FROM ZERO TO ONE

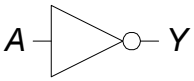
Logic Gates

- **Perform logic functions:**
  - inversion (NOT), AND, OR, NAND, NOR, etc.
- **Single-input:**
  - NOT gate, buffer
- **Two-input:**
  - AND, OR, XOR, NAND, NOR, XNOR
- **Multiple-input**

FROM ZERO TO ONE

Single-Input Logic Gates

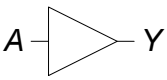
NOT



$Y = \overline{A}$

A	Y
0	
1	

BUF



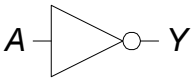
$Y = A$

A	Y
0	
1	

FROM ZERO TO ONE

Single-Input Logic Gates

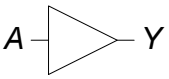
NOT



$Y = \overline{A}$

A	Y
0	1
1	0

BUF



$Y = A$

A	Y
0	0
1	1

FROM ZERO TO ONE

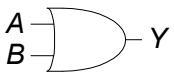
Two-Input Logic Gates

AND

$Y = AB$

A	B	Y
0	0	
0	1	
1	0	
1	1	

OR



$Y = A + B$

A	B	Y
0	0	
0	1	
1	0	
1	1	

FROM ZERO TO ONE

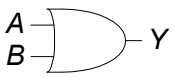
Two-Input Logic Gates

AND

$Y = AB$

A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

OR



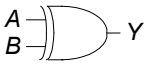
$Y = A + B$

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	1

FROM ZERO TO ONE

More Two-Input Logic Gates

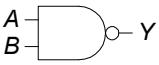
XOR



$Y = A \oplus B$

A	B	Y
0	0	
0	1	
1	0	
1	1	

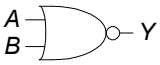
NAND



$Y = \overline{AB}$

A	B	Y
0	0	
0	1	
1	0	
1	1	

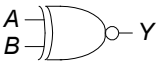
NOR



$Y = \overline{A + B}$

A	B	Y
0	0	
0	1	
1	0	
1	1	

XNOR



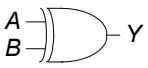
$Y = \overline{A \oplus B}$

A	B	Y
0	0	
0	1	
1	0	
1	1	

FROM ZERO TO ONE

More Two-Input Logic Gates

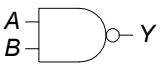
XOR



$Y = A \oplus B$

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

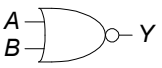
NAND



$Y = \overline{AB}$

A	B	Y
0	0	1
0	1	1
1	0	1
1	1	0

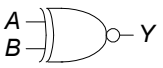
NOR



$Y = \overline{A + B}$

A	B	Y
0	0	1
0	1	0
1	0	0
1	1	0

XNOR



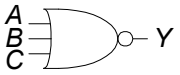
$Y = \overline{A \oplus B}$

A	B	Y
0	0	1
0	1	0
1	0	0
1	1	1

FROM ZERO TO ONE

Multiple-Input Logic Gates

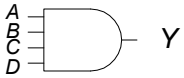
NOR3



$Y = \overline{A+B+C}$

A	B	C	Y
0	0	0	
0	0	1	
0	1	0	
0	1	1	
1	0	0	
1	0	1	
1	1	0	
1	1	1	

AND4



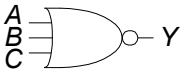
$Y = ABCD$

A	B	C	Y
0	0	0	
0	0	1	
0	1	0	
0	1	1	
1	0	0	
1	0	1	
1	1	0	
1	1	1	

FROM ZERO TO ONE

Multiple-Input Logic Gates

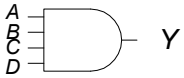
NOR3



$Y = \overline{A+B+C}$

A	B	C	Y
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	0

AND4



$Y = ABCD$

A	B	C	Y
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

- Multi-input XOR: Odd parity

ELSEVIER

FROM ZERO TO ONE

Logic Levels

- Discrete voltages represent 1 and 0
- For example:
  - 0 = *ground* (GND) or 0 volts
  - 1 = V_{DD} or 5 volts
- What about 4.99 volts? Is that a 0 or a 1?
- What about 3.2 volts?

ELSEVIER

FROM ZERO TO ONE

Logic Levels

- *Range* of voltages for 1 and 0
- Different ranges for inputs and outputs to allow for *noise*

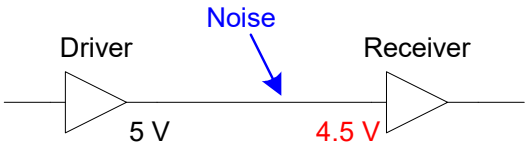
FROM ZERO TO ONE

What is Noise?

FROM ZERO TO ONE

What is Noise?

- **Anything that degrades the signal**
  - E.g., resistance, power supply noise, coupling to neighboring wires, etc.
- **Example:** a gate (driver) outputs 5 V but, because of resistance in a long wire, receiver gets 4.5 V



ELSEVIER

FROM ZERO TO ONE

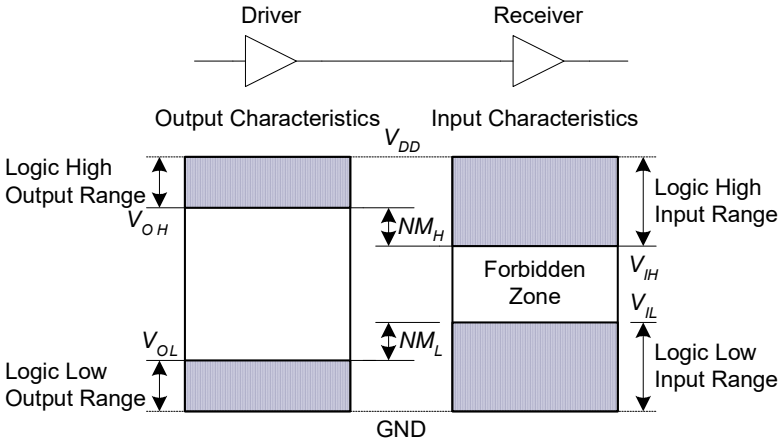
The Static Discipline

- With logically valid inputs, every circuit element must produce logically valid outputs
- Use limited ranges of voltages to represent discrete values

ELSEVIER

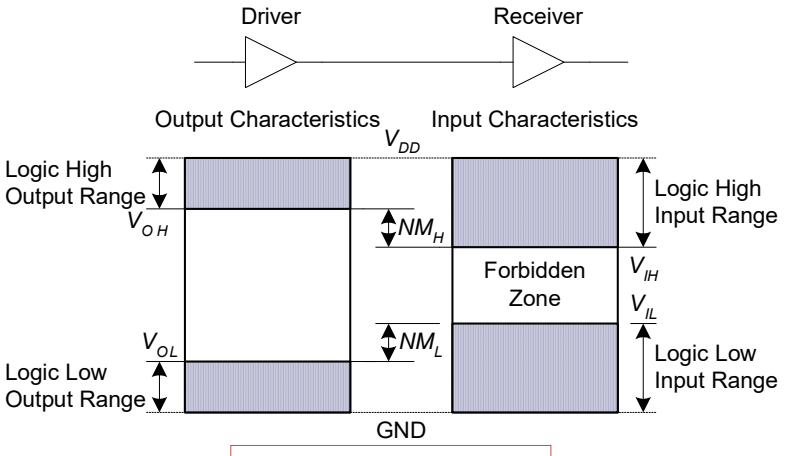
FROM ZERO TO ONE

Logic Levels



FROM ZERO TO ONE

Noise Margins



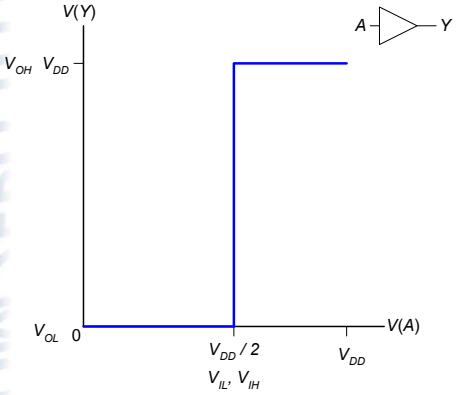
$$NM_H = V_{OH} - V_{IH}$$

$$NM_L = V_{IL} - V_{OL}$$

DC Transfer Characteristics

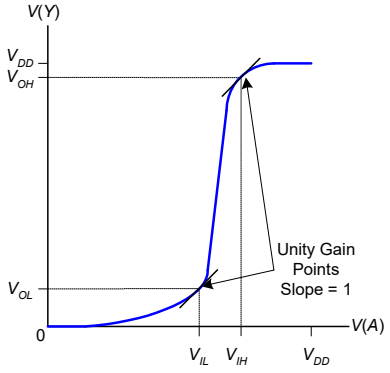
FROM ZERO TO ONE

Ideal Buffer:



$NM_H = NM_L = V_{DD}/2$

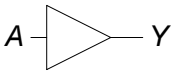
Real Buffer:

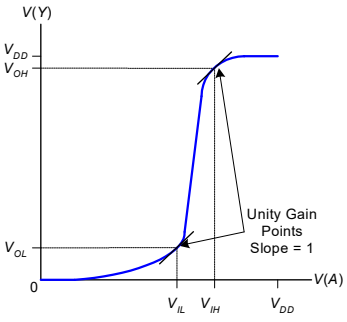


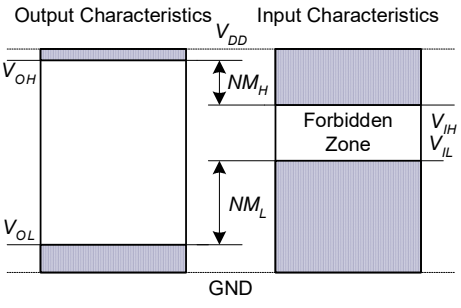
NM_H , $NM_L < V_{DD}/2$

DC Transfer Characteristics

FROM ZERO TO ONE







FROM ZERO TO ONE

V_{DD} Scaling

- In 1970's and 1980's, V_{DD} = 5 V
- V_{DD} has dropped
  - Avoid frying tiny transistors
  - Save power
- 3.3 V, 2.5 V, 1.8 V, 1.5 V, 1.2 V, 1.0 V, …
- Be careful connecting chips with different supply voltages

Chips operate because they contain magic smoke

Proof:

- if the magic smoke is let out, the chip stops working

FROM ZERO TO ONE

Logic Family Examples

Logic Family	V_{DD}	V_{IL}	V_{IH}	V_{OL}	V_{OH}
TTL	5 (4.75 - 5.25)	0.8	2.0	0.4	2.4
CMOS	5 (4.5 - 6)	1.35	3.15	0.33	3.84
LVTTL	3.3 (3 - 3.6)	0.8	2.0	0.4	2.4
LVCMOS	3.3 (3 - 3.6)	0.9	1.8	0.36	2.7