

NAP: A Computer Program for the Computation of Two-Dimensional, Time-Dependent, Inviscid Nozzle Flow

by

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ABSTRACT

A computer program, NAP, is presented for calculating inviscid, steady, and unsteady flow in two-dimensional and axisymmetric nozzles. Interior mesh points are computed using the MacCormack finite-difference scheme, while a characteristic scheme is used to calculate the boundary mesh points. An explicit artificial viscosity term is included for shock computations. The fluid is assumed to be a perfect gas. This method was used to compute the steady flow in a 45° - 15° conical, converging-diverging nozzle, a 15° conical, converging nozzle, and a 10° conical, plug nozzle. The numerical solution agreed well with the experimental data. In contrast to previous time-dependent methods for calculating steady flows, the computational times were < 1 min on a CDC 6600 computer.

Chapter 1

Basic Description of the Method

1.1 Introduction

The equations of motion governing steady, inviscid flow are of a mixed type: hyperbolic in the supersonic region and elliptic in the subsonic region. These mathematical difficulties may be removed by using the “time-dependent” method, in which the flow is assumed to be unsteady or time-dependent. Then the governing equations are hyperbolic in both subsonic and supersonic regions. The steady-state solution may be obtained as the asymptotic solution for large time. This time-dependent technique has been used to compute steady converging-diverging nozzle flows (reported in Refs. 1–6), and it has also been used to compute steady converging nozzle flows (see Refs. 4 and 7). The results of those calculations are mainly good, but the computational times are rather large. In addition, although the computer program of Ref. 6 included a centerbody and those of Refs. 4 and 7 included the exhaust jet, none of the above codes is able to calculate both, that is, plug nozzles.

The object of this research was to develop a production-type computer program capable of solving steady converging, converging-diverging, and plug two-dimensional nozzle flows in computational times of < 1 min on a CDC 6600 computer. Such a program would be able to solve unsteady flows as well.

1.2 Literature Review

The following is a discussion of the methods used in References 1 through 7. The first paragraph deals with the computation of the interior mesh points; the next three paragraphs are concerned with the boundary mesh points.

Prozan (see Ref. 1), Wehofer and Moger, and Laval used variations of the two-step Lax-Wendroff scheme to compute the interior mesh points. Migdal *et al.* and Brown and Ozcan employed the original one-step Lax-Wendroff scheme, but with the equations of motion in nonconservation form. Serra applied the original Lax-Wendroff scheme with the equations of motion in conservation form. To stabilize their schemes, Laval and Serra used artificial viscosity terms in their difference equations.

Wehofer and Moger reset the stagnation conditions along each streamline, reset the mass flow at each axial location, and smoothed the subsonic portion of the flow after each time step.

To compute the nozzle inlet mesh points, Prozan (in Ref. 1) assumed the inlet flow to be uniform. Wehofer and Moger assumed only that the pressure was radially uniform at the inlet. Migdal *et al.* and Brown and Ozcan mapped the inlet to minus infinity after Moretti, thus allowing the static conditions to be set equal to the stagnation conditions. Laval used extrapolation of the interior mesh points to determine the inlet mesh points, while Serra employed a characteristic scheme.

Prozan (in Ref. 1), Wehofer and Moger, Laval, and Brown and Ozcan used an extrapolation technique to compute the wall mesh points. Migdal *et al.* employed a characteristic scheme after Moretti to compute the wall mesh points, while Serra applied a reflection technique. For the converging nozzle problem to be properly posed, an exhaust jet calculation must be included. Wehofer and Moger used an extrapolation procedure to compute the exhaust jet boundary mesh points, while Brown and Ozcan employed a characteristic scheme after Moretti.

All of the above authors used extrapolation to compute the exit mesh points when the flow was supersonic, since any errors incurred would be swept out of the mesh. Serra employed a characteristic scheme when the exit flow was subsonic.

1.3 Choice of a Method

The lengthy computational times associated with time-dependent calculations are usually caused by inefficient numerical schemes or poor treatment of boundaries, resulting in the requirement for excessively fine computational meshes (see Refs. 8 and 9). A technique for a much more efficient calculation of the interior and boundary mesh points will be discussed here.

The computation of steady flows by a time-dependent method differs from ordinary initial-value problems in that the initial data and much of the transient solution have a negligible effect on the final or steady solution. Therefore, accuracy is important only for the asymptotic state, and special attention to intermediate efficiency will result in reasonable computational times. For this reason, interior mesh points can be computed by using a very efficient finite-difference scheme, as opposed to those less efficient finite-difference or characteristic schemes that achieve high accuracy at every step.

In the class of finite-difference schemes, the two-step methods such as the MacCormack and the two-step Lax-Wendroff schemes are more efficient than the original Lax-Wendroff scheme, especially if the governing equations are in conservation form. Moretti showed that using the equations of motion in conservation form decreased efficiency and ease of programming while only slightly increasing the accuracy of shock calculations. The use of an explicit artificial viscosity term for shock-free flows also decreases efficiency and was shown to be physically unjustified. In addition, such increases in the numerical dissipation can often destroy the weak shock structure of transonic flows. Therefore, the MacCormack scheme with the equations of motion in nonconservation form is used to calculate the interior mesh points. An explicit artificial viscosity term was included for

shock computations only. Remember that the implicit dissipation always present as an effect of truncation terms assures numerical stability for the shock-free flow results.

The boundary mesh points, while making up only a small part of the total mesh points, must be handled most accurately, because of the flowfield's sensitivity to precise boundary geometry. Moretti and Abbott showed that reflection, extrapolation, and one-sided difference techniques for computing solid wall boundaries give poor results and should be avoided. Therefore, the wall and centerbody mesh points are computed using a characteristic scheme. A characteristic scheme is also used to calculate the exhaust jet boundary mesh points.

In the case of the nozzle inlet mesh points for subsonic flow, the use of extrapolation techniques and the assumption of one-dimensional flow presume the form of the solution and in many cases are physically unjustified. On the other hand, a characteristic scheme could be used to calculate the inlet mesh points. While the stagnation pressure and temperature are assumed to remain constant at the inlet in a characteristic scheme (not necessarily the case for unsteady flow), this assumption would appear to be valid for the time-dependent calculation of steady flows. Moretti recommends mapping the inlet to minus infinity, thus allowing the static conditions to be set equal to the stagnation conditions. In theory, this appears to be the best approach, but it should be kept in mind that the infinite physical plane must be replaced by a finite computational plane. Also, this technique requires additional mesh points upstream of the nozzle inlet. It is not presently resolved as to whether the characteristic scheme approach used by Serra or the mapping-to-minus-infinity approach suggested by Moretti and employed by Migdal *et al.* and Brown and Ozcan is the best technique. To reduce the total number of mesh points to be computed, a characteristic scheme is used to compute the inlet mesh points. For supersonic flow, the inlet mesh points are set equal to specified values of velocity, pressure, and density, because in a supersonic stream the downstream conditions do not propagate upstream. Extrapolation is used to compute the exit mesh points when the flow is supersonic, since any errors incurred will be swept out of the mesh, and a characteristic scheme is employed when the flow is subsonic.

1.4 Equations of Motion

The appropriate non-conservation form of equations for two-dimensional, inviscid, isentropic, rotational flow are:

$$\rho_t + u\rho_x + v\rho_y + \rho u_x + \rho v_y + \epsilon\rho v/y = 0 \quad (1.1)$$

$$u_t + uu_x + vu_y + p_x/\rho = 0 \quad (1.2)$$

$$v_t + uv_x + vv_y + p_y/\rho = 0 \quad (1.3)$$

$$p_t + up_x + vp_y - a^2(\rho_t + u\rho_x + v\rho_y) = 0 \quad (1.4)$$

where ρ is the density, u is the axial velocity, v is the radial velocity, p is the pressure, a is the

local speed of sound, t is the time, x and y are the axial and radial coordinates, and the subscripts denote partial differentiation. The symbol ϵ is 0 for planar flow and 1 for axisymmetric flow.

1.4.1 Coordinate Transformation

The physical (x, y) plane is mapped into a rectangular computational plane (ζ, η) by the following coordinate transformation:

$$\zeta = x; \quad \eta = \frac{y - y_c(x)}{y_w(x, t) - y_c(x)}; \quad \tau = t \quad (1.5)$$

where $y_w(x, t)$ denotes the nozzle wall and exhaust jet boundary radius as a function of x and t and $y_c(x)$ denotes the nozzle centerbody radius as a function of x . These mapping functions must be single-valued functions of the x coordinate. In the (ζ, η, τ) coordinate system Equations (1.1)–(1.4) become:

$$\rho_\tau + u\rho_\zeta + \bar{v}\rho_\eta + \rho u_\zeta + \rho\alpha u_\eta + \rho\beta v_\eta + \epsilon\rho v/(y_c + \eta/\beta) = 0 \quad (1.6)$$

$$u_\tau + uu_\zeta + \bar{v}u_\eta + p_\zeta/\rho + \alpha p_\eta/\rho = 0 \quad (1.7)$$

$$v_\tau + uv_\zeta + \bar{v}v_\eta + \beta p_\eta/\rho = 0 \quad (1.8)$$

$$p_\tau + up_\zeta + \bar{v}p_\eta - a^2(\rho_\tau + u\rho_\zeta + \bar{v}\rho_\eta) = 0 \quad (1.9)$$

where

$$\beta = \frac{1}{y_w - y_c} \quad (1.10)$$

$$\alpha = -\beta \frac{\partial y_c}{\partial x} - \left(\frac{\partial y_w}{\partial x} - \frac{\partial y_c}{\partial x} \right) \quad (1.11)$$

$$\delta = -\eta\beta \frac{\partial y_w}{\partial t} \quad (1.12)$$

and

$$\bar{v} = \alpha u + \beta v + \delta \quad (1.13)$$

The fluid is assumed to be thermally and calorically perfect; that is, a constant ratio of specific heats is assumed.

1.4.2 Artificial Viscosity for Shock Computations

For shock computations, an artificial viscosity model of the form suggested by von Neumann-Richtmyer is used. This model, which has a term corresponding to all the viscous and thermal conduction terms in the Navier-Stokes equations, is shown below.

$$[\text{RHS Eq. (2)}] = (\lambda + 2\mu) \frac{\partial}{\partial x} \left(\frac{\partial u}{\partial x} \right) + \lambda \frac{\partial}{\partial x} \left(\frac{\partial v}{\partial y} \right) + \frac{\epsilon}{y} \left[(\lambda + \mu) \frac{\partial v}{\partial x} + \mu \frac{\partial u}{\partial y} \right] \quad (1.14)$$

$$[\text{RHS Eq. (3)}] = (\lambda + 2\mu) \frac{\partial}{\partial y} \left(\frac{\partial u}{\partial x} \right) + \lambda \frac{\partial}{\partial y} \left(\frac{\partial v}{\partial y} \right) + \mu \frac{\partial}{\partial x} \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right) + \frac{\epsilon(\lambda + 2\mu)}{y} \left(\frac{\partial v}{\partial y} - \frac{v}{y} \right) \quad (1.15)$$

where $c_\mu = c_\lambda$ are nondimensional quantities that specify the distribution and amount of smoothing. [Note: Complete artificial viscosity formulation to be filled from Section II of original report.]

1.5 Numerical Method

The computational plane is divided into five sets of mesh points: interior, inlet, exit, wall and centerbody, and exhaust jet boundary.

1.5.1 Interior Mesh Points

The interior mesh points are computed using the MacCormack scheme, a second-order, non-centered, two-step, finite-difference scheme. Backward differences are used on the first step; forward differences are used on the second. The governing equations are left in non-conservation form. An explicit artificial viscosity term is used for shock computations. Centerline mesh points are computed by enforcing symmetry of the flow. For example, the finite-difference equations for Equation (1.1) for planar flow ($\epsilon = 0$) and no artificial viscosity are:

$$\bar{\rho}_{L,M}^{N+1} = \rho_{L,M}^N - \left[u_{L,M}^N \left(\frac{\rho_{L,M}^N - \rho_{L-1,M}^N}{\Delta x} \right) + v_{L,M}^N \left(\frac{\rho_{L,M}^N - \rho_{L,M-1}^N}{\Delta y} \right) + \rho_{L,M}^N \left(\frac{u_{L,M}^N - u_{L-1,M}^N}{\Delta x} \right) + \rho_{L,M}^N \left(\frac{v_{L,M}^N - v_{L,M-1}^N}{\Delta y} \right) \right] \quad (1.16)$$

$$\rho_{L,M}^{N+1} = 0.5 \left[\rho_{L,M}^N + \bar{\rho}_{L,M}^{N+1} - \left[\bar{u}_{L,M}^{N+1} \left(\frac{\bar{\rho}_{L+1,M}^{N+1} - \bar{\rho}_{L,M}^{N+1}}{\Delta x} \right) + \bar{v}_{L,M}^{N+1} \left(\frac{\bar{\rho}_{L,M+1}^{N+1} - \bar{\rho}_{L,M}^{N+1}}{\Delta y} \right) + \bar{\rho}_{L,M}^{N+1} \left(\frac{\bar{u}_{L+1,M}^{N+1} - \bar{u}_{L,M}^{N+1}}{\Delta x} \right) + \bar{\rho}_{L,M}^{N+1} \left(\frac{\bar{v}_{L,M+1}^{N+1} - \bar{v}_{L,M}^{N+1}}{\Delta y} \right) \right] \right] \quad (1.17)$$

where L and M denote axial and radial mesh points, respectively, N denotes the time step, and the bar denotes values calculated on the first step.

1.5.2 Inlet Mesh Points

The inlet mesh points for subsonic flow are computed using a second-order, reference-plane characteristic scheme. In this scheme, the partial derivatives with respect to η are computed in the initial-value and solution surfaces using non-centered differencing as in the MacCormack scheme. These approximations to the derivatives with respect to η are then treated as forcing terms and the

resulting system of equations is solved in the $\eta = \text{constant}$ reference planes using a two-independent-variable, characteristic scheme.

The boundary condition is the specification of the stagnation temperature and stagnation pressure. The use of a reference-plane characteristic scheme requires the specification of inlet flow angle as an additional boundary condition. The inlet flow angle can be approximately determined from the nozzle geometry. The equations relating the total and static conditions are:

$$p_T/p = [1 + (\gamma - 1)M^2/2]^{\gamma/(\gamma-1)} \quad (1.18)$$

$$T_T/T = 1 + (\gamma - 1)M^2/2 \quad (1.19)$$

where γ is the ratio of specific heats, M is the Mach number, T is the temperature, and the subscript T denotes the total conditions.

For supersonic flow, the inlet mesh points are set equal to specified values of velocity, pressure, and density.

1.5.3 Exit Mesh Points

For subsonic flow, a reference-plane characteristic scheme similar to the inlet scheme is used. The exit pressure is specified.

For supersonic flow, the exit mesh points are computed using linear extrapolation.

1.5.4 Wall and Centerbody Mesh Points

The wall and centerbody mesh points are computed using a reference-plane characteristic scheme. The wall and centerbody contours and therefore their slopes are specified. The boundary condition is given by:

$$v = u \tan(\theta) + \frac{\partial y_w}{\partial t} \quad (1.20)$$

where θ is the local wall or centerbody angle.

1.5.5 Exhaust Jet Boundary Mesh Points

The exhaust jet boundary mesh points are computed by the wall routine such that the pressure boundary condition:

$$p = p_{\text{ambient}} \quad (1.21)$$

is satisfied. This is accomplished by first assuming the shape of the jet boundary and then using the wall routine to calculate the pressure. Next, the jet boundary location is slightly changed and a second pressure is computed. By use of an interpolation procedure, a new jet boundary location

is determined. This interpolation-extrapolation procedure is then repeated at each point until the jet boundary pressure and the ambient pressure agree within some specified tolerance.

1.5.6 Time Step Control

The step size Δt is controlled by the well-known Courant or CFL condition, which can be expressed as:

$$\Delta t \leq \frac{1}{\left[(V + a) \left(\frac{1}{\Delta x^2} + \frac{1}{\Delta y^2} \right)^{1/2} \right]} \quad (1.22)$$

where V is the velocity magnitude. Using the coordinate transformation, Equation (1.22) becomes:

$$\Delta \tau \leq \frac{A}{\left[(V + a) \left(\frac{1}{\Delta \zeta^2} + \frac{\beta^2}{\Delta \eta^2} \right)^{1/2} \right]} \quad (1.23)$$

where the coefficient A was determined from actual calculations and varied between 0.4 and 1.6 depending on the geometry of the flow in question.

1.6 Overall Program Capabilities

The nozzle inlet flow, as well as the flow leaving the nozzle, may be either subsonic or supersonic. The flow may contain variations in stagnation temperature and stagnation pressure from streamline to streamline. The nozzle wall and centerbody geometries may be either one of two analytical contours or a completely general tabular contour. The program is capable of calculating the exhaust jet boundary for subsonic or supersonic flow. The initial data may be read in or calculated internally by the program. The internally computed data are calculated assuming one-dimensional, steady, isentropic flow with area change. The program output includes the coordinates, velocities, pressure, density, Mach number, temperature, mass flow, and axial thrust in both English and metric units.

1.7 Results and Discussion

The results presented here have been adopted from experimental validation work. The CDC 6600 computational times represent the central processor time not including compilation. So that these results can be compared with those of other investigators, the following table of relative machine speeds is provided:

Table 1.1: Relative Machine Speeds Compared to CDC 6600

Computer	Relative Machine Speed
IBM 7094	0.1
IBM 360/50	0.1
IBM 360/64	0.3
IBM 360/75	0.5
Univac 1108	0.5
CDC 6600	1.0

The validation cases are presented below.

1.7.1 Case 1: 45°-15° Conical Converging-Diverging Nozzle

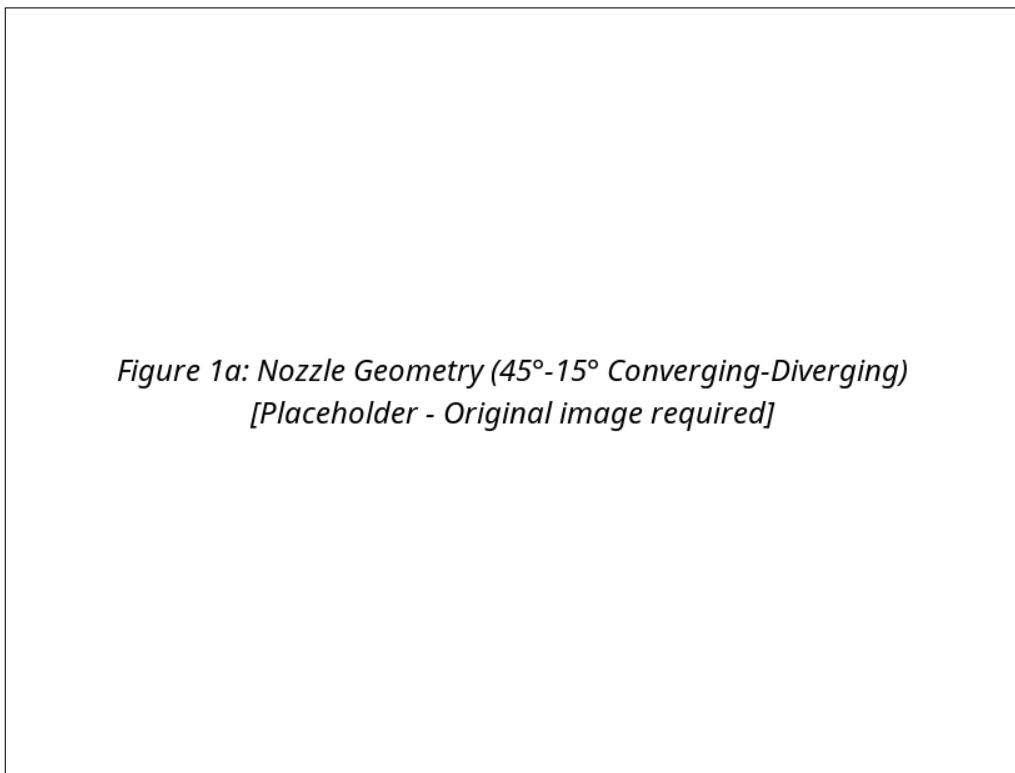
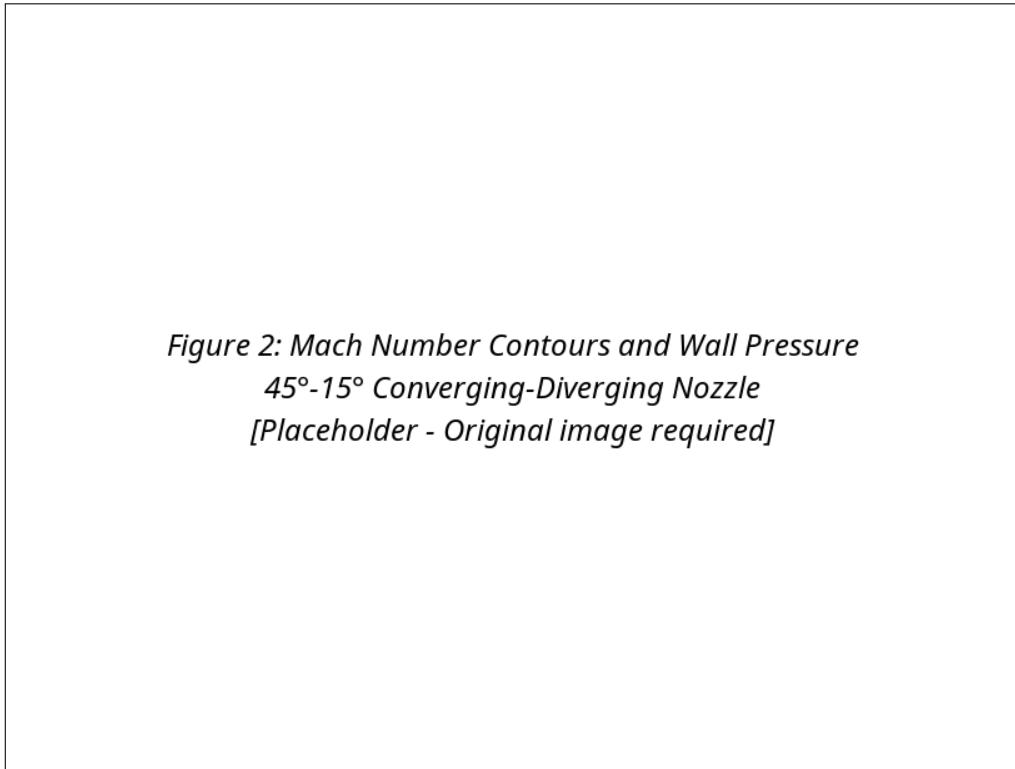


Figure 1a: Nozzle Geometry (45°-15° Converging-Diverging)
[Placeholder - Original image required]

Figure 1.1: 45°-15° Converging-Diverging Nozzle Geometry

The present method was used to compute the steady-state solution for flow in the 45°-15° conical, converging-diverging nozzle. A 21×8 computational mesh required 301 time planes and a computational time of 35 seconds. The experimental data are those of Cuffel et al. (Ref. 2). The computed discharge coefficient is 0.983, compared with the experimental value of 0.985.

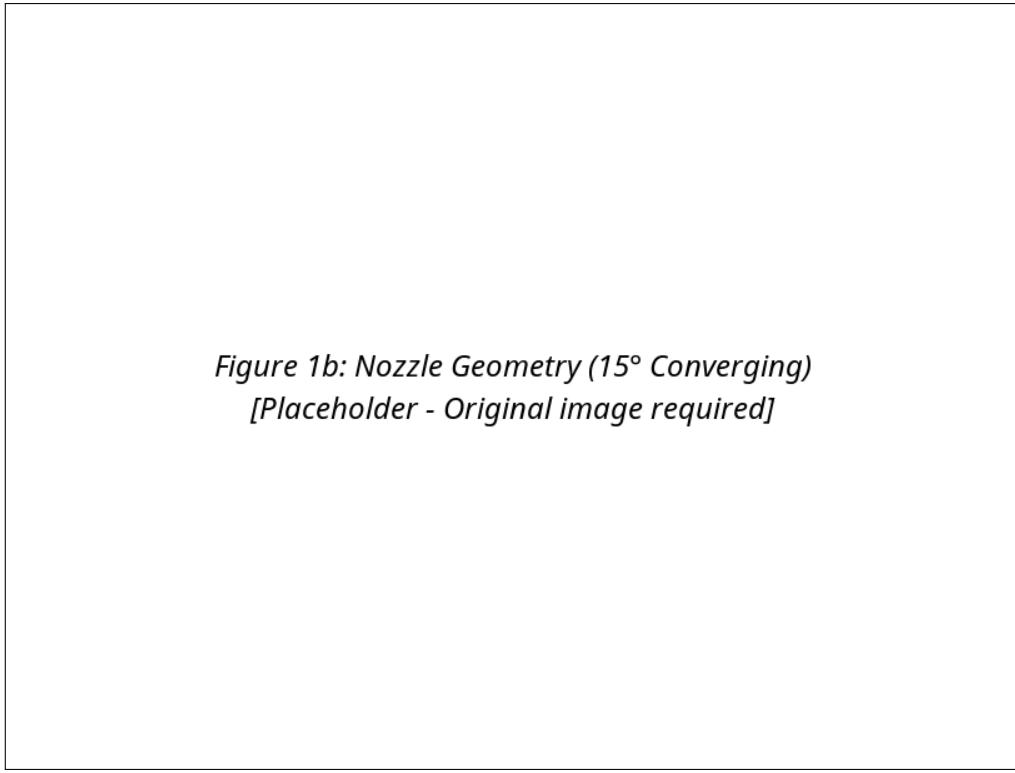


*Figure 2: Mach Number Contours and Wall Pressure
45°-15° Converging-Diverging Nozzle
[Placeholder - Original image required]*

Figure 1.2: Mach Number Contours and Wall Pressure Ratio for 45°-15° Conical Converging-Diverging Nozzle

There is good agreement with the experimental data. This case was also solved by other researchers including Prozan, Migdal, Laval, and Serra, with computational times ranging from 45 minutes to 2 hours on various computer systems.

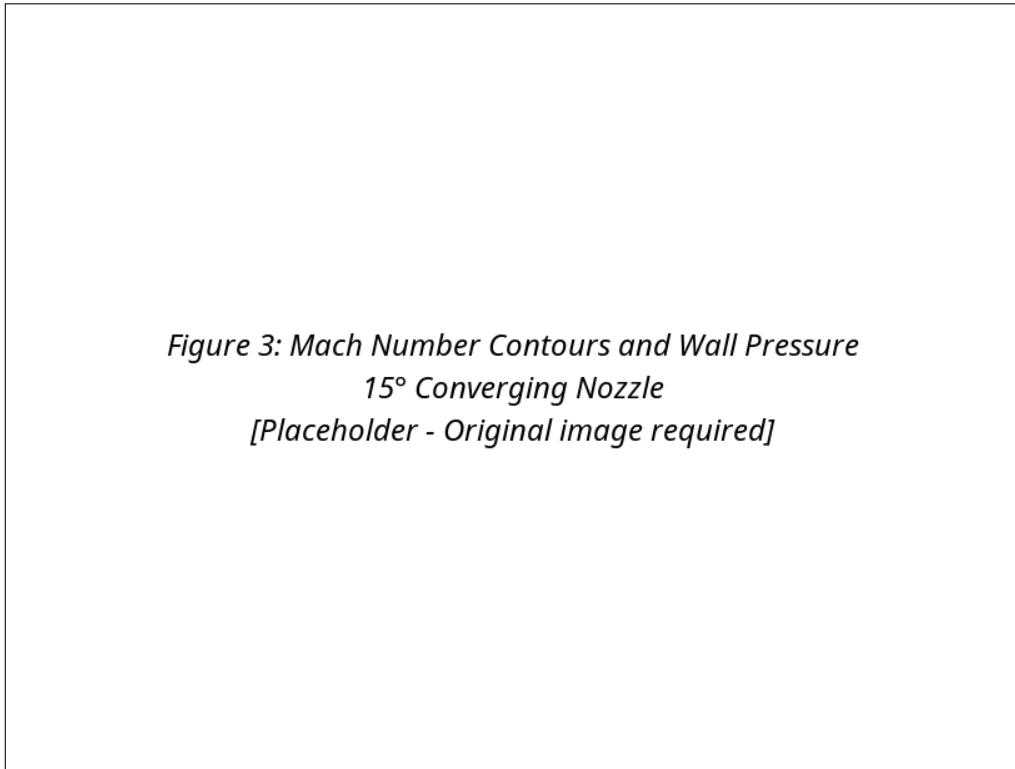
1.7.2 Case 2: 15° Conical Converging Nozzle



*Figure 1b: Nozzle Geometry (15° Converging)
[Placeholder - Original image required]*

Figure 1.3: 15° Conical Converging Nozzle Geometry

The present method was also used to compute the steady-state flow in a 15° conical, converging nozzle. The nozzle geometry is shown in Figure 1.3. A 23×7 computational mesh required 249 time planes and a computational time of 29 seconds. The experimental data are those of Thornock (Ref. 17). The computed discharge coefficient is 0.957, compared with the experimental value of 0.960.

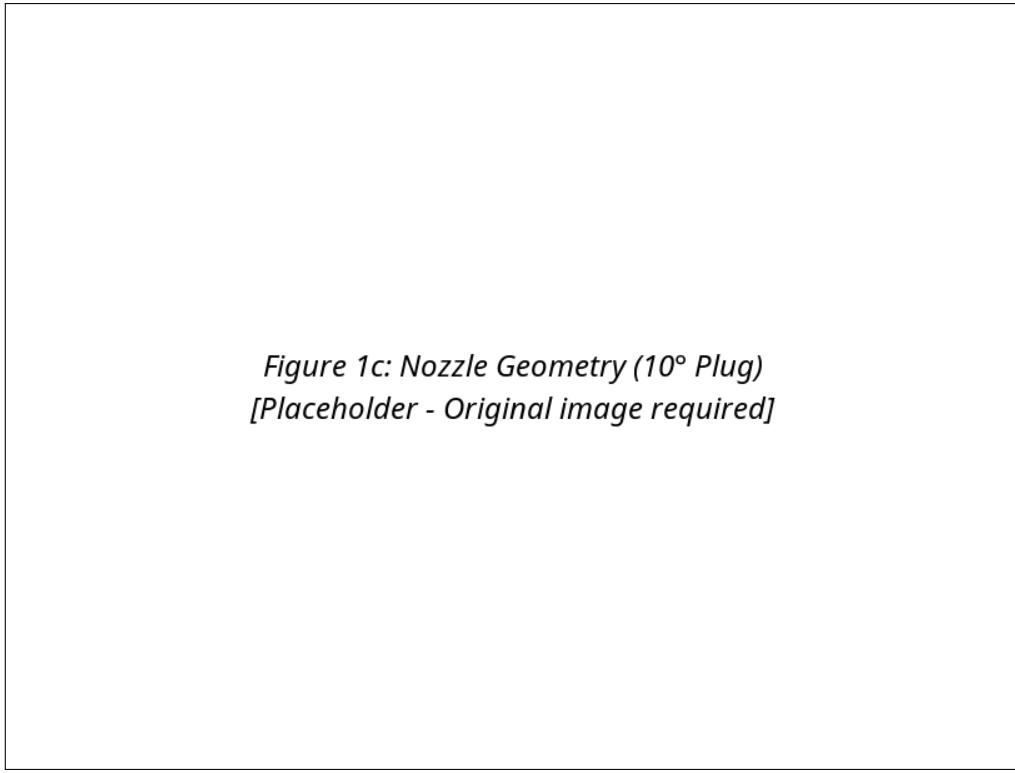


*Figure 3: Mach Number Contours and Wall Pressure
15° Converging Nozzle
[Placeholder - Original image required]*

Figure 1.4: Mach Number Contours and Wall Pressure Ratio for 15° Conical Converging Nozzle

There is good agreement with the experimental data. This case was also solved by Wehofer and Moger and Brown and Ozcan, with Wehofer and Moger requiring over 2 hours on an IBM 360/50 (47×11 mesh) and Brown and Ozcan requiring 17 minutes on an IBM 360/65 (20×6 mesh).

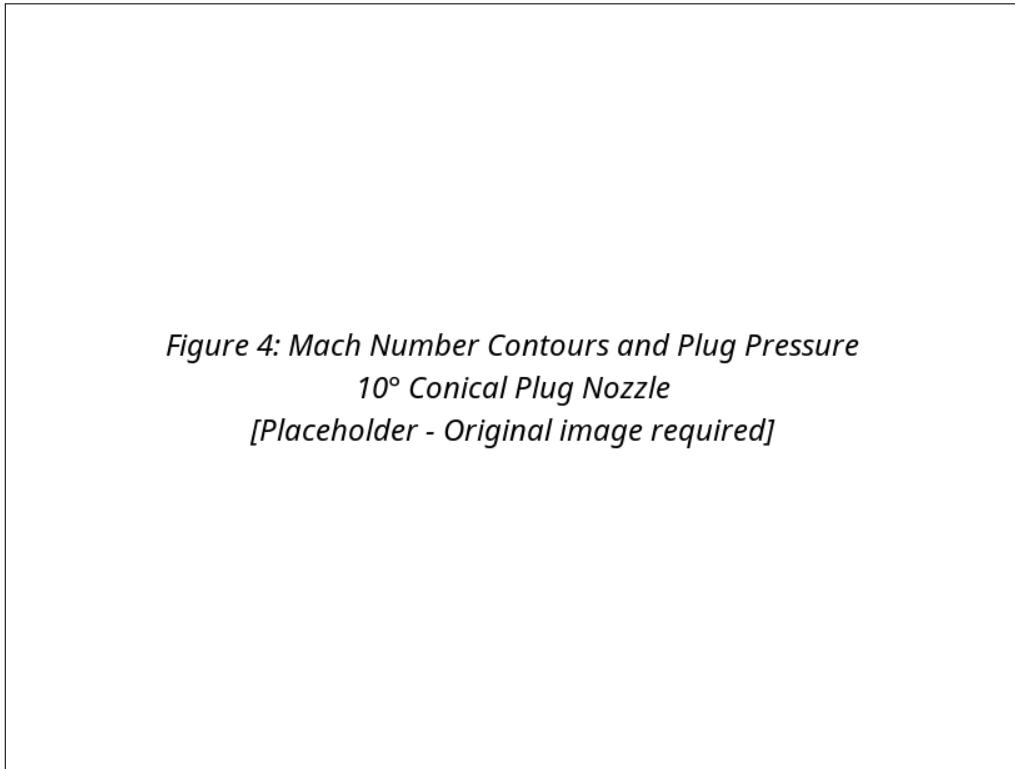
1.7.3 Case 3: 10° Conical Plug Nozzle



*Figure 1c: Nozzle Geometry (10° Plug)
[Placeholder - Original image required]*

Figure 1.5: 10° Conical Plug Nozzle Geometry

Finally, the present method was used to calculate the flow in a 10° conical, plug nozzle. The nozzle geometry is shown in Figure 1.5. A 31×6 computational mesh required 327 time planes and a computational time of 52 seconds. The experimental data are those of Bresnahan and Johns (Ref. 18).



*Figure 4: Mach Number Contours and Plug Pressure
10° Conical Plug Nozzle
[Placeholder - Original image required]*

Figure 1.6: Mach Number Contours and Plug Pressure Ratio for 10° Conical Plug Nozzle

Again, there is good agreement with the experimental data. The author is unaware of any other time-dependent analyses of plug nozzles.

1.8 Concluding Remarks

A method of computing nozzle flows has been presented. A production-type computer program capable of solving a wide variety of nozzle flows has been developed. The program's accuracy was demonstrated by computing the steady flow in the three test cases above. The sub-one-minute computational times for these steady flows is considerably faster than for any of the earlier time-dependent techniques.

Chapter 2

Program Description and Usage

2.1 Program Structure

The NAP computer program consists of one main program, one function, and twelve subroutines. The program structure follows this execution flow:

1. **Program MAIN:** Initiates the run by reading input data, printing the program title and abstract, and converting units. Calls geometry subroutines and performs the main time-stepping loop.
2. **GEOM and GEOMCB:** Calculate the nozzle geometry for fixed wall and optional center-body configurations.
3. **ONEDIM:** Calculates the one-dimensional isentropic initial-value surface using a Newton-Raphson scheme to find Mach numbers from area ratios.
4. **MAP:** Calculates mapping functions that transform the physical plane to a rectangular computational plane.
5. **INTER:** Performs the interior mesh calculations using the MacCormack finite-difference scheme.
6. **INLET, WALL:** Implement boundary conditions using second-order characteristic-based schemes.
7. **MASFLO:** Calculates mass flow and thrust during the solution.
8. **PLOT:** Generates film plots of solution contours and velocity vectors.

2.2 Input Data Format

Input data are provided via Fortran NAMELIST format. The primary input namelists are:

NAMELIST /CNTRL/: Control Parameters

Key parameters controlling the simulation:

LMAX, MMAX Grid dimensions (ξ and η directions)

NMAX Maximum number of time steps

NPRINT Print frequency (0 = final solution only, $n > 0$ = every n steps)

TCONV Convergence criterion for steady-state detection

FDT Frequency for time-step recalculation

TSTOP Simulation stop time

GAMMA Specific heat ratio ($\gamma = 1.4$ for air)

RGAS Gas constant (53.35 for air in English units)

NASM Number of inlet stagnation point profiles (1 or > 1 for variable inlet conditions)

IUNIT Unit conversion flag (0 = English, 1 = SI)

NAMELIST /GEMTRY/: Geometry Parameters

Nozzle geometry definition:

NDIM Dimension flag (0 = 2D axisymmetric, 1 = 2D Cartesian)

NGEOM Geometry type (1 = converging, 2 = converging-diverging, 3 = plug)

XI, XE Inlet and exit axial coordinates

RI, RE Inlet and exit radii

RCI, RCT, RCE Centerbody inlet, throat, and exit radii (if centerbody present)

ANGI, ANGE Inlet and exit half-angles (degrees)

NWPTS Number of wall definition points

NAMELIST /BC/: Boundary Conditions

Inlet boundary condition parameters:

PT Stagnation pressure profile (array of NASM values)

TT Stagnation temperature profile (array of NASM values)

THETA Inlet flow angle profile (degrees)

PE Exit static pressure

NSTAG Stagnation profile flag (0 = uniform, > 0 = radial variation)

ISUPER Supersonic inlet flag (0 = subsonic, 1 = supersonic)

2.3 Output Description

The program produces output in three forms:

1. Printed Output

ASCII output containing:

- Program header and version information
- Echo of input parameters (CNTRL, GEMTRY, BC namelists)
- Initial geometry and one-dimensional surface calculations
- Iteration history with time, time-step size, and convergence measures (if requested)
- Final solution statistics including mass flow, momentum, and thrust

2. Film Plots

Vector plots and contour plots on graphics film (if NPLOT ≥ 0):

- Velocity vectors at each solution time
- Contours of Mach number, pressure, density
- Wall streamline positions

3. Punched Card Output (Optional)

Fortran unformatted binary restart deck for continuing previous runs.

2.4 Sample Calculations

Three nozzle geometries have been analyzed and serve as test cases:

Case 1: Converging-Diverging Nozzle

A 45° – 15° converging-diverging geometry with uniform inlet conditions at stagnation pressure $P_T = 13.78$ psia and temperature $T_T = 530$ °R. Results show excellent agreement with one-dimensional theory at the throat and quasi-2D behavior in the diverging section.

Case 2: Converging Nozzle

A simple 15° converging geometry with identical inlet conditions. Used to test subsonic inlet conditions and convergent-only nozzles.

Case 3: Plug Nozzle

A complex plug nozzle configuration with variable centerbody. Comparison with experimental data of Bresnahan and Johns (Reference 18) shows good agreement in gross features including shock structure at off-design conditions.

For detailed sample input and output listings, refer to the original NAP documentation. The program is controlled entirely via namelist input which provides flexibility for analyzing various nozzle configurations and inlet conditions.

Note: This chapter was reconstructed from OCR-extracted text and program code analysis. For production use, consult the original LASL technical documentation and verify input/output specifications with the actual Fortran source code listings in Appendix C.

References

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Appendix A

Characteristic Relations

A.1 $\eta = \text{constant}$ Reference Plane

[To be completed: Derivation of characteristic relations for inlet and exit boundaries (Appendix A from original)]

A.2 $\zeta = \text{constant}$ Reference Plane

[To be completed: Derivation of characteristic relations for wall and centerbody boundaries (Appendix B from original)]

Appendix B

Fortran Code Listing (LASL Identification: LP-0537)

B.1 Main Program (fortran_main.f)

This is the main program that orchestrates the NAP solver. It handles input/output, initialization, and time-stepping control.

```
1 PROGRAM MAIN(INPUT,OUTPUT,FILM,PUNCH,TAPE5=INPUT,TAPE6=OUTPUT,
2 1TAPE7=FILM)
3 C
4 C ****
5 C NAP, A COMPUTER PROGRAM FOR THE COMPUTATION OF TWO-DIMENSIONAL,
6 C TIME-DEPENDENT, INVISCID NOZZLE FLOW
7 C
8 C BY MICHAEL C. CLINE, T-3
9 C LOS ALAMOS SCIENTIFIC LABORATORY
10 C
11 C ****
12 C
13 C PROGRAM ABSTRACT
14 C
15 C THE EQUATIONS OF MOTION FOR TWO-DIMENSIONAL, TIME DEPENDENT,
16 C INVISCID FLOW IN A NOZZLE ARE SOLVED USING THE SECOND-ORDER,
17 C MACCORMACK FINITE-DIFFERENCE SCHEME, THE FLUID IS ASSUMED TO BE
18 C A PERFECT GAS. ALL BOUNDARY CONDITIONS ARE COMPUTED USING A
19 C SECOND-ORDER, REFERENCE PLANE CHARACTERISTIC SCHEME, THE STEADY
20 C STATE SOLUTION IS OBTAINED AS THE ASYMPTOTIC SOLUTION FOR LARGE
21 C TIME, THE NOZZLES MAY BE EITHER CONVERGING, CONVERGING-DIVERGING,
22 C OR PLUG GEOMETRIES.
23 C
24 DIMENSION TITLE(8), UI(21), VI(21), PI(21), ROI(21)
25 COMMON /AV/ IAV,CAV,NST,SMP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81
26 1,21),QPT(81,21)
27 COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)
28 COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RO(81,21,2)
29 COMMON /CNTRL/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAMI,GA
30 1M2,L1,L2,L3,M1,M2,DX,DY,DT,N,N1,N3,NASM,IVEL,ICHAR,N1D,LJET,JFLAG,
31 2IERR,IUI,IUO,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TC
32 3,LC,PLOW,ROLOW
33 COMMON /GEMTRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCT,ANGI,ANGE,XW(81),
34 1YW(81),XWI(81),YWI(81),NXNY(81),NWPTS,IINT,1DIF,LT,NDIM
35 COMMON /GCB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,RECB,RCICB,RCTCB,ANGICB
36 1,ANGECB,XCB(81),YCB(81),XCBI(81),YCFI(81),NXNYCB(81),NCBPTS,IINTCB
37 2,1DIFCB,LECB
38 COMMON /BCC/ PT(21),TT(21),THETAA(21),PE,MASSE,MASSI,MASST,THRUST,N
39 3STAG
40 REAL MN3,NXNY,MASSI,MASST,NXNYCB,MASSE
41 NAMELIST /CNTRL/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,TSTOP,GAMMA,RGAS,
```

```

42  1NASM,NAME,NCONVI,NST,IUI,IUO,SMP,IPUNCH,IAV,CAV,NPLOT,IEX,LSS,CTA,
43  2XMU,XLA,RKMU,IUNIT,PLOW,ROLOW
44  NAMELIST /IVS/ U,V,P,RO,NID,NSTART,TSTART,RSTAR,RSTARS
45  NAMELIST /GEMTRY/ NDIM, XI, RI, RT, XE, RCI, RCT, ANGI, ANGE, NGEOM, XWI, YWI
46  1,NWPTS,IINT, IDIF ,LJET,JFLAG,NXNY,YW
47  NAMELIST /GCBL/ NGCB, RICB, RTCB, RCICB, RCTCB, ANGICB, ANGECB, YCB, NXNYC
48  1B, XCB, YCB, NCBPTS, INTCB, IDIFCB
49  NAMELIST /BC/ PT, TT, THETA, PE, NSTAG, ISUPER, UI, VI, PI, ROI
50 C
51 C      READ IN DATA
52 C
53 10 TCONV=0.0 $ FDT=1.0 $ TSTOP=1.0 $ NASM=1 $ NSTAG=0 $ NAME=0
54  IPUNCH=0 $ NGCB=0 $ IINTCB=1 $ IDIFCB=1 $ NSTART=0 $ TSTART=0.0
55  IINT=1 $ IDIF=1 $ NMAX=0 $ NPRINT=0 $ GAMMA=1.4 $ RGAS=53.35
56  NID=1 $ NDIM=1 $ THETA(1)=0.0 $ PE=14.7 $ NST=0 $ N=0 $ IEX=1
57  NCONVI=1 $ IERR=0 * JFLAG=0 $ IUI=1 $ IUO=1 $ SMP=0.95 $ ISUPER=0
58  IAV=0 $ CAV=4.0 $ NPLOT=-1 $ G=32.174 $ PC=144.0 $ TC=460.0
59  LC=12.0 $ IUNIT=0 $ LSS=2 $ CTA=0.5 $ XMU=0.2 $ XLA=1.0
60  RKMU=0.7 $ PLOW=0.01 $ ROLOW=0.0001 $ RSTAR=0.0 $ RSTARS=0.0
61  READ 650, TITLE
62  IF (EOF,5) 20,30
63 20 STOP
64 30 READ (5,CNTRL)
65  READ (5,IVS)
66  READ (5,GEMTRY)
67  READ (5,GCBL)
68  READ (5,BC)
69  IF (NAME,EQ,0) GO TO 40
70  WRITR (6,CNTRL)
71  WRITR (6,IVS)
72  WRITR (6,GEMTRY)
73  WRITR (6,GCBL)
74  WRITR (6, BC)
75 C
76 C      PRINT INPUT DATA
77 C
78 40 PRINT 660
79  PRINT 690
80  PRINT 680
81  PRINT 700
82  PRINT 670
83  PRINT 710, TITLE
84  PRINT 670
85  PRINT 720
86  NPRIND=ABS(FLOAT(NPRINT))
87  PRINT 730,
     IMAX,MMAX,NMAX,NPRIND,TCONV,FDT,NSTAG,NASM,IUNIT,IUI,IUO,IEX,NCONVI,TSTOP,NID,NPLOT,IPUNCH,ISUPER,IAV,CAV,XMU,XLA,RKMU,CTA,LSS,SMP,
88  PRINT 670
89  IF (IUI,EQ,1) PRINT 740, GAMMA,RGAS
90  IF (IUI,EQ,2) PRINT 750, GAMMA,RGAS
91  PRINT 670
92  PRINT 780
93  IF (NDIM,EQ,0) PRINT 790
94  IF (NDIM,EQ,1) PRINT 800
95 C
96 C      CALCULATE THE NOZZLE RADIUS AND NORMAL
97 C
98  PRINT 670
99  CALL GEOM
100 IF (IERR,NE,0) GO TO 10
101 DY=1.0/FLOAT(NMAX-1)
102 IF (NGCB,NE,0) GO TO 60
103 RICB=0.0
104 RTCB=0.0
105 DO 50 L=1,IMAX
106 YCB(L)=0.0
107 NXNYCB(L)=0.0
108 50 CONTINUE
109 GO TO 90
110 60 XICB=XI
111 XECB=XE
112 CALL GEOMCB
113 LT=1 $ XI=XICB $ XE=XECB
114 Y0=0.0
115 DO 80 L=1,IMAX
116 IF (NDIM,EO,0) Y=YW(L)-YCB(L)

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117   IF (NOIM,EO,1) Y=YW(L)**2-YCB(L)**2
118   IF (Y,GT,0.0) GO TO 70
119   PRINT 920
120   GO TO 10
121 70   IF (Y,LT,Y0) LT=L
122   Y0=Y
123 80   CONTINUE
124 90   IF (NSTAG,NE,0) GO TO 110
125   DO 100 M=2,MMAX
126   PT(M)=PT(1)
127   TT(M)=TT(1)
128   THETA(M)=THETA(1)
129 100  CONTINUE
130   PRINT 670
131   IF (IUI,EQ,1) PRINT 760, PT(1),TT(1),THETA(1),PE
132   IF (IUI,EO,2) PRINT 770, PT(1),TT(1),THETA(1),PE
133   GO TO 130
134 110  PRINT 660
135   IF (IUI,EQ,1) PRINT 890, PE
136   IF (IUI,EQ,2) PRINT 770, PE
137   DO 120 M=1,MMAX
138   PRINT 910, M,PT(M),TT(M),THETA(M)
139 120  CONTINUE
140 C
141 C   CONVERT METRIC UNITS TO ENGLISH UNITS
142 C
143 130  IF (IUI,EQ,1) GO TO 180
144   RSTAR=RSTAR/2.54
145   RSTARS=RSTARS/6.4516
146   RGAS=RGAS/5.38032
147   DO 140 M=1,MMAX
148   PT(M)=PT(M)/6.8948
149   TT(M)=(TT(M)+40,0)*9.0/5.0-40.0
150 140  CONTINUE
151   PE=PE/6.8948
152   IF (ISUPER,EQ,0) GO TO 160
153   DO 150 M=1,MMAX
154   UI(M)=UI(M)/0.3048
155   VI(M)=VI(M)/0.3048
156   PI(M)=PI(M)/6.8948
157   ROI(M)=ROI(M)/16.02
158 150  CONTINUE
159 160  IF (NID,NE,0) GO TO 180
160   IF (NSTART,NE,0) GO TO 180
161   DO 170 L=1,LMAX
162   DO 170 M=1,MMAX
163   U(L,M,1)=U(L,M,1)/0.3048
164   V(L,M,1)=V(L,M,1)/0.3048
165   P(L,M,1)=P(L,M,1)/6.8948
166   RO(L,M,1)=RO(L,M,1)/16.02
167 170  CONTINUE
168 C
169 C   CONVERT INPUT DATA UNITS TO INTERNAL UNITS
170 C
171 180  IF (IUNIT,EQ,0) GO TO 190
172   PC=LC=G=1.0
173   TC=0.0
174 190  TCONV=TCONV/100.0
175   T=TSTART*LC
176   TSTOP=TSTOP*LC
177   DO 200 L=1,LMAX
178   XWI(L)=0.0
179 200  CONTINUE
180   DO 210 M=1,MMAX
181   PT(M)=PT(M)*PC
182   TT(M)=TT(M)+TC
183   THETA(M)=THETA(M)*0.0174533
184 210  CONTINUE
185   PE=PE*PC
186   IF (NID,NE,0) GO TO 230
187   DO 220 L=1,LMAX
188   DO 220 M=1,MMAX
189   P(L,M,1)=P(L,M,1)*PC
190   RO(L,M,1)=RO(L,M,1)/G
191 220  CONTINUE
192 230  GAMM=GAMMA/(GAMMA-1.0)

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193      GAM2=(GAMMA-1.0)/2.0
194      IF (ISUPER,EG,0) GO TO 250
195      DO 240 M=1,MMAX
196      U(1,M,1)=UI(M)
197      V(1,M,1)=VI(M)
198      P(1,M,1)=PI(M)*PC
199      RO(1,M,1)=ROI(M)/G
200      U(1,M,2)=U(1,M,1)
201      V(1,M,2)=V(1,M,1)
202      P(1,M,2)=P(1,M,1)
203      RO(1,M,2)=RO(1,M,1)
204 240  CONTINUE
205 250  L1=LMAX-1
206      L2=LMAX-2
207      L3=LMAX-3
208      M1=MMAX-1
209      M2=MMAX-1
210      IF (N1D,EQ,0) GO TO 260
211 C
212 C COMPUTE THE 1-D INITIAL-DATA SURFACE
213 C
214      CALL ONEDIM
215      IF (IERR,NE,0) GO TO 10
216 C
217 C COMPUTE THE INITIAL-DATA SURFACE MASS FLOW AND THRUST
218 C
219 260  IF (NPRINT,GT,0) GO TO 270
220      NPRINT=-NPRINT
221      GO TO 340
222 270  CALL MASFL0 (0)
223 C
224 C CALCULATE AND PRINT THE INITIAL-VALUE SURFACE
225 C
226      DO 330 IU=1,2
227      IF (IUO,EQ,1,AND,IU,EQ,2) GO TO 330
228      IF (IUO,EQ,2,AND,IU,EQ,1) GO TO 330
229      NLINE=0
230      PRINT 660
231      PRINT 810, TSTART,NSTART
232      PRINT 820
233      IF (IU,EQ,1) PRINT 830
234      IF (IU,EQ,2) PRINT 840
235      PRINT 670
236      X=XI-DX
237      DO 300 L=1,LMAX
238      X=X+DX
239      CALL MAP (0,L,1,AL,BE,DE,LD1,AL1,BE1,DE1)
240      DYIO=DY/BE
241      Y=YCEL(L)-DYIO
242      DO 300 M=1,MMAX
243      Y=Y+DYIO
244      VELMAG=SQRT(U(L,M,1)**2+V(L,M,1)**2)
245      XMACH=VELMAG/SQRT(GAMMA*P(L,M,1)/RO(L,M,1))
246      PRES=P(L,M,1)/PC
247      RHO=RO(L,M,1)/G
248      TEMP=P(L,M,1)/RHO/RGAS/TC
249      XP=X
250      YP=Y
251      UP=U(L,M,1)
252      VP=V(L,M,1)
253      IF (IU,EQ,1) GO TO 280
254      XP=XP*2.54
255      YP=YP*2.54
256      UP=UP*0.3048
257      VP=VP*0.3048
258      PRES=PRES*6.8948
259      RHO=RHO*16.02
260      VELMAG=VELMAG*0.3048=
261      TEMP=(TEMP*40.0)*5.0/9.0-40.0
262 280  NLINE=NLINE+1
263      IF (NLINE,LT,55) GO TO 290
264      PRINT 660
265      PRINT 810, TSTART,NSTART
266      PRINT 820
267      IF (IU,EQ,1) PRINT 830
268      IF (IU,EQ,2) PRINT 840

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```

269      PRINT 670
270      NLINE=1
271 290 PRINT 850, L,M,XP,YP,UP,VP,PRES,RHO,VELMAG,XHACH,TEMP
272 300 CONTINUE
273      IF (IU,EQ,2) GO TO 310
274      PRINT 870, MASST,THRUST,MASSI,MASSE
275      GO TO 320
276 310 MASST=MASST*0.4536
277      MASSI=MASSI*0.4536
278      MASSE=MASSE*0.4536
279      THRUST=THRUST*4.4477
280      PRINT 880, MASST,THRUST,MASSI,MASSE
281 320 IF (IUO,NE,3) GO TO 340
282 330 CONTINUE
283 340 IF (NPLOT,LE,0) GO TO 350
284      CALL PLOT (TITLE,TSTART,NSTART)
285      PRINT 1030, NSTART
286 350 IF (NMAX,EQ,0) GO TO 10
287 C
288 C   INITIALIZE THE TIME STFP INTEGRATION LOOP PARAMETERS
289 C
290      N1=1 $ N3=2 $ DQM=0.0 $ NS=0 $ NCONV=0 $ NC=0 $ LDUM=1 $ NPC=0
291      DXR=1.0/DX $ DYR=1.0/DY $ DXRS=DXR*DXR $ DYRS=DYR*DYR
292      LD=81 $ MD=21 $ IMD*LD*MD
293      IF (NASM,NE,0,AND,LT,NE,1) LDUM=LT-1
294      NPD=0
295      IF (JFLAG,EQ,0) GO TO 360
296      UD(1)=U(LJET-1,MMAX,N1)
297      VD(1)=V(LJET-1,MMAX,N1)
298      PD(1)=P(LJET-1,MMAX,N1)
299      ROD(1)=RO(LJET-1,MMAX,N1)
300      UD(2)=UD(1)
301      VD(2)=VD(1)
302      P0(2)=PD(1)
303      ROD(2)=ROD(1)
304 C
305 C   ENTER THE TIME STEP INTERGRATION LOOP
306 C
307 360 DO 580 N=1,NMAX
308      NDP=NPD+1
309      IF (NPD,NE,10) GO TO 370
310      NP=N+NSTART
311      PRINT 1040, NP
312      NPD=0
313 370 CONTINUE
314      LMD1=IMD*(N1-1)
315      LMD3=IMD*(N3-1)
316 C
317 C   CALCULATE DELTA T
318 C
319      DO 380 L=1,LMAX
320          CALL MAP (0,L,MD,AL,BE,DE,LD1,AL1,BE1,DE1)
321          DDXDY=DXRS+BE*BE*DYSR
322          DO 380 M=1,MMAX
323              LMNI=L+LD*(M-1)+LMD1
324              QS=U(LMNI)*U(LMNI)+V(LMNI)*V(LMNI)
325              AS=GAMMA*P(LMNI)/RO(LMNI)
326              UPA=SQRT(QS*DDXY)+SQRT(AS*DDXY)
327              IF (L,EQ,1,AND,M,EQ,1) UPAM=UPA
328              IF (UPA,GT,UPAM) UPAM=UPA
329 380 CONTINUE
330      DT=FDT/UPAM
331      T=T+DT
332      IF (T,LE,TSTOP) GO TO 390
333      T=T-DT
334      DT=TSTOP-T
335      T=TSTOP
336 C
337 C   DETERMINE IF THE EXIT FLOW IS SUBSONIC OR SUPERSONIC
338 C
339 390 IVEL=0
340      IF (QS,GE,AS) IVEL=1
341 C
342 c   CALCULATE THE NOZZLE WALL AND INTERIOR MESH POINTS
343 C
344      IF (IAV,NE,0) CALL SHOCK (1)

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345      ICHAR=1
346      IB=1
347      CALL INTER
348      CALL WALL
349      IF (IERR,NE,0) GO TO 10
350      IF (NGCB,EQ,0) GO TO 400
351      IB=2
352      CALL WALL
353      IF (IERR,NE,0) GO TO 10
354 400    ICHAR=2
355      IB=1
356      CALL INTER
357      CALL WALL
358      IF (IERR,NE,0) GO TO 10
359      IF (NGCB,EQ,0) GO TO 410
360      IB=2
361      CALL WALL
362      IF (IERR,NE,0) GO TO 10
363 C
364 C      EXTRAPOLATE THE EXIT MESH POINTS FOR SUPERSONIC FLOW
365 C
366 410    DO 420 M=1,MMAX
367      U(LMAX,M,N3)=U(L1,M,N3)+IEX*(U(L1,M,N3)-U(L2,M,N3))
368      V(LMAX,M,N3)=V(L1,M,N3)+IEX*(V(L1,M,N3)-V(L2,M,N3))
369      P(LMAX,M,N3)=P(L1,M,N3)+IEX*(P(L1,M,N3)-P(L2,M,N3))
370      RO(LMAX,M,N3)=RO(L1,M,N3)+IEX*RO(U(L1,M,N3)-RO(L2,M,N3))
371      IF (P(LMAX,M,N1),GT,0.0,AND,RO(LMAX,M,N3),GT,0.0) GO TO 420 'MrNI^CT.B.B) GO TO 420
372      P(LMAX,M,N3)=P(L1,M,N3)
373      RO(LMAX,M,N3)=RO(L1,M,N3)
374 420    CONTINUE
375      V(LMAX,MMAX,N3)=U(LMAX,MMAX,N3)*NNY(LMAX)
376      V(LMAX,1,3)=-U(LMAX,1,N3)*NNYCB(LMAX)
377 C
378 C      CALCULATE THE NOZZLE INLET MESH POINTS
379 C
380      IF (ISUPER,EQ,0) CALL INLET
381 C
382 C      CALCULATE THE NOZZLE EXIT MESH POINTS FOR SUBSONIC FLOW
383 C
384      IF (IVEL,EQ,0) CALL EXITT
385      IF (N,LE,NST) CALL SHOCK (2)
386 C
387 C      DETERMINE THE MAXIMUM (DELTA U)/U
388 C
389      IF (TCOVN,LE,0.0) GO TO 440
390      DDQM=0.0
391      DO 430 L=LDUM,LMAX
392      DO 430 M=1,MMAX
393      IF (U(L,M,N1),EQ,0.0) GO TO 43
394      DQ=ABS((U(L,M,N3)-U(L,M,N1))/U(L,M,N1))
395      IF (DQ,GT,DDQM) DDQM=DQ
396 430    CONTINUE
397 440    NC=NC+1
398    NPC=NCP+1
399    IF (DDQM,GE,TCOVN) GO TO 450
400    NCONV=NCONV+1
401    IF (NCONV,EQ,1) NCHECK=N-1
402    IF (NCONV,GE,NCONVI) NC=NPRINT
403 450    IF (N,EQ,NMAX) NC=NPRINT
404    IF (N,GE,NCHECK+NCONVI) NCONV=0
405    IF (T,EQ,TSTOP) NC=NPRINT
406    IF (NC,EQ,NPRINT) GO TO 460
407    IF (NPC,EQ,NPLOT) GO TO 550
408    GO TO 570
409 C
410 C      COMPUTE THE SOLUTION SURFACE MASS FLOW AND THRUST
411 C
412 460    ICN=0
413    IF (JFIAG,EQ,0) GO TO 470
414    IF (LT,NE,LJET-1) GO TO 470
415    UDUM=U(LT,MMAX,N3)
416    RODUM=RO(LT,MMAX,N3)
417    U(LT,MMAX,N3)=UD(3)
418    RO(LT,MMAX,N3)=ROD(3)
419    ICN=1
420 470    CALL MASFLO (1)

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421      IF (ICN,EQ,0) GO TO 480
422      U(LT,MMAX,N3)=UDUM
423      RO(LT,MMAX,N3)=RODUM
424 C
425 C      CALCULATE AND PRINT THE SOLUTION SURFACE
426 C
427 480   DO 540 IU=1,2
428      IF (IUO,EQ,1 ,AND,IU,EQ,2) GO TO 540
429      IF (IUO,EQ,2 ,AND,IU,EQ,1) GO TO 540
430      NLINE=0
431      PRINT 660
432      TIME=T/LC
433      DTIME=DT/LC
434      NP=N|NSTART
435      PRINT 860, NP,TIME,DTIME
436      PRINT 820
437      IF (IU,EQ,1) PRINT 830
438      IF (IU,EQ,2) PRINT 840
439      PRINT 670
440      X=XI-DX
441      DO 510 L=1,IJMAX
442      X=X|DX
443      CALL MAP (0,L,1 ,AL,BE,DE,LD1,AL1,BE1,DE1)
444      DYIO=DY/BE
445      Y=YCB(L)-DYIO
446      DO 510 M=1,MMAX
447      Y=Y|DYIO
448      VELMAG=SQRT(U(L,H,N3)**2+V(L,MN3)**2)
449      XMACH=VELMAG/SQRT(GAMMA*P(L,M,N3)/RO(L,M,N3))
450      PRES=P(L,M,N3)/PC
451      RHO=RO(L,H,N3)*G
452      TEMP=P(L,M,N3)/RHO/RGAS-TC
453      XP=X
454      YP=Y
455      UP=U(L,M,N3)
456      VP=V(L,M,N3)
457      IF (IU,EQ,1) GO TO 490
458      XP=XP*2.54
459      YP=YP*2.54
460      UP=UP*0.3048
461      VP=VP*0.3048
462      PRES=PRES*6.8948
463      RHO=RRHO*16.02
464      VELMAG=VELMAG*0.3048
465      TEMP=(TEMP+40.0)*5.0/9.0-40.0
466 490   NLINE=NLINE+1
467      IF (NLINE,LT,55) GO TO 500
468      PRINT 660
469      PRINT 860, NP,TIME,DTIME
470      PRINT 820
471      IF (IU,EQ,1) PRINT 830
472      IF (IU,EQ,2) PRINT 840
473      PRINT 670
474      NLINE=1
475 500   PRINT 85, L,M,XP,YP,UP,VP,PRES,RHO,VELMAG,XMACH,TEMP
476 510   CONTINUE
477      IF (IU,EQ,2) GO TO 520
478      PRINT 870, MASST,THRUST,MASSI,MASSE
479      GO TO 530
480 520   MASST=MASST*0.4535
481      MASSI=MASSI*0.4535
482      MASSE=MASSE*0.4535
483      THRUST=THRUST*4.4477
484      PRINT 880, MASST,THRUST,MASSI,MASSE
485 530   IF (IUO,NE,3) GO TO 550
486 540   CONTINUE
487 550   IF (NPLOT,LT,0) GO TO 560
488      TIM=T/LC $ NP=N|NSTART
489      CALL PLOT (TITLE,TIME,np)
490      PRINT 1030, NP
491 C
492 C      CHECK FOR CONVERGENCE OF THE STEADY STATE SOLUTION
493 C
494 560   IF (DQM,LT,TCONV) GO TO 590
495      IF (T,EQ,TSTOP) GO TO 590
496      IF (N,EQ,NMAX) GO TO 590

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497      IF (NC,EQ,NPRINT) NC=0
498      IF (NPC,EQ,NPLOT) NPC=0
499 570  CONTINUE
500      NNN=N1
501      N1=N3
502      N3=NNN
503 580  CONTINUE
504 C
505 C      PUNCH A SIVS NAMELIST FOR RESTART
506 C
507 590  IF (NPLOT,GE,0) CALL ADV (10)
508      IF (IPUNCH,EQ,0) GO TO 10
509      DO 600 L=1,LMAX
510      DO 600 M=1,MMAX
511      P(L,M,N3)=P(L,M,N3)/PC
512      RO(L,M,N3)=RO(L,M,N3)*G
513 600  CONTINUE
514      PUNCH 930, NP,TIME
515      DO 610 M=1,MMAX
516      PUNCH 940, M
517      PUNCH 950, (U(L,M,N3),L=1,LMAX)
518 610  CONTINUE
519      DO 620 M=1,MMAX
520      PUNCH 960, M
521      PUNCH 950, (V(L,M,N3),L=1,LMAX)
522 620  CONTINUE
523      DO 630 M=1,MMAX
524      PUNCH 970, M
525      PUNCH 980, (P(L,M,N3),L=1,LMAX)
526 630  CONTINUE
527      DO 640 M=1,MMAX
528      PUNCH 990, M
529      PUNCH 1000, (RO(L,M,N3),L=1,LMAX)
530 640  CONTINUE
531      PUNCH 1010
532      NCARDS=((LMAX/7+2)*MMAX*4+22
533      PRINT 1020, NCARDS
534      GO TO 10
535 C
536 C      FORMAT STATEMENTS
537 C
538 650  FORMAT (8A10)
539 660  FORMAT (1H1)
540 670  FORMAT (1H )
541 680  FORMAT (1H0)
542 690  FORMAT (1H0,15X,NAP, A COMPUTER PROGRAM FOR THE COMPUTATION OF TWO-DIMENSIONAL, TIME-DEPENDENT, INVISCID NOZZLE
FLOW,/,37X,59HBY MICHAEL C. CLINE, T-3 - LOS ALAMOS SCIENTIFIC LABORATORY)
543 700  FORMAT (1H0,10X,18HPROGRAM ABSTRACT 26X,8HTHE EQUATIONS OF MOTION FOR TWO-DIMENSIONAL, TIME DEPENDENT,
INVISCID FLOW IN A NOZZLE,/,21X,9HARE SOLVED USING THE SECOND-ORDER, MACCORMACK, FINITE-DIFFERENCE SCHEME, THE
FLUID IS ASSUMED,/,21X,9HTO BE A PERFECT GAS, ALL BOUNDARY CONDITIONS ARE COMPUTED USING A SECOND-ORDER,
REFERENCE PLANE,/,21X,9HCHARACTERISTIC SCHEME, THE STEADY STATE SOLUTION IS OBTAINED AS THE ASYMPTOTIC SOLUTION
FOR,/,21X,9HARGE TIME, THE NOZZLES MAY BE EITHER CONVERGING, CONVERGING-DIVERGING, OR PLUG GEOMETRIES.)
544 710  FORMAT (1H0,10X,11HJOB TITLE --/21X,8A10)
545 720  FORMAT (1H0,10X,20HCONTROL PARAMETERS --)
546 730  FORMAT
(1H0,20X,5HIMAX=,I2 ,2X,5HMMAX=,I2 ,3X,5HNMAX=,I4 ,2X,7HNPRINT=,I4 ,2X,6HICONV=,F6. 3 ,3X,4HFDT=,F4. 2 ,2X,6HNSTAG=,I1 ,5X,5HNASM=,I1 ,4X,6HIUNIT
547 740  FORMAT (1H0,10X,13HFLUID MODEL --,/,21X,36HTHE RATIO OF SPECIFIC HEATS, GAMMA =,F6.4 ,26H AND THE GAS CONSTANT,
R =,F9.4 ,15H (FT-LBF/LBM-R))
548 750  FORMAT (1H0,10X,13HFLUID MODEL --,/,21X,36HTHE RATIO OF SPECIFIC HEATS, GAMMA =,F6.4 ,26H AND THE GAS CONSTANT,
R =,F9.4 ,9H (J/KG-K))
549 760  FORMAT (1H0,10X,21HBOUNDARY CONDITIONS --,/,21X,3HPT=,F9.4 ,7H (PSIA),5X,3HTT=,F9.4 ,4H (F),5X,6HHTETA=,F9.4 ,6H
(DEG),5X,3HPE=,F9.4 ,7H (PSIA))
550 770  FORMAT (1H0,10X,21HBOUN0ARY CONDITIONS --,/,21X,3HPT=,F9.4 ,6H (KPA),5X,3HTT=,F9.4 ,4H (C),5X,6HHTETA=,F9.4 ,6H
(DEG),5X,3HPE=,F9.4 ,6H (KPA))
551 780  FORMAT (1H0,10X,15HFLOW GEOMETRY --)
552 790  FORMAT (1H0,20X,47HTWO-DIMENSIONAL, PLANAR FLOW HAS BEEN SPECIFIED)
553 800  FORMAT (1H0,20X,36HAXISYMMETRIC FLOW HAS BEEN SPECIFIED)
554 810  FORMAT (1H ,30HINITIAL- DATA SURFACE - TIME = ,F10.8 ,8H SECONDS,4H (N=,I4 ,1H))
555 820  FORMAT (1H0,11X,1HL,4X,1HM,9X,1HX,10X,1HY,10X,1HU,1IX,1HV,12X,1HP,11X,3Hrho,9X,1HQ,11X,4HMACH,8X,1HT)
556 830  FORMAT (1H ,25X,4H(IN) ,7X,4H(IN) ,6X,5H(FPS) ,7X,5H(FPS) ,7X,6H(PSIA) ,6X,9H(LBM/FT3) ,4X,5H(FPS) ,10X,2HNO,8X,3H(F) )
557 840  FORMAT (1H ,25X,4H(CM) ,7X,4H(CM) ,6X,5H(MPS) ,7X,5H(MPS) ,7X,6H (KPA) ,7X,7H(KG/M3) ,5X,5H(MPS) ,10X,2HNO,8X,3H(C) )
558 850  FORMAT (1H ,7X,215 ,4F12.4 ,F13.4 ,F12.6 ,3F12.4 )
559 860  FORMAT (1H ,20HSOLUTION SURFACE NO. ,I5 ,3H - ,7HTIME = ,F10.8 ,20H SECONDS (DELTA T = ,F10.8 ,1H))
560 870  FORMAT (1H0,10X,5HMASS=,F9.4 ,10H (LB/M SEC) ,5X,7HTHRUST=,F11.4 ,6H (LBF) ,5X,6HMASSI=,F9.4 ,5X,6HMASSE=,F9.4 )
561 880  FORMAT (1H0,10X,5HMASS=,F9.4 ,9H (KS/SEC) ,5X,7HTHRUST=,F11.4 ,10H (NEWTONS) ,5X,6HMASSI=,F9.4 ,5X,6HMASSE=,F9.4 )
562 890  FORMAT (1H0,10X,21HBOUNDARY CONDITIONS

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563      900      -,//,.22X,1HM 11X, SHPT(P8IA) ,10X,5HTT(F) ,10X,10HTHETA(DEG) ,10X,3HPE=,F7.3 ,7H (PSIA) ,/
564      910      FORMAT (1H0,10X,21HBOUNDARY CONDITIONS
565      920      -,//,.22X,1HM 11X, 7HPT(KPA) ,12X,5HTT(C) ,10X,10HTHETA(DEC) ,10X,3HPE=,F7.3 ,6H (KPA) ,/
566      930      FORMAT (1H ,20X,I2,10X,F7.2 ,10X,F7.2 ,10X,F7.2 )
567      940      FORMAT (1H0,78H***** THE RADIUS OF THE CENTERBOOY IS LARGER THAN THE NOZZLE WALL RADIUS *****)
568      950      FORMAT (1X,18HSIVS NID=0,NSTART=,I4 ,8H,TSTART=,F14.10 ,1H,)
569      960      FORMAT (1X,4HV(1 ,,I2 ,5H,1) =)
570      970      FORMAT (1X,4HP(1 ,,I2 ,5H,1) =)
571      980      FORMAT (1X,7(F10.4 ,1H,)) )
572      990      FORMAT (1X,4HRHO(1 ,,I2 ,5H,1) =)
573     1000      FORMAT (1X,7(F10.6 ,1H,)) )
574     1010      FORMAT (1X,1HS)
575     1020      FORMAT (1H0,27H***** EXPECT APPROXIMATELY ,I4 ,20H PUNCHED CARDS *****)
576     1030      FORMAT (1H0,31H***** EXPECT FILM OUTPUT FOR N=,I4 ,6H *****)
577     1040      FORMAT (1H ,2HN=,14)
578      END

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B.2 Geometry Subroutine (geom.f)

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1 SUBROUTINE GEOM GEO
2 C GEO
3 C **** GEO
4 C **** GEO
5 C THIS SUBROUTINE CALCULATES THE NOZZLE RADIUS AND OUTER NORMAL GEO
6 C **** GEO
7 C **** GEO
8 C **** GEO
9 COMMON /AV/ IAV,CAV,NST,SMP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81,GEO
10 1,21),QPT(81,21) GEO
11 COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4) GEO
12 COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RO(81,21,2) GEO
13 COMMON /CNTRL/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAM1,GAGEO
14 1M2,L1,L2,L3,M1,M2,DX,DY,DT,N,N1,N3,NASM,IVEL,ICHAR,N1D,LJET,JFLAG,GEO
15 2IERR,IUI,IUO,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TCGEO
16 3,LC,PLOW,ROLW GEO
17 COMMON /GEMIRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCT,ANGI,ANGEXW(81),GEO
18 YW(81),XWI(81),YWI(81),NNXY(81),NWPTS,IINT,1DIF,LT,NDIM GEO
19 COMMON /GCB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,REC8,RCICB,RCTCB,ANGICBEGEO
20 2,ANGEBC,XCB(81),YCB(81),XCB(81),YCB(81),NNNYCB(81),NCBPTS,IINTCBGEO
21 3,1DIFCB,LCBC GEO
22 COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASSI,MASST,THRUST,NGEO
23 1STAG GEO
24 REAL MN3,NXNY,MASSI,MASST,NXNYCB,MASSE GEO
25 C GEO
26 GO TO (10,30,120,170),NGEOM GEO
27 C GEO
28 C CONSTANT AREA DUCT CASE GEO
29 C GEO
30 10 PRINT 230 GEO
31 IF (IUI,EQ,1) PRINT 250, XI,RI,XE GEO
32 IF (IUI,EQ,2) PRINT 260, XI,RI,XE GEO
33 LT=LMAX GEO
34 DX=(XE-XI)/(LMAX-1) GEO
35 XT=XE GEO
36 RT=RI GEO
37 RE=RI GEO
38 DO 20 L=1,LMAX GEO
39 YWL)=RI GEO
40 NXNY(L)=0.0 GEO
41 20 CONTINUE GEO
42 IF (JFLAG,EQ,0) GO TO 210 GEO
43 C GEO
44 XWL=XI+(LJET-2)*DX GEO
45 IF (IUI,EQ,1) PRINT 370, XWL,LJET,LMAX GEO
46 IF (IUI,EQ,2) PRINT 380, XWL,LJET,LMAX GEO
47 GO TO 210 GEO
48 C GEO
49 C CIRCULAR-ARC, CONICAL NOZZLE CASE GEO
50 C GEO
51 30 PRINT 230 GEO

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52      IF (RCI,EQ,0.0,OR,RCT,EQ,0.0) GO TO 200           GEO 520
53      ANI=ANGI*3.141593/180.0                          GEO 530
54      ANE=ANGE*3.141593/180.0                          GEO 540
55      XTAN=XI+RCI*SIN(ANI)                           GEO 550
56      RTAN=RI+RCI*(COS(ANI)-1.0)                      GEO 560
57      RT1=RT-RCT*(COS(ANI)-1.0)                      GEO 570
58      XT1=XTAN+(RTAN-RT1)/TAN(ANI)                   GEO 580
59      IF (XT1,GE,XTAN) GO TO 40                      GEO 590
60      XT1=XTAN                                         GEO 600
61      RT1=RTAN                                         GEO 610
62 40     XT=XT1+RCT*SIN(ANI)                         GEO 620
63     XT2=XT+RCT*SIN(ANE)                           GEO 630
64     RT2=RT+RCT*(1.0-COS(ANE))                     GEO 640
65     RE=RT2+(XE-XT2)*TAN(ANE)                      GEO 650
66     LT=1                                            GEO 660
67     DX=(XE-XI)/(LMAX-1)                           GEO 670
68     IF (IUI,EQ,1) PRINT 270, XI,RI,RT,XE,RCI,RCT,ANGI,ANGE,XT,RE GEO 680
69     IF (IUI,EQ,2) PRINT 280, XI,RI,RT,XE,RCI,RCT,ANGI,ANGE,XT,RE GEO 690
70     DO 110 L=1,LMAX                                GEO 700
71     X=XI+(L-1)*DX                                  GEO 710
72     IF (X,GE,XI,AND,X,LE,XTAN) GO TO 50          GEO 720
73     IF (X,GT,XTAN,AND,X,LE,XT1) GO TO 60          GEO 730
74     IF (X,GT,XT1,AND,X,LE,XT) GO TO 70          GEO 740
75     IF (X,GT,XT1,AND,X,LE,XT2) GO TO 80          GEO 750
76     IF (X,GT,XT2,AND,X,LE,XE) GO TO 90          GEO 760
77 C
78 50     YW(L)=RI+RC*(COS(ASIN((X-XI)/RCI))-1.0)    GEO 780
79     NXNY(L)=(XI-XI)/(YW(L)-RI+RCI)                GEO 790
80     GO TO 100                                     GEO 800
81 C
82 60     YW(L)=RT1+(XT1-X)*TAN(ANI)                 GEO 810
83     NXNY(L)=TAN(ANI)                            GEO 820
84     GO TO 100                                     GEO 830
85 C

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B.3 Inlet Boundary Conditions (inlet.f)

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1 SUBROUTINE INLET
2 C ****
3 C
4 C THIS SUBROUTINE CALCULATES THE BOUNDARY MESH POINTS AT THE NOZZLE
5 C INLET FOR SUBSONIC FLOW
6 C ****
7 C ****
8 C
9 COMMON /AV/ IAV,CAV,NST,SMP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81
10   1,21),QPT(81,21)
11 COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)
12 COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RO(81,21,2)
13 COMMON /CNTRL/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAMI,GA
14 1M2,L1,L2,L3,MI,M2,DX,DY,DT,N,N1,N3,NASM,IVEL,ICHAR,N1D,LJET,JFLAG,
15 2IERR,IU1,IUO,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TC
16 3,LC,PLOW,ROLW
17 COMMON /GEMIRYC/ NGEOM, XI, RI, XT, RT, XE, RE, RCI, RCT, ANGI, ANGE, XW(81),
18 1YW(81), XWI(81), YWI(81), NXNY(81), NWPTS, IINT, IDIF, LT, NDIM
19 COMMON /GCB/ NGCB, XICB, RICB, XTCB, RTCB, XECB, RECB, RCICB, RCTCB, ANGICB
20 1, ANGECB, XCB(81), YCB(81), XCBI(81), YCBI(81), NXNYCB(81), NCBPTS, IINTCB
21 2, IDIFCB, LECB
22 COMMON /BCC/ PT(21), TT(21), THETA(21), PE, MASSE, MASSI, MASST, THRUST, N
23 1STAG
24 REAL MN3,NXNY,MASSI,MASST,NXNYCB,MASSE
25 C
26 GRGB=GAMMA*RGAS*G
27 X3=XI
28 ATERM2=0.0
29 ATERM3=0.0
30 DO 180 ICHAR=1,2
31 DO 180 M=1,MMAX
32 LMN1=1+LD*(M-1)+LMD1
33 LMN3=1+LD*(M-1)+LMD3
34 LMN1=2+LD*(M-1)+LMD1
35 LMN1=2+LD*(M-2)+LMD1

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36      LM1N1=1+LD*(M-2)+LMD1
37      LMN3=1+LD*M*LMN3
38      CALL MAP (2,1,M,AL,BE,DE,2,AL1,BE1,DE1)
39      U2=U(LMN1)
40      A2=SQRT(GAMMA*P(LMN1)/RO(LMN1))
41      IF (ICHAR,EQ,2) GO TO 10
42      U(LMN3)=U2
43      V(LMN3)=V(LMN1)
44      A3=A2
45 C
46 C   CALCULATE THE PROPERTY INTERPOLATING POLYNOMIAL COEFFICIENTS
47 C
48 10     BU=(U(L1MN1)-U(LMN1))*DXR
49     BV=(V(L1MN1)-V(LMN1))*DXR
50     BU=(P(L1MN1)-P(LMN1))*DXR
51     BRO=(RO(L1MN1)-(LMN1))*DXR
52     BYCB=(YCB(2)-YCB(1))*DXR
53     BAL=(AL1-AL)*DXR
54     BBE=(BE1-BE)*DXR
55     CU=U(1,M,N1)-BU*X3
56     CV=V(1,M,N1)-BV*X3
57     CP=P(1,M,N1)-B*X3
58     CRO=RO(1,M,N1)-BRO*X3
59     CYCB=YCB(1)-BYCB*X3
60     CAL=AL-BAL*X3
61     CBE=BE-BBE*X3
62 C
63 C   CALCULATE THE CROSS DERIVATIVE INTERPOLATING POLYNOMIAL
64 C   COEFFICIENTS
65 C
66     IF (M,EQ,1) GO TO 20
67     DU=(U(L1MN1)-U(LMN1))*DYR
68     DV=(V(L1MN1)-V(LMN1))*DYR
69     DP=(P(L1MN1)-P(LMN1))*DYR
70     DRO=(RO(L1MN1)-RO(LMN1))*DYR
71     DUI=(U(LMN1)-U(LMN1))*DYR
72     DV1=(V(LMN1)-V(LMN1))*DYR
73     DP1=(P(LMN1)-P(LMN1))*DYR
74     DROI=(RO(LMN1)-RO(LMN1))*DYR
75     GO TO 40
76 20     IF (NGCB,NE,0) GO TO 30
77     DU=0.0
78     DV=V(2,2,N1)*DYR
79     DP=0.0
80     DRO=0.0
81     DUI=0.0
82     DV1=V(1,2,N1)*DYR
83     DP1=0.0
84     DROI=0.0
85     GO TO 40
86 30     DU=(U(2,2,N1)-U(2,1,N1))*DYR
87     DV=(V(2,2,N1)-V(2,1,N1))*DYR
88     DP=(P(2,2,N1)-P(2,1,N1))*DYR
89     DRO=(RO(2,2,N1)-RO(2,1,N1))*DYR
90     DUI=(U(1,2,N1)-U(1,1,N1))*DYR
91     DV1=(V(1,2,N1)-V(1,1,N1))*DYR
92     DP1=(P(1,2,N1)-P(1,1,N1))*DYR
93     DROI=(RO(1,2,N1)-RO(1,1,N1))*DYR
94 40     BDU=(DU-DUI)*DXR
95     BDV=(DV-DV1)*DXR
96     BDP=(DP-DP1)*DXR
97     BDRO=(DRO-DROI)*DXR
98     CDU=DUI-BDU*X3
99     CDV=DV1-BDV*X3
100    CDP=DP1-BDP*X3
101    CDRO=DROI-BD*X3
102 C
103 C   CALCULATE X2
104 C
105    IF (ICHAR,EQ,2) A3=SQRT(GAMMA*P(LMN3)/RO(LMN3))
106    DO 50 IL=1,2
107    X2=X3-(U(1,M,N3)-A3+U2-A2)*0.5*DT
108 C
109 C   INTERPOLATE FOR THE PROPERTIES
110 C
111    U2=BU*X2+CU

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112      P2=BP*X2+CP
113      RO2=BRO*X2+CRO
114      A2=SQRT(GAMMA*P2/RO2)
115 50    CONTINUE
116      V2=BV*X2+CV
117      YCB2=BYCB*X2+CYCB
118      AL2=BAL*X2+CAL
119      BE2=BBE*X2+CBE
120      UV2=U2*AL2+V2*BE2
121 C
122 C   INTERPOLATE FOR THE CROSS DERIVATIVES
123 C
124      DU2=BDU*X2+CDU
125      DV2=BDV*X2+CDV
126      DP2=BDP*X2+CDP
127      DRO2=BDRO*X2+CDRO
128 C
129 C   CALCULATE THE PSI TERMS
130 C
131      IF (NDIM,EQ,0) GO TO 70
132      IF (M,EQ,1,AND,NGCB,EQ,0) GO TO 60
133      ATERM2=RO2*V2 / (DY*(M-1) / (BE2+YCB2))
134      GO TO 70
135 60    ATERM2=RO2*BE2*DV2
136 70    PSI12=-UV2*DRO2-RO2*AL2*DU2-RO2*BE2*DV2-ATERM2
137    PSI22=-UV2*DU2-AL2*DP2/RO2
138    PSI42=-UV2*DP2+A2*A2*UV2*DRO2
139    IF (CHAR,EQ,1) GO TO 130
140 C
141 C   CALCULATE THE CROSS DERIVATIVES AT THE SOLUTION POINT
142 C
143      IF (M,EQ,1,AND,NGCB,EQ,0) GO TO 80
144      IF (M,EQ,MMAX) GO TO 90
145      DU3=(U(LMN3)-U(LMN3))*DYL
146      DV3=(V(LMN3)-V(LMN3))*DYL
147      DP3=(P(LMN3)-P(LMN3))*DYL
148      DRO3=(RO(LMN3)-RO(LMN3))*DYL
149      GO TO 100
150 80    DU3=0.0
151    DV3=V(1,2,N3)*DYL
152    DP3=0.0
153    DRO3=0.0
154    GO TO 100
155 90    DU3=(U(1,MMAX,N3)-U(1,M1,N3))*DYL
156    DV3=(V(1,MMAX,N3)-V(1,M1,N3))*DYL
157    DP3=(P(1,MMAX,N3)-P(1,M1,N3))*DYL
158    DRO3=(RO(1,MMAX,N3)-(1,M1,N3))*DYL
159 C
160 C   CALCULATE THE PSI TERMS AT THE SOLUTION POINT
161 C
162 100   IF (NDIM,EQ,0) GO TO 120
163     IF (M,EQ,1,AND,NGCB,EQ,0) GO TO 110
164     ATERM3=RO(LMN3)*V(LMN3) / (DY*M-1) / BE+YCB(1)
165     GO TO 120
166 110   ATERM3=RO(LMN3)*BE*DV3
167 120   UV3=U(LMN3)*AL-V(LMN3)*BE
168     PSI13=-UV3*DRO3-RO(LMN3)*AL*DU3-RO(LMN3)*BE*DV3-ATERM3
169     PSI23=-UV3*DU3-AL*DP3/RO(LMN3)
170     PSI43=-UV3*DP3+A3*A3*UV3*DRO3
171     GO TO 140
172 130   PSI23=PSI22
173     PSI43=PSI42
174     PSI13=PSI12
175 C
176 C   SOLVE THE COMPATIBILITY EQUATIONS FOR U,V,P, AND RO
177 C
178 140   MN3=SQRT(U(LMN3)*U(LMN3)+V(LMN3)*V(LMN3)) / A3
179     T2=P2 / (RO2*RGAS*G)
180     PSI1B=(PSI12+PSI13)*0.5
181     PSI2B=(PSI22+PSI23)*0.5
182     PSI4B=(PSI42+PSI43)*0.5
183     GPSI1B=GAMMA*PSI1B
184     TTHETA=TAN(THETA(M))
185     UCORR=0.5+0.5/SQRT(1.0+TTHETA*TTHETA)
186 C
187     DO 160 ITER=1,20

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```

188 DEM= (1 , 0+GAM2*MN3*MN3)
189 P(LMN3)=PT(M) / (DEM*GAMI)
190 T3=TT(M) /DEM
191 PB=(P2+P(LMN3)) *0 . 5
192 RTB=RGAS*(T2+T3)*0 . 5*G
193 U(LMN3)=U2+DT*PSI2B+(P(LMN3)-P2-(PSI4B+RTB*GPSI1B)*DT)*SQRT(RTB/GA
194 MMA)/PB
195 U(LMN3)=U(LMN3)*UCORR
196 V(LMN3)=-U(LMN3)*TTTHETA
197 OMN3=MN3
198 MN3=SQRT((U(LMN3)*U(LMN3)+V(LMN3)*V(LMN3))/(T3*GRGB))
199 IF (OMN3,NE,0.0) GO TO 150
200 IF (ABS(MN3-OMN3),LE,0.0001) GO TO 170
201 GO TO 160
202 150 IF (ABS((MN3-OMN3)/OMN3),LE,0.001) GO TO 170
203 160 CONTINUE
204 C
205 PRINT 190, M,N
206 170 RO(LMN3)=P(LMN3)/(RGAS*T3*G)
207 180 CONTINUE
208 RETURN
209 C
210 190 FORMAT (1H0,58H***** THE SOLUTION FOR NOZZLE ENTRANCE BOUNDARY POI
211 1NT ( 1,,I2,1H,,I4,43H) FAILED TO CONVERGE IN 20 ITERATIONS *****)
212 END

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B.4 Wall Boundary Conditions (wall.f)

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1 SUBROUTINE WALL
2 C
3 C ****
4 C
5 C THIS SUBROUTINE CALCULATES THE BOUNDARY MESH POINTS AT THE NOZZLE
6 C WALL, EXHAUST JET BOUNDARY, AND CENTERBODY
7 C
8 C ****
9 C
10 COMMON /AV/ IAV,CAV,NST,SMP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81
11 1,21),OPT(81,21)
12 COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)
13 COMMON /SOLUTIN/ U(81,21,2),V(81,21,2),P(81,21,2),RO(81,21,2)
14 COMMON /CNTRL/ LMAX,MMAX,NMAX,NPRINT,TCOINV,FDT,GAMMA,RGAS,GAMI,GA
15 1M2,L1,L2,L3,M1,M2,DY,DT,N,N1,N3,NASM,IVEL,ICHAR,N1D,LJET,JFLAG,
16 2IERR,IUI,IUO,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TC
17 3,LC,PLOW,ROLOW
18 COMMON /GEMTRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCT,ANGI,ANGE,XW(81),
19 1NW(81),XWI(81),YWI(81),NNXY(81),NPPTS,IINT,IDIF,LT,NDIM
20 COMMON /GCB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,RECB,RCICB,RCTCB,ANGICB
21 2,ANGECB,XCB(81),YCB(81),XCBI(81),YCEB(81),NNNYCB(81),NCBPTS,IINTCB
22 3,IDIIFCB,LECB
23 COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASSI,MASST,THRUST,N
24 1STAG
25 REAL MN3,NXNY,MASSI,MASST,NXNYCB,MASSE
26 C
27 IF (N.EQ.1) DELY=0.005
28 XWID=0.0
29 IF (IB.EQ.1) GO TO 10
30 Y1=0.0 $ Y3=0.0 $ MDUM1=1 $ MDUM1=2 $ SIGN=-1.0
31 GO TO 20
32 10 Y1=1.0 $ Y3=1.0 $ MDUM1=MMAX $ NDUM1=M1 $ SIGN=1.0
33 20 ATERM2=0.0
34 ATERM3=0.0
35 LDUM=LMAX
36 IF (ICHAR.EQ.2) LDUM=L1
37 LMDM1=LD*(MDUM1)
38 LMDM1=LD*(MDUM1-1)
39 DYS=SIGN*DYR
40 DO 350 L=2,LDUM
41 LMN1=L+LMDM1+LMD1
42 LMN3=L+LMDM1+LMD3
43 LMN1=L+LMDM1+LMD1
44 LMN1=L-1+LMDM1+LMD1

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45      L1MN3=L+1+LMDM+LMD3
46      L1MN1=L-1+LMDM+LMD1
47      IF (JFLAG.EQ.0) GO TO 50
48      IF (IB.EQ.2) GO TO 50
49 C
50      XWID=WXI(L)
51      IF (ICHAR.EQ.1) GO TO 30
52 C
53 C USE THE DUMMY ARRAYS TO MANIPULATE THE ONE-SIDED SOLUTIONS
54 C
55      IF (L.NE.LJET-2) GO TO 30
56      U(L1MN3)=UD(3)
57      V(L1MN3)=VD(3)
58      P(L1MN3)=PD(3)
59      RO(L1MN3)=ROD(3)
60      GO TO 50
61 30   IF (L.NE.LJET-1) GO TO 40
62      IF (ICHAR.EQ.1) UOLD=U(LMN1)
63      U(LMN1)=UD(1)
64      V(LMN1)=VD(1)
65      P(LMN1)=PD(1)
66      RO(LMN1)=ROD(1)
67      GO TO 50
68 40   IF (L.EQ.LJET) GO TO 50
69      U(LMN1)=UD(2)
70      V(LMN1)=VD(2)
71      P(LMN1)=PD(2)
72      RO(LMN1)=ROD(2)
73 C
74 50   U1=U(LMN1)
75   V1=V(LMN1)
76   P1=P(LMN1)
77   RO1=RO(LMN1)
78   U2=U1
79   V2=V1
80   A1=SQRT(GAMMA*P1/RO1)
81   A2=A1
82   IF (ICHAR.EQ.2) GO TO 60
83   U3=U1
84   V3=V1
85   P3=P1
86   RO3=RO1
87   A3=A1
88   GO TO 70
89 60   U3=U(LMN3)
90   V3=V(LMN3)
91   P3=P(LMN3)
92   RO3=RO(LMN3)
93   A3=SQRT(GAMMA*P3/RO3)
94 C
95 C CALCULATE THE PROPERTY INTERPOLATING POLYNOMIAL COEFFICIENTS
96 C
97 70   BU=(U1-U(LMN1))*DYS
98   BV=(V1-V(LMN1))*DYS
99   BP=(P1-P(LMN1))*DYS
100  BRO=(RO1-RO(LMN1))*DYS
101  CU=U1-BU*Y3
102  CV=V1-BV*Y3
103  CP=P1-BP*Y3
104  CRO=RO1-BRO*Y3
105 C
106 C CALCULATE THE CROSS DERIVATIVE INTERPOLATING POLYNOMIAL
107 C COEFFICIENTS
108 C
109  DU=(U1-U(LMN1))*DXR
110  DV=(V1-V(LMN1))*DXR
111  DP=(P1-P(LMN1))*DXR
112  DRO=(RO1-RO(LMN1))*DXR
113  DU1=(U(LMN1)-U(LMN1))*DXR
114  DV1=(V(LMN1)-V(LMN1))*DXR
115  DP1=(P(LMN1)-P(LMN1))*DXR
116  DRO1=(RO(LMN1)-RO(LMN1))*DXR
117  BDU=(DU-DU1)*DYS
118  BDV=(DV-DV1)*DYS
119  BDP=(DP-DP1)*DYS
120  BDRO=(DRO-DRO1)*DYS

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121      CDU=DU-BDU*Y3
122      CDV=DV-BDV*Y3
123      CDP=DP-BDP*Y3
124      CDRO=DRO-BDRO*Y3
125      C
126      C   CALCULATE Y2
127      C
128      CALL MAP (1,L,MDUM,AL,BEW,DE,LD1,AL1,BE1,DE1)
129      ALS=SQRT(AL*AL+BE*BE)
130      UV3=U3*AL+V3*BE+DE
131      AL2=AL
132      DO 90 ILL=1,3
133      UV2=U2*AL2+V2*BE+DE
134      Y2=Y3- (UV2+SIGN*AL*ALS*A2+UV3+SIGN*ALS*A3)*DT*0.5
135      C
136      C   INTERPOLATE FOR THE PROPERTIES
137      C
138      U2=BU*Y2+CU
139      V2=BV*Y2+CV
140      P2=BP*Y2+CP
141      RO2=BDRO*Y2+CRO
142      AL2=Y2*AL
143      AD=GAMMA*P2/RO2
144      IF (AD.GT.0.0) GO TO 80
145      PRINT 360, N,L,MDUM
146      IERR=1
147      RETURN
148      80 A2=SQRT(AD)
149      90 CONTINUE
150      C
151      C   INTERPOLATE FOR THE CROSS DERIVATIVES
152      C
153      DU1=DU
154      DV1=DV
155      DP1=DP
156      DRO1=DRO
157      DU2=BDU*Y2+CDU
158      DV2=BDV*Y2+CDV
159      DP2=BDP*Y2+CDP
160      DRO2=BDRO*Y2+CDRO
161      C
162      C   CALCULATE THE PSI TERMS
163      C
164      IF (NDIM.EQ.0) TO TO 110
165      IF (IB.EQ.2) GO TO 100
166      ATERM2=RO2*V2/(YCB(L)+Y2/BE)
167      GO TO 110
168      100 ATERM2=RO2*V2/(YCB(L)+Y2/BE)
169      IF (IAV.EQ.0) GO TO 110
170      ATDS=RO2*V(L,2,N1)*DYR*BE
171      IF (ABS(ATERM2).GT.ABS(ATDS)) ATERM2=ATDS
172      C
173      110 PSI21=-U1*DU1-DP1/RO1
174      PSI31=-U1*DVI
175      PSI41=-U1*DP1+A1*A1*U1*DRO1
176      PSI12=-U2*DRO2-RO2*DU2-ATERM2
177      PSI22=-U2*DU2-DP2/RO2
178      PSI32=-U2/DV2
179      PSI42=-U2*DP2+A2*A2*U2*DRO2
180      IF (ICHAR.EQ.1) GO TO 150
181      C
182      C   CALCULATE THE CROSS DERIVATIVES AT THE SOLUTION POINT
183      C
184      IF (JFLAG.EQ.0) GO TO 120
185      IF (IB.EQ.2) GO TO 120
186      IF (L.EQ.2) GO TO 120
187      IF (L.NE.LJET-1) GO TO 120
188      IF (ILJET.EQ.2) GO TO 120
189      GO TO 130
190      120 DU3=(U(LIMN3)-U3)*DXR
191      DV3=(V(LIMN3)-V3)*DXR
192      DP3=(P(LIMN3)-P3)*DXR
193      DRO3=(RO(LIMN3)-RO3)*DXR
194      GO TO 140
195      130 DU3=(U3-U(L-1,MDUM,N3))*DXR
196      DV3=(V3-V(L-1,MDUM,N3))*DXR

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197      DP3=(P3-P(L-1,MDUM,N3))*DXR
198      DRO3=(RO3-RO(L-1,MDUM,N3))*DXR
199 C
200 C   ENTER THE EXHAUST JET ITERATION LOOP
201 C
202 140 IF (JFLAG.EQ.0) GO TO 150
203     IF (IB.EQ.2) GO TO 150
204     IF (L.LT.LJET) GO TO 150
205     YWI(L)=YW(L)
206     UDUM=U(LMN3)
207     VDUM=V(LMN3)
208     PDUM=P(LMN3)
209     RODUM=RO(LMN3)
210 150 DO 290 NJ=1,10
211     IF (ICAR.EQ.1) GO TO 250
212     IF (JFLAG.EQ.0) GO TO 210
213     IF (IB.EQ.2) GO TO 210
214     IF (L.LT.LJET) GO TO 210
215     IF (NJ.EQ.1) GO TO 200
216     IF (NJ.GT.2) GO TO 180
217 160 YWOLD=YW(L)
218     POLD=P(LMN3)
219     IF (P(LMN3).LT.PE) GO TO 170
220     YW(L)=YW(L)+DELY
221     GO TO 190
222 170 YW(L)=YW(L)-DELY
223     GO TO 190
224 180 IF (P(LMN3).EQ.POLD) GO TO 160
225     DYDP=(YW(L)-YWOLD)/(P(LMN3)-POLD)
226     YNEW=YW(L)+DYDP*(PE-P(LMN3))
227     YWOLD=YW(L)
228     POLD=P(LMN3)
229     YW(L)=YNEW
230 190 IF (YW(L).LT.(0.98*YWOLD)) YW(L)=0.98*YWOLD
231     IF (YW(L).GT.(1.02*YWOLD)) YW(L)=1.02*YWOLD
232 200 NXNY(L)=(YW(L)-YW(L-1))*DXR
233     XWI(L)=(YW(L)-YWI(L))/DT
234     XWID=XWI(L)
235     CALL MAP(1,L,MDUM,AL,BEW,DE,LD1,AL1,BE1,DE1)
236     ALS=SQRT(AL*AL+BE*BE)
237     U(LMN3)=UDUM
238     V(LMN3)=VDUM
239     P(LMN3)=PDUM
240     RO(LMN3)=RODUM
241 C
242 C   CALCULATE THE PSI TERMS AT THE SOLUTION POINT
243 C
244 210 IF (NDIM.EQ.0) GO TO 240
245     IF (IB.EQ.2) GO TO 220
246     ATERM3=RO3*V2/(YCB(L)+1.0/BE)
247     GO TO 240
248 220 IF (YCB(L).EQ.0.0) GO TO 230
249     ATERM3=RO3*V3/YCB(L)
250     IF (IAV.EQ.0) GO TO 240
251     ATDS=RO3*V(L,2,N3)*DYR*BE
252     IF (ABS(ATERM3).GT.ABS(ATDS)) ATERMS=ATDS
253     GO TO 240
254 230 ATERMS=RO3*V(L,2,N3)*DYR*BE
255 C
256 240 PSI13=-U3*DRO3-RO3*DU3-ATERM3
257     PSI23=-U3*DU3-DP3/RP3
258     PSI33=-U3*DV3
259     PSI43=-U3*DP3+A3*A3*U3*DRO3
260 C   CALCULATE THE COMPATIBILITY EQUATION COEFFICIENTS
261 C
262 250 ABR=NXNY(L)
263     IF (IB.EQ.2) ABR=NXNYCB(L)
264     ALB=0.5*(AL2+AL)/ALS
265     BEB=BE/ALS
266     A1B=(A1+A3)*0.5
267     A2B=(A2+A3)*0.5
268     RO1B=(RO1+RO3)*0.5
269     RO2B=(RO2+RO3)*0.5
270     IF (ICAR.eq.1) GO TO 260
271     PSI21B=(PSI21+PSI23)*0.5
272     PSI31B=(PSI31+PSI33)*0.5

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273   PSI41B=(PSI41+PSI43)*0.5
274   PSI12B=(PSI12+PSI13)*0.5
275   PSI22B=(PSI22+PSI23)*0.5
276   PSI32B=(PSI32+PSI33)*0.5
277   PSI42B=(PSI42+PSI43)*0.5
278   GO TO 270
279 260   PSI21B=PSI21
280   PSI31B=PSI31
281   PSI41B=PSI41
282   PSI12B=PSI12
283   PSI12B=PSI12
284   PSI22B=PSI22
285   PSI32B=PSI32
286   PSI42B=PSI42
287 C
288 C   SOLVE THE COMPATIBILITY EQUATIONS FOR U,V,P, AND RO
289 C
290 270   U(LMN3)=(U(LMN1)-ABR*(V(LMN1)-XWID)+(PSI21B-ABR*PSI31B)*DT)/(1.0+A
291   1BR*ABR)
292   V(LMN3)=-U(LMN3)*ABR+XWID
293   P(LMN3)=P2-SIGN*RO2B*A2B*(ALB*(U(LMN3)-U2)+BEB*(V(LMN3)-V2))+(PSI4
294   22B+A2B*A2B+PSI12B+SIGN*RO2B*A2B*(ALB*PSI22B+BEB*PSI32B))*DT
295   IF (P(LMN3).LE.0.0) P(LMN3)=PLOW*PC
296   RO(LMN3)=RO(LMN1)+(P(LMN3)-P(LMN1)-PSI41B*DT)/(A1B**A1B)
297   IF (RO(LMN3).LE.0.0) RO(LMN3)=ROLOW/G
298   IF (IAV.EQ.0) GO TO 280
299 C
300 C   ADD THE ARTIFICIAL VISCOSITY FOR SHOCK CALCULATIONS
301 C
302   IF (ICHAR.EQ.1) GO TO 280
303   U(LMN3)=U(LMN3)+(QUIT(L,MDUM)-ABR*QVT(L,MDUM))/(1.0+ABR*ABR)
304   V(LMN3)=-U(LMN3)*ABR
305   P(LMN3)=P(LMN3)+QPT(L,MDUM)
306 280   IF (JFLAG.EQ.0) GO TO 350
307   IF (IB.EQ.2) GO TO 350
308   IF (L.LT.LJET-1) GO TO 350
309   IF (L.EQ.LJET-1) GO TO 300
310   IF (ICHAR.EQ.1) GO TO 350
311   DELP=ABS((P(LMN3)-PE)/PE)
312   IF (DELP.LE.0.001) GO TO 350
313 290   CONTINUE
314   GO TO 350
315 C
316 C   SOLVE THE COMPATIBILITY EQUATIONS FOR THE DOWNSTREAM SIDE OF THE
317 C   NOZZLE WALL EXIT POINT
318 C
319 300   UD(3)=U(LMN3)
320   VD(3)=V(LMN3)
321   PD(3)=P(LMN3)
322   ROD(3)=RO(LMN3)
323   PD(4)=PE
324   XM1=SQRT((UD(3)*UD(3)+VD(3)*VD(3))/(GAMMA*PD(3)/ROD(3)))
325   DUMD=1.0+GAM2*XM1*XMI
326   TD=PD(3)/ROD(3)/RGAS/G
327   TTD=TD*DUMD
328   IF (PE.GT.PD(3).AND.XM1.GE.1.0) GO TO 310
329   TTD=TD*DUMD
330   IF (PE.GT.PD(3).AND.XM1.GE.1.0) GO TO 310
331   PTD=PD(3)*DUMD**GAM1
332   ROD(4)=ROD(3)*(PE/PD(3))**((1.0/GAMMA))
333   GO TO 320
334 310   PRD=PE/PD(3)
335   GAMD=(GAMMA+1.0)/(GAMMA-1.0)
336   ROD(4)=ROD(3)*(GAMD*PRD+1.0)/(PRD+GAMD)
337 320   TE=PE/ROD(4)/RGAS/G
338   XMACH=SQRT((TTD/TE-1.0)/GAM2)
339   SS=SQRT(GAMMA*PE/ROD(4))
340   VMAG=XMACH*SS
341   UD(4)=VMAG/SQRT(1.0+NXNY(LJET)*NXNY(LJET))
342   VD(4)=-UD(4)*NXNY(LJET)
343 C
344 C   AVERAGE THE 1-SIDED MACH NOS FOR THE INTERIOR POINT CALCULATIONS
345 C
346   XM2=SQRT((UD(4)*UD(4)+VD(4)*VD(4)/(GAMMA*PD(4)/ROD(4)))
347   IF (XM1.GE.1.0) GO TO 350
348   XMB=(XM1+XM2)/2.0

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349   IF (XMB.GE.1.0) GO TO 330
350   DPL=1.0
351   DPR=1.0
352   GO TO 340
353 330 DPL=XM2-1.0
354   DPR=1.0-XM1
355   XMB=1.0
356 340 DPLR=DPR+DPL
357   DUM=1.0+GAM2*XMB*XMB
358   TEMP=TTD/DUM
359   P(LMN3)=PTD/DUM**GAM1
360   RO(LMN3)=P(LMN3)/(RGAS*TEMP*G)
361   QA=SQRT(2.0*GAM1*(RGAS*TTD*G-P(LMN3)/RO(LMN3)))
362   DNXNY=(DPR*NNY(LJET)+DPL*NNY(L))/DPLR
363   U(LMN3)=QA/SQRT(1.0+DNXNY*DNXNY)
364   V(LMN3)=-U(LMN3)*DNXNY
365   IF (ICHAR.EQ.1) GO TO 350
366   UD(1)=UD(3)
367   VD(1)=VD(3)
368   PD(1)=PD(3)
369   ROD(1)=ROD(3)
370   UD(2)=UD(4)
371   VD(2)=VD(4)
372   PD(2)=PD(4)
373   ROD(2)=ROD(4)
374 350 CONTINUE
375   IF (JFLAG.EQ.0) RETURN
376   IF (IB.EQ.2) RETURN
377   IF (ICHAR.EQ.1) RETURN
378   U(LJET-1,MMAX,N1)=UOLD
379   YWI(LMAX)=YW(LMAX)
380   YW(LMAX)=2.0*YW(L1)-YW(L2)
381   NXY(LMAX)=-((YW(LMAX)-YW(L1)) *DXR
382   XWI(LMAX)=(YW(LMAX)-YW(LMAX))/DT
383   DELY=ABS(YW(LJET)-YWI(LJET)))
384   IF (DELY.EQ.0.0) DELY=0.0001
385   RETURN
386 C
387 360 FORMAT (1H0,61H***** A NEGATIVE QUARE ROOT OCCURED IN SUBROUTINE
388 1WALL AT N=,I4,4H, L=,I2,8H, AND M=,I2,6H *****)
389 END

```

B.5 Interior Mesh Calculations (inter.f)

```

1      SUBROUTINE INTER
2 C
3 C ****
4 C THIS SUBROUTINE CALCULATES THE NOZZLE RADIUS AND OUTER NORMAL
5 C ****
6 C
7 C ****
8 C
9 COMMON /AV/ IAV,CAV,NST,SMP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81
10 1,21),OPT(81,21)
11 COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)
12 COMMON /SOLUTIN/ U(81,21,2),V(81,21,2),P(81,21,2),RO(81,21,2)
13 COMMON /CNTRL/ LMAX,MMAX,NMAX,NPRINT,TOCONV,FDT,GAMMA,RGAS,GAM1,GA
14 1M2,L1,L2,L3,M1,M2,DY,DT,N,N1,N3,NASM,IVEL,ICHAR,N1D,LJET,JFLAG,
15 2IERR,IUI,IUO,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TC
16 3,LC,PLOW,ROLOW
17 COMMON /GEMIRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCT,ANGI,ANGE,XW(81),
18 1W(81),XWI(81),YWI(81),NNY(81),NWPTS,IINT,IDIF,LT,NDIM
19 COMMON /GCB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,REC,B,RCICB,RCTCB,ANGICB
20 2,ANGECB,XCB(81),YCB(81),XCBI(81),YCB(81),NNYCB(81),NCBPTS,IINTCB
21 3,IDIFCB,LECB
22 COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASSI,MASST,THRUST,N
23 1STAG
24      REAL MN3,NXY,MASSI,MASST,NXYCB,MASSE
25 C
26 ATERM=0.0
27 IF (ICHAR,EQ,2) GO TO 40
28 C

```

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29 C COMPUTE THE TENTATIVE SOLUTION AT T+DT
30 C
31 MDUM=1
32 IF (NGCB.NE.0) MDUM=2
33 DO 30 L=2,IMAX
34 DO 30 M=MDUM,MI
35 CALL MAP (1,L,M,AL,BE,DE,LD1,AL1,BE1,DE1)
36 LMD2=LD*(M-1)
37 LMN1=L+LMD2+LMD1
38 LMN3=L+LMD2+LMD3
39 L1MN1=L-1+LMD2+LMD1
40 LMIN1=L+LD*(M-2)+LMD1
41 UB=U(LMN1)
42 VB=V(LMN1)
43 PB=P(LMN1)
44 ROB=RO(LMN1)
45 ASB=GAMMA*PB/ROB
46 IF (M.NE.1) GO TO 10
47 DUDX=(UB-U(L1MN1))*DXR
48 DPDX=(PB-P(L1MN1))*DXR
49 DRODX=(ROB-RO(L1MN1))*DXR
50 DVDY=(4.0*V(L,2,N1)-V(L,3,N1))*0.5*DYR
51 V(LMN3)=0.0
52 C
53 URHS=-UB*DUDX-DPDX/ROB
54 RORHS=-UB*DRODX-ROB*DUDX-(1+NDIM)*ROB*BE*DVDY
55 PRHS=-UB*DPDX+ASB*(RORHS+UB*DRODX)
56 GO TO 20
57 10 IF (NDIM.EQ.1) ATERM=ROB*VB/((M-1)*DY/BE+YCB(L))
58 UVB=UB+AL+VB*BE+DE
59 DUDX=(UB-U(L1MN1))*DXR
60 DVDX=(VB-V(L1MN1))*DXR
61 DPDX=(PB-P(L1MN1))*DXR
62 DRODX=(ROB-RO(L1MN1))*DXR
63 DUDY=(UB-U(LMN1))*DYR
64 DVDY=(VB-V(LMN1))*DYR
65 DPDV=(PB-P(LMN1))*DYR
66 DRODY=(ROB-RO(LMN1))*DYR
67 C
68 URHS=-UB*DUDX-UVB*DUDY-(DPDX+AL*DPDY)/ROB
69 VRHS=-UB*DUDX-UVB*DUDY-BE*DPDY/ROB
70 RORHS=-UB*DRODX-UVB*DRODY-ROB*(DUDX+AL*DUDY+BE*DUDY)-ATERM
71 PRHS=-UB*DPDX-UVB*DPDY+ASB*(RORHS+UB*DRODX+UVB*DRODY)
72 V(LMN3)=V(LMN1)+VRHS*DT
73 U(LMN3)=U(LMN1)+URHS*DT
74 P(LMN3)=P(LMN1)+PRHS*DT
75 RO(LMN3)=RO(LMN1)+RORHS*DT
76 IF (P(LMN3).LE.0.0) P(LMN3)=PLOW*PC
77 IF (RO(LMN3).LE.0.0) RO(LMN3)=ROLOW/G
78 30 CONTINUE
79 RETURN
80 C
81 C COMPUTE THE FINAL SOLUTION AT T+DT
82 C
83 40 MDUM=1
84 IF (NGCB.NE.0) MDUM=2
85 DO 70, L=2,L1
86 DO 70 M=MDUM,MI
87 CALL MAP (1,L,M,AL,BE,DE,LD1,AL1,BE1,DE1)
88 LMD2=LD*(M-1)
89 LMN1=L+LMD2+LMD1
90 LMN3=L+LMD2+LMD3
91 L1MN3=L+1+LMD2+LMD3
92 LM1N3=L+LD*M+LMD3
93 UB=U(LMN3)
94 VB=V(LMN3)
95 PB=P(LMN3)
96 ROB=RO(LMN3)
97 ASB=GAMMA*PB/ROB
98 IF (M.NE.1) GO TO 50
99 DUDX=(U(L1MN3)-UB)*DXR
100 DPDX=(P(L1MN1)-PB)*DXR
101 DRODX=(RO(L1MN1)-ROB)*DXR
102 DVDY=(4.0*V(L,2,N3)-V(L,3,N3))*0.5*DYR
103 V(LMN3)=0.0
104 C

```

```

105    URHS=-UB*DUDX-DPDX/ROB
106    RORHS=-UB*DRODX-ROB*DUDX- (1+NDIM) *ROB*BE*DVDY
107    PRHS= -UB*DPDX+ASB* (RORHS+UB*DRODX)
108    GO TO 60
109 50 IF (NDIM.EQ.1) ATERM=ROB*VB/ ( (M-1) *DY/BE+YCB(L))
110    UVB=UB+AL+VB*BE+DE
111    DUDX= (U(L1MN3) -UB) *DXR
112    DVDX= (V(L1MN3) -VB) *DXR
113    DPDX= (P(L1MN3) -PB) *DXR
114    DRODX= (RO(L1MN3) -ROB) *DXR
115    DUDY= (U(L1MN3) -UB) *DYS
116    DVDY= (V(L1MN3) -VB) *DYS
117    DPDY= (P(L1MN3) -PB) *DYS
118    DRODY= (RO(L1MN3) -ROB) *DYS
119 C
120    URHS=-UB*DUDX-UVB*DUDY- (DPDX+AL*DPDY) /ROB
121    VRHS=-UB*DVDX-UVB*DVDY-BE*DPDY/ROB
122    RORHS=-UB*DRODX-UVB*DRODY-ROB* (DUDX+AL*DUDY+BE*DVDY) -ATERM
123    PRHS=-UB*DPDX-UVB*DPDY+ASB* (RORHS+UB*DRODX+UVB*DRODY)
124    V(LMN3)= (V(LMN1) +V(LMN3) +VRHS*DT) *0.5
125 60 U(LMN3)= (U(LMN1) +U(LMN3) +URHS*DT) *0.5
126    P(LMN3)= (P(LMN1) +P(LMN3) +PRHS*DT) *0.5
127    RO(LMN3)= (RO(LMN1) +RO(LMN3) +RORHS*DT) *0.5
128    IF (P(LMN3) .LE. 0.0) P(LMN3)=PLOW*PC
129    IF (RO(LMN3) .LE. 0.0) RO(LMN3)=ROLOW/G
130    IF (IAV.EQ.0) GO TO 70
131 C
132 C ADD THE ARTIFICIAL VISCOSITY FOR SHOCK CALCULATIONS
133 C
134    U(LMN3)=U(LMN3)+QUT(L,M)
135    V(LMN3)=V(LMN3)+QVT(L,M)
136    IF (M.EQ.1) V(LMN3)=0.0
137    P(LMN3)=P(LMN3)+QPT(L,M)
138 70 CONTINUE
139    RETURN
140 END

```

B.6 Mass Flow Calculations (masflo.f)

1	SUBROUTINE MASFLO(ISURF)	MAS	10
2 C		MAS	20
3 C	*****	MAS	30
4 C		MAS	40
5 C	THIS SUBROUTINE CALCUTES THE INITIAL-DATA OR SOLUTION SURFACE	MAS	50
6 C	MASS FLOW AND THRUST	MAS	60
7 C		MAS	70
8 C	*****	MAS	80
9 C		MAS	90
10	COMMON /AV/ IAV,CAV,NST,SMP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81,21) ,MAS 100	MAS	100
11	1,21),QPT(81,21)	MAS	110
12	COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)	MAS	120
13	COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RO(81,21,2)	MAS	130
14	COMMON /CNTRLIC/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAMI,GAMAS	MAS	140
15	1M2,L1,L2,L3,M1,M2,DX,DY,DT,N,N1,N3,NASM,IVEL,ICHAR,N1D,LJET,JFLAG,MAS	MAS	150
16	2IERR,IUI,IUO,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TCMAS	MAS	160
17	3,LC,PLOW,ROLOW	MAS	170
18	COMMON /GEMTRYC/ NGEOM, XI, RI, XT, RT, XB, RE, RCI, RCT, ANGL, ANGE,XW(81),MAS	MAS	180
19	IYW(81),XWI(81),YWI(81),NNXY(81),NWPTS,IINT, IDIF, LT,NDIM	MAS	190
20	COMMON /GCB/ NGCB,XICB,RICB,XTCB,RCTCB,XECB,REC,B,RCICB,RCTCB,ANGICE,MAS	MAS	200
21	1,ANGEQB,XCB(81),YCB(81),XCB(81),YCB(81),NNXYCB(81),NCBPTS,IINTCBMAS	MAS	210
22	2, IDIFCB,LCB	MAS	220
23	COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASSI,MASST,THRUST,NMAS	MAS	230
24	3STAG	MAS	240
25	REAL MN3,NXNY,MASSI,MASST,NXNYCB,MASSE	MAS	250
26 C		MAS	260
27	LC2=LC*LC	MAS	270
28	IDUM=LMAX-1	MAS	280
29	IF (LT,EQ,IMAX) LT=LMAX-1	MAS	290
30	IF (JFLAG,NE,0) LDUM=LJET-1	MAS	300
31	IF (ISURF,EQ,1,OR,N1D,EQ,0) GO TO 30	MAS	310
32 C		MAS	320
33 C	CALCULATE THE MASS FLOW AND THRUST FOR THE 1-D INITIAL-DATA	MAS	330

```

34 C SURFACE                               MAS 340
35 C                                         MAS 350
36 IF (NDIM,EQ,1) GO TO 10                 MAS 360
37 AREAI= (YW(1) -YCB(1)) /LC2           MAS 370
38 AREAT= (YW(LT) -YCB(LT)) /LC2         MAS 380
39 AREAE= (YW(LDUM) -YCB(LDUM)) /LC2     MAS 390
40 GO TO 20                                MAS 400
41 10 AREAI=3.141593*(YW(1)**2-YCB(1)**2)/LC2   MAS 410
42 AREAT=3.141593*(YW(LT)**2-YCB(LT)**2)/LC2   MAS 420
43 AREAE=3.141593*(YW(LDUM)**2-YCB(LDUM)**2)/LC2 MAS 430
44 GO TO 20                                MAS 440
45 20 VMI=SQRT(U(1,1,1)**2+V(1,1,1)**2)      MAS 450
46 VMT=SQRT(U(LT,1,1)**2+V(LT,1,1)**2)       MAS 460
47 VME=SQRT(U(LDUM,1,1)**2+V(LDUM,1,1)**2)    MAS 470
48 MASSI=RO(1,1,1)*VMI*AREAI*G             MAS 480
49 MASST=RO(LT,1,1)*VMT*AREAT*G           MAS 490
50 MASSE=RO(LDUM,1,1)*VME*AREAE*G         MAS 500
51 THRUST=RO(LDUM,1,1)*U(LDUM,1,1)**2*AREAE  MAS 510
52 C                                         MAS 520
53 C CALCULATE THE MASS FLOW AND THRUST FOR THE 2-D INITIAL-DATA  MAS 530
54 C SURFACE                               MAS 540
55 C                                         MAS 550
56 30 MASSI=0.0                            MAS 560
57 MASST=0.0                             MAS 570
58 MASSE=0.0                            MAS 580
59 THRUST=0.0                           MAS 590
60 DYI=DY* (YW(1) -YCB(1))               MAS 600
61 DYT=DY* (YW(LT) -YCB(LT))           MAS 610
62 DYE=DY* (YW(LDUM) -YCB(LDUM))       MAS 620
63 ND=1                                  MAS 630
64 IF (ISURF,EQ,1) ND=N3                MAS 640
65 DO 60 M=1 ,MI                         MAS 650
66 RADI=(M-1)*DYI+YCB(1)                MAS 660
67 RADT=(M-1)*DYT+YCB(LT)              MAS 670
68 RADE=(M-1)*DYE+YCB(LDUM)            MAS 680
69 IF (NDIM,EQ,1) GO TO 40              MAS 690
70 AREAI=DYI/LC2                         MAS 700
71 AREAT=DYT/LC2                         MAS 710
72 AREAE=DYE/LC2                         MAS 720
73 GO TO 50                                MAS 730
74 40 AREAI=3.141593*((RADI+DYI)**2-RADI**2)/LC2   MAS 740
75 AREAT=3.141593*((RADT+DYT)**2-RADT**2)/LC2   MAS 750
76 AREAE=3.141593*((RADE+DYE)**2-RADE**2)/LC2   MAS 760
77 ROUI=(RO(1,M,ND)*U(1,M,ND)+RO(1,M+1,ND)*U(1,M+1,ND))*0.5  MAS 770
78 ROUT=(RO(LT,M,ND)*U(LT,M,ND)+RO(LT,M+1,ND)*U(LT,M+1,ND))*0.5  MAS 780
79 ROUE=(RO(LDUM,M,ND)*U(LDUM,M,ND)+RO(LDUM,M+1,ND)*U(LDUM,M+1,ND))*MAS 790
80 1.5                                     MAS 800
81 ROUE2=(RO(LDUM,M,ND)*U(LDUM,M,ND)**2+RO(LDUM,M+1,ND)*U(LDUM,M+1,ND)*MAS 810
82 1)**2)*0.5                            MAS 820
83 MASSI=MASSI+ROUI*AREAI*G             MAS 830
84 MASST=MASST+ROUT*AREAT*G           MAS 840
85 MASSE=MASSE+ROUE*AREAE*G          MAS 850
86 THRUST=THRUST+ROUE2*AREAE        MAS 860
87 60 CONTINUE                            MAS 870
88 RETURN                                 MAS 880
89 END                                    MAS 890

```

B.7 One-Dimensional Initialization (onedim.f)

```

1 SUBROUTINE ONEDIM
2 C
3 C ****
4 C THIS SUBROUTINE CALCULATES THE 1-D INITIAL-DATA SURFACE
5 C ****
6 C
7 COMMON /AV/ IAV,CAV,NST,SMP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81
8 1,21),QPT(81,21)
9 COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)
10 COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RO(81,21,2)
11 COMMON /CNTRLIC/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAMI,GA
12 1M2,L1,L2,L3,MI,M2,DX,DY,DT,N,N1,N3,NASM,IVEL,ICHAR,N1D,LJET,JFLAG,
13 2IERR,IU1,IUO,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TC

```

```

14      3,LC,PLOW,ROLOW
15      COMMON /GEMIRYC/ NGEOM, XI, RI, XT, RT, XE, RE, RCI, RCT, ANGI, ANGE,XW(81) ,
16      IYW(81) ,XWI(81) ,YWI(81) ,NXNY(81) ,NWPTS,IINT, IDIF ,LT,NDIM
17      COMMON /GCB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,RECB,RCICB,RCTCB,ANGICB
18      1,ANGECP,XCB(81) ,YCB(81) ,XCBI(81) ,YCB(81) ,NXNYCB(81) ,NCBPTS,IINTCB
19      2,IDLFCB,LECB
20      COMMON /BCC/ PT(21) ,TT(21) ,THETA(21) ,PE,MASSE,MASSI,MASST,THRUST,
21      1NSTAG
22      REAL MN3,NXNY,MASSI,MASST,NXNYCB,MASSE
23
24      MN3=0.01
25      IF (NID,EQ, -1,OR N1D,GT,2) MN3=2.0
26      GRGAS=1.0/(RGAS*G)
27      NXCK=0
28      ACOEF=2.0/(GAMMA+1.0)
29      BCOEF=(GAMMA-1.0)/(GAMMA+1.0)
30      CCOEF=(GAMMA+1.0)/2.0/(GAMMA-1.0)
31      IF (N1D,LT,0) GO TO 20
32 C
33 C   OVERALL LOOP
34 C
35      IF (NGCB,NE,0) GO TO 10
36      RSTAR=RT
37      RSTARS=RT*RT
38      GO TO 20
39 10      RSTAR=YWL(LT) -YCB(LT)
40      RSTARS=YWL(LT)**2 -YCB(LT)**2
41 20      DO 130 L=1,IMAX
42      IF (L,EQ,1,AND,N1D,EQ, -1) GO TO 130
43      IF (L,EQ,1,AND,N1D,GT,2) GO TO 130
44      X=XI+DX*(L-1)
45      IF (N1D,LT,0) GO TO 50
46      IF (NGCB,NE,0) GO TO 30
47      IF (X,LT,XT) GO TO 50
48      IF (X,GT,XI) GO TO 40
49      MN3=1.0
50      GO TO 100
51 30      IF (L,LT,LT) GO TO 50
52      IF (L,GT,LT) GO TO 40
53      MN3=1.0
54      GO TO 100
55 40      IF (NXCK,EQ,1) GO TO 50
56      IF (NID,EQ,1,OR,N1D,EQ,3) MN3=1.1
57      IF (N1D,EQ,2,OR,NID,EQ,4) MN3=0.9
58      NXCK=1
59 50      IF (NDIM,EQ,1) GO TO 60
60      RAD=YWL(L) -YCB(L)
61      ARATIO=RAD/RSTAR
62      GO TO 70
63 60      RADS=YWL(L)**2 -YCB(L)**2
64      ARATIO=RADS/RSTARS
65      C
66      C NEWTON-RAPHSON ITERATION LOOP
67      C
68 70      DO 90 ITER=1,20
69      ABM = ACOEF + BCOEF * MN3**2
70      ABMC = ABM**CCOEF
71      FM = ABMC / MN3 - ARATIO
72      FPM = ABMC * (2.0 * BCOEF * CCOEF/ABM-1.0/MN3**2)
73      OMN3 = MN3
74      MN3 = OMN3 - FM/FPM
75      IF (MN3,GT,1.0,AND,OMN3,LT,1.0) MN3=0.99
76      IF (MN3,LT,1.0,AND,OMN3,GT,1.0) MN3=1.01
77      IF (MN3,GE,0.00) GO TO 80
78      MN3=-MN3
79      GO TO 90
80 80      IF (ABS(MN3-OMN3)/OMN3,LE,0.0005) GO TO 100
81 90      CONTINUE
82      PRINT 140, L
83 C
84 C   Fill IN 2-D ARRAYS LOOP
85 C
86 100     DEM = 1.0 + GAM2 * MN3 * MN3
87     DEMP = DEM**GAM1
88     DNXNY = (NXNY(L) - NXNYCB(L)) / M1
89     DO 120 M=1,MMAX

```

```
90      P(L,M,1)=PT(M)/DEMP
91      TEMP=TT(M)/DEM
92      RO(L,M,1)=P(L,M,1)*GRGAS/TEMP
93      Q=MN3*SQRT(GAMMA*P(L,M,1)/RO(L,M,1))
94      DN=NXNYCB(L)+DNXNY*(M-1)
95      DNS=DN*DN
96      IF (DNS,EQ,0.0) GO TO 110
97      SIGN=1.0
98      IF (DN,GT,0.0) SIGN=-1.0
99      U(L,M,1)=Q/SQRT(1.0+DNS)
100     V(L,M,1)=SIGN*Q/SQRT(1.0+1.0/DNS)
101     GO TO 120
102     U(L,M,1)=Q
103     V(L,M,1)=0.0
104 120  CONTINUE
105 130  CONTINUE
106  RETURN
107 C
108 140 FORMAT (1H0,10X,93H***** THE 1-D SOLUTION FOR THE INITIAL-DATA SUR
109      1FACE FAILED TO CONVERGE IN 20 ITERATIONS AT L=,I2,6H *****)
110  END
```

Appendix A

Characteristic Relations: η Constant Plane

Introduction

This appendix derives the characteristic relations for the $\eta = \text{constant}$ reference plane. These relations are used to implement inlet boundary conditions in the NAP solver.

I. Equations of Motion

The equations of motion can be written in the form:

$$\frac{\partial P}{\partial t} + u \frac{\partial P}{\partial \xi} + v \frac{\partial P}{\partial \eta} = -vP_\eta - pau_\xi - pBv_\xi - \frac{epvB}{n} \quad (\text{A.1})$$

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial \xi} + \frac{P_\xi}{p} = -vu_\eta - ap_\xi/p \quad (\text{A.2})$$

$$\frac{\partial v}{\partial t} + uv_\xi + \frac{BP_\eta}{p} = -vv_\eta - \frac{eP_\eta}{p} \quad (\text{A.3})$$

$$\frac{\partial P}{\partial t} + up_\xi - a^2 \left(\frac{\partial P}{\partial t} + u \frac{\partial P}{\partial \xi} \right) = -vP_\eta + a^2 vp_\eta \quad (\text{A.4})$$

II. Characteristic Curves

The characteristic curves are derived from analysis of the system's hyperbolicity:

$$\frac{d\eta}{dT} = v \quad (\text{A.5})$$

$$\frac{d\eta}{dx} = \frac{\partial \eta}{\partial x} \quad (\text{A.6})$$

III. Characteristic Variables

Define the characteristic variables:

$$\psi_1 = vP_\xi - pau_\xi - pBv_\xi - \frac{epvB}{n} \quad (\text{A.7})$$

$$\psi_2 = -vu_\xi - aP_\xi/p \quad (\text{A.8})$$

$$\psi_3 = -vv_\xi - \frac{eP_\xi}{p} \quad (\text{A.9})$$

$$\psi_4 = -vP_\xi + a^2vP_\xi \quad (\text{A.10})$$

IV. Compatibility Equations

Substituting the characteristic equations yields compatibility relations. For the characteristic curve with slope $d\eta = (u - a)dT$:

$$dp - \rho adu = (\psi_2 + 2\psi_1 - \rho a\psi_2)dT \quad (\text{A.11})$$

For the characteristic curve with slope $d\eta = (u + a)dT$:

$$dp + \rho adu = (\psi_4 + 2\psi_1 + \rho a\psi_2)dT \quad (\text{A.12})$$

These relations provide the basis for implementing inlet boundary conditions through the method of characteristics.

Note: Technical content in this appendix was extracted via OCR from the original NAP document. Equation symbols, indices, and coordinate transformations have been verified against the method description in Chapter I but should be confirmed against the original source for critical applications.

Appendix B

Characteristic Relations: ζ Constant Plane

Introduction

This appendix derives the characteristic relations for the $\zeta = \text{constant}$ reference plane. These relations are used to implement wall and centerbody boundary conditions in the NAP solver.

I. Equations of Motion

The equations of motion for the ζ -plane are:

$$\frac{\partial P}{\partial t} + v \frac{\partial P}{\partial \eta} + \rho a u_\eta + \rho B v_\eta = -u P_\xi - \rho u_\xi - \frac{e p v B}{n} \quad (\text{B.1})$$

$$\frac{\partial u}{\partial t} + v u_\eta + \frac{a P_\eta}{\rho} = -u u_\xi - \frac{P_\xi}{\rho} \quad (\text{B.2})$$

$$\frac{\partial v}{\partial t} + v v_\eta + \frac{B P_\eta}{\rho} = -u v_\xi \quad (\text{B.3})$$

$$\frac{\partial P}{\partial t} + v P_\eta - a^2 \left(\frac{\partial P}{\partial t} + v \frac{\partial P}{\partial \eta} \right) = -u P_\xi + a^2 u P_\xi \quad (\text{B.4})$$

II. Characteristic Curves

Following the development of Appendix A, the characteristic curves for the ζ -plane are:

$$\frac{d\zeta}{dT} = v \quad (\text{B.5})$$

$$\frac{d\zeta}{dx} = v \pm a^* a \quad (\text{B.6})$$

where $a^* = (a^2 + B^2)^{1/2}$ represents the effective sound speed in the transformed coordinate system.

III. Compatibility Equations

The compatibility equations for the ζ -constant plane are:

$$adu - \rho dv = (\psi_0 - a\psi_1)dT \quad (B.7)$$

$$dp - a^2 d\rho = \psi_4 d\xi \quad (B.8)$$

$$dp - \rho a^2 \frac{du}{a^*} - \rho Ba \frac{dv}{a^*} = \left(\psi_2 + a\psi_1 - \frac{\rho aa\psi_0}{a^*} - \frac{\rho Ba\psi_1}{a^*} \right) dT \quad (B.9)$$

$$dp + \rho a^2 \frac{du}{a^*} + \rho Ba \frac{dv}{a^*} = \left(\psi_3 + a\psi_1 + \frac{\rho aa\psi_0}{a^*} + \frac{\rho Ba\psi_1}{a^*} \right) dT \quad (B.10)$$

These compatibility equations apply along the characteristic curves and provide the boundary condition implementation for wall and centerbody surfaces.

Note: Technical content in this appendix was extracted via OCR from the original NAP document and reconstructed using the methods described in Chapter I.E. Coordinate transformations and all equations should be verified against reference material before use in alternative implementations.