

Measures of Central Tendency

EDP 613

Week 3

Basic Idea



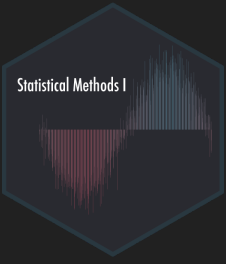
The mean, median and mode are measures of central tendency and attempt to summarize the typical value of a variable.

Why?

These may help us draw conclusions about a specific group or compare different groups using a single numerical value.



Recall Distributions

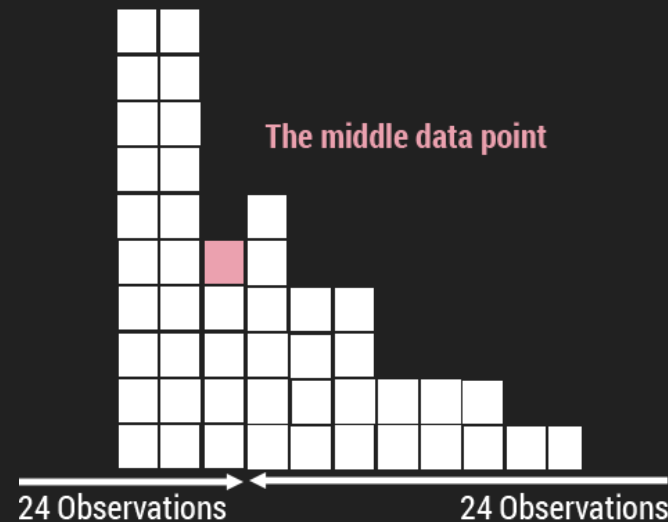


Measures of Central Tendency: The Mean

- The *average* number.
- There are other types of means (e.g. geometric, harmonic, etc.) but we are only using the *arithmetic* mean.
- Essentially the **balancing point** or center of mass of a distribution
- Found by adding all data points and dividing by the number of data points

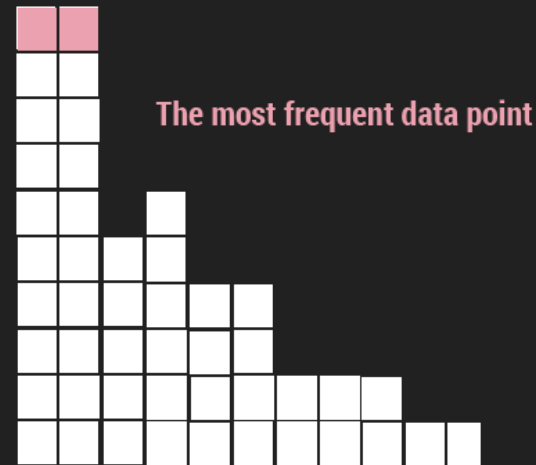
Measures of Central Tendency: The Median

- The *middle* number
- Essentially the **point that cuts a data set in half**
- Found by ordering data points from least to greatest or greatest to least and locating the middle number - if there are two middle data points, they are averaged



Measures of Central Tendency: The Mode

- The *most frequent* number
- Essentially the point that occurs the most
- Found by determining the data point(s) that appear the most - if none exists, then there is no mode





Basic Procedure: The Mean

- **Mean**
 - Add the numbers up, divide by the total number of values in the set.
 - Denoted by \bar{Y}

Example

Compute the mean for the following sample: $\{21.3, 31.4, 12.7, 41.6\}$

Solution

$$\begin{aligned}\bar{Y} &= \frac{21.3 + 31.4 + 12.7 + 41.6}{4} \\ &= \frac{107}{4} \\ &= 26.75\end{aligned}$$

Give it a Try

Compute the mean for the following sample: $\{2, 5, 5, 7, 7, 8, 9\}$

Solution

$$\bar{Y} = \frac{2 + 5 + 5 + 7 + 7 + 8 + 9}{6}$$

$$= \frac{43}{6}$$

$$\approx 7.17$$

Basic Procedure: The Median

- **Median**
 - Put the numbers in order from least to greatest or greatest to least and find the middle number.
 - If there are two middle numbers, average them.

Example

Compute the median for the following sample: $\{2, 5, 5, 7, 7\}$

Solution

- Since these data point are already in numerical order, we can use them as is without reordering.
- $n = 5$ which is an odd number so we can locate the median by

$$\frac{n + 1}{2} = \frac{5 + 1}{2} = \frac{6}{2} = 3$$

telling us to look in the *third position* from either side of the list of numbers.

- In

$$\{2, 5, 5, 7, 7\}$$

the middle number is 5 so that must be the median!

Give it a Try

Compute the mean for the following sample: $\{21.3, 31.4, 12.7, 41.6\}$

Solution

- Since these data point are NOT already in numerical order, we must reorder them.

$$\{12.7, 21.3, 31.4, 41.6\}$$

- $n = 4$ which is an even number so we can locate the median by taking the mean of the the numbers in

- $\frac{n}{2} = \frac{4}{2} = 2$, or the *second position*
- $\frac{n}{2} + 1 = \frac{4}{2} + 1 = 3$, or the *third position*
- So the median is

$$\frac{21.3 + 31.4}{2} = 26.35$$

Basic Procedure: The Mode



- **Mode**
 - Find the number(s) that appear the most.
 - If none exists, then there is no mode.

Example

Compute the mode for the following sample: $\{2, 5, 5, 7, 7\}$

Solution

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Data point	Frequency
2	1
5	2
7	2

- The data points 5 and 7 repeat twice while 2 only appears once.
- The modes are 5 and 7.
- Known as *bimodal*. Three modes would be *trimodal* and so on.

Give it a Try

Compute the mode for the following sample: $\{21.3, 31.4, 12.7, 41.6\}$

Solution

- No data point appears more than once points appear once.
- Therefore there is no mode.

Something to Think About



- A statistic is **resistant** if its value is not affected by extreme values (large or small) in the data set.
- Which of the measures of central tendency are resistant?

That's it. We will work more with R next week!

