# Problem psi

$$R_0, X \vdash_{\text{ipl}} \tilde{g}$$
?

### Not Proved

Clauses in  $R_0$ : 24

Clauses in X: 9

Atoms: 22

Calls to the SAT-solver: 14

Restarts: 4

Worlds in the countermodel: 3

 $R_0$  and X are defined at the end of the document

### Start

(0)  $R_0 \vdash_{\mathbf{c}} \tilde{g}$ ?

 $No(\emptyset)$ 

New world:  $w_0$ 

$$\frac{W \mid \lambda \text{ s.t. } w \not \succ_W \lambda}{w_0 \mid \emptyset \mid \lambda_0, \lambda_1, \lambda_2, \lambda_3, \lambda_4, \lambda_5, \lambda_6, \lambda_7, \lambda_8}$$

Selected:  $\langle w_0, \lambda_0 = (p_4 \to p_3) \to \tilde{p}_{11} \rangle$ 

(1)  $R_0, w_0, p_4 \vdash_{c} p_3$ ?

No( $\{\tilde{p}_{10}, \tilde{p}_{14}, p_4\}$ )

New world:  $w_1$ 

W		$\lambda$ s.t. $w \not\succ_W \lambda$	
$w_1$	$ ilde{p}_{10}, ilde{p}_{14},p_4$	$\lambda_3,  \lambda_4,  \lambda_5,  \lambda_7,  \lambda_8$	
$w_0$	Ø	$\lambda_2, \lambda_3, \lambda_4, \lambda_5, \lambda_6, \lambda_7, \lambda_8$	

Selected:  $\langle w_1, \lambda_3 = (p_3 \to p_2) \to \tilde{p}_8 \rangle$ 

(2)  $R_0, w_1, p_3 \vdash_{\mathsf{c}} p_2$ ?

Yes( $\{\tilde{p}_{10}, p_3\}$ )

 $R_0, \, \tilde{p}_{10}, \, p_3 \, \vdash_{\mathrm{c}} \, p_2$ 

New clause:  $\varphi_0 = \tilde{p}_{10} \to \tilde{p}_8$ 

 $R_1 = R_0, \varphi_0$ 

#### Restart 1

(3) 
$$R_1 \vdash_{\mathsf{c}} \tilde{g}$$
?

No(
$$\{\tilde{p}_{11},\,\tilde{p}_{14},\,\tilde{p}_{7},\,p_{3}\}$$
)

New world:  $w_2$ 

Selected: 
$$\langle w_2, \lambda_1 = (p_4 \to p_1) \to \tilde{p}_{13} \rangle$$

(4) 
$$R_1, w_2, p_4 \vdash_{\mathbf{c}} p_1 ?$$

Yes(
$$\{\tilde{p}_{11}, p_4\}$$
)

$$R_1, \, \tilde{p}_{11}, \, p_4 \, \vdash_{\mathrm{c}} \, p_1$$

New clause: 
$$\varphi_1 = \tilde{p}_{11} \rightarrow \tilde{p}_{13}$$

$$R_2 = R_1, \varphi_1$$

### Restart 2

### (5) $R_2 \vdash_{\mathbf{c}} \tilde{g}$ ?

No(
$$\{\tilde{p}_{10}, \, \tilde{p}_{14}, \, \tilde{p}_8, \, p_4\}$$
)

New world:  $w_3$ 

W		$\lambda \text{ s.t. } w \not\succ_W \lambda$
$w_3$	$ ilde{p}_{10}, ilde{p}_{14}, ilde{p}_{8},p_{4}$	$\lambda_4, \lambda_5, \lambda_7, \lambda_8$

Selected: 
$$\langle w_3, \lambda_4 = (p_2 \to p_3) \to \tilde{p}_7 \rangle$$

## (6) $R_2, w_3, p_2 \vdash_{\mathbf{c}} p_3 ?$

No(
$$\{\tilde{p}_1, \tilde{p}_{10}, \tilde{p}_{14}, \tilde{p}_8, p_2, p_4\}$$
)

New world:  $w_4$ 

W		$\lambda$ s.t. $w \not \succ_W \lambda$
$w_4$	$\tilde{p}_1, \tilde{p}_{10}, \tilde{p}_{14}, \tilde{p}_8, p_2, p_4$	$\lambda_8$
$w_3$	$\tilde{p}_{10},\tilde{p}_{14},\tilde{p}_{8},p_{4}$	$\lambda_7, \lambda_8$

Selected: 
$$\langle w_4, \lambda_8 = (p_0 \to \bot) \to \tilde{g} \rangle$$

(7) 
$$R_2, w_4, p_0 \vdash_{\mathbf{c}} \bot ?$$

No(
$$\{\tilde{g}, \tilde{p}_1, \tilde{p}_{10}, \tilde{p}_{14}, \tilde{p}_8, p_0, p_2, p_4\}$$
)

New world:  $w_5$ 

W		$\lambda$ s.t. $w \not \succ_W \lambda$
$w_5$	$\tilde{g},  \tilde{p}_1,  \tilde{p}_{10},  \tilde{p}_{14},  \tilde{p}_8,  p_0,  p_2,  p_4$	Ø
$w_4$	$\tilde{p}_1,\tilde{p}_{10},\tilde{p}_{14},\tilde{p}_8,p_2,p_4$	Ø
$w_3$	$ ilde{p}_{10}, ilde{p}_{14}, ilde{p}_{8},p_{4}$	$\lambda_7$

Selected:  $\langle w_3, \lambda_7 = (p_1 \to p_2) \to \tilde{p}_1 \rangle$ 

(8) 
$$R_2, w_3, p_1 \vdash_{c} p_2$$
?  
 $Yes(\{\tilde{p}_{14}, p_1\})$   
 $R_2, \tilde{p}_{14}, p_1 \vdash_{c} p_2$ 

New clause: 
$$\varphi_2 = \tilde{p}_{14} \rightarrow \tilde{p}_1$$

$$R_3 = R_2, \varphi_2$$

### Restart 3

(9) 
$$R_3 \vdash_{\mathbf{c}} \tilde{g}$$
 ?  
No( $\{\tilde{p}_{10}, \tilde{p}_{13}, \tilde{p}_2, \tilde{p}_8, p_1\}$ )

New world:  $w_6$ 

Selected:  $\langle w_6, \lambda_0 = (p_4 \to p_3) \to \tilde{p}_{11} \rangle$ 

(10) 
$$R_3, w_6, p_4 \vdash_{\mathbf{c}} p_3 ?$$

$$\operatorname{Yes}(\left\{\tilde{p}_{13},\,p_{4}\right\})$$

$$R_3, \, \tilde{p}_{13}, \, p_4 \, \vdash_{\mathrm{c}} \, p_3$$

New clause: 
$$\varphi_3 = \tilde{p}_{13} \rightarrow \tilde{p}_{11}$$

$$R_4 = R_3, \varphi_3$$

### Restart 4

(11) 
$$R_4 \vdash_{c} \tilde{g}$$
?

No(
$$\{\tilde{p}_1, \, \tilde{p}_{10}, \, \tilde{p}_{14}, \, \tilde{p}_8, \, p_4\}$$
)

New world:  $w_7$ 

Selected:  $\langle w_7, \lambda_4 = (p_2 \to p_3) \to \tilde{p}_7 \rangle$ 

(12)  $R_4, w_7, p_2 \vdash_{\mathbf{c}} p_3 ?$ 

No(
$$\{\tilde{p}_1, \tilde{p}_{10}, \tilde{p}_{14}, \tilde{p}_8, p_2, p_4\}$$
)

New world:  $w_8$ 

W		$\lambda$ s.t. $w \not\succ_W \lambda$
$w_8$	$\tilde{p}_1,\tilde{p}_{10},\tilde{p}_{14},\tilde{p}_8,p_2,p_4$	$\lambda_8$
$w_7$	$\tilde{p}_1,\tilde{p}_{10},\tilde{p}_{14},\tilde{p}_8,p_4$	$\lambda_8$

Selected:  $\langle w_8, \lambda_8 = (p_0 \to \bot) \to \tilde{g} \rangle$ 

(13)  $R_4, w_8, p_0 \vdash_{\mathbf{c}} \bot ?$ 

No(
$$\{\tilde{g}, \tilde{p}_1, \tilde{p}_{10}, \tilde{p}_{14}, \tilde{p}_8, p_0, p_2, p_4\}$$
)

New world:  $w_9$ 

W		$\lambda$ s.t. $w \not \succ_W \lambda$
$w_9$	$\tilde{g},  \tilde{p}_1,  \tilde{p}_{10},  \tilde{p}_{14},  \tilde{p}_8,  p_0,  p_2,  p_4$	Ø
$w_8$	$\tilde{p}_1,\tilde{p}_{10},\tilde{p}_{14},\tilde{p}_8,p_2,p_4$	Ø
$w_7$	$ ilde{p}_1, ilde{p}_{10}, ilde{p}_{14}, ilde{p}_{8},p_4$	Ø

## Countermodel found

# Problem description

Flat clauses  $R_0$  (24):

- 1.  $\tilde{p}_1 \wedge \tilde{p}_2 \rightarrow \tilde{p}_0$
- $2. \ \tilde{p}_3 \to p_3$
- 3.  $\tilde{p}_3 \rightarrow p_4$
- 4.  $\tilde{p}_4 \rightarrow p_2$
- 5.  $\tilde{p}_4 \rightarrow \tilde{p}_3$
- 6.  $\tilde{p}_5 \rightarrow p_1$
- 7.  $\tilde{p}_5 \rightarrow \tilde{p}_4$
- 8.  $\tilde{p}_0 \rightarrow \tilde{p}_5$
- 9.  $\tilde{p}_7 \wedge \tilde{p}_8 \rightarrow \tilde{p}_6$

- 10.  $\tilde{p}_6 \rightarrow \tilde{p}_5$
- 11.  $\tilde{p}_{10} \wedge \tilde{p}_{11} \rightarrow \tilde{p}_9$
- 12.  $\tilde{p}_9 \rightarrow \tilde{p}_5$
- 13.  $\tilde{p}_{13} \wedge \tilde{p}_{14} \rightarrow \tilde{p}_{12}$
- 14.  $\tilde{p}_{12} \rightarrow \tilde{p}_5$
- 15.  $p_0 \rightarrow \tilde{g}$
- 16.  $p_1 \wedge p_2 \wedge p_3 \wedge p_4 \rightarrow \tilde{g}$
- 17.  $p_3 \to \tilde{p}_{11}$
- 18.  $p_1 \to \tilde{p}_{13}$
- 19.  $p_4 \to \tilde{p}_{10}$
- 20.  $p_2 \rightarrow \tilde{p}_8$
- 21.  $p_3 \rightarrow \tilde{p}_7$
- 22.  $p_1 \rightarrow \tilde{p}_2$
- 23.  $p_4 \rightarrow \tilde{p}_{14}$
- 24.  $p_2 \rightarrow \tilde{p}_1$

Implication clauses X (9):

- $\lambda_0 = (p_4 \to p_3) \to \tilde{p}_{11}$
- $\lambda_1 = (p_4 \to p_1) \to \tilde{p}_{13}$
- $\lambda_2 = (p_3 \to p_4) \to \tilde{p}_{10}$
- $\lambda_3 = (p_3 \to p_2) \to \tilde{p}_8$
- $\lambda_4 = (p_2 \to p_3) \to \tilde{p}_7$
- $\lambda_5 = (p_2 \to p_1) \to \tilde{p}_2$
- $\lambda_6 = (p_1 \to p_4) \to \tilde{p}_{14}$
- $\lambda_7 = (p_1 \to p_2) \to \tilde{p}_1$
- $\lambda_8 = (p_0 \to \bot) \to \tilde{g}$

Added clauses (4):

- $\varphi_0 = \tilde{p}_{10} \rightarrow \tilde{p}_8$
- $\varphi_1 = \tilde{p}_{11} \rightarrow \tilde{p}_{13}$
- $\varphi_2 = \tilde{p}_{14} \to \tilde{p}_1$
- $\varphi_3 = \tilde{p}_{13} \to \tilde{p}_{11}$