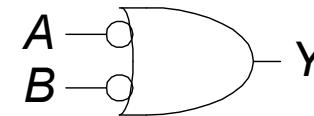
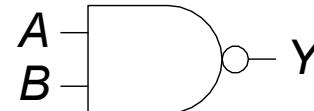
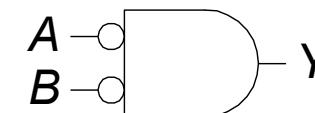
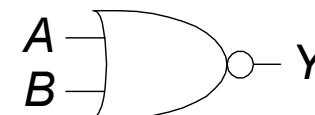


# DeMorgan's Theorem

$$\bullet Y = \overline{AB} = \overline{A} + \overline{B}$$



$$\bullet Y = \overline{A + B} = \overline{A} \cdot \overline{B}$$



# Bubble Pushing

- **Backward:**

- Body changes
- Adds bubbles to inputs



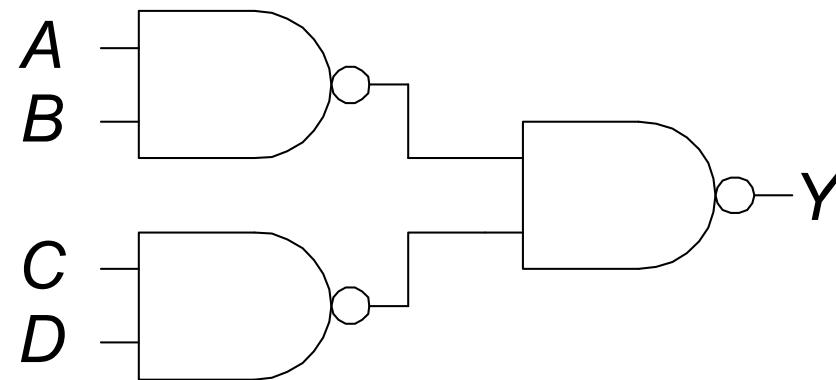
- **Forward:**

- Body changes
- Adds bubble to output



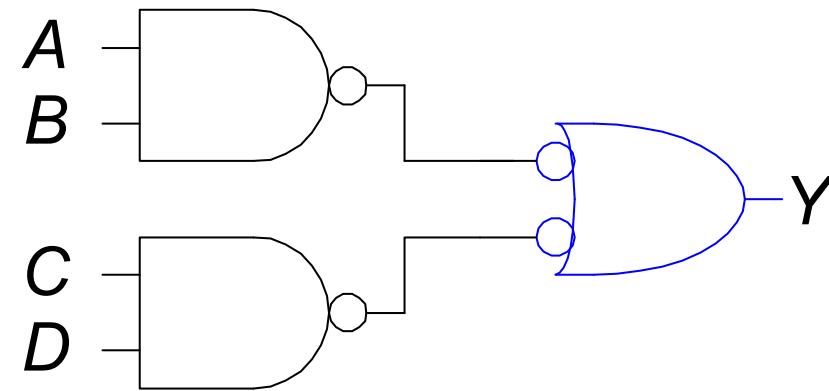
# Bubble Pushing

- What is the Boolean expression for this circuit?



# Bubble Pushing

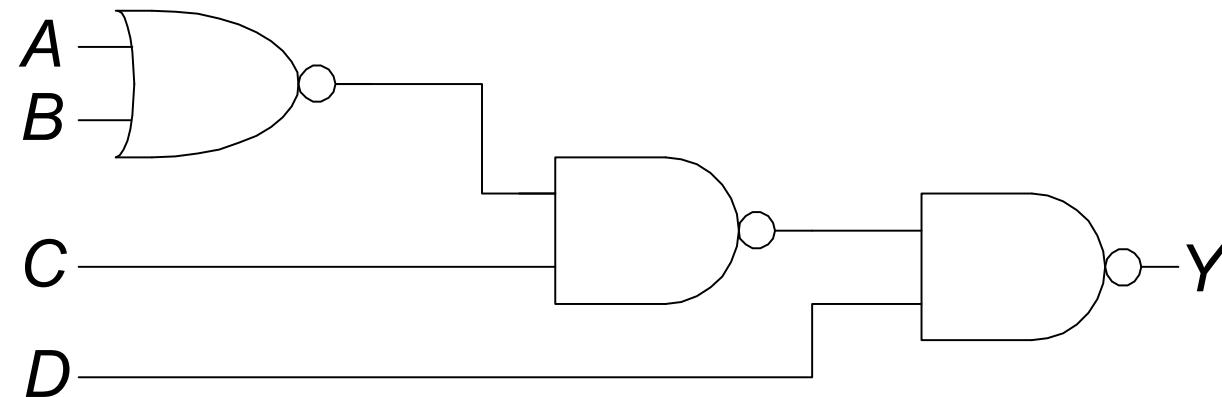
- What is the Boolean expression for this circuit?



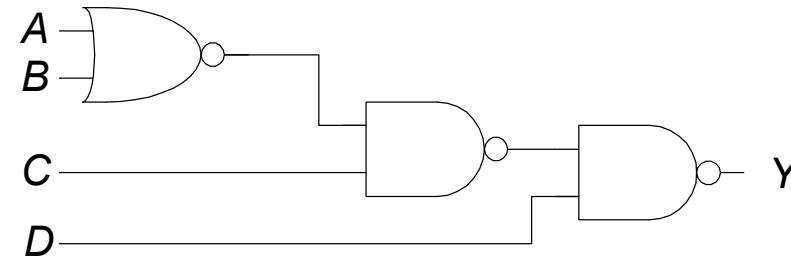
$$Y = AB + CD$$

# Bubble Pushing Rules

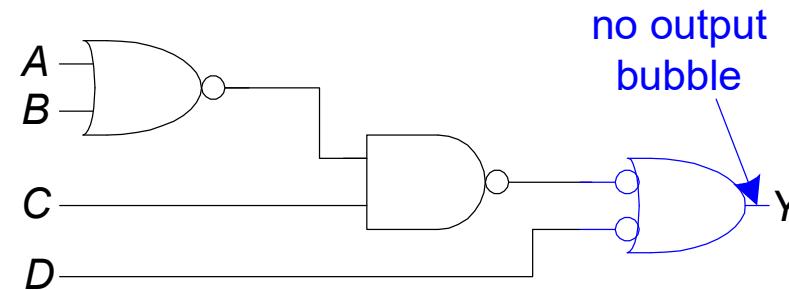
- Begin at output, then work toward inputs
- Push bubbles on final output back
- Draw gates in a form so bubbles cancel



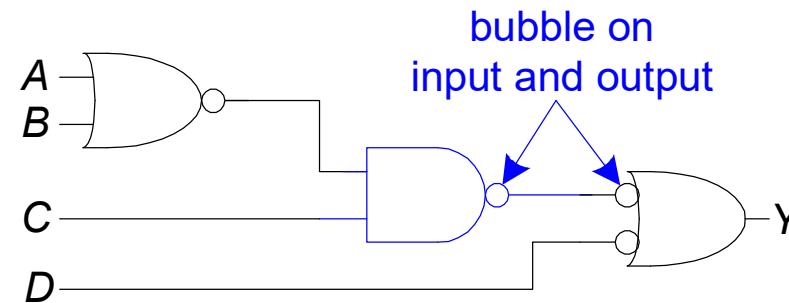
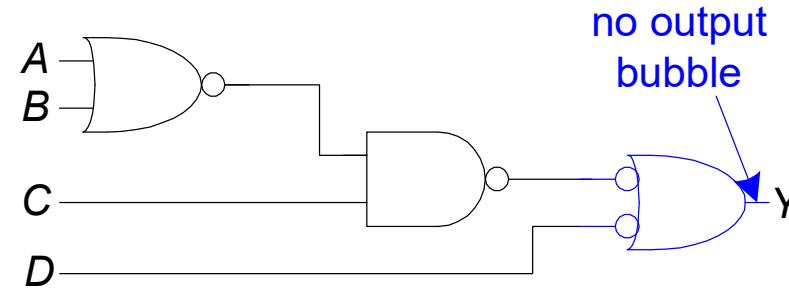
# Bubble Pushing Example



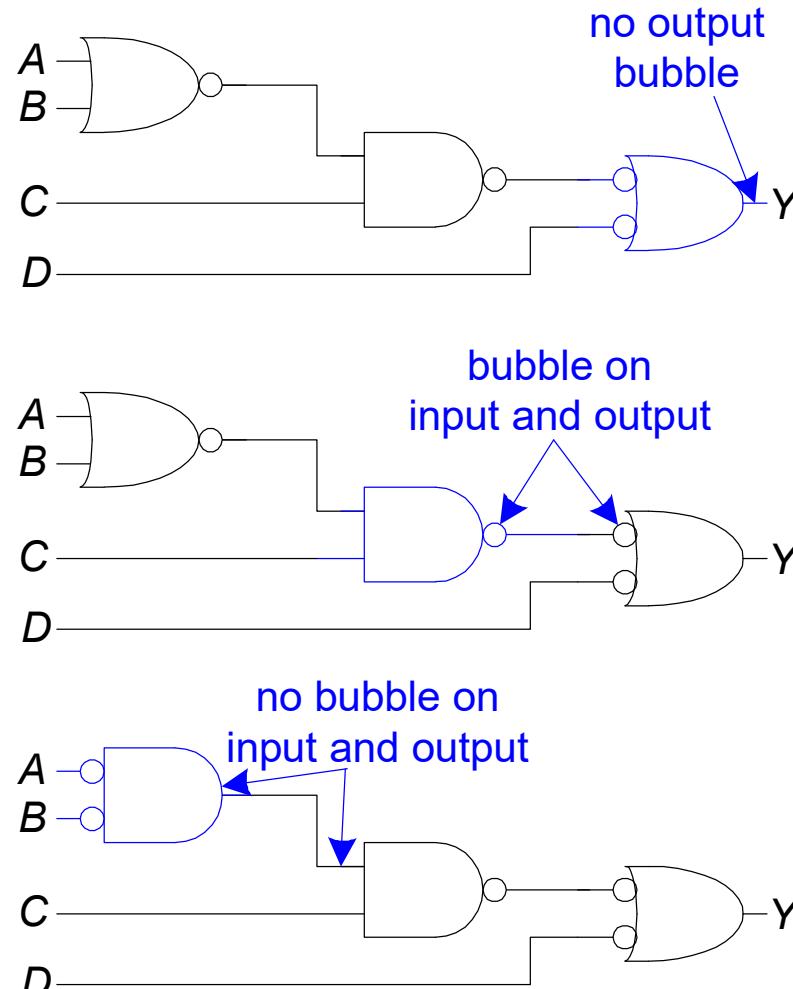
# Bubble Pushing Example



# Bubble Pushing Example



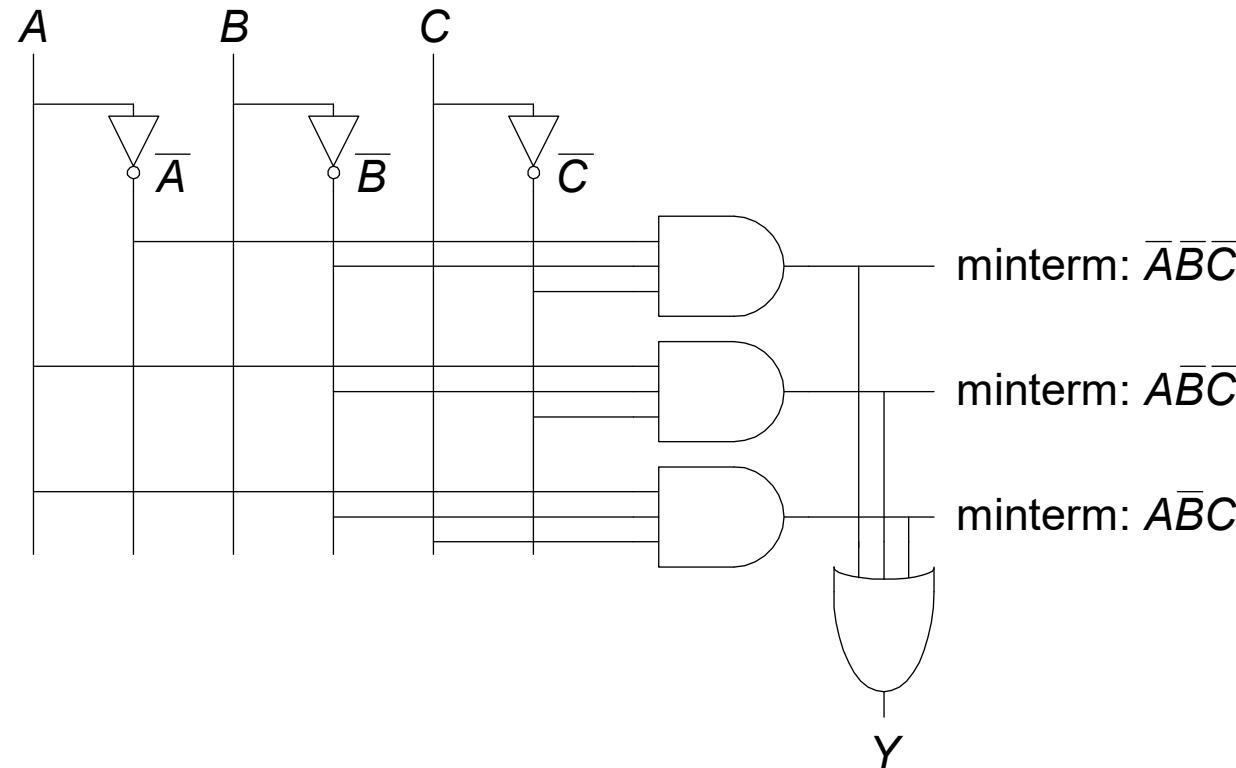
# Bubble Pushing Example



$$Y = \overline{A}\overline{B}C + \overline{D}$$

# From Logic to Gates

- Two-level logic: ANDs followed by ORs
- Example:  $Y = \overline{A}\overline{B}\overline{C} + A\overline{B}\overline{C} + A\overline{B}C$



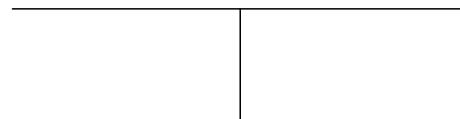
# Circuit Schematics Rules

- Inputs on the left (or top)
- Outputs on right (or bottom)
- Gates flow from left to right
- Straight wires are best

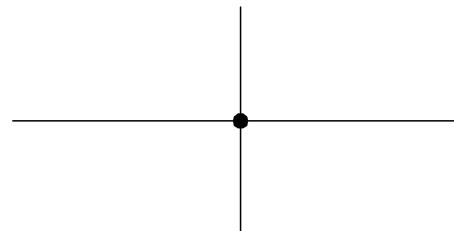
# Circuit Schematic Rules (cont.)

- Wires always connect at a T junction
- A dot where wires cross indicates a connection between the wires
- Wires crossing *without* a dot make no connection

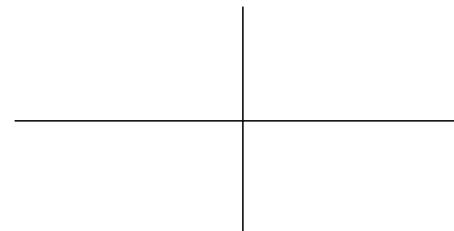
wires connect  
at a T junction



wires connect  
at a dot



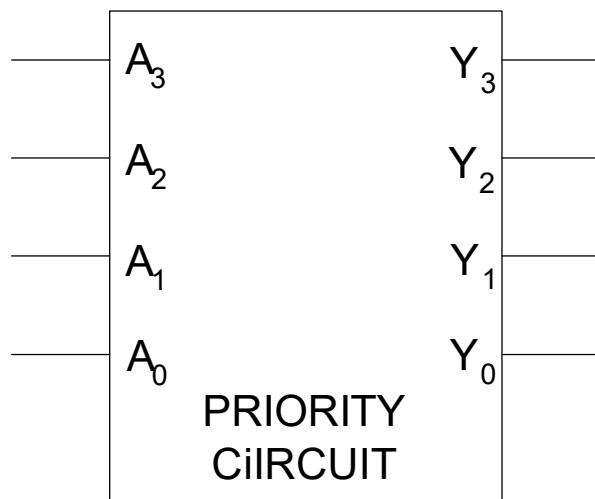
wires crossing  
without a dot do  
not connect



# Multiple-Output Circuits

- **Example: Priority Circuit**

Output asserted  
corresponding to  
most significant  
TRUE input

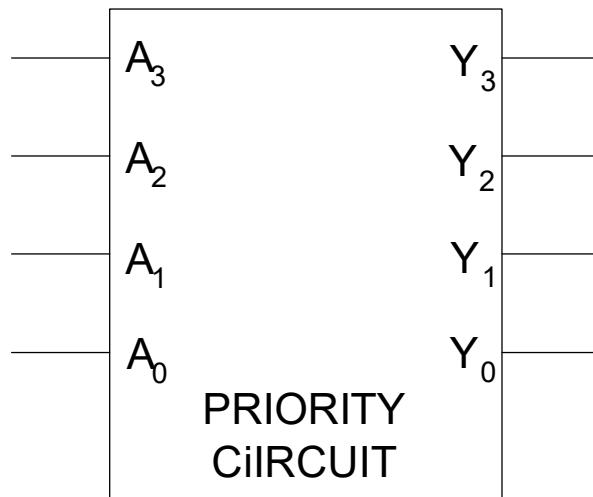


$A_3$	$A_2$	$A_1$	$A_0$	$Y_3$	$Y_2$	$Y_1$	$Y_0$
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	1
0	0	1	0	1	0	0	0
0	0	1	1	1	0	1	1
0	1	0	0	0	1	0	0
0	1	0	1	0	1	1	0
0	1	1	0	1	0	0	0
0	1	1	1	1	0	0	1
1	0	0	0	0	0	1	0
1	0	0	1	0	1	0	0
1	0	1	0	1	1	0	0
1	0	1	1	1	1	1	1
1	1	0	0	0	0	1	0
1	1	0	1	1	0	0	1
1	1	1	0	0	1	0	0
1	1	1	1	1	1	1	0
1	1	1	1	1	1	1	1

# Multiple-Output Circuits

- **Example: Priority Circuit**

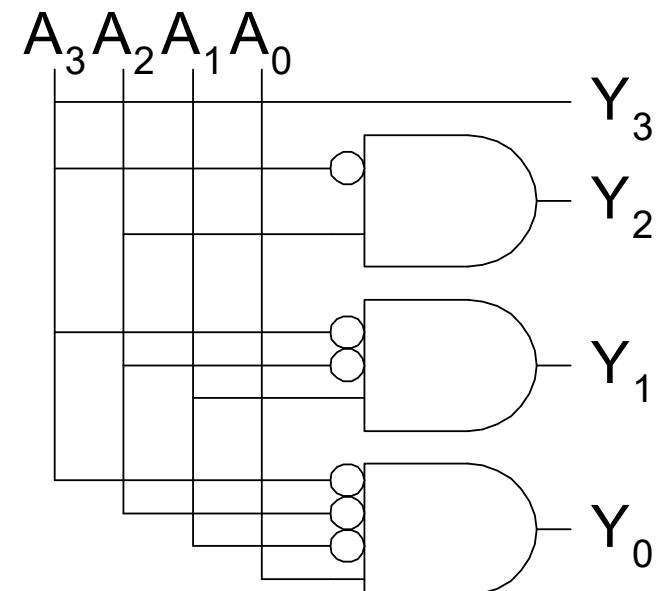
Output asserted  
corresponding to  
most significant  
TRUE input



$A_3$	$A_2$	$A_1$	$A_0$	$Y_3$	$Y_2$	$Y_1$	$Y_0$
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	1
0	0	1	0	0	0	1	0
0	0	1	1	0	0	1	0
0	1	0	0	0	1	0	0
0	1	0	1	0	1	0	0
0	1	1	0	0	1	0	0
0	1	1	1	0	1	0	0
1	0	0	0	0	1	0	0
1	0	0	1	1	0	0	0
1	0	1	1	1	1	0	0
1	1	0	0	1	1	0	0
1	1	0	1	1	1	0	0
1	1	1	0	1	1	0	0
1	1	1	1	1	1	0	0

# Priority Circuit Hardware

$A_3$	$A_2$	$A_1$	$A_0$	$Y_3$	$Y_2$	$Y_1$	$Y_0$
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	1
0	0	1	0	0	0	1	0
0	0	1	1	0	0	1	0
0	1	0	0	0	1	0	0
0	1	0	1	0	1	0	0
0	1	1	0	0	1	0	0
0	1	1	1	0	1	0	0
1	0	0	0	1	0	0	0
1	0	0	1	1	0	0	0
1	0	1	0	1	0	0	0
1	1	0	0	1	0	0	0
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1	1	1	0	1	0	0	0
1	1	1	1	1	0	0	0



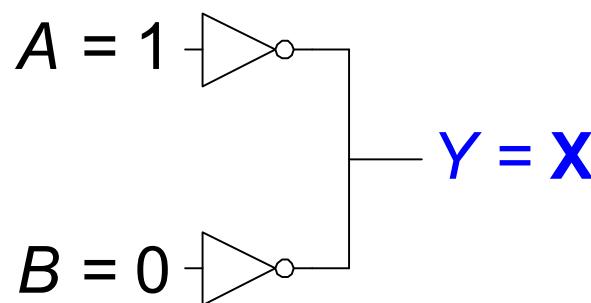
# Don't Cares

$A_3$	$A_2$	$A_1$	$A_0$	$Y_3$	$Y_2$	$Y_1$	$Y_0$
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	1
0	0	1	0	0	0	1	0
0	0	1	1	0	0	1	0
0	1	0	0	0	1	0	0
0	1	0	1	0	1	0	0
0	1	1	0	0	1	0	0
0	1	1	1	0	1	0	0
1	0	0	0	1	0	0	0
1	0	0	1	1	0	0	0
1	0	1	0	1	0	0	0
1	0	1	1	1	0	0	0
1	1	0	0	1	0	0	0
1	1	0	1	1	0	0	0
1	1	1	0	1	0	0	0
1	1	1	1	1	0	0	0

$A_3$	$A_2$	$A_1$	$A_0$	$Y_3$	$Y_2$	$Y_1$	$Y_0$
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	1
0	0	1	X	X	X	1	0
0	1	X	X	1	0	0	0

# Contention: X

- Contention: circuit tries to drive output to 1 **and** 0
  - Actual value somewhere in between
  - Could be 0, 1, or in forbidden zone
  - Might change with voltage, temperature, time, noise
  - Often causes excessive power dissipation



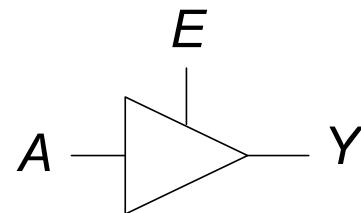
- Warnings:**
  - Contention usually indicates a **bug**.
  - X is used for “don’t care” and contention** - look at the context to tell them apart



# Floating: Z

- Floating, high impedance, open, high Z
- Floating output might be 0, 1, or somewhere in between
  - A voltmeter won't indicate whether a node is floating

Tristate Buffer



E	A	Y
0	0	Z
0	1	Z
1	0	0
1	1	1

# Tristate Busses

- Floating nodes are used in tristate busses
  - Many different drivers
  - Exactly one is active at once

