

COMP 285: Practice Midterm Questions

The following are questions meant to help you practice, and cannot be submitted for a grade.

Important Notes

- *It is meant to give you a chance to do some practice questions after having reviewed the slides, quizzes, in-class exercises, homeworks, etc.*
- *It should give a rough sense of some ways questions might be posed, though there's no guarantee that the actual midterm will have the exact same format (at a minimum, one difference is that the actual midterm will show the point values associated with the questions).*
- *It should give a rough idea of the level of mastery expected generally, though more/less mastery may be expected for any given topic.*

Thanks for reading the notes above - the big picture thing is that I want to be sure you use this resource appropriately, while at the same time **do not neglect the many other more comprehensive resources!**

Asymptotic Analysis

1. $O(n/100 + \log(n) + 200)$ can be simplified to $O(n)$. True or False?
2. $2x + x^2/2 = \Theta(x^2 + 2x + x \log(x))$. True or False?
3. $x + 20 = \Omega(999)$. True or False?

For questions 4 - 6, refer to the *containsDuplicates* pseudocode.

```
algorithm containsDuplicates
  input: size n vector of ints called vec
  output: true if vec contains duplicates, false otherwise

  for i = 0...n-1
    for j = i + 1...n-1 // Notice we start at i + 1, not j
      if vec[i] == vec[j]
        return true
  return false
```

4. What is the **best-case runtime** of containsDuplicates? Define n, provide a tight upper bound with Big-O, and justify your answer.
5. What is the **worst-case runtime** of containsDuplicates? Define n, provide a tight upper bound with Big-O, and justify your answer.
6. What is the **worst-case space complexity** of containsDuplicates? Define n, provide a tight upper bound with Big-O, and justify your answer.

Using the Right Tools

7. Which of the data structure implementations below have $O(1)$ runtime on average for element insertions? Select **ALL** that apply.
- A stack (C++: `std::stack`)
 - A queue (C++: `std::queue`)
 - A hash set (C++: `std::unordered_set`)
 - A hash map (C++: `std::unordered_map`)
 - A vector (C++: `std::vector`)
8. Which of the data structure implementations below have $O(1)$ runtime on average for element searching? Select **ALL** that apply.
- A stack (C++: `std::stack`)
 - A queue (C++: `std::queue`)
 - A hash set (C++: `std::unordered_set`)
 - A hash map (C++: `std::unordered_map`)
 - A vector (C++: `std::vector`)
9. Which of the data structure implementations below have $O(1)$ runtime on average for element removal? Select **ALL** that apply.
- A stack (C++: `std::stack`)
 - A queue (C++: `std::queue`)
 - A hash set (C++: `std::unordered_set`)
 - A hash map (C++: `std::unordered_map`)
 - A vector (C++: `std::vector`)

Sorting

10. Which array of the following will CountingSort take the most number of steps on? Select **ONE**.

- a. [1, 2, 3, 4, 5, 6]
- b. [5, 43, 3, 11, 6, 9]
- c. [3, 1, 34, 3, 4, 81]
- d. [4, 4754, 4, 24, 1, 33]

11. For each of the below, explain in 1 - 2 sentences what they mean with respect to sorting.

- Adaptive

- Stability

- In-Place

12. Given an array is already sorted, which sort will take the least time? Select **ONE**.

- a. Insertion Sort
- b. Quick Sort
- c. Merge Sort
- d. Selection Sort

For questions 12 - 13, refer to quickSort provided.

```
algorithm quickSort
  Input: vector<int> vec of size N
  Output: vector<int> with sorted elements

  if N < 2
    return vec
  pivot = findPivot(vec)
  left = new empty vec
  right = new empty vec
  for index i = 0, 1, 2, ... N-2
    if vec[i] <= pivot
      left.push_back(vec[i])
    else
      right.push_back(vec[i])
  return quickSort(left) + [pivot] + quickSort(right)
```

13. Suppose findPivot is a function which finds the element that will partition the list in two (nearly) equal halves in linear time while using constant space. What is the **worst-case runtime** of quickSort in this case? Justify your answer.

14. Challenge: what is the **worst-case space complexity** of quickSort in this case? Justify your answer.

Master Theorem

15. Find the runtime of an algorithm described by the following recurrence relation:

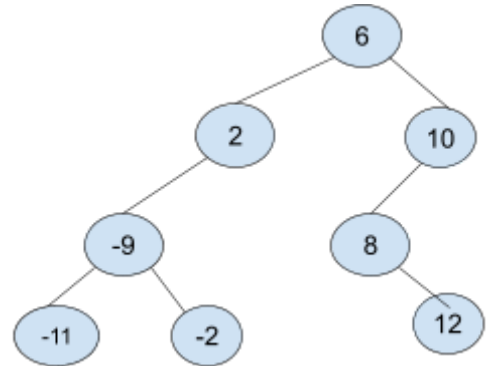
$T(n) = T(n/2) + O(1)$. You may show your work for partial credit.

16. Write a recurrence relation for MergeSort. You may show your work for partial credit.

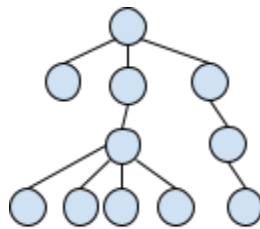
Trees

17. Is the tree on the right a Binary Search Tree? Explain.

18. What would an post-order traversal of this tree print out?



19. Complete the recursive case of countAtLevel in the box, which counts the number of nodes at each level in a Tree.



k = 0, #
nodes = 1

k = 1, #
nodes = 3

k = 2, #
nodes = 2

k = 3, #
nodes = 5

algorithm countAtLevel

input: TreeNode root and a level k

output: the number of nodes at level k in root

if level == 0 // base case

return 1

total = 0

for each element child in root->getChildren()

total +=

return total

20. What is the **best-case runtime** of searching for a node in a balanced BST. Give an example of when the best-case happens.

21. What is the **worst-case runtime of searching** for a node in a **balanced** BST. Give an example of when the worst-case happens.

For question 21, use the following pseudocode

```
BSTremove(t, v) // from visualgo.net
  search for v
  if v is a leaf
    delete leaf v
  else if v has 1 child
    bypass v
  else replace v with successor
```

22. Draw what the BST *t* below will look like after `BSTremove(t, 8)`. (*Hint: Which node must replace the root node in order to maintain the BST property?*)

