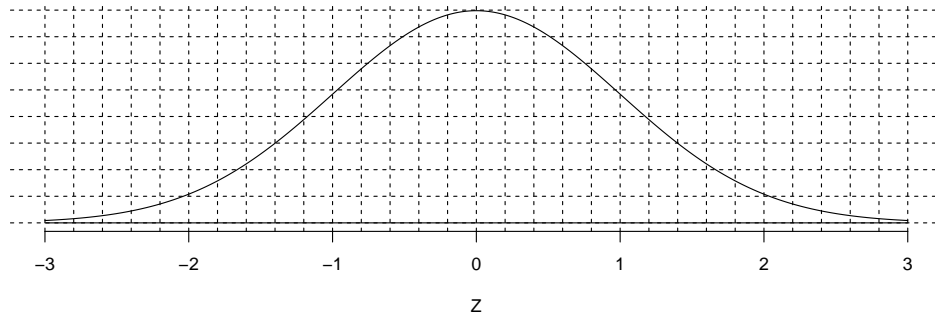


You should count about 16 shaded squares, giving a probability of about 0.16.

(b) The probability is 0.1585.

50. **Problem:**

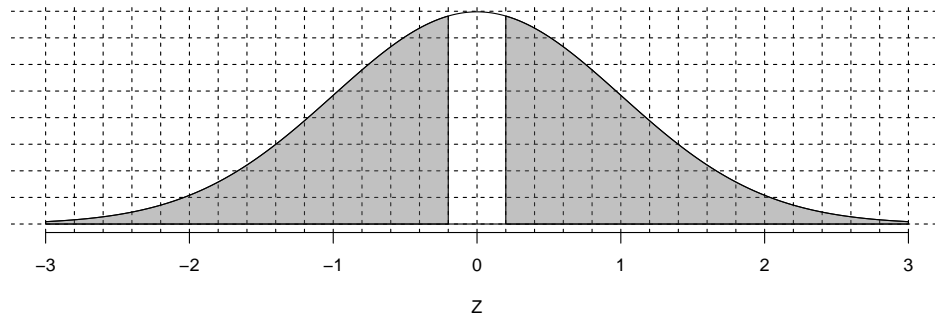
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(|Z| > z) = 0.84$  by shading and counting.
- (b) Determine  $z$  such that  $P(|Z| > z) = 0.84$  by using the  $z$ -table.

**Solution:**

(a) The shaded regions are shown below.



When you have shaded 84 squares, starting at both tails, you should end near  $z = 0.2$ . Really, you want to shade 42 squares starting from the left and also 42 squares starting from the right.

(b) Each tail has half the two-tail area. So each tail has an area of 0.42. We can find the  $z$  score with this left area. . .

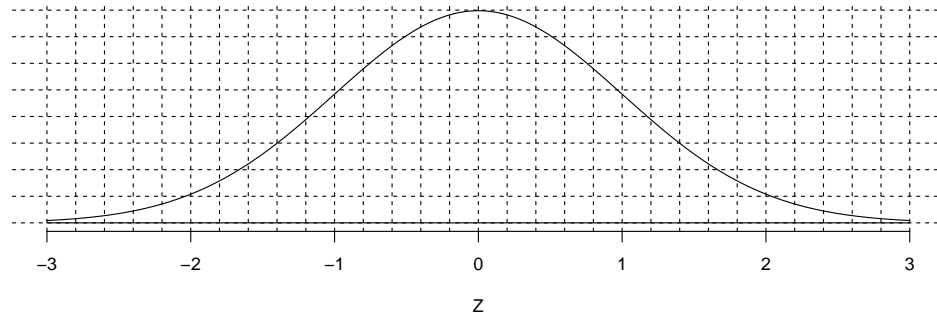
$$z_{\text{left tail}} = -0.2$$

But, we want the positive value (the right tail's  $z$  boundary).

$$z = \boxed{0.2}$$

51. **Problem:**

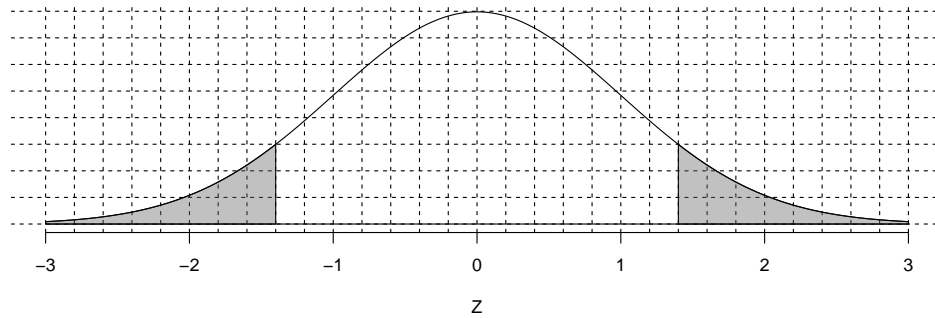
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(|Z| > 1.4)$  by shading and counting.
- (b) Determine  $P(|Z| > 1.4)$  by using the z-table.

**Solution:**

(a) The shaded regions are shown below.

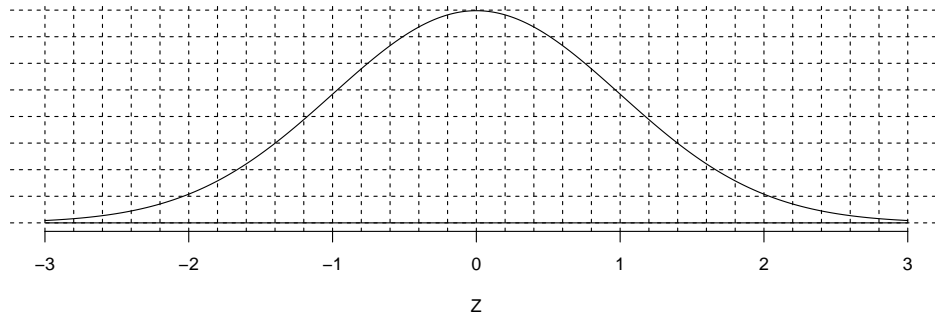


You should count about 16 shaded squares, giving a probability of about 0.16.

(b) The probability is 0.1615.

52. **Problem:**

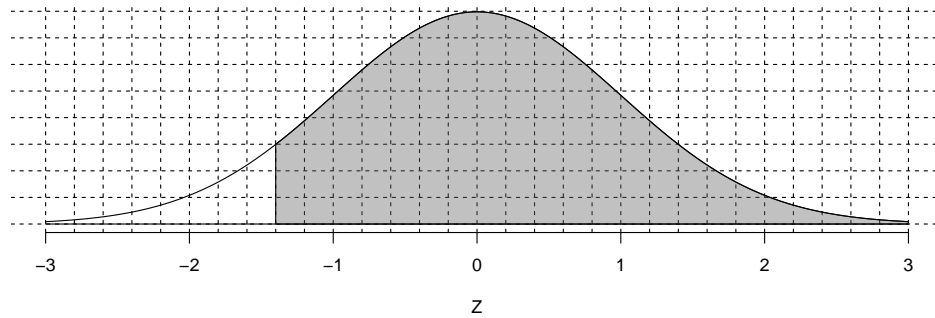
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(Z > -1.4)$  by shading and counting.
- (b) Determine  $P(Z > -1.4)$  by using the z-table.

**Solution:**

(a) The shaded region is shown below.



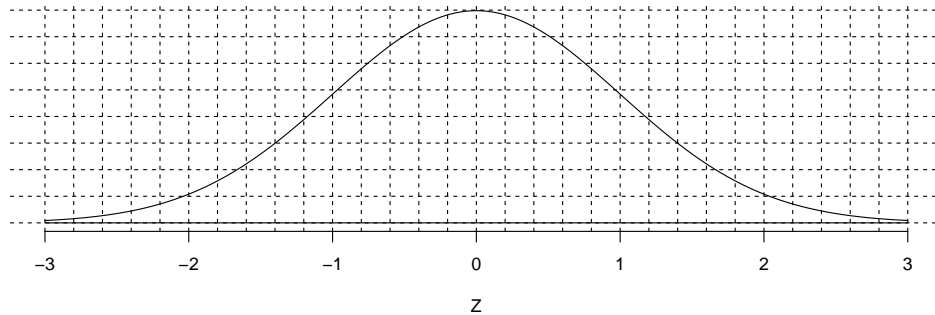
You should count about 92 shaded squares, giving a probability of about 0.92.

(b) The probability is 0.9192.



53. **Problem:**

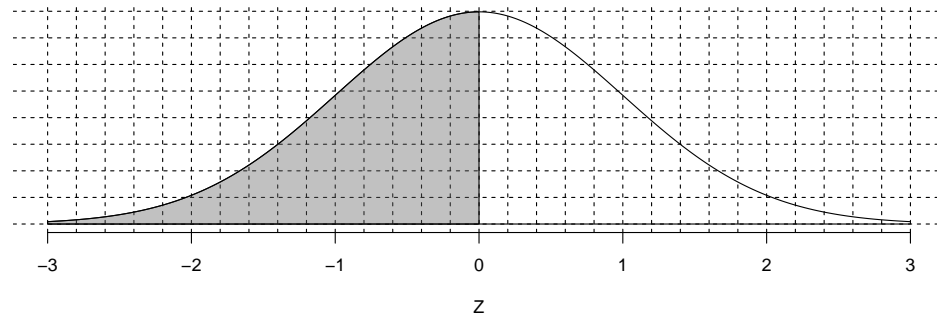
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(Z < 0)$  by shading and counting.
- (b) Determine  $P(Z < 0)$  by using the z-table.

**Solution:**

(a) The shaded region is shown below.

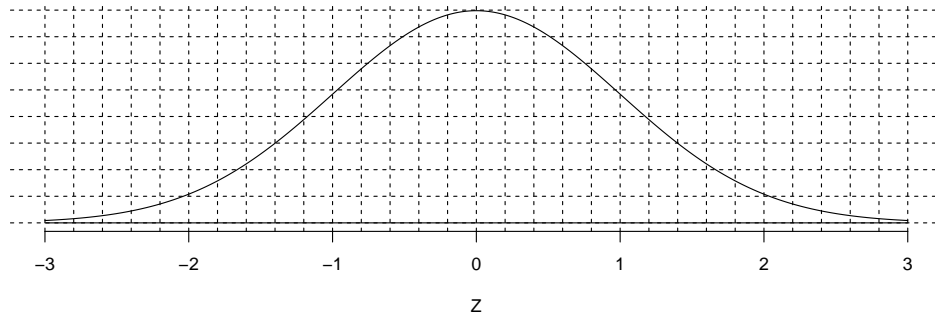


You should count about 50 shaded squares, giving a probability of about 0.5.

(b) The probability is 0.5.

54. **Problem:**

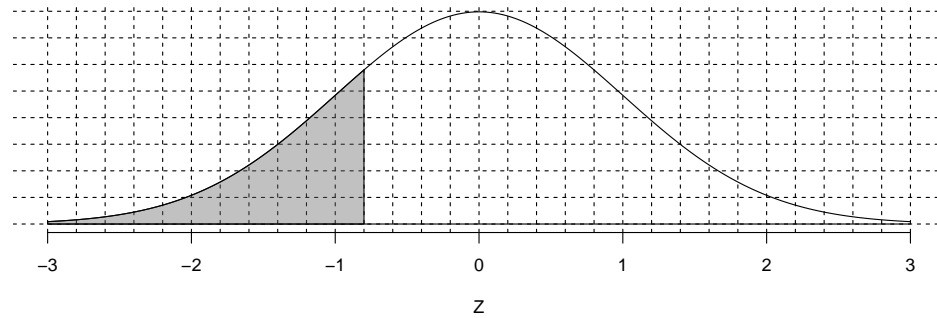
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $z$  such that  $P(Z < z) = 0.21$  by shading and counting.
- (b) Determine  $z$  such that  $P(Z < z) = 0.21$  by using the  $z$ -table.

**Solution:**

(a) The shaded region is shown below.

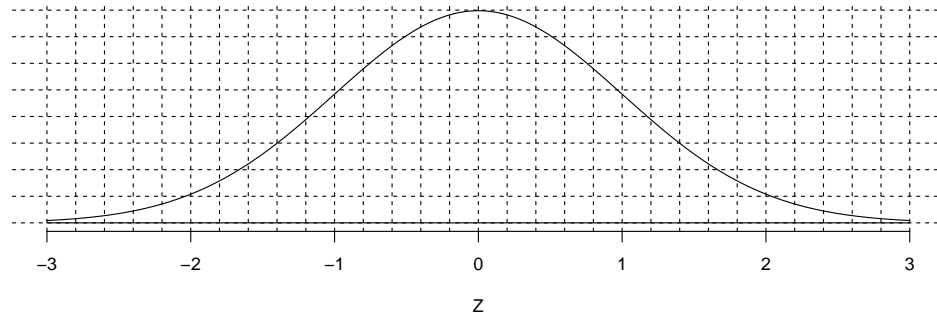


When you have shaded 21 squares, starting on the left, you should end around  $z = -0.8$ .

(b)  $z \approx -0.81$

55. **Problem:**

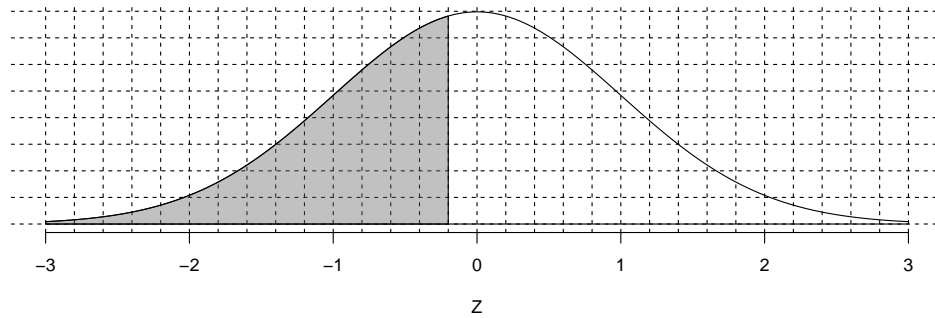
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(Z < -0.2)$  by shading and counting.
- (b) Determine  $P(Z < -0.2)$  by using the z-table.

**Solution:**

(a) The shaded region is shown below.

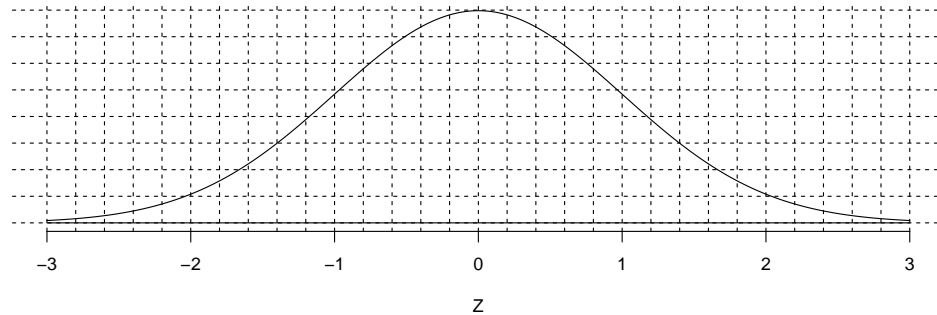


You should count about 42 shaded squares, giving a probability of about 0.42.

(b) The probability is 0.4207.

56. **Problem:**

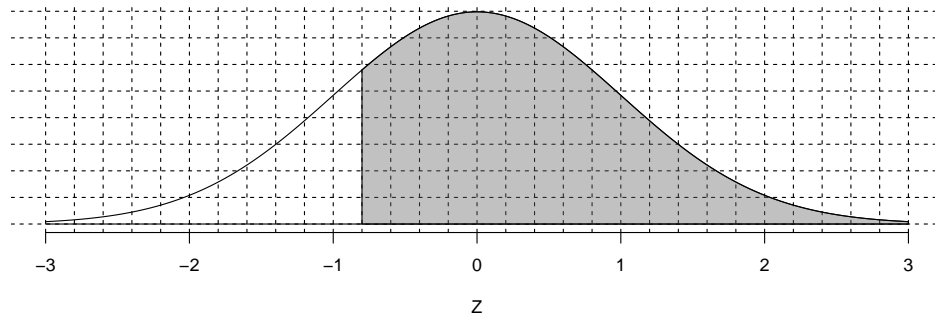
The figure below shows the standard normal density. Each grid square represents 1% of probability.



- (a) Estimate  $P(Z > -0.8)$  by shading and counting.
- (b) Determine  $P(Z > -0.8)$  by using the z-table.

**Solution:**

(a) The shaded region is shown below.



You should count about 79 shaded squares, giving a probability of about 0.79.

(b) The probability is 0.7881.