



## An optimised catch-only assessment method for data poor fisheries

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Abstract:	Catch statistics are perhaps the easiest data to collect and are a widely available source of information for many fisheries. However, it is currently difficult to provide scientific advice for fishery managers using only catch data. We develop a catch-only method for stock assessment of data-poor fisheries. It uses time series of catches and two priors, one for the intrinsic population growth rate derived from natural mortality, and another for stock depletion based on catch trends. The method is based on a biomass dynamics model, along with an algorithm to search the possible parameter space. The utility of this method is demonstrated by applying it to 13 stocks in Australia that are assessed using Stock Synthesis—an assessment package that can make use of a variety of data sources. The estimated parameters, including carrying capacity, intrinsic population growth rate, maximum sustainable yield and depletion from the catch-only method are broadly comparable with those from the full assessments. The circumstances in which the method can perform poorly, such as longer-term changes in productivity and episodic recruitment, are highlighted.

1 An optimised catch-only assessment method for data poor fisheries

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3 Alternative 1: Fisheries stock assessment using catch data

4 Alternative 2: OCOM—a catch-based assessment method

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## 21 Abstract

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53   INTRODUCTION

54   Catch statistics are the most widely available fisheries data, with catch records for most

55   fisheries worldwide maintained by the FAO (Garibaldi 2012). However, it is difficult to

56   estimate reference points and to assess stock status using only catch data. Even the simplest

57   assessment methods such as surplus production (aka biomass dynamics) and depletion

58   models require additional information, such as fishing effort, to derive catch-per-unit-effort

59   (CPUE) indices that could be used as an index of relative biomass (Quinn and Deriso 1999).

60   However, information on effort is not available for many fisheries, or is difficult to measure

61   or standardize, or CPUE cannot be used as an indicator of biomass because of factors such as

62   changes over time in efficiency, and because the distribution of fishing effort does not match

63   that of the species of interest.

64   The idea of conducting stock assessments using primarily catch data was first explored by

65   Kimura and Tagart (1982) and Kimura *et al.* (1984) using so-called Stock Reduction Analysis

66   (SRA). In SRA, the biomass dynamics involve annual constant recruitment added to the total

67   biomass at the start of each year less fishery catch. A set of nonlinear catch equations is

68   solved for instantaneous fishing mortality and average recruitment, conditioning on an

69   assumed value for the instantaneous natural mortality rate ( $M$ ), initial stock size and the

70   decline in stock size. There has been an increased interest in using SRA during the last

71 decade. For example, Walters *et al.* (2006) used a Monte Carlo SRA method, and Dick and  
 72 MacCall (2011) proposed Depletion-Based Stock Reduction Analysis (DB-SRA), which  
 73 merged stochastic SRA with Depletion-Corrected Average Catch (DCAC, MacCall, 2009).  
 74 Martell and Froese (2013) used similar stochastic methods to estimate MSY using catch data  
 75 and “resilient” as a prior for the population growth rate in a surplus production model. This  
 76 Catch-MSY method has been extended recently to estimate reference points (Froese *et al.*  
 77 2016).

78 A prior distribution for stock depletion ( $d$ , the proportion of biomass depleted due to fishing  
 79 relative to unfished stock size ( $B_0$ ) or the theoretical carrying capacity level  $K$  (i.e.  $d = 1 -$   
 80  $B_y/K$ ), where  $B_y$  is stock size in year  $y$ ) is a necessary input parameter for these catch-only  
 81 methods, but is typically assumed based on auxiliary information. Consequently, Thorson and  
 82 Cope (2014) used age-composition data for recent years in a catch curve analysis to estimate  
 83 fishing mortality for those years, a method they referred to as “catch-curve stock reduction  
 84 analysis” (CC-SRA). Bentley and Langley (2012) included additional known information  
 85 such as exploitation rates and biomass in some years to constrain the simulated stochastic  
 86 stock biomass trajectories. The basic idea that underlies these approaches is similar: to  
 87 reconstruct possible trajectories of stock change from the start of the fishery, given (i)  
 88 informative priors on stock dynamics (e.g., on carrying capacity and population growth rate),  
 89 (ii) assumed or estimated stock status (either biomass or relative depletion) in a recent year,  
 90 and (iii) historical catches. Since the end point is approximately fixed in these approaches, the  
 91 process of selecting the intrinsic population growth rate,  $r$ , and  $K$  to determine biomass  
 92 trajectories involves “threading the needle”, as discussed by Walters *et al.* (2006): starting  
 93 from biomass in the first year, randomly choosing  $K$  and  $r$ , and ending at the predefined  $B_y$   
 94 range. Biomass trajectories in these approaches are determined by only two variables: a  
 95 biomass at the start of the fishery (relative to  $K$ ) and a population growth rate (for example  $r$

96 in the surplus production model). Invalid trajectories, e.g. those resulting in extinction, are  
97 discarded. Combinations of valid parameters can be found that match the current biomass or  
98 current depletion by tracing back from the most recent stock status and historical removals.

99 Although SRA is conceptually simple, with a fixed time-series of catch there is a wide range  
100 of  $K$  and  $r$  combinations that may lead to the same range of ending stock sizes (Martell and  
101 Froese 2013). Hence, it is necessary to provide reasonable priors on carrying capacity, growth  
102 rate, depletion, as well as other parameters depending on the specific methods. However, the  
103 choice of prior distributions (for example, uniform, lognormal) and their values (range, mean,  
104 variance etc.) will affect the results. Defining and defending sensible priors is often difficult.  
105 Further, it has been shown that catch-only methods are very sensitive to the priors,  
106 particularly that for depletion (Dick and MacCall 2011; Zhou *et al.* 2013; Carruthers *et al.*  
107 2014; Wetzel and Punt 2015), e.g. the effect of fishing on the population can be  
108 underestimated when an overly-optimistic prior for depletion is assumed and vice versa.

109 Recently, there have been developments in research relevant to data-poor assessment  
110 methods. For example, Zhou *et al.* (2012) derived relationships between fishing mortality-  
111 based biological reference points and life history parameters using a meta-analysis of global  
112 data-rich species. Further, Chen *et al.*<sup>1</sup> directly estimated the intrinsic population growth rate  
113 parameter in the Schaefer surplus production model using life-history parameters, specifically  
114 the natural mortality rate  $M$ . The results of these studies can be used to formulate a prior for  
115 the population growth rate parameter for use in SRA methods. In addition, a boosted  
116 regression trees (BRT) model has been developed to estimate stock depletion using only  
117 catch data (Zhou *et al.* in press). This BRT model is calibrated using data from the RAM

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<sup>1</sup> Chen, Z., Zhou, S., Ye, Y., Smith, D., and Zhang, K. In review. Relationship between intrinsic rate of population increase and natural mortality in fish and invertebrates.

Legacy Database (RAMLD), and models depletion as a function of various catch trends represented by the parameters of linear regressions of scaled catch over varying time periods.

A catch-only method was recently developed and applied to several data poor stocks (Zhou and Sharma 2013; Zhou *et al.* 2013; IFOP 2014; IOTC Secretariat 2014; IOTC 2015; Martin and Robinson 2016). We use recent developments to enhance this method and refer to it as optimized catch-only method (OCOM) because it uses an optimization algorithm rather than stochastic “thread the needle” approaches. The enhancements include incorporating priors from the newly-developed  $r \sim M$  relationship and BRT model, and an algorithm to search for feasible parameter values. We first describe the method and then apply it to 13 stocks in Australia’s Southern and Eastern Scalefish and Shark Fishery (SESSF) that have been assessed using Stock Synthesis (Methot and Wetzel 2013). This modified OCOM mainly uses catch data with some basic life history parameters to derive a prior for  $r$ , to estimate key biological quantities, including virgin biomass, intrinsic population growth, annual biomass, and depletion, as well as management quantities such as  $MSY$ ,  $B_{MSY}$ , and  $F_{MSY}$  (respectively the biomass and exploitation rate corresponding to  $MSY$ ). Although it is not a purely catch-only method as originally developed, the modified OCOM belongs to the class of methods that focuses on catch data and does not need information required by classic methods of stock assessments (e.g., age, length, sex, maturity, gear selectivity, fishing effort), and is consequently still a catch-only assessment method (c.f. Wetzel and Punt 2015).

### Materials and methods

We use the Graham-Schaefer surplus production model, as it is very simple and has been widely used:

$$B_{y+1} = B_y + rB_y \left(1 - \frac{B_y}{K}\right) - C_y \quad (1)$$

141 where  $B_y$  is the biomass at the start of time step  $y$ ,  $r$  is the intrinsic growth rate,  $K$  is the  
 142 carrying capacity (equal to the virgin or initial biomass  $B_0$  for a surplus production model, but  
 143  $K$  may differ from the initial biomass for a Stock Synthesis assessment), and  $C_y$  is the (known)  
 144 catch during time-step  $y$ . This model has two unknown parameters,  $r$  and  $K$ . Because  
 145 depletion  $d = 1 - S = 1 - B_y/K$ , where  $S$  is referred to as stock saturation (Zhou *et al.* in press),  
 146  $K$  in equation 1 can be solved if prior information on  $r$  and  $S$  (or  $d$ ) is available.

#### 147 **Productivity prior $r$**

148 A meta-analysis based on data for 245 fish species yielded the following relationships  
 149 between  $r$  and the instantaneous natural mortality rate  $M$  (Zhou *et al.* 2012):  $F_{MSY} = 0.87M$   
 150 (SD = 0.05) for teleosts, and  $F_{MSY} = 0.41M$  (SD = 0.09) for chondrichthyans. A separate  
 151 study<sup>1</sup> based on 189 stocks, and  $r$  values produced by the Graham-Schaefer surplus  
 152 production model, led to the relationships  $\bar{r} = 2.02M$  for invertebrates (SD = 0.21),  $\bar{r} =$   
 153  $0.76M$  for elasmobranchs (SD = 0.11), and  $\bar{r} = 1.72M$  for teleosts (SD = 0.09). Assuming  $r$   
 154  $= 2 F_{MSY}$ , which is the case for the Schaefer model, the results from these two studies are  
 155 quite similar. Therefore, we assume  $r \sim \text{normal}(\bar{r} = 1.72M, \text{SD} = 0.18)$  for teleosts, and  $r \sim$   
 156  $\text{normal}(\bar{r} = 0.79M, \text{SD} = 0.22)$  for chondrichthyans based on the average from these two  
 157 studies. Measurement error in  $M$  is estimated to be  $\sigma_M^2 = 0.23$  (Zhou *et al.* 2012). To avoid  
 158 potentially negative values being sampled, we transfer the normal distributions to a  
 159 lognormal distribution:  $r \sim \text{lognormal}(\mu_r, \sigma_r^2)$ , where  $\mu_r = \log(\bar{r} - \sigma_r^2 / 2)$ , and  $\sigma_r^2 \approx \sigma_M^2$ .  
 160 Natural mortality may be unavailable for many data-poor species (but not the example  
 161 SESSF stocks in this study) in which case it is necessary to estimate this parameter using  
 162 empirical life-history invariant equations, for example:

- 163 •  $M = 4.899t_{max}^{-0.916}$ , where  $t_{max}$  is the maximum age (Then *et al.* 2014);



- 164 •  $M = 4.118k^{0.73}L_{\infty}^{-0.33}$ , where  $k$  and  $L_{\infty}$  are Bertalanffy growth parameters (Then *et al.*
- 165 2014);
- 166 •  $M = 1.82k$  (Charnov *et al.* 2013);
- 167 •  $M = 1.65/t_{mat}$ , where  $t_{mat}$  is maturation age (Jensen 1996).

#### 168 **Prior for saturation $S$**

169 Zhou *et al.* (in press) parameterized relationships between  $S_e = B_e/K$  ( $B_e$  is the biomass at the  
 170 end of the time series) and catch history using the parameters of linear regressions of catch  
 171 trends over various time periods based on the RAMLD. They also provided a way to  
 172 construct probability distributions for  $B_e/K$  for use as a prior in data-poor assessment methods:

173  $S \sim sNorm(\text{mean} = S_{BRT} - 0.072, \text{SD} = 0.189, \text{skewness} = 0.763)$ , when  $S_{BRT} \leq 0.5$

174  $S \sim sNorm(\text{mean} = S_{BRT} + 0.179, \text{SD} = 0.223, \text{skewness} = 0.904)$ , where  $S_{BRT} > 0.5$ ,

175 where  $sNorm$  is a skewed normal distribution,  $S_{BRT}$  is the BRT-predicted point estimate of  
 176  $B_e/K$ , and  $S$  is the prior constrained within the range of  $[0, 1]$ .

#### 177 **Model implementation**

178 Model implementation involves: (i) drawing a large number (e.g.,  $n = 10,000$ ) of values for  $r$   
 179 and  $S$  from their priors; and (ii) deriving  $K$  in Model (1) by solving  $|B_e/K - S|$  using an  
 180 optimization algorithm (function “optimize” in R). For each random  $r$  and  $S$ , the algorithm  
 181 finds the optimal corresponding  $K$  value. With the large number of  $r$ - $S$  pairs, the search  
 182 process identifies all corresponding  $K$  values. This approach also improves the search  
 183 efficiency as every random draw ends up with a feasible  $K$  value, unlike the “thread the  
 184 needle” approach where a large number of random draws may be invalid because the  
 185 stochastic ending biomass does not fall within the predefined  $S$  interval (e.g., Walters *et al.*  
 186 2006; Dick and MacCall 2011; Martell and Froese 2013). The search range can be very wide,  
 187 for example  $K$  between  $C_{max}$  and  $300C_{max}$ , where  $C_{max}$  is the maximum catch in the time

series. This part of the approach is the same as the so-called “backwards approach” developed to assess baleen whales (e.g. Butterworth and Punt 1995; Punt and Butterworth 1996). Each random sample of  $r$  and  $S$  determines the corresponding values for  $K$  and  $B_e$ .

**Parameter derivation**

The above steps lead to  $n$  sets of values for  $r$ ,  $S$ , and  $K$ , as well as derived quantities such as  $MSY = rK/4$ . Summary statistics (e.g., mean, median, geometric mean, and percentiles) for these distributions are obtained from the samples. The distributions for  $r$  and  $S$  are samples from their prior distributions. Therefore, the final joint distributions for these parameters are not “posterior probability distributions” in the sense of Bayesian statistical inference, but are rather implied prior distributions for quantities derived from  $r$  and  $S$ .

**Application**

We applied OCOM to 13 stocks in Australia’s SESSF to validate the method and compare its results with those from data-intensive “full” assessments. We used catch data (landings plus discards) from the most recent assessments, although we recognize that discard information may not be available for many data-poor species. The effect of not including discards is the same as under-reporting catch. If the ratio of under-reporting to the total catch is constant over time, the OCOM will proportionally under-estimate  $K$  and  $MSY$ , but  $r$  and  $S$  will be unaffected. OCOM requires an estimate of natural mortality in addition to catch data. We adopted the values for  $M$  in the actual assessments of these stocks (instead of estimating  $M$  using the empirical equations presented above) to avoid differences in outputs due to different input data. Many SESSF stocks have distinctive life history and catch series, and have been assessed using Stock Synthesis (SS), a stock assessment method based on an age-structured population dynamics model, which can use a broad range of data sources (Methot and Wetzels, 2013; Dichmont *et al.* 2016). The length of catch history ranged from 25 to 100

years. Fishing mortality was generally low compared to global stocks (Worm *et al.* 2009), which might lead to difficulties for catch-only methods because low fishing intensity might be insufficient to change the abundance detectable by the method. The mean fishing mortality over time,  $\bar{F}$  from SS, for the 13 stocks varied between 0.031 and 0.135  $y^{-1}$ , with an average of 0.085  $y^{-1}$ . For SESSF stocks, the target reference point is  $F_{48}$ . The ratio  $\bar{F}/F_{48}$  ranged from 0.23 for School Whiting to 3.39 for Orange Roughy, with an average value of 1.20 for all 13 stocks. Gemfish East, Orange Roughy, and Redfish have the highest values for  $\bar{F}/F_{48}$  due to their high  $F_y$  in early years and low  $F_{48}$ .

Routine (not necessarily annual) stocks assessments are conducted for the stocks in the SESSF. The assessments use a range of data inputs, including landings, discards, standardized catch-rate indices, length-composition, age-composition, and sex ratio, as well as auxiliary information on natural mortality, stock-recruit steepness, maturity, etc. (Tuck 2014). The assessments estimate unfished recruitment, the deviations in annual recruitment about the stock-recruit relationship, selectivity as a function of age or length, and (in some cases) natural mortality and growth. The SS assessments also produce benchmark quantities, including unfished spawning biomass, unfished biomass for age 0+ fish, target spawning biomass and target fishing mortality rate. The target reference points are typically associated with the biomass  $0.48B_0$ , a default proxy value assumed to correspond to maximum economic yield MEY (Smith *et al.* 2008). Hence, the outputs from these routine assessments are MEY proxies and not directly comparable with the outputs of the Schaefer surplus production model (i.e., carrying capacity in terms of exploitable biomass, MSY, and  $F_{MSY}$ ). To make the results comparable, we re-ran the assessments using the same data and computed outputs associated with MSY (the fits to the data and the estimates of the parameters of the population dynamics model were unchanged). We defined exploitable biomass as the biomass for all ages equal to that for which fishery selectivity at age was 0.5 or larger.

Because fishable age varied among fleets, the age corresponding to 0.5 selectivity was weighted by the relative fishing mortality rate by fleet for stocks that were harvested using multiple gears. This process led to values for  $B_0$  (in units of exploitable biomass),  $F_{MSY}$ ,  $MSY$ , and  $B_e/B_0$  ( $= S$ ) for each of the 13 stocks.

The results for OCOM were also compared with those from the Catch-MSY method (Martell and Froese 2013). Catch-MSY requires a “resilience” parameter, which we obtained from fishbase.org. The parameter  $r$  was defined by resilience category as:  $r$  between 0.6-1.5 for High resilience, between 0.2-1 for Medium resilience, between 0.05-0.5 for Low resilience, and between 0.015-0.1 for Very low resilience. Catch-MSY defines  $B_e/K$  based on  $C_e/C_{max}$ :  $S$  between 0.3-0.7 for  $C_e/C_{max} > 0.5$ , and between 0.01-0.4 for  $C_e/C_{max} \leq 0.5$ . The original Catch-MSY method did not attempt to estimate stock depletion. We derived stock saturation for Catch-MSY by extracting an additional parameter—the biomass at the end of the estimated time series,  $B_e$ , from equation (1), and as usual, divided by the corresponding  $K$ . We used four statistics to evaluate model performance. For each stock, we calculated error (deviation)  $E$ , absolute error  $AE$ , relative error  $RE$ , and absolute relative error  $ARE$ :

$$E_{m,\theta} = \hat{\theta}_m - \theta_{SS}$$

$$AE_{m,\theta} = |\hat{\theta}_m - \theta_{SS}| \quad (2)$$

$$RE_{m,\theta} = \frac{\hat{\theta}_m - \theta_{SS}}{\theta_{SS}}$$

$$ARE_{m,\theta} = \frac{|\hat{\theta}_m - \theta_{SS}|}{\theta_{SS}}$$

where  $\hat{\theta}_m$  is the value from method  $m$  (OCOM or Catch-MSY) for the quantity  $\theta$  (i.e.,  $K$ ,  $F_{MSY}$ ,  $MSY$ , and  $S$ ) and  $\theta_{SS}$  is the maximum likelihood estimate from Stock Synthesis. We used the geometric mean to summarize the outputs from Catch-MSY as this summary

statistic was recommended for this method by Martell and Froese (2013). We compared the geometric mean and median of OCOM outputs, and found they were similar so we only report results based on the median for OCOM. To compare OCOM and Catch-MSY, we used mean values of the four statistics (i.e.,  $F_{MSY}$ ,  $K$ ,  $MSY$ , and  $S$ ) across all 13 stocks, i.e., ME, MAE, MRE, and MARE. Note that these measures are relative to SS. It was difficult to directly compare results between different methods because of differences in model assumptions (e.g., whether the initial biomass is assumed to equal  $K$  and the shape of the production function). Nevertheless, comparisons with data-rich fully quantitative assessments should indicate the general reliability and potential utility of the OCOM method.

## Results

### *Biomass series*

First we compare the biomass trajectories from OCOM with the “true” results derived from SS. Figure 1 plots the time series of biomass from SS with a sample of the biomass trajectories (central 25% to 75%) from OCOM. The catch time series are also shown to help understand the behaviour of OCOM. The biomass time series from OCOM match those from SS very well, with the SS result falling mostly within the range of OCOM outputs for five stocks (Deepwater Flathead, Morwong West, Pink Ling West, Redfish, and Tiger Flathead). The biomass trends for three other stocks are similar, but the absolute levels differ considerably (Bight Redfish, Orange Roughy, School Whiting). The biomass series from the SS assessments for Blue Grenadier and Silver Warehou exhibit marked fluctuations due to episodic recruitment, and SS yields estimates of biomass higher than  $B_0$  in some years, which OCOM does not detect (OCOM assumes that the biomass is less than  $K$  for all years). The trends in OCOM differ greatly from those provided by SS for Gemfish East and Morwong East. Specifically, OCOM overestimates biomass for Gemfish East both initially and at the end of the time series. Both Gemfish East and Morwong East are thought to have undergone

longer-term changes in productivity, which are reflected in the SS results but cannot be accounted for by OCOM.

### ***Population parameters***

We now examine OCOM in terms of its ability to estimate the four parameters of interest – carrying capacity  $K$ , stock productivity represented by  $F_{MSY}$  ( $= 0.5r$ ), maximum sustainable yield MSY, and stock saturation  $S$  (see Table 1 and an example of their distributions for Bight Redfish in Figure 2).

Across the 13 stocks, the average  $K$  value from SS is 25,149t compared with 32,274t from OCOM. OCOM overestimates  $K$  for about half of the stocks (seven out of 13 so unbiased in this respect) (Figure 3), but the overestimates are greater than the underestimates, resulting in an overall average overestimate of 7,125t (about 28% of the average  $K$  from SS). The relative errors range from -0.36 to +2.31, with an average of 0.38. The largest overestimate is 56,698t for Orange Roughy, and the largest relative error is +2.31 for Morwong East (note that  $K$  from SS is smaller than the initial biomass in SS; Figure 1; the difference between SS and OCOM is smaller if  $K$  from OCOM is compared with the initial biomass from SS). The mean absolute errors, MAEs, and mean absolute relative errors, MAREs, for  $K$  for OCOM (9,856t and 0.51 respectively) are correspondingly higher than the ME and MRE values (Table 3).

The average  $F_{MSY}$  value for SS for the 13 stocks is 0.43 compared with 0.16 for OCOM.

There is a consistent bias for  $F_{MSY}$ , with OCOM leading to high values for  $F_{MSY}$  for only one stock (Gemfish East). Several stocks have very high negative relative errors (-0.94 for Bight Redfish, -0.86 for Morwong West, and -0.84 for Orange Roughy; note that the minimum relative error is -1). Gemfish East has the highest positive relative error, +1.78. The negative relative errors for  $F_{MSY}$  occur in part because the shape of the underlying production functions differs between SS and OCOM, with  $B_{MSY}/B_0$  occurring at 0.5 for OCOM and at less than 0.5

308 (often substantially so, e.g. Bight Redfish) for SS (Figure 4). SS estimates the production  
 309 function accounting for the yield-per-recruit and stock-recruitment relationships.  
 310 Consequently, the yield function approximates the (often asymptotic) yield-per-recruit  
 311 function when exploitable age is older than maturation age and stock-recruitment steepness is  
 312 high, which is the case for Bight Redfish and Morwong West. Hence, given approximately  
 313 the same MSY and  $B_0$  values, SS must produce a larger  $F_{MSY}$  than OCOM (Figure 5).

314 Of more management relevance than  $K$  and  $F_{MSY}$  (or  $r$ ) is MSY. For the 13 stocks, the  
 315 average MSY value from SS is 1,541t. The average value for MSY from OCOM is 1,947t,  
 316 about 26% higher. The extent of this discrepancy arises almost entirely from two stocks –  
 317 Gemfish East and Morwong East (Table 1; Figure 3). Morwong East is estimated to have  
 318 undergone a significant “regime shift” (see discussion) and the SS results reflect the more  
 319 recent lower productivity regime. The SS assessment for Gemfish East also estimates very  
 320 low productivity in recent years and hence a low MSY. In other respects, MSY is estimated  
 321 quite well by OCOM, with approximately equal positive and negative relative errors. If the  
 322 two “problem” stocks are excluded, the mean relative error drops from 0.63 to 0.02 (i.e.  
 323 nearly unbiased), and the mean absolute relative error from 0.75 to 0.13.

324 Also of considerable management relevance are the estimates of stock saturation  $S$ . Across  
 325 the 13 stocks, the average value for SS is 0.41, with an among-stock range from 0.09 to 0.78.  
 326 For OCOM, the average value is 0.37, with an among-stock range from 0.10 to 0.82. Stock  
 327 saturation is over-estimated for seven and under-estimated for six stocks by OCOM, and the  
 328 MRE of the 13 stocks is 0. Five of the stocks have errors within the range  $\pm 0.1$ , eight within  
 329  $\pm 0.2$  and ten within  $\pm 0.3$ . The mean absolute error is 0.19.

330 The comparison between OCOM and SS in Table 1 and Fig 1 is based on OCOM using the  
 331 same values for  $M$  as the SS assessments. The Supplementary Material shows that the results

are robust to basing  $M$  in OCOM instead on values for  $M$  and other life-history parameters (i.e.,  $t_{max}$ ,  $k$ ,  $L_{\infty}$ , and  $t_{mat}$ ) from Fishbase.

### ***Comparison with Catch-MSY***

Catch-MSY results in similar estimates of the four key parameters as OCOM (Table 2), but its mean values for all these parameters have larger errors (relative to SS) than OCOM. For example, the mean  $K$  for SS, OCOM, and Catch-MSY are 25,149t, 32,274t, and 35,653t, respectively. The mean  $F_{MSY}$  is more similar between OCOM and Catch-MSY (0.16 compared to 0.12) than SS (0.43). However, Catch-MSY yielded a narrow range of  $F_{MSY}$  values around a mean of 0.12 (range: 0.05 and 0.20). In contrast, the prior for OCOM based on  $M$  better includes extreme values for  $F_{MSY}$ , and its estimated  $F_{MSY}$  extends from 0.03 for Orange Roughy to 0.44 for School Whiting (Table 1). Using the  $S$  prior based on the BRT prediction, OCOM also yields a wider range for  $S$  than Catch-MSY, ranging from 0.10 to 0.82. In contrast, the estimates of  $S$  from Catch-MSY  $S$  fall into two narrow bands, one between 0.1 and 0.19 and the second one between 0.53 and 0.57. On average, Catch-MSY underestimates  $S$  by 43% while OCOM underestimates  $S$  by 11%. OCOM is more accurate than Catch-MSY for all parameters based on the mean error (ME) (Table 3). For the other three criteria, i.e., mean absolute error (MAE), mean relative error (MRE), and mean absolute relative error (MARE), OCOM outperforms Catch-MSY for three out of four parameters. Using mean absolute relative error and excluding the two “problem” stocks (Gemfish East and Morwong East), OCOM outperforms Catch-MSY by 9% for  $F_{MSY}$ , 29% for  $MSY$ , and 11% for  $S$ , but underperforms -4% for  $K$ . Overall, based on four statistics by four parameters, OCOM outperforms Catch-MSY by 13 to 3 (Table 3). However, due to large variability, the improvement in OCOM may not appear to be substantial for the 13 stocks tested.

### **Discussion**



Development of data-poor methods that primarily use catch data has attracted increasing interest in recent years. We present a modified optimized catch-only assessment method that uses prior information from recent studies, adding another tool to the existing toolbox in this category. In general, our method yields reasonable estimates for most stocks we examined. Because of its limited data requirements and simplicity, the data preparation and assessment process can be very quick. Using the steps described in the Materials and Methods and written in R (R Core Team 2013), the method can produce results in minutes. The procedure can be designed for batch processing data for a large number of species. Using prior information for  $r$  and  $S$  that have been derived from data-rich stocks (Zhou et al. 2012, in press) has advantages over arbitrarily assuming a value or a range for these quantities as is the case for other data-poor methods. Unlike the “thread the needle” approach, using an optimisation algorithm also has computational advantages, which ensures little chance of missing possible viable values.

Comparing results between different assessment methods is not straightforward. For example model outputs are sensitive to various assumptions about priors, life history parameters, and the time series of data used, even for data-intensive integrated assessments (Ichinokawa *et al.* 2014). We examine potential reasons that lead to the differences between the results from SS and OCOM. The error of  $F_{MSY}$  is not symmetric: OCOM underestimates  $F_{MSY}$  for all stocks except Gemfish East. The main reason is that, unlike  $B_0$  and  $MSY$ ,  $F_{MSY}$  is model-dependent, which implies that it is not comparable between SS and OCOM. Ideally, the same surplus production model should be applied to OCOM and SS to compare them. Unfortunately, neither SS nor OCOM has such an option.

Catch-MSY also performs quite well for these 13 stocks;  $K$  and  $MSY$  are similar between the two simple approaches. Catch-MSY tends to be insensitive to very small or very large values,

particularly for the productivity parameter  $r$ . This may be caused by its three categories of  $r$  prior using resilience. The assumed  $S$  prior has two choices: between 0.3 and 0.7, and between 0.01 and 0.4, depending on the  $C_e/C_{\max}$  ratio. Hence, it is understandable that estimated  $S$  also ends in one of the two narrow bands. Catch-MSY derives a prior for  $r$  based on “resilience” found in Fishbase.org and  $S$  based on  $C_e/C_{\max}$  ratio. This appears to be simpler than OCOM, where  $r$  is based on  $M$ , and  $S$  is based on the BRT model. However, because  $M$  can be derived from alternative methods and BRT modelling has been established, implementing OCOM is fully automatic with an input file containing the time series of catch data, similar to Catch-MSY.

#### ***Why OCOM cannot mimic SS – three example stocks***

Assessment of the Gemfish East stock is challenging. Stock assessments since the late 1980s show a sharp decline in adult biomass during the early 1980s and weak cohorts spawned in the late 1980s (Little and Rowling 2010). Natural mortality is assumed to be  $0.38\text{yr}^{-1}$  (Tuck 2014). However, SS yields a very low estimate of  $F_{MSY}$  ( $= 0.08\text{yr}^{-1}$ ), about 20% of the  $M$  value.  $F_{MSY}$  is generally close to  $M$  (Quinn and Deriso 1999; Zhou *et al.* 2012). SS also yielded a low MSY of 540t. OCOM’s estimated MSY of 3,687t is closer to the average observed catch of 2,786t during the first 30 years. Using an index of abundance, as well as age and length data, SS estimates lower productivity and a lower MSY in recent years because the productivity of Gemfish East is estimated to have dropped substantially over time with no evidence for recovery even under low removals (Punt and Smith, 1999). OCOM is unable to capture this effect because it assumes constant  $K$  and  $r$  over the entire catch history and is not able to update the prior distribution for  $r$ .

Bight Redfish is a long-lived species with a low natural mortality ( $M = 0.1\text{yr}^{-1}$ ). The stock assessment using SS in recent years (between 2000 and 2015) resulted in a wide range of

estimates (Haddon 2015). For example, the unfished female spawning biomass varied between 5,451t and 31,660t, depending on the time period used and assumptions regarding biological parameters. The difficulties in these assessments may partially be due to low contrast in biomass due to a history of relatively low fishing mortality rates. For example, SS results are sensitive to the assumed gear selectivity and the age range used to derive exploitable biomass (Zhou, SS sensitivity test results not included).

Recruitment of Morwong East has been below average since 1985 (Wayte 2013; Tuck 2014). The decline in recruitment is likely due to a climate-induced regime shift (Wayte 2013). SS estimates a low current  $B_0$  of 7,693t and a low current MSY of 468t (Table 1), following the estimated regime shift in the late 1980s. This new  $B_0$  and MSY are much lower than the estimated mean exploitable biomass of 25,556t in the first 40 years from 1914 to 1954, and the mean observed catch of 1,743t over 40 years from 1946 to 1985 (c.f. Figure 1). In contrast, OCOM uses the entire time series and results in  $B_0 = 25,435t$  and  $MSY = 1,374t$ . OCOM also yields similar estimates of  $F_{MSY}$  for the Eastern and Western stocks because it is based on the same prior. Again, OCOM is unable to detect a productivity change due to a regime shift because it assumes constant  $K$  and  $r$  over the entire catch history. This inability to detect productivity change or environmental regime shifts is a major weakness of OCOM. This simple method assumes that the population follows a certain dynamic process and is not primarily environmentally-driven. The stationary production function using an average population growth rate  $r$  and an average carrying capacity  $K$  is unable to capture long term shifts in average recruitment or highly variable population dynamics. In addition, OCOM cannot detect abrupt changes in carrying capacity and maximum sustainable yield. This is evident for Morwong East, which exhibits some of the largest differences in estimated management parameters between SS and OCOM.

428 *The value of OCOM for management purposes*

429 OCOM is a data-poor assessment method that mainly utilizes catch data, so should not be  
430 expected to accurately replicate assessments based on more sophisticated methods and much  
431 more data, such as SS. What can we conclude about its robustness from the comparisons  
432 presented here? The answer depends, to a large extent, on what information is being sought  
433 from such an analysis.

434 1. The performance in estimating MSY and  $S$  is of much more management relevance than in  
435 estimating  $K$  and  $F_{MSY}$  (or  $r$ ). The latter are in a sense “nuisance” parameters that in  
436 combination may offer insights on more important parameters. For example,  $r$  and  $K$  may be  
437 poorly estimated but their product (note that  $MSY = rK/4$ ) may be better estimated. This  
438 seems to be the case in these results.

439 2. In some cases, a method such as OCOM may be used to assess the status of an individual  
440 stock. In that case, considerations of both bias and variance arise, and the user would want to  
441 have some idea of just how poor a single estimate may be (and whether it is more likely to be  
442 biased high or low). In other cases, OCOM may be used to estimate management quantities  
443 across a range of stocks simultaneously, in which case the average or ensemble statistics  
444 become more important. For example, data-poor methods have been used to try to assess the  
445 status of large numbers of stocks at a time, in efforts to estimate global or regional status of  
446 fisheries (Froese *et al.* 2012; Costello *et al.* 2012, 2016).

447 3. Estimated management quantities may be used as the basis for harvest strategies or  
448 management procedures. Properly constructed harvest strategies (that include harvest control  
449 rules as well as estimates of stock status) can be made somewhat “robust” to uncertainties in  
450 management quantities such as MSY and  $S$ . This is an important topic not dealt with in this

451 paper, but now widely explored in a range of recent publications (Carruthers *et al.* 2014;  
452 Wetzel and Punt 2015).

453 Building on these considerations, OCOM should be used with some care in assessing and  
454 managing individual stocks. Considering MSY, it seems to perform quite well in most  
455 situations, but performed poorly where there were large temporal changes in stock  
456 productivity or episodic recruitment. Such changes have been well documented for Morwong  
457 East (Wayte 2013), and are considered plausible for Gemfish East as well (Punt and Simth  
458 1999; Little and Rowling 2010). However, it will likely be very difficult to predict whether  
459 such changes have occurred for data-poor stocks. In the absence of such considerations, some  
460 additional level of precaution would be required in using MSY estimates to manage a fishery,  
461 particularly as MSY itself is a “limit” management quantity.

462 For assessing current stock status (saturation  $S$ ), the prior from the BRT model performs  
463 reasonably well, though individual relative errors can be quite large. Estimates of  $S$  appear to  
464 be unbiased (very low values for ME and MRE) and mean absolute errors are tolerable (0.19).  
465  $S$  is valid in the range 0 to 1, so absolute errors may be of more management interest than  
466 relative errors. Additionally, most management concern is about low stock sizes, so the  
467 ability to estimate  $S$  at the low end of the range may be much more important than at the high  
468 end of the range. Four of the SS stocks are estimated to be below 0.3K and OCOM “picked”  
469 this for three of those stocks (Gemfish East, Orange Roughy and Redfish). It also indicated  
470 lower levels of  $S$  for two further stocks – Morwong East, which is appropriate considering the  
471 regime change, and Tiger Flathead, which appears to be an error. Viewed overall, OCOM  
472 may perform reasonably well in estimating stock depletion for an ensemble of stocks.

### 473 *Caveats and future work*

474 OCOM requires a prior for  $r$ , which is based on natural mortality  $M$ . Accuracy in estimating  
475  $M$  will affect the results of OCOM. It may be difficult to obtain reliable estimates of  $M$ . For  
476 School Whiting, previous SS assessments have suggested a range of values for this parameter  
477 from 0.37 to 0.90yr<sup>-1</sup> (Day 2010). Using  $M = 0.57\text{yr}^{-1}$  in this study results in  $F_{MSY} = 0.44$  and  
478  $K = 15,101\text{t}$ . Further studies of the robustness of OCOM and its sensitivity to various inputs  
479 and assumptions are required.

480 Although OCOM can use catch data to estimate several key management quantities,  
481 additional information, if available, can be incorporated into the method to enhance its power.  
482 Possible information includes one or more years with estimates of absolute abundance, a  
483 relative abundance index, an estimate of fishing mortality rate, and more than one year of  
484 fishing effort data. This means that the default method can be tailored to accommodate  
485 various cases depending on data availability.

486 OCOM is based on a particular surplus production model and produces MSY-related  
487 reference points. Achieving MSY has been a traditional fisheries objective, and most  
488 management regimes have been built around this framework. Among the key parameters,  
489 MSY is the least biased quantity from OCOM (if Gemfish East and Morwong East are  
490 excluded). Using MSY as a reference point and catch as an indicator could be used to form a  
491 simple harvest control rule for fisheries management, particularly for data-poor stocks  
492 (Martell and Froese 2013; Carruthers *et al.* 2014). Since OCOM can also estimate annual  
493 biomass, hence fishing mortality rate  $F$ , the pair of  $F_y - F_{MSY}$  could be used for  $F$ -based  
494 management. However, further research to improve its accuracy for individual species may  
495 be needed, and the performance of harvest strategies based on OCOM-derived quantities  
496 requires careful testing using management strategic evaluation methods (Punt *et al.* 2016).

497 Moreover, analysis would be required to examine what properties of the catch time series  
498 themselves (length of time series, multiple peaks and troughs, error in catch data, etc.) seem  
499 to facilitate more robust estimation by methods like OCOM.

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609

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610 Table 1. Comparison of key parameters from Stock Synthesis (SS) and OCOM for 13 SESSF stocks.  $S = B_e/K$ , RE = relative error.

ID	Stock Common name	Scientific name	SS				OCOM				RE			
			$K$	$F_{MSY}$	$MSY$	$S$	$K$	$F_{MSY}$	$MSY$	$S$	$K$	$F_{MSY}$	$MSY$	$S$
1	Bight Redfish	Centroberyx gerrardi	7,735	1.45	611	0.63	12,537	0.08	529	0.69	0.62	-0.94	-0.13	0.09
2	Blue Grenadier	Macruronus novaezelandiae	70,993	0.22	4,435	0.78	67,203	0.14	4,650	0.34	-0.05	-0.37	0.05	-0.57
3	Deepwater Flathead	Neoplatycephalus conatus	15,164	0.29	1,257	0.47	11,482	0.18	1,061	0.31	-0.24	-0.37	-0.16	-0.34
4	Gemfish East	Rexea solandri	15,146	0.08	538	0.13	32,337	0.23	3,687	0.19	1.14	1.78	5.85	0.44
5	Morwong East	Nemadactylus macropterus	7,693	0.23	468	0.34	25,435	0.12	1,469	0.10	2.31	-0.51	2.14	-0.72
6	Morwong West	Nemadactylus macropterus	1,943	0.80	185	0.63	1,846	0.11	108	0.32	-0.05	-0.86	-0.42	-0.50
7	Orange Roughy	Hoplostethus atlanticus	81,054	0.20	2,192	0.23	137,752	0.03	2,148	0.15	0.70	-0.84	-0.02	-0.34
8	Pink Ling East	Genypterus blacodes	15,670	0.16	789	0.20	10,078	0.16	805	0.37	-0.36	-0.00	0.02	0.87
9	Pink Ling West	Genypterus blacodes	10,893	0.23	789	0.43	12,221	0.16	893	0.79	0.12	-0.29	0.13	0.82
10	Redfish	Centroberyx affinis	31,537	0.09	980	0.09	37,627	0.08	1,439	0.12	0.19	-0.19	0.47	0.30
11	School Whiting	Sillago flindersi	8,578	1.25	2,268	0.65	15,101	0.44	3,042	0.82	0.76	-0.65	0.34	0.27
12	Silver Warehou	Seriola punctata	25,715	0.36	2,686	0.32	24,056	0.22	2,683	0.39	-0.06	-0.38	-0.00	0.22
13	Tiger Flathead	Neoplatycephalus richardsoni	34,818	0.28	2,830	0.49	31,882	0.18	2,793	0.20	-0.08	-0.37	-0.01	-0.58
	Mean		25,149	0.43	1,541	0.41	32,274	0.16	1,946.72	0.37	0.38	-0.31	0.63	-0.00

611

612 Table 2. Comparison of key parameters from Catch-MSY and from Stock Synthesis output for 13 SESSF stocks.  $S = B_e/K$ , RE = relative error.

Stock	SS				Catch-MSY					RE			
	$K$	$F_{MSY}$	$MSY$	$S$	$K$	$F_{MSY}$	$MSY$	$S$	Resilience	$K$	$F_{MSY}$	$MSY$	$S$
Bight Redfish	7,735	1.45	611	0.63	6,645	0.12	388	0.15	Very low	-0.14	-0.92	-0.37	-0.77
Blue Grenadier	70,993	0.22	4,435	0.78	71,682	0.12	4,192	0.19	Low	0.01	-0.46	-0.05	-0.76
Deepwater Flathead	15,164	0.29	1,257	0.47	14,930	0.12	910	0.16	Low	-0.02	-0.58	-0.28	-0.66
Gemfish East	15,146	0.08	538	0.13	55,126	0.09	2,459	0.15	Low	2.64	0.09	3.57	0.15
Morwong East	7,693	0.23	468	0.34	45,412	0.05	1,151	0.15	Low	4.90	-0.78	1.46	-0.55
Morwong West	1,943	0.80	185	0.63	1,865	0.11	105	0.10	Low	-0.04	-0.86	-0.43	-0.85
Orange Roughy	81,054	0.20	2,192	0.23	133,945	0.09	6,105	0.16	Very low	0.65	-0.53	1.79	-0.31
Pink Ling East	15,670	0.16	789	0.20	12,794	0.11	686	0.13	Low	-0.18	-0.32	-0.13	-0.36
Pink Ling West	10,893	0.23	789	0.43	8,064	0.12	489	0.19	Low	-0.26	-0.47	-0.38	-0.56
Redfish	31,537	0.09	980	0.09	29,920	0.13	2,018	0.16	Medium	-0.05	0.42	1.06	0.81
School Whiting	8,578	1.25	2,268	0.65	18,928	0.18	1,727	0.53	Medium	1.21	-0.85	-0.24	-0.18
Silver Warehou	25,715	0.36	2,686	0.32	30,669	0.17	2,651	0.53	Medium	0.19	-0.52	-0.01	0.69
Tiger Flathead	34,818	0.28	2,830	0.49	33,510	0.20	3,283	0.57	Medium	-0.04	-0.30	0.16	0.15
Mean	25,149	0.43	1,541	0.41	35,653	0.12	2,013	0.24		0.68	-0.47	0.47	-0.25

613

614

615

616 Table 3. Comparison of model performance between OCOM and Catch-MSY. ME: mean error; MAE: mean absolute error; MRE: mean relative  
 617 error; MARE: mean absolute relative error. All statistics are relative to Stock Synthesis estimates.

Statistics	OCOM				Catch-MSY			
	$K$	$F_{MSY}$	$MSY$	$S$	$K$	$F_{MSY}$	$MSY$	$S$
ME	7125	-0.27	406	-0.05	11386	-0.28	518	-0.14
MAE	9856	0.29	473	0.19	13045	0.29	817	0.20
MRE	0.38	-0.31	0.63	0.00	0.68	-0.47	0.47	-0.25
MARE	0.51	0.58	0.75	0.46	0.79	0.55	0.76	0.52

618

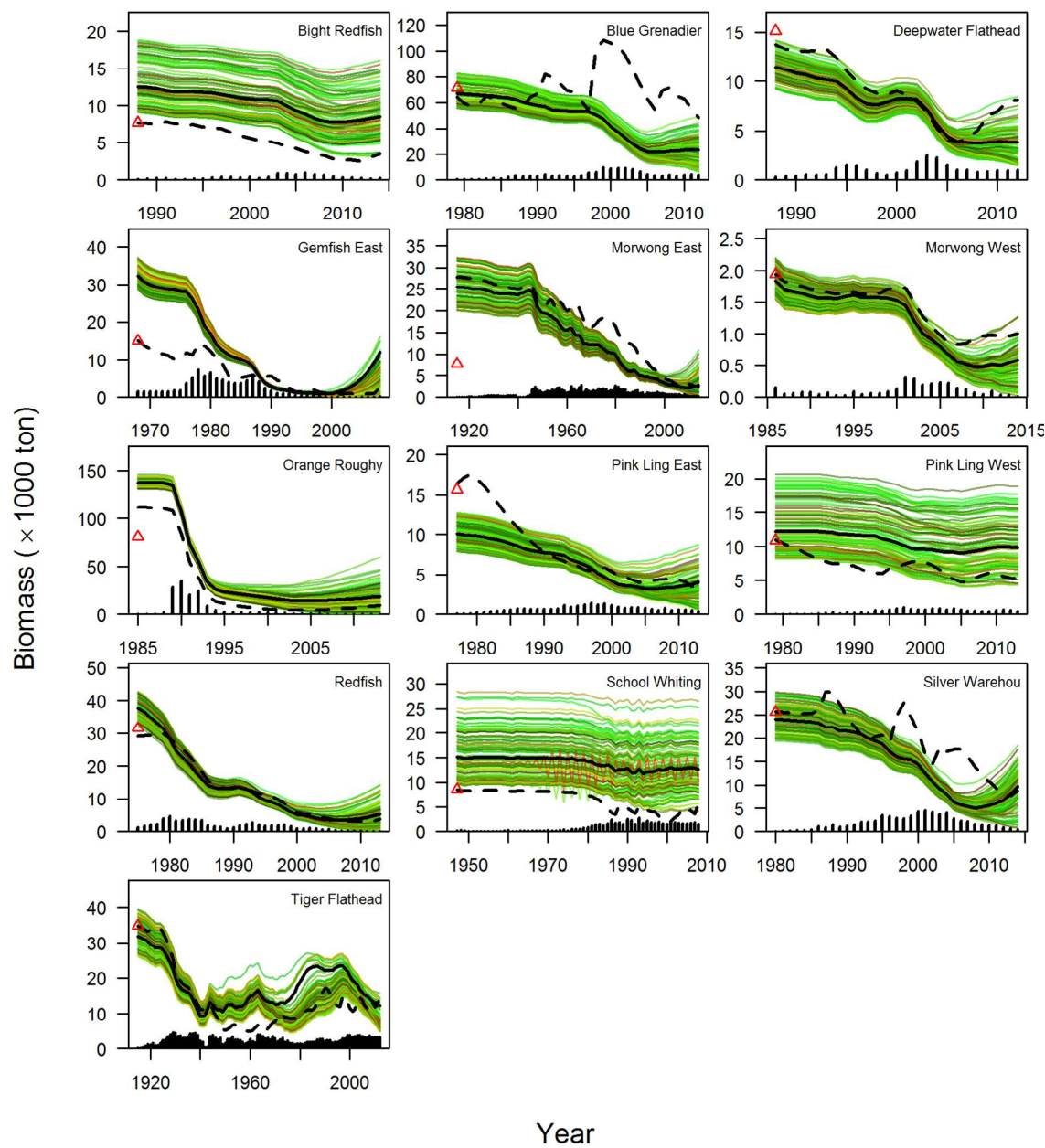
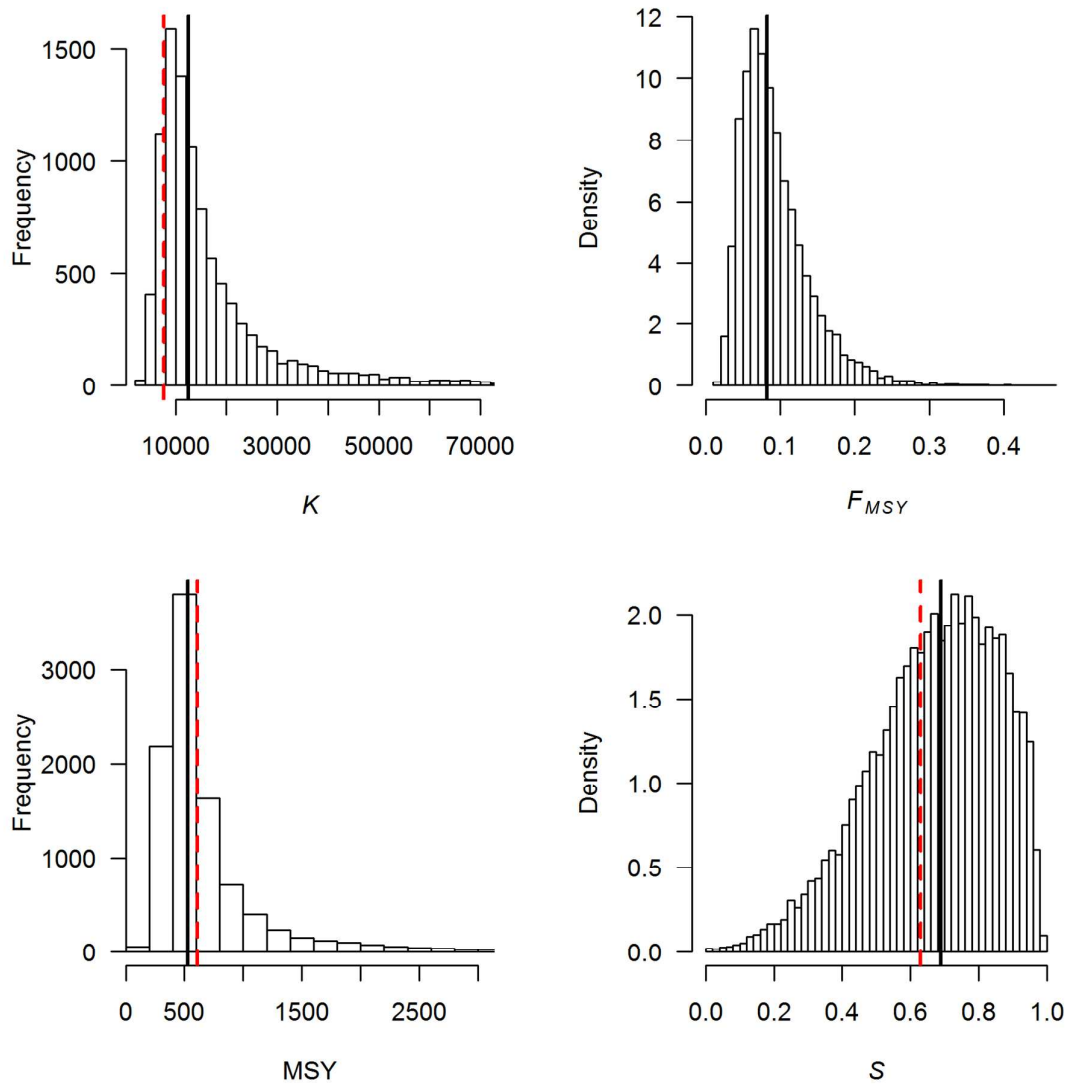


Figure 1. OCOM-estimated exploitable biomass trajectories (coloured lines) from 100  $r$ - $K$  pairs for 13 SESSF stocks. The solid black line is the median, the black dashed line is the “true” biomass from SS, the red triangle is estimated  $K$  from SS, and the vertical bars are the observed catch. Note that the start of the solid black line is the median  $K$  from OCOM, and the start of the dashed line is the initial biomass from SS.





627

628

629 Figure 2. Distribution of four parameter outputs from OCOM for Bight Redfish. The vertical  
 630 black lines are the medians, and the red lines are point estimates from Stock Synthesis.  $F_{MSY}$   
 631 = 1.45 for SS is outside of the range of values plotted.

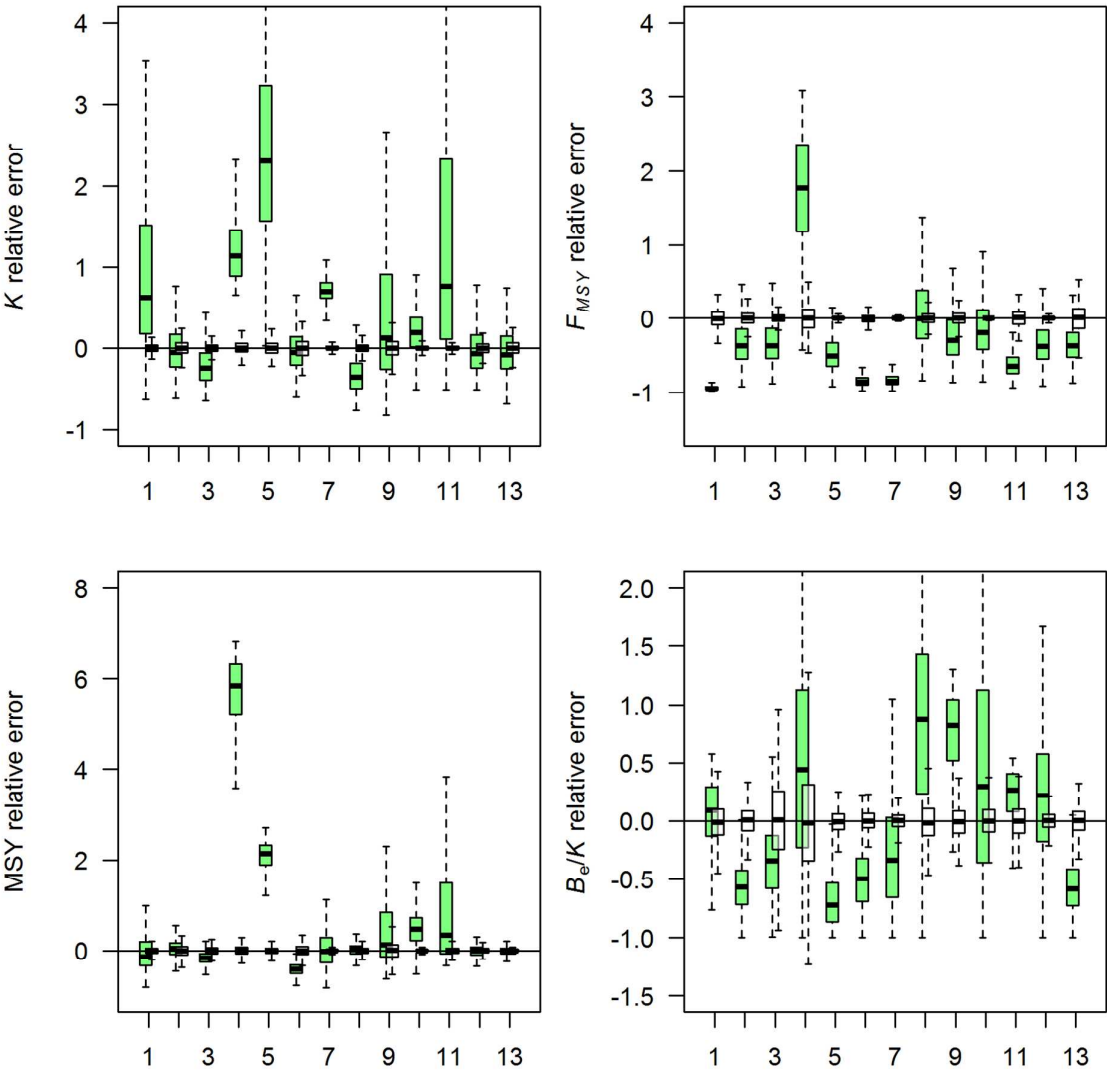
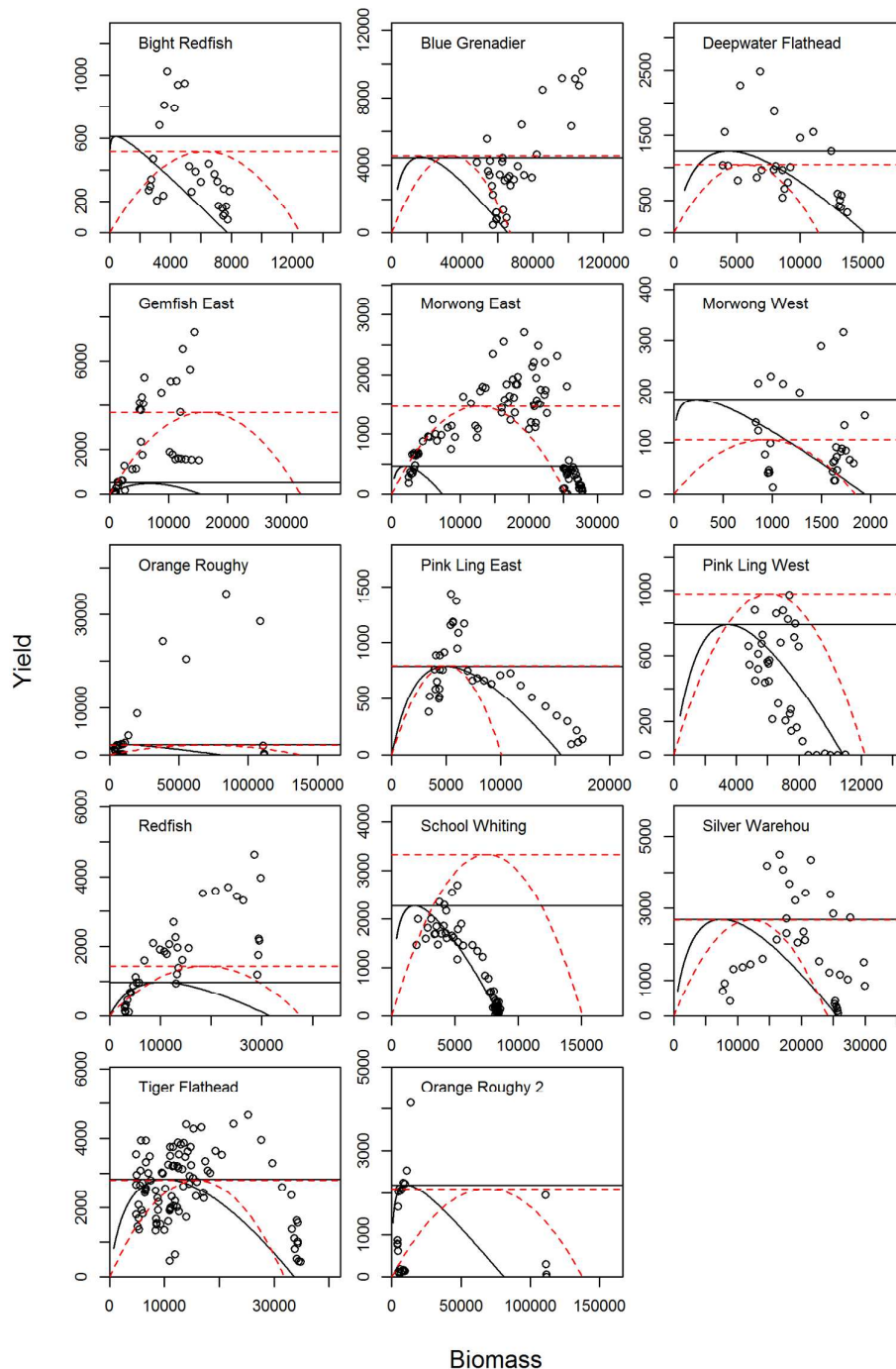
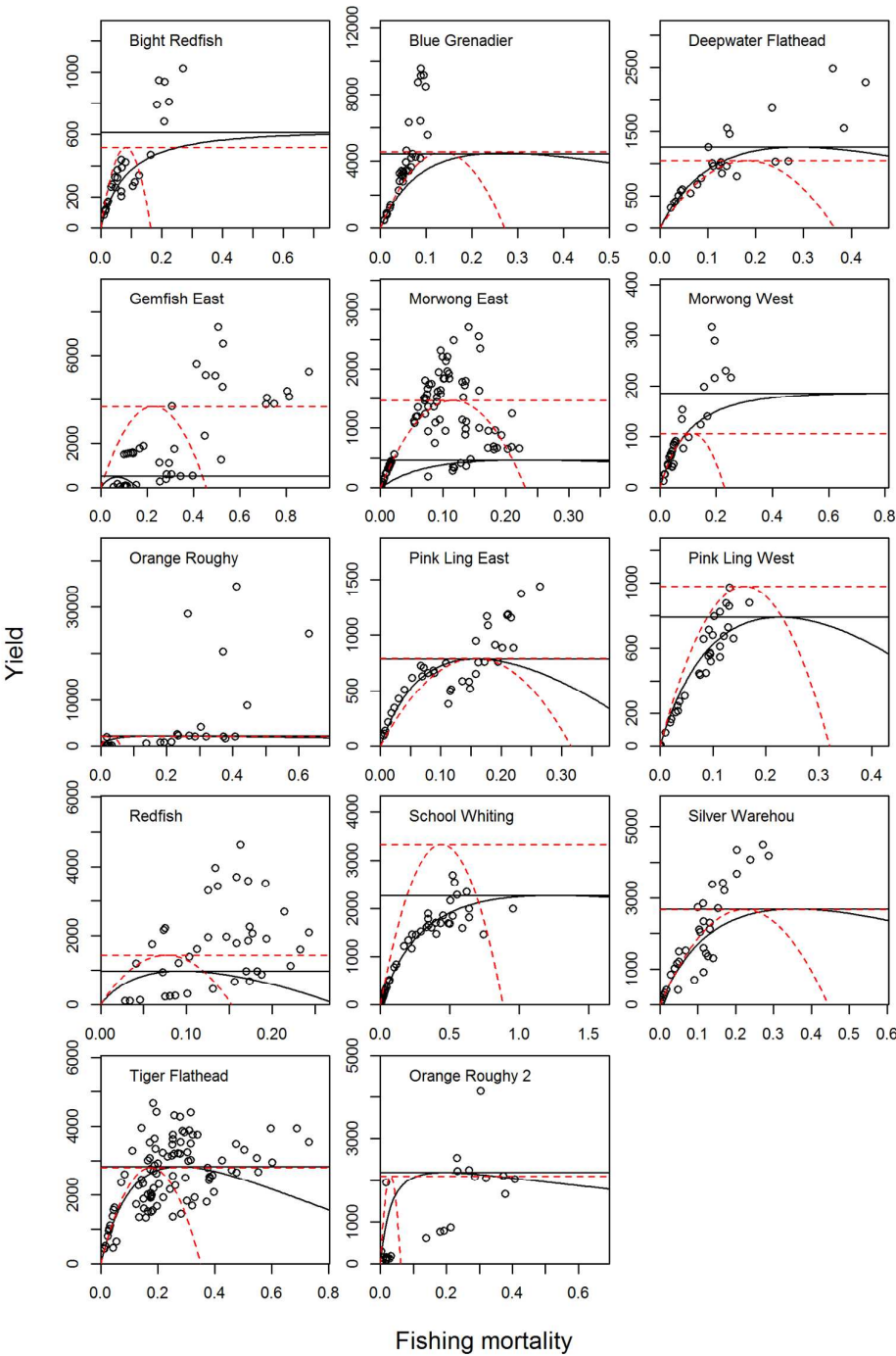


Figure 3. Comparison of four parameters between OCOM (green) and SS (white) for the 13 SESSF stocks. The boxplots for OCOM are based on 10,000 samples whereas the boxplots for SS are based on the point estimate and the (asymptotic) standard error. Stock number is the same as stock ID in Table 1 (i.e., number 4 is Gemfish East and number 5 is Morwong East).



639

640 Figure 4. Equilibrium relationships between yield and exploitable biomass from SS (black  
 641 solid lines) and OCOM (red dashed lines). The circles are observed catch versus SS-  
 642 estimated exploitable biomass, and the horizontal lines are the estimated MSYs. The last  
 643 panel repeats Orange Roughy but the bounding y-axis between 0 and 5,000t so the five large  
 644 data points are not shown.



645

646 Figure 5. Equilibrium relationships between yield and fishing mortality rate based on  
647 parameters estimated by SS (black solid lines) and OCOM (red dashed lines). The circles are  
648 observed catch versus SS estimated exploitable biomass and the horizontal lines are the  
649 estimated MSY values. The last panel repeats Orange Roughy but bounding the y-axis  
650 between 0 and 5,000t so five large data points are not shown.

## Supplementary material

### 1. Using natural mortality from Fishbase

We used the natural mortality rates that are adopted in SS to compare the results from the OCOM and SS assessments for the 13 SESSF stocks, in the main text. However, natural mortality may be unavailable for some species in other data-poor fisheries. For these species, we suggest obtaining values for natural mortality from Fishbase.org and applying four empirical equations using other life-history parameters. To see how  $M$  from Fishbase may affect the results, we obtained  $M$  or other life-history parameters directly from Fishbase for the SESSF species. Fishbase has values for  $M$  for four of the 11 species so we used other life-history parameters, i.e., maximum age, von Bertalanffy growth parameters, and maturation age to obtain average  $M$  for the remaining seven species. The biomass trajectories are very similar to those in the main text (Figure S1 vs Figure 1). Performance appears to be slightly worse for some stocks (e.g., Redfish and Silver Warehou), but better for others (e.g., Bight Redfish, Orange Roughy, and School Whiting). Overall, using  $M$  from Fishbase reduces relative error for  $K$  and  $F_{msy}$  but increases it for MSY (Table S1 vs Table 1).

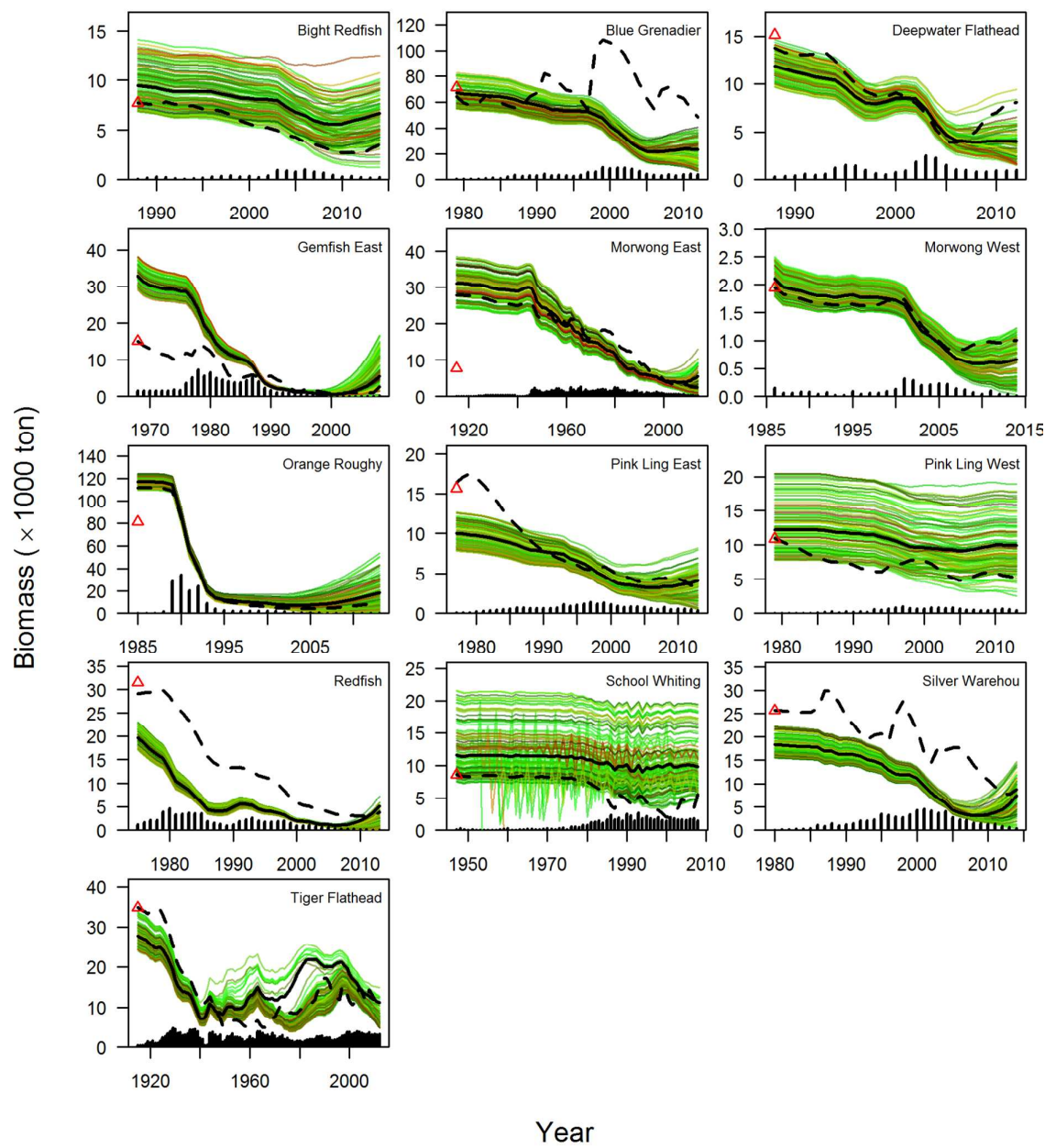


Figure S1. OCOM-estimated exploitable biomass trajectories (coloured lines) from 100  $r$ - $K$  pairs for 13 SESSF stocks using  $M$  from Fishbase. The solid black line is the median, the black dashed line is the "true" biomass from SS, the red triangle is estimated  $K$  from SS, and the vertical bars are the observed catch. Note that the start of the solid black line is the median  $K$  from OCOM, and the start of the dashed line is the initial biomass from SS.

Table S1. Comparison of estimates of  $K$ ,  $F_{MSY}$  and  $MSY$  from Stock Synthesis (SS) and OCOM for 13 SESSF stocks. RE = relative error.  $M_{SS} = M$  used in SS.  $M_{fb} = M$  from Fishbase.

Stock	SS			OCOM			RE				
	$K$	$F_{msy}$	$MSY$	$K$	$F_{msy}$	$MSY$	$K$	$F_{msy}$	$MSY$	$M_{SS}$	$M_{fb}$
Bight Redfish	7,735	1.45	611	9,454	0.12	580	0.22	-0.91	-0.05	0.11	0.16
Blue Grenadier	70,993	0.22	4,435	66,843	0.14	4,672	-0.06	-0.36	0.05	0.18	0.18
Deepwater Flathead	15,164	0.29	1,257	11,862	0.17	1,044	-0.22	-0.40	-0.17	0.24	0.23
Gemfish East	15,146	0.08	538	32,866	0.22	3,651	1.17	1.70	5.78	0.38	0.36
Morwong East	7,693	0.23	468	31,156	0.09	1,374	3.05	-0.62	1.93	0.15	0.12
Morwong West	1,943	0.80	185	2,106	0.09	97	0.08	-0.89	-0.48	0.15	0.12
Orange Roughy	81,054	0.20	2,192	116,774	0.08	4,876	0.44	-0.57	1.22	0.04	0.11
Pink Ling East	15,670	0.16	789	10,028	0.16	806	-0.36	0.01	0.02	0.21	0.21
Pink Ling West	10,893	0.23	789	12,189	0.16	896	0.12	-0.28	0.14	0.21	0.21
Redfish	31,537	0.09	980	19,612	0.25	2,410	-0.38	1.59	1.46	0.10	0.37
School Whiting	8,578	1.25	2,268	11,556	0.62	3,351	0.35	-0.50	0.48	0.58	0.84
Silver Warehou	25,715	0.36	2,686	18,262	0.32	2,958	-0.29	-0.10	0.10	0.30	0.50
Tiger Flathead	34,818	0.28	2,830	27,733	0.21	2,909	-0.20	-0.25	0.03	0.27	0.37
Mean RE	25,149	0.43	1,541	28,496	0.20	2,279	0.30	-0.12	0.81		



## 2. R codes for OCOM

```
#####
##                               Optimized catch-only method function  ##
#####

## Predictors for BRT model
# First load the following function catchParam.
# This function derives 56 predictors based on catch history.
# It can be used for batch processing of multiple stocks.
# Data format must be 3 columns: stock, yr, catch.

require(segmented)
require(gbm)
require(dismo)
require(fGarch) # for skewed normal dist

catchParam = function(catchData) {
  sid = unique(as.character(catchData$stock))
  n.stock = length(sid)
  para = matrix(NA, n.stock, 57)
  n.ab = 7 # number of years at the beginning and ending time series
  a=b=a0=b0=matrix(0, n.stock, n.ab)
  for(i in 1:n.stock) {
    stk = sid[i]
    dat = subset(catchData, stock==stk)
    yr = dat$yr-min(dat$yr) + 1
    midYr = mean(yr)
    C = dat$catch/max(dat$catch) # regressions are based on scaled catch
    C05max = sum(C[-length(C)]>0.5)
    Cmean = mean(C)
    nyr = length(yr)
    nyrToCmax = min(yr[C==max(C)]-yr[1]+1)
    nyrToCmaxR = nyrToCmax/nyr
    nyrAfterCmax = nyr-nyrToCmax
    yr.cent = yr-midYr # regressions are based on centred year
    line0 = lm(C~yr.cent)
    yr1.cent = yr[1:nyrToCmax]-mean(yr[1:nyrToCmax])
    line1 = lm(C[1:nyrToCmax]~yr1.cent)
    yr2.cent = yr[nyrToCmax:nyr]-mean(yr[nyrToCmax:nyr])
    line2 = lm(C[nyrToCmax:nyr]~yr2.cent)
    aa0 = summary(line0)$coeff[1]; bb0 = summary(line0)$coeff[2] #all yr
    aa1 = summary(line1)$coeff[1]; bb1 = summary(line1)$coeff[2] #before Cmax
    aa2 = summary(line2)$coeff[1]; bb2 = summary(line2)$coeff[2] #after Cmax
    for (j in 1:n.ab) { # periodical regressions
      yrLast.cent = yr[(nyr-j):nyr]-mean(yr[(nyr-j):nyr])
      l.last = lm(C[(nyr-j):nyr]~yrLast.cent) # last several years
      a[i,j] = summary(l.last)$coeff[1];
      b[i,j]=summary(l.last)$coeff[2]
      yrBegin.cent = yr[1:(j+1)]-mean(yr[1:(j+1)])
      l.begin = lm(C[1:(j+1)] ~ yrBegin.cent) # beginning several years
      a0[i,j] = summary(l.begin)$coeff[1]
      b0[i,j] = summary(l.begin)$coeff[2] }
  }
}

# segmented regression: use yr and breakpoint is between 0-1
```



```

f = tryCatch(segmented(line0, seg.Z=~yr, psi=list(yr=median(yr))) , error=function(err) {})
if(is.null(f)) {
  a.spline = NA; b1.spline = NA; b2.spline = NA; breakPoint = NA
} else {
  a.spline = summary(f)$coef[1]
  b1.spline = summary(f)$coef[2]
  slp= slope(f)
  b2.spline = slp$yr[2]
  breakPoint = (round(f$psi.history[[5]],0)-yr[1] +1)/nyr
}
para[i,] = c(aa0, aa1, aa2, bb0, bb1, bb2, a[i,], b[i,], a0[i,], b0[i,], a.spline, b1.spline,b2.spline,
breakPoint, C[1:n.ab], C[(nyr-n.ab): nyr], Cmean, nyrToCmaxR, nyr, C05max)
} # end params
colnames(para) = c('a.AllYr', 'a.BfMax', 'a.AfMax', 'b.AllYr', 'b.BfMax', 'b.AfMax',
paste('a.LsY',1:n.ab, sep=""), paste('b.LsY',1:n.ab, sep=""), paste("a.BgY", 1:n.ab, sep = ""),
paste('b.BgY', 1:n.ab, sep=""), 'a.seg', 'b1.seg', 'b2.seg', 'breakPoint', paste('c.BgY',1:n.ab, sep=""),
paste('c.LsY', n.ab:0, sep=""), 'Cmean', 'nyrToCmaxR', 'nyr', 'C05max')
para = data.frame(stock=sid, para)
return(para)
}

#### biomass dynamics model: one parameter r, using optimize
BDM = function(K, r, S, b, C) {
  nyr = length(C)
  B = vector()
  B[1] = K*b
  for (i in 1:nyr) {
    B[i+1] = max(min(B[i]+r*B[i]*(1-B[i]/K)-C[i], K), 0)
  }
  if (all(B[-nyr]>C) & all(B<=K)) abs(B[nyr]/K-S) else max(K)*10^4
}

### derive S = B/K prior bwt [0,1]
Sdistrib = function(n, s_mean) {
  nv = 0 ; n.redo = 0
  while(nv < n) {
    n.redo = n.redo+1
    if(s_mean<=0.5) {
      si1 = rsnorm(n*n.redo, mean=max(s_mean,0)-0.072, sd=0.189, xi=0.763)
      si = si1[si1>0 & si1<1]
    } else if(s_mean>0.5) {
      si1 = rsnorm(n*n.redo, mean=max(s_mean,0)+0.179, sd=0.223, xi=0.904)
      si = si1[si1>0 & si1<1]
    }
    if(length(si)>n) si = sample(si,n);
    nv = length(si)
  }
  return (si)
}

### draw biomass trajectories
drawBt = function(cdat, oc0){
  B = Bmed = vector()
  n.sim = 100
  oc1 = oc0[oc0$obj<0.01 & oc0$k>1.01*min(oc0$k) & oc0$k<0.99*max(oc0$k), c(2:5)] #
eliminate bordering effect
  oc2 = oc1[oc1$k>quantile(oc1$k, 0.25) & oc1$k<quantile(oc1$k, 0.75),]

```

```

smp = sample(1:nrow(oc2), n.sim, replace=T)
if(min(oc2$k)>1000) {
  k = oc2[smp,1]/1000
  C = cdat$catch/1000
} else {
  k = oc2[smp,1]
  C = cdat$catch }
r = oc2[smp,2]
kmed = median(k); rmed = median(r)
stock = cdat$stock[1]
yr=cdat$yr; nyr = length(yr)

plot(rep(0, nyr)~yr, type='n', ylim=c(0, max(k)*1.2), xlab="", ylab="", las=1, yaxs='i')#
expression("B (" %%% "1000t)", las=1)
legend("topright", legend=stock, bty='n', cex=0.8)
Bmed[1] = kmed
for (j in 1:n.sim){
  B[1] = k[j]
  for(t in 1:(nyr-1)) {
    B[t+1] = (B[t]+r[j]*B[t]*(1-B[t]/k[j])-C[t]
    Bmed[t+1] = (Bmed[t]+rmed*Bmed[t]*(1-Bmed[t]/kmed)-C[t]
  }
  lines(yr, B, col=rgb(runif(1,0,j)/n.sim,(n.sim-runif(1,0,j))/n.sim, 1/(n.sim+100), alpha=0.6) )
}
lines(yr, Bmed, lwd=2)
lines(C~yr, type='h', lwd=2 )

mtext('Year', side=1, line=2, outer=T)
if(min(oc2$k)>1000) mtext(expression('Biomass (' %%% '1000 ton)'), side=2, line=2, outer=T)
else mtext(expression('Biomass (ton)'), side=2, line=2, outer=T)
}

#####
#           Optimized Catch-Only Method           #
#           December 2016                         #
#####

require(fGarch) # for skewed normal dist
require(plyr)

## Import catch and M data
## catch data must have three columns: stock, yr, catch
## natural mortality data has two columns: stock, M
## Example: SESS stocks in Australia
Dir =("E:/")
catchData =read.table(paste0(Dir, 'catchData.txt'), head=T)
sessM =read.table(paste0(Dir, 'sessM.txt'), head=T)

## if M is unknown, derive M from other life history parameters, e.g.:
M = vector()
M[1] = 4.899*Tmax^-0.916      # Tmax = max age
M[2] = 4.11*k^0.73*Linf^-0.33 # k and Linf: Bertalanffy growth parameters
M[3] = 1.82*k
M[4] = 1.65/Tmat             # Tmax = maturation age

```

```

M = mean(M)

## derive prior for stock saturation S = B/K
## load saved BRT models: two alternative models. You can use 1 or both models.
## model 1: BRTmodelP8 (using 8 predictors )
## model 2: BRTmodelP38 (using 38 predictors)
load(file = paste0(Dir, "BRTmodelP8.RData")) # model 1
load(file = paste0(Dir, "BRTmodelP38.RData")) # model 2

## derive predictors from catch history
sessPar = catchParam(catchData)

## centering the first 37 predictors
sessParCent = scale(sessPar[,2:38], center=BRTmodelP8$parMean, scale=F)

## construct predition data
stockName = unique(as.character(catchData$stock))
nstk = length(stockName)
predDat = data.frame(stock=stockName, sessParCent, sessPar[,39:57])

## estimating saturation S
s8 = predict.gbm(BRTmodelP8$model, predDat, n.trees=BRTmodelP8$model$gbm.call$best.trees,
type="response")
s38 = predict.gbm(BRTmodelP38$model, predDat,
n.trees=BRTmodelP38$model$gbm.call$best.trees, type="response")

## Bias correction
## for model 1
slr8.a = BRTmodelP8$slr[[1]]; slr8.b = BRTmodelP8$slr[[2]];
sBC8 = (s8-slr8.a)/slr8.b
sBC8[sBC8<=0] = 0.01

## for model 2
slr38.a = BRTmodelP38$slr[[1]]; slr38.b = BRTmodelP38$slr[[2]];
sBC38 = (s38-slr38.a)/slr38.b
sBC38[sBC38<=0] = 0.01

## Output S
sessS = data.frame(stock=stockName, S8=sBC8, S38=sBC38, S = (sBC8+sBC38)/2)

#####
#####      OCOM      #####
#####

n = 10000
summ = array(NA, dim=c(5,4,nstk))

for (i in 1:nstk) { # i=1
  stk = stockName[i]
  dat = subset(catchData, stock==stk)
  C = dat$catch ;
  yr = dat$yr
## derive r prior with lognorm dist
  M = sessM$M[sessM$stock==stk]
  r_mean = M*1.72; r_var = 0.23      # for teleosts

```

```

r_sig = sqrt(log(r_var/(r_mean)^2+1))
## r_mean = 0.79*M ; r_var = 0.23      # for chondrichthyans
r_mu = log(r_mean)-r_sig^2/2
ri = rlnorm(n, r_mu, r_sig)

## derive S prior btw 0 and 1
s_mean = sessS[sessS$stock==stk, 4] # column 2 = BRTmodelP8
si = Sdistrib(n, s_mean)

rs = cbind(r=ri, s=si)
k.low = max(C); k.up=max(C)*200
opt = apply(rs, 1, function(x) { optimize(BDM, c(k.low, k.up), r=x[["r"]], S=x[["s"]], b=1, C=C) })

ki = sapply(opt, '[', 1)
msy = ki*ri/4
obji = sapply(opt, '[', 2)
kr = data.frame(k=ki, r=ri, msy, s=si, obj=obji)
write.csv(kr, paste0(Dir, "test/krms", i, ".csv", sep=""))

## summary
kr2 = kr
kr2[kr2$k<1.01*k.low | kr2$k>0.99*k.up | kr2$obj>0.01,] = NA # bordering effect
kr2 = na.omit(kr2)
# plot(log(kr2$k), log(kr2$r), xlab="K", ylab='r')
# abline(h=mean(log(kr$r)), v=mean(log(kr$k)), lty=2, col=2)
summ[,i] = apply(kr2, 2, function(x) quantile(x, c(0.05, 0.25, 0.5, 0.75, 0.95)))[1:4]
}

## summary result
summ2 = adply(summ, 3)
colnames(summ2)=c('stockID', 'k', 'r', 'MSY', 'S')
sumOut = data.frame(percent=rep(c(5, 25, 50, 75, 95),nstk), summ2)
write.csv(sumOut, paste0(Dir, "result.csv"))

#####
## distribution
par(mfrow=c(2,2), mai=c(.8,.8,0.1,0.1))
hist(kr2$k, xlab='K', main="", las=1); abline(v=median(kr$k), lwd=2);
hist(kr2$r, xlab='r', main="", las=1); abline(v=median(kr$r), lwd=2);
hist(kr2$msy, xlab='MSY', main="", las=1); abline(v=median(kr$msy), lwd=2);
hist(kr2$s, xlab='S', main="", las=1); abline(v=median(kr$s), lwd=2);

#####
## draw 100 biomass trajectories

windows()
par(mfrow=c(5,3), mai=c(.2,.25,0.1,0.1), omi=c(0.5,0.5,0,0))

for (i in 1:nstk) { # i=1
  cdat = subset(catchData, stock==stockName[i])
  oc0 = read.csv(paste0(Dir,'test\\krms', i, '.csv', sep=""))
  drawBt(cdat, oc0)
}

```