main

March 22, 2020

1 Project Introduction

This is a comprehensive data science project for the Final of WISERCLUB 2019-2020. The project is about **Business Analytics** and **Data Mining**. It consists of three parts: Part 1: Explorative Data Analysis Part 2: Data Preprocessing Part 3: Model Training and Prediction Each part has seversal problems. We have got two csv files, named *data.csv* and *holiday.csv*, derived from a new retail specialty coffee operator. The task is to use data and models to find hidden information.

1.1 Packages used in the project

pandas, numpy, matplotlib, scipy, math, datetime, sklearn, xgboost, imblearn

1.2 Methods used in the project

Aggregate Functions (groupby in Pandas), Hypothesis Testing (T test, F test), String Format, Lambda Expression, Adaboost, Random Forest, Cross Validation, Xgboost, GridSearchCV, Oversampling

Now, let's begin the exploration in the ocean of data. Since the project is very informative, you can use the contents of Jupyter Notebook to help you locate and read for convenience.

2 Part 1: Explorative Data Analysis

- 1. Find the time span of the order data.
- 2. Find the number of orders each day. a. Boss: we need to design two different strategies for sales in workdays and sales in weekends. True or False? Explain.
- 3. Find the number of users.
- 4. Find ten commodities with the highest sales and draw graphs with x-axis the commodity name and y-axis the # of orders.
- 5. Find the discount rate of each order and concat it onto the original dataset with column name *discount_rate*. You may use *pay_money*, *coffeestore_share_money*, *commodity_origin_money* and *commodity_income*.
- 6. Find the average discount of each week. One week should consist of Sunday to Saturday.

- 7. Find the *Retention Rate* of any five days. It is the ratio of users purchasing again on the next day. For example, if you want to compute the *Retention Rate* on 2019-02-10, then you need to find users who bought goods on 02-09 and 02-10.
- 8. Find the *Week Retention Rate* of any day, which means finding users buying at that day and buying again within the next seven days.
- 9. Find the *Week Retention Rate* of any day for *new users*, which means finding users buying at that day *for the first time* and buying again within the next seven days.
- 10. Find the *Retention Rate WITHIN* one week of new users. You could choose any week you want, but it must consist of Sunday to Saturday. You need to find users buying the first product and buying again within that week.
- 11. Find "Active Users" (which means the number of orders of one user is greater equal to 5).
- 12. Write the table you get in 11 as a csv file with filename *ActiveUser.csv*.
- 13. Provide a description of the number of orders for each active user (# of ActiveUser, mean, range, std, variance, skewness and kurtosis).

```
In [1]: import numpy as np
        import pandas as pd
        import matplotlib.pyplot as plt
        import matplotlib
        matplotlib.rcParams['font.family'] = 'SimHei'
In [2]: Data = pd.read_csv("data.csv", encoding = "UTF-8")
        Data.head()
Out [2]:
           Unnamed: 0 Unnamed: 0.1
                                                     phone_no
                                                               member_id \
        0
                    0
                                  0 2019-01-25 13901387938
                                                                    14442
        1
                                  1 2019-01-27 13901387938
                                                                    14442
                    1
        2
                    2
                                  2 2019-01-23 13901387938
                                                                   14442
        3
                    3
                                  3 2019-02-01 13901387938
                                                                   14442
        4
                                  4 2019-01-27 13901387938
                                                                   14442
          commodity_code commodity_name commodity_origin_money
                                                                 coupon_id \
        0
                   SP025
                                                        27.0
                                                                 7045.0
        1
                   SP209
                                NFC
                                                        24.0
                                                                    NaN
        2
                   SP025
                                                        27.0
                                                                 5589.0
        3
                   SP025
                                                        27.0
                                                                 6604.0
        4
                   SP010
                                                      27.0
                                                               6947.0
                                                              commodity_income \
           coupon_money one_category_name two_category_name
                  19.44
                                                                    7.56
        0
                   0.00
                                                                   0.00
        1
        2
                  22.14
                                                                    4.86
        3
                  19.44
                                                                    7.56
        4
                  14.04
                                                                    12.96
```

```
1
                0.00
                                           0.0
        2
                4.86
                                           0.0
        3
                7.56
                                           0.0
        4
               12.96
                                           0.0
In [3]: Holiday = pd.read_csv("holiday.csv", encoding = "UTF-8")
        Holiday.head()
Out[3]:
                   dt month
                               weekday week_of_year type
                                                            last_type \
          2017-10-09
                          10
                                     1
                                                  41
                                                          0
        0
        1 2017-10-10
                          10
                                     2
                                                   41
                                                         0
                                                                     0
        2 2017-10-11
                          10
                                     3
                                                  41
                                                         0
                                                                     0
        3 2017-10-12
                          10
                                     4
                                                  41
                                                                     0
                                                          0
        4 2017-10-13
                                     5
                                                  41
                                                                     0
                          10
           holiday_distance holiday_code
        0
                        -82
        1
                        -81
                                         0
        2
                                         0
                        -80
                        -79
                                         0
        3
        4
                                         0
                        -78
2.1 Problem 1Find the time span of the order data.
Method 1: groupby
In [4]: Data.groupby('dt')[['dt']].count().head(1)
Out [4]:
                       dt
        2019-01-20 69859
In [5]: Data.groupby('dt')[['dt']].count().tail(1)
Out [5]:
                       dt.
        dt
```

0.0

coffeestore_share_money

pay_money

2019-03-01 53279

Method 2: loop

7.56

0

The time span of the order data: 2019-01-20 to 2019-03-01

In [6]: print('The time span of the order data:',Data['dt'].min(),'to', Data['dt'].max())

2.2 Problem 2Find the number of orders each day.

The number of orders each day:

Out[7]:		daily_orders
	dt	
	2019-01-20	69859
	2019-01-21	117686
	2019-01-22	118409
	2019-01-23	126331
	2019-01-24	125764
	2019-01-25	122092
	2019-01-26	77779
	2019-01-27	66399
	2019-01-28	106025
	2019-01-29	104704
	2019-01-30	101047
	2019-01-31	97701
	2019-02-01	87458
	2019-02-02	64267
	2019-02-03	43106
	2019-02-04	7113
	2019-02-05	8516
	2019-02-06	7769
	2019-02-07	7655
	2019-02-08	7822
	2019-02-09	8452
	2019-02-10	8241
	2019-02-11	40365
	2019-02-12	43334
	2019-02-13	50789
	2019-02-14	49092
	2019-02-15	49836
	2019-02-16	29672
	2019-02-17	25179
	2019-02-18	52260
	2019-02-19	51624
	2019-02-20	53121
	2019-02-21	51817
	2019-02-22	53685
	2019-02-23	31964
	2019-02-24	27414
	2019-02-25	53969

2019-02-26	50018
2019-02-27	48970
2019-02-28	51272
2019-03-01	53279

2.2.1 Problem 2-aBoss: we need to design two different strategies for sales in workdays and sales in weekends.

Answer: True. As you can see from the data above, the orders in workdays are much greater than orders in weekends. Thus, different strategies for sales should be designed. Here are the relevant descriptive statistics and hypothesis testings.

1. Separate weekdays and weekends

```
In [8]: Holiday = Holiday[(Holiday['dt'] > '2019-01-19') & (Holiday['dt'] < '2019-03-02')] # .</pre>
        Holiday.head()
Out [8]:
                     dt month weekday week_of_year type last_type
             2019-01-20
        468
                             1
                                      7
                                                     3
                                                                      0
                                                           1
        469
             2019-01-21
                             1
                                      1
                                                     4
                                                           0
                                                                      0
                             1
                                      2
                                                     4
                                                           0
                                                                      0
        470
             2019-01-22
        471 2019-01-23
                             1
                                      3
                                                     4
                                                           0
                                                                      0
                                                           0
        472
             2019-01-24
                                      4
                                                                      0
             holiday_distance holiday_code
        468
                          -15
        469
                          -14
                                           0
        470
                          -13
                                           0
        471
                          -12
                                           0
        472
                          -11
In [9]: orders = Data.groupby('dt')[['dt']].count()
        orders.columns = ['daily_orders']
        holiday_weekday = Holiday['weekday']
        holiday_weekday = holiday_weekday.to_frame()
        holiday_weekday.index = Holiday['dt']
        holiday_weekday.columns = ['weekday']
        orders_day = pd.concat([orders, holiday_weekday], axis = 1)
        orders_day.head()
Out [9]:
                    daily_orders weekday
        dt
                                        7
        2019-01-20
                           69859
        2019-01-21
                          117686
                                        1
        2019-01-22
                          118409
                                        2
        2019-01-23
                          126331
                                        3
```

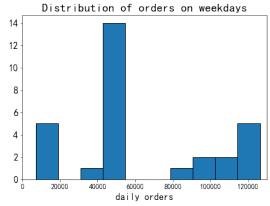
4

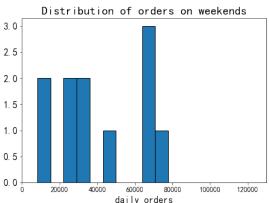
125764

2019-01-24

2. Descriptive statistics of weekdays and weekends

```
In [11]: desc_weekday = orders_weekday['daily_orders'].to_frame().describe()
         desc weekday.columns = ['daily orders weekday']
         desc_weekend = orders_weekend['daily_orders'].to_frame().describe()
         desc weekend.columns = ['daily orders weekend']
         pd.concat([desc_weekday, desc_weekend], axis = 1)
Out[11]:
                daily_orders_weekday daily_orders_weekend
                           30.000000
                                                  11.000000
         count
                        63317.433333
                                               41121.090909
         mean
         std
                        38163.933323
                                               24806.559328
         min
                         7113.000000
                                               8241.000000
         25%
                        49000.500000
                                               26296.500000
         50%
                        52038.500000
                                               31964.000000
         75%
                       100210.500000
                                               65333.000000
                       126331.000000
                                               77779.000000
         max
In [12]: plt.figure(figsize = (16,5))
         plt.subplot(1,2,1)
         plt.hist(orders_weekday['daily_orders'], edgecolor='black')
         plt.title('Distribution of orders on weekdays', fontsize = 20)
         plt.xticks(fontsize = 12)
         plt.yticks(fontsize = 16)
         plt.xlabel('daily orders', fontsize = 16)
         plt.xlim(0, 130000)
         plt.subplot(1,2,2)
         plt.hist(orders_weekend['daily_orders'], edgecolor='black')
         plt.title('Distribution of orders on weekends', fontsize = 20)
         plt.xticks(fontsize = 12)
         plt.yticks(fontsize = 16)
         plt.xlabel('daily orders', fontsize = 16)
         plt.xlim(0, 130000)
         plt.show()
```





In [13]: import matplotlib.lines as mlines

```
plt.figure(figsize = (16,5))
    plt.subplot(1,2,1)
    plt.boxplot(orders_weekday['daily_orders'], widths = 0.7, labels = ['daily orders'],
                 meanline = True, showmeans = True, medianprops = {'color': 'red', 'linewiches
    plt.title('Distribution of orders on weekdays', fontsize = 20)
    plt.ylim(0, 130000)
    plt.xticks(fontsize = 16)
    plt.yticks(fontsize = 16)
    median line = mlines.Line2D([], [], color = 'red', label = 'median')
    plt.legend(handles=[median_line], fontsize=16)
    plt.subplot(1,2,2)
    plt.boxplot(orders_weekend['daily_orders'], widths = 0.7, labels = ['daily orders'],
                 meanline = True, showmeans = True, medianprops = {'color': 'red', 'linewie
    plt.title('Distribution of orders on weekends', fontsize = 20)
    plt.ylim(0, 130000)
    plt.xticks(fontsize = 16)
    plt.yticks(fontsize = 16)
    plt.legend(handles=[median_line], fontsize = 16)
    plt.show()
       Distribution of orders on weekdays
                                              Distribution of orders on weekends
120000
                                median
                                       120000
                                                                       median
100000
                                       100000
80000
                                        80000
60000
                                        60000
```

40000

20000

0

daily orders

3. Test whether var(orders_weekday) = var(orders_weekend)

daily orders

40000

20000

0

Method 1: F Test

```
In [15]: from scipy.stats import f
                     def ftest(n1, n2, var1, var2):
                                         F test
                               F = var1 / var2
                               p_{value} = 2 * min(f.sf(F, n1-1, n2-1), 1 - f.sf(F, n1-1, n2-1))
                               print('F =',round(F, 6))
                               print('critical_region:','F <',round(f.isf(0.975, 29, 10),6),'or','F >',round(f.isf(0.975, 29, 20),6),'or','F >',round(f.isf(0.975, 29, 20),6),'or','F >',round(f.isf(0.975, 20),6),'or','F >',round(
                               if p_value < 0.05: # at the 5% signicance level
                                         print('p-value=',round(p_value, 6))
                                        print('Reject the hypothesis orders_weekday_var = orders_weekend_var.')
                                        print('Thus, orders_weekday_mean is not equal to orders_weekend_mean at 5% co
                               else:
                                        print('p-value=',round(p_value, 6))
                                        print('Accept the hypothesis orders_weekder_var = orders_weekend_var.')
                                        print('Thus, orders_weekday_mean = orders_weekend_mean at 5% confidence level
                     ftest(n1, n2, orders_weekday_var, orders_weekend_var)
F = 2.366863
critical_region: F < 0.39548 or F > 3.318587
p-value= 0.152171
Accept the hypothesis orders_weekder_var = orders_weekend_var.
Thus, orders_weekday_mean = orders_weekend_mean at 5% confidence level.
      Method 2: Levene Test
In [16]: from scipy import stats
                     Levene test: Homogeneity test of variances
                     leveneTestRes = stats.levene(orders_weekday['daily_orders'], orders_weekend['daily_orders'],
                     print('w-value=%6.4f, p-value=%6.4f' %leveneTestRes)
w-value=0.8195, p-value=0.3709
4. Test whether mean(orders_weekday) = mean(orders_weekend) Method 1: Self-defining
Two Sample T Test Function
In [17]: # two sample t test with equal variance, one-sided
                     from scipy.stats import t
```

def ttest(n1, n2, mean1, mean2, var1, var2):

```
111
                 two sample T test with equal unknown variance, one-sided
             sp2 = ((n1-1)*var1 + (n2-1)*var2)/(n1+n2-2) # sp2 = 1240813903.8532245
             T = (orders_weekday_mean - orders_weekend_mean) / ((sp2/n1+sp2/n2) ** 0.5)
             p_value = t.sf(T, n1+n2-2)
             print('T =',round(T, 6))
             print('critical_region:','T >',round(t.isf(0.05, n1+n2-2),6))
             if p_value < 0.05:</pre>
                                  # at the 5% signicance level
                 print('p-value=',round(p_value ,6))
                 print('Reject the hypothesis orders_weekday_mean = orders_weekend_mean.')
                 print('Thus, orders_weekday_mean > orders_weekend_mean at 5% confidence level
             else:
                 print('p-value=',round(p_value ,6))
                 print('Accept the hypothesis orders_weekday_mean = orders_weekend_mean.')
                 print('Thus, orders_weekday_mean = orders_weekend_mean at 5% confidence level
         ttest(n1, n2, orders_weekday_mean, orders_weekend_mean, orders_weekday_var, orders_weekday_var
T = 1.787694
critical_region: T > 1.684875
p-value= 0.040799
Reject the hypothesis orders_weekday_mean = orders_weekend_mean.
Thus, orders_weekday_mean > orders_weekend_mean at 5% confidence level.
```

Method 2: Two Sample T Test by using 'from scipy import stats'

Though we cannot reject the hyphothesis that sales in workdays and sales in weekends are different at 5% confidence level for two-sided test, we can reject it at 5% confidence level for one-sided test. Thus, the sales in weekdays are higher than sales in weekends.

From the histograms and boxplots above, it is noted that the number of some daily orders are below 20000 both on weekdays and weekends. Looking up the corresponding dates in the calendar according to the specific data we get in Problem 2, we find that the dates with orders below 20000 is during the Spring Festival of 2019.

2019-02-05	8516	2
2019-02-06	7769	3
2019-02-07	7655	4
2019-02-08	7822	5
2019-02-09	8452	6
2019-02-10	8241	7

From the table above, it can be considered that there is no difference between the number of orders on weekdays and weekends during the Spring Festival. This is a special case. However, after dropping the data during the Spring Festival, as you can see from the table and boxplots below, it is obvious that the difference between the number of orders on weekdays and weekends is significant.

```
In [20]: slice_orders_weekday = orders_weekday[orders_weekday['daily_orders'] > 20000]
         slice_orders_weekend = orders_weekend[orders_weekend['daily_orders'] > 20000]
         desc_slice_weekday = slice_orders_weekday['daily_orders'].to_frame().describe()
         desc_slice_weekday.columns = ['daily_orders_weekday']
         desc_slice_weekend = slice_orders_weekend['daily_orders'].to_frame().describe()
         desc_slice_weekend.columns = ['daily_orders_weekend']
         pd.concat([desc_slice_weekday, desc_slice_weekend], axis = 1)
Out [20]:
                daily_orders_weekday daily_orders_weekend
         count
                           25.000000
                                                   9.000000
                        74425.920000
         mean
                                               48404.333333
         std
                        31442.615071
                                               20999.623199
         min
                        40365.000000
                                               25179.000000
         25%
                        50789.000000
                                               29672.000000
         50%
                        53279.000000
                                               43106.000000
         75%
                       104704.000000
                                               66399.000000
                       126331.000000
                                              77779.000000
         max
In [21]: import matplotlib.lines as mlines
         plt.figure(figsize = (16,5))
         plt.subplot(1,2,1)
         plt.boxplot(slice_orders_weekday['daily_orders'], widths = 0.7, labels = ['daily orders']
                     meanline = True, showmeans = True, medianprops = {'color': 'red', 'linewi
         plt.title('Distribution of orders on weekdays\n(except the days during the Spring Fes
         plt.ylim(0, 130000)
         plt.xticks(fontsize = 16)
         plt.yticks(fontsize = 16)
         median_line = mlines.Line2D([], [], color = 'red', label = 'median')
         plt.legend(handles=[median_line], fontsize=16)
         plt.subplot(1,2,2)
         plt.boxplot(slice_orders_weekend['daily_orders'], widths = 0.7, labels = ['daily orders']
                     meanline = True, showmeans = True, medianprops = {'color': 'red', 'linewic
         plt.title('Distribution of orders on weekends\n(except the days during the Spring Fes
```

plt.ylim(0, 130000)

```
plt.xticks(fontsize = 16)
     plt.yticks(fontsize = 16)
     plt.legend(handles=[median_line], fontsize = 16)
     plt.show()
        Distribution of orders on weekdays
                                                         Distribution of orders on weekends
    (except the days during the Spring Festival)
                                                    (except the days during the Spring Festival)
120000
                                     median
                                                120000
                                                                                      median
100000
                                                100000
 80000
                                                 80000
 60000
                                                 60000
40000
                                                 40000
 20000
                                                 20000
                     daily orders
                                                                     daily orders
```

We can also do the hypothesis testings to verify our conclusion.

```
In [22]: n3 = len(slice_orders_weekday)
         n4 = len(slice orders weekend)
         slice_orders_weekday_mean = slice_orders_weekday['daily_orders'].mean()
         slice orders weekend mean = slice orders weekend['daily orders'].mean()
         slice_orders_weekday_var = slice_orders_weekday['daily_orders'].var()
         slice_orders_weekend_var = slice_orders_weekend['daily_orders'].var()
         print('(Except the days during the Spring Festival)')
         ftest(n3, n4, slice_orders_weekday_var, slice_orders_weekend_var)
(Except the days during the Spring Festival)
F = 2.24189
critical_region: F < 0.39548 or F > 3.318587
p-value= 0.237908
Accept the hypothesis orders_weekder_var = orders_weekend_var.
Thus, orders weekday mean = orders weekend mean at 5% confidence level.
In [23]: # two sample t test with equal variance, one-sided
         print('(Except the days during the Spring Festival)')
         ttest(n3, n4, slice_orders_weekday_mean, slice_orders_weekend_mean, slice_orders_week
(Except the days during the Spring Festival)
T = 1.956517
critical_region: T > 1.693889
p-value= 0.029589
Reject the hypothesis orders_weekday_mean = orders_weekend_mean.
```

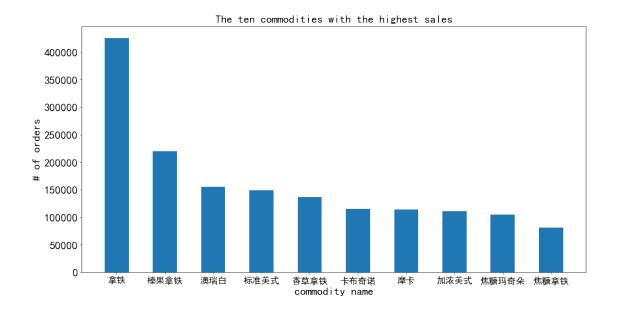
Thus, orders_weekday_mean > orders_weekend_mean at 5% confidence level.

2.3 Problem 3Find the number of users.

2.4 Problem 4Find ten commodities with the highest sales.

Draw graphs with x-axis the commodity name and y-axis the # of orders.

```
In [25]: commodities = Data.groupby('commodity_name')[['commodity_name']].count()
         commodities.columns = ['orders']
         top10_commodities = commodities.sort_values(by = ['orders'], ascending = False).head(
         print('The ten commodities with the highest sales:')
         top10_commodities
The ten commodities with the highest sales:
Out [25]:
                         orders
         commodity_name
                       425514
                     219627
                      155506
                     148666
                     136841
                     115475
                       113754
                     110526
                    105081
                      81120
In [26]: # top10_commodities.reset_index()
         top10_commodities.insert(0, 'commodity_name', top10_commodities.index)
         list_names = top10_commodities.commodity_name.tolist()
         list_sales = top10_commodities.orders.tolist()
         plt.figure(figsize = (16, 8))
         plt.bar(list_names, height = list_sales, width = 0.5)
         plt.title('The ten commodities with the highest sales', fontsize = 20)
         plt.xticks(fontsize = 16)
         plt.yticks(fontsize = 20)
         plt.xlabel('commodity name', fontsize = 20)
         plt.ylabel('# of orders', fontsize = 20)
         plt.show()
```



2.5 Problem 5Find the discount rate of each order and concat it onto the original dataset with column name *discount_rate*.

```
In [27]: discount_rate = Data.commodity_income / Data.commodity_origin_money # Series
         discount_rate = discount_rate.to_frame()
         discount_rate.columns=['discount_rate']
         Data = pd.concat([Data, discount rate], axis = 1)
         Data.head()
Out [27]:
            Unnamed: 0 Unnamed: 0.1
                                                       phone no
                                                                 member id \
                                                dt
         0
                     0
                                    0
                                       2019-01-25
                                                    13901387938
                                                                      14442
                                       2019-01-27
                                                    13901387938
                                                                      14442
         1
                      1
                                    1
         2
                     2
                                       2019-01-23
                                                    13901387938
                                                                      14442
         3
                      3
                                    3
                                       2019-02-01
                                                    13901387938
                                                                      14442
         4
                      4
                                       2019-01-27
                                                    13901387938
                                                                      14442
           commodity_code commodity_name commodity_origin_money
                                                                    coupon_id \
                    SP025
                                                          27.0
                                                                   7045.0
         0
                    SP209
                                  NFC
                                                          24.0
         1
                                                                       NaN
         2
                    SP025
                                                          27.0
                                                                    5589.0
         3
                    SP025
                                                          27.0
                                                                    6604.0
         4
                    SP010
                                                        27.0
                                                                 6947.0
                                                                commodity_income \
            coupon_money one_category_name two_category_name
                                                                       7.56
                    19.44
         0
         1
                    0.00
                                                                      0.00
         2
                   22.14
                                                                       4.86
         3
                   19.44
                                                                       7.56
```

4 14.04 12.96

	<pre>pay_money</pre>	coffeestore_share_money	discount_rate
0	7.56	0.0	0.28
1	0.00	0.0	0.00
2	4.86	0.0	0.18
3	7.56	0.0	0.28
4	12.96	0.0	0.48

2.6 Problem 6Find the average discount of each week. (One week should consist of Sunday to Saturday.)

```
In [28]: # find which seven days could be combined into one week
         holiday_day = Holiday.groupby(['week_of_year'])[['week_of_year']].count()
         holiday_day.columns = ['days']
         holiday_day
Out [28]:
                       days
         week_of_year
                          1
         3
                          7
         4
         5
         6
                          7
         7
                          7
         8
                          7
         9
In [29]: holiday_week_of_year = Holiday['week_of_year']
         holiday_week_of_year = holiday_week_of_year.to_frame()
         holiday_week_of_year.index = Holiday['dt']
         holiday_week_of_year.columns = ['week_of_year']
         discount_rate_sum = Data.groupby('dt')[['discount_rate']].sum()
         discount_rate_sum.columns = ['discount_rate_sum']
         discount = pd.concat([dt_sales, discount_rate_sum, holiday_week_of_year], axis = 1)
         discount.head()
Out [29]:
                     daily_orders discount_rate_sum week_of_year
         dt
         2019-01-20
                            69859
                                         25703.825175
                                                                  3
                                                                  4
         2019-01-21
                           117686
                                         44597.227917
                                                                  4
                                         44737.627817
         2019-01-22
                           118409
         2019-01-23
                           126331
                                         47913.169124
                                                                  4
         2019-01-24
                           125764
                                         48211.078974
```

```
discount_rate_weekly = discount_rate_weekly.to_frame()
         discount_rate_weekly.columns=['discount_rate_weekly']
         average_discount = pd.concat([average_discount, discount_rate_weekly], axis = 1)
         average_discount.rename(columns = {"daily_orders": "weekly_orders"}, inplace = True)
         average_discount
Out [30]:
                       weekly_orders discount_rate_sum discount_rate_weekly
         week_of_year
                              754460
                                           286698.672087
                                                                      0.380005
         5
                              604308
                                           241709.679206
                                                                      0.399978
         6
                               55568
                                           19649.704967
                                                                      0.353615
         7
                              288267
                                          135698.193614
                                                                      0.470738
                              321885
                                          149798.599166
                                                                      0.465379
```

discount_rate_weekly = average_discount.discount_rate_sum / average_discount.daily_ore

The average discount of each week:

2.7 Problem 7Find the *Retention Rate* of any five days. It is the ratio of users purchasing again on the next day.

Here are three methods. Method 1 is easy to figure out but it is tedious. Method 2 is an improvement on Method 1. Method 3 is is an improvement on Method 2. It is recommended and more useful.

Method 1: Compute Retention Rate of given five days directly

```
slice_0122 = slice_0122a.drop_duplicates(subset = ['member_id'], keep = 'first', inple
slice_0123 = slice_0123a.drop_duplicates(subset = ['member_id'], keep = 'first', inple
slice_0124 = slice_0124a.drop_duplicates(subset = ['member_id'], keep = 'first', inple
slice_0125 = slice_0125a.drop_duplicates(subset = ['member_id'], keep = 'first', inple
print('The retention rate of 2019-01-21 to 2019-01-25:',
    round(len(slice_0120['member_id'].loc[slice_0120['member_id'].isin(slice_0121['member_id'].ioc[slice_0121['member_id'].isin(slice_0122['member_id'].ioc[slice_0122['member_id'].isin(slice_0123['member_id'].loc[slice_0123['member_id'].isin(slice_0124['member_id'].ioc[slice_0124['member_id'].isin(slice_0125['member_id'].ioc[slice_0124['member_id'].isin(slice_0125['member_id'].loc[slice_0124['member_id'].isin(slice_0125['member_id'].ioc[slice_0124['member_id'].ioc[slice_0124['member_id'].ioc[slice_0125['member_id'].ioc[slice_0124['member_id'].ioc[slice_0124['member_id'].ioc[slice_0125['member_id'].ioc[slice_0124['member_id'].ioc[slice_0125['member_id'].ioc[slice_0124['member_id'].ioc[slice_0125['member_id'].ioc[slice_0124['member_id'].ioc[slice_0125['member_id'].ioc[slice_0124['member_id'].ioc[slice_0125['member_id'].ioc[slice_0125['member_id'].ioc[slice_0124['member_id'].ioc[slice_0125['member_id'].ioc[slice_0125['member_id'].ioc[slice_0124['member_id'].ioc[slice_0125['member_id'].ioc[slice_0124['member_id'].ioc[slice_0125['member_id'].ioc[slice_0124['member_id'].ioc[slice_0125['member_id'].ioc[slice_0125['member_id'].ioc[slice_0125['member_id'].ioc[slice_0125['member_id'].ioc[slice_0124['member_id'].ioc[slice_0125['member_id'].ioc[slice_0124['member_id'].ioc[slice_0124['member_id'].ioc[slice_0124['member_id'].ioc[slice_0124['member_id'].ioc[slice_0124['member_id'].ioc[slice_0124['member_id'].ioc[slice_0124['member_id'].ioc[slice_0124['member_id'].ioc[slice_0124['member_id'].ioc[slice_0124['member_id'].ioc[slice_0124['member_id'].ioc[slice_0124['member_id'].ioc[slice_0124['member_id'].ioc[slice_0124['member_
```

The retention rate of 2019-01-21 to 2019-01-25: 0.1523 0.2463 0.2353 0.2278 0.221

Method 2: Compute Retention Rate of given five days by using loop and 'format'

```
In [33]: slice_dt_all = [] # slice Data by dt(date)
         slice_dt_uni = [] # drop duplicates about users of slice_dt_all
         num_user_buy = [] # number of users purchasing on that day
         num_user_buy_again = [] # number of users purchasing again on the next day
         retention_rate = [] # the ratio of users purchasing again on the next day
         for j in range(6):
             # The conditions of the slice will change with the specific dates
             # We use the example 2019-01-21 to 2019-01-25
             slice_dt_all.append(Data['dt'] > '2019-01-{}'.format(j+19)) & (Data['dt'] <</pre>
             slice_dt_uni.append(slice_dt_all[j].drop_duplicates(subset = ['member_id'], keep = ['member_id']
             num_user_buy.append(len(slice_dt_uni[j]))
             if j > 0:
                 user_buy_again = slice_dt_uni[j-1].member_id.loc[slice_dt_uni[j-1].member_id.
                 num_user_buy_again.append(len(user_buy_again))
                 if num_user_buy[j-1] == 0:
                     print('There are no users purchasing again on the next day!'
                            'Thus, the retention rate of this day cannot be computed!')
                     break
                 retention_rate.append(round(num_user_buy_again[j-1] / num_user_buy[j-1], 4))
         print('The retention rate of 2019-01-21 to 2019-01-25:', ', '.join(str(i) for i in re-
The retention rate of 2019-01-21 to 2019-01-25: 0.1523, 0.2463, 0.2353, 0.2278, 0.221
```

Method 3: Compute Retention Rate of any five days by using loop and 'import datetime'

```
In [34]: import datetime

slice_dt_all = [] # slice Data by dt(date)

slice_dt_uni = [] # drop duplicates about users of slice_dt_all
```

```
num_user_buy = [] # number of users purchasing on that day
num_user_buy_again = [] # number of users purchasing again on the next day
retention_rate = [] # the ratio of users purchasing again on the next day
first_dt = input('Please enter the first day that you want to compute the retention re
date = datetime.datetime.strptime(first_dt, '%Y-%m-%d')
if date <= datetime.datetime(2019, 1, 20, 0, 0) or date > datetime.datetime(2019, 2,
    last_date = date + datetime.timedelta(days=4)
    last_dt = last_date.strftime("%Y-%m-%d")
    print('The retention rate of {} to {}'.format(first_dt, last_dt),
          'cannot be computed! Some dates are not in the time span!')
else:
    for j in range(6):
        date1 = date - datetime.timedelta(days=2)
        date2 = date
        dt1 = date1.strftime("%Y-%m-%d")
        dt2 = date2.strftime("%Y-%m-%d")
        slice_dt_all.append(Data[(Data['dt'] > dt1) & (Data['dt'] < dt2)])</pre>
        slice_dt_uni.append(slice_dt_all[j].drop_duplicates(subset = ['member_id'], k
        num_user_buy.append(len(slice_dt_uni[j])) # number of users buying on one day
        if j > 0:
            user_buy_again = slice_dt_uni[j-1].member_id.loc[slice_dt_uni[j-1].member_
            num_user_buy_again.append(len(user_buy_again)) # number of users buying a
            if num_user_buy[j-1] == 0:
                print('There are no users purchasing on the day before that day!'
                      'Thus, the retention rate of this day cannot be computed!')
                break
            else:
                retention_rate.append(round(num_user_buy_again[j-1] / num_user_buy[j-
        date = date + datetime.timedelta(days=1)
    last_date = date - datetime.timedelta(days=2)
    last_dt = last_date.strftime("%Y-%m-%d")
    if num_user_buy[j-1] == 0:
        pass
    else:
        print('The retention rate of {} to {}:'.format(first_dt, last_dt), ', '.join()
```

Please enter the first day that you want to compute the retention rate (from 2019-01-21 to 2019-01-21 to 2019-01-25: 0.1523, 0.2463, 0.2353, 0.2278, 0.221

2.8 Problem 8Find the Week Retention Rate of any day, which means finding users buying at that day and buying again within the next seven days.

Method 1: Compute Week Retention Rate of the given day directly

Method 2: Compute Week Retention Rate of any day by using 'import datetime'

```
In [36]: import datetime
                    slice_dt_all = [] # slice Data by dt(date)
                    slice_dt_uni = [] # drop duplicates about users of slice_dt_all
                    dt = input('Please enter the day that you want to compute the week retention rate (from
                    date = datetime.datetime.strptime(dt, '%Y-%m-%d')
                    if date < datetime.datetime(2019, 1, 20, 0, 0) or date > datetime.datetime(2019, 2, 2)
                             print('The week retention rate of {}'.format(dt), 'cannot be computed! Some dates
                    else:
                              # slice of that day
                             date1 = date - datetime.timedelta(days=1)
                             date2 = date + datetime.timedelta(days=1)
                             dt1 = date1.strftime("%Y-%m-%d")
                             dt2 = date2.strftime("%Y-%m-%d")
                             slice_dt_all.append(Data['dt'] > dt1) & (Data['dt'] < dt2)])</pre>
                             slice_dt_uni.append(slice_dt_all[0].drop_duplicates(subset = ['member_id'], keep = ['member_id']
                             num_user_buy = len(slice_dt_uni[0]) # number of users buying at that day
                              # slice of the next seven days
                             date3 = date
                             date4 = date + datetime.timedelta(days=8)
                             dt3 = date3.strftime("%Y-%m-%d")
                             dt4 = date4.strftime("%Y-%m-%d")
                             slice_dt_all.append(Data[(Data['dt'] > dt3) & (Data['dt'] < dt4)])</pre>
                             slice_dt_uni.append(slice_dt_all[1].drop_duplicates(subset = ['member_id'], keep = ['member_id']
                             user_buy_again = slice_dt_uni[0].member_id.loc[slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_uni[0].member_id.isin(slice_dt_u
                             num_user_buy_again = len(user_buy_again) # number of users buying again within th
                              if num_user_buy == 0:
                                       print('There are no users buying at that day!'
                                                     'Thus, the week retention rate of this day cannot be computed!')
                              else:
                                       retention_rate = round(num_user_buy_again / num_user_buy, 4)
                                      print('The week retention rate of {}:'.format(dt), retention_rate)
```

Please enter the day that you want to compute the week retention rate (from 2019-01-20 to 2019-The week retention rate of 2019-01-20: 0.5108 2.9 Problem 9Find the Week Retention Rate of any day for new users, which means finding users buying at that day for the first time and buying again within the next seven days.

Method 1: Compute Week Retention Rate of the given day for new users directly

The week retention rate of 2019-01-21 for new users: 0.6026

Method 2: Compute Week Retention Rate of any day for new users by using 'import date-time'

```
In [38]: import datetime
         slice_dt_all = [] # slice Data by dt(date)
         slice_dt_uni = [] # drop duplicates about users of slice_dt_all
         print('Please enter the day that you want to compute the week retention rate for new
         dt = input()
         date = datetime.datetime.strptime(dt, '%Y-%m-%d')
         if date < datetime.datetime(2019, 1, 20, 0, 0) or date > datetime.datetime(2019, 2, 2)
             print('The week retention rate of {} for new users'.format(dt),
                    'cannot be computed! Some dates are not in the time span!')
         else:
             # slice of that day
             date1 = date - datetime.timedelta(days=1)
             date2 = date + datetime.timedelta(days=1)
             dt1 = date1.strftime("%Y-%m-%d")
             dt2 = date2.strftime("%Y-%m-%d")
             slice_dt_all.append(Data[(Data['dt'] > dt1) & (Data['dt'] < dt2)])</pre>
             slice_dt_uni.append(slice_dt_all[0].drop_duplicates(subset = ['member_id'], keep = ['member_id']
             # slice of the next seven days
             date3 = date
             date4 = date + datetime.timedelta(days=8)
             dt3 = date3.strftime("%Y-%m-%d")
             dt4 = date4.strftime("%Y-%m-%d")
             slice_dt_all.append(Data[(Data['dt'] > dt3) & (Data['dt'] < dt4)])</pre>
```

slice_dt_uni.append(slice_dt_all[1].drop_duplicates(subset = ['member_id'], keep = ['member_id']

Please enter the day that you want to compute the week retention rate for new users (from 2019-01-21

The week retention rate of 2019-01-21 for new users: 0.6026

2.10 Problem 10Find the *Retention Rate WITHIN* one week of new users.

Method 1: Compute the Retention Rate WITHIN one given week of new users step by step

```
In [39]: # slice_0121_0127a = Data[(Data['dt'] > '2019-01-20') & (Data['dt'] < '2019-01-28')]</pre>
         \# slice_0121_0127 = slice_0121_0127a.drop_duplicates(subset = ['member_id'], keep = '.
         # new user in 2019-01-21 to 2019-01-27
         new_user = slice_0121_0127[-slice_0121_0127['member_id'].isin(slice_0120['member_id']
         slice_0121_0127_mem_dt_order = slice_0121_0127a.groupby(['member_id','dt'])['member_id','dt'])
         slice_0121_0127_mem_dt_order = slice_0121_0127_mem_dt_order.to_frame()
         slice_0121_0127_mem_dt_order.columns = [['orders']]
         slice_0121_0127_mem_dt_order.head()
Out [39]:
                               orders
         member_id dt
         1520
                                    2
                   2019-01-22
                                    2
                   2019-01-25
                                    2
         1525
                   2019-01-21
                   2019-01-25
                                    1
         1533
                   2019-01-22
                                    3
In [40]: slice_0121_0127_mem_dt_order = slice_0121_0127_mem_dt_order.reset_index()
         slice_0121_0127_mem_dt_order.index.names = ['num']
         slice_0121_0127_mem_dt_order.columns = ['member_id','dt','orders']
         slice_0121_0127_mem_dt_order.head()
Out [40]:
              member_id
                                 dt orders
         num
         0
                   1520 2019-01-22
                                           2
```

```
1
                   1520 2019-01-25
                                           2
         2
                   1525 2019-01-21
                                           2
         3
                   1525 2019-01-25
                                           1
                   1533 2019-01-22
                                           3
In [41]: slice_0121_0127_mem_dt = slice_0121_0127_mem_dt_order.groupby('member_id')[['dt']].co
         slice_0121_0127_mem_dt = slice_0121_0127_mem_dt[slice_0121_0127_mem_dt['dt'] == True]
         \#\ slice\_0121\_0127\_mem\_dt.insert(0, \ 'member\_id', \ slice\_0121\_0127\_mem\_dt.index)
         slice_0121_0127_mem_dt = slice_0121_0127_mem_dt.reset_index()
         slice_0121_0127_mem_dt.index.names = ['num']
         slice_0121_0127_mem_dt.head()
Out [41]:
              member_id
                           dt
         num
         0
                   1520 True
         1
                   1525 True
         2
                   1557 True
         3
                   1575 True
                   1613 True
In [42]: new_user_buy_again = new_user['member_id'].loc[new_user['member_id'].isin(slice_0121_e
         retention_rate_within_one_week = round(len(new_user_buy_again) / len(new_user), 4) #
         print('The retention rate within 2019-01-21 to 2019-01-27 of new users:', retention_rate
```

Method 2: Compute the Retention Rate WITHIN any week of new users by using 'import datetime'

The retention rate within 2019-01-21 to 2019-01-27 of new users: 0.3058

```
In [43]: import datetime
         def retention_rate_within_one_week_of_new_users(dt):
             slice_dt_all = []
             slice_dt_uni = []
             date = datetime.datetime.strptime(dt, '%Y-%m-%d')
              # slice of one week
             date1 = date - datetime.timedelta(days=1)
             date2 = date + datetime.timedelta(days=7)
             dt1 = date1.strftime("%Y-%m-%d")
             dt2 = date2.strftime("%Y-%m-%d")
             slice_dt_all.append(Data[(Data['dt'] > dt1) & (Data['dt'] < dt2)])</pre>
             slice_dt_uni.append(slice_dt_all[0].drop_duplicates(subset = ['member_id'], keep = ['member_id']
              # slice of old users
             date3 = date
             dt3 = date3.strftime("%Y-%m-%d")
             slice_dt_all.append(Data[Data['dt'] < dt3])</pre>
```

```
slice_dt_uni.append(slice_dt_all[1].drop_duplicates(subset = ['member_id'], keep
             # new users in this week
             new_user = slice_dt_uni[0][-slice_dt_uni[0].member_id.isin(slice_dt_uni[1].member_
             slice_week_mem_dt_order = slice_dt_all[0].groupby(['member_id','dt'])['member_id']
             slice_week_mem_dt_order = slice_week_mem_dt_order.to_frame()
             slice_week_mem_dt_order.columns = [['orders']]
             slice_week_mem_dt_order = slice_week_mem_dt_order.reset_index()
             slice_week_mem_dt_order.index.names = ['num']
             slice_week_mem_dt_order.columns = ['member_id','dt','orders']
             slice_week_mem_dt = slice_week_mem_dt_order.groupby('member_id')[['dt']].count()>
             slice_week_mem_dt = slice_week_mem_dt[slice_week_mem_dt['dt'] == True]
             slice_week_mem_dt = slice_week_mem_dt.reset_index()
             slice_week_mem_dt.index.names = ['num']
            new_user_buy_again = new_user['member_id'].loc[new_user['member_id'].isin(slice_w
             if len(new_user) == 0:
                 print('There are no new users buying this week!'
                       ' Thus, the retention rate within this week of new users cannot be comp
             retention_rate_within_one_week = round(len(new_user_buy_again) / len(new_user), 4
             date4 = date + datetime.timedelta(days=6)
             dt4 = date4.strftime("%Y-%m-%d")
             print('The retention rate within {} to {} of new users:'.format(dt, dt4), retention
In [44]: slice_Holiday = Holiday[(Holiday['dt'] > '2019-01-19') & (Holiday['dt'] < '2019-03-02</pre>
         slice_Holiday = slice_Holiday[['dt','weekday', 'week_of_year']]
        pd.pivot_table(slice_Holiday, index = 'week_of_year', columns = 'weekday', aggfunc = :
Out [44]:
                               dt
                                            2
                                                        3
                                                                                5
        weekday
                                1
        week_of_year
         3
         4
                       2019-01-21 2019-01-22 2019-01-23 2019-01-24 2019-01-25
        5
                       2019-01-28 2019-01-29 2019-01-30 2019-01-31 2019-02-01
        6
                       2019-02-04 2019-02-05 2019-02-06 2019-02-07 2019-02-08
        7
                       2019-02-11 2019-02-12 2019-02-13 2019-02-14 2019-02-15
        8
                       2019-02-18 2019-02-19 2019-02-20 2019-02-21 2019-02-22
        9
                       2019-02-25 2019-02-26 2019-02-27 2019-02-28 2019-03-01
        weekday
                                6
                                            7
        week_of_year
                                   2019-01-20
         3
```

```
4
                       2019-01-26 2019-01-27
         5
                       2019-02-02 2019-02-03
                       2019-02-09 2019-02-10
         6
         7
                       2019-02-16 2019-02-17
                       2019-02-23 2019-02-24
         8
                                0
In [45]: week_num = input('Please enter the week of year (from 4 to 8): ')
         week_num = eval(week_num)
         if type(week_num) == int:
             if week_num < 4 or week_num > 8:
                 print('The retention rate within this week of new users cannot be computed! So
             else:
                 dt = '2019-01-21'
                 for j in range (4, 9):
                     if week_num == j:
                         retention_rate_within_one_week_of_new_users(dt)
                         break
                     else:
                         date = datetime.datetime.strptime(dt, '%Y-%m-%d')
                         date = date + datetime.timedelta(days=7)
                         dt = date.strftime("%Y-%m-%d")
                         i += 1
         else:
             print('Please enter the correct digit format!')
Please enter the week of year (from 4 to 8): 4
The retention rate within 2019-01-21 to 2019-01-27 of new users: 0.3058
```

Note: The retention rate within the 7^{th} week (2019-02-11 to 2019-02-17) or 8^{th} week (2019-02-18 to 2019-02-24) of 2019 of new users cannot be computed since there are no new users that week.

2.11 Problem 11Find "Active Users" (which means the number of orders of one user is greater equal to 5).

2.12 Problem 12Write the table you get in 11 as a csv file with filename *ActiveUser.csv*.

```
In [47]: active_users.to_csv('ActiveUser.csv')
```

2.13 Problem 13Provide a description of the number of orders for each active user (# of ActiveUser, mean, range, std, variance, skewness and kurtosis).

```
In [48]: # # The number of ActiveUser is 166308
         # len(active users.drop duplicates(subset = ['member id'], keep = 'first', inplace = .
         # from numpy import mean, ptp, var, std
         # print(mean(active_user_order), ptp(active_user_order), var(active_user_order), std(
In [49]: active_user_order = active_users.groupby('member_id')[['commodity_name']].count()
         active_user_order.columns = ['orders']
         active user order.head()
Out [49]:
                    orders
         member id
         1525
                         7
         1533
                        12
         1557
                        50
         1574
                        24
         1575
                       139
In [50]: active_user_order.describe()
Out [50]:
                       orders
         count
                166308.000000
                    10.418188
         mean
                     7.599244
         std
         min
                     5.000000
         25%
                     6.000000
         50%
                     8.000000
         75%
                    12.000000
         max
                   585.000000
In [51]: print('# of ActiveUser:',int(active_user_order.count()))
         print('mean:', round(float(active_user_order.mean()), 6))
         print('range:', int(active_user_order.max()-active_user_order.min()))
         print('std:', round(float(active_user_order.std()), 6))
         print('variance:', round(float(active_user_order.var()), 6))
         print('skewness:', round(float(active_user_order.skew()), 6))
         print('kurtosis:', round(float(active_user_order.kurt()), 6))
# of ActiveUser: 166308
mean: 10.418188
range: 580
std: 7.599244
variance: 57.748512
skewness: 6.542469
kurtosis: 241.357987
```

3 Part 2: Data Preprocessing

- 1. Remove the first column of the data in *data.csv*, because it is just a copy of index.
- 2. Boss: To implement Collaborative Filtering in recommendation systems, we need a user-item table to show the number of orders for each user and each item. Try to construct *user-item* table. An example of user-item pair: (Phone_No,)
- 3. Boss: Life is not like a Markov Chain, which means everyone's past behavior is correlated with his present one.

And that is why we could exploit past purchase behavior to predict their future buying trends. Try to construct a dataset to show this past purchasing behavior trend. For convenience, several instructions are proposed as follows a. Two days correspond to one dimension. b. The last two days of the time span of the data should be the *future*, which means it corresponds to the *target* field for the

following data mining models. c. The length of each user vector must be maximized. d. The dataset should be a DataFrame in Pandas, so you could customize the columns as you wish. For example, if the time span is from 2019-02-01 to 2019-02-10, then there are 10 days altogether. So each user corresponds to

a 5-dimensional vector, with 4 features and 1 target dimension. The vector [4, 0, 0, 0, 1] means this user bought one good

between 02-09 and 02-10, and four goods between 02-01 and 02-02. Additionally, the length of each user vector MUST BE 5

because of the rule c.

3.1 Problem 1Remove the first column of the data in data.csv, because it is just a copy of index.

```
In [52]: # Data.columns
         Data.drop(['Unnamed: 0'], axis = 1, inplace = True)
         Data.head()
Out [52]:
                                                  member_id commodity_code
            Unnamed: 0.1
                                         phone_no
         0
                         2019-01-25
                                      13901387938
                                                        14442
                                                                       SP025
                       1 2019-01-27 13901387938
                                                        14442
                                                                       SP209
         1
         2
                       2 2019-01-23 13901387938
                                                        14442
                                                                       SP025
                       3 2019-02-01 13901387938
         3
                                                        14442
                                                                       SP025
                       4 2019-01-27 13901387938
                                                        14442
                                                                       SP010
           commodity_name
                          commodity_origin_money
                                                   coupon_id
                                                               coupon_money \
         0
                                         27.0
                                                   7045.0
                                                                  19.44
                  NFC
                                         24.0
                                                                   0.00
         1
                                                     NaN
         2
                                         27.0
                                                  5589.0
                                                                  22.14
         3
                                         27.0
                                                  6604.0
                                                                  19.44
                                                                14.04
         4
                                       27.0
                                                6947.0
                                               commodity_income pay_money \
           one_category_name two_category_name
                                                       7.56
                                                                  7.56
         1
                                                      0.00
                                                                 0.00
```

2			4.86	4.86
3			7.56	7.56
4			12.96	12.96
	coffeestore_share_money	discount_rate		
0	0.0	0.28		
1	0.0	0.00		
2	0.0	0.18		
3	0.0	0.28		
4	0.0	0.48		

3.2 Problem 2

Boss: To implement Collaborative Filtering in recommendation systems, we need a user-item table to show the number of orders for each user and each item. Try to construct *user-item* table. An example of user-item pair: (Phone_No,)

In [53]: slice_user_item = Data[['Unnamed: 0.1', 'phone_no', 'commodity_name']]

```
# slice_user_item.rename(columns={'Unnamed: 0.1': 'orders'}, inplace = True)
         slice_user_item.columns = ['orders', 'phone_no', 'commodity_name']
         user_item_table = pd.pivot_table(slice_user_item, index = 'phone_no', columns = 'comm')
                                              aggfunc = len, fill_value = 0)
In [54]: user_item_table.head() # len(user_item_table)=466886
Out [54]:
                           orders
         commodity_name NFC NFC NFC NFC NFC 330ml
         phone_no
         51379898
                                0
                                          0
                                                       0
                                                                  0
                                                                                             0
         57047978
                                0
                                          0
                                                       0
                                                                 0
                                                                                 0
                                                                                             0
                                0
         61120518
                                          0
                                                       0
                                                                 0
                                                                                 0
                                                                                             0
         62288158
                                0
                                          0
                                                       0
                                                                 0
                                                                                             0
                                                                                 1
         64618166
                                0
                                          0
                                                       0
                                                                  0
                                                                                 0
                                                                                             0
                                                       . . .
         commodity_name
         phone_no
         51379898
                             0
                                   0
                                           0
                                                                  0
                                                                          0
                                                                                0
                                                                                       0
                                                                                             0
         57047978
                             0
                                   0
                                           0
                                                   0
                                                                  0
                                                                          0
                                                                                0
                                                                                       0
                                                                                             0
         61120518
                             0
                                   0
                                           0
                                                   0
                                                                  0
                                                                          0
                                                                                0
                                                                                       0
                                                                                             0
                             0
                                           0
                                                                  0
                                                                          0
                                                                                0
                                                                                             0
         62288158
                                   0
                                                   0
                                                                                       0
         64618166
                             0
                                   0
                                           0
                                                                 0
                                                                                0
                                                                                             0
         commodity_name
         phone_no
         51379898
                               0
                                      0
                                                  0
                                                        0
                                                                0
         57047978
                               0
                                      0
                                                         0
                                                                0
```

3.3 Problem 3

Boss: Life is not like a Markov Chain, which means everyone's past behavior is correlated with his present one. And that is why we could exploit past purchase behavior to predict their future buying trends. Try to construct a dataset to show this past purchasing behavior trend.

```
In [55]: import math
        print('The length of each user vector:', math.floor(len(orders)/2)) # len(order) = 41
The length of each user vector: 20
In [56]: slice_0121_0301 = Data[Data['dt'] > '2019-01-20']
         slice_user_date = slice_0121_0301[['Unnamed: 0.1', 'phone_no', 'dt']]
         # slice_user_date.rename(columns={'Unnamed: 0.1': 'orders'}, inplace = True)
         slice_user_date.columns = ['orders', 'phone_no', 'dt']
         slice_user_date.head()
Out [56]:
           orders
                       phone_no
                                         dt
        0
                0 13901387938 2019-01-25
         1
                 1 13901387938 2019-01-27
         2
                 2 13901387938
                                2019-01-23
         3
                 3 13901387938 2019-02-01
                 4 13901387938 2019-01-27
```

The following function is used to make two days correspond to one dimension.

```
else:
                     j += 1
             return period
In [58]: dim = slice_user_date.dt.apply(lambda x: determine_period(x))
         dim = dim.to_frame()
         dim.columns=['period']
         slice_user_date = pd.concat([slice_user_date, dim], axis = 1)
         slice_user_date.drop(['dt'], axis = 1, inplace = True)
         slice_user_date.head()
Out [58]:
            orders
                       phone_no period
                 0 13901387938
         0
         1
                                      4
                 1 13901387938
         2
                                      2
                 2 13901387938
                 3 13901387938
                                      6
                 4 13901387938
                                      4
In [59]: user_date_table = pd.pivot_table(slice_user_date, index = 'phone_no', columns = 'peri-
         user_date_table.head()
Out [59]:
                  orders
                                        7 8 9 10 11 12 13 14 15 16 17 18 19 20
         period
                                 5
                                     6
         phone_no
         51379898
                             0
                                1
                                   0
                                      0
                                         0
                                            0
                                                0
                                                   0
                                                      0
                                                         0
                                                            0
                                                               0
                                                                  0
                                                                     0
                                                                        0
                                                                           0
         62288158
                         0
                             0
                                0
                                   1
                                      0
                                         0
                                            0
                                                0
                                                   0
                                                      1
                                                         0
                                                            1
                                                               0
                                                                  0
                                                                     1
                                                                        1
         65310185
                       1
                         0
                             0 0
                                   0
                                      0
                                         0
                                            0
                                                0
                                                   0
                                                     0
                                                         0
                                                            0
                                                               0
                                                                  1
                                                                     0
                                                                        0
                                                                           0
         67443044
                       0 0 1
                                0
                                      0
                                         0
                                            0
                                               0
                                                  0
                                                     0
                                                                     0
                                   0
                                                         0
                                                            0
                                                               0
                                                                  0
                                                                        0
                                                                           0
                                                                             0 0
                                                0
                                                   0
         67469370
                                   0
                                            0
                                                     0
                                                         0
                                                            0
                                                               0
                                                                  0
```

4 Part 3: Model Training and Prediction

Boss: For the target field, 1 means he purchased in the future and 0 means he did not. Then you could use traditional classification algorithms to predict the future behaviors of all users.

- 1. Transform the data you got from the last section into an array in Numpy.
- 2. Split the data into features X and targets Y.
- 3. Use *Adaboost*, *Random Forest* in Sklearn to construct the model for prediction with 3-fold cross validation
 - a. (Optional) Use *Xgboost*. b. Boss: Please do not use *Naive-Bayes* or *Support Vector Machine* in this project. True or False? Explain.
- 4. Tune your model and report the best metrics you could get for your model and the corresponding confusion matrix and model name. At least Adaboost and Random Forest should be used for tuning. Here are some suggestions.
 - a. Try to do oversampling or undersampling. This is an imbalanced classification problem.

b. Change the parameters of each model (e.g. *scale_pos_weight* in *Xgboost* and probability threshold), more information could

be found in the Official Documentations. c. Accuracy is not suitable to be an evaluation metric in this case. Use F1-measure. d. Try to not record the # of orders for each user. Record whether he bought the goods instead, 1 if he bought and 0 otherwise. e. Try to record the active-user feature. Many users did not only buy one cup of drink during two days, so whether one user is

active should be taken into consideration. f. Try to split the data with respect to Workdays and Weekends and train two different models. If that is the best choice, then

you should report two metrics, one for Workdays Model and the other one for Weekends Model.

5. After tuning, try to explain why your model works better.

4.1 Problem 1Transform the data you got from the last section into an array in Numpy.

```
In [60]: dataset = np.array(user_date_table) # user_date_table.values
```

4.2 Problem 2Split the data into features X and targets Y.

Boss: For the target field, 1 means he purchased in the future and 0 means he did not. Then you could use traditional classification algorithms to predict the future behaviors of all users.

4.3 Problem 3Use Adaboost, Random Forest in Sklearn to construct the model for prediction with 3-fold cross validation.

```
In [65]: from sklearn.model_selection import train_test_split

X_train, X_test, y_train, y_test = train_test_split(X, y, random_state = 42) # test_s
```

Adaboost

0

0.90

0.97

```
In [66]: from sklearn.metrics import classification_report
         from sklearn.ensemble import AdaBoostClassifier
         from sklearn.model_selection import cross_val_score
         AdaBoost_clf = AdaBoostClassifier(n_estimators = 10)
                                                                # default # of weak classifie
         AdaBoost_clf.fit(X_train, y_train)
         y_prediction = AdaBoost_clf.predict(X_test)
         print('Train score: {:.3f}'.format(AdaBoost_clf.score(X_train, y_train)))
         print('Test score: {:.3f}'.format(AdaBoost_clf.score(X_test, y_test)))
         print(classification_report(y_test, y_prediction))
Train score: 0.888
Test score: 0.887
                          recall f1-score
              precision
                                              support
           0
                   0.90
                             0.98
                                       0.94
                                                99407
           1
                   0.62
                             0.25
                                       0.35
                                                14217
                                       0.89
                                               113624
   accuracy
  macro avg
                             0.61
                                       0.65
                                               113624
                   0.76
weighted avg
                   0.87
                             0.89
                                       0.86
                                               113624
In [67]: # 3-fold cross validation
         acc_scores = cross_val_score(AdaBoost_clf, X_train, y_train, cv = 3) # model, raw_dat
         print(acc_scores) # accuracy
[0.88711892 0.88814863 0.88802542]
  Random Forest
In [68]: from sklearn.ensemble import RandomForestClassifier
         random_forest_clf = RandomForestClassifier()
         random_forest_clf.fit(X_train, y_train)
         y_prediction = random_forest_clf.predict(X_test)
         print('Train score: {:.3f}'.format(random_forest_clf.score(X_train, y_train)))
         print('Test score: {:.3f}'.format(random_forest_clf.score(X_test, y_test)))
         print(classification_report(y_test, y_prediction))
Train score: 0.952
Test score: 0.879
              precision recall f1-score
                                              support
```

0.93

99407

```
1
                   0.54
                             0.24
                                       0.33
                                                14217
                                       0.88
                                               113624
   accuracy
                   0.72
                                       0.63
                                               113624
  macro avg
                             0.60
weighted avg
                   0.85
                             0.88
                                       0.86
                                               113624
In [69]: # 3-fold cross validation
        acc_scores = cross_val_score(random_forest_clf, X_train, y_train, cv = 3) # model, ra
        print(acc_scores) # accuracy
[0.87932127 0.87910125 0.88008695]
4.3.1 Problem 3-aXgboost
In [70]: import xgboost as xgb
        from xgboost import XGBClassifier
        from sklearn.metrics import accuracy_score
        from sklearn import metrics
        dtrain = xgb.DMatrix(X_train, label = y_train)
         dtest = xgb.DMatrix(X_test, label = y_test)
        params={'booster':'gbtree', 'max_depth': 2, 'eta': 1, # Booster parameters: max_de
                 'objective': 'binary:logistic', # objective [ default=reg:linear], logistic r
                 'eval_metric': 'auc', # The evaluation index needed to verify the data, auc:
                                       #'nthread': 4, # of CPU threads
                 'lambda': 0, # [default=0], L2 regular penalty coefficient, the larger the pa
                               # alpha [default=0], L1 regular penalty coefficient, can make t
                 'subsample': 1, # subsample [default=1], random sampling of training samples
                 'colsample_bytree': 1, # colsample_bytree [default=1], the proportion of rand
                 'min_child_weight': 2,  # min_child_weight [default=1], max_delta_step [defau
                 'seed': 0} # seed [default=0]
        num_round = 10
        bst1 = xgb.train(params, dtrain, num_round)
        train_pred = bst1.predict(dtrain)
```

y_prediction = (y_pred >= 0.5)*1 # let 0.5 be the threshold

train_prediction = (train_pred >= 0.5)*1 # let 0.5 be the threshold

print('Train accuracy: {:.3f}'.format(accuracy_score(y_train, train_prediction)))
print('Test accuracy: {:.3f}\n'.format(accuracy_score(y_test, y_prediction)))

y_pred = bst1.predict(dtest)

```
print(classification_report(y_test, y_prediction))

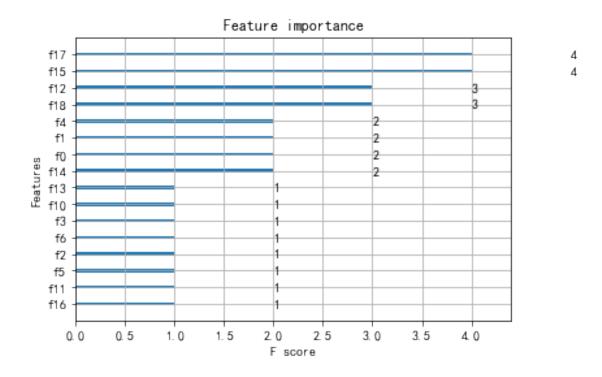
confusion_matrix = pd.DataFrame(metrics.confusion_matrix(y_test, y_prediction))
confusion_matrix.columns = ['not buy [0]', 'buy [1]']
confusion_matrix.index = ['predict not buy [0]', 'predict buy [1]']
print('confusion matrix:\n', confusion_matrix)
```

Train accuracy: 0.888
Test accuracy: 0.888

	precision	recall	f1-score	support
0	0.90	0.98	0.94	99407
1	0.64	0.24	0.35	14217
accuracy			0.89	113624
macro avg	0.77	0.61	0.64	113624
weighted avg	0.87	0.89	0.87	113624

confusion matrix:

not buy [0] buy [1]
predict not buy [0] 97437 1970
predict buy [1] 10773 3444



```
In [72]: bst2 = XGBClassifier(max_depth = 2, n_estimators = num_round, silent = True, objective
         bst2.fit(X_train, y_train)
         train_prediction = bst2.predict(X_train)
         y_prediction = bst2.predict(X_test)
         print('Train accuracy: {:.3f}'.format(accuracy_score(y_train, train_prediction)))
         print('Test accuracy: {:.3f}\n'.format(accuracy_score(y_test, y_prediction)))
         print(classification_report(y_test, y_prediction))
         confusion_matrix = pd.DataFrame(metrics.confusion_matrix(y_test, y_prediction))
         confusion_matrix.columns = ['not buy [0]', 'buy [1]']
         confusion_matrix.index = ['predict not buy [0]', 'predict buy [1]']
         print('confusion matrix:\n ', confusion_matrix)
         # 3-fold cross validation
         acc_scores = cross_val_score(bst2, X_train, y_train, cv = 3)
         print('\n3-fold cross validation:')
         print(acc_scores)
Train accuracy: 0.888
Test accuracy: 0.887
              precision
                           recall f1-score
                                              support
           0
                   0.89
                             0.99
                                       0.94
                                                99407
                   0.70
                             0.17
                                       0.27
           1
                                                 14217
                                       0.89
                                               113624
    accuracy
  macro avg
                   0.80
                             0.58
                                       0.61
                                                113624
weighted avg
                   0.87
                             0.89
                                       0.86
                                               113624
confusion matrix:
                       not buy [0]
                                    buy [1]
predict not buy [0]
                           98358
                                     1049
predict buy [1]
                           11795
                                     2422
```

4.3.2 Problem 3-b

3-fold cross validation:

[0.88766458 0.88846547 0.88833345]

Boss: We could, but we do not use Naive Bayes or Support Vector Machine in this project. **Answer:** True. Reasons are as follows.

Why do we not use Naive Bayes in this project? Because Naive Bayes model assumes that attributes are independent from each other, this assumption is often not valid in practical applications. When the correlation between attributes is large, the result of classification is not good. In this project, whether the users will purchased in the future is correlated with their past behaviors. Meanwhile, we need to know the prior probability, which usually depends on the assumption.

Why do we not use Support Vector Machine in this project? If we use linear SVM, the data of users' purchasing behavior may be linearly indivisible. If we use kernel trick, it may be overfitting. Moreover, finding the best model requires us to test different combinations of kernel functions and model parameters. When the sample data is very large, the process of training is very time-consuming, which will also consume a lot of memory.

4.4 Problem 4Tune your model and report the best metrics you could get for your model and the corresponding confusion matrix and model name. At least Adaboost and Random Forest should be used for tuning.

d. Try to not record the # of orders for each user. Record whether he bought the goods instead, 1 if he bought and 0 otherwise.

a. Try to do oversampling or undersampling. This is an imbalanced classification problem.

4.4.1 To be continued...

Random Forest

```
In [77]: from sklearn.model_selection import GridSearchCV, RandomizedSearchCV
        from sklearn.metrics import f1_score
         # default model
         # n_estimators = 10, criterion='gini', max_depth = None, min_samples_split = 2, min_s
         # max features = 'auto', max leaf nodes = None, min impurity decrease = 0.0, min impu
         # bootstrap = True, oob_score = False, n_jobs = 1, random_state = None, verbose = 0,
        random_forest_clf = RandomForestClassifier()
        param_test = {'n_estimators': list(range(5, 16))}
        clf = GridSearchCV(random_forest_clf, param_grid = param_test, scoring = 'f1', cv = 3
        clf.fit(X_train, y_train)
        y_preds = clf.predict(X_test)
        test_f1 = f1_score(y_test, y_preds)
        print('f1 scoce: {:.3f}'.format(test_f1))
        print('confusion matrix:\n', metrics.confusion_matrix(y_test, y_preds))
        print('The best f1 score: {:.3f}'.format(clf.best_score_))
        print('The best measure', clf.best_estimator_) # get the classification model for th
f1 scoce: 0.333
confusion matrix:
 [[96645 2762]
 [10823 3394]]
The best f1 score: 0.333
The best measure RandomForestClassifier(bootstrap=True, ccp_alpha=0.0, class_weight=None,
                       criterion='gini', max_depth=None, max_features='auto',
                      max_leaf_nodes=None, max_samples=None,
```

min_impurity_decrease=0.0, min_impurity_split=None,

```
min_samples_leaf=1, min_samples_split=2,
min_weight_fraction_leaf=0.0, n_estimators=13,
n_jobs=None, oob_score=False, random_state=None,
verbose=0, warm_start=False)
```

Xgboost

```
In [78]: from sklearn.model_selection import GridSearchCV, RandomizedSearchCV
         from sklearn.metrics import f1_score
         # params = {'max_depth': 2, 'eta': 0.1, 'silent': 1, 'objective': 'binary:logistic' }
         bst = XGBClassifier(max_depth = 2, learning_rate = 0.1, silent = True, objective = 'b
         param_test = {'n_estimators': list(range(100, 141, 1))}
         clf = GridSearchCV(estimator = bst, param_grid = param_test, scoring = 'f1', cv = 3)
         clf.fit(X_train, y_train)
         y_preds = clf.predict(X_test)
         test_f1 = f1_score(y_test, y_preds)
         print('f1 scoce: {:.3f}'.format(test_f1))
         print('confusion matrix:\n', metrics.confusion_matrix(y_test, y_preds))
         print('The best f1 score: {:.3f}'.format(clf.best_score_))
         print('The best measure', clf.best_estimator_) # get the classification model for th
f1 scoce: 0.336
confusion matrix:
 [[97667 1740]
 [11000 3217]]
The best f1 score: 0.341
The best measure XGBClassifier(base_score=0.5, booster=None, colsample_bylevel=1,
              colsample_bynode=1, colsample_bytree=1, gamma=0, gpu_id=-1,
              importance_type='gain', interaction_constraints=None,
              learning_rate=0.1, max_delta_step=0, max_depth=2,
              min_child_weight=1, missing=nan, monotone_constraints=None,
              n_estimators=137, n_jobs=0, num_parallel_tree=1,
              objective='binary:logistic', random_state=0, reg_alpha=0,
              reg_lambda=1, scale_pos_weight=1, silent=True, subsample=1,
              tree_method=None, validate_parameters=False, verbosity=None)
```

e. Try to record the active-user feature. Many users did not only buy one cup of drink during two days, so whether one user is active should be taken into consideration.

```
62288158
                   0 0
                         0
                                   0
                                      0
                                                                                      0
                            0
                                1
                                         0
                                                0
                                                     1
                                                         0
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In [80]: active_state = user_date_table_temp.index.isin(active_users['phone_no']) # array of T
         active_state = active_state.astype(int) # array of 1 and 0
         active_state = pd.DataFrame(active_state, index = user_date_table.index, columns = ['
         user_date_active_table = pd.concat([active_state, user_date_table_temp], axis = 1)
         user_date_active_table.head()
Out[80]:
                                                   7
                                                     8 9 ...
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                   active-user 1 2 3 4 5 6
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         [5 rows x 21 columns]
In [81]: dataset_new = np.array(user_date_active_table)
In [82]: X, Y = dataset_new[:,0:20], dataset_new[:,20]
In [83]: y = Y
         X[X > 0] = 1
         y[y > 0] = 1
In [84]: X
Out[84]: array([[0, 0, 0, ..., 0, 0, 0],
                [1, 0, 0, \ldots, 1, 0, 0],
```

```
[0, 1, 0, ..., 0, 0, 0],
...,
[1, 0, 1, ..., 0, 0, 0],
[0, 0, 0, ..., 0, 0, 0],
[0, 0, 0, ..., 0, 0, 0]], dtype=int64)

In [85]: y

Out[85]: array([0, 1, 0, ..., 1, 0, 0], dtype=int64)
```

4.4.2 To be continued...

f. Split the data with respect to Weekdays and Weekends and train two different models.

4.4.3 To be continued...

4.5 Problem 5After tuning, try to explain why your model works better.

Hint: For every case you try in Problem 4, please record the result and the trend. Does the model behave better or worse? The performances will show you the hidden information of the data and you could use business intuition to explain the phenomenons. That is the answer of Problem 5.

4.5.1 To be continued...

Indeed, tuning models is the most difficult problem of this project and it is very time-consuming since there are many cases for us to consider. Frankly speaking, I am not very familiar with some models and I still have a long way to go.