



# Collateral Management and Counterparty Credit Risk

## Summary

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- ◆ Benefits of Collateral Posting
- ◆ Collateral Arrangement Forms
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- ◆ Valuation under Collateral Arrangement
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## Collateral Definition

- ◆ Collateral is a property or an asset that a borrower offers as a way for a lender to secure the loan.
- ◆ Collateral arrangement is a risk reduction tool that mitigates risk by improving recovery and reducing credit exposure.
- ◆ Collateral doesn't turn a bad counterparty into a good one and doesn't eliminate credit risk. Instead, it just reduces the loss at the default time.
- ◆ Collateral management is an essential element in the plumbing of the financial system.
- ◆ Collateral assets: mainly cash; also equities, bonds, MBS, debt instruments.

### Special Treatments in the Derivatives Market

- ◆ The Bankruptcy code generally prevents creditors from seizing assets of a firm in bankruptcy. This provision is called the “automatic stay”.
- ◆ The code affords a special treatment to financial derivative contracts, which exempts these contracts from the “automatic stay”.
- ◆ The special treatment is also called a safe harbor.
- ◆ The safe harbor allows counterparties to terminate derivative contracts with a debtor in bankruptcy and seize the underlying collaterals.

# Collateral

## Benefits of Collateral Posting

- ◆ Reduce credit risk.
- ◆ Free credit lines with existing counterparties.
- ◆ Increase business with counterparties.
- ◆ Expand the range of counterparties.
- ◆ Equalize the disparity in counterparty creditworthiness.

# Collateral

## Collateral Arrangement Forms

- ◆ There are two types of collateral arrangement: pledge and title transfer.
- ◆ Pledge
  - ◆ The giver posts collateral to the taker.
  - ◆ The giver still owns the collateral.
  - ◆ If the giver defaults, the taker can take the cash or sell the securities.
  - ◆ It is widely used in US.
- ◆ Title Transfer
  - ◆ The taker owns the collateral.
  - ◆ The giver is only entitled to the return of fungible securities and/or repayment of cash.
  - ◆ It is widely used in the stock-lending and repo market.

## Credit Support Annex (CSA)

- ◆ CSA (or Margin Agreement or Collateral Agreement) is a legal document that regulates collateral posting.
- ◆ It specifies a variety of terms related to collateral posting.
  - ◆ Threshold (TH) defines the amount below which no collateral is posted.
  - ◆ Minimum transfer amount (MTA) is the minimum amount that can be transferred for any margin call.
  - ◆ Independent amount (or initial margin or haircut) is the amount of collateral required to open a position.
- ◆ Collateral posting rules
  - ◆ If  $\text{Value} > \text{TH} + \text{MTA}$ , collateral is called and  $\text{collateral} = \text{Value} - \text{TH} - \text{MTA}$
  - ◆ If  $\text{Value} \leq \text{TH} + \text{MTA}$ , no collateral is called.

## Valuation under Collateral Arrangement

- ◆ A simple example: a financial contract pays  $X$  at maturity  $T$ .
- ◆ Valuation without collateral arrangement
  - ◆ At time  $T$ , the contract either defaults or survives.
  - ◆ The default probability is  $p$  and the survival probability is  $q$  where  $q = 1-p$ .
  - ◆ The survival payoff is  $X$  and the default value is  $\varphi X$  where  $\varphi$  is the recovery rate.
  - ◆ The present value of the contract is the discounted expectation of all the possible payoffs, i.e.,

$$V(t) = (p\varphi X + qX)D(t)$$

where  $D(t)$  is the discount factor.

# Collateral

## Valuation under Collateral Arrangement (Cont)

- ◆ Valuation with collateral arrangement
  - ◆ At time  $T$ , the contract either defaults or survives.
  - ◆ If the party survives, the survival payoff is  $X$  and the taker returns the collateral to the giver. In this case, collateral has no effect at all.
  - ◆ If the party defaults, the default payment is the collateral  $C$ .
  - ◆ The present value of the contract is the discounted expectation of all the possible payoffs and given by

$$V_c(t) = (pC + qX)D(t)$$

- ◆ Normally  $C > p\varphi$ , thus  $V_c(t) > V(t)$ .
- ◆ Conclusions:
  - Collateral affects default payoff only.
  - Collateral improves recovery.
  - Collateral increases value.

## Credit Exposure under Collateral Arrangement

- ◆ Settlement period (call period) is the time period from the time of the collateral called to the time of the collateral exchanged.
- ◆ Liquidation period (cure period) is the time period from the most recent exchange of collateral until the defaulting counterparty is closed out.
- ◆ Margin period of risk = settlement period + liquidation period.
- ◆ Let  $MTM_t = \max(\sum_i MTM_t^i, 0)$  be the portfolio value at time  $t$  where  $MTM_t^i$  is the value of i-th trade at time  $t$ .

### Credit Exposure under Collateral Arrangement (Cont)

- ◆ If we assume that the collateral asset is cash only, the credit exposure is given by

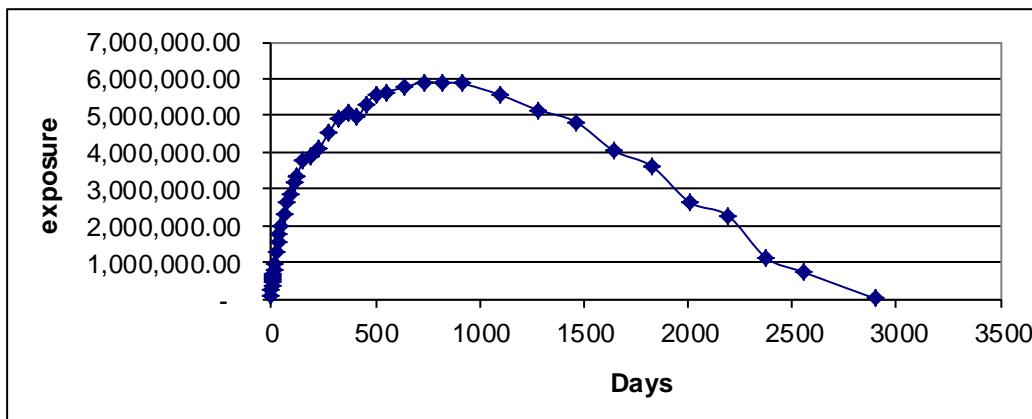
$$E_c(t) = \begin{cases} MTM_t & \text{if } MTM_t \leq TH + MTA \\ TH + MTA & \text{if } MTM_t > TH + MTA \end{cases}$$

- ◆ If the collateral is non cash, then  $MTM_t = \max(\sum_i MTM_t^i, 0) + MTM_t^C$  where  $MTM_t^C$  is the value of the collateral asset. In other words, we need to simulate the value change of the collateral asset during the margin period of risk.

## Collateral

### Credit Exposure under Collateral Arrangement (Cont)

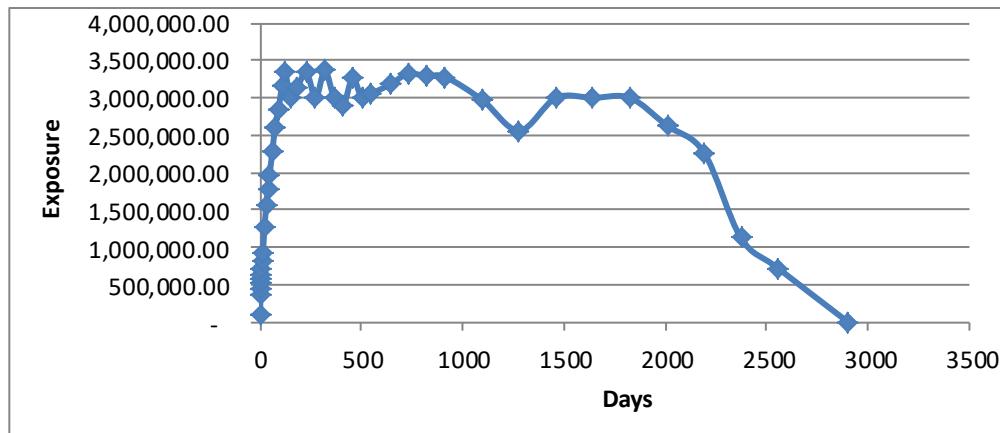
- The credit exposure of an uncollateralized interest rate swap is shown below



## Collateral

### Credit Exposure under Collateral Arrangement (Cont)

- The credit exposure of a collateralized interest rate swap is shown below



# Thanks!



You can find more details at  
<https://finpricing.com/lib/EqWarrant.html>