

# Monocular Visual Odometry

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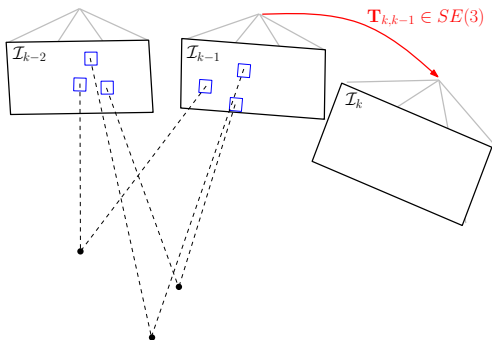
# Feature-based Visual Odometry

## Goal

*Estimate relative pose  $\mathbf{T}_{k,k-1}$  of new frame w.r.t. previous frame.*

## Pipeline

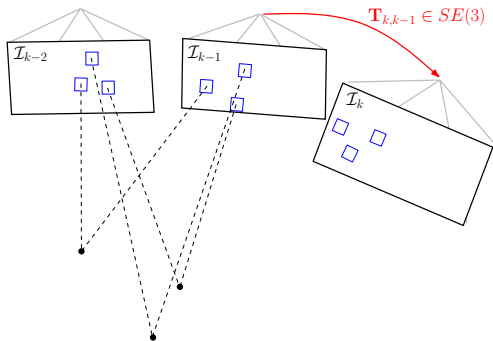
1. Feature selection
2. Feature matching
3. Pose estimation
4. Pose refinement
5. Triangulation



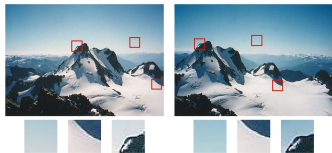
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## Pipeline

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## Which features?

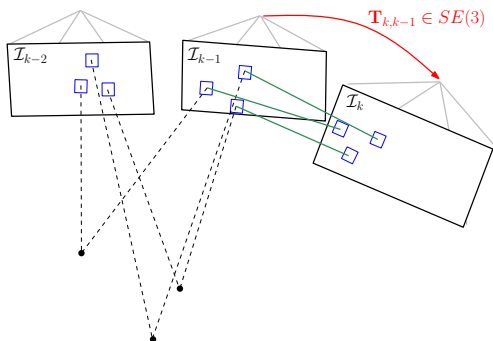


Source: Szeliski, "Computer Vision: Algorithms and Applications", Springer 2010.

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## Pipeline

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## Matching Strategies

- Fast: SSD/NCC over small patch
- Robust: Match invariant feature descriptors

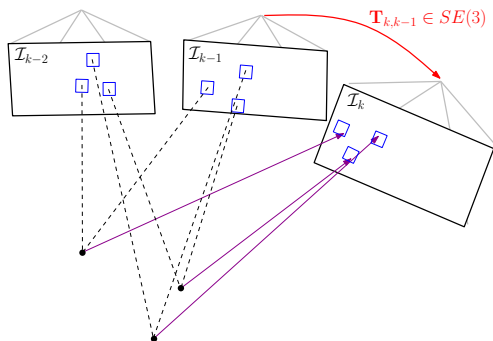
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## Epipolar Geometry

Three 3D point to 2D feature correspondences are necessary to estimate the 3D camera pose.

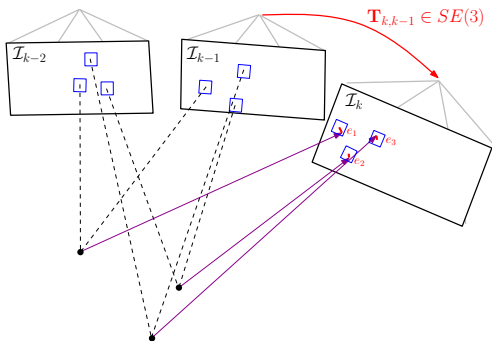


# Feature-based Visual Odometry

## Pipeline

1. Feature selection
2. Feature matching
3. Pose estimation
4. **Pose refinement**
5. Triangulation

Minimize reprojection errors



$$\mathbf{T}_{k,k-1} = \arg \min_{\mathbf{T}} \frac{1}{2} \sum_i \| \mathbf{u}_i - \pi(\mathbf{T}_{k-1} \mathbf{p}_i) \|^2 .$$

Can be solved with Gauss  
Newton.

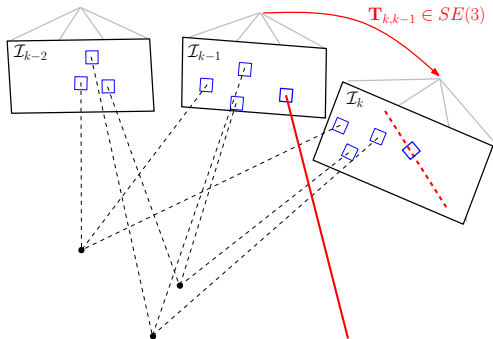
# Feature-based Visual Odometry

## Pipeline

1. Feature selection
2. Feature matching
3. Pose estimation
4. Pose refinement
5. **Triangulation**

## Triangulation

Search along Epipolar line for matching feature.



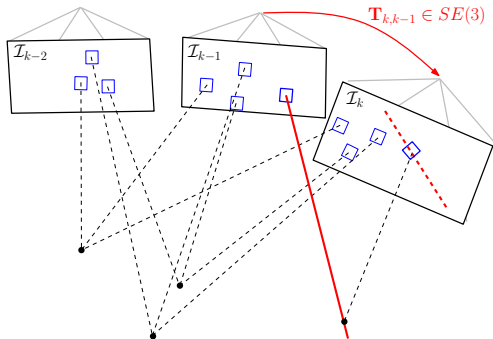
# Feature-based Visual Odometry

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## Triangulation

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# Dense Tracking

$$\mathbf{T}_{k,k-1} = \arg \min_{\mathbf{T}} \iint_{\bar{\mathcal{R}}} \rho \left[ \delta \mathcal{I}(\mathbf{T}, \mathbf{u}) \right] d\mathbf{u}.$$

$$\delta \mathcal{I}(\mathbf{T}, \mathbf{u}) = \mathcal{I}_k \left( \pi \left( \mathbf{T} \cdot \pi^{-1}(\mathbf{u}, \mathbf{z}_{\mathbf{u}}) \right) \right) - \mathcal{I}_{k-1}(\mathbf{u}) \quad \forall \mathbf{u} \in \bar{\mathcal{R}},$$

- ▶ itemized item 1
- ▶ itemized item 2
- ▶ itemized item 3

## Theorem

*In a right triangle, the square of hypotenuse equals the sum of squares of two other sides.*