

# Exploratory Data Analysis

Introduction to Data Analysis with Python - Spring Semester 2026

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# Table of Contents

1. Exploratory Data Analysis
  - 1.1 Summary Statistics
    - Central Tendency
    - Spread
2. Graphical Exploratory Data Analysis
3. Multivariate Non-Graphical Data Analysis
4. Multivariate Graphical Exploratory Data Analysis
5. Conclusion

# Exploratory Data Analysis

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# What is Exploratory Data Analysis?

## Definition

**Exploratory Data Analysis (EDA)** is the process of visually and statistically examining datasets to uncover patterns, spot anomalies, test hypotheses, and check assumptions using summary statistics and graphical representations.

## Goals of EDA:

- Understand data structure and distributions, thus uncovering relationships between variables
- Detect outliers and missing values
- Formulate and test hypotheses
- Guide the choice of applicable models

# Types of EDA

There are 4 types of EDA:

- **Non-graphical**: it consists of **summary statistics**.
- **Graphical**: summarizing data properties in a **diagrammatic or pictorial** way.
- **Univariate**: takes only **one variable** into account.
- **Multivariate**: takes into account **multiple variables and their relation**.

*This part of the presentation greatly follows the contents of the [Stanford lecture about EDA](#), which I recommend reading.*

# Population vs Sample – Overview

## Key Idea:

- **Population:** Entire set of data or subjects you want to study.
- **Sample:** A subset of the population used to make estimates.

The values for the **population** are usually unavailable, hence the necessity of analyzing it through the **samples**.

**Quick Tip:** Population = everyone, Sample = some of them

## Attention!

Always distinguish between population and sample. Using the wrong formulas can lead to incorrect analysis results!

# Exploratory Data Analysis

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## Summary Statistics

# Central Tendency

## Definition

The **central tendency** measures attempt to describe a datasets with a value that represents the centre of its distribution.

- Common measures of central tendency:
  - **Mean** – Arithmetic average
  - **Median** – Middle value
  - **Mode** – Most frequent value

# Mean (Arithmetic Average)

- Represents the central value of the dataset.

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

- $\bar{x}$ : Sample mean
- $x_i$ : Individual value
- $n$ : Total number of observations
- Sum of all of the data values divided by the number of values

## Mean: Example

**Dataset:**

$$x = [2, 4, 4, 6, 8, 10, 10, 10]$$

**Mean:**

$$\text{Mean} = \frac{\sum x_i}{n} = \frac{2 + 4 + 4 + 6 + 8 + 10 + 10 + 10}{8} = \frac{54}{8} = 6.75$$

# Median

- The middle value when data is sorted.
- Not sensitive to outliers.

$$\text{Median} = \begin{cases} x_{\frac{n+1}{2}}, & \text{if } n \text{ is odd} \\ \frac{1}{2}(x_{\frac{n}{2}} + x_{\frac{n}{2}+1}), & \text{if } n \text{ is even} \end{cases}$$

## Median: Example

**Dataset:**

$$x = [2, 4, 4, 6, 8, 10, 10, 10]$$

**Median:** - Sorted data: [2, 4, 4, 6, 8, 10, 10, 10] - Number of points  
 $n = 8$  (even), median = average of 4th and 5th values:

$$\text{Median} = \frac{6 + 8}{2} = 7$$

# Mode

- The **mode** is the value that appears most frequently in the dataset.
- A dataset can have one mode (unimodal), more than one (multimodal), or none.

## Mode: Example

**Dataset:**

$$x = [2, 4, 4, 6, 8, 10, 10, 10]$$

**Mode:** - Most frequent value(s): 10

$$\text{Mode} = 10$$

# Spread

## Definition

The **spread** is an indicator of how far away from the center we are still likely to find data values.

- Common measures of spread:
  - Variance
  - Standard Deviation
  - Interquartile range

# Unbiasedness

**Unbiasedness:** when calculated for many different random samples from the same population, the average should match the corresponding population quantity. Therefore, when calculating spread metrics for a **sample** and not for the whole population, the denominator will be different.

- $n - 1$  instead of  $n$  for **variance** and **standard deviation**
- For other metrics, unbiaseding can be more complicated - in any case, **we do not delve into the mathematical details of unbiasedness in this class!**

# Variance

**Variance:**

$$s^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$$

- Measures **average squared distance** of data from the mean.

# Standard Deviation

## Standard Deviation:

$$s = \sqrt{\frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2}$$

- Square root of the variance.
- It expresses **distance from the mean**, but it is in the same units as the data.
- Commonly used to express data dispersion, and useful to detect **outliers**.

# Interquartile Range (IQR)

**Range:**

$$\text{Range} = \max(x) - \min(x)$$

**Interquartile Range:**

$$\text{IQR} = Q_3 - Q_1$$

- Range of the middle 50% of the data.
- $Q_1$ : 25th percentile,  $Q_3$ : 75th percentile
- Because the values in the top and bottom quarter of the data can be moved without influencing IQR, IQR is very **robust** against outliers.  
This is not true for range, which can **drastically change** if the analyzed sample changes!
- Useful for detecting outliers.

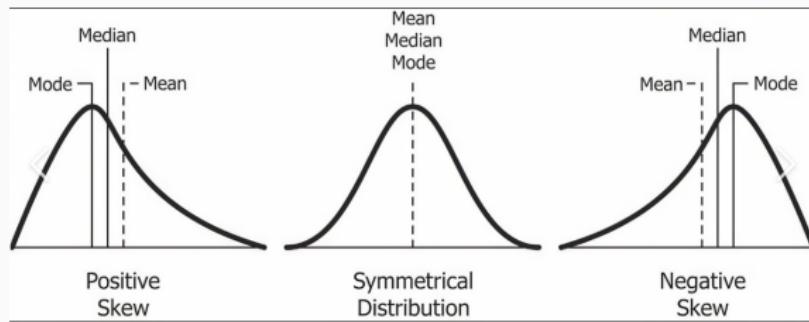
# Skewness

$$\text{Skewness} = \frac{1}{n} \sum_{i=1}^n \left( \frac{x_i - \bar{x}}{s} \right)^3$$

- You start by the **mean** ( $\bar{x}$ ) and **standard deviation** ( $s$ ) of your dataset; the computed values are divided by the **population size**.
- Measures **asymmetry** of the data distribution.
- In simplified terms, you can think of it as a measure that tells you if the data is "**leaning**" towards one side.
- Positive: right-skewed, Negative: left-skewed

The above formula refers to **population**. As the purpose of this class is for you to understand the **theory** behind summary statistics, we will not delve into the details of unbiasedness.

# Skewness: Example



**Figure 1:** Example of left- and right-skewness.

Source: [Analytics Vidhya](#)

# Kurtosis

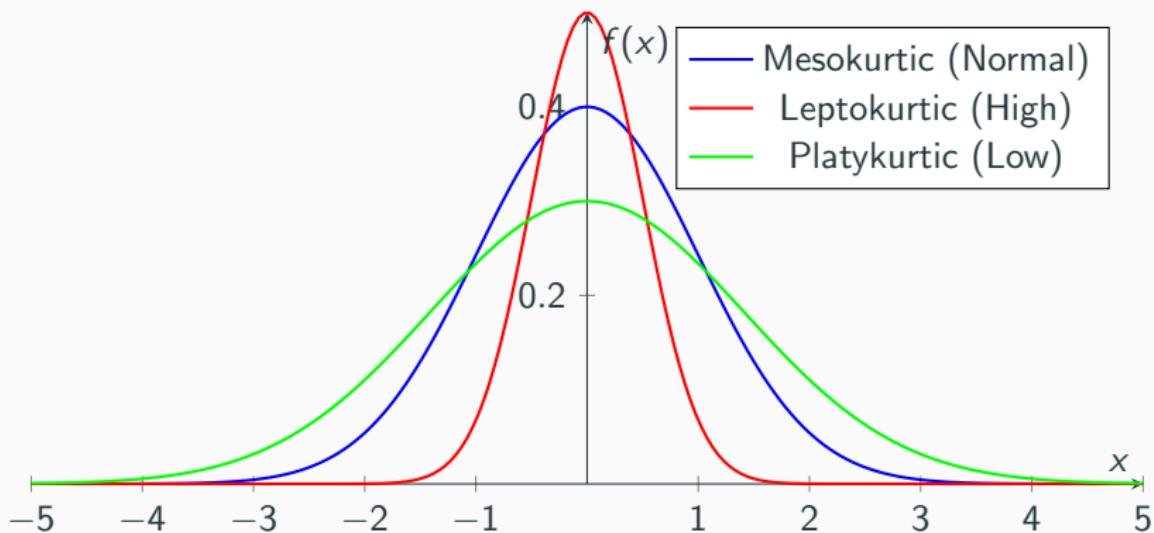
$$\text{Kurtosis} = \frac{1}{n} \sum_{i=1}^n \left( \frac{x_i - \bar{x}}{s} \right)^4$$

- You start by the **mean** ( $\bar{x}$ ) and **standard deviation** ( $s$ ) of your dataset; the computed values are divided by the **population size**.
- Measures "**peakedness**" of the distribution.
- High kurtosis = heavy tails
- Kurtosis can tell you whether the dataset contains more **extreme values** (= high tails)

The above formula refers to **population**. As the purpose of this class is for you to understand the **theory** behind summary statistics, we will not delve into the details of unbiasedness.

# Kurtosis: Example

Comparison of Different Kurtosis Levels



# Graphical Exploratory Data Analysis

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# Graphical EDA

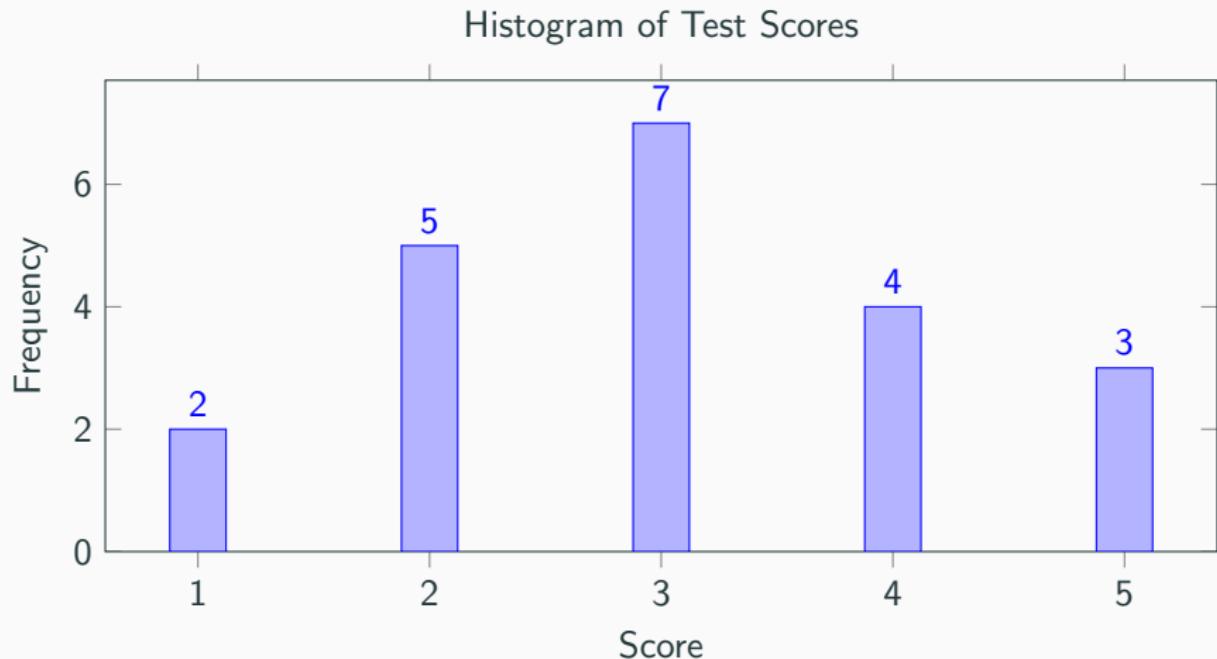
- Last lecture: different types of diagrams, and how to plot them
- Focus of this lecture:
  - How the learned visualization techniques relate to your data
  - What they tell you about your data
  - When and how to choose the right visualization techniques

# Sample Dataset

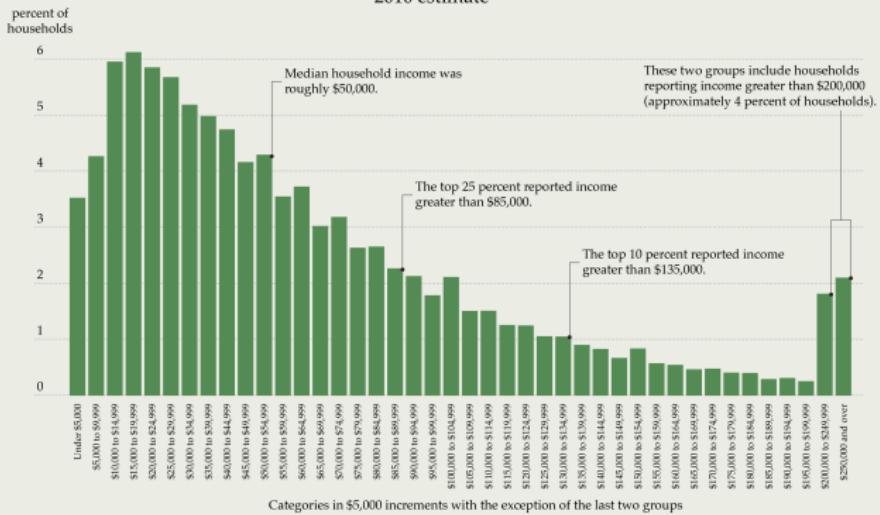
Data	Frequency
1	2
2	5
3	7
4	4
5	3

**Table 1:** Data and Frequency Table

# Histograms



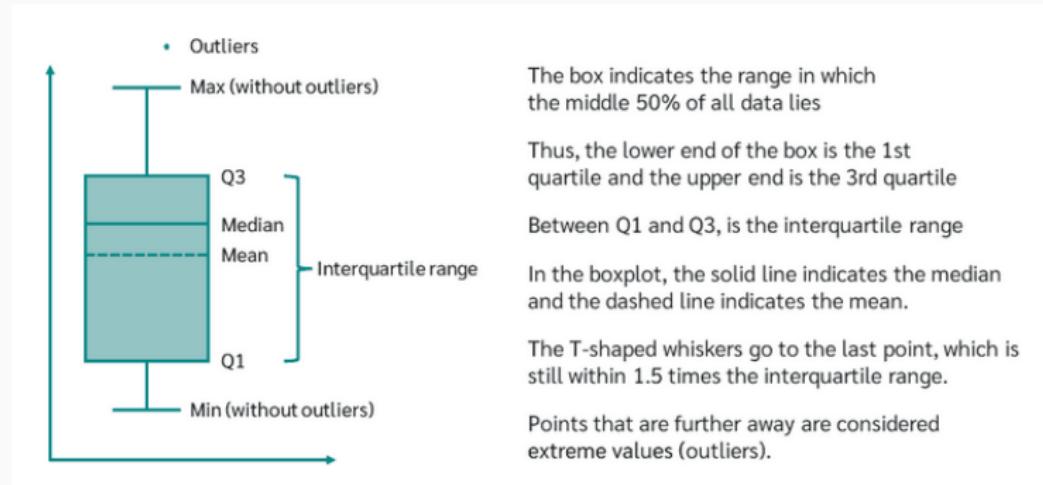
## Distribution of annual household income in the United States 2010 estimate



Source: U.S. Census Bureau, Current Population Survey, 2011 Annual Social and Economic Supplement

Source: [Wikimedia Commons](#).

# Boxplots



**Figure 2:** Explanation of boxplots.

Source: [Datatab](#).

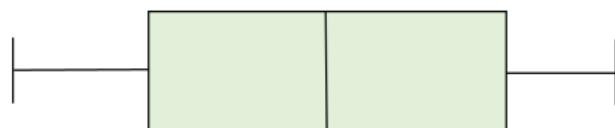
**Left Skewed**



**Right Skewed**

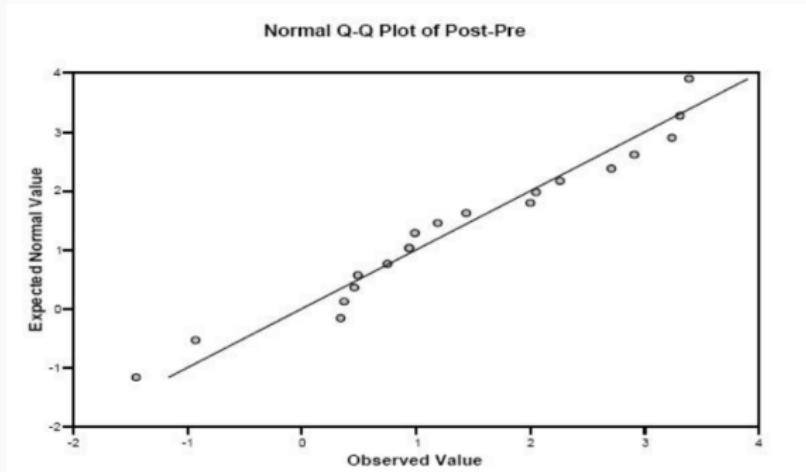


**No Skew**



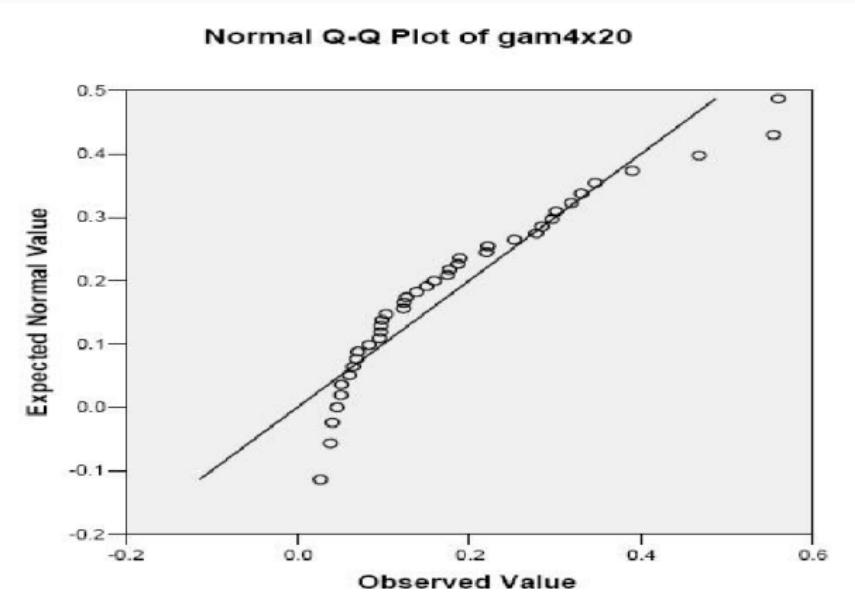
**Figure 3:** How to spot skewness in boxplots.

# Quantile-Normal Plots



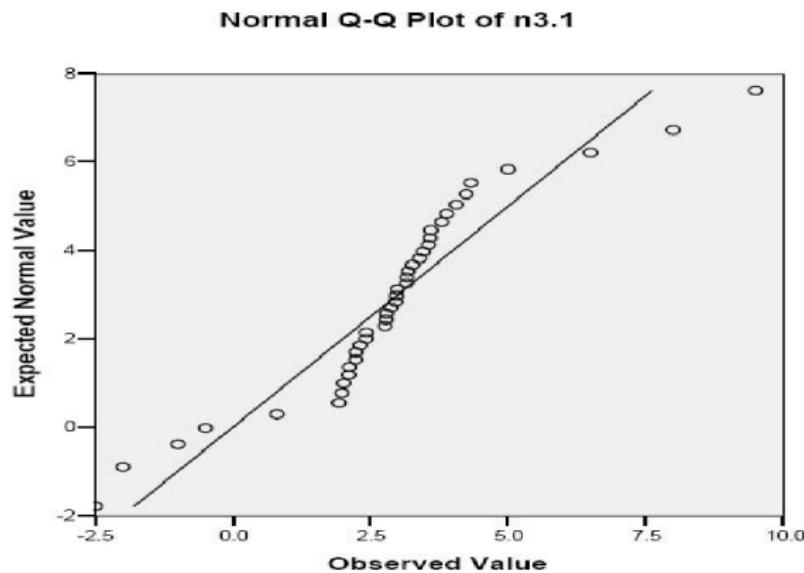
**Figure 4:** Example of quantile-normal plot where the data approximately follows normal distribution.

Source: [Stanford lectures on EDA](#).



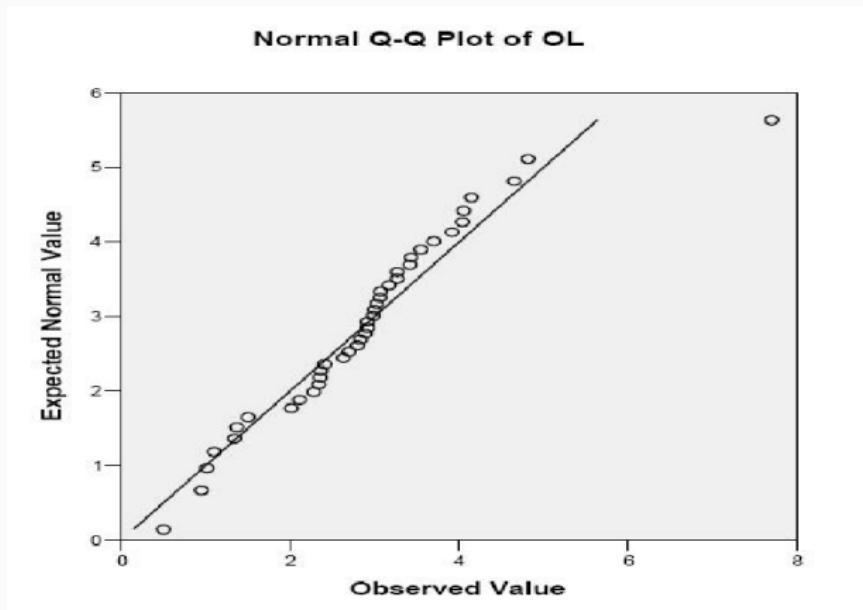
**Figure 5:** Example of quantile-normal plot displaying right skew.

Source: [Stanford lectures on EDA](#).



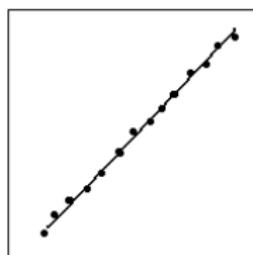
**Figure 6:** Example of quantile-normal plot with fat tails (positive kurtosis).

Source: [Stanford lectures on EDA](#).

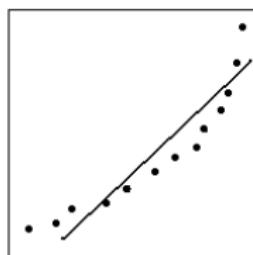


**Figure 7:** Example of quantile-normal plot with an outlier.

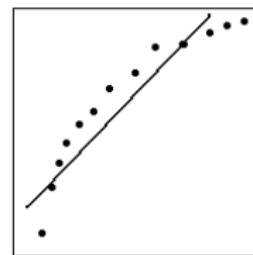
Source: [Stanford lectures on EDA](#).



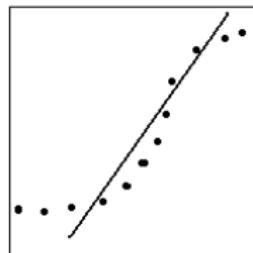
a. Normal



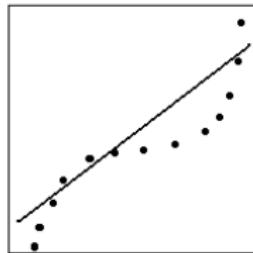
b. Skewed to the Left



c. Skewed to the Right



d. Thick Tails



e. Thin Tails

**Figure 8:** Examples of interpretations of quantile-normal plots.

Source: [Normal Plot](#)

# Multivariate Non-Graphical Data Analysis

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## Cross-Tabulation

Subject ID	Age Group	Sex
GW	young	F
JA	middle	F
TJ	young	M
JMA	young	M
JMO	middle	F
JQA	old	F
AJ	old	F
MVB	young	M
WHH	old	F
JT	young	F
JKP	middle	M

Age and sex data for a population sample.

Age Group / Sex	Female	Male	Total
young	2	3	5
middle	2	1	3
old	3	0	3
Total	7	4	11

Cross-Tabulation of the original data.

## What Are Covariance and Correlation?

- Both measure the relationship between two variables.
- **Covariance:** Indicates the strength and direction of the relationship:  
*How much does one variable change if the other one changes?*
- **Correlation:** Indicates the strength and direction, **standardized**.

Here, we will present **sample** covariance and correlation (remember the definition of unbiasedness). To compute **population** correlation and covariance, the denominator will be  $n$  instead of  $n - 1$ .

# Sample Covariance

**Definition:**

$$\text{Cov}(X, Y) = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{n - 1}$$

- Positive: Variables move in the same direction.
- Negative: Variables move in opposite directions.
- Covariance near 0: Variables vary independently.
- Magnitude depends on units (not standardized).

# Sample Correlation

**Definition:**

$$r = \frac{\text{Cov}(X, Y)}{\sigma_X \sigma_Y}$$

where  $\sigma_X$  and  $\sigma_Y$  are standard deviations of  $X$  and  $Y$ .

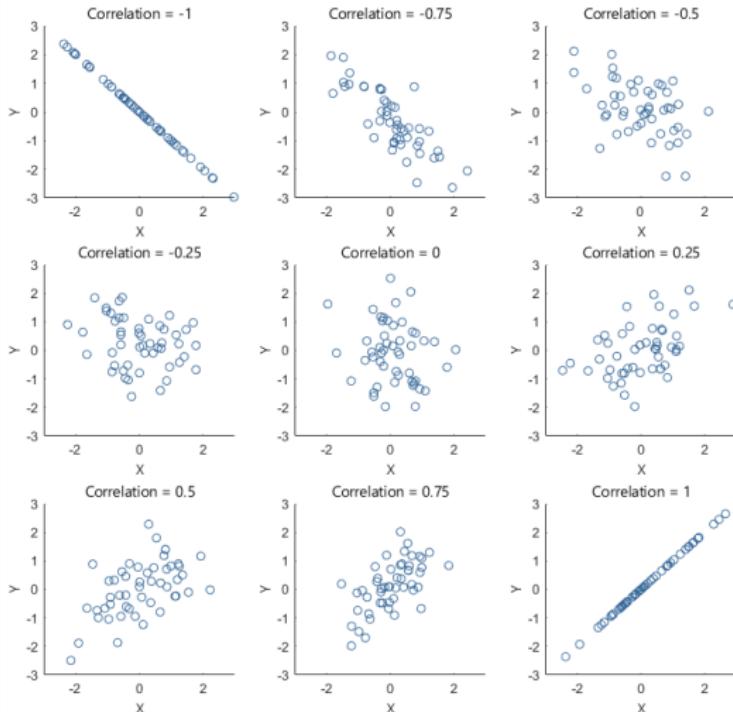
- Ranges from  $-1$  to  $+1$ .
- $r = 1$ : Perfect positive relationship.
- $r = -1$ : Perfect negative relationship.
- $r = 0$ : No linear relationship.

## Relationship Between Covariance and Correlation

- Covariance measures direction, correlation standardizes it.
- Correlation removes the effect of units.
- Formula:  $\rho = \frac{\text{Cov}(X, Y)}{\sigma_X \sigma_Y}$

# Visualization of Correlation

Realizations of couples of random variables X and Y  
with different correlation coefficients

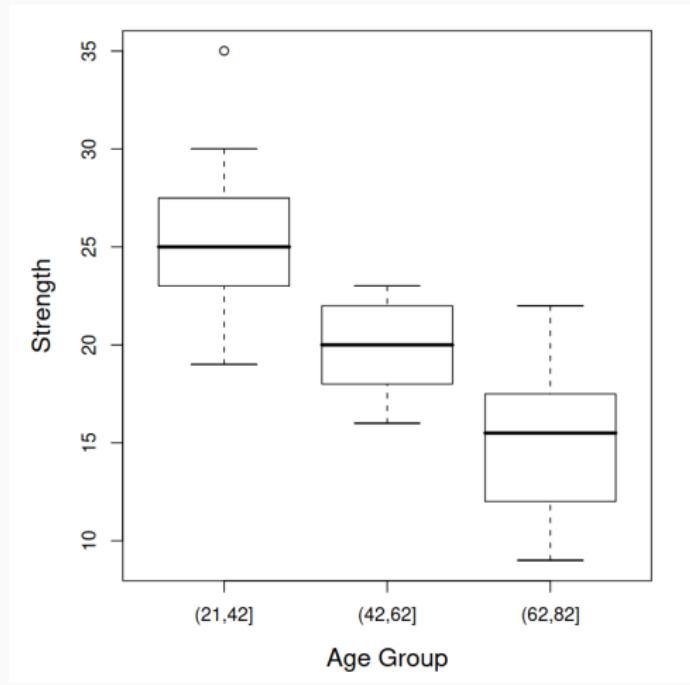


- Strong positive correlation: points close to upward line.
- Strong negative correlation: points close to downward line.
- No correlation: points scattered randomly.

# Multivariate Graphical Exploratory Data Analysis

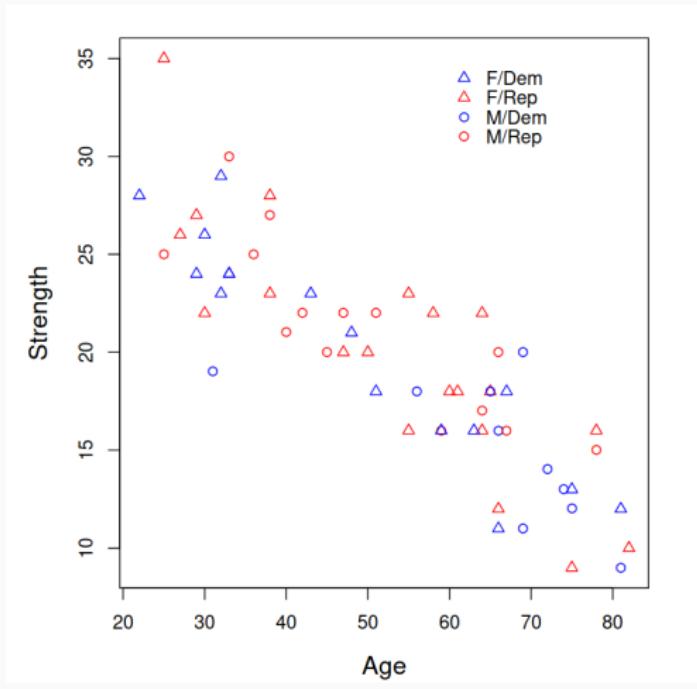
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# Side by Side Boxplots



**Figure 9:** Example of side-by-side boxplot.

# Scatterplots



**Figure 10:** Example of scatterplot.

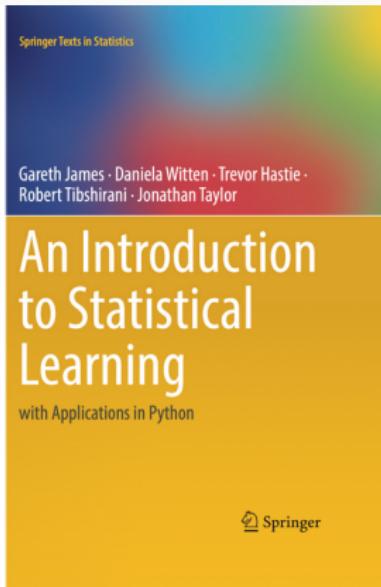
## Conclusion

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## Take-home messages

- Reviewed and extended basic statistical concepts
- Applications of EDA to real-world data
- Revising of Pandas and Seaborn
- **ToDo:** exercising implementation of EDA in Python (homework to come on Moodle - stay tuned!)
- **Next:** Statistical modeling foundations.

# Recommended Readings



[Python Data Science Handbook](#)

[An Introduction to Statistical Learning](#)