

# Design space exploration for novel reduced-vortex turbine rotors using free vortex wake methods

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slides available at:  
[cfrontin.github.io/NAWEA.pdf](https://cfrontin.github.io/NAWEA.pdf)

# Wind turbine power optimization (status quo)

maximize  $\{c_i, \theta_i\}_{i=1}^N C_P$   
subject to E.o.M.

approximated by

maximize  $\{c_i, \theta_i\}_{i=1}^N C_P$   
subject to BEM eqns.

a simplified yet common  
blade design problem:

- maximize power output
- changing chord and twist

given a geometry, power is  
approximated by the BEM  
equations

power-maximizing chord and  
lift distributions determined  
algorithmically (using dozens  
of solutions of BEM eqn.)

# Blade design methods *mimic* reality

## *BEM-based design*

basic aerodynamic model  
    ⇐ airfoil lift and drag polars  
neglect all interactions between  
    vortices and blade sections  
tip and wake rotation effects  
    ⇐ simple engineering models  
intuitive modeling assumptions  
    ⇐ a different era of computing

## *Idealized design*

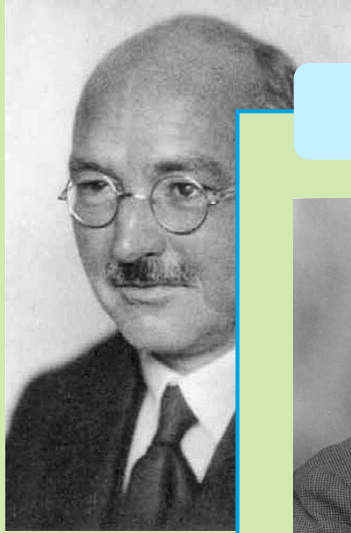
optimization across full spectrum  
    of aerodynamic behavior  
full consideration of coupling

- spanwise vortex distribution
- tip and wake treatment
- radial/spanwise  
    flow/interactions

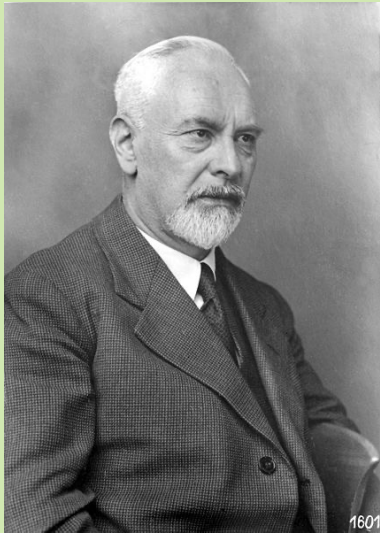
resolve the effects of all relevant  
    features of turbine flow in space  
    and time

# All simulation methods mimic reality ... at different levels of cost and fidelity

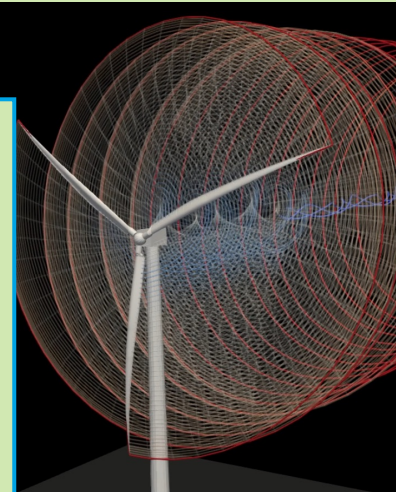
BEM



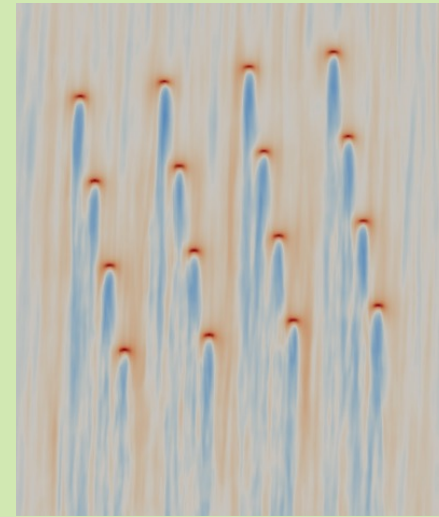
Lifting Lines



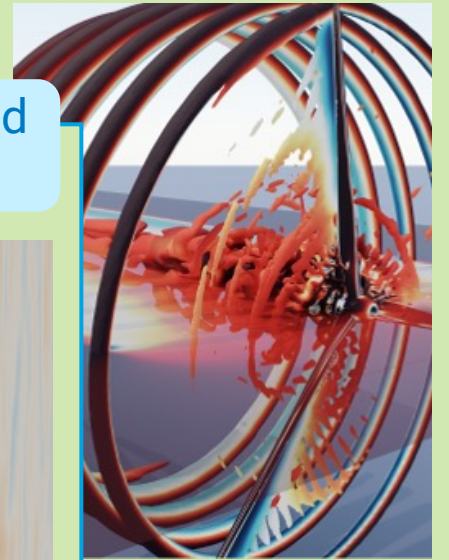
Vortex Methods



Actuator Modeled  
CFD



Blade-resolving CFD



increasing cost, increasing fidelity

# Can physical wind turbines be designed to generate more power than BEM designs?

Madsen, et. al., 2022:

- post-hoc winglet modification for turbine blades
- CFD-based optimization
  - maximize  $C_P$  without increasing thrust
  - 1-2% improvement in  $C_P$
  - twist, chord, and tip geometry variation

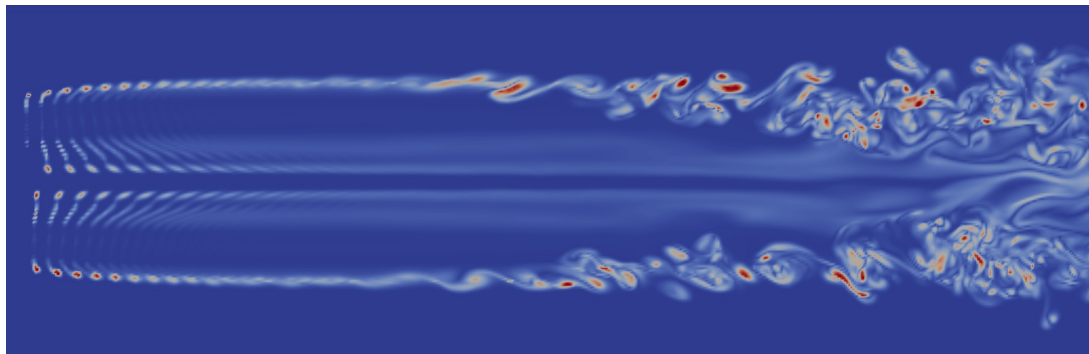
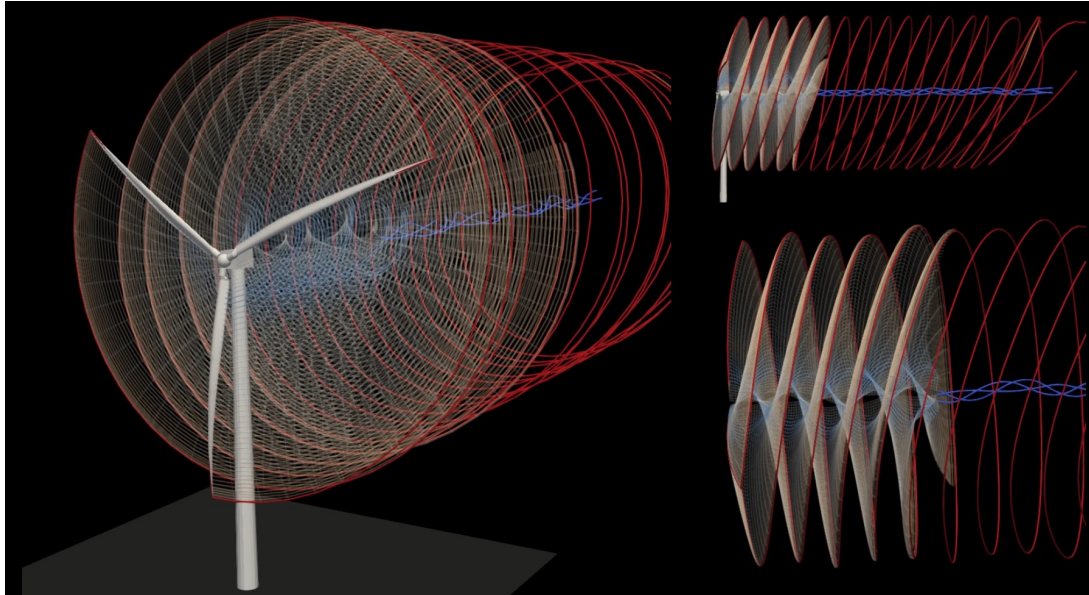
Barlas, et. al., (2021 & 2022):

- experimental studies of winglet modification
- multi-fidelity simulation comparison against experimental results
- broad agreement
  - all methods include some non-representation of physical phenomena

Can we create designs using mid-fidelity methods that outperform BEM-based designs?



# OLAF: NREL's Free Vortex Wake Solver



OLAF:

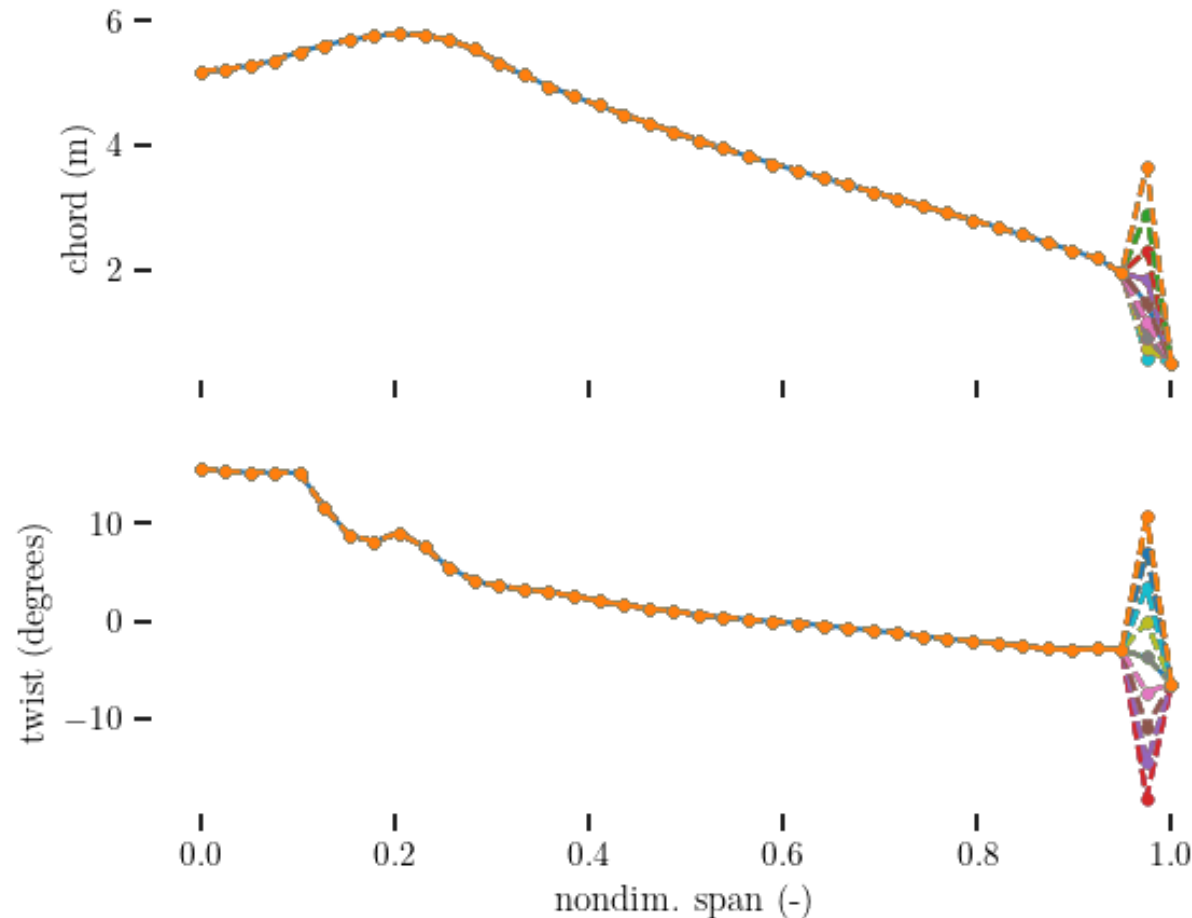
- medium-fidelity aero discretization
- discretizes vortices allowing convection, stretching, dissipation, etc.
- under the hood:
  - blades: lifting-line method
  - near wake: vortex lattice
  - far wake: convecting Lagrangian filaments for root/tip vortices



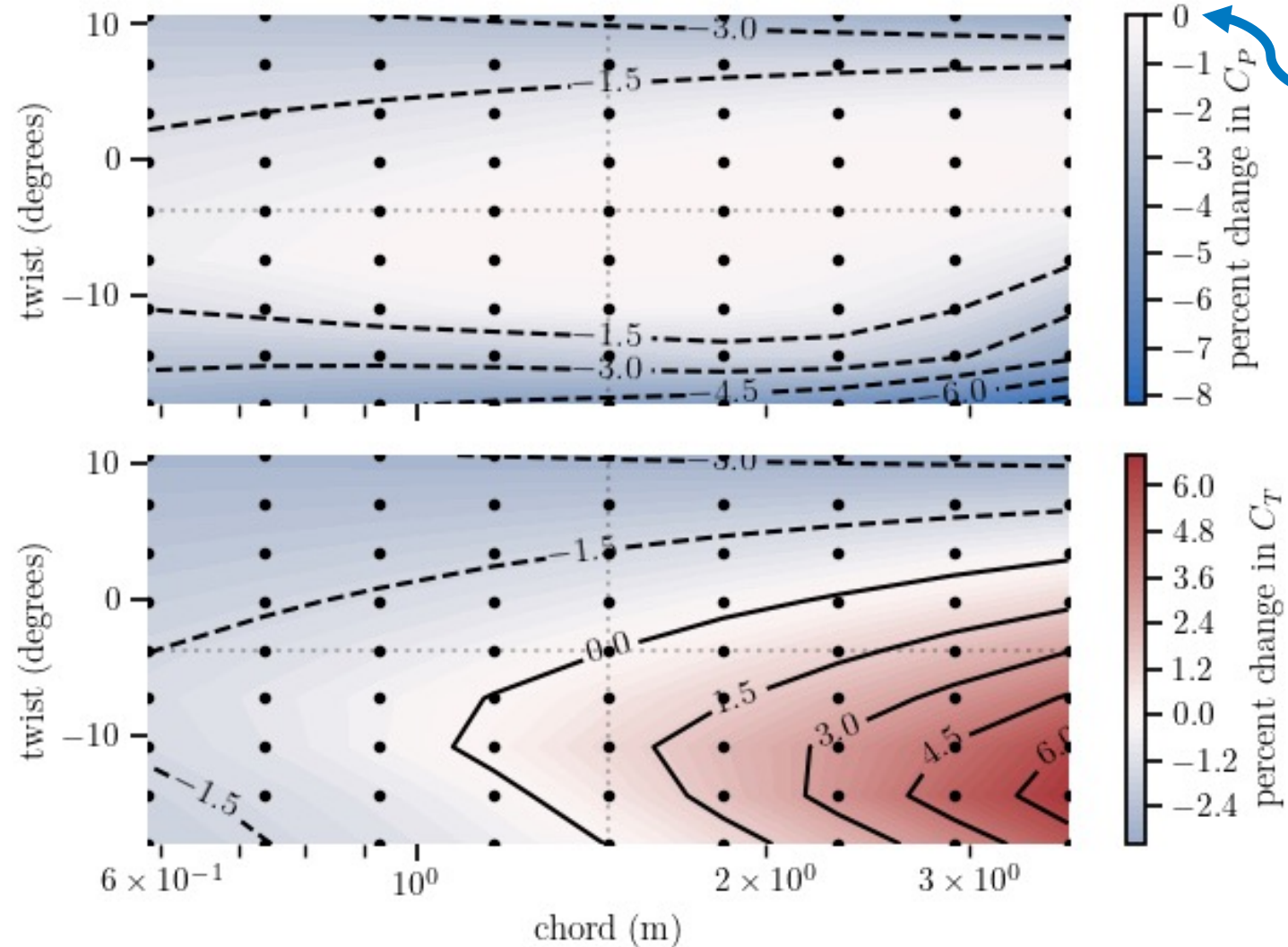
# Design of experiments: perturbations

make perturbations

- chord & twist
- 9x9 grid
- at each point:  
evaluate aero  
performance
  - BEM
  - OLAF (FVW)  
w/ 150 pts.  
(converged)

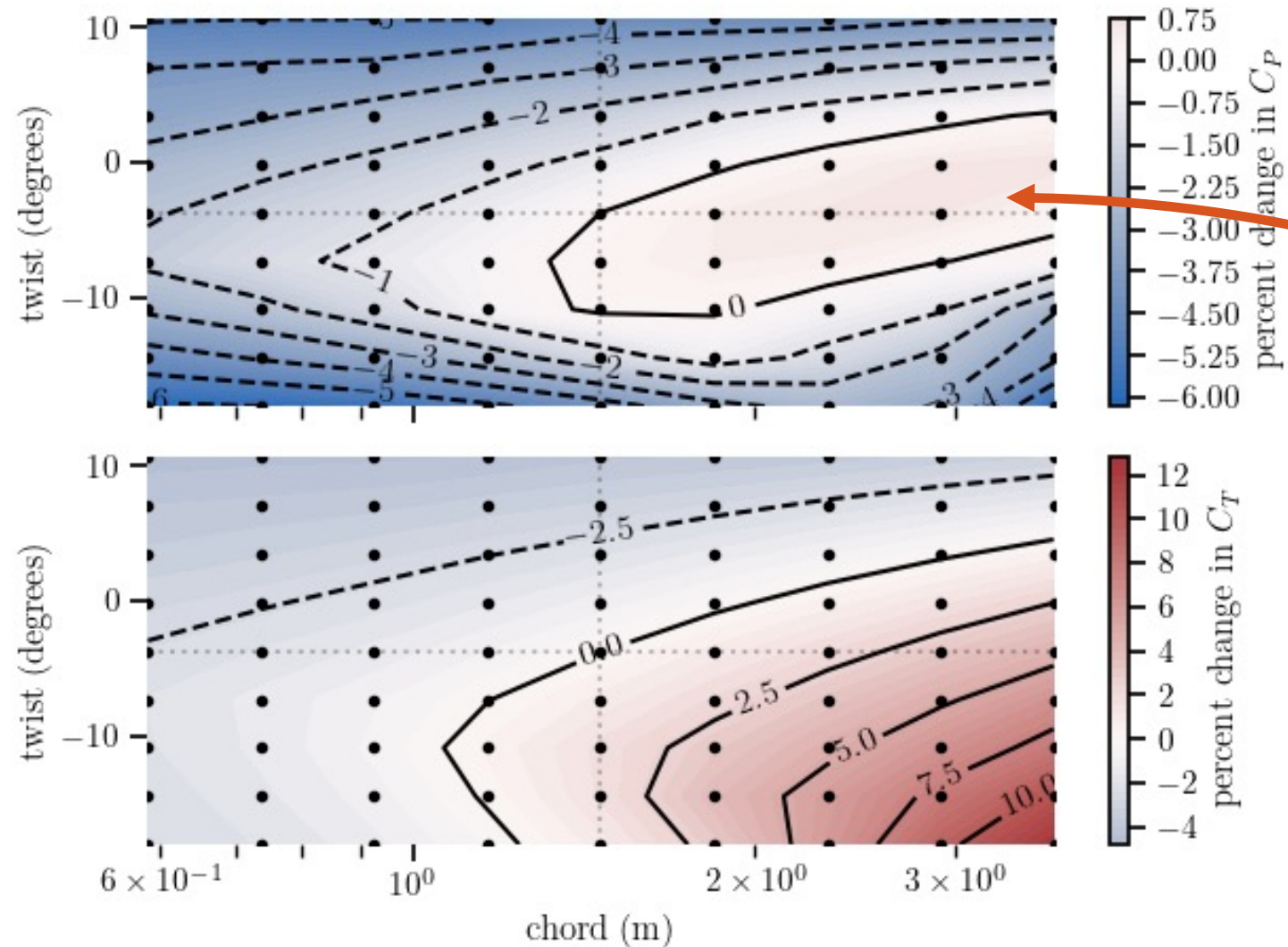


# Design of experiments: BEM



across the  
response surface,  
power is nowhere  
improved

# Design of experiments: OLAF



significant region  
in the design  
space where  
OLAF >> BEM

Can we create optimal designs  
using mid-fidelity methods  
in the design loop?

# Wind turbine power optimization (proposed)

maximize  $\{c_i, \theta_i\}_{i=1}^N C_P$   
subject to E.o.M.

approximated by

maximize  $\{c_i, \theta_i\}_{i=1}^N C_P$   
subject to F.V.W. E.o.M.

rather than BEM, use OLAF FVW  
to design the rotor blade

some subtle changes:

- interactions between blade sections introduced
  - formerly:  
 $\Delta C_P \Leftarrow \Delta(\text{flow})_j \Leftarrow \Delta\{c_j, \theta_j\}$
  - now:  
 $\Delta C_P \Leftarrow \{\Delta(\text{flow})_j\}_{j=1}^N \Leftarrow \Delta\{c_j, \theta_j\}_{j=1}^N$
- optimization more complex
  - global local subproblem

# Wind turbine power optimization w/ SNOPT

maximize  $\{c_i, \theta_i\}_{i=1}^N C_P$

subject to E.o.M.

approximated by

maximize  $\{c_i, \theta_i\}_{i=1}^N C_P$

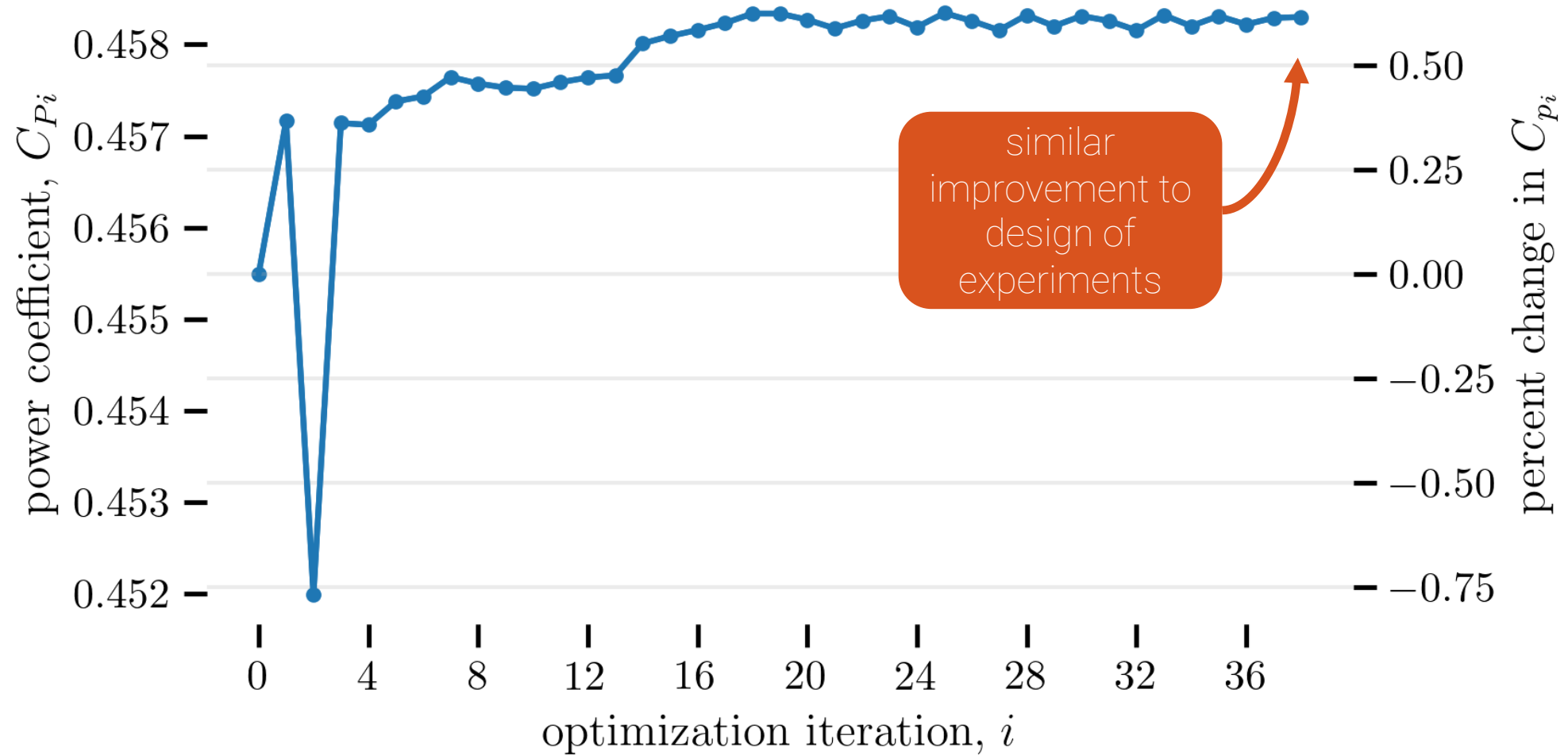
subject to F.V.W. E.o.M.

optimization problem  
implemented with SNOPT  
(Sparse Nonlinear *Opt*imizer)

use OLAF FVW, w/ 50 pts.

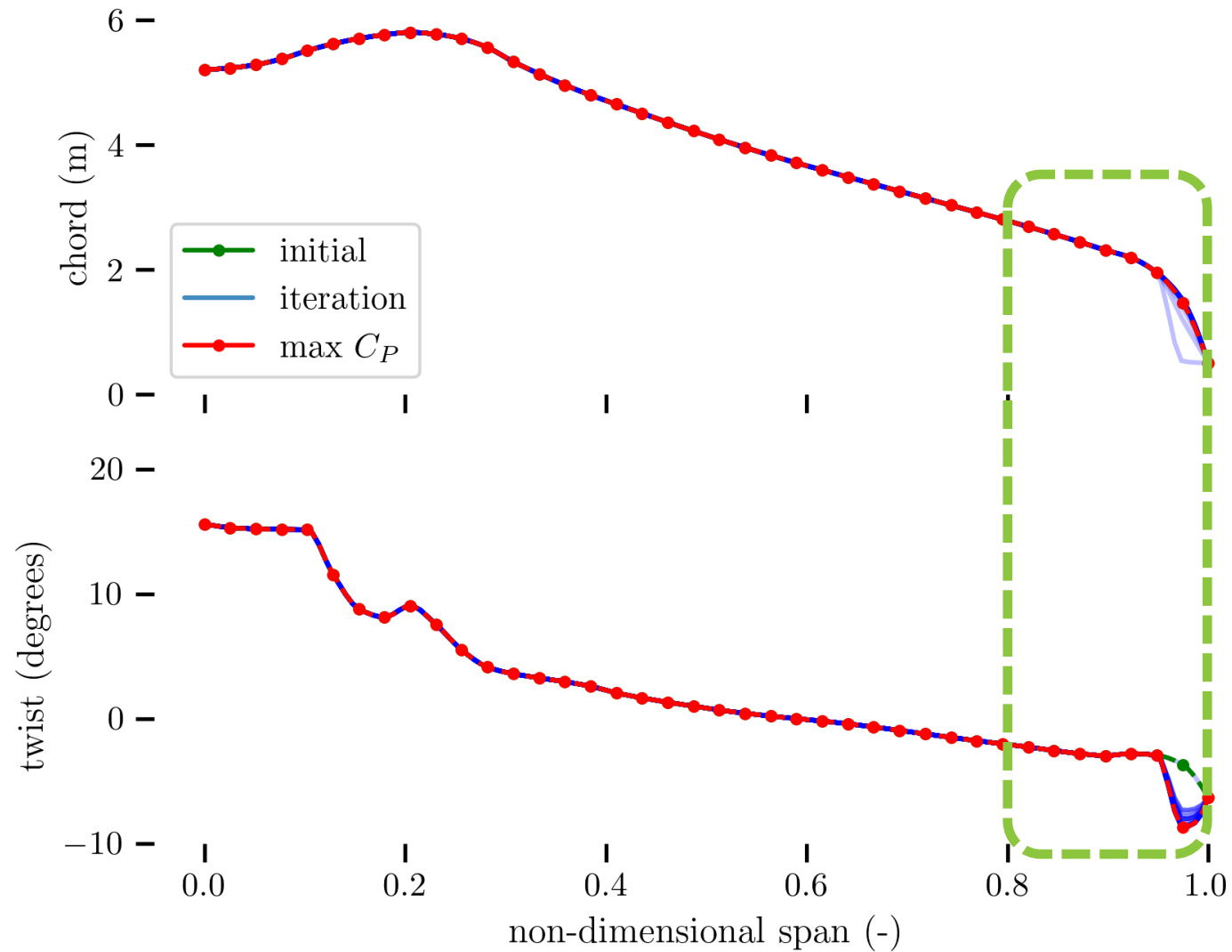
- not directly comparable to previous solution space
- for cost savings in optimization loop

# Optimization: convergence

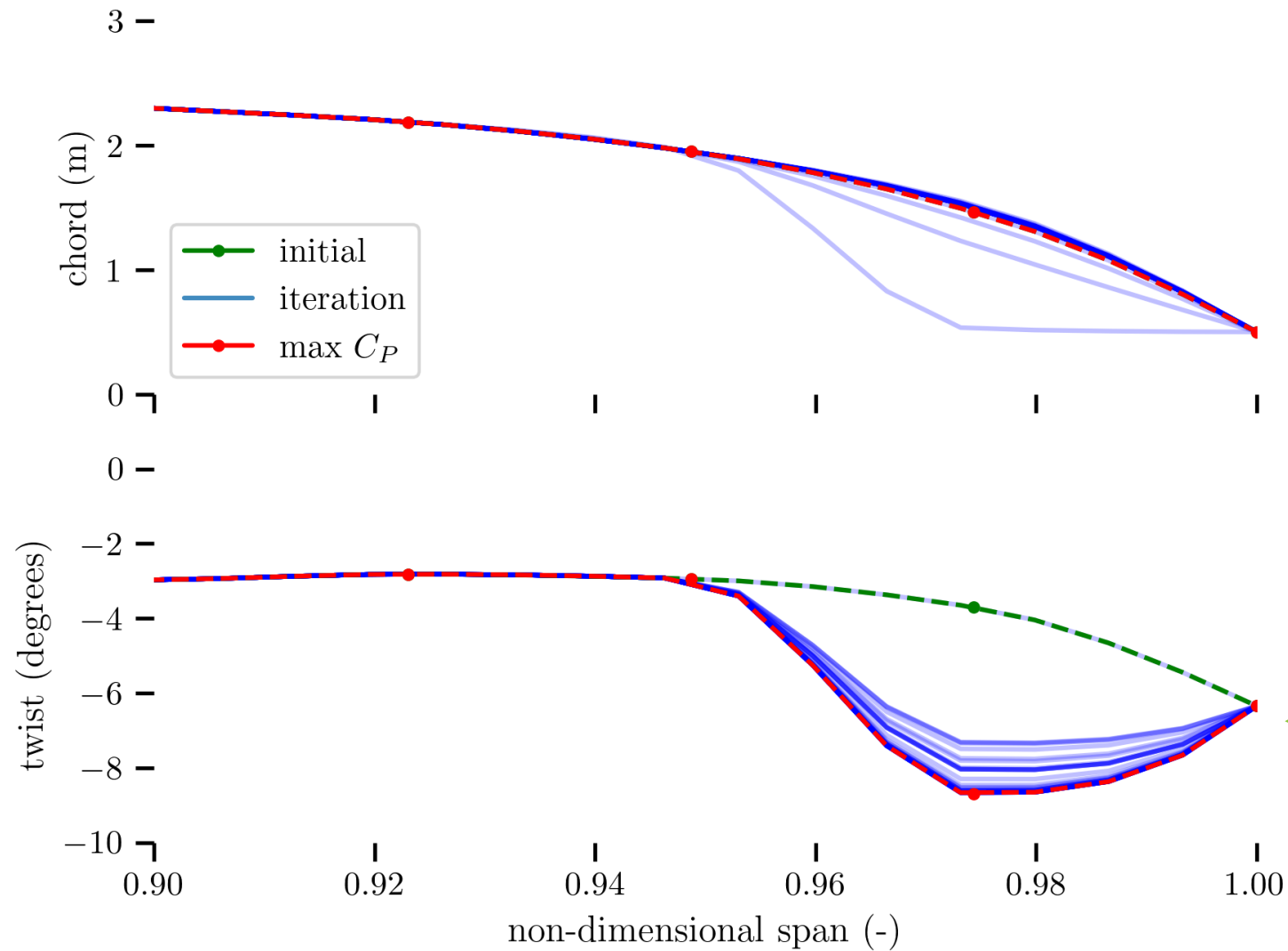




# Optimization: design iterations



# Optimization: design iterations

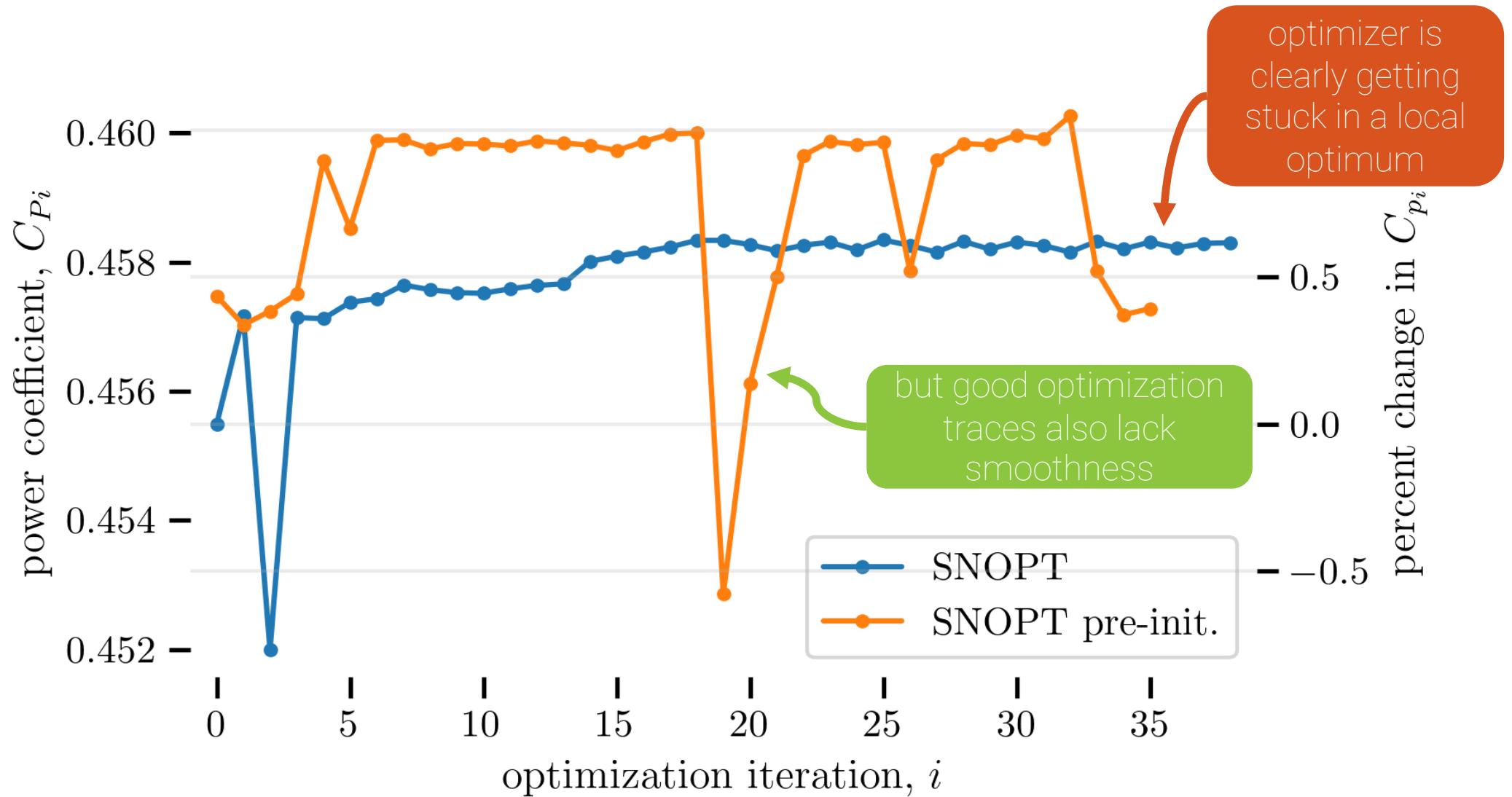


# Optimization/design of experiments disagree

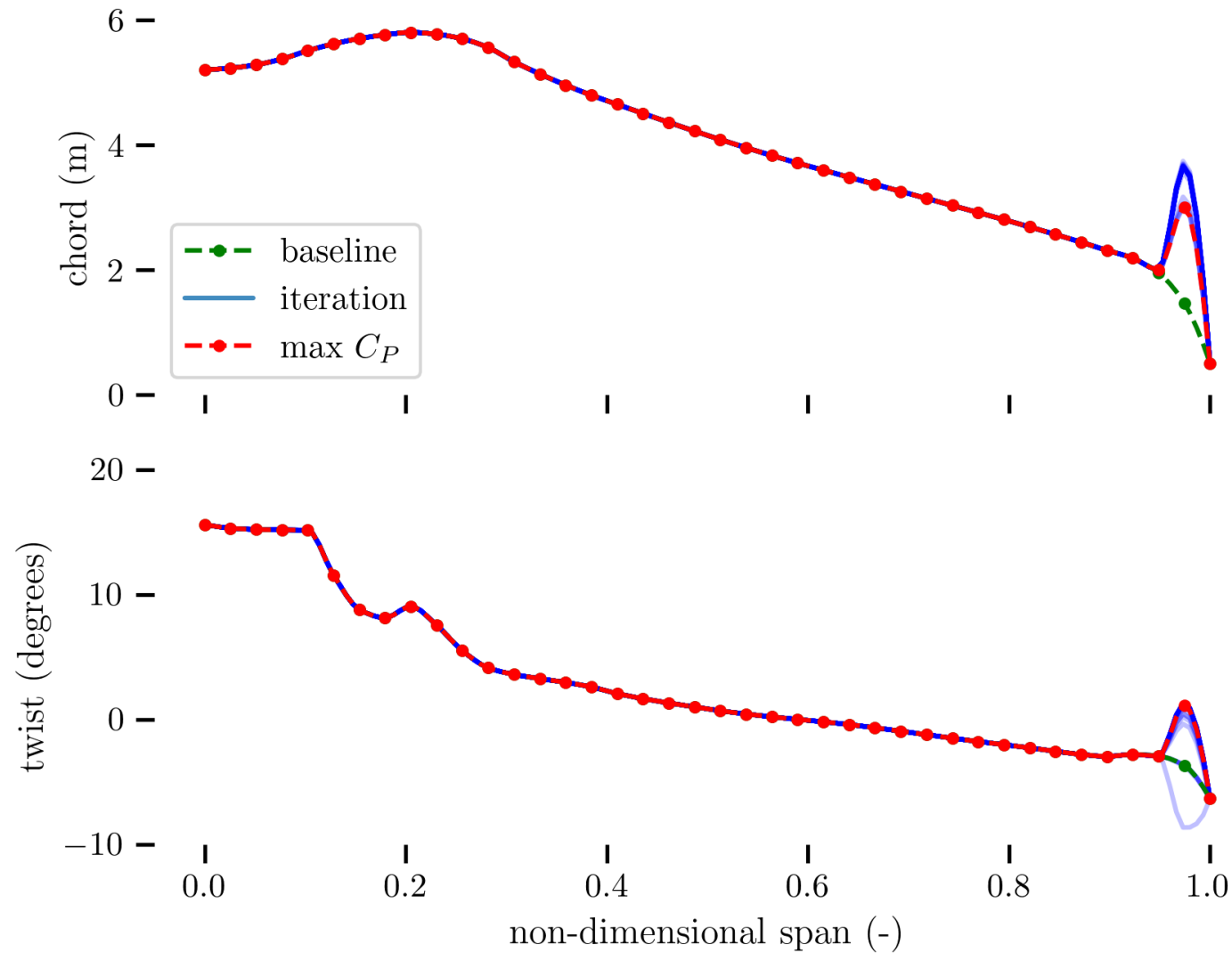
Potential causes:

- (in)stability of FVW solutions
  - FVW: variable-DOF representation of convected vortices
  - highly nonlinear interactions between vortex filaments
  - FVW requires numerical diffusion & truncation
  - are finite-difference gradient computations reliable?
- non-convexity of solution space
  - do local minima prevent global optimality?
- optimization into numerical features
  - is the optimizer attempting to exploit non-physical numerical phenomena?

# Optimization: sensitivity to starting point



# Optimization: coached design iterations



# Conclusions

“Can real wind turbines generate more power than BEM-based designs predict?”

- OLAF FVW solutions discover designs that out-perform traditional BEM-optimal rotors

“Can we create optimal designs using mid-fidelity methods in the design loop?”

- FVW (OLAF) currently inconclusive as a tool for optimization: stability & smoothness concerns
- further research is necessary to enable reliable, robust FVW-in-the-loop design capabilities

# The path forward

## Goals:

- improve FVW stability
- improve gradients:
  - differentiable FVW solver?
  - gradient verification
- explore with global optimization toolset
  - verify convergence of local optimization methods
- verify physicality of optimizer-favored phenomena
  - validate optimal designs w.r.t. blade-resolved CFD & experiments
  - will FVW-optimal rotors out-perform BEM-optimal rotors in real use?



# Thank you for your attention!

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# Image sources

Betz portrait: Wikipedia,

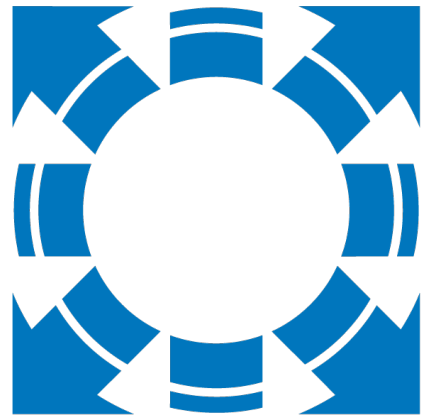
[https://en.wikipedia.org/wiki/File:Albert\\_Betz.jpg](https://en.wikipedia.org/wiki/File:Albert_Betz.jpg)

Prandtl portrait: DLR-Archiv Göttingen c/o Wikipedia,

[https://commons.wikimedia.org/wiki/File:Prandtl\\_portrait.jpg](https://commons.wikimedia.org/wiki/File:Prandtl_portrait.jpg)

OLAF/vortex method screenshots: courtesy of Emmanuel Branlard

Blade-resolved CFD screenshot: courtesy of Ganesh Vijayakumar



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