

1. Solution

Let x represent a datum of interest. Let i represent that datum's index. Let ℓ represent that datum's percentile. Let n represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given $x = 144.129$. This means $i = 9$. We know $n = 10$. Determine the percentile ℓ .

$$\ell = \frac{9}{10}$$

$$\ell = 0.9$$

So, the percentile rank is $\boxed{0.9}$, or 90th percentile.

(b) We are given $\ell = 0.4$. We can use algebra to solve for i .

$$\ell = \frac{i}{n}$$

Multiply both sides by n .

$$n \cdot (\ell) = n \cdot \left(\frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate i .

$$i = (10)(0.4)$$

$$i = 4$$

Determine the x associated with $i = 4$.

$$x = \boxed{123.235}$$

(c) The mean: $\bar{x} = \frac{1273.39}{10} = \boxed{127.34}$

(d) If n is odd, then median is $x_{i=\frac{n+1}{2}}$, the value of x when $i = \frac{n+1}{2}$. Otherwise, if n is even, the median is mean of $x_{i=\frac{n}{2}}$ and $x_{i=\frac{n}{2}+1}$. In this case, $n = 10$ and so n is even.

$$\text{median} = \frac{x_5 + x_6}{2} = \frac{124.523 + 125.213}{2}$$

So, median = $\boxed{124.868}$.

2. Solution

Let x represent a datum of interest. Let i represent that datum's index. Let ℓ represent that datum's percentile. Let n represent the sample size (number of measurements). In general,

$$\ell = \frac{i}{n}$$

(a) We are given $x = 119.489$. This means $i = 17$. We know $n = 25$. Determine the percentile ℓ .

$$\ell = \frac{17}{25}$$

$$\ell = 0.68$$

So, the percentile rank is $\boxed{0.68}$, or 68th percentile.

(b) We are given $\ell = 0.56$. We can use algebra to solve for i .

$$\ell = \frac{i}{n}$$

Multiply both sides by n .

$$n \cdot (\ell) = n \cdot \left(\frac{i}{n} \right)$$

Simplify both sides.

$$n\ell = i$$

To make me happy, switch the sides.

$$i = n\ell$$

Now, we can evaluate i .

$$i = (25)(0.56)$$

$$i = 14$$

Determine the x associated with $i = 14$.

$$x = \boxed{118.344}$$

(c) The mean: $\bar{x} = \frac{2954.784}{25} = \boxed{118.19}$

(d) If n is odd, then median is $x_{i=\frac{n+1}{2}}$, the value of x when $i = \frac{n+1}{2}$. Otherwise, if n is even, the median is mean of $x_{i=\frac{n}{2}}$ and $x_{i=\frac{n}{2}+1}$. In this case, $n = 25$ and so n is odd.

$$\text{median} = x_{(25+1)/2} = x_{13}$$

So, median = $\boxed{117.707}$.