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Issued: January 1977

**NAP: A Computer Program for the
Computation of Two-Dimensional,
Time-Dependent, Inviscid Nozzle Flow**

by

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CONTRACT W-7405-ENG. 36

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Work supported by the US Energy Research and Development Administration,
Magnetic Fusion Energy Division.

Printed in the United States of America. Available from
National Technical Information Service
U.S. Department of Commerce
5285 Port Royal Road
Springfield, VA 22161
Price: Printed Copy \$5.00 Microfiche \$3.00

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NAP: A COMPUTER PROGRAM FOR THE
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ABSTRACT

A computer program, NAP, is presented for calculating inviscid, steady, and unsteady flow in two-dimensional and axisymmetric nozzles. Interior mesh points are computed using the MacCormack finite-difference scheme, while a characteristic scheme is used to calculate the boundary mesh points. An explicit artificial viscosity term is included for shock computations. The fluid is assumed to be a perfect gas. This method was used to compute the steady flow in a 45° - 15° conical, converging-diverging nozzle, a 15° conical, converging nozzle, and a 10° conical, plug nozzle. The numerical solution agreed well with the experimental data. In contrast to previous time-dependent methods for calculating steady flows, the computational times were < 1 min on a CDC 6600 computer.

I. BASIC DESCRIPTION OF THE METHOD

A. Introduction

The equations of motion governing steady, inviscid flow are of a mixed type: hyperbolic in the supersonic region and elliptic in the subsonic region. These mathematical difficulties may be removed by using the "time-dependent" method, in which the flow is assumed to be unsteady or time-dependent. Then the governing equations are hyperbolic in both subsonic and supersonic regions. The steady-state solution may be obtained as the asymptotic solution for large time. This time-dependent technique has been used to compute steady converging-diverging nozzle flows (reported in Refs. 1-6), and it has also been used to compute steady converging nozzle flows (see Refs. 4 and 7). The results of those calculations are mainly good, but the computational times are rather large. In addition, although the computer program of Ref. 6 included a centerbody and those of Refs. 4 and 7 included the exhaust jet, none of the above codes is able to calculate both, that is, plug nozzles.

The object of this research was to develop a production-type computer program capable of solving steady converging, converging-diverging, and plug two-dimensional nozzle flows in computational times of < 1 min on a CDC 6600 computer. Such a program would be able to solve unsteady flows as well.

B. Literature Review

The following is a discussion of the methods used in Refs. 1 through 7. The first paragraph deals with the computation of the interior mesh points; the next three paragraphs are concerned with the boundary mesh points.

Prozan (see Ref. 1), Wehofer and Moger,⁴ and Laval⁵ used variations of the two-step Lax-Wendroff scheme to compute the interior mesh points. Migdal et al.³ and Brown and Ozcan⁷ employed the original one-step Lax-Wendroff scheme, but with the equations of motion in nonconservation form. Serra⁶ applied the original Lax-Wendroff scheme with the equations of motion in conservation form. To stabilize their schemes, Laval and Serra used artificial viscosity terms in their difference equations. Wehofer and

Moger reset the stagnation conditions along each streamline, reset the mass flow at each axial location, and smoothed the subsonic portion of the flow after each time step.

To compute the nozzle inlet mesh points, Prozan (in Ref. 1) assumed the inlet flow to be uniform. Wehofer and Moger assumed only that the pressure was radially uniform at the inlet. Migdal et al. and Brown and Ozcan mapped the inlet to minus infinity after Moretti,⁸ thus allowing the static conditions to be set equal to the stagnation conditions. Laval used extrapolation of the interior mesh points to determine the inlet mesh points, while Serra employed a characteristic scheme.

Prozan (in Ref. 1), Wehofer and Moger, Laval, and Brown and Ozcan used an extrapolation technique to compute the wall mesh points. Migdal et al. employed a characteristic scheme after Moretti⁸ to compute the wall mesh points, while Serra applied a reflection technique. For the converging nozzle problem to be properly posed, an exhaust jet calculation must be included. Wehofer and Moger used an extrapolation procedure to compute the exhaust jet boundary mesh points, while Brown and Ozcan employed a characteristic scheme after Moretti.⁸

All of the above authors used extrapolation to compute the exit mesh points when the flow was supersonic, since any errors incurred would be swept out of the mesh. Serra employed a characteristic scheme when the exit flow was subsonic.

C. Choice of a Method

The lengthy computational times associated with time-dependent calculations are usually caused by inefficient numerical schemes or poor treatment of boundaries, resulting in the requirement for excessively fine computational meshes (see Refs. 8 and 9). A technique for a much more efficient calculation of the interior and boundary mesh points will be discussed here.

The computation of steady flows by a time-dependent method differs from ordinary initial-value problems in that the initial data and much of the transient solution have a negligible effect on the final or steady solution. Therefore, accuracy is important only for the asymptotic state, and special attention to intermediate efficiency will result in reasonable computational times. For this reason, interior mesh points can be computed by using a very

efficient finite-difference scheme, as opposed to those less efficient finite-difference or characteristic schemes that achieve high accuracy at every step.

In the class of finite-difference schemes, the two-step methods such as the MacCormack¹⁰ and the two-step Lax-Wendroff schemes¹¹ are more efficient than the original Lax-Wendroff scheme,¹¹ especially if the governing equations are in conservation form. Moretti¹² showed that using the equations of motion in conservation form decreased efficiency and ease of programming while only slightly increasing the accuracy of shock calculations. The use of an explicit artificial viscosity term for shock-free flows also decreases efficiency and was shown to be physically unjustified.¹² In addition, such increases in the numerical dissipation can often destroy the weak shock structure of transonic flows. Therefore, the MacCormack scheme with the equations of motion in nonconservation form is used to calculate the interior mesh points. An explicit artificial viscosity term was included for shock computations only. Remember that the implicit dissipation always present as an effect of truncation terms assures numerical stability for the shock-free flow results.

The boundary mesh points, while making up only a small part of the total mesh points, must be handled most accurately,⁸ because of the flow-field's sensitivity to precise boundary geometry. Moretti⁸ and Abbett⁹ showed that reflection, extrapolation, and one-sided difference techniques for computing solid wall boundaries give poor results and should be avoided. Therefore, the wall and centerbody mesh points are computed using a characteristic scheme. A characteristic scheme is also used to calculate the exhaust jet boundary mesh points.

In the case of the nozzle inlet mesh points for subsonic flow, the use of extrapolation techniques and the assumption of one-dimensional flow presume the form of the solution and in many cases are physically unjustified. On the other hand, a characteristic scheme could be used to calculate the inlet mesh points. While the stagnation pressure and temperature are assumed to remain constant at the inlet in a characteristic scheme (not necessarily the case for unsteady flow), this assumption

would appear to be valid for the time-dependent calculation of steady flows. Moretti⁸ recommends mapping the inlet to minus infinity, thus allowing the static conditions to be set equal to the stagnation conditions. In theory, this appears to be the best approach, but it should be kept in mind that the infinite physical plane must be replaced by a finite computational plane. Also, this technique requires additional mesh points upstream of the nozzle inlet. It is not presently resolved as to whether the characteristic scheme approach used by Serra or the mapping-to-minus-infinity approach suggested by Moretti⁸ and employed by Migdal et al. and Brown and Ozcan is the best technique. To reduce the total number of mesh points to be computed, a characteristic scheme is used to compute the inlet mesh points. For supersonic flow, the inlet mesh points are set equal to specified values of velocity, pressure, and density, because in a supersonic stream the downstream conditions do not propagate upstream.

Extrapolation is used to compute the exit mesh points when the flow is supersonic, since any errors incurred will be swept out of the mesh, and a characteristic scheme is employed when the flow is subsonic.

D. Equations of Motion

The appropriate nonconservation form of equations for two-dimensional, inviscid, isentropic, rotational flow are

$$\rho_t + u\rho_x + v\rho_y + \rho u_x + \rho v_y + \epsilon\rho v/y = 0, \quad (1)$$

$$u_t + uu_x + vu_y + p_x/\rho = 0, \quad (2)$$

$$v_t + uv_x + vv_y + p_y/\rho = 0, \quad (3)$$

$$p_t + up_x + vp_y - a^2(\rho_t + u\rho_x + v\rho_y) = 0, \quad (4)$$

where ρ is the density, u is the axial velocity, v is the radial velocity, p is the pressure, a is the local speed of sound, t is the time, x and y are the axial and radial coordinates, and the subscripts denote partial differentiation. The symbol ϵ is 0 for planar flow and 1 for axisymmetric flow.

The physical (x,y) plane is mapped into a rectangular computational plane (ζ,η) by the following coordinate transformation:

$$\zeta = x; \quad \eta = \frac{y - y_c(x)}{y_w(x,t) - y_c(x)}; \quad \tau = t, \quad (5)$$

where $y_w(x,t)$ denotes the nozzle wall and exhaust jet boundary radius as a function of x and t and $y_c(x)$ denotes the nozzle centerbody radius as a function of x . These mapping functions must be single-valued functions of the x coordinate. In the (ζ,η,τ) coordinate system Eqs. (1) through (4) become

$$\rho_\tau + u\rho_\zeta + \bar{v}\rho_\eta + \rho u_\zeta + \rho\alpha u_\eta + \rho\beta v_\eta + \epsilon\rho v/(y_c + \eta/\beta) = 0, \quad (6)$$

$$u_\tau + uu_\zeta + \bar{v}u_\eta + p_\zeta/\rho + \alpha p_\eta/\rho = 0, \quad (7)$$

$$v_\tau + uv_\zeta + \bar{v}v_\eta + \beta p_\eta/\rho = 0, \quad (8)$$

$$p_\tau + up_\zeta + \bar{v}p_\eta - a^2(\rho_\tau + u\rho_\zeta + \bar{v}\rho_\eta) = 0, \quad (9)$$

where

$$\beta = \frac{1}{y_w - y_c}; \quad \alpha = -\beta \frac{\partial y_c}{\partial x} - \eta\beta \left(\frac{\partial y_w}{\partial x} - \frac{\partial y_c}{\partial x} \right);$$

$$\delta = -\eta\beta \frac{\partial y_w}{\partial t}, \quad (10)$$

$$\bar{v} = \alpha u + \beta v + \delta. \quad (11)$$

The fluid is assumed to be thermally and calorically perfect; that is, a constant ratio of specific heats is assumed.

For shock computations, an artificial viscosity model of the form suggested by von Neumann-Richtmyer¹¹ is used. This model, which has a term corresponding to all the viscous and thermal conduction terms in the Navier-Stokes equations, is shown below.

$$[\text{RHS Eq. (21)}] = (\lambda + 2\mu) \frac{\partial}{\partial x} \left(\frac{\partial u}{\partial x} \right) + \lambda \frac{\partial}{\partial x} \left(\frac{\partial v}{\partial y} \right) + \mu \frac{\partial}{\partial y} \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right) + \frac{\epsilon}{y} \left[(\lambda + \mu) \frac{\partial v}{\partial x} + \mu \frac{\partial u}{\partial y} \right], \quad (12)$$

$$\begin{aligned}
[\text{RHS Eq. (3)}] &= (\lambda + 2\mu) \frac{\partial}{\partial y} \left(\frac{\partial u}{\partial x} \right) + \lambda \frac{\partial}{\partial y} \left(\frac{\partial v}{\partial y} \right) \\
&+ \mu \frac{\partial}{\partial x} \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right) + \frac{\epsilon(\lambda + 2\mu)}{y} \left(\frac{\partial v}{\partial y} - \frac{v}{y} \right), \\
(13)
\end{aligned}$$

$$\begin{aligned}
[\text{RHS Eq. (4)}] &= \rho(\gamma - 1) \left\{ (\lambda + 2\mu) \left[\left(\frac{\partial u}{\partial x} \right)^2 + \left(\frac{\partial v}{\partial y} \right)^2 \right] \right. \\
&+ \mu \left[\left(\frac{\partial u}{\partial y} \right)^2 + \left(\frac{\partial v}{\partial x} \right)^2 \right] + 2\lambda \frac{\partial u}{\partial x} \frac{\partial v}{\partial y} \\
&+ 2\mu \frac{\partial u}{\partial y} \frac{\partial v}{\partial x} + k \left[\frac{\partial}{\partial x} \left(\frac{\partial T}{\partial x} \right) + \frac{\partial}{\partial y} \left(\frac{\partial T}{\partial y} \right) \right] \\
&+ \frac{\epsilon v}{y} \left[(\lambda + 2\mu) \frac{v}{y} + 2\lambda \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) \right. \\
&\left. \left. + \frac{k}{v} \frac{\partial T}{\partial y} \right] \right\}, \\
(14)
\end{aligned}$$

$$\lambda = 2c c_\lambda \Delta x \Delta y \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right),$$

$$\mu = 2c c_\mu \Delta x \Delta y \left(\frac{\partial v}{\partial x} + \frac{\partial u}{\partial y} \right),$$

$$k = \frac{\mu \gamma R}{(\gamma - 1) \text{Pr}},$$

where c , c_λ , and c_μ are nondimensional quantities that specify the distribution and amount of smoothing, γ is the ratio of specific heats, R is the gas constant, Δx and Δy are the axial and radial mesh spacing, and Pr is the Prandtl number.

In the (ζ, η, τ) coordinate system Eqs. (12) through (14) become

$$\begin{aligned}
[\text{RHS Eq. (7)}] &= (\lambda + 2\mu) \left(\frac{\partial}{\partial \zeta} + \alpha \frac{\partial}{\partial \eta} \right) \left(\frac{\partial u}{\partial \zeta} + \alpha \frac{\partial u}{\partial \eta} \right) \\
&+ \lambda \left(\frac{\partial}{\partial \zeta} + \alpha \frac{\partial}{\partial \eta} \right) \left(\beta \frac{\partial v}{\partial \eta} \right) + \mu \beta \frac{\partial}{\partial \eta} \left(\beta \frac{\partial u}{\partial \eta} \right. \\
&+ \left. \frac{\partial v}{\partial \zeta} + \alpha \frac{\partial v}{\partial \eta} \right) + \frac{\epsilon}{\eta} \left[(\lambda + \mu) \left(\frac{\partial v}{\partial \zeta} \right. \right. \\
&\left. \left. + \alpha \frac{\partial v}{\partial \eta} \right) + \mu \beta \frac{\partial u}{\partial \eta} \right], \\
(15)
\end{aligned}$$

$$\begin{aligned}
[\text{RHS Eq. (8)}] &= (\lambda + 2\mu) \beta \frac{\partial}{\partial \eta} \left(\frac{\partial u}{\partial \zeta} + \alpha \frac{\partial u}{\partial \eta} \right) + \lambda \frac{\beta \partial}{\partial \eta} \left(\beta \frac{\partial v}{\partial \eta} \right) \\
&+ \mu \left(\frac{\partial}{\partial \zeta} + \alpha \frac{\partial}{\partial \eta} \right) \left(\beta \frac{\partial u}{\partial \eta} + \frac{\partial v}{\partial \zeta} + \alpha \frac{\partial v}{\partial \eta} \right) \\
&+ \frac{\epsilon(\lambda + 2\mu)}{\eta} \left(\beta \frac{\partial v}{\partial \eta} - \frac{v}{\eta} \right), \\
(16)
\end{aligned}$$

$$\begin{aligned}
[\text{RHS Eq. (9)}] &= \rho(\gamma - 1) \left\{ (\lambda + 2\mu) \left[\left(\frac{\partial u}{\partial \zeta} + \alpha \frac{\partial u}{\partial \eta} \right)^2 \right. \right. \\
&+ \left. \left(\beta \frac{\partial v}{\partial \eta} \right)^2 \right] + \mu \left[\left(\beta \frac{\partial u}{\partial \eta} \right)^2 + \left(\frac{\partial v}{\partial \zeta} + \alpha \frac{\partial v}{\partial \eta} \right)^2 \right] \\
&+ 2\lambda \left(\frac{\partial u}{\partial \zeta} + \alpha \frac{\partial u}{\partial \eta} \right) \left(\beta \frac{\partial v}{\partial \eta} \right) \\
&+ 2\mu \left(\beta \frac{\partial u}{\partial \eta} \right) \left(\frac{\partial v}{\partial \zeta} + \alpha \frac{\partial v}{\partial \eta} \right) + k \left[\left(\frac{\partial}{\partial \zeta} \right. \right. \\
&+ \left. \alpha \frac{\partial}{\partial \eta} \right) \left(\frac{\partial T}{\partial \zeta} + \alpha \frac{\partial T}{\partial \eta} \right) + \beta \frac{\partial}{\partial \eta} \left(\beta \frac{\partial T}{\partial \eta} \right) \left. \right] \\
&+ \frac{\epsilon v}{\eta} \left[(\lambda + 2\mu) \frac{v}{\eta} + 2\lambda \left(\frac{\partial u}{\partial \zeta} + \alpha \frac{\partial u}{\partial \eta} \right. \right. \\
&\left. \left. + \beta \frac{\partial v}{\partial \eta} \right) + \frac{k}{v} \beta \frac{\partial T}{\partial \eta} \right] \left. \right\}, \\
(17)
\end{aligned}$$

$$\lambda = 2c c_\lambda \Delta \zeta \frac{\Delta \eta}{\beta} \left(\frac{\partial u}{\partial \zeta} + \alpha \frac{\partial u}{\partial \eta} + \beta \frac{\partial v}{\partial \eta} \right),$$

$$\mu = 2c c_\mu \Delta \zeta \frac{\Delta \eta}{\beta} \left(\frac{\partial v}{\partial \zeta} + \alpha \frac{\partial v}{\partial \eta} + \beta \frac{\partial u}{\partial \eta} \right),$$

where $\bar{\eta} = y_c + \eta/\beta$, and y_c = centerbody radius. These terms are nonzero only when the divergence of the velocity is negative.

E. Numerical Method

The computational plane is divided into five sets of mesh points: interior, inlet, exit, wall and centerbody, and exhaust jet boundary.

1. Interior Mesh Points. The interior mesh points are computed using the MacCormack scheme, a second-order, noncentered, two-step, finite-difference scheme. Backward differences are used on the first step; forward differences are used on the second. The governing equations are left in non-conservation form. An explicit artificial viscosity term is used for shock computations. Centerline mesh points are computed by enforcing symmetry of the flow. For example, the finite-difference equations for Eq. (1) for planar flow ($\epsilon = 0$) and no artificial viscosity are

$$\begin{aligned} \bar{\rho}_{L,M}^{N+1} = & \bar{\rho}_{L,M}^N - \left[u_{L,M}^N \left(\frac{\bar{\rho}_{L,M}^N - \bar{\rho}_{L-1,M}^N}{\Delta x} \right) \right. \\ & + v_{L,M}^N \left(\frac{\bar{\rho}_{L,M}^N - \bar{\rho}_{L,M-1}^N}{\Delta y} \right) \\ & + \bar{\rho}_{L,M}^N \left(\frac{u_{L,M}^N - u_{L-1,M}^N}{\Delta x} \right) \\ & \left. + \bar{\rho}_{L,M}^N \left(\frac{v_{L,M}^N - v_{L,M-1}^N}{\Delta y} \right) \right] \Delta t, \end{aligned} \quad (18)$$

$$\begin{aligned} \rho_{L,M}^{N+1} = & 0.5 \left\{ \bar{\rho}_{L,M}^N + \bar{\rho}_{L,M}^{N+1} - \left[\bar{u}_{L,M}^{N+1} \left(\frac{\bar{\rho}_{L+1,M}^{N+1} - \bar{\rho}_{L,M}^{N+1}}{\Delta x} \right) \right. \right. \\ & + \bar{v}_{L,M}^{N+1} \left(\frac{\bar{\rho}_{L,M+1}^{N+1} - \bar{\rho}_{L,M}^{N+1}}{\Delta y} \right) \\ & + \bar{\rho}_{L,M}^{N+1} \left(\frac{\bar{u}_{L+1,M}^{N+1} - \bar{u}_{L,M}^{N+1}}{\Delta x} \right) \\ & \left. \left. + \bar{\rho}_{L,M}^{N+1} \left(\frac{\bar{v}_{L,M+1}^{N+1} - \bar{v}_{L,M}^{N+1}}{\Delta y} \right) \right] \Delta t \right\}, \end{aligned} \quad (19)$$

where L and M denote axial and radial mesh points, respectively, N denotes the time step, and the bar denotes values calculated on the first step. A complete description of the method is given in Ref. 10.

2. Inlet Mesh Points. The inlet mesh points for subsonic flow are computed using a second-order, reference-plane characteristic scheme. In this

scheme, the partial derivatives with respect to η are computed in the initial-value and solution surfaces using noncentered differencing as in the MacCormack scheme. These approximations to the derivatives with respect to η are then treated as forcing terms and the resulting system of equations is solved in the $\eta = \text{constant}$ reference planes using a two-independent-variable, characteristic scheme. The characteristic relations for the $\eta = \text{constant}$ reference planes are derived in Appendix A. The boundary condition is the specification of the stagnation temperature and stagnation pressure. The use of a reference-plane characteristic scheme requires the specification of inlet flow angle as an additional boundary condition. The inlet flow angle can be approximately determined from the nozzle geometry. The equations relating the total and static conditions are

$$p_T/p = [1 + (\gamma - 1) M^2/2]^{\gamma/(\gamma-1)}, \quad (20)$$

$$T_T/T = 1 + (\gamma - 1) M^2/2, \quad (21)$$

where γ is the ratio of specific heats, M is the Mach number, T is the temperature, and the subscript T denotes the total conditions.

The characteristic relations relating the interior flow to the nozzle inlet flow are Eq. (A-43) in Appendix A and can be written as

$$\begin{aligned} dp - \rho a du &= (\psi_4 + a^2 \psi_1 - \rho a \psi_2) d\tau \\ \text{for } d\xi &= (u-a) d\tau, \end{aligned} \quad (22)$$

where the top equation is called the compatibility equation and the bottom equation is called the characteristic curve equation. The ψ terms (see Appendix A) represent the derivatives in the η direction. Equation (22) may be written in finite-difference form by first replacing the differentials by differences along the characteristic curve. Next, the coefficients are either evaluated in the initial-value plane (first step) or considered to be the average of the coefficients evaluated in both the initial-value and solution planes (second step). Finally, the ψ terms are treated as follows: on the first step the coefficients and derivatives, using backward differences, are evaluated in the initial-

value plane; on the second and final step the coefficients and derivatives, now using forward differences, are evaluated in the solution plane and then averaged with the ψ terms from the first step. Equations (20), (21), and (22), along with the inlet flow angle and the equation of state $p = \rho RT$, where R is the gas constant, form a system of five equations for the five variables u , v , p , ρ , and T .

A brief description of the unit processes of this scheme is given below. The intersection of the characteristic curve through the solution point with the initial-value line in the $\eta = \text{constant}$ plane is determined by solving the characteristic curve equation. The coefficient $u-a$ is evaluated in the initial-value plane. The dependent variables and derivatives in the ψ terms are calculated at the intersection point using linear interpolation. Next, the compatibility equation, along with Eqs. (20) and (21) and the equation of state, are used to calculate the variables at the solution point. An iterative solution of these equations is required. Thus the first step has been used to compute all inlet mesh points. In the second step, the characteristic curve equation is solved again. Now the coefficient $u-a$ is the average of the values in the initial-value plane and the first-step solution plane. Again, linear interpolation is used to obtain the variables at the intersection point. Finally, the compatibility equation, now with averaged coefficients and ψ terms, is used along with Eqs. (20) and (21) and the equation of state to determine the final solution.

A reference-plane characteristic scheme was chosen over a bicharacteristic scheme because the increased accuracy of a bicharacteristic scheme seemed not to be worth the increased computational time for time-dependent flows.

For supersonic flow, the inlet mesh points are set equal to specified values of velocity, pressure, and density.

3. Exit Mesh Points. For subsonic flow, a reference-plane characteristic scheme similar to the inlet scheme is used. The exit pressure is specified. The characteristic relations relating the interior flow to the nozzle exit flow are Eqs. (A-41), (A-42), and (A-44). These equations can be written as

$$\left. \begin{aligned} dp - a^2 d\rho &= \psi_4 d\tau \\ dv &= \psi_3 d\tau \end{aligned} \right\} \text{ for } d\zeta = u d\tau, \quad (23)$$

$$dp + \rho a du = (\psi_4 + a^2 \psi_1 + \rho a \psi_2) d\tau \quad \text{for } d\zeta = (u+a) d\tau. \quad (24)$$

These equations are written in finite-difference form in the same manner as was done for the nozzle inlet scheme. Equations (23), (24), and (25), along with the exit pressure condition, form a system of four equations for the variables u , v , p , and ρ .

For supersonic flow, the exit mesh points are computed using linear extrapolation.

4. Wall and Centerbody Mesh Points. The wall and centerbody mesh points are also computed using a reference-plane characteristic scheme. In this scheme, the derivatives with respect to ζ are approximated, and the resulting system of equations is solved in the $\zeta = \text{constant}$ reference planes. The characteristic relations for the $\zeta = \text{constant}$ reference planes are given in Appendix B. The wall and centerbody contours and therefore their slopes are specified. The boundary condition is given by

$$v = u \tan \theta + \partial y_w / \partial \tau, \quad (25)$$

where θ is the local wall or centerbody angle.

The characteristic relations relating the interior flow to the flow at the nozzle wall are Eqs. (B-15), (B-16), and (B-18) in Appendix B. These equations are

$$\left. \begin{aligned} \beta du - \alpha dv &= (\beta \psi_2 - \alpha \psi_3) d\tau \\ dp - a^2 d\rho &= \psi_4 d\tau \end{aligned} \right\} \text{ for } d\eta = \bar{v} d\tau, \quad (27)$$

$$dp + \rho \alpha a du / \alpha^* + \rho \beta a dv / \alpha^* = (\psi_4 + a^2 \psi_1 + \rho \alpha a \psi_2 / \alpha^* + \rho \beta a \psi_3 / \alpha^*) d\tau \quad \text{for } d\eta = (\bar{v} + \alpha^* a) d\tau. \quad (28)$$

These equations are written in finite-difference form in the same manner as was done for the nozzle inlet scheme. Equations (26), (27), (28), and (29) form a system of four equations for the four variables u , v , p , and ρ .

5. Exhaust Jet Boundary Mesh Points. The exhaust jet boundary mesh points are computed by the wall routine such that the pressure boundary condition

$$p = p_{\text{ambient}} \quad (30)$$

is satisfied. This is accomplished by first assuming the shape of the jet boundary and then using the wall routine to calculate the pressure. Next, the jet boundary location is slightly changed and a second pressure is computed. By use of an interpolation procedure, a new jet boundary location is determined. This interpolation-extrapolation procedure is then repeated at each point until the jet boundary pressure and the ambient pressure agree within some specified tolerance.

When an exhaust jet calculation is made, the nozzle wall exit lip mesh point becomes a singularity and, therefore, is treated by a special procedure. First, an upstream solution is computed at the exit mesh point, using the flow tangency condition as the boundary condition and backward ζ differences in both the initial-value and solution planes. Next, a downstream solution is calculated, using Eq. (30) as the boundary condition and the total conditions calculated from the upstream mesh point. The upstream solution is used when computing wall mesh points upstream of the exit mesh point, whereas the downstream solution is used when computing downstream wall mesh points. A third exit mesh point solution to be used for interior mesh point calculation is determined as follows. When the upstream solution is subsonic, the two solution Mach numbers are averaged such that the averaged Mach number is less than or equal to one. This Mach number is then used to calculate the exit mesh point solution to be used to compute the interior mesh points. When the upstream solution is supersonic, the upstream solution is used to calculate the interior mesh points.

6. Step Size. The step size Δt is controlled by the well-known Courant or C-F-L condition which can be expressed as

$$\Delta t \leq 1/[(V + a) (1/\Delta x^2 + 1/\Delta y^2)^{1/2}] \quad (31)$$

where V is the velocity magnitude. Using Eqs. (5)

and (10), Eq. (31) can be written as

$$\Delta t \leq A/[(V + a) (1/\Delta \zeta^2 + \beta^2/\Delta \eta^2)^{1/2}] \quad (32)$$

where the coefficient A was determined from actual calculations and varied between 0.4 and 1.6 depending on the geometry of the flow in question.

F. Overall Program

The nozzle inlet flow, as well as the flow leaving the nozzle, may be either subsonic or supersonic. The flow may contain variations in stagnation temperature and stagnation pressure from streamline to streamline. The nozzle wall and centerbody geometries may be either one of two analytical contours or a completely general tabular contour. The program is capable of calculating the exhaust jet boundary for subsonic or supersonic flow. The initial data may be read in or calculated internally by the program. The internally computed data are calculated assuming one-dimensional, steady, isentropic flow with area change. The program output includes the coordinates, velocities, pressure, density, Mach number, temperature, mass flow, and axial thrust in both English and metric units.

G. Results and Discussion

The results presented here have been published in Ref. 13. The CDC 6600 computational times represent the central processor time not including compilation. So that these results can be compared with those of other investigators, the following table of relative machine speeds is given.

Computer	Relative Machine Speed
IBM 7094	0.1
IBM 360/50	0.1
IBM 360/65	0.3
IBM 360/75	0.5
Univac 1108	0.5
CDC 6600	1.0

These relative speeds were obtained from Refs. 14 and 15 and are only rough estimates because values may vary considerably depending on the compiler and machine configuration. In each case, the one-dimensional values computed internally by the program were the initial data. When the relative change in axial velocity in the throat and downstream regions was less than a prescribed convergence tolerance, the flow was assumed to have reached steady state. The convergence tolerance was found

to be a function of the mesh spacing, flow speed, and nozzle geometry. For the results presented here, a convergence tolerance of 0.003% was used for flows without exhaust jet calculations; 0.005% for flows with exhaust jet calculations.

The present method was used to compute the steady-state solution for flow in the 45°-15° conical, converging-diverging nozzle shown in Fig. 1a. The Mach number contours and wall pressure ratio are shown in Fig. 2. Although the code works with English and metric units, the units in the original publication of the experimental data (English) were used here. The experimental data are those of Cuffel et al.² The computed discharge coefficient is 0.983, compared with the experimental value of 0.985. The 21x8 computational mesh required 301 time planes and a computational time of 35 s. There is good agreement with the experimental data. This case was also

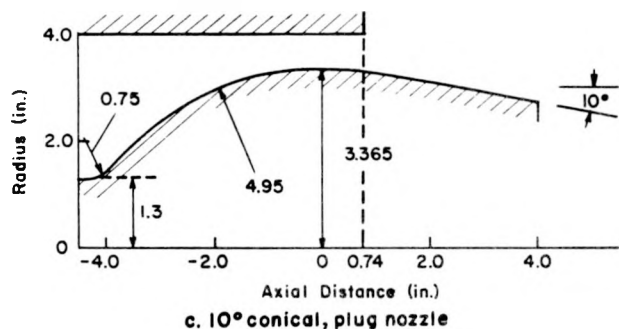
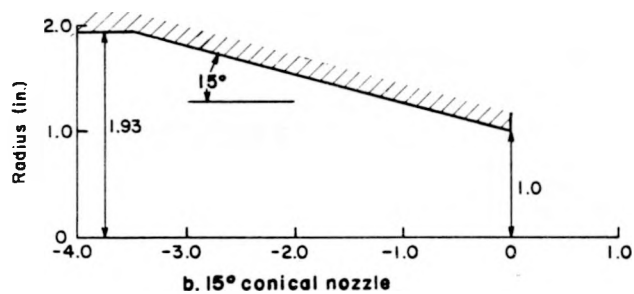
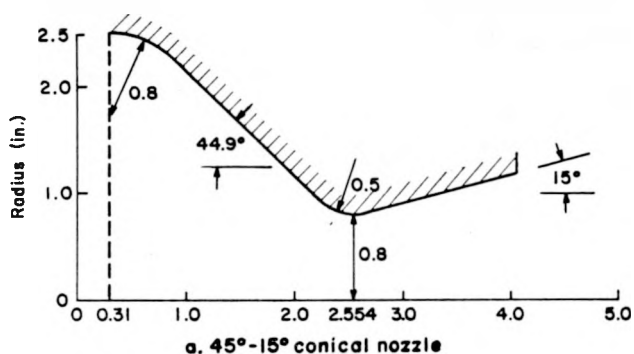


Fig. 1. Nozzle geometries.

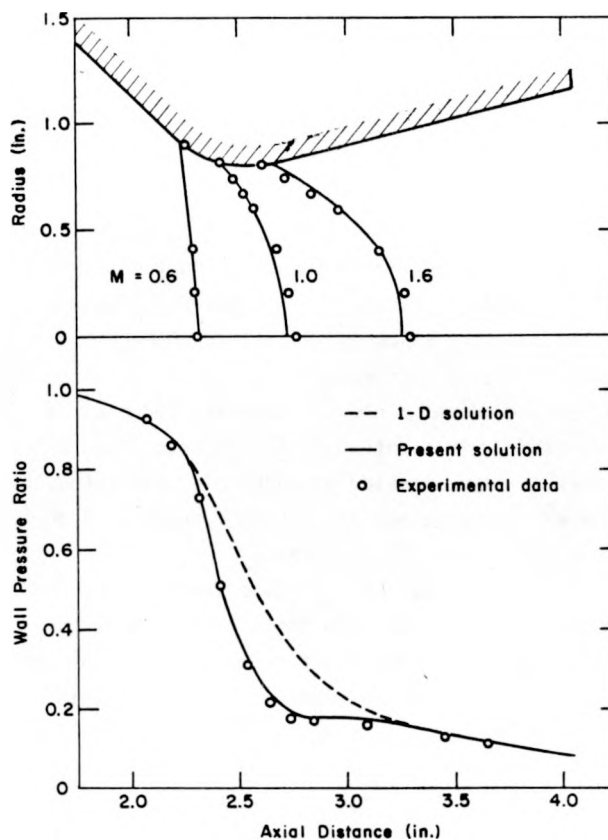


Fig. 2. Mach number contours (above) and wall pressure ratio for 45°-15° conical nozzle.

solved by Prozan (see Ref. 2), Migdal, Laval, and Serra. The details of Prozan's computation were not reported by Cuffel et al., but Saunders reported a time of 45 min on a CDC 3200 (23x11 mesh) for computing the flow in a nozzle with a large radius of curvature. Migdal et al. reported a computational time of less than 5 min on an IBM 350/75; Laval reported a computational time on the order of 2 h on an IBM 360/50 (61x21 mesh); and Serra reported a computational time of 80 min on a Univac 1108 (3000 mesh points). This case was also solved by Prozan and Kooker,¹⁶ using a relaxation scheme to solve the steady, irrotational equations of motion. Their computational time was 5 to 10 min on an IBM 7094 (21x11 mesh).

The present method was also used to compute the steady-state flow in a 15° conical, converging nozzle. The nozzle geometry is shown in Fig. 1b. The Mach number contours and wall pressure ratio for a nozzle pressure ratio of 2.0 are shown in Fig. 3. The experimental data are those of Thornock.¹⁷ The computed discharge coefficient is 0.957, compared

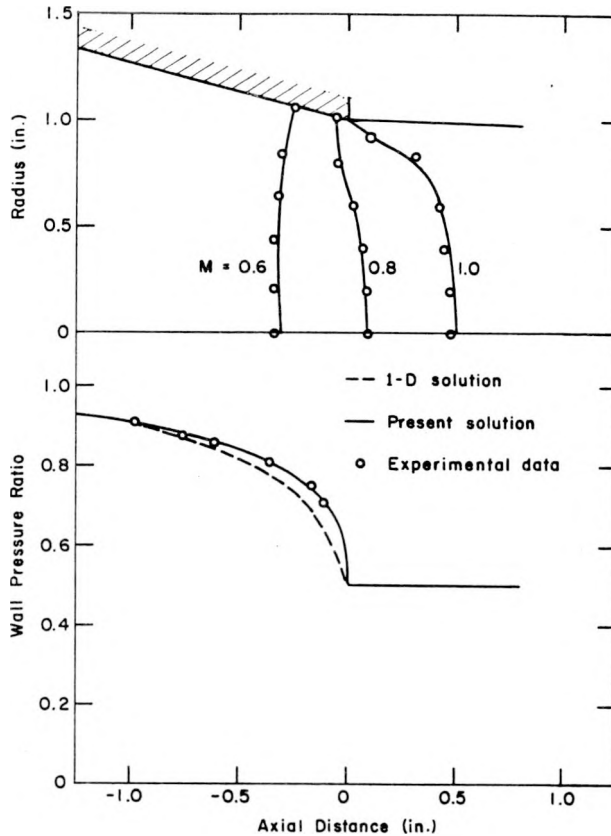


Fig. 3. Mach number contours (above) and wall pressure ratio for 15° conical nozzle.

with the experimental value of 0.960. The 23x7 computational mesh required 249 time planes and a computational time of 29 s. There is good agreement with the experimental data. This case was also solved by Wehofer and Moger and Brown and Ozcan. Wehofer and Moger's solution for a pressure ratio of 2 required over 2 h on an IBM 360/50 (47x11 mesh); Brown and Ozcan's results required 17 min on an IBM 360/65 (20x6 mesh).

Finally, the present method was used to calculate the flow in a 10° conical, plug nozzle. The nozzle geometry is shown in Fig. 1c. The Mach number contours and plug pressure ratio for a nozzle pressure ratio of 3.29 are shown in Fig. 4. The experimental data are those of Bresnahan and Johns.¹⁸ The 31x6 computational mesh required 327 time planes and a computational time of 52 s. Again, there is good agreement with the experimental data. The author is unaware of any other time-dependent analyses of plug nozzles.

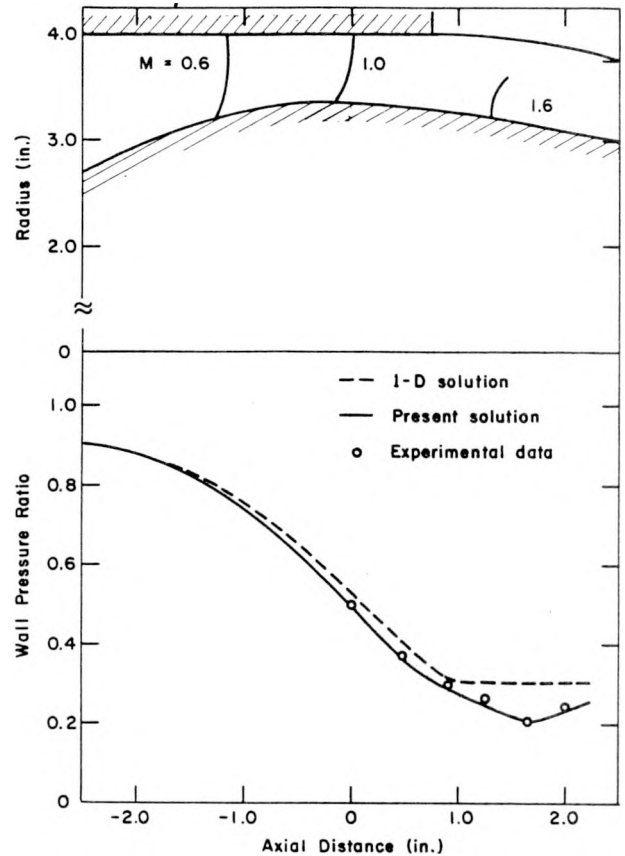


Fig. 4. Mach number contours (above) and plug pressure ratio for 10° conical plug nozzle.

H. Concluding Remarks

A method of computing nozzle flows has been presented. A production-type computer program capable of solving a wide variety of nozzle flows has been developed. The program's accuracy was demonstrated by computing the steady flow in a 45°-15° conical, converging-diverging nozzle, a 15° conical, converging nozzle, and a 10° conical, plug nozzle. The < 1-min computational time for these steady flows is considerably faster than for any of the earlier time-dependent techniques.

II. DESCRIPTION AND USE OF THE NAP PROGRAM

A. Subroutine Description

The computer program consists of one program, one function, and twelve subroutines.

1. Program MAIN. Program MAIN initiates a run by reading in the input data. Next, the program title, abstract, and input data descriptions are printed. The program then calls subroutines GEOM and GEOMCB to calculate the nozzle geometry. The

input data are then converted to the internal units. If requested, program MAIN calls subroutine ØNEDIM to calculate the one-dimensional, initial-value surface. Program MAIN then prints the initial-value surface, which includes a mass flow and thrust calculation made by subroutine MASFLØ. Next, subroutine PLØT is called and it plots the data on film. The final part of MAIN consists of the time-step loop, which performs the following operations: calculates the next time-step size; calls subroutine INTER to compute the interior mesh points; calls subroutine WALL to compute the wall mesh points; calls subroutine INLET to compute the inlet mesh points for subsonic flow; calls subroutine EXITT to compute the exit mesh points for subsonic flow; calls subroutine MASFLØ to compute the mass flow and thrust; prints the solution surface; calls subroutine PLØT to plot the data on film; checks the solution for its convergence to the steady-state solution; and punches the last solution plane on cards for restart.

2. Subroutine GEØM. Subroutine GEØM calculates the nozzle-wall coordinates and slopes for four different wall geometries: a constant area duct, a circular-arc, conical nozzle, and two tabular input nozzles. In the case of the first tabular nozzle, a completely general set of wall coordinates is input. Subroutine GEØM then calls subroutine MTLUP, which interpolates for equally spaced coordinates. Next, subroutine GEØM calls function DIF, which calculates the slopes of the equally spaced coordinates. For the second tabular nozzle, equally spaced coordinates and slopes are read in.

3. Subroutine GEØMCB. Subroutine GEØMCB calculates the nozzle centerbody coordinates and slopes for four different centerbody geometries and is the same as subroutine GEØM.

4. Subroutine MTLUP. Subroutine MTLUP was taken from the NASA Langley program library. The data of this version is 9-12-69. This subroutine is called by subroutines GEØM and GEØMCB to interpolate the nozzle-wall and centerbody coordinates for equally spaced coordinates.

5. Function DIF. Function DIF was also taken from the NASA Langley program library. The date of this version is 8-1-68. This function is called by subroutines GEØM and GEØMCB to calculate the slopes of the nozzle-wall and centerbody coordinates.

6. Subroutine ØNEDIM. Subroutine ØNEDIM is called by program MAIN to compute the one-dimension-

al, isentropic, initial-value surface. A Newton-Raphson scheme is used to calculate the Mach number for the area ratios, which are determined from the nozzle geometry.

7. Subroutine MAP. Subroutine MAP calculates the mapping functions that map the physical plane to a rectangular computational plane. Therefore, this subroutine is called before each mesh point is calculated.

8. Subroutine MASFLØ. Subroutine MASFLØ is called by program MAIN to calculate the mass flow and thrust for the initial-value and solution surfaces. This subroutine uses the trapezoidal rule to evaluate the mass flow and thrust integrals.

9. Subroutine PLØT. Subroutine PLØT produces velocity vector plots, and contours of density, pressure, temperature, and Mach number plots using the SC-4020 microfilm recorder. English units are used for the contour values. This subroutine uses five LASL system routines: GETQ, ADV, LINCNT, PLT, and DRV. GETQ obtains the job identification label. ADV advances the film. LINCNT indexes a specified horizontal line on each frame. PLT and DRV plot a plus sign at a specified point and draw a vector between two specified points, respectively. If this program is used on non-LASL computers, these five routines will have to be replaced by their respective counterparts on another computing system.

10. Subroutine SHØCK. Subroutine SHØCK calculates the artificial viscosity for shock computations. The artificial viscosity model is a quadratic viscosity after von Neumann-Richtmyer and has a term corresponding to all the viscous and thermal-conduction terms in the Navier-Stokes equations. In addition, this subroutine adds numerical smoothing to stabilize the calculations for very nonuniform initial-data surfaces or to accelerate the convergence to steady state.

11. Subroutine INTER. Subroutine INTER is called by program MAIN to calculate the interior mesh points. The technique used by this subroutine is the MacCormack, second-order, finite-difference scheme.

12. Subroutine WALL. Subroutine WALL is called by program MAIN to compute the wall, centerbody, and exhaust jet boundary mesh points. This subroutine uses a second-order, reference-plane characteristic scheme and also controls the inter-

polation process for locating the exhaust jet boundary.

13. Subroutine INLET. Subroutine INLET is called by program MAIN to compute the inlet mesh points for subsonic flow. A second-order, reference-plane characteristic scheme is employed by subroutine INLET.

14. Subroutine EXITT. Subroutine EXITT is called by program MAIN to calculate the exit mesh points when the flow is subsonic. It uses a second-order, reference-plane characteristic scheme.

B. Input Data Description

The program input data is entered by a title card and five namelists. The namelists are CNTRL, IVS, GEMTRY, GCBL, and BC. The title card and each namelist are discussed below. The program will continue reading in data decks and executing them until a file mark is encountered. After each data deck is executed, the default values for the input data are restored before the next data deck is read in.

1. Title Card. The first card of each data deck is a title card consisting of 80 alphanumeric characters which identify the job. This card must always be the first card of the data deck, even if no information is specified on the card. The five namelists must appear in the order in which they are discussed below.

2. Namelist CNTRL. This namelist inputs the parameters that control the overall logic of the program.

LMAX	An integer specifying the number of mesh points in the X or axial direction (81 maximum). No default value is specified.
MMAX	An integer specifying the number of mesh points in the Y or radial direction (21 maximum). No default value is specified.
NMAX	An integer specifying the maximum number of time steps. For NMAX = 0, only the initial-data surface is computed and printed (provided NPRINT > 0). The default value is 0.
NPRINT	An integer specifying the amount of output desired. For NPRINT = N, every Nth solution plane, plus the initial-data and final solution planes, are printed. For NPRINT = -N, every Nth solution plane, plus the final solution plane, are print-

ed. For NPRINT = 0, only the final solution plane is printed. The default value is 0.

TCØNV	Specifies the axial velocity steady-state convergence tolerance in percent. If less than or equal to zero, the convergence is not checked. The default is 0.0.
FDT	A parameter that premultiplies the allowable C-F-L time step. It is desirable to use as large a value of FDT as possible without causing the computation to become unstable. Values as large as 1.6 have been used successfully for shock-free flows, while values of 0.4 to 0.6 are required for flows with shocks. The default value is 1.0.
GAMMA	Denotes the ratio of specific heats. The default value is 1.4.
RGAS	Denotes the gas constant in lbf-ft/lbm-°R if English units are used, or J/kg-°K if metric units are used. The default value is 53.35.
TSTØP	Specifies the physical time, in seconds, at which the computations will be stopped. The default value is 1.0.
IAV	An integer which, if nonzero, requests the addition of a local artificial viscosity to stabilize calculations in the vicinity of a shock. The value of FDT must be reduced to ~0.6. The default value for IAV is 0.
IUI	An integer specifying the type of units to be used for the input quantities. If IUI equals 1, English units are assumed; if equal to 2, metric units are assumed. In using any default values, make sure the values correspond to the proper units. The default value is 1.
IUØ	Same as IUI except for output quantities. If IUØ equals 3, both English and metric units are printed. The default value is 1.
IPUNCH	An integer which, if nonzero, punches the last solution plane on cards for restart. The default value is 0.
NPLOT	An integer which, if greater than or equal to zero, plots both velocity vectors and contours of density, pressure,

	temperature, and Mach number on a SC-4020 microfilm recorder. For NPLOT = N, all Nth solution planes, plus the initial-data and final solution plane, are plotted. For NPLOT = 0, only the final solution plane is plotted. The default value is -1.		
NST	An integer denoting the time step at which a small amount of numerical smoothing is stopped. This smoothing may be required to stabilize the calculations for very nonuniform initial-data surfaces. Some initial smoothing caused subsonic flows to reach steady state faster, but this was not the case for transonic and supersonic flows. The default value is 0 (no smoothing). When using the restart option, make sure NST is set equal to zero.	RKMU	Denotes the Prandtl number for the fluid used in the artificial viscosity model. The default value is 0.7.
The remaining parameters in namelist CNTRL are less important than the parameters given above. For most nozzle flows, these remaining parameters can be left at their default values.		CTA	Denotes the amount of time-averaging for the artificial viscosity. For CTA = 1.0, the values at the current time step are used. For CTA = 0.0, the values at the previous time step are used. For CTA between 0.0 and 1.0, a linear average is used. The default value is 0.5.
NASM	An integer specifying which part of the flowfield is tested for steady-state convergence. For NASM = 0, the entire flowfield is tested. For NASM = 1, the transonic and supersonic (throat region to exit) regions are tested. The default value is 1.	LSS	An integer specifying the axial meshpoint at which the addition of the artificial viscosity will begin. The default value is 2.
NAME	An integer which, when nonzero, causes the five namelists to be printed in addition to the regular output. The default value is 0.	PLØW	If the pressure becomes negative during a calculation, it is set equal to PLØW (psia). The default value is 0.01 psia.
NCØNVI	An integer specifying how many times the convergence tolerance TCØNV must be satisfied on consecutive time steps before the solution is considered to have converged. The default value is 1.	RØLØW	If the density becomes negative during a calculation, it is set equal to RØLØW (lbm/ft ³). The default value is 0.0001 lbm/ft ³ .
IUNIT	An integer which, when equal to zero, causes the program to use either English or metric units (see IUI and IUO). For IUNIT equal to 1, a nondimensional set of units is used. The default value is 0.	SMP	A parameter controlling the amount of smoothing (provided NST ≠ 0). The dependent variables are smoothed by the following formula: $u_{L,M} = SMP * u_{L,M} + (1.0 - SMP) * (u_{L+1,M} + u_{L,M+1} + u_{L-1,M} + u_{L,M-1}) / 4.0$ The default value is 0.95.
CAV	Denotes the artificial viscosity premultiplier c in the equations for λ and μ. The default value is 4.0.	<u>3. Namelist IVS.</u> This namelist specifies the flow variables for the initial-data surface.	
XMU	Denotes the coefficient c _μ in the equation for μ in the artificial viscosity model. A nondimensional value is used. The default value is 0.2.	NID	An integer specifying the type of initial-data surface desired. For NID = 0, a two-dimensional, initial-data surface is read in. A value of U, V, P, and RØ (discussed below) must be read in for all L = 1 to LMAX and M = 1 to MMAX mesh points. For NID ≠ 0, a one-dimensional data surface is computed internally.
		XLA	Denotes the coefficient c _λ in the equation for λ in the artificial viscosity model. A nondimensional value is used. The default value is 1.0.

The following combinations are possible:

N1D = -2 subsonic	} see RSTAR and RSTARS
N1D = -1 supersonic	
N1D = 1 subsonic-sonic-supersonic	} No additional data is needed
N1D = 2 subsonic-sonic-subsonic	
N1D = 3 supersonic-sonic-supersonic	
N1D = 4 supersonic-sonic-subsonic	

The default value is 1.

U(L,M,1) An array denoting the X or axial direction velocity component in ft/s or m/s. For N1D = 0, U(L,M,1) must be input for L = 1 to LMAX and M = 1 to MMAX. For N1D ≠ 0, U(L,M,1) is not input. No default values are specified.

V(L,M,1) An array denoting the Y or radial direction velocity component in ft/s or m/s. See U(L,M,1) for additional information. No default values are specified.

P(L,M,1) An array denoting the pressure in psia or kPa. See U(L,M,1) for additional information. No default values are specified.

RØ(L,M,1) An array denoting the density in lbm/ft³ or kg/m³. See U(L,M,1) for additional information. No default values are specified.

RSTAR, RSTARS If N1D = -1 or -2, either RSTAR for planar or RSTARS for axisymmetric flow must be input. RSTAR is the area per unit depth, in inches or cm, where the Mach number is unity. RSTARS is the area divided by π , in in.² or cm², where the Mach number is unity. No default values are specified.

If the restart option is to be used, the initial run must have been made with IPUNCH ≠ 0 in CNTRL, thereby causing a new IVS deck to be punched. The new IVS replaces the one used in the initial run and includes two additional parameters, NSTART and TSTART, which denote, respectively, the time step and physical time where the solution was restarted.

When N1D ≠ 0, the initial data is calculated using one-dimensional, isentropic theory. However, the axial and radial velocity components are adjusted while keeping the magnitude constant and satisfying the flow angle. The flow angles are linearly interpolated between the slope of the wall

and centerbody.

4. Namelist GEMTRY. This namelist specifies the parameters that define the nozzle-wall contour.

NDIM An integer denoting the flow geometry. For NDIM = 0, two-dimensional, planar flow is assumed, and for NDIM = 1, axisymmetric flow is assumed. The default value is 1.

NGEØM An integer specifying one of four different nozzle-wall geometries. A discussion of these four cases follows the definitions of the additional parameters in this namelist. No default value is specified.

XI The axial coordinate, in inches or cm, of the nozzle-wall inlet. No default value is specified.

RI The radial coordinate, in inches or cm, of the nozzle-wall inlet. No default value is specified.

RT The radial coordinate, in inches or cm, of the nozzle-wall throat. No default value is specified.

XE The axial coordinate, in inches or cm, of the nozzle-wall exit. No default value is specified.

RCI The radius of curvature, in inches or cm, of the nozzle-wall inlet. No default value is specified.

RCT The radius of curvature, in inches or cm, of the nozzle-wall throat. No default value is specified.

ANGI The angle, in degrees, of the converging section. No default value is specified.

ANGE The angle, in degrees, of the diverging section. No default value is specified.

XWI A one-dimensional array of nonequally spaced axial coordinates in inches or cm. No default values are specified.

YWI A one-dimensional array of radial coordinates, in inches or cm, corresponding to the axial coordinates in array XWI. No default values are specified.

NWPTS An integer specifying the number of entries in arrays XWI and YWI. The maximum value is 81. No default value is specified.

IINT An integer specifying the order of interpolation used. The maximum value is 2. The default value is 1.

IDIF An integer specifying the order of differentiation used. The maximum value is 5. The default value is 1.

YW A one-dimensional array of radial coordinates, in inches or cm, which correspond to LMAX equally spaced axial coordinates. No default values are specified.

NXNY A one-dimensional array (floating point) of the negative of the wall slopes corresponding to the elements of YW. No default values are specified.

JFLAG An integer which, when nonzero, denotes that an exhaust jet calculation is to be carried out. The default value is 0.

LJET An integer specifying the first mesh point of the exhaust jet boundary. For example, if the nozzle wall ends at the 10th axial mesh point, LJET = 11. The program assumes that the nozzle always ends at a mesh point. No default value is specified.

The following is a discussion of the four different wall geometries considered by this program.

a. Constant area duct (NGEOM = 1). The parameters XI, RI (radius of the duct), and XE must be specified.

b. Circular-arc, conical nozzle wall (NGEOM = 2). The geometry for this case is shown in Fig. 5. The parameters XI, RI, RT, XE, RCI, RCT, ANGI, and ANGE are specified. The axial coordinate of the throat and the radius of the exit are computed internally.

c. General nozzle wall (NGEOM = 3). An arbitrary nozzle-wall contour is specified by tabular input. NWPTS axial and radial coordinate pairs are specified by the arrays XWI and YWI, respectively. For good accuracy, one coordinate pair should be the nozzle throat. The tabular data need not be equally

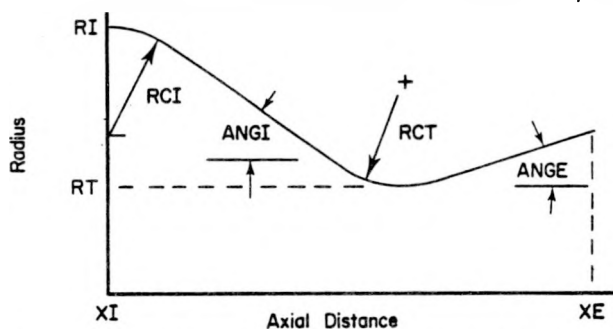


Fig. 5. Circular-arc, conical nozzle-wall geometry.

spaced. From the specified values of NWPTS, XWI, YWI, IINT, and IDIF, the program uses IINT-order interpolation to obtain LMAX equally spaced nozzle-wall contour points. Next, IDIF-order differentiation is used to obtain the nozzle-wall slope at these LMAX points.

d. General nozzle wall (NGEOM = 4). An arbitrary nozzle-wall contour is specified by tabular input. LMAX radial coordinates and the negative of their slopes are specified by the arrays YW and NXNY, respectively. These radial coordinates correspond to the LMAX equally spaced, axial mesh points. Therefore, XI and XE are input instead of each axial coordinate. For good accuracy, one pair of coordinates should be the nozzle throat.

5. Namelist GCBL. This namelist specifies the parameters that define the nozzle centerbody geometry. If no centerbody is present, this namelist is left blank but must still be present in the data deck.

NGCB An integer which, when nonzero, specifies one of four different centerbody geometries. A discussion of these four cases will follow the definitions of the additional parameters in this namelist. The default value is 0.

RICB The radial coordinate, in inches or cm, of the centerbody inlet. No default value is specified.

RTCB The radial coordinate, in inches or cm, of the centerbody maximum radius. No default value is specified.

RCICB The radius of curvature, in inches or cm, of the centerbody inlet. No default value is specified.

RCTCB The radius of curvature, in inches or cm, of the centerbody maximum radius. No default value is specified.

ANGICB The angle, in degrees, of the converging section. No default value is specified.

ANGEGB The angle, in degrees, of the diverging section. No default value is specified.

XCBI A one-dimensional array of nonequally spaced axial coordinates in inches or cm. No default values are specified.

YCBI A one-dimensional array of radial coordinates, in inches or cm, corresponding to the axial coordinates in array XCBI. No default value are specified.

NCBPTS	An integer specifying the number of entries in arrays XCBI and YCBI. The maximum value is 81. No default value is specified.
IINTCB	An integer specifying the order of interpolation used. The maximum value is 2. The default value is 1.
IDIFCB	An integer specifying the order of differentiation used. The maximum value is 5. The default value is 1.
YCB	A one-dimensional array of radial coordinates, in inches or cm, which correspond to LMAX equally spaced axial coordinates. No default values are specified.
NXNYCB	A one-dimensional array (floating point) of the negative of the centerbody slopes corresponding to the elements of YCB. No default values are specified.

The following is a discussion of the four different centerbody geometries considered by this program.

a. Cylindrical centerbody (NGCB = 1). The parameter RICB (radius of the centerbody) must be specified.

b. Circular-arc, conical centerbody (NGCB = 2). The geometry for this case is shown in Fig. 6. The parameters RICB, RTCB, RCICB, RCTCB, ANGICB, and ANGECB are specified. The axial coordinate of the maximum radius and the radius of the exit are computed internally.

c. General centerbody (NGCB = 3). An arbitrary centerbody contour is specified by tabular input. NCBPTS axial and radial coordinate pairs are specified by the arrays XCBI and YCBI, respectively. The tabular data need not be equally spaced. From the specified values of NCBPTS, XCBI, YCBI, IINTCB, and IDIFCB, the program uses IINTCB-

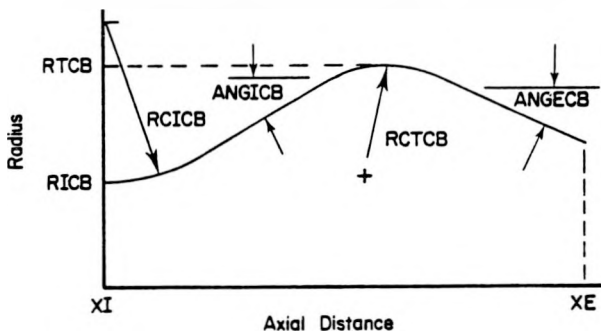


Fig. 6. Circular-arc, conical nozzle centerbody geometry.

order interpolation to obtain LMAX equally spaced centerbody contour points. Next, IDIFCB-order differentiation is used to obtain the centerbody slope at these LMAX points.

d. General centerbody (NGCB = 4). An arbitrary centerbody contour is specified by tabular input. LMAX radial coordinates and the negative of their slopes are specified by the arrays YCB and NXNYCB, respectively. These radial coordinates correspond to the LMAX equally spaced, axial mesh points.

6. Namelist BC. This namelist specifies the flow variables for the nozzle inlet and exit computational boundaries.

NSTAG An integer which, when nonzero, denotes that variable total pressure PT, variable total temperature TT, and variable flow angle THETA (all discussed below) across the nozzle inlet have been specified. If NSTAG \neq 0, then a value for PT, TT, and THETA must be specified at the M = 1 to MMAX points even if one or two of the variables are constant. If NSTAG = 0, only the first value for each of the three arrays needs to be specified. The default value is 0.

PT(M) A one-dimensional array denoting the stagnation pressure, in psia or kPa, across the nozzle inlet. No default values are specified.

TT(M) A one-dimensional array denoting the stagnation temperature, in °F or °C, across the nozzle inlet. No default values are specified.

THETA(M) A one-dimensional array denoting the flow angle, in degrees, across the nozzle inlet. The default value is THETA(1) = 0.0, which is meaningful only when NSTAG = 0.

PE The pressure, in psia or kPa to which the nozzle is exiting. This pressure is used to compute the nozzle exit conditions when the flow is subsonic and the exhaust jet boundary location when an exhaust jet calculation is requested. The default value is 14.7.

ISUPER An integer which, when nonzero, specifies that the inlet flow is supersonic. For this case the boundary condition is the

specification of the variables UI, VI, PI, and RØI discussed below. The default value is 0.

- UI(M) A one-dimensional array denoting the axial velocity, in ft/s or m/s, across the nozzle inlet. This array, as well as the arrays VI, PI, and RØI below, start with the centerline or centerbody value and end with the wall value. No default values are specified.
- VI(M) Same as UI, except radial velocity.
- PI(M) Same as UI, except pressure in psia or kPa.
- RØI(M) Same as UI, except density in lbm/ft³ or kg/m³.

The present version of this program allows for a maximum of 81 axial and 21 radial mesh points. To increase or decrease the maximum number of mesh points, the dimensions of the arrays QUT, QVT, and QPT in common AV, the arrays U,V,P, and RØ in common SØLUTN, the arrays XW, YW, NXNY, XWI, and YWI in common GEMTRY, the arrays XCB, YCB, NXNYCB, XCBI, and YCBI in common GCB, the arrays PT, TT, and THETA in common BCC, the arrays UI, VI, PI and RØI in program MAIN, the arrays YW and NXNY in subroutine GEØMCB, and the array CQ in subroutine PLØT must be changed to the desired values. In addition, card MAI 2950 must be changed such that LD and MD correspond to the new maximum axial and radial mesh points respectively.

C. Output Description

Program output consists of printed output, film plots, and punched cards for restart. The program has no options to output any results on magnetic tapes. For all computer-printed figures, the number zero has a slash through it, while the typed text has a slash through the letter O.

The first page (or first two pages in the tabular input nozzle case), of output includes the program title, abstract, list of control parameters, fluid model, flow geometry, nozzle geometry, and boundary conditions.

Following the title page is the initial-data surface. This data is either data that has been input or a one-dimensional solution that has been computed by the program. All units are given. At the bottom of the initial-data surface is the mass flow at the minimum cross section (MASS), the thrust (THRUST) due to the exit momentum only, the inlet

mass flow (MASSI), and the exit mass flow (MASSE). For planar flow the mass flow units are lbm/in-s or kg/in-s and the thrust units are lb_f/in. or newtons/in. When the initial-data surface is the one-dimensional solution calculated by the program, the mass flow and thrust values are also the one-dimensional values, even though the velocity components are not.

After the initial-data surface has been printed, the solution surfaces are printed. These surfaces have the same format as the initial-data surface. Each solution surface gives the flowfield for a certain value of time. As many solution planes as desired are printed by varying the input data. If the artificial viscosity option is used, a page of artificial viscosity parameters is printed before each solution plane. Also, film plots are made for each requested time step. When the computation is stopped because the flow has satisfied the convergence tolerance, the physical time equals TSTØP, or the maximum number of time steps has been reached, the final solution plane is always printed and plotted. As in the case of the initial-data surface, the mass flow and thrust are printed below the solution surface. The thrust calculation includes only the exit momentum.

D. Sample Calculations

1. Case No. 1 - Converging-Diverging Nozzle.

The nozzle geometry for this case is shown in Fig. 1a. and results are shown in Fig. 2. The data deck and printed output are presented in Figs. 7 and 8, respectively.

a. Namelist CNTRL. This case used a 21x8 mesh; therefore, LMAX = 21 and MMAX = 8. The maximum number of time steps NMAX is set equal to 400. The convergence tolerance TCØNV is set equal to 0.003. The step-size premultiplier FDT is set equal to 1.6. The additional parameters are left equal to their default values.

b. Namelist IVS. A one-dimensional, subsonic-sonic-supersonic, initial-data surface was computed by the program; therefore, no input is required.

c. Namelist GEMTRY. For this case, the nozzle wall is a conical, converging-diverging nozzle; therefore, NGEØM = 2. The axial location of the inlet XI equals 0.31 in., the radius of the inlet RI equals 2.5 in., the radius of the throat RT equals 0.8 in., and the axial location of the exit XE equals 4.05 in. The radius of curvature of the inlet RCI

```

CASE NO. 1 - CONVERGING-DIVERGING NOZZLE (45 DEG INLET, 15 DEG EXIT)
$CNTRL LMAX=21,MMAX=8,NMAX=400,TCONV=0.003,FDT=1.6 $
$IVS $
$GENTRY NGEOM=2,XI=0.31,RI=2.5,RT=0.8,XE=4.05,RCI=0.8,RCI=0.5,ANGI=44.8A,
ANGE=15.0 $
$GCBL $
$BC PT=70.0,TT=80.0 $

```

Fig. 7. Case No. 1 data deck.

NAP, A COMPUTER PROGRAM FOR THE COMPUTATION OF TWO-DIMENSIONAL, TIME-DEPENDENT, INVISCID NOZZLE FLOW
BY MICHAEL C. CLINE, T-3 - LOS ALAMOS SCIENTIFIC LABORATORY

PROGRAM ABSTRACT -

THE EQUATIONS OF MOTION FOR TWO-DIMENSIONAL, TIME DEPENDENT, INVISCID FLOW IN A NOZZLE ARE SOLVED USING THE SECOND-ORDER, MACCORMACK, FINITE-DIFFERENCE SCHEME, THE FLUID IS ASSUMED TO BE A PERFECT GAS, ALL BOUNDARY CONDITIONS ARE COMPUTED USING A SECOND-ORDER, REFERENCE PLANE CHARACTERISTIC SCHEME, THE STEADY STATE SOLUTION IS OBTAINED AS THE ASYMPTOTIC SOLUTION FOR LARGE TIME, THE NOZZLES MAY BE EITHER CONVERGING, CONVERGING-DIVERGING, OR PLUG GEOMETRIES,

JOB TITLE -

CASE NO. 1 - CONVERGING-DIVERGING NOZZLE (45 DEG INLET, 15 DEG EXIT)

CONTROL PARAMETERS -

LMAX=21 MMAX= 0 NMAX= 400 NPRINT= 0 TCONV= .003 FDT=1.60 NSTAG=0 NASH=1 IUNIT=0
IUI=1 IUC=1 IEX=1 NCONVI= 1 YSTOP=1.00000 NID= 1 NPLOT= -1 IPUNCH=0 ISUPER=0
IAV=0 CAV= 5.0 XMU=1.00 XLA=0.00 RKMU= .50 CTA= .50 LSS= 2 SMP= .95 NST= 0

FLUID MODEL -

THE RATIO OF SPECIFIC HEATS, GAMMA =1.4000 AND THE GAS CONSTANT, R = 53.3500 (FT-LBF/LBM-R)

FLOW GEOMETRY -

AXISYMMETRIC FLOW HAS BEEN SPECIFIED

NOZZLE GEOMETRY -

A CIRCULAR-ARC, CONICAL NOZZLE HAS BEEN SPECIFIED BY XI= .3100 (IN), RI= 2.5000 (IN),
RT= .8000 (IN), XE= 4.0500 (IN), RCI= .8000 (IN), RCT= .5000 (IN), ANGI= 44.00 (DEG),
AND ANGE= 15.00 (DEG). THE COMPUTED VALUES ARE XT= 2.5540 (IN) AND RE= 1.1832 (IN).

BOUNDARY CONDITIONS -

PI= 70.0000 (PSIA) TI= 80.0000 (F) THETA= 0.0000 (DEG) PE= 14.7000 (PSIA)

N= 10
N= 20
N= 30
N= 40
N= 50
N= 60
N= 70
N= 80
N= 90
N= 100
N= 110
N= 120
N= 130

Fig. 8. Case No. 1 output.

N# 140
N# 150
N# 160
N# 170
N# 180
N# 190
N# 200
N# 210
N# 220
N# 230
N# 240
N# 250
N# 260
N# 270
N# 280
N# 290
N# 300

Fig. 8 (cont)

SOLUTION SURFACE NO. 301 - TIME = .00162916 SECONDS (DELTA T = .00000541)

L	M	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBM/FT ³)	Q (FPS)	MACH NO	T (F)
1	1	.3100	0.0300	144.3320	-0.0000	69.2160	.347087	144.3320	.1269	78.2651
1	2	.3100	.3571	141.7219	-0.0000	69.2440	.347187	141.7219	.1246	78.3272
1	3	.3100	.7143	128.2883	-0.0000	69.3801	.347675	128.2883	.1128	78.6293
1	4	.3100	1.0714	109.3612	-0.0000	69.5491	.348279	109.3612	.0961	79.0040
1	5	.3100	1.4286	86.4350	-0.0000	69.7181	.348884	86.4350	.0759	79.3778
1	6	.3100	1.7857	62.2730	-0.0000	69.8536	.349368	62.2730	.0547	79.6771
1	7	.3100	2.1429	39.9999	-0.0000	69.9396	.349675	39.9999	.0351	79.8668
1	8	.3100	2.5000	19.8533	-0.0000	69.9851	.349838	19.8533	.0174	79.9672
2	1	.4970	0.0000	146.0691	0.0000	69.2904	.347288	146.0691	.1284	78.5319
2	2	.4970	.3540	143.4827	-4.4481	69.3196	.347388	143.5516	.1262	78.6038
2	3	.4970	.7080	130.0260	-8.4555	69.4507	.347845	130.3006	.1145	78.9123
2	4	.4970	1.0619	110.9310	-10.9369	69.6135	.348395	111.4688	.0979	79.3234
2	5	.4970	1.4159	87.8029	-11.7973	69.7741	.348920	88.5919	.0778	79.7545
2	6	.4970	1.7699	63.3199	-10.8059	69.8959	.349328	64.2353	.0564	80.0651
2	7	.4970	2.1239	40.7250	-8.3105	69.9730	.349708	41.5643	.0365	80.0739
2	8	.4970	2.4778	20.2377	-4.8653	70.0063	.349850	20.8143	.0183	80.1108
3	1	.6840	0.0000	153.2220	0.0000	69.1441	.346842	153.2220	.1347	78.0858
3	2	.6840	.3439	150.4176	-8.0795	69.1721	.346941	150.6344	.1325	78.1501
3	3	.6840	.6878	136.5817	-15.2234	69.2963	.347379	137.4275	.1208	78.4365
3	4	.6840	1.0317	116.4617	-19.6710	69.4572	.347946	118.1113	.1038	78.8078
3	5	.6840	1.3755	92.1280	-21.2109	69.6187	.348556	94.5382	.0831	79.1154
3	6	.6840	1.7194	66.2422	-19.7198	69.7494	.349177	69.1149	.0607	79.1672
3	7	.6840	2.0633	42.2740	-15.8931	69.8388	.349479	45.1628	.0397	79.3908
3	8	.6840	2.4072	21.3548	-11.2935	69.8902	.349784	24.1572	.0212	79.3180
4	1	.8710	0.0000	165.0230	0.0000	69.0375	.346366	165.0230	.1451	77.9945
4	2	.8710	.3243	161.8471	-12.7268	69.0718	.346482	162.3467	.1428	78.0821
4	3	.8710	.6487	148.1388	-24.0734	69.2124	.346970	150.0821	.1319	78.4187
4	4	.8710	.9739	127.6638	-31.8727	69.4034	.347638	131.5824	.1156	78.8667
4	5	.8710	1.2973	102.9220	-35.8438	69.6042	.348388	108.9846	.0957	79.2632
4	6	.8710	1.6217	76.1942	-35.2481	69.7817	.348968	83.9523	.0737	79.7398
4	7	.8710	1.9460	51.5053	-32.0512	69.9154	.349415	60.6636	.0532	80.0812
4	8	.8710	2.2703	29.4211	-28.9397	70.0166	.349804	41.2688	.0362	81.4995
5	1	1.0580	0.0000	184.0563	0.0000	68.7938	.345583	184.0563	.1620	77.3041
5	2	1.0580	.2977	180.4888	-16.5732	68.8270	.345704	181.2481	.1595	77.3811
5	3	1.0580	.5955	167.0840	-31.6930	68.9608	.346189	170.0632	.1496	77.6716
5	4	1.0580	.8932	146.2731	-42.9213	69.1497	.346899	152.4403	.1341	78.0406
5	5	1.0580	1.1909	120.6574	-49.3831	69.3592	.347728	130.3722	.1146	78.3850
5	6	1.0580	1.4887	92.4029	-49.9827	69.5637	.348495	105.0170	.0923	78.7833
5	7	1.0580	1.7864	66.3097	-46.6519	69.7342	.349073	81.0763	.0712	79.2094
5	8	1.0580	2.0841	45.6459	-45.4552	69.8646	.351093	64.4183	.0567	77.2645
6	1	1.2450	0.0000	208.6485	0.0000	68.3644	.343931	208.6485	.1838	76.5209
6	2	1.2450	.2711	204.5468	-20.3330	68.4076	.344081	205.5549	.1810	76.6265
6	3	1.2450	.5423	191.1932	-39.2038	68.5551	.344612	195.1712	.1718	76.9548
6	4	1.2450	.8134	169.6380	-54.0883	68.7762	.345419	178.0522	.1567	77.4270
6	5	1.2450	1.0845	142.5697	-63.7640	69.0343	.346336	156.1792	.1374	78.0158
6	6	1.2450	1.3557	111.8738	-65.9052	69.3108	.347214	129.8432	.1141	78.7985
6	7	1.2450	1.6268	83.9892	-64.4311	69.5343	.348057	105.8563	.0930	79.2339
6	8	1.2450	1.8979	60.8033	-60.6288	69.8047	.348123	85.9223	.0753	81.2287
7	1	1.4320	0.0000	244.4324	0.0000	67.8755	.342319	244.4324	.2155	75.1934
7	2	1.4320	.2445	239.7789	-25.3265	67.9268	.342507	241.1127	.2126	75.3031
7	3	1.4320	.4891	226.5992	-49.2547	68.0787	.343078	231.8906	.2044	75.6076
7	4	1.4320	.7336	204.3108	-69.2211	68.3138	.343971	215.7177	.1901	76.0607
7	5	1.4320	.9781	174.9460	-82.8765	68.6031	.345044	193.5836	.1705	76.6578
7	6	1.4320	1.2226	140.4528	-87.7474	68.9166	.346251	165.6098	.1458	77.2313

Fig. 8 (cont)

SOLUTION SURFACE NO. 301 - TIME = .00162716 SECONDS (DELTA T = .00000541)

L	"	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBH/FT3)	Q (FPS)	MACH NO	T (F)
7	7	1.4320	1.4672	107.5888	-85.8497	69.2024	.347572	137.6427	.1211	77.7176
7	8	1.4320	1.7117	79.2457	-78.9145	69.5794	.349485	111.8364	.0984	77.3792
8	1	1.6190	0.0000	289.8529	0.0000	66.7858	.338237	289.8529	.2561	72.9549
8	2	1.6190	.2179	284.6910	-28.5977	66.9547	.338482	286.1237	.2528	73.1195
8	3	1.6190	.4359	271.8205	-56.1340	67.0238	.339096	277.5561	.2451	73.4932
8	4	1.6190	.6538	248.8184	-88.3286	67.2999	.340096	261.4613	.2388	74.1227
8	5	1.6190	.8717	217.8973	-98.7450	67.6666	.341368	238.4991	.2103	75.8325
8	6	1.6190	1.0896	178.2156	-108.4389	68.1022	.342872	208.6898	.1838	76.1139
8	7	1.6190	1.3076	139.1469	-118.3320	68.5385	.344469	177.5810	.1563	77.0468
8	8	1.6190	1.5255	103.3920	-128.9598	69.3688	.345942	145.9131	.1279	81.2318
9	1	1.8060	0.0000	353.4364	0.0000	65.5800	.334882	353.4364	.3132	69.8416
9	2	1.8060	.1913	348.2441	-34.5414	65.6636	.334394	349.9529	.3101	70.0227
9	3	1.8060	.3826	336.6731	-68.5580	65.8359	.335051	343.5825	.3043	70.3717
9	4	1.8060	.5740	314.9155	-100.6910	66.1349	.336185	330.6213	.2927	70.9827
9	5	1.8060	.7653	282.8929	-128.3042	66.5481	.337729	310.6298	.2748	71.8578
9	6	1.8060	.9566	248.3598	-147.2737	67.8482	.339698	281.8987	.2491	72.7483
9	7	1.8060	1.1479	192.8554	-154.1167	67.6139	.341812	246.2463	.2174	73.9216
9	8	1.8060	1.3393	133.7156	-133.1567	68.7510	.346700	188.7076	.1664	75.2468
10	1	1.9930	0.0000	436.8635	0.0000	62.9419	.324223	436.8635	.3893	63.9988
10	2	1.9930	.1647	432.1713	-35.7768	63.0217	.324588	433.6496	.3864	64.1953
10	3	1.9930	.3294	423.3175	-71.8588	63.1559	.324995	429.8775	.3822	64.5243
10	4	1.9930	.4942	404.2725	-107.9751	63.4842	.325878	418.4434	.3725	65.1589
10	5	1.9930	.6589	373.7684	-142.2246	63.7957	.327237	399.9133	.3556	66.2876
10	6	1.9930	.8236	328.4187	-171.8434	64.2934	.329012	370.6682	.3292	67.4514
10	7	1.9930	.9883	264.4466	-185.8527	65.8844	.331875	322.7626	.2862	69.3341
10	8	1.9930	1.1538	173.8843	-172.3688	65.8445	.333145	244.2672	.2157	73.4752
11	1	2.1800	0.0000	549.3454	0.0000	59.7185	.312647	549.3454	.4935	55.5636
11	2	2.1800	.1381	546.9087	-38.8868	59.7792	.312892	548.2758	.4925	55.6838
11	3	2.1800	.2762	543.1126	-79.2687	59.8393	.313169	548.8669	.4938	55.7461
11	4	2.1800	.4144	534.6434	-124.1219	59.9824	.313885	548.8623	.4929	55.9318
11	5	2.1800	.5525	518.7335	-174.8851	60.2578	.314978	547.4286	.4914	56.3641
11	6	2.1800	.6906	491.7599	-234.3386	60.7872	.316985	544.7487	.4888	56.9273
11	7	2.1800	.8287	448.5535	-301.6778	61.5756	.320739	540.5643	.4844	58.1852
11	8	2.1800	.9668	392.7455	-391.1038	61.5951	.321452	554.2664	.4972	57.1991
12	1	2.3670	0.0000	703.1835	0.0000	53.3954	.288589	703.1835	.6419	39.4842
12	2	2.3670	.1195	705.4581	-38.2450	53.2788	.288114	706.1862	.6448	39.8686
12	3	2.3670	.2389	711.9686	-62.2785	52.9868	.286719	714.6793	.6533	38.8537
12	4	2.3670	.3584	724.8761	-98.6945	52.2435	.284195	730.7714	.6692	36.1859
12	5	2.3670	.4779	742.4833	-142.4451	51.1951	.280222	756.8238	.6945	33.1228
12	6	2.3670	.5974	769.8538	-199.6792	49.5354	.274167	795.3273	.7347	27.6732
12	7	2.3670	.7168	806.1984	-274.8574	47.8968	.266882	851.4989	.7946	17.8985
12	8	2.3670	.8363	926.4913	-373.6663	48.8628	.242468	999.8858	.9555	-5.1888
13	1	2.5540	0.0000	867.9594	0.0000	45.7225	.258957	867.9594	.8111	16.5731
13	2	2.5540	.1143	873.9191	-18.6820	45.4031	.257720	874.1188	.8177	15.5161
13	3	2.5540	.2266	887.6345	-37.8442	44.6459	.254768	888.4489	.8333	13.8183
13	4	2.5540	.3429	914.6763	-56.5883	43.2240	.249189	916.4197	.8648	8.1917
13	5	2.5540	.4571	958.2686	-72.8883	40.8916	.239928	961.8287	.9148	.8397
13	6	2.5540	.5714	1029.4131	-84.1867	37.8759	.224347	1032.8498	.9976	-13.9336
13	7	2.5540	.6857	1148.3874	-75.4358	38.8928	.197584	1150.7826	1.1425	-37.8882
13	8	2.5540	.8000	1368.1926	-8.8522	22.7786	.157750	1368.1926	1.4137	-78.2496
14	1	2.7410	0.0000	1057.9841	0.0000	36.8264	.218543	1057.9841	1.8231	-15.8889
14	2	2.7410	.1189	1067.8182	4.8614	35.4948	.216255	1067.8292	1.8349	-16.9857
14	3	2.7410	.2378	1089.2563	11.4888	34.3251	.211179	1089.3168	1.8689	-21.2789
14	4	2.7410	.3568	1130.3124	26.9883	32.2818	.201817	1130.6344	1.1114	-29.3362

Fig. 8 (cont)

SOLUTION SURFACE NO. 301 - TIME = .00162916 SECONDS (DELTA T = .00000541)

L	M	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBM/FT ³)	Q (FPS)	MACH NO	T (F)
14	5	2.7410	.4757	1193.1032	59.7150	28.9781	.187120	1194.5967	1.1919	-42.0154
14	6	2.7410	.5946	1286.8774	125.7866	24.3779	.165031	1293.0103	1.3210	-61.2883
14	7	2.7410	.7135	1418.7214	259.2371	18.2527	.133085	1442.2116	1.5291	-89.8075
14	8	2.7410	.8325	1505.1920	403.3150	13.9588	.100703	1558.2894	1.7074	-113.3946
15	1	2.9280	.0000	1229.8892	0.0000	27.4288	.179803	1229.8892	1.2364	-48.2460
15	2	2.9280	.1261	1248.8800	32.2297	26.8607	.177122	1241.2985	1.2516	-50.6718
15	3	2.9280	.2522	1263.7231	67.2349	25.6518	.171356	1265.4984	1.2843	-55.9399
15	4	2.9280	.3782	1305.5670	116.1644	23.5457	.161098	1318.7247	1.3462	-65.4968
15	5	2.9280	.5043	1363.5225	186.1417	20.6584	.146475	1376.1675	1.4388	-79.3179
15	6	2.9280	.6304	1434.6074	283.8963	17.2610	.128325	1462.4288	1.5657	-96.9372
15	7	2.9280	.7565	1495.9417	379.2887	14.3497	.111752	1543.2763	1.6918	-113.4188
15	8	2.9280	.8826	1523.8676	488.1848	13.2341	.104698	1576.7956	1.7414	-118.8198
16	1	3.1150	0.0000	1379.6124	0.0000	28.5366	.146067	1379.6124	1.4447	-88.5866
16	2	3.1150	.1332	1389.4688	57.2871	28.0520	.143567	1398.6493	1.4611	-83.8881
16	3	3.1150	.2665	1409.1488	116.9047	19.8318	.138250	1413.9898	1.4964	-88.4294
16	4	3.1150	.3977	1443.4828	190.1083	17.3330	.129183	1455.9477	1.5687	-97.8448
16	5	3.1150	.5330	1485.3858	276.8617	15.2534	.117647	1518.9669	1.6476	-110.8416
16	6	3.1150	.6662	1525.9339	367.4337	13.2773	.106148	1569.5483	1.7425	-122.3815
16	7	3.1150	.7994	1549.1994	421.6142	12.1092	.098925	1605.5458	1.8819	-129.6083
16	8	3.1150	.9327	1556.6257	417.8966	11.9876	.097596	1611.5375	1.8855	-128.4656
17	1	3.3020	0.0000	1507.1846	0.0000	15.3438	.118416	1507.1846	1.6440	-118.2754
17	2	3.3020	.1404	1514.6529	77.2857	14.9837	.116398	1516.6234	1.6597	-112.5417
17	3	3.3020	.2808	1529.1232	155.3746	14.2210	.112077	1536.9967	1.6942	-117.5164
17	4	3.3020	.4212	1552.9446	242.7868	13.8118	.105050	1571.8886	1.7537	-125.6938
17	5	3.3020	.5616	1577.8868	331.4854	11.7860	.097193	1612.8556	1.8239	-134.9123
17	6	3.3020	.7020	1595.3473	413.6915	10.7335	.091868	1645.6385	1.8821	-141.8784
17	7	3.3020	.8424	1597.4821	431.4881	10.4723	.089155	1654.6318	1.8956	-142.9533
17	8	3.3020	.9828	1597.3852	427.9967	10.5899	.089348	1653.6528	1.8859	-140.8538
18	1	3.4890	0.0000	1612.8423	0.0000	11.5688	.096652	1612.8423	1.8295	-136.9232
18	2	3.4890	.1476	1616.9281	91.6926	11.3298	.095191	1619.5259	1.8433	-138.7643
18	3	3.4890	.2951	1625.8324	182.2494	10.8849	.091988	1636.8152	1.8742	-142.9296
18	4	3.4890	.4427	1639.4993	276.8881	10.8197	.088843	1662.4818	1.9240	-149.2947
18	5	3.4890	.5902	1649.7378	358.9217	9.3866	.082482	1688.3296	1.9726	-155.1532
18	6	3.4890	.7378	1651.7627	412.3465	8.9842	.080145	1702.4548	1.9965	-157.4273
18	7	3.4890	.8853	1641.7622	427.9168	9.1585	.081814	1696.6129	1.9813	-154.8662
18	8	3.4890	1.0329	1638.9946	439.1673	9.2411	.081865	1696.8121	1.9733	-152.3877
19	1	3.6760	0.0000	1704.8268	0.0000	8.8149	.079438	1704.8268	2.0885	-168.4557
19	2	3.6760	.1547	1706.2877	101.8366	8.6716	.078488	1709.2764	2.0911	-161.7878
19	3	3.6760	.3094	1709.9698	198.9763	8.3402	.076384	1721.5868	2.0445	-164.9768
19	4	3.6760	.4641	1714.2779	293.1834	7.8884	.073245	1739.1688	2.0888	-169.3852
19	5	3.6760	.6189	1712.3564	365.8767	7.6860	.071258	1751.8884	2.1843	-171.8626
19	6	3.6760	.7736	1701.8635	403.9740	7.6934	.071783	1749.1524	2.0967	-170.3935
19	7	3.6760	.9283	1685.4753	428.4454	8.8075	.073682	1737.1245	2.0679	-166.3468
19	8	3.6760	1.0838	1682.1898	450.7198	7.9878	.073848	1741.4474	2.0677	-164.8157
20	1	3.8630	0.0000	1766.8661	0.0000	6.9239	.066761	1766.8661	2.1542	-188.8643
20	2	3.8630	.1619	1767.1843	105.9888	6.8519	.066258	1778.3558	2.1615	-188.8484
20	3	3.8630	.3237	1767.8745	206.8870	6.6633	.064921	1779.1443	2.1885	-182.9639
20	4	3.8630	.4856	1765.8631	297.6374	6.4524	.063388	1789.9821	2.2828	-185.2113
20	5	3.8630	.6475	1755.9466	368.1684	6.4495	.063276	1792.5837	2.2845	-184.8822
20	6	3.8630	.8094	1748.1859	391.2931	6.7291	.065123	1783.6368	2.1787	-181.8971
20	7	3.8630	.9712	1723.3741	415.9469	7.8217	.066976	1772.8593	2.1499	-177.8232
20	8	3.8630	1.1331	1719.3424	468.6964	6.9351	.065991	1779.9942	2.1559	-176.3486
21	1	4.0580	0.0000	1829.7862	0.0000	5.8329	.054892	1829.7862	2.3553	-208.8585
21	2	4.0580	.1698	1828.8818	118.7794	5.8322	.054812	1831.4345	2.3559	-208.5265

Fig. 8 (cont)

SOLUTION SURFACE NO. 301 - TIME = .00162916 SECONDS (DELTA T = .00000541)

L	M	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBM/FT ³)	Q (FPS)	MACH NO	T (F)					
21	3	4.0500	.3381	1824.1799	214.7978	4.9865	.053538	1836.7827	2.3632	-208.6011					
21	4	4.0500	.5071	1815.8484	302.0914	5.0164	.053515	1840.8054	2.3607	-206.9819					
21	5	4.0500	.6761	1799.5367	354.4601	5.2938	.055301	1834.1141	2.3278	-201.6568					
21	6	4.0500	.8451	1778.5083	378.6123	5.7648	.058542	1818.3617	2.2752	-194.2078					
21	7	4.0500	1.0142	1761.2728	411.4485	6.0360	.060351	1808.6933	2.2456	-190.0439					
21	8	4.0500	1.1832	1756.5757	470.6731	5.8824	.058942	1818.5418	2.2603	-190.6220					
MASS=		3.1653 (LBM/SEC)		THRUST=		172.3716 (LBF)		MASS1=		3.3454		MASS2=		3.1829	

Fig. 8 (cont)

equals 0.8 in., while the radius of curvature of the throat RCT equals 0.5 in. The angle of the converging section ANGI equals 44.88° , while the angle of the diverging section is 15° . No other input is required.

d. Namelist GCBL. This nozzle has no centerbody, and no input is required.

e. Namelist BC. The total pressure PT equals 70 psia and the total temperature TT equals 80°F . No other input is required.

2. Case No. 2 - Converging Nozzle. The nozzle geometry for this case is shown in Fig. 1b and results are shown in Fig. 3. The data deck and printed output are presented in Figs. 9 and 10, respectively.

a. Namelist CNTRL. This case uses a 23×7 mesh; therefore, LMAX = 23 and MMAX = 7. The maximum number of time steps NMAX is set equal to 400. The convergence tolerance TC \emptyset NV is set equal to 0.005. The step-size premultiplier FDT is set equal to 1.4. The additional parameters are left equal to their default values.

b. Namelist IVS. No input is required because a one-dimensional, subsonic-sonic-supersonic, initial-data surface was computed by the program.

c. Namelist GEMTRY. For this case, the nozzle is a conical converging nozzle and either the NGE \emptyset M = 3 or 4 option could be used. For this case, the NGE \emptyset M = 4 option was chosen; therefore, the YW and NXNY arrays must be input. The axial location of the inlet XI equals -3.6 in. and the axial location of the exit XE equals 0.8 in. Since an exhaust jet calculation is required for convergent sonic nozzles, JFLAG is set equal to 1. The nozzle ends at the 19th axial mesh point; therefore, LJET is set equal to 20. The values of YW and NXNY for L = 20 to 23 are an initial guess of the shape of the exhaust jet. No other input is required.

d. Namelist GCBL. This nozzle has no centerbody, and no input is required.

e. Namelist BC. The total pressure PT equals 25.0 psia, the total temperature TT equals 180.0°F , and the ambient pressure to which the jet is exiting PE is 12.5 psia. No other input is required.

3. Case No. 3 - Converging-Diverging, Plug Nozzle. The nozzle geometry for this case is shown in Fig. 1c and results are shown in Fig. 4. The data deck and printed output are presented in Figs. 11 and 12, respectively.

a. Namelist CNTRL. This case used a 31 by 6 mesh; therefore, LMAX = 31 and MMAX = 6. The maximum number of time steps NMAX is set equal to 400. The convergence tolerance TC \emptyset NV is set equal to 0.005. The step-size premultiplier FDT is set equal to 1.6. The additional parameters are left equal to their default values.

b. Namelist IVS. A one-dimensional subsonic-sonic-supersonic, initial-data surface was computed by the program; therefore, no input is required.

c. Namelist GEMTRY. For this case, the nozzle wall is a constant area duct; therefore, NGE \emptyset M is set equal to 1. The axial location of the inlet XI and exit XE are equal to -4.44 and 2.96 in., respectively. The duct radius RI is 4.0 in. Since an exhaust jet calculation is required for plug nozzles, JFLAG is set equal to 1. The duct ends at the 22nd mesh point; therefore, LJET is set equal to 23. The NGE \emptyset M = 1 option specifies a constant radius as the initial guess of the shape of the exhaust jet. No other input is required.

d. Namelist GCBL. For this case, the nozzle centerbody is a conical, converging-diverging nozzle; therefore, NGCB = 2. The radii of the inlet RICB and throat RTCB sections are 1.3 and 3.365 in., respectively. The radii of curvature of the inlet RCICB and throat RCTCB, sections are 0.75 and 4.95 in., respectively. The angles of the inlet ANGICB and exit ANGECB sections are 45.0° and 10.0° , respectively. No other input is required.

e. Namelist BC. The total pressure PT equals 100.0 psia, the total temperature TT equals 70.0°F , and the ambient pressure to which the nozzle is exiting PE is 30.4 psia. No other input is required.

ACKNOWLEDGMENT

The initial phase of this research was accomplished while the author held a National Research Council Postdoctoral Resident Research Associateship supported by the NASA Langley Research Center, Hampton, VA.

REFERENCES

1. L. M. Saunders, "Numerical Solution of the Flow Field in the Throat Region of a Nozzle," Brown Engineering Co. report BSVD-P-66-TN-001 (NASA CR 82601) (August 1966).
2. R. F. Cuffel, L. H. Back, and P. F. Massier, "Transonic Flow-Field in a Supersonic Nozzle with Small Throat Radius of Curvature," AIAA J. 7, 1364-1366 (July 1969).

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CASE NO. 2 - CONVERGING NOZZLE (15 DEG INLET, PT/PE=2.0)
$CNTRL LMAX=23,MMAX=7,NMAX=400,TCONV=0.005,FDY=1.4 3
$IVS 3
$GEMTRY NGEOM=4,XI=-3.6,XE=0.8,JFLAG=1,LJET=20,
YW=1.93,1.91103,1.85744,1.80385,1.75026,1.69667,1.64308,1.58949,1.5359,
1.48231,1.42872,1.37513,1.32154,1.26795,1.21436,1.16077,1.10718,1.05359,
1.0,1.01,1.02,1.03,1.04,
NXNY=0.0,18*0.26795,4*-0.05 3
$GCBL 3
$BC PT=25,0,TT=180,0,PE=12.5 3

```

Fig. 9. Case No. 2 data deck.

NAP, A COMPUTER PROGRAM FOR THE COMPUTATION OF TWO-DIMENSIONAL, TIME-DEPENDENT, INVISCID NOZZLE FLOW

BY MICHAEL C. CLINE, T-3 - LOS ALAMOS SCIENTIFIC LABORATORY

PROGRAM ABSTRACT -

THE EQUATIONS OF MOTION FOR TWO-DIMENSIONAL, TIME DEPENDENT, INVISCID FLOW IN A NOZZLE ARE SOLVED USING THE SECOND-ORDER, MACCORMACK, FINITE-DIFFERENCE SCHEME, THE FLUID IS ASSUMED TO BE A PERFECT GAS. ALL BOUNDARY CONDITIONS ARE COMPUTED USING A SECOND-ORDER, REFERENCE PLANE CHARACTERISTIC SCHEME. THE STEADY STATE SOLUTION IS OBTAINED AS THE ASYMPTOTIC SOLUTION FOR LARGE TIME. THE NOZZLES MAY BE EITHER CONVERGING, CONVERGING-DIVERGING, OR PLUG GEOMETRIES,

JOB TITLE -

CASE NO. 2 - CONVERGING NOZZLE (15 DEG INLET, PT/PE=2.0)

CONTROL PARAMETERS -

LMAX=23	MMAX= 7	NMAX= 400	NPRINT= 0	TCNV= .005	FDT=1.40	NSTAG=0	NASH=1	IUNIT=0
IUI=1	IUD=1	IEX=1	NCONVI= 1	TSTOP=1.00000	NID= 1	NPLOT= -1	IPUNCH=0	ISUPER=0
IAD=0	CAV= 5.0	XMU=1.00	XLA=0.00	RKMU= .50	CTA= .50	LSS= 2	SMP= .95	NST= 0

FLUID MODEL -

THE RATIO OF SPECIFIC HEATS, GAMMA =1.4000 AND THE GAS CONSTANT, R = 53.3500 (FT-LBF/LBM-R)

FLOW GEOMETRY -

AXISYMMETRIC FLOW HAS BEEN SPECIFIED

Fig. 10. Case No. 2 output.

NOZZLE GEOMETRY -

A GENERAL NOZZLE HAS BEEN SPECIFIED BY THE FOLLOWING PARAMETERS, XT= -.0000 (IN), RT= 1.0000 (IN),

L	XW(IN)	YW(IN)	SLOPE
1	-3.6000	1.9300	-0.0000
2	-3.4000	1.9110	-.2680
3	-3.2000	1.8574	-.2680
4	-3.0000	1.8030	-.2680
5	-2.8000	1.7503	-.2680
6	-2.6000	1.6967	-.2680
7	-2.4000	1.6431	-.2680
8	-2.2000	1.5895	-.2680
9	-2.0000	1.5359	-.2680
10	-1.8000	1.4823	-.2680
11	-1.6000	1.4287	-.2680
12	-1.4000	1.3751	-.2680
13	-1.2000	1.3215	-.2680
14	-1.0000	1.2679	-.2680
15	-.8000	1.2144	-.2680
16	-.6000	1.1608	-.2680
17	-.4000	1.1072	-.2680
18	-.2000	1.0536	-.2680
19	-.0000	1.0000	-.2680
20	.2000	1.0100	.0500
21	.4000	1.0200	.0500
22	.6000	1.0300	.0500
23	.8000	1.0400	.0500

AN EXHAUST JET CALCULATION HAS BEEN REQUESTED. THE NOZZLE ENDS AT X= -.0000 (IN). THE MESH POINTS L= 20 TO L= 23 ARE AN INITIAL APPROXIMATION TO THE EXHAUST JET BOUNDARY.

BOUNDARY CONDITIONS -

PT= 25.0000 (PSIA) TT= 180.0000 (F) THETA= 0.0000 (DEG) PE= 12.5000 (PSIA)

N= 10
N= 20
N= 30
N= 40
N= 50
N= 60
N= 70
N= 80
N= 90
N= 100
N= 110
N= 120
N= 130
N= 140
N= 150
N= 160
N= 170
N= 180
N= 190
N= 200
N= 210
N= 220
N= 230
N= 240
N= 250

Fig. 10 (cont)

SOLUTION SURFACE NO. 250 - TIME = .00150212 SECONDS (DELTA T = .00000638)

L	H	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBH/FT3)	Q (FPS)	MACH NO	T (F)
1	1	-3.6000	0.0000	218.2506	-0.0000	24.4617	.103809	218.2506	.1765	176.0323
1	2	-3.6000	.5217	216.3467	-0.0000	24.4710	.103837	216.3467	.1750	176.1012
1	3	-3.6000	.6433	211.0650	-0.0000	24.4963	.103914	211.0650	.1707	176.2889
1	4	-3.6000	.9650	202.4249	-0.0000	24.5363	.104035	202.4249	.1637	176.5859
1	5	-3.6000	1.2867	189.9110	-0.0000	24.5914	.104202	189.9110	.1535	176.9940
1	6	-3.6000	1.6083	174.1160	-0.0000	24.6561	.104398	174.1160	.1407	177.4720
1	7	-3.6000	1.9300	164.5359	-0.0000	24.6934	.104510	164.5359	.1329	177.7474
2	1	-3.4000	0.0000	220.5038	0.0000	24.4990	.103923	220.5038	.1783	176.3022
2	2	-3.4000	.3185	218.7409	-4.0464	24.5109	.103960	218.7783	.1769	176.3904
2	3	-3.4000	.6370	213.8199	-8.2875	24.5401	.104048	213.9805	.1730	176.6059
2	4	-3.4000	.9555	205.9606	-13.4604	24.5896	.104198	206.4000	.1668	176.9704
2	5	-3.4000	1.2740	194.7161	-20.2002	24.6637	.104423	195.7611	.1582	177.5146
2	6	-3.4000	1.5925	180.9249	-29.6254	24.7622	.104722	183.3343	.1480	178.2341
2	7	-3.4000	1.9110	174.0626	-46.6401	24.8416	.104960	180.2029	.1454	178.8254
3	1	-3.2000	0.0000	227.1668	0.0000	24.4463	.103763	227.1668	.1838	175.9150
3	2	-3.2000	.3096	225.7720	-5.3792	24.4543	.103787	225.8360	.1827	175.9741
3	3	-3.2000	.6191	221.6900	-10.9482	24.4738	.103846	221.9601	.1795	176.1190
3	4	-3.2000	.9287	215.5644	-17.4423	24.5049	.103941	216.2689	.1749	176.3485
3	5	-3.2000	1.2383	207.0481	-25.0312	24.5548	.104092	208.5557	.1686	176.7162
3	6	-3.2000	1.5479	198.1668	-35.7006	24.6088	.104257	201.3569	.1627	177.1105
3	7	-3.2000	1.8574	198.2077	-53.1097	24.6476	.104374	205.1997	.1658	177.3994
4	1	-3.0000	0.0000	235.6639	0.0000	24.4175	.103676	235.6639	.1907	175.6968
4	2	-3.0000	.3006	234.4539	-7.3429	24.4250	.103699	234.5689	.1898	175.7526
4	3	-3.0000	.6013	230.8325	-14.8498	24.4423	.103752	231.3097	.1871	175.8806
4	4	-3.0000	.9019	225.5461	-23.0375	24.4701	.103836	226.7196	.1834	176.0856
4	5	-3.0000	1.2026	218.3708	-31.7397	24.5143	.103971	220.6654	.1784	176.4092
4	6	-3.0000	1.5032	211.9665	-43.1284	24.5537	.104092	216.3096	.1749	176.6889
4	7	-3.0000	1.8038	212.2437	-56.8707	24.6087	.104231	219.7309	.1776	177.0544
5	1	-2.8000	0.0000	247.5469	0.0000	24.3459	.103458	247.5469	.2004	175.1670
5	2	-2.8000	.2917	246.5466	-8.7738	24.3526	.103479	246.7027	.1997	175.2160
5	3	-2.8000	.5834	243.3623	-17.7079	24.3666	.103521	244.0057	.1975	175.3216
5	4	-2.8000	.8751	238.7445	-27.0514	24.3904	.103594	240.2721	.1944	175.4974
5	5	-2.8000	1.1668	232.0556	-37.0282	24.4250	.103699	235.7813	.1908	175.7524
5	6	-2.8000	1.4585	227.6809	-48.4235	24.4573	.103798	232.7812	.1883	175.9860
5	7	-2.8000	1.7503	228.6649	-61.2708	24.5005	.103929	236.7314	.1914	176.3066
6	1	-2.6000	0.0000	261.7128	0.0000	24.2648	.103213	261.7128	.2119	174.5560
6	2	-2.6000	.2828	260.8302	-10.1521	24.2709	.103232	261.0277	.2114	174.6021
6	3	-2.6000	.5656	257.8653	-20.3801	24.2848	.103274	258.6694	.2094	174.7047
6	4	-2.6000	.8483	253.6428	-30.8959	24.3073	.103343	255.5175	.2069	174.8705
6	5	-2.6000	1.1311	248.3621	-41.6794	24.3390	.103440	251.8351	.2038	175.1021
6	6	-2.6000	1.4139	243.7855	-53.3241	24.3676	.103529	249.5492	.2020	175.3015
6	7	-2.6000	1.6967	244.3368	-65.4700	24.4135	.103665	252.9561	.2047	175.6627
7	1	-2.4000	0.0000	278.6913	0.0000	24.1552	.102879	278.6913	.2258	173.7395
7	2	-2.4000	.2738	277.8506	-11.4203	24.1616	.102899	278.0932	.2253	173.7883
7	3	-2.4000	.5477	275.0155	-22.8667	24.1768	.102942	275.9645	.2236	173.8962
7	4	-2.4000	.8215	270.9450	-34.4379	24.1995	.103014	273.1248	.2213	174.0711
7	5	-2.4000	1.0954	265.9299	-46.0672	24.2306	.103129	269.8906	.2186	174.3033
7	6	-2.4000	1.3692	261.4584	-57.9952	24.2601	.103199	267.7156	.2168	174.5205
7	7	-2.4000	1.6431	261.2947	-70.0139	24.3087	.103348	270.5122	.2190	174.8742
8	1	-2.2000	0.0000	298.2684	0.0000	24.0233	.102479	298.2684	.2419	172.7423
8	2	-2.2000	.2649	297.4346	-12.6689	24.0303	.102500	297.7043	.2414	172.7947
8	3	-2.2000	.5298	294.5968	-25.3010	24.0464	.102549	295.6813	.2398	172.9156
8	4	-2.2000	.7947	290.4766	-37.9156	24.0724	.102629	292.9407	.2375	173.1089
8	5	-2.2000	1.0597	285.3708	-50.3370	24.1059	.102732	289.7842	.2349	173.3559

Fig. 10 (cont)

SOLUTION SURFACE NO. 250 - TIME = .00158212 SECONDS (DELTA T = .00000638)

L	M	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBH/FT3)	Q (FPS)	MACH NO	T (F)
8	6	-2.2000	1.3246	280.4825	-62.7287	24.1385	.102833	287.4114	.2329	173.5864
8	7	-2.2000	1.5895	279.4577	-74.8807	24.1921	.102992	289.3160	.2344	174.8116
9	1	-2.0000	0.0000	320.7490	0.0000	23.8619	.101985	320.7490	.2604	171.5322
9	2	-2.0000	.2560	319.8654	-13.9317	23.8697	.102009	320.1687	.2599	171.5911
9	3	-2.0000	.5120	316.9519	-27.7697	23.8881	.102065	318.1661	.2582	171.7312
9	4	-2.0000	.7679	312.6118	-41.4462	23.9188	.102156	315.3473	.2559	171.9570
9	5	-2.0000	1.0239	307.1939	-54.7331	23.9557	.102271	312.0317	.2531	172.2427
9	6	-2.0000	1.2799	301.6978	-67.7192	23.9939	.102387	309.2046	.2508	172.5310
9	7	-2.0000	1.5359	299.5372	-80.2610	24.0541	.102574	310.1038	.2514	172.9667
10	1	-1.8000	0.0000	346.3661	0.0000	23.6682	.101395	346.3661	.2815	170.8524
10	2	-1.8000	.2471	345.3925	-15.2419	23.6768	.101421	345.7286	.2810	170.1177
10	3	-1.8000	.4941	342.3345	-30.3344	23.6978	.101486	343.6758	.2793	170.2769
10	4	-1.8000	.7412	337.6399	-45.1344	23.7321	.101591	340.6432	.2767	170.5347
10	5	-1.8000	.9882	331.7133	-59.3789	23.7754	.101724	336.9860	.2737	170.8565
10	6	-1.8000	1.2353	325.4397	-73.1379	23.8208	.101866	333.5568	.2708	171.1825
10	7	-1.8000	1.4823	321.9512	-86.2668	23.8898	.102071	333.3085	.2705	171.7416
11	1	-1.6000	0.0000	375.5134	0.0000	23.4324	.100671	375.5134	.3056	168.2648
11	2	-1.6000	.2381	374.4108	-16.6154	23.4421	.100700	374.7873	.3050	168.3393
11	3	-1.6000	.4762	371.1089	-33.0393	23.4659	.100773	372.6485	.3032	168.5224
11	4	-1.6000	.7144	366.0622	-49.0830	23.5053	.100894	369.3381	.3005	168.8245
11	5	-1.6000	.9525	359.5270	-64.4590	23.5554	.101047	365.2597	.2970	169.2101
11	6	-1.6000	1.1906	352.3245	-79.1683	23.6098	.101213	361.1097	.2936	169.6314
11	7	-1.6000	1.4287	347.3365	-93.0688	23.6904	.101465	359.5893	.2922	170.2123
12	1	-1.4000	0.0000	408.9079	0.0000	23.1479	.099799	408.9079	.3334	166.0546
12	2	-1.4000	.2292	407.6655	-18.1308	23.1585	.099832	408.0685	.3327	166.1365
12	3	-1.4000	.4584	404.2326	-36.0390	23.1845	.099912	405.8359	.3308	166.3361
12	4	-1.4000	.6876	398.6307	-53.4933	23.2283	.100047	402.2039	.3278	166.6697
12	5	-1.4000	.9168	391.3549	-70.1610	23.2850	.100224	397.5943	.3239	167.0972
12	6	-1.4000	1.1459	383.0706	-86.0187	23.3495	.100426	392.6096	.3197	167.5669
12	7	-1.4000	1.3751	376.3341	-100.8387	23.4443	.100707	389.6098	.3171	168.3548
13	1	-1.2000	0.0000	447.1313	0.0000	22.7906	.098693	447.1313	.3653	163.2986
13	2	-1.2000	.2203	445.7369	-19.6613	22.8027	.098730	446.1704	.3645	163.3940
13	3	-1.2000	.4405	442.1427	-39.1094	22.8313	.098819	443.8690	.3626	163.6186
13	4	-1.2000	.6608	436.0959	-58.1395	22.8806	.098971	439.9543	.3593	164.0057
13	5	-1.2000	.8810	428.1243	-76.4190	22.9464	.099173	434.8911	.3550	164.5264
13	6	-1.2000	1.1013	418.6672	-93.7621	23.0238	.099408	429.0379	.3508	165.1462
13	7	-1.2000	1.3215	409.9834	-109.8551	23.1400	.099777	424.4462	.3461	165.9803
14	1	-1.0000	0.0000	491.8170	0.0000	22.3572	.097356	491.8170	.4030	159.8453
14	2	-1.0000	.2113	490.2796	-21.5428	22.3701	.097396	490.7527	.4021	159.9470
14	3	-1.0000	.4226	486.6123	-42.8966	22.3991	.097487	488.4994	.4002	160.1742
14	4	-1.0000	.6340	480.2180	-63.8922	22.4504	.097647	484.4498	.3967	160.5728
14	5	-1.0000	.8453	471.4310	-84.0395	22.5213	.097870	478.8631	.3920	161.1150
14	6	-1.0000	1.0566	460.5844	-103.1474	22.6094	.098150	471.9930	.3861	161.7650
14	7	-1.0000	1.2677	449.1457	-120.3486	22.7455	.098553	464.9899	.3800	162.9506
15	1	-.8000	0.0000	543.6828	0.0000	21.7821	.095555	543.6828	.4471	155.2834
15	2	-.8000	.2024	542.0487	-22.9703	21.7965	.095600	542.5352	.4461	155.4009
15	3	-.8000	.4048	538.4690	-45.8802	21.8258	.095691	540.4200	.4443	155.6414
15	4	-.8000	.6072	531.9002	-68.7134	21.8802	.095860	536.3202	.4408	156.0874
15	5	-.8000	.8096	522.6432	-91.1922	21.9605	.096107	530.5392	.4358	156.7555
15	6	-.8000	1.0120	510.3910	-112.8464	22.0651	.096426	522.7172	.4291	157.6460
15	7	-.8000	1.2144	496.5545	-133.0518	22.2581	.097051	514.0711	.4215	159.0362
16	1	-.6000	0.0000	605.7994	0.0000	21.0913	.093395	605.7994	.5005	149.5466
16	2	-.6000	.1935	604.2591	-25.2777	21.1046	.093437	604.7876	.4997	149.6538
16	3	-.6000	.3869	601.2402	-50.6770	21.1282	.093513	603.3722	.4984	149.8407

Fig. 10 (cont)

SOLUTION SURFACE NO. 250 - TIME = .00158212 SECONDS (DELTA T = .00000638)

L	H	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBM/FT3)	U (FPS)	MACH NO	T (F)
16	4	-.6000	.5804	595.4506	-76.5530	21.1741	.093661	600.3513	.4958	150.2000
16	5	-.6000	.7738	586.3424	-102.2688	21.2470	.093898	595.1943	.4913	150.7570
16	6	-.6000	.9673	573.5778	-128.0177	21.3467	.094228	587.6905	.4848	151.4746
16	7	-.6000	1.1608	553.1442	-148.2150	21.5507	.094828	572.6572	.4717	153.4126
17	1	-.4000	0.0000	679.9293	0.0000	20.1120	.090272	679.9293	.5656	141.3566
17	2	-.4000	.1845	678.6968	-25.3110	20.1200	.090297	679.1686	.5649	141.4296
17	3	-.4000	.3691	676.8210	-51.0818	20.1274	.090319	678.7459	.5646	141.5005
17	4	-.4000	.5536	672.4041	-77.9199	20.1488	.090384	676.9038	.5629	141.7062
17	5	-.4000	.7381	664.7553	-106.3046	20.1967	.090527	673.2015	.5596	142.1826
17	6	-.4000	.9226	649.7738	-136.1958	20.2636	.090717	663.8933	.5516	142.9160
17	7	-.4000	1.1072	627.9869	-168.2691	20.7049	.092179	650.1400	.5386	146.2742
18	1	-.2000	0.0000	767.7202	0.0000	18.9623	.086583	767.7202	.6441	131.1364
18	2	-.2000	.1756	767.7310	-26.9237	18.9591	.086574	768.2037	.6446	131.0940
18	3	-.2000	.3512	768.7246	-55.0030	18.9365	.086506	770.6898	.6468	130.8548
18	4	-.2000	.5268	770.0819	-86.4261	18.9007	.086403	774.9165	.6506	130.4457
18	5	-.2000	.7024	770.7476	-121.8434	18.8823	.086372	780.3190	.6553	130.0779
18	6	-.2000	.8780	774.0238	-175.1882	18.7029	.085858	793.6018	.6676	127.9712
18	7	-.2000	1.0536	731.2056	-195.9265	19.2978	.087683	756.9999	.6336	134.0480
19	1	.0000	0.0000	881.7838	0.0000	17.2847	.081088	881.7838	.7499	115.4064
19	2	.0000	.1667	884.8922	-21.7872	17.2351	.080919	885.1603	.7531	114.8961
19	3	.0000	.3333	892.4690	-44.5059	17.1895	.080589	893.5780	.7611	113.6201
19	4	.0000	.5000	907.4413	-69.5616	16.8712	.079729	910.1036	.7768	111.1565
19	5	.0000	.6667	929.8310	-95.3880	16.5257	.078596	934.7109	.8004	107.5286
19	6	.0000	.8333	978.9132	-136.3003	15.7535	.076019	988.4337	.8457	99.3511
19	7	.0000	1.0000	1016.1021	-147.6067	15.2390	.074031	1026.7674	.8886	95.6104
20	1	.2000	0.0000	1001.4017	0.0000	15.3667	.074543	1001.4017	.8660	96.4174
20	2	.2000	.1659	1006.6100	-10.2280	15.2797	.074239	1006.6620	.8713	95.5332
20	3	.2000	.3310	1010.5216	-20.1734	15.0807	.073541	1010.7213	.8833	93.5037
20	4	.2000	.4977	1041.5218	-28.0663	14.7043	.072212	1041.8999	.9066	89.6199
20	5	.2000	.6637	1074.2768	-28.8371	14.1890	.070371	1074.6638	.9397	84.2341
20	6	.2000	.8296	1138.3593	-40.2369	13.1441	.066588	1139.0702	1.0067	72.7999
20	7	.2000	.9955	1143.2730	-26.9502	12.4972	.064252	1193.5773	1.0626	64.9985
21	1	.4000	0.0000	1099.4854	0.0000	13.7553	.068831	1099.4854	.9657	79.4089
21	2	.4000	.1659	1103.1248	-1.2130	13.6961	.068616	1103.1255	.9695	78.7672
21	3	.4000	.3317	1111.2973	-2.4079	13.5634	.068134	1111.2999	.9780	77.3249
21	4	.4000	.4976	1125.6585	-2.8971	13.3319	.067290	1125.6623	.9930	74.7738
21	5	.4000	.6634	1140.3012	.7380	13.1050	.066459	1140.3014	1.0083	72.2436
21	6	.4000	.8293	1163.6872	-.5522	12.7467	.065140	1163.6873	1.0329	68.1722
21	7	.4000	.9951	1190.9668	-2.0159	12.4996	.064260	1190.9685	1.0603	65.0239
22	1	.6000	0.0000	1161.1336	0.0000	12.7426	.065154	1161.1336	1.0309	67.8962
22	2	.6000	.1660	1162.4664	1.8530	12.7227	.065079	1162.4678	1.0323	67.6732
22	3	.6000	.3320	1165.5589	3.5348	12.6768	.064908	1165.5642	1.0356	67.1596
22	4	.6000	.4980	1170.6776	4.7717	12.5970	.064612	1170.6873	1.0410	66.2712
22	5	.6000	.6640	1173.8592	7.0631	12.5493	.064427	1173.8804	1.0444	65.7481
22	6	.6000	.8299	1178.9652	7.5425	12.5091	.064270	1178.9893	1.0493	65.3489
22	7	.6000	.9959	1192.3993	4.7125	12.4965	.064249	1192.4086	1.0616	64.9867
23	1	.8000	0.0000	1222.7818	-0.0000	11.7299	.061477	1222.7818	1.0992	55.0064
23	2	.8000	.1661	1221.8079	4.9190	11.7494	.061543	1221.8178	1.0980	55.3043
23	3	.8000	.3322	1219.8205	9.4775	11.7902	.061682	1219.8573	1.0955	55.9309
23	4	.8000	.4984	1215.6967	12.4405	11.8637	.061934	1215.7603	1.0907	57.0332
23	5	.8000	.6645	1207.4172	13.4183	11.9936	.062396	1207.4918	1.0814	58.0296
23	6	.8000	.8306	1194.2432	15.6371	12.2716	.063399	1194.3456	1.0659	62.4479
23	7	.8000	.9967	1193.8317	4.7182	12.4934	.064238	1193.8410	1.0629	64.9495

MASS= 1.5757 (LBM/SEC) THRUST= 44.7800 (LBF) MASSI= 1.5915 MASSE= 1.5757

Fig. 10 (cont)

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CASE NO. 3 ~ CONVERGING=DIVERGING, PLUG NOZZLE (10 DEG CONE, PT/PE=3.29)
SCNTRL LMAX=31,MMAX=6,NMAX=400,TCONV=0.005,FDT=1.6  $
STVS  $
SGENTRY NGEOM=1,XI=-4.440,XE=2.9600,RI=4.0,JFLAG=1,LJET=23  $
$GCB L NGCB=2,RCB=1.3,RTCB=3.365,RCICB=0.75,RCTCB=4.95,
ANGICB=45.0,ANGECB=10.0  $
SBC PT=100.0,TT=70.0,PE=30.4  $

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Fig. 11. Case No. 3 data deck.

NAP, A COMPUTER PROGRAM FOR THE COMPUTATION OF TWO-DIMENSIONAL, TIME-DEPENDENT, INVISCID NOZZLE FLOW

BY MICHAEL C. CLINE, 1-3 - LOS ALAMOS SCIENTIFIC LABORATORY

PROGRAM ABSTRACT -

THE EQUATIONS OF MOTION FOR TWO-DIMENSIONAL, TIME DEPENDENT, INVISCID FLOW IN A NOZZLE ARE SOLVED USING THE SECOND-ORDER, MACCORMACK, FINITE-DIFFERENCE SCHEME. THE FLUID IS ASSUMED TO BE A PERFECT GAS. ALL BOUNDARY CONDITIONS ARE COMPUTED USING A SECOND-ORDER, REFERENCE PLANE CHARACTERISTIC SCHEME. THE STEADY STATE SOLUTION IS OBTAINED AS THE ASYMPTOTIC SOLUTION FOR LARGE TIME. THE NOZZLES MAY BE EITHER CONVERGING, CONVERGING-DIVERGING, OR PLUG GEOMETRIES.

JOB TITLE -

CASE NO. 3 - CONVERGING-DIVERGING, PLUG NOZZLE (10 DEG CONE, PT/PE=3.29)

CONTROL PARAMETERS -

LMAX=31 MMAX= 6 NMAX= 400 NPRINT= 0 TCONV= .005 FDT=1.60 NSTAG=0 NASH=1 IUNIT=0
IUI=1 IUO=1 IEX=1 NCONV= 1 TSTOP=1.00000 NID= 1 NPLOT= -1 IPUNCH=0 ISUPER=0
IAV=0 CAV= 5.0 XHU=1.00 XLA=0.00 RKMU= .50 CTA= .50 LSS= 2 SMP= .95 NST= 0

FLUID MODEL -

THE RATIO OF SPECIFIC HEATS, GAMMA =1.4000 AND THE GAS CONSTANT, R = 53.3500 (FT-LBF/LBM-R)

FLOW GEOMETRY -

AXISYMMETRIC FLOW HAS BEEN SPECIFIED

NOZZLE GEOMETRY -

A CONSTANT AREA DUCT HAS BEEN SPECIFIED BY XI= -4.4400 (IN), RI= 4.0000 (IN), AND XE= 2.9600 (IN)

AN EXHAUST JET CALCULATION HAS BEEN REQUESTED. THE NOZZLE ENDS AT X= .7400 (IN). THE MESH POINTS L= 23 TO L= 31 ARE AN INITIAL APPROXIMATION TO THE EXHAUST JET BOUNDARY.

A CIRCULAR-ARC, CONICAL CENTERBODY HAS BEEN SPECIFIED BY XTCB= -4.4400 (IN), RICB= 1.3000 (IN), RTCB= 3.3650 (IN), XECB= 2.9600 (IN), RCICB= .7500 (IN), RCTCB= 4.9500 (IN), ANGICB= 45.00 (DEG), AND ANGECB= 10.00 (DEG). THE COMPUTED VALUES ARE XTCB= -.0140 (IN) AND RECB= 2.9170 (IN).

BOUNDARY CONDITIONS -

PT= 100.0000 (PSIA) TT= 70.0000 (F) THETA= 0.0000 (DEG) PE= 30.4000 (PSIA)

N= 10
N= 20
N= 30
N= 40
N= 50
N= 60
N= 70
N= 80

Fig. 12. Case No. 3 output.

N= 90
N= 100
N= 110
N= 120
N= 130
N= 140
N= 150
N= 160
N= 170
N= 180
N= 190
N= 200
N= 210
N= 220
N= 230
N= 240
N= 250
N= 260
N= 270
N= 280
N= 290
N= 300
N= 310
N= 320
N= 330
N= 340

Fig. 12 (cont)

SOLUTION SURFACE NO. 345 - TIME = .00237634 SECONDS (DELTA T = .00000691)

L	M	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBM/FT ³)	Q (FPS)	MACH NO	T (F)
1	1	-4.4400	1.3000	109.4812	-0.0000	99.3430	.506883	109.4812	.0971	69.0027
1	2	-4.4400	1.8400	106.0169	-0.0000	99.3831	.507029	106.0169	.0940	69.0638
1	3	-4.4400	2.3800	212.9815	-0.0000	97.5259	.500243	212.9815	.1894	66.2199
1	4	-4.4400	2.9200	236.6861	-0.0000	96.9532	.498143	236.6861	.2107	65.3351
1	5	-4.4400	3.4600	276.8857	-0.0000	95.8470	.494076	276.8857	.2468	63.6156
1	6	-4.4400	4.0000	273.4428	-0.0000	95.9570	.494481	273.4428	.2437	63.7873
2	1	-4.1933	1.3417	107.4307	37.4142	99.2108	.506393	113.7593	.1009	68.8098
2	2	-4.1933	1.8734	104.0377	29.6151	99.2062	.506362	108.1707	.0960	68.8175
2	3	-4.1933	2.4050	214.2242	22.4820	97.4455	.499962	215.3593	.1915	66.0820
2	4	-4.1933	2.9367	237.1094	13.9520	96.9338	.498071	237.5195	.2114	65.3056
2	5	-4.1933	3.4683	277.6715	7.3298	95.8509	.494092	277.7683	.2476	63.6205
2	6	-4.1933	4.0000	274.0878	0.0000	95.9535	.494468	274.0878	.2443	63.7824
3	1	-3.9467	1.4851	112.9896	98.6735	98.7348	.504664	150.0103	.1332	68.0751
3	2	-3.9467	1.9881	119.2811	55.7369	99.1459	.506168	131.6609	.1168	68.6990
3	3	-3.9467	2.4911	230.3713	50.8948	97.1220	.498801	235.9263	.2099	65.5554
3	4	-3.9467	2.9940	245.1004	28.8405	96.7471	.497390	246.7914	.2197	65.0115
3	5	-3.9467	3.4970	284.0408	15.4501	95.6688	.493423	284.4796	.2537	63.3345
3	6	-3.9467	4.0000	279.0134	0.0000	95.8206	.493979	279.0134	.2487	63.5740
4	1	-3.7000	1.7293	133.0260	133.0260	97.9867	.501924	188.1272	.1672	66.9351
4	2	-3.7000	2.1835	152.2549	70.3057	98.2987	.503055	167.7034	.1490	67.4243
4	3	-3.7000	2.6376	251.8800	69.9268	96.4944	.496505	261.4141	.2328	64.5736
4	4	-3.7000	3.0917	258.5497	37.0252	96.2556	.495578	261.1873	.2327	64.2546
4	5	-3.7000	3.5459	293.1525	20.9197	95.3831	.492369	293.8980	.2622	62.8874
4	6	-3.7000	4.0000	287.4930	0.0000	95.5579	.493011	287.4930	.2564	63.1645
5	1	-3.4533	1.9750	165.0872	159.4938	97.2086	.499081	229.5475	.2042	65.7285
5	2	-3.4533	2.3800	189.7552	88.9515	97.4650	.500033	209.5695	.1864	66.1113
5	3	-3.4533	2.7850	274.0965	86.3530	95.8902	.494289	287.3773	.2562	63.6267
5	4	-3.4533	3.1900	275.5988	45.2297	95.7240	.493625	279.2855	.2498	63.4220
5	5	-3.4533	3.5950	305.6406	25.4583	95.0148	.491013	306.7070	.2738	62.3876
5	6	-3.4533	4.0000	300.2397	0.0000	95.1903	.491657	300.2397	.2679	62.5870
6	1	-3.2067	2.1978	205.2765	173.2552	96.0735	.494989	268.6183	.2394	63.9703
6	2	-3.2067	2.5582	229.6718	104.2084	96.2531	.495595	252.1495	.2247	64.2229
6	3	-3.2067	2.9187	297.7834	94.9364	95.0783	.491294	312.5506	.2790	62.3581
6	4	-3.2067	3.2791	296.9730	50.8083	94.9696	.490842	301.2929	.2689	62.2412
6	5	-3.2067	3.6396	321.7514	27.9020	94.4542	.488941	322.9590	.2885	61.4256
6	6	-3.2067	4.0000	317.4202	0.0000	94.6142	.489529	317.4202	.2835	61.6822
7	1	-2.9600	2.3929	246.1173	182.2747	94.9109	.490626	306.2642	.2734	62.1473
7	2	-2.9600	2.7143	267.6866	117.9731	95.0919	.491347	292.5299	.2611	62.3756
7	3	-2.9600	3.0357	323.2732	100.9577	94.2213	.488127	338.6709	.3027	61.0076
7	4	-2.9600	3.3571	321.5757	56.3837	94.1319	.487751	326.4813	.2918	60.9145
7	5	-2.9600	3.6786	341.9079	29.8608	93.7507	.486340	343.2094	.3069	60.3106
7	6	-2.9600	4.0000	338.8474	0.0000	93.8859	.486837	338.8474	.3030	60.5294
8	1	-2.7133	2.5647	289.9157	188.6100	93.5079	.485435	345.8682	.3094	59.9300
8	2	-2.7133	2.8514	307.9821	127.9301	93.7199	.486292	333.4952	.2983	60.1912
8	3	-2.7133	3.1385	353.1446	104.0948	93.1129	.484017	368.1668	.3296	59.2511
8	4	-2.7133	3.4257	350.7214	60.2814	93.0513	.483748	355.8642	.3186	59.1957
8	5	-2.7133	3.7128	367.0750	30.9629	92.7906	.482778	368.3786	.3299	58.7817
8	6	-2.7133	4.0000	365.0832	0.0000	92.9035	.483193	365.0832	.3269	58.9667
9	1	-2.4667	2.7146	335.9522	191.6407	91.9380	.479683	386.7687	.3469	57.4175
9	2	-2.4667	2.9717	350.4988	134.3668	92.1960	.480650	375.3716	.3365	57.7394
9	3	-2.4667	3.2288	387.1967	105.6010	91.7925	.479105	401.3389	.3600	57.1358
9	4	-2.4667	3.4859	384.1126	63.0205	91.7586	.478944	389.2481	.3492	57.1185
9	5	-2.4667	3.7429	397.2721	31.6727	91.5882	.478304	398.5327	.3576	56.8485
9	6	-2.4667	4.0000	396.0271	0.0000	91.6830	.478654	396.0271	.3553	57.0061

Fig. 12 (cont)

SOLUTION SURFACE NO. 345 - TIME = .00237634 SECONDS (DELTA T = .00000691)

L	M	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBH/FT3)	Q (FPS)	MACH NO	T (F)
10	1	-2.2200	2.8463	385.7795	192.0533	90.0749	.472645	430.9412	.3876	54.3954
10	2	-2.2200	3.0770	396.9902	137.6490	90.3795	.473882	420.1767	.3778	54.7871
10	3	-2.2200	3.3078	426.5248	105.6109	90.1440	.472945	439.4053	.3952	54.4635
10	4	-2.2200	3.5385	422.6905	64.3804	90.1463	.472923	427.5654	.3845	54.5002
10	5	-2.2200	3.7693	433.1660	31.9255	90.0516	.472562	434.3409	.3907	54.3518
10	6	-2.2200	4.0000	432.3408	0.0000	90.1354	.472872	432.3408	.3888	54.4940
11	1	-1.9733	2.9607	440.1175	189.7053	87.8573	.464311	479.2614	.4326	50.7368
11	2	-1.9733	3.1606	448.0872	138.0339	88.2164	.465769	468.8662	.4230	51.2102
11	3	-1.9733	3.3764	471.3597	104.1647	88.1287	.465373	482.7320	.4356	51.1456
11	4	-1.9733	3.5843	466.6714	64.4745	88.1745	.465519	471.1042	.4250	51.2510
11	5	-1.9733	3.7921	474.8778	31.7414	88.1431	.465393	475.9374	.4294	51.2060
11	6	-1.9733	4.0000	474.2174	0.0000	88.2221	.465686	474.2174	.4278	51.3423
12	1	-1.7267	3.8593	500.0783	184.4158	85.1723	.454142	532.9986	.4833	46.2146
12	2	-1.7267	3.2474	504.7398	135.5893	85.6008	.455882	522.6344	.4736	46.8202
12	3	-1.7267	3.4356	522.3541	101.1329	85.6519	.456001	532.0542	.4820	46.9892
12	4	-1.7267	3.6237	516.6715	63.2783	85.7507	.456353	520.5320	.4715	47.1831
12	5	-1.7267	3.8119	522.8704	31.0492	85.7759	.456442	523.7915	.4744	47.2336
12	6	-1.7267	4.0000	522.1891	0.0000	85.8554	.456738	522.1891	.4729	47.3748
13	1	-1.4800	3.1429	566.2529	175.5815	81.9333	.441756	592.8501	.5405	40.6179
13	2	-1.4800	3.3143	567.4408	130.0717	82.4540	.443870	582.1578	.5304	41.4801
13	3	-1.4800	3.4858	579.7939	96.2310	82.6443	.444521	587.7255	.5352	41.8215
13	4	-1.4800	3.6572	572.9430	60.6967	82.8076	.445125	576.1491	.5245	42.1299
13	5	-1.4800	3.8286	577.3073	29.7520	82.8869	.445422	578.0735	.5262	42.2757
13	6	-1.4800	4.0000	576.4726	0.0000	82.9705	.445737	576.4726	.5246	42.4267
14	1	-1.2333	3.2125	639.0676	162.4290	78.0504	.426727	659.3865	.6054	33.6883
14	2	-1.2333	3.3700	636.5520	121.0465	78.6926	.429342	647.9589	.5943	34.7195
14	3	-1.2333	3.5275	643.9203	89.0877	79.0292	.430567	650.0539	.5958	35.4213
14	4	-1.2333	3.6850	635.7200	56.5499	79.2706	.431485	638.2302	.5847	35.8779
14	5	-1.2333	3.8425	638.3532	27.7308	79.4040	.431995	638.9553	.5852	36.1254
14	6	-1.2333	4.0000	637.2739	0.0000	79.4949	.432340	637.2739	.5835	36.2970
15	1	-.9867	3.2685	718.4278	143.9795	73.4700	.408725	732.7132	.6786	25.1849
15	2	-.9867	3.4148	711.9765	107.8925	74.2675	.411994	720.1048	.6660	26.5599
15	3	-.9867	3.5611	714.5835	79.2171	74.7626	.413865	718.9610	.6642	27.5894
15	4	-.9867	3.7074	704.8565	50.5751	75.0970	.415164	706.6686	.6524	28.2372
15	5	-.9867	3.8537	705.8355	24.8312	75.2871	.415905	706.2721	.6518	28.6006
15	6	-.9867	4.0000	704.4402	0.0000	75.3868	.416293	704.4402	.6500	28.7919
16	1	-.7400	3.3115	803.7732	119.1784	68.1821	.387547	812.5607	.7607	14.8693
16	2	-.7400	3.4492	793.2104	89.8965	69.1705	.391649	798.2882	.7458	16.7076
16	3	-.7400	3.5869	791.2734	66.8987	69.8382	.394253	794.0294	.7408	18.1298
16	4	-.7400	3.7246	779.9013	42.4700	70.2801	.396011	781.0568	.7280	19.0199
16	5	-.7400	3.8623	779.2786	20.8999	70.5298	.397005	779.5588	.7262	19.5177
16	6	-.7400	4.0000	777.5410	0.0000	70.6408	.397439	777.5410	.7242	19.7486
17	1	-.4933	3.3417	893.9432	86.9769	62.2513	.363220	898.1644	.8519	2.6020
17	2	-.4933	3.4734	879.1927	66.3566	63.4636	.368344	881.6933	.8340	5.0490
17	3	-.4933	3.6050	873.0032	49.2059	64.3169	.371780	874.3888	.8254	6.9467
17	4	-.4933	3.7367	859.9066	31.9340	64.8781	.374068	860.4994	.8113	8.1395
17	5	-.4933	3.8683	857.7794	15.7672	65.1907	.375342	857.9243	.8083	8.7992
17	6	-.4933	4.0000	855.6361	0.0000	65.3116	.375837	855.6361	.8059	9.0498
18	1	-.2467	3.3595	987.1818	46.4557	55.8187	.336086	988.2743	.9522	-11.7118
18	2	-.2467	3.4876	968.3785	36.6601	57.2806	.342422	969.0721	.9303	-8.4827
18	3	-.2467	3.6157	958.2832	28.1325	58.3275	.346782	958.6961	.9179	-6.0113
18	4	-.2467	3.7438	943.5326	18.7218	59.0161	.349673	943.7183	.9020	-4.4493
18	5	-.2467	3.8719	939.9736	9.3489	59.3931	.351253	940.0201	.8976	-3.6020
18	6	-.2467	4.0000	937.6150	0.0000	59.5321	.351811	937.6150	.8950	-3.2594

Fig. 12 (cont)

SOLUTION SURFACE NO. 345 - TIME = .00237634 SECONDS (DELTA T = .00000691)

L	M	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBH/FT3)	Q (FPS)	MACH NO	T (F)
19	1	.0000	3.3650	1081.4354	-3.0549	49.1261	.306824	1081.4393	1.0612	-27.8336
19	2	.0000	3.4920	1058.8194	.3966	50.8497	.314533	1058.8195	1.0340	-23.6353
19	3	.0000	3.6190	1045.5491	2.5186	52.0884	.319889	1045.5522	1.0172	-20.4885
19	4	.0000	3.7460	1029.0488	2.6347	52.9016	.323416	1029.0521	.9990	-18.4954
19	5	.0000	3.8730	1024.3133	1.4601	53.3412	.325314	1024.3143	.9932	-17.4236
19	6	.0000	4.0000	1020.9992	0.0000	53.4719	.325911	1020.9992	.9897	-17.1525
20	1	.2467	3.3581	1173.1244	-61.8584	42.3494	.276131	1174.7541	1.1778	-46.0380
20	2	.2467	3.4865	1148.0302	-42.2793	44.3423	.285302	1148.8084	1.1443	-40.6080
20	3	.2467	3.6149	1132.0781	-26.9501	45.7752	.291831	1132.3988	1.1227	-36.6236
20	4	.2467	3.7433	1114.2692	-15.5124	46.7326	.296129	1114.3772	1.1014	-34.0414
20	5	.2467	3.8716	1107.7929	-6.9782	47.2613	.298489	1107.8149	1.0932	-32.6288
20	6	.2467	4.0000	1107.0192	0.0000	47.5041	.299451	1107.0192	1.0913	-31.8133
21	1	.4933	3.3389	1269.0032	-130.7462	35.7235	.244355	1275.7200	1.3101	-65.3967
21	2	.4933	3.4711	1238.3914	-93.2116	37.9196	.255030	1241.8944	1.2646	-58.6786
21	3	.4933	3.6034	1219.8855	-62.9528	39.5784	.262856	1221.5088	1.2360	-53.5867
21	4	.4933	3.7356	1200.0219	-39.8646	40.7549	.268366	1200.6576	1.2097	-50.0979
21	5	.4933	3.8678	1193.6524	-20.1323	41.3780	.271205	1193.8222	1.2002	-48.3097
21	6	.4933	4.0000	1179.4275	0.0000	41.3454	.271483	1179.4275	1.1867	-48.9338
22	1	.7400	3.3072	1331.6916	-205.2378	30.9496	.220443	1347.4142	1.4120	-81.0462
22	2	.7400	3.4458	1305.5170	-155.2045	32.8860	.230385	1314.7103	1.3663	-74.7132
22	3	.7400	3.5843	1288.8579	-111.5273	34.4362	.238202	1293.6743	1.3360	-69.7912
22	4	.7400	3.7229	1272.2609	-71.9720	35.4028	.243148	1274.2950	1.3113	-66.9984
22	5	.7400	3.8614	1267.2158	-32.7531	35.8114	.245264	1267.6390	1.3026	-65.8919
22	6	.7400	4.0000	1286.7778	0.0000	35.2207	.241585	1286.7778	1.3233	-66.4902
23	1	.9867	3.2649	1383.2720	-243.9082	27.2685	.201293	1404.6112	1.4984	-94.3544
23	2	.9867	3.4123	1374.5314	-187.5136	28.2471	.206581	1387.2628	1.4731	-90.9272
23	3	.9867	3.5596	1374.0087	-128.3918	28.8864	.209959	1380.0740	1.4609	-88.6462
23	4	.9867	3.7070	1372.0843	-67.7226	29.0913	.210905	1373.7546	1.4524	-87.6901
23	5	.9867	3.8543	1375.5143	-12.7883	29.2328	.211388	1375.5738	1.4524	-86.7353
23	6	.9867	4.0016	1355.3965	9.0224	30.4018	.217243	1355.4266	1.4227	-82.2787
24	1	1.2333	3.2214	1434.0378	-252.0596	24.1425	.184583	1456.1601	1.5809	-106.9657
24	2	1.2333	3.3752	1436.4195	-196.1252	24.5272	.186714	1449.7469	1.5706	-105.4328
24	3	1.2333	3.5291	1442.6305	-135.8278	24.8334	.188222	1449.0107	1.5664	-103.8817
24	4	1.2333	3.6829	1429.7078	-89.7732	25.6828	.192670	1432.5235	1.5486	-100.2039
24	5	1.2333	3.8367	1397.4981	-69.4626	27.8136	.203959	1399.2234	1.4878	-91.9200
24	6	1.2333	3.9905	1354.6985	-61.0675	30.3938	.217202	1356.0742	1.4234	-82.2982
25	1	1.4800	3.1779	1401.9167	-261.3019	21.3229	.168627	1504.7777	1.6616	-118.6924
25	2	1.4800	3.3359	1482.1809	-207.8316	21.7522	.171088	1496.6810	1.6481	-116.8278
25	3	1.4800	3.4939	1474.3214	-165.8729	22.8291	.177072	1483.6231	1.6224	-112.0096
25	4	1.4800	3.6519	1433.9630	-149.1645	25.1620	.189852	1441.7004	1.5549	-102.2670
25	5	1.4800	3.8098	1392.5720	-137.2705	27.8314	.204048	1399.3220	1.4877	-91.8457
25	6	1.4800	3.9678	1349.1683	-124.2698	30.4025	.217246	1354.8794	1.4221	-82.2663
26	1	1.7267	3.1344	1509.8281	-266.2235	20.0212	.161484	1533.1197	1.7096	-125.3505
26	2	1.7267	3.2942	1499.4577	-251.5096	20.6565	.165113	1520.4047	1.6878	-122.3211
26	3	1.7267	3.4540	1463.9559	-241.1145	22.8440	.177299	1483.6789	1.6230	-112.2279
26	4	1.7267	3.6137	1417.7407	-227.3063	25.5073	.191743	1435.8471	1.5457	-100.9358
26	5	1.7267	3.7735	1380.4098	-207.8969	27.9914	.204894	1395.9772	1.4830	-91.2585
26	6	1.7267	3.9333	1342.5048	-187.8490	30.4071	.217269	1355.5834	1.4228	-82.2483
27	1	1.9733	3.0909	1459.0269	-257.2658	22.5791	.175554	1481.5348	1.6221	-112.8446
27	2	1.9733	3.2505	1447.6522	-284.2170	22.7877	.176792	1475.2885	1.6135	-112.0919
27	3	1.9733	3.4101	1421.8776	-293.0628	24.3402	.185340	1451.7650	1.5730	-105.5272
27	4	1.9733	3.5696	1394.0753	-279.9659	26.1367	.195040	1421.9095	1.5251	-98.2955
27	5	1.9733	3.7292	1365.8397	-260.7981	28.2135	.206032	1390.5157	1.4754	-90.3841
27	6	1.9733	3.8888	1334.1585	-240.7433	30.4107	.217288	1355.7051	1.4229	-82.2369

Fig. 12 (cont)

SOLUTION SURFACE NO. 345 - TIME = .00237634 SECONDS (DELTA T = .00000691)

L	M	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBM/FT3)	Q (FPS)	MACH NO	T (F)
28	1	2.2200	3.0475	1410.7945	-248.7612	25.4098	.192169	1432.5583	1.5469	-103.1005
28	2	2.2200	3.2047	1406.2072	-302.8893	25.0046	.189801	1438.4577	1.5561	-104.4101
28	3	2.2200	3.3620	1391.8446	-333.8577	25.5297	.192227	1431.3254	1.5421	-101.5240
28	4	2.2200	3.5193	1370.4248	-334.0730	26.7231	.190370	1410.5562	1.5090	-96.3879
28	5	2.2200	3.6766	1346.7431	-320.5242	28.5479	.207844	1384.3600	1.4667	-89.2631
28	6	2.2200	3.8339	1317.7933	-293.3750	30.3985	.217221	1350.0549	1.4170	-82.2726
29	1	2.4667	3.0040	1291.9779	-227.8106	32.9470	.231216	1311.9087	1.3646	-75.3852
29	2	2.4667	3.1572	1303.0941	-283.3728	31.6862	.224897	1333.5495	1.3950	-79.7104
29	3	2.4667	3.3104	1313.7524	-335.5893	30.4038	.218006	1355.9372	1.4256	-83.5673
29	4	2.4667	3.4637	1313.3000	-362.5924	29.8082	.214542	1362.4354	1.4352	-84.9830
29	5	2.4667	3.6169	1309.8925	-363.4159	30.1072	.215866	1359.3710	1.4292	-83.5434
29	6	2.4667	3.7702	1315.1981	-339.5192	30.3952	.217210	1358.3149	1.4257	-82.2946
30	1	2.7133	2.9605	1194.3369	-210.5938	40.0065	.264795	1212.7615	1.2251	-52.1976
30	2	2.7133	3.1101	1210.9114	-238.5102	38.6329	.258294	1234.1772	1.2530	-56.2885
30	3	2.7133	3.2598	1240.8253	-278.4410	36.0241	.245565	1271.6827	1.3037	-64.0377
30	4	2.7133	3.4095	1267.3081	-314.9771	33.3000	.242040	1305.8638	1.3535	-72.6441
30	5	2.7133	3.5591	1293.9764	-334.6486	31.3972	.222419	1336.5495	1.3968	-78.9811
30	6	2.7133	3.7088	1306.3885	-325.0857	30.3957	.217212	1346.2286	1.4130	-82.2909
31	1	2.9600	2.9170	1096.6960	-193.3771	47.0660	.298373	1113.6143	1.1009	-38.2290
31	2	2.9600	3.0631	1118.7287	-193.6476	45.5797	.291692	1135.3648	1.1278	-38.2301
31	3	2.9600	3.2092	1167.8982	-221.2927	41.6444	.273125	1188.6785	1.1953	-48.4494
31	4	2.9600	3.3552	1221.3161	-267.3618	36.7919	.249537	1250.2381	1.2785	-62.0356
31	5	2.9600	3.5013	1278.0603	-305.8814	32.6871	.228973	1314.1543	1.3657	-74.6800
31	6	2.9600	3.6474	1297.5788	-322.8935	30.3963	.217213	1337.1503	1.4035	-82.2872

MASS= 33.9930 (LBM/SEC) THRUST= 1353.5464 (LBF) MASSI= 34.5377 MASSE= 33.8257

8EJ

Fig. 12 (cont)

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APPENDIX A

ETA CONSTANT REFERENCE PLANE CHARACTERISTIC RELATIONS

I. EQUATIONS OF MOTION

The equations of motion, Eqs. (6) through (9), can be written as

$$\rho_\tau + u\rho_\zeta + \rho u_\zeta = -\bar{v}\rho_\eta - \rho\alpha u_\eta - \rho\beta v_\eta - \epsilon\rho v\beta/\eta, \quad (\text{A-1})$$

$$u_\tau + uu_\zeta + p_\zeta/\rho = -\bar{v}u_\eta - \alpha p_\eta/\rho, \quad (\text{A-2})$$

$$v_\tau + uv_\zeta = -\bar{v}v_\eta - \beta p_\eta/\rho, \quad (\text{A-3})$$

$$p_\tau + up_\zeta - a^2(\rho_\tau + u\rho_\zeta) = -\bar{v}p_\eta + a^2\bar{v}\rho_\eta. \quad (\text{A-4})$$

Letting

$$\psi_1 = -\bar{v}\rho_\eta - \rho\alpha u_\eta - \rho\beta v_\eta - \epsilon\rho v\beta/\eta, \quad (\text{A-5})$$

$$\psi_2 = -\bar{v}u_\eta - \alpha p_\eta/\rho, \quad (\text{A-6})$$

$$\psi_3 = -\bar{v}v_\eta - \beta p_\eta/\rho, \quad (\text{A-7})$$

$$\psi_4 = -\bar{v}p_\eta + a^2\bar{v}\rho_\eta, \quad (\text{A-8})$$

Eqs. (A-1) through (A-4) become

$$\rho_\tau + u\rho_\zeta + \rho u_\zeta = \psi_1, \quad (\text{A-9})$$

$$u_\tau + uu_\zeta + p_\zeta/\rho = \psi_2, \quad (\text{A-10})$$

$$v_\tau + uv_\zeta = \psi_3, \quad (A-11)$$

$$p_\tau + up_\zeta - a^2\rho_\tau - a^2u\rho_\zeta = \psi_4. \quad (A-12)$$

II. CHARACTERISTIC CURVES

A linear combination of the equations of motion can be formed by multiplying Eqs. (A-9) through (A-12) by ℓ_i , $i = 1, 2, 3, 4$, respectively, and then summing them. This linear combination can be written as

$$\begin{aligned} & \ell_1 (\rho_\tau + u\rho_\zeta + \rho u_\zeta - \psi_1) \\ & + \ell_2 (u_\tau + uu_\zeta + p_\zeta/\rho - \psi_2) + \ell_3 (v_\tau + uv_\zeta - \psi_3) \\ & + \ell_4 (p_\tau + up_\zeta - a^2\rho_\tau - a^2u\rho_\zeta - \psi_4) = 0. \end{aligned} \quad (A-13)$$

Rearrangement of Eq. (A-13) yields

$$\begin{aligned} & (u\ell_1 - a^2u\ell_4)\rho_\zeta + (\ell_1 - a^2\ell_4)\rho_\tau + (\rho\ell_1 + u\ell_2)u_\zeta \\ & + \ell_2u_\tau + u\ell_3v_\zeta + \ell_3v_\tau + (\ell_2/\rho + u\ell_4)p_\zeta + \ell_4p_\tau \\ & = \ell_1\psi_1 + \ell_2\psi_2 + \ell_3\psi_3 + \ell_4\psi_4. \end{aligned} \quad (A-14)$$

The following set of vectors can be defined, where the components are the coefficients of the partial derivatives in Eq. (A-14).

$$W_1 = (u\ell_1 - a^2u\ell_4, \ell_1 - a^2\ell_4), \quad (A-15)$$

$$W_2 = (\rho\ell_1 + u\ell_2, \ell_2), \quad (A-16)$$

$$W_3 = (u\ell_3, \ell_3), \quad (A-17)$$

$$W_4 = (\ell_2/\rho + u\ell_4, \ell_4). \quad (A-18)$$

Therefore, Eq. (A-14) can be written as

$$\begin{aligned} & d_{W_1} \rho + d_{W_2} u + d_{W_3} v + d_{W_4} p \\ & = \ell_1\psi_1 + \ell_2\psi_2 + \ell_3\psi_3 + \ell_4\psi_4, \end{aligned} \quad (A-19)$$

where $d_{W_1} \rho$ is defined as the derivative of ρ in the direction of the vector W_1 , etc.

A question is now posed: Can the ℓ_i , $i = 1, 2, 3, 4$, be chosen such that the vectors W_j , $j = 1, 2, 3, 4$, would be linearly dependent or, in other words, would lie in one direction. If such ℓ_i do exist, the curve which contains the vectors W_j is called the characteristic curve, its normal N is called the characteristic normal, and Eq. (A-19) is called the compatibility equation. Therefore, if $N = (N_\zeta, N_\tau)$ is the characteristic normal in the ζ - τ plane, N and W_j are related by

$$N \cdot W_j = 0 \quad (j = 1, 2, 3, 4). \quad (A-20)$$

When Eq. (A-20) is expanded,

$$(u\ell_1 - a^2u\ell_4) N_\zeta + (\ell_1 - a^2\ell_4) N_\tau = 0, \quad (A-21)$$

$$(\rho\ell_1 + u\ell_2) N_\zeta + \ell_2 N_\tau = 0, \quad (A-22)$$

$$u\ell_3 N_\zeta + \ell_3 N_\tau = 0, \quad (A-23)$$

$$(\ell_2/\rho + u\ell_4) N_\zeta + \ell_4 N_\tau = 0. \quad (A-24)$$

In matrix form, Eqs. (A-21) through (A-24) become

$$\begin{vmatrix} uN_\zeta + N_\tau & 0 & 0 & -a^2(uN_\zeta + N_\tau) \\ pN_\zeta & uN_\zeta + N_\tau & 0 & 0 \\ 0 & 0 & uN_\zeta + N_\tau & 0 \\ 0 & N_\zeta/\rho & 0 & uN_\zeta + N_\tau \end{vmatrix} \begin{vmatrix} \ell_1 \\ \ell_2 \\ \ell_3 \\ \ell_4 \end{vmatrix} = 0. \quad (A-25)$$

Equation (A-25) is a system of homogeneous equations. For Eq. (A-25) to have a nontrivial solution, the coefficient matrix must be singular; in other words, its determinant must equal zero. Setting the determinant equal to zero yields

$$(uN_\zeta + N_\tau)^2 [(uN_\zeta + N_\tau)^2 - a^2 N_\zeta^2] = 0. \quad (A-26)$$

Setting the first factor of Eq. (A-26) equal to zero yields

$$uN_\zeta + N_\tau = 0 . \quad (A-27)$$

Setting the second factor of Eq. (A-26) equal to zero yields

$$uN_\zeta + N_\tau = \pm aN_\zeta . \quad (A-28)$$

Noting that $d\zeta/d\tau = -N_\tau/N_\zeta$, Eqs. (A-27) and (A-28) can be written as

$$d\zeta/d\tau = u , \quad (A-29)$$

$$d\zeta/d\tau = u\bar{a} . \quad (A-30)$$

Equation (A-29) represents the projection of the flow pathlines on the $\eta = \text{constant}$ planes. Equation (A-30) represents the projection of the Mach cones on the $\eta = \text{constant}$ planes.

III. SOLUTION FOR THE ℓ_i

If the compatibility equation (A-19) is to be used, the arbitrary parameters ℓ_i must be evaluated in the following manner. Consider first the characteristic curve given by Eq. (A-27). Substituting Eq. (A-27) into Eq. (A-25) yields

$$\begin{vmatrix} 0 & 0 & 0 & 0 \\ \rho N_\zeta & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & N_\zeta/\rho & 0 & 0 \end{vmatrix} \begin{vmatrix} \ell_1 \\ \ell_2 \\ \ell_3 \\ \ell_4 \end{vmatrix} = 0 . \quad (A-31)$$

Since the rank of the coefficient matrix of Eq. (A-31) is two, there are two independent solutions for ℓ_i . From Eq. (A-31),

$$\ell_1 = \ell_2 = 0, \ell_3 \text{ and } \ell_4 \text{ are arbitrary.} \quad (A-32)$$

Therefore, two possible solutions are

$$\ell_1 = \ell_2 = \ell_3 = 0, \ell_4 = 1 , \quad (A-33)$$

$$\ell_1 = \ell_2 = \ell_4 = 0, \ell_3 = 1 . \quad (A-34)$$

Consider next the characteristic curve given by Eq. (A-28). Substituting Eq. (A-28) into Eq. (A-25) yields

$$\begin{vmatrix} \pm aN_\zeta & 0 & 0 & \mp a^3 N_\zeta \\ \rho N_\zeta & \pm aN_\zeta & 0 & 0 \\ 0 & 0 & \pm aN_\zeta & 0 \\ 0 & N_\zeta/\rho & 0 & \pm aN_\zeta \end{vmatrix} \begin{vmatrix} \ell_1 \\ \ell_2 \\ \ell_3 \\ \ell_4 \end{vmatrix} = 0 . \quad (A-35)$$

Since the rank of the coefficient matrix of Eq. (A-35) is three, there is only one independent solution for ℓ_i . From Eq. (A-35),

$$\ell_3 = 0, \ell_1 = a^2 \ell_4, \ell_2 = \mp \rho a \ell_4 . \quad (A-36)$$

Therefore, one possible solution is

$$\ell_1 = a^2, \ell_2 = \mp \rho a, \ell_3 = 0, \ell_4 = 1 . \quad (A-37)$$

IV. COMPATIBILITY EQUATIONS

Substituting Eqs. (A-33) and (A-34) into Eq. (A-14) yields

$$p_\tau + u p_\zeta - a^2 (\rho_\tau + u \rho_\zeta) = \psi_4 , \quad (A-38)$$

$$v_\tau + u v_\zeta = \psi_3 . \quad (A-39)$$

Substituting Eq. (A-37) into Eq. (A-14) yields

$$\begin{aligned} & a^2 (\rho_\tau + u \rho_\zeta + \rho u_\zeta - \psi_1) \mp \rho a (u_\tau + u u_\zeta + p_\zeta/\rho - \psi_2) \\ & + p_\tau + u p_\zeta - a^2 (\rho_\tau + u \rho_\zeta) - \psi_4 = 0 . \end{aligned} \quad (A-40)$$

Equations (A-38) through (A-40) can be written as

$$dp - a^2 d\rho = \psi_4 d\tau \quad \left\{ \begin{array}{l} \text{for } d\zeta = u d\tau , \end{array} \right. \quad (A-41)$$

$$dv = \psi_3 d\tau \quad \left\{ \begin{array}{l} \text{for } d\zeta = u d\tau , \end{array} \right. \quad (A-42)$$

$$dp - \rho a du = (\psi_4 + a^2 \psi_1 - \rho a \psi_2) d\tau \quad \text{for } d\zeta = (u-a) d\tau , \quad (A-43)$$

$$dp + \rho a du = (\psi_4 + a^2 \psi_1 + \rho a \psi_2) d\tau \quad \text{for } d\zeta = (u+a) d\tau . \quad (A-44)$$

APPENDIX B
ZETA CONSTANT REFERENCE PLANE CHARACTERISTIC RELATIONS

I. EQUATIONS OF MOTION

The equations of motion, Eqs. (6) through (9), can be written as

$$\rho_\tau + \bar{v}\rho_\eta + \rho\alpha u_\eta + \rho\beta v_\eta = -u\rho_\zeta - \rho u_\zeta - \epsilon\rho v\beta/\eta, \quad (B-1)$$

$$u_\tau + \bar{v}u_\eta + \alpha p_\eta/\rho = -uu_\zeta - p_\zeta/\rho, \quad (B-2)$$

$$v_\tau + \bar{v}v_\eta + \beta p_\eta/\rho = -uv_\zeta, \quad (B-3)$$

$$p_\tau + \bar{v}p_\eta - a^2(\rho_\tau + \bar{v}\rho_\eta) = -u\rho_\zeta + a^2u\rho_\zeta. \quad (B-4)$$

Letting

$$\psi_1 = -u\rho_\zeta - \rho u_\zeta - \epsilon\rho v\beta/\eta, \quad (B-5)$$

$$\psi_2 = -uu_\zeta - p_\zeta/\rho, \quad (B-6)$$

$$\psi_3 = -uv_\zeta, \quad (B-7)$$

$$\psi_4 = -u\rho_\zeta + a^2u\rho_\zeta, \quad (B-8)$$

Eqs. (B-1) through (B-4) become

$$\rho_\tau + \bar{v}\rho_\eta + \rho\alpha u_\eta + \rho\beta v_\eta = \psi_1, \quad (B-9)$$

$$u_\tau + \bar{v}u_\eta + \alpha p_\eta/\rho = \psi_2, \quad (B-10)$$

$$v_\tau + \bar{v}v_\eta + \beta p_\eta/\rho = \psi_3, \quad (B-11)$$

$$p_\tau + \bar{v}p_\eta - a^2(\rho_\tau + \bar{v}\rho_\eta) = \psi_4. \quad (B-12)$$

II. CHARACTERISTIC CURVES

Following the development of Appendix A, the characteristic curves can be shown to be

$$d\eta/d\tau = \bar{v}, \quad (B-13)$$

$$d\eta/d\tau = \bar{v} \mp \alpha^* a, \quad (B-14)$$

where $\alpha^* = (\alpha^2 + \beta^2)^{1/2}$.

III. COMPATIBILITY EQUATIONS

Again, following the development of Appendix A, the compatibility equations can be shown to be

$$\beta du - \alpha dv = (\beta\psi_2 - \alpha\psi_3)d\tau \quad \left. \begin{array}{l} \text{for } d\eta = \bar{v}d\tau, \\ \text{for } d\eta = (\bar{v} - \alpha^* a)d\tau, \end{array} \right\} \quad (B-15)$$

$$dp - a^2 d\rho = \psi_4 d\tau \quad (B-16)$$

$$dp - \rho\alpha du/\alpha^* - \rho\beta dv/\alpha^* = (\psi_4 + a^2\psi_1 - \rho\alpha\psi_2/\alpha^* - \rho\beta\psi_3/\alpha^*)d\tau \quad \text{for } d\eta = (\bar{v} - \alpha^* a)d\tau \quad (B-17)$$

$$dp + \rho\alpha du/\alpha^* + \rho\beta dv/\alpha^* = (\psi_4 + a^2\psi_1 + \rho\alpha\psi_2/\alpha^* + \rho\beta\psi_3/\alpha^*)d\tau \quad \text{for } d\eta = (\bar{v} + \alpha^* a)d\tau. \quad (B-18)$$

APPENDIX C
FORTRAN IV LISTING OF THE NAP PROGRAM

LASL Identification: LP-0537

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C      PROGRAM MAIN(INPUT,OUTPUT,FILM,PUNCH,TAPE5=INPUT,TAPE6=OUTPUT,    MAI  10
C      1TAPE7=FILM)                                                    MAI  20
C      *****                                                        MAI  30
C      *****                                                        MAI  40
C      MAP, A COMPUTER PROGRAM FOR THE COMPUTATION OF TWO-DIMENSIONAL, MAI  50
C      TIME-DEPENDENT, INVISCID NOZZLE FLOW                            MAI  60
C      MAI  70
C      BY MICHAEL C. CLINE, T=3                                         MAI  80
C      LOS ALAMOS SCIENTIFIC LABORATORY                                MAI  90
C      *****                                                        MAI 100
C      *****                                                        MAI 110
C      *****                                                        MAI 120
C      PROGRAM ABSTRACT                                                MAI 130
C      THE EQUATIONS OF MOTION FOR TWO-DIMENSIONAL, TIME DEPENDENT, MAI 140
C      INVISCID FLOW IN A NOZZLE ARE SOLVED USING THE SECOND-ORDER, MAI 150
C      MACCORMACK, FINITE-DIFFERENCE SCHEME, THE FLUID IS ASSUMED TO BE MAI 160
C      A PERFECT GAS. ALL BOUNDARY CONDITIONS ARE COMPUTED USING A MAI 170
C      SECOND-ORDER, REFERENCE PLANE CHARACTERISTIC SCHEME, THE STEADY MAI 180
C      STATE SOLUTION IS OBTAINED AS THE ASYMPTOTIC SOLUTION FOR LARGE MAI 190
C      TIME, THE NOZZLES MAY BE EITHER CONVERGING, CONVERGING-DIVERGING, MAI 200
C      OR PLUG GEOMETRIES. MAI 210
C      MAI 220
C      DIMENSION TITLE(8), UI(21), VI(21), PI(21), ROI(21)           MAI 230
C      COMMON /AV/ IAV,CAV,NST,8MP,LSS,CTA,XMU,XLA,RKMU,OUT(81,21),QVT(81, MAI 240
C      1,21),OPT(81,21) MAI 250
C      COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4) MAI 260
C      COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RO(81,21,2) MAI 270
C      COMMON /CNTRLC/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAMI,GAMA MAI 280
C      1M2,L1,L2,L3,M1,M2,DX,DY,DT,N,N1,N3,NASM,IVEL,ICAR,NID,LJET,JFLAG, MAI 290
C      2IERR,IUI,IUO,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TC MAI 300
C      3,LC,PLOW,ROLOW MAI 310
C      COMMON /GEMTRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCT,ANGI,ANGE,XW(81), MAI 320
C      1YW(81),XWI(81),YWI(81),NXNY(81),NWPTS,IINT,IDIF,LT,NDIM MAI 330
C      COMMON /GCB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,RECB,RCICB,RCTCB,ANGICB MAI 340
C      1,ANGECB,XCB(81),YCB(81),XCB1(81),YCB1(81),NXNYCB(81),NCBPTS,IINTCB MAI 350
C      2,IDIFCB,LECB MAI 360
C      COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASSI,MASST,THRUST,NMAI 370
C      1STAG MAI 380
C      REAL MN3,NXNY,MASSI,MASST,NXNYCB,MASSE MAI 390
C      NAMELIST /CNTRL/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,TSTOP,GAMMA,RGAS, MAI 400
C      1NASM,NAME,NCONVI,NST,IUI,IUO,8MP,IPUNCH,IAV,CAV,NPLOT,IEX,LSS,CTA, MAI 410
C      2XMU,XLA,RKMU,IUNIT,PLOW,ROLOW MAI 420
C      NAMELIST /IVS/ U,V,P,RO,NID,NSTART,TSTART,RSTAR,RSTARS MAI 430
C      NAMELIST /GEMTRY/ NDIM,XI,RI,RT,XE,RCI,RCT,ANGI,ANGE,NGEOM,XWI,YWI MAI 440
C      1,NWPTS,IINT,IDIF,LJET,JFLAG,NXNY,YW MAI 450
C      NAMELIST /GCB1/ NGCB,RICB,RTCB,RCICB,RCTCB,ANGICB,ANGECB,YCB,NXNYCB MAI 460
C      1B,XCB1,YCB1,NCBPTS,IINTCB,IDIFCB MAI 470
C      NAMELIST /BC/ PT,TT,THETA,PE,NSTAG,ISUPER,UI,VI,PI,ROI MAI 480
C      MAI 490
C      READ IN DATA                                                    MAI 500
C      MAI 510
C      TCONV=0.0 $ FDT=1.0 $ TSTOP=1.0 $ NASM=1 $ NSTAG=0 $ NAME=0 MAI 520
C      IPUNCH=0 $ NGCB=0 $ IINTCB=1 $ IDIFCB=1 $ NSTART=0 $ TSTART=0.0 MAI 530
C      IINT=1 $ IDIF=1 $ NMAX=0 $ NPRINT=0 $ GAMMA=1.4 $ RGAS=53.35 MAI 540
C      NID=1 $ NDIM=1 $ THETA(1)=0.0 $ PE=14.7 $ NST=0 $ N=0 $ IEX=1 MAI 550
C      NCONVI=1 $ IERR=0 $ JFLAG=0 $ IUI=1 $ IUO=1 $ SMP=0.95 $ ISUPER=0 MAI 560
C      IAV=0 $ CAV=0.0 $ NPLOT=-1 $ G=32.174 $ PC=144.0 $ TC=460.0 MAI 570
C      LC=12.0 $ IUNIT=0 $ LSS=2 $ CTA=0.5 $ XMU=0.2 $ XLA=1.0 MAI 580
C      RKMU=0.7 $ PLOW=0.01 $ ROLOW=0.0001 $ RSTAR=0.0 $ RSTARS=0.0 MAI 590
C      READ 650, TITLE MAI 600
C      IF (EOF,5) 20,30 MAI 610
C      STOP MAI 620
C      20 READ (5,CNTRL) MAI 630
C      30 READ (5,IVS) MAI 640
C      READ (5,GEMTRY) MAI 650
C      READ (5,GCB1) MAI 660
C      READ (5,BC) MAI 670
C      IF (NAME,EQ,0) GO TO 40 MAI 680
C      WRITE (6,CNTRL) MAI 690
C      WRITE (6,IVS) MAI 700
C      WRITE (6,GEMTRY) MAI 710
C      WRITE (6,GCB1) MAI 720
C      WRITE (6,BC) MAI 730
C      PRINT INPUT DATA MAI 740
C      MAI 750
C      PRINT 660 MAI 760
C      PRINT 690 MAI 770
C      PRINT 680 MAI 780
C      PRINT 700 MAI 790
C      PRINT 670 MAI 800
C      MAI 810
C      MAI 820
C      MAI 830

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	PRINT 710, TITLE	MAI 840
	PRINT 670	MAI 850
	PRINT 720	MAI 860
	NPRIND=ABS(FLOAT(NPRINT))	MAI 870
	PRINT 730, LMAX, HMAX, NMAX, NPRIND, TCONV, PDT, NSTAG, NASM, IUNIT, IUI, IUHAI	MAI 880
	10, IEX, NCONVI, TSTOP, NID, NPLOT, IPUNCH, ISUPER, IAV, CAV, XMU, XLA, RKMU, CTMAI	MAI 890
	2A, LSS, SMP, NST	MAI 900
	PRINT 670	MAI 910
	IF (IUI, EQ, 1) PRINT 740, GAMMA, RGAS	MAI 920
	IF (IUI, EQ, 2) PRINT 750, GAMMA, RGAS	MAI 930
	PRINT 670	MAI 940
	PRINT 780	MAI 950
	IF (NDIM, EQ, 0) PRINT 790	MAI 960
	IF (NDIM, EQ, 1) PRINT 800	MAI 970
C		MAI 980
C	CALCULATE THE NOZZLE RADIUS AND NORMAL	MAI 990
C		MAI 1000
	PRINT 670	MAI 1010
	CALL GEOM	MAI 1020
	IF (IERR, NE, 0) GO TO 10	MAI 1030
	DY=1.0/FLOAT(HMAX-1)	MAI 1040
	IF (NGCB, NE, 0) GO TO 60	MAI 1050
	RICB=0.0	MAI 1060
	RTCB=0.0	MAI 1070
	DO 50 L=1, LMAX	MAI 1080
	YCB(L)=0.0	MAI 1090
	NXNYCB(L)=0.0	MAI 1100
50	CONTINUE	MAI 1110
	GO TO 90	MAI 1120
60	XICB=XI	MAI 1130
	XECB=XE	MAI 1140
	CALL GEOMCB	MAI 1150
	LT=1 \$ XI=XICB \$ XE=XECB	MAI 1160
	YO=0.0	MAI 1170
	DO 80 L=1, LMAX	MAI 1180
	IF (NDIM, EQ, 0) Y=YW(L)-YCB(L)	MAI 1190
	IF (NDIM, EQ, 1) Y=YW(L)**2-YCB(L)**2	MAI 1200
	IF (Y, GT, 0.0) GO TO 70	MAI 1210
	PRINT 920	MAI 1220
	GO TO 10	MAI 1230
70	IF (Y, LT, YO) LT=L	MAI 1240
	YO=Y	MAI 1250
80	CONTINUE	MAI 1260
90	IF (NSTAG, NE, 0) GO TO 110	MAI 1270
	DO 100 M=2, HMAX	MAI 1280
	PT(M)=PT(1)	MAI 1290
	TT(M)=TT(1)	MAI 1300
	THETA(M)=THETA(1)	MAI 1310
100	CONTINUE	MAI 1320
	PRINT 670	MAI 1330
	IF (IUI, EQ, 1) PRINT 760, PT(1), TT(1), THETA(1), PE	MAI 1340
	IF (IUI, EQ, 2) PRINT 770, PT(1), TT(1), THETA(1), PE	MAI 1350
	GO TO 130	MAI 1360
110	PRINT 660	MAI 1370
	IF (IUI, EQ, 1) PRINT 890, PE	MAI 1380
	IF (IUI, EQ, 2) PRINT 900, PE	MAI 1390
	DO 120 M=1, HMAX	MAI 1400
	PRINT 910, M, PT(M), TT(M), THETA(M)	MAI 1410
120	CONTINUE	MAI 1420
C		MAI 1430
C	CONVERT METRIC UNITS TO ENGLISH UNITS	MAI 1440
C		MAI 1450
130	IF (IUI, EQ, 1) GO TO 100	MAI 1460
	RSTAR=RSTAR/2.54	MAI 1470
	RSTARS=RSTARS/6.4516	MAI 1480
	RGAS=RGAS/5.38032	MAI 1490
	DO 140 M=1, HMAX	MAI 1500
	PT(M)=PT(M)/6.8948	MAI 1510
	TT(M)=(TT(M)+40.0)*9.0/5.0-40.0	MAI 1520
140	CONTINUE	MAI 1530
	PE=PE/6.8948	MAI 1540
	IF (ISUPER, EQ, 0) GO TO 160	MAI 1550
	DO 150 M=1, HMAX	MAI 1560
	UI(M)=UI(M)/0.3048	MAI 1570
	VI(M)=VI(M)/0.3048	MAI 1580
	PI(M)=PI(M)/6.8948	MAI 1590
	ROI(M)=ROI(M)/16.02	MAI 1600
150	CONTINUE	MAI 1610
160	IF (NID, NE, 0) GO TO 100	MAI 1620
	IF (NSTART, NE, 0) GO TO 100	MAI 1630
	DO 170 L=1, LMAX	MAI 1640
	DO 170 M=1, HMAX	MAI 1650
	U(L, M, 1)=U(L, M, 1)/0.3048	MAI 1660

	V(L,M,1)=V(L,M,1)/0.3048	MAI 1670
	P(L,M,1)=P(L,M,1)/6.8948	MAI 1680
	RO(L,M,1)=RO(L,M,1)/16.02	MAI 1690
170	CONTINUE	MAI 1700
C		MAI 1710
C	CONVERT INPUT DATA UNITS TO INTERNAL UNITS	MAI 1720
C		MAI 1730
180	IF (IUNIT,EQ,0) GO TO 190	MAI 1740
	PC=LC=G=1.0	MAI 1750
	TC=0.0	MAI 1760
190	TCONV=TCONV/100.0	MAI 1770
	T=TSTART*LC	MAI 1780
	TSTOP=TSTOP*LC	MAI 1790
	DO 200 L=1,LMAX	MAI 1800
	XHI(L)=0.0	MAI 1810
200	CONTINUE	MAI 1820
	DO 210 M=1,MMAX	MAI 1830
	PT(M)=PT(M)*PC	MAI 1840
	TT(M)=TT(M)+TC	MAI 1850
	THETA(M)=THETA(M)*0.0174533	MAI 1860
210	CONTINUE	MAI 1870
	PE=PE*PC	MAI 1880
	IF (NID,NE,0) GO TO 230	MAI 1890
	DO 220 L=1,LMAX	MAI 1900
	DO 220 M=1,MMAX	MAI 1910
	P(L,M,1)=P(L,M,1)*PC	MAI 1920
	RO(L,M,1)=RO(L,M,1)/G	MAI 1930
220	CONTINUE	MAI 1940
230	GAM1=GAMMA/(GAMMA+1.0)	MAI 1950
	GAM2=(GAMMA+1.0)/2.0	MAI 1960
	IF (ISUPER,EQ,0) GO TO 250	MAI 1970
	DO 240 M=1,MMAX	MAI 1980
	U(1,M,1)=UI(M)	MAI 1990
	V(1,M,1)=VI(M)	MAI 2000
	P(1,M,1)=PI(M)*PC	MAI 2010
	RO(1,M,1)=ROI(M)/G	MAI 2020
	U(1,M,2)=U(1,M,1)	MAI 2030
	V(1,M,2)=V(1,M,1)	MAI 2040
	P(1,M,2)=P(1,M,1)	MAI 2050
	RO(1,M,2)=RO(1,M,1)	MAI 2060
240	CONTINUE	MAI 2070
250	L1=LMAX-1	MAI 2080
	L2=LMAX-2	MAI 2090
	L3=LMAX-3	MAI 2100
	M1=MMAX-1	MAI 2110
	M2=MMAX-2	MAI 2120
	IF (NID,EQ,0) GO TO 260	MAI 2130
C		MAI 2140
C	COMPUTE THE J=D INITIAL=DATA SURFACE	MAI 2150
C		MAI 2160
	CALL ONEDIM	MAI 2170
	IF (IERR,NE,0) GO TO J0	MAI 2180
C		MAI 2190
C	COMPUTE THE INITIAL=DATA SURFACE MASS FLOW AND THRUST	MAI 2200
C		MAI 2210
260	IF (NPRINT,GT,0) GO TO 270	MAI 2220
	NPRINT=NPRINT	MAI 2230
	GO TO 340	MAI 2240
270	CALL MASFLO (0)	MAI 2250
C		MAI 2260
C	CALCULATE AND PRINT THE INITIAL=VALUE SURFACE	MAI 2270
C		MAI 2280
	DO 330 IU=1,2	MAI 2290
	IF (IU,EQ,1.AND,IU,EQ,2) GO TO 330	MAI 2300
	IF (IU,EQ,2.AND,IU,EQ,1) GO TO 330	MAI 2310
	NLINE=0	MAI 2320
	PRINT 660	MAI 2330
	PRINT 810, TSTART,NSTART	MAI 2340
	PRINT 820	MAI 2350
	IF (IU,EQ,1) PRINT 830	MAI 2360
	IF (IU,EQ,2) PRINT 840	MAI 2370
	PRINT 670	MAI 2380
	X=XI+DX	MAI 2390
	DO 300 L=1,LMAX	MAI 2400
	X=X+DX	MAI 2410
	CALL MAP (0,L,1,AL,BE,DE,LD1,AL1,BE1,DE1)	MAI 2420
	DYIO=DY/BE	MAI 2430
	Y=YCB(L)=DYIO	MAI 2440
	DO 300 M=1,MMAX	MAI 2450
	Y=Y+DYIO	MAI 2460
	VELMAG=SQRT(U(L,M,1)**2+V(L,M,1)**2)	MAI 2470
	XMACH=VELMAG/SQRT(GAMMA*P(L,M,1)/RO(L,M,1))	MAI 2480
	PRES=P(L,M,1)/PC	MAI 2490

	RHO=RO(L,M,1)*G	MAI 2500
	TEMP=P(L,M,1)/RHO/RGAS-TC	MAI 2510
	XP=X	MAI 2520
	YP=Y	MAI 2530
	UP=U(L,M,1)	MAI 2540
	VP=V(L,M,1)	MAI 2550
	IF (IU,EQ,1) GO TO 260	MAI 2560
	XP=XP*2.54	MAI 2570
	YP=YP*2.54	MAI 2580
	UP=UP*0.3048	MAI 2590
	VP=VP*0.3048	MAI 2600
	PRES=PRES*6.8948	MAI 2610
	RHO=RHO*16.02	MAI 2620
	VELMAG=VELMAG*0.3048	MAI 2630
	TEMP=(TEMP+40.0)*5.0/9.0+40.0	MAI 2640
280	NLINE=NLINE+1	MAI 2650
	IF (NLINE,LT,55) GO TO 290	MAI 2660
	PRINT 660	MAI 2670
	PRINT 810, TSTART,NSTART	MAI 2680
	PRINT 820	MAI 2690
	IF (IU,EQ,1) PRINT 830	MAI 2700
	IF (IU,EQ,2) PRINT 840	MAI 2710
	PRINT 670	MAI 2720
	NLINE=1	MAI 2730
290	PRINT 850, L,M,XP,YP,UP,VP,PRES,RHO,VELMAG,XMACH,TEMP	MAI 2740
300	CONTINUE	MAI 2750
	IF (JU,EQ,2) GO TO 310	MAI 2760
	PRINT 870, MASSI,THRUST,MASSI,MASSE	MAI 2770
	GO TO 320	MAI 2780
310	MASSI=MASSI*0.4536	MAI 2790
	MASSI=MASSI*0.4536	MAI 2800
	MASSE=MASSE*0.4536	MAI 2810
	THRUST=THRUST*4.4477	MAI 2820
	PRINT 880, MASSI,THRUST,MASSI,MASSE	MAI 2830
320	IF (IU,NE,3) GO TO 340	MAI 2840
330	CONTINUE	MAI 2850
340	IF (NPLOT,LE,0) GO TO 350	MAI 2860
	CALL PLOT (TITLE,TSTART,NSTART)	MAI 2870
	PRINT 1030, NSTART	MAI 2880
350	IF (NMAX,EQ,0) GO TO 10	MAI 2890
C		MAI 2900
C	INITIALIZE THE TIME STEP INTEGRATION LOOP PARAMETERS	MAI 2910
C		MAI 2920
	N1=1 \$ N3=2 \$ DQM=0.0 \$ N3=0 \$ NCONV=0 \$ NC=0 \$ LDUM=1 \$ NPC=0	MAI 2930
	DXR=1.0/DX \$ DYR=1.0/DY \$ DXRS=DXR*DXR \$ DYRS=DYR*DYR	MAI 2940
	LD=0.1 \$ MD=2.1 \$ LMD=LD*MD	MAI 2950
	IF (NASH,NE,0,AND,LT,NE,1) LDUM=LT-1	MAI 2960
	NPD=0	MAI 2970
	IF (JFLAG,EQ,0) GO TO 360	MAI 2980
	UD(1)=U(LJET-1,MMAX,N1)	MAI 2990
	VD(1)=V(LJET-1,MMAX,N1)	MAI 3000
	PD(1)=P(LJET-1,MMAX,N1)	MAI 3010
	ROD(1)=RO(LJET-1,MMAX,N1)	MAI 3020
	UD(2)=UD(1)	MAI 3030
	VD(2)=VD(1)	MAI 3040
	PD(2)=PD(1)	MAI 3050
	ROD(2)=ROD(1)	MAI 3060
C		MAI 3070
C	ENTER THE TIME STEP INTERGRATION LOOP	MAI 3080
C		MAI 3090
360	DO 500 N=1,NMAX	MAI 3100
	NPD=NPD+1	MAI 3110
	IF (NPD,NE,10) GO TO 370	MAI 3120
	NP=N+NSTART	MAI 3130
	PRINT 1040, NP	MAI 3140
	NPD=0	MAI 3150
370	CONTINUE	MAI 3160
	LMD1=LMD*(N1=1)	MAI 3170
	LMD3=LMD*(N3=1)	MAI 3180
C		MAI 3190
C	CALCULATE DELTA T	MAI 3200
C		MAI 3210
	DO 300 L=1,LMAX	MAI 3220
	CALL MAP (0,L,MD,AL,BE,DE,LD1,AL1,BE1,DE1)	MAI 3230
	DXDY=DXRS+BE*BE+DYRS	MAI 3240
	DO 300 M=1,MMAX	MAI 3250
	LMN1=L+LD*(M=1)+LMD1	MAI 3260
	QS=U(LMN1)*U(LMN1)+V(LMN1)*V(LMN1)	MAI 3270
	AS=GAHMA*P(LMN1)/RO(LMN1)	MAI 3280
	UPA=SQRT(QS*DXDY)+SQRT(AS*DXDY)	MAI 3290
	IF (L,EQ,1,AND,M,EQ,1) UPAM=UPA	MAI 3300
	IF (UPA,GT,UPAM) UPAM=UPA	MAI 3310

380	CONTINUE	MAI 3320
	DT=FDT/UPAM	MAI 3330
	T=T+DT	MAI 3340
	IF (T,LE,TSTOP) GO TO 390	MAI 3350
	T=T+DT	MAI 3360
	DT=TSTOP-T	MAI 3370
	T=TSTOP	MAI 3380
C		MAI 3390
C	DETERMINE IF THE EXIT FLOW IS SUBSONIC OR SUPERSONIC	MAI 3400
C		MAI 3410
390	IVEL=0	MAI 3420
	IF (QS,GE,AS) IVEL=1	MAI 3430
C		MAI 3440
C	CALCULATE THE NOZZLE WALL AND INTERIOR MESH POINTS	MAI 3450
C		MAI 3460
	IF (IAV,NE,0) CALL SHOCK (1)	MAI 3470
	ICAR=1	MAI 3480
	IB=1	MAI 3490
	CALL INTER	MAI 3500
	CALL WALL	MAI 3510
	IF (IERR,NE,0) GO TO 10	MAI 3520
	IF (NGCB,EQ,0) GO TO 400	MAI 3530
	IB=2	MAI 3540
	CALL WALL	MAI 3550
	IF (IERR,NE,0) GO TO 10	MAI 3560
400	ICAR=2	MAI 3570
	IB=1	MAI 3580
	CALL INTER	MAI 3590
	CALL WALL	MAI 3600
	IF (IERR,NE,0) GO TO 10	MAI 3610
	IF (NGCB,EQ,0) GO TO 410	MAI 3620
	IB=2	MAI 3630
	CALL WALL	MAI 3640
	IF (IERR,NE,0) GO TO 10	MAI 3650
C		MAI 3660
C	EXTRAPOLATE THE EXIT MESH POINTS FOR SUPERSONIC FLOW	MAI 3670
C		MAI 3680
410	DO 420 M=1,MMAX	MAI 3690
	U(LMAX,M,N3)=U(L1,M,N3)+IEX*(U(L1,M,N3)-U(L2,M,N3))	MAI 3700
	V(LMAX,M,N3)=V(L1,M,N3)+IEX*(V(L1,M,N3)-V(L2,M,N3))	MAI 3710
	P(LMAX,M,N3)=P(L1,M,N3)+IEX*(P(L1,M,N3)-P(L2,M,N3))	MAI 3720
	RO(LMAX,M,N3)=RO(L1,M,N3)+IEX*(RO(L1,M,N3)-RO(L2,M,N3))	MAI 3730
	IF (P(LMAX,M,N3),GT,0,0,AND,RO(LMAX,M,N3),GT,0,0) GO TO 420	MAI 3740
	P(LMAX,M,N3)=P(L1,M,N3)	MAI 3750
	RO(LMAX,M,N3)=RO(L1,M,N3)	MAI 3760
420	CONTINUE	MAI 3770
	V(LMAX,M,N3)=U(LMAX,M,N3)*NXNY(LMAX)	MAI 3780
	V(LMAX,1,N3)=U(LMAX,1,N3)*NXNYCB(LMAX)	MAI 3790
C		MAI 3800
C	CALCULATE THE NOZZLE INLET MESH POINTS	MAI 3810
C		MAI 3820
	IF (ISUPER,EQ,0) CALL INLET	MAI 3830
C		MAI 3840
C	CALCULATE THE NOZZLE EXIT MESH POINTS FOR SUBSONIC FLOW	MAI 3850
C		MAI 3860
	IF (IVEL,EQ,0) CALL EXITT	MAI 3870
	IF (N,LE,NST) CALL SHOCK (2)	MAI 3880
C		MAI 3890
C	DETERMINE THE MAXIMUM (DELTA U)/U	MAI 3900
C		MAI 3910
	IF (TCONV,LE,0,0) GO TO 440	MAI 3920
	DQM=0,0	MAI 3930
	DO 430 L=LDUM,LMAX	MAI 3940
	DO 430 M=1,MMAX	MAI 3950
	IF (U(L,M,N1),EQ,0,0) GO TO 430	MAI 3960
	DQ=ABS((U(L,M,N3)-U(L,M,N1))/U(L,M,N1))	MAI 3970
	IF (DQ,GT,DQM) DQM=DQ	MAI 3980
430	CONTINUE	MAI 3990
440	NC=NC+1	MAI 4000
	NPC=NPC+1	MAI 4010
	IF (DQM,GE,TCONV) GO TO 450	MAI 4020
	NCONV=NCONV+1	MAI 4030
	IF (NCONV,EQ,1) NCHECK=N+1	MAI 4040
	IF (NCONV,GE,NCONVI) NC=NPRINT	MAI 4050
450	IF (N,EQ,NMAX) NC=NPRINT	MAI 4060
	IF (N,GE,NCHECK+NCONVI) NCONV=0	MAI 4070
	IF (T,EQ,TSTOP) NC=NPRINT	MAI 4080
	IF (NC,EQ,NPRINT) GO TO 460	MAI 4090
	IF (NPC,EQ,NPLOT) GO TO 550	MAI 4100
	GO TO 570	MAI 4110
C		MAI 4120
C	COMPUTE THE SOLUTION SURFACE MASS FLOW AND THRUST	MAI 4130
C		MAI 4140

460	ICN=0	MAI 4150
	IF (JFLAG,EQ,0) GO TO 470	MAI 4160
	IF (LT,NE,LJET-1) GO TO 470	MAI 4170
	UDUM=U(LT,MMAX,N3)	MAI 4180
	RODUM=RO(LT,MMAX,N3)	MAI 4190
	U(LT,MMAX,N3)=UD(3)	MAI 4200
	RO(LT,MMAX,N3)=ROD(3)	MAI 4210
	ICN=1	MAI 4220
470	CALL MASFLO (1)	MAI 4230
	IF (ICN,EQ,0) GO TO 480	MAI 4240
	U(LT,MMAX,N3)=UDUM	MAI 4250
	RO(LT,MMAX,N3)=RODUM	MAI 4260
C		MAI 4270
C	CALCULATE AND PRINT THE SOLUTION SURFACE	MAI 4280
C		MAI 4290
480	DO 540 IU=1,2	MAI 4300
	IF (IU,EQ,1,AND,IU,EQ,2) GO TO 540	MAI 4310
	IF (IU,EQ,2,AND,IU,EQ,1) GO TO 540	MAI 4320
	NLINE=0	MAI 4330
	PRINT 660	MAI 4340
	TIME=T/LC	MAI 4350
	DTIME=DT/LC	MAI 4360
	NP=N+NSTART	MAI 4370
	PRINT 860, NP, TIME, DTIME	MAI 4380
	PRINT 820	MAI 4390
	IF (IU,EQ,1) PRINT 830	MAI 4400
	IF (IU,EQ,2) PRINT 840	MAI 4410
	PRINT 670	MAI 4420
	X=XI+DX	MAI 4430
	DO 510 L=1,LMAX	MAI 4440
	X=X+DX	MAI 4450
	CALL MAP (0,L,1,AL,BE,DE,LD1,AL1,BE1,DE1)	MAI 4460
	DYIO=DY/BE	MAI 4470
	Y=YCB(L)+DYIO	MAI 4480
	DO 510 M=1,MMAX	MAI 4490
	Y=Y+DYIO	MAI 4500
	VELMAG=SQRT(U(L,M,N3)**2+V(L,M,N3)**2)	MAI 4510
	XMACH=VELMAG/SQRT(GAMMA*P(L,M,N3)/RO(L,M,N3))	MAI 4520
	PRES=P(L,M,N3)/PC	MAI 4530
	RHO=RO(L,M,N3)*G	MAI 4540
	TEMP=P(L,M,N3)/RHO/RGAS=TC	MAI 4550
	XP=X	MAI 4560
	YP=Y	MAI 4570
	UP=U(L,M,N3)	MAI 4580
	VP=V(L,M,N3)	MAI 4590
	IF (IU,EQ,1) GO TO 490	MAI 4600
	XP=XP*2.54	MAI 4610
	YP=YP*2.54	MAI 4620
	UP=UP*0.3048	MAI 4630
	VP=VP*0.3048	MAI 4640
	PRES=PRES*6.8948	MAI 4650
	RHO=RHO*16.02	MAI 4660
	VELMAG=VELMAG*0.3048	MAI 4670
	TEMP=(TEMP+40.0)*5.0/9.0-40.0	MAI 4680
490	NLINE=NLINE+1	MAI 4690
	IF (NLINE,LT,55) GO TO 500	MAI 4700
	PRINT 660	MAI 4710
	PRINT 860, NP, TIME, DTIME	MAI 4720
	PRINT 820	MAI 4730
	IF (IU,EQ,1) PRINT 830	MAI 4740
	IF (IU,EQ,2) PRINT 840	MAI 4750
	PRINT 670	MAI 4760
	NLINE=1	MAI 4770
500	PRINT 850, L, M, XP, YP, UP, VP, PRES, RHO, VELMAG, XMACH, TEMP	MAI 4780
510	CONTINUE	MAI 4790
	IF (IU,EQ,2) GO TO 520	MAI 4800
	PRINT 870, MASSI, THRUST, MASSI, MASSE	MAI 4810
	GO TO 530	MAI 4820
520	MASSI=MASSI*0.4536	MAI 4830
	MASSE=MASSI*0.4536	MAI 4840
	MASSE=MASSE*0.4536	MAI 4850
	THRUST=THRUST*4.4477	MAI 4860
	PRINT 880, MASSI, THRUST, MASSI, MASSE	MAI 4870
530	IF (IU,NE,3) GO TO 550	MAI 4880
540	CONTINUE	MAI 4890
550	IF (NPLOT,LT,0) GO TO 560	MAI 4900
	TIME=T/LC & NP=N+NSTART	MAI 4910
	CALL PLOT (TITLE, TIME, NP)	MAI 4920
	PRINT 1030, NP	MAI 4930
C		MAI 4940
C	CHECK FOR CONVERGENCE OF THE STEADY STATE SOLUTION	MAI 4950
C		MAI 4960

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560 IF (DQM,LT,ICONV) GO TO 590
    IF (T,EQ,TSTOP) GO TO 590
    IF (N,EQ,NMAX) GO TO 590
    IF (NC,EQ,NPRINT) NC=0
    IF (NPC,EQ,NPLOT) NPC=0
570 CONTINUE
    NNN=N1
    N1=N3
    N3=NNN
580 CONTINUE
C
C PUNCH A SIVS NAMELIST FOR RESTART
C
590 IF (NPLOT,GE,0) CALL ADV (10)
    IF (IPUNCH,EQ,0) GO TO 10
    DO 600 L=1,LMAX
    DO 600 M=1,MMAX
    P(L,M,N3)=P(L,M,N3)/PC
    RO(L,M,N3)=RO(L,M,N3)*G
600 CONTINUE
    PUNCH 930, NP,TIME
    DO 610 M=1,MMAX
    PUNCH 940, M
    PUNCH 950, (U(L,M,N3),L=1,LMAX)
610 CONTINUE
    DO 620 M=1,MMAX
    PUNCH 960, M
    PUNCH 950, (V(L,M,N3),L=1,LMAX)
620 CONTINUE
    DO 630 M=1,MMAX
    PUNCH 970, M
    PUNCH 980, (P(L,M,N3),L=1,LMAX)
630 CONTINUE
    DO 640 M=1,MMAX
    PUNCH 990, M
    PUNCH 1000, (RO(L,M,N3),L=1,LMAX)
640 CONTINUE
    PUNCH 1010
    NCARDS=(LMAX/7+2)*MMAX*4+2
    PRINT 1020, NCARDS
    GO TO 10
C
C
C FORMAT STATEMENTS
C
650 FORMAT (A10)
660 FORMAT (1H1)
670 FORMAT (1H )
680 FORMAT (1H0)
690 FORMAT (1H0,15X,100HNAME, A COMPUTER PROGRAM FOR THE COMPUTATION OF
1 TWO-DIMENSIONAL, TIME-DEPENDENT, INVISCID NOZZLE FLOW,/,/37X,59H8MAI 5450
2Y MICHAEL C. CLINE, 1-3 - LOS ALAMOS SCIENTIFIC LABORATORY) MAI 5470
700 FORMAT (1H0,10X,18HPROGRAM ABSTRACT =,/,/26X,86HTHE EQUATIONS OF MM
10TION FOR TWO-DIMENSIONAL, TIME DEPENDENT, INVISCID FLOW IN A NOZZMAI 5490
2LE,/,/21X,93HARE SOLVED USING THE SECOND-ORDER, MACCORMACK, FINITE=MAI 5500
3DIFFERENCE SCHEME. THE FLUID IS ASSUMED,/,/21X,95HTO BE A PERFECT GMAI 5510
4AS, ALL BOUNDARY CONDITIONS ARE COMPUTED USING A SECOND-ORDER, REFMAI 5520
SERENCE PLANE,/,/21X,91HCHARACTERISTIC SCHEME, THE STEADY STATE SOLUMAI 5530
6TION IS OBTAINED AS THE ASYMPTOTIC SOLUTION FOR,/,/21X,91HLARGE TIMMAI 5540
7E, THE NOZZLES MAY BE EITHER CONVERGING, CONVERGING-DIVERGING, OR MAI 5550
8PLUG GEOMETRIES,.) MAI 5560
710 FORMAT (1H0,10X,11HJOB TITLE =,/,/21X,A10) MAI 5570
720 FORMAT (1H0,10X,20HCONTROL PARAMETERS =) MAI 5580
730 FORMAT (1H0,20X,5HLMAX=,I2,2X,5HMMAX=,I2,3X,5HNM=,I4,2X,7HNPRINTMAI 5590
1=,I4,2X,6HTCONV=,F6,3,3X,4HFDI=,F4,2,2X,6HNSIAG=,I1,5X,5HNSMAI 5600
24X,6HIUNIT=,I1,/,/21X,4HIUI=,I1,4X,4HIUD=,I1,5X,4HIEX=,I1,6X,7HNCONMAI 5610
3VI=,I2,4X,6HTSTOP=,F7,5,2X,4HNIID=,I2,4X,6HNPLOT=,I4,2X,7HIPUNCH=,IMAI 5620
41,2X,7HISUPER=,I1,/,/21X,4HIAV=,I1,4X,4HCAY=,F4,1,2X,4HXMU=,F4,2,3XMAI 5630
5,4HXL=,F4,2,5X,5HMKMU=,F5,2,5X,4HCTA=,F4,2,2X,4HLS=,I2,6X,4H8MP=MAI 5640
6,F4,2,2X,4HNSI=,I4) MAI 5650
740 FORMAT (1H0,10X,13HFLUID MODEL =,/,/21X,36HTHE RATIO OF SPECIFIC MM
1EATS, GAMMA =,F6,4,26H AND THE GAS CONSTANT, R =,F9,4,15H (FT-LBF/MAI 5660
2LBM-R)) MAI 5680
750 FORMAT (1H0,10X,13HFLUID MODEL =,/,/21X,36HTHE RATIO OF SPECIFIC MM
1EATS, GAMMA =,F6,4,26H AND THE GAS CONSTANT, R =,F9,4,9H (J/KG-K))MAI 5690
760 FORMAT (1H0,10X,21HBOUNDARY CONDITIONS =,/,/21X,3HPT=,F9,4,7H (PSI)MAI 5710
1A),5X,3HTI=,F9,4,4H (F),5X,6HTHETA=,F9,4,6H (DEG),5X,3HPE=,F9,4,7HMAI 5720
2 (PSIA)) MAI 5730
770 FORMAT (1H0,10X,21HBOUNDARY CONDITIONS =,/,/21X,3HPT=,F9,4,6H (KPA)MAI 5740
1),5X,3HTI=,F9,4,4H (C),5X,6HTHETA=,F9,4,6H (DEG),5X,3HPE=,F9,4,6H MAI 5750
2(KPA)) MAI 5760
780 FORMAT (1H0,10X,15HFLOW GEOMETRY =) MAI 5770
790 FORMAT (1H0,20X,47HTWO-DIMENSIONAL, PLANAR FLOW HAS BEEN SPECIFIEDMAI 5780
1) MAI 5790

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800  FORMAT (1H0,20X,36MAXISYMMETRIC FLOW HAS BEEN SPECIFIED)      MAI 5800
810  FORMAT (1H ,30HINITIAL-DATA SURFACE = TIME = ,F10,8,8H SECONDS,4H MAI 5810
      1(N=,I4,1H))                                                  MAI 5820
820  FORMAT (1H0,11X,1HL,4X,1HM,9X,1HX,10X,1HY,10X,1HU,11X,1HV,12X,1HP,MAI 5830
      111X,3HRHO,9X,1HQ,11X,4HMMACH,8X,1HT)                        MAI 5840
830  FORMAT (1H ,25X,4H(IN),7X,4H(IN),6X,5H(FPS),7X,5H(FPS),7X,6H(P8IA)MAI 5850
      1,6X,9H(LBM/FT3),4X,5H(FPS),10X,2HNO,8X,3H(F))              MAI 5860
840  FORMAT (1H ,25X,4H(CM),7X,4H(CM),6X,5H(MPS),7X,5H(MPS),7X,6H (KPA)MAI 5870
      1,7X,7H(KG/M3),5X,5H(MPS),10X,2HNO,8X,3H(C))               MAI 5880
850  FORMAT (1H ,7X,2IS,4F12,4,F13,4,F12,6,3F12,4)                MAI 5890
860  FORMAT (1H ,20HSOLUTION SURFACE NO.,IS,3H = ,7HTIME = ,F10,8,20H 3MAI 5900
      1ECONDS (DELTA T = ,F10,8,1H))                              MAI 5910
870  FORMAT (1H0,10X,5HMASS=F9,4,10H (LBM/SEC),5X,7HTHRUST=F11,4,6H (MAI 5920
      1LBF),5X,6HMASSI=F9,4,5X,6HMASS=F9,4)                      MAI 5930
880  FORMAT (1H0,10X,5HMASS=F9,4,9H (KG/SEC),5X,7HTHRUST=F11,4,10H (NMAI 5940
      1EWTONS),5X,6HMASSI=F9,4,5X,6HMASS=F9,4)                  MAI 5950
890  FORMAT (1H0,10X,21HBOUNDARY CONDITIONS =,/,22X,1HM,11X,8HPT(P8IA)MAI 5960
      1,10X,5HTT(F),10X,10HTHETA(DEG),10X,3HPE=F7,3,7H (P8IA),/) MAI 5970
900  FORMAT (1H0,10X,21HBOUNDARY CONDITIONS =,/,22X,1HM,11X,7HPT(KPA),MAI 5980
      112X,5HTT(C),10X,10HTHETA(DEG),10X,3HPE=F7,3,6H (KPA),/)  MAI 5990
910  FORMAT (1H ,20X,I2,10X,F7,2,10X,F7,2,10X,F7,2)              MAI 6000
920  FORMAT (1H0,78H***** THE RADIUS OF THE CENTERBODY IS LARGER THAN TMAI 6010
      1HE NOZZLE WALL RADIUS *****)                            MAI 6020
930  FORMAT (1X,18HSIVS NID=0,NSTART=,I4,8H,TSTART=F14,10,1H,)    MAI 6030
940  FORMAT (1X,4HU(1,,I2,5H,1) =)                                MAI 6040
950  FORMAT (1X,7(F10,3,1H,))                                     MAI 6050
960  FORMAT (1X,4HV(1,,I2,5H,1) =)                                MAI 6060
970  FORMAT (1X,4HP(1,,I2,5H,1) =)                                MAI 6070
980  FORMAT (1X,7(F10,4,1H,))                                     MAI 6080
990  FORMAT (1X,5HRO(1,,I2,5H,1) =)                               MAI 6090
1000  FORMAT (1X,7(F10,6,1H,))                                     MAI 6100
1010  FORMAT (1X,1HS)                                              MAI 6110
1020  FORMAT (1H0,27H***** EXPECT APPROXIMATELY ,I4,20H PUNCHED CARDS **MAI 6120
      1***)                                                        MAI 6130
1030  FORMAT (1H0,31H***** EXPECT FILM OUTPUT FOR N=,I4,6H ***** MAI 6140
1040  FORMAT (1H ,2HN=,I4)                                         MAI 6150
      END                                                         MAI 6160

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C      SUBROUTINE GEOM                                GEO 10
C      *****                                GEO 20
C      THIS SUBROUTINE CALCULATES THE NOZZLE RADIUS AND OUTER NORMAL    GEO 30
C      *****                                GEO 40
C      *****                                GEO 50
C      *****                                GEO 60
C      *****                                GEO 70
C      *****                                GEO 80
C      COMMON /AV/ IAV,CAV,NST,8MP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81,21),OPT(81,21) GEO 90
C      1,21),OPT(81,21)                                GEO 100
C      COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)          GEO 110
C      COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RO(81,21,2)    GEO 120
C      COMMON /CNTRLC/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAM1,GAGEO 130
C      1M2,L1,L2,L3,M1,M2,DX,DY,DT,N,N1,N3,NASH,IYEL,ICHAR,NID,LJET,JFLAG,GEO 140
C      2IERR,IUI,IUO,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TCGEO 150
C      3,LC,PLOW,ROLOW                                GEO 160
C      COMMON /GEMTRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCT,ANGI,ANGE,XW(81),GEO 170
C      1YW(81),XWI(81),YWI(81),NXNY(81),NHPTS,IINT,IDIF,LT,NOIM          GEO 180
C      COMMON /GCB/ NGCB,XICB,RCIB,XTCB,RTCB,XECB,RECB,RCICB,RCTCB,ANGICBGEO 190
C      1,ANGECB,XCB(81),YCB(81),XCB1(81),YCB1(81),NXNYCB(81),NCBPTS,IINTCBGEO 200
C      2,IDIFCB,LECB                                GEO 210
C      COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASSI,MASST,THRUST,NGEO 220
C      1STAG                                GEO 230
C      REAL MN3,NXNY,MASSI,MASST,NXNYCB,MASSE          GEO 240
C      GO TO (10,30,120,170), NGEOM                    GEO 250
C      CONSTANT AREA DUCT CASE                          GEO 260
C      PRINT 230                                         GEO 270
C      IF (IUI,EQ,1) PRINT 250, XI,RI,XE                GEO 280
C      IF (IUI,EQ,2) PRINT 260, XI,RI,XE                GEO 290
C      LT=LMAX                                           GEO 300
C      DX=(XE-XI)/(LMAX-1)                               GEO 310
C      XT=XE                                              GEO 320
C      RT=RI                                              GEO 330
C      RE=RI                                              GEO 340
C      DO 20 L=1,LMAX                                    GEO 350
C      YW(L)=RI                                           GEO 360
C      NXNY(L)=0.0                                         GEO 370
C      CONTINUE                                           GEO 380
C      IF (JFLAG,EQ,0) GO TO 210                          GEO 390
C      XWL=XI+(LJET-2)*DX                                GEO 400
C      IF (IUI,EQ,1) PRINT 370, XWL,LJET,LMAX            GEO 410
C      IF (IUI,EQ,2) PRINT 380, XWL,LJET,LMAX            GEO 420
C      GO TO 210                                         GEO 430
C      CIRCULAR-ARC, CONICAL NOZZLE CASE                 GEO 440
C      PRINT 230                                         GEO 450
C      IF (RCI,EQ,0.0,OR,RCT,EQ,0.0) GO TO 200          GEO 460
C      ANI=ANGI*3.141593/180.0                          GEO 470
C      ANE=ANGE*3.141593/180.0                          GEO 480
C      XTAN=XI+RCI*SIN(ANI)                             GEO 490
C      RTAN=RI+RCI*(COS(ANI)-1.0)                       GEO 500
C      RT1=RT-RCT*(COS(ANI)-1.0)                       GEO 510
C      XT1=XTAN+(RTAN-RT1)/TAN(ANI)                     GEO 520
C      IF (XT1,GE,XTAN) GO TO 40                        GEO 530
C      XT1=XTAN                                           GEO 540
C      RT1=RTAN                                           GEO 550
C      XT=XT1+RCT*SIN(ANI)                               GEO 560
C      XT2=XT+RCT*SIN(ANE)                               GEO 570
C      RT2=RT+RCT*(1.0-COS(ANE))                       GEO 580
C      RE=RT2+(XE-XT2)*TAN(ANE)                         GEO 590
C      LT=1                                               GEO 600
C      DX=(XE-XI)/(LMAX-1)                               GEO 610
C      IF (IUI,EQ,1) PRINT 270, XI,RI,RT,XE,RCI,RCT,ANGI,ANGE,XT,RE    GEO 620
C      IF (IUI,EQ,2) PRINT 280, XI,RI,RT,XE,RCI,RCT,ANGI,ANGE,XT,RE    GEO 630
C      DO 10 L=1,LMAX                                    GEO 640
C      X=XI+(L-1)*DX                                      GEO 650
C      IF (X,GE,XI,AND,X,LE,XTAN) GO TO 50              GEO 660
C      IF (X,GT,XTAN,AND,X,LE,XT1) GO TO 60             GEO 670
C      IF (X,GT,XT1,AND,X,LE,XT) GO TO 70               GEO 680
C      IF (X,GT,XT,AND,X,LE,XT2) GO TO 80               GEO 690
C      IF (X,GT,XT2,AND,X,LE,XE) GO TO 90               GEO 700
C      YW(L)=RI+RCI*(COS(ASIN((X-XI)/RCI))-1.0)         GEO 710
C      NXNY(L)=(X-XI)/(YW(L)-RI+RCI)                   GEO 720
C      GO TO 100                                         GEO 730
C      YW(L)=RT1+(XT1-X)*TAN(ANI)                       GEO 740
C      NXNY(L)=TAN(ANI)                                 GEO 750
C      GO TO 100                                         GEO 760
C      YW(L)=RT1+(XT1-X)*TAN(ANI)                       GEO 770
C      NXNY(L)=TAN(ANI)                                 GEO 780
C      GO TO 100                                         GEO 790
C      YW(L)=RT1+(XT1-X)*TAN(ANI)                       GEO 800
C      NXNY(L)=TAN(ANI)                                 GEO 810
C      GO TO 100                                         GEO 820
C      YW(L)=RT1+(XT1-X)*TAN(ANI)                       GEO 830
C      NXNY(L)=TAN(ANI)                                 GEO 840
C      GO TO 100                                         GEO 850

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C		GEO	850
70	YH(L)=RT+RCT*(1,0=COS(ASIN((XT-X)/RCT)))	GEO	860
	NXNY(L)=(XT-X)/(RCT+RT-YH(L))	GEO	870
	GO TO 100	GEO	880
C		GEO	890
80	YH(L)=RT+RCT*(1,0=COS(ASIN((X-XT)/RCT)))	GEO	900
	NXNY(L)=(XT-X)/(RCT+RT-YH(L))	GEO	910
	GO TO 100	GEO	920
C		GEO	930
90	YH(L)=RT2+(X-XT2)*TAN(ANE)	GEO	940
	NXNY(L)=-TAN(ANE)	GEO	950
C		GEO	960
100	IF (L,EQ,1) GO TO 110	GEO	970
	IF (YH(L),LT,YH(LT)) LT=L	GEO	980
110	CONTINUE	GEO	990
	IF (JFLAG,EQ,0) GO TO 210	GEO	1000
C		GEO	1010
	XNL=XI+(LJET-2)*DX	GEO	1020
	IF (IUI,EQ,1) PRINT 370, XNL,LJET,LMAX	GEO	1030
	IF (IUI,EQ,2) PRINT 380, XNL,LJET,LMAX	GEO	1040
	GO TO 210	GEO	1050
C		GEO	1060
C	GENERAL NOZZLE CASE - INPUT WALL COORDINATES ONLY	GEO	1070
C		GEO	1080
120	PRINT 240	GEO	1090
	PRINT 230	GEO	1100
	XI=XWI(1)	GEO	1110
	XE=XWI(NWPTS)	GEO	1120
	DX=(XE-XI)/(LMAX-1)	GEO	1130
	XW(1)=XI	GEO	1140
	XW(LMAX)=XE	GEO	1150
	YH(1)=YWI(1)	GEO	1160
	YH(LMAX)=YWI(NWPTS)	GEO	1170
	RI=YW(1)	GEO	1180
	RE=YW(LMAX)	GEO	1190
	LT=1	GEO	1200
	DO 130 L=2,NWPTS	GEO	1210
	IF (YWI(L),LE,YWI(LT)) LT=L	GEO	1220
130	CONTINUE	GEO	1230
	XT=XWI(LT)	GEO	1240
	RT=YWI(LT)	GEO	1250
	IF (IUI,EQ,1) PRINT 290, XT,RT,IINT,IDIF	GEO	1260
	IF (IUI,EQ,2) PRINT 300, XT,RT,IINT,IDIF	GEO	1270
	LT=1	GEO	1280
	L1=LMAX-1	GEO	1290
	IP=1	GEO	1300
	DO 140 L=2,L1	GEO	1310
	XW(L)=XI+DX*(L-1)	GEO	1320
	CALL MTLUP (XW(L),YH(L),IINT,NWPTS,NWPTS,1,IP,XWI,YWI)	GEO	1330
	IF (L,EQ,1) GO TO 140	GEO	1340
	IF (YH(L),LE,YH(LT)) LT=L	GEO	1350
140	CONTINUE	GEO	1360
	LDUM=NWPTS	GEO	1370
	IF (LMAX,GT,NWPTS) LDUM=LMAX	GEO	1380
	DO 160 L=1,LDUM	GEO	1390
	IF (L,GT,LMAX) GO TO 150	GEO	1400
	SLOPE=DIF(L,IDIF,LMAX,XW,YH)	GEO	1410
	NXNY(L)=-SLOPE	GEO	1420
150	IF (L,LE,NWPTS,AND,L,LE,LMAX) PRINT 330, L,XWI(L),YWI(L),XW(L),YH(L),SLOPE	GEO	1430
	IF (L,GT,NWPTS,AND,L,LE,LMAX) PRINT 340, L,XW(L),YH(L),SLOPE	GEO	1440
	IF (L,LE,NWPTS,AND,L,GT,LMAX) PRINT 350, L,XWI(L),YWI(L)	GEO	1450
160	CONTINUE	GEO	1460
	IF (JFLAG,EQ,0) GO TO 210	GEO	1470
C		GEO	1480
	IF (IUI,EQ,1) PRINT 370, XW(LJET-1),LJET,LMAX	GEO	1490
	IF (IUI,EQ,2) PRINT 380, XW(LJET-1),LJET,LMAX	GEO	1500
	GO TO 210	GEO	1510
C		GEO	1520
C	GENERAL NOZZLE CASE - INPUT WALL COORDINATES AND SLOPES	GEO	1530
C		GEO	1540
170	PRINT 240	GEO	1550
	PRINT 230	GEO	1560
	DX=(XE-XI)/(LMAX-1)	GEO	1570
	RI=YW(1)	GEO	1580
	RE=YW(LMAX)	GEO	1590
	LT=1	GEO	1600
	DO 180 L=2,LMAX	GEO	1610
	IF (YH(L),LE,YH(LT)) LT=L	GEO	1620
180	CONTINUE	GEO	1630
	XT=XI+(LT-1)*DX	GEO	1640
	RT=YW(LT)	GEO	1650
	IF (IUI,EQ,1) PRINT 310, XT,RT	GEO	1660
		GEO	1670

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      IF (IUI,EQ,2) PRINT 320, XT,RT
      DO 190 L=1,LMAX
      XW(L)=XI+DX*(L-1)
      SLOPE=NXNY(L)
      PRINT 360, L,XW(L),YW(L),SLOPE
190  CONTINUE
      IF (JFLAG,EQ,0) GO TO 210

C
      IF (IUI,EQ,1) PRINT 370, XW(LJET-1),LJET,LMAX
      IF (IUI,EQ,2) PRINT 380, XW(LJET-1),LJET,LMAX
      GO TO 210

C
200  PRINT 390
      IERR=1
      RETURN

C
210  IF (IUI,EQ,1) RETURN
      DO 220 L=1,LMAX
      YW(L)=YW(L)/2.54
220  CONTINUE
      XT=XT/2.54
      RT=RT/2.54
      IF (NGCB,NE,0) RETURN
      XI=XI/2.54 & XE=XE/2.54
      DX=DX/2.54
      RETURN

C
C  FORMAT STATEMENTS
C
230  FORMAT (1H0,10X,17HNOZZLE GEOMETRY =)
240  FORMAT (1H1)
250  FORMAT (1H0,20X,46HA CONSTANT AREA DUCT HAS BEEN SPECIFIED BY XI=,
1F8.4,10H (IN), RI=F8.4,14H (IN), AND XE=F8.4,5H (IN))
260  FORMAT (1H0,20X,46HA CONSTANT AREA DUCT HAS BEEN SPECIFIED BY XI=,
1F8.4,10H (CM), RI=F8.4,14H (CM), AND XE=F8.4,5H (CM))
270  FORMAT (1H0,20X,56HA CIRCULAR=ARC, CONICAL NOZZLE HAS BEEN SPECIFIED
1ED BY XI=F8.4,10H (IN), RI=F8.4,6H (IN),,,21X,3HRT=F8.4,10H (IGEO
2N), XE=F8.4,11H (IN), RCI=F8.4,11H (IN), RCT=F8.4,12H (IN), ANGGE0
3I=F8.4,2,7H (DEG),,,21X,9HAND ANGE=F8.4,2,35H (DEG), THE COMPUTED VGE0
4ALUES ARE XT=F8.4,13H (IN) AND RE=F8.4,6H (IN),)
280  FORMAT (1H0,20X,56HA CIRCULAR=ARC, CONICAL NOZZLE HAS BEEN SPECIFIED
1ED BY XI=F8.4,10H (CM), RI=F8.4,6H (CM),,,21X,3HRT=F8.4,10H (CGEO
2H), XE=F8.4,11H (CM), RCI=F8.4,11H (CM), RCT=F8.4,12H (CM), ANGGE0
3I=F8.4,2,7H (DEG),,,21X,9HAND ANGE=F8.4,2,35H (DEG), THE COMPUTED VGE0
4ALUES ARE XT=F8.4,13H (CM) AND RE=F8.4,6H (CM),)
290  FORMAT (1H0,20X,60HA GENERAL NOZZLE HAS BEEN SPECIFIED BY THE FOLLGEO
10WING PARAMETERS, XT=F8.4,10H (IN), RT=F8.4,6H (IN),,,21X,5HIINGEO
2T=F8.4,1,7H, IDIF=F8.4,1,1H,/,22X,1HL,10X,7HXXI(IN),10X,7HYMI(IN),11X,
36HXX(IN),11X,6HYW(IN),12X,5HSLOPE,/)
300  FORMAT (1H0,20X,60HA GENERAL NOZZLE HAS BEEN SPECIFIED BY THE FOLLGEO
10WING PARAMETERS, XT=F8.4,10H (CM), RT=F8.4,6H (CM),,,21X,5HIINGEO
2T=F8.4,1,7H, IDIF=F8.4,1,1H,/,22X,1HL,10X,7HXXI(CM),10X,7HYMI(CM),11X,
36HXX(CM),11X,6HYW(CM),12X,5HSLOPE,/)
310  FORMAT (1H0,20X,60HA GENERAL NOZZLE HAS BEEN SPECIFIED BY THE FOLLGEO
10WING PARAMETERS, XT=F8.4,10H (IN), RT=F8.4,6H (IN),,,22X,1HL,
211X,6HXX(IN),11X,6HYW(IN),12X,5HSLOPE,/)
320  FORMAT (1H0,20X,60HA GENERAL NOZZLE HAS BEEN SPECIFIED BY THE FOLLGEO
10WING PARAMETERS, XT=F8.4,10H (CM), RT=F8.4,6H (CM),,,22X,1HL,
211X,6HXX(CM),11X,6HYW(CM),12X,5HSLOPE,/)
330  FORMAT (1H ,20X,12,7X,F10.4,7X,F10.4,7X,F10.4,7X,F10.4,7X,F10.4)
340  FORMAT (1H ,20X,12,41X,F10.4,7X,F10.4,7X,F10.4)
350  FORMAT (1H ,20X,12,7X,F10.4,7X,F10.4)
360  FORMAT (1H ,20X,12,7X,F10.4,7X,F10.4,7X,F10.4)
370  FORMAT (1H0,20X,69HAN EXHAUST JET CALCULATION HAS BEEN REQUESTED,
1 THE NOZZLE ENDS AT X=F8.4,11H (IN), THE,,21X,14HMESH POINTS L=
2,13,6H TO L=13,50H ARE AN INITIAL APPROXIMATION TO THE EXHAUST JEGEO
3T BOUNDARY,)
380  FORMAT (1H0,20X,69HAN EXHAUST JET CALCULATION HAS BEEN REQUESTED,
1 THE NOZZLE ENDS AT X=F8.4,11H (CM), THE,,21X,14HMESH POINTS L=
2,13,6H TO L=13,50H ARE AN INITIAL APPROXIMATION TO THE EXHAUST JEGEO
3T BOUNDARY,)
390  FORMAT (1H0,44H***** RCI OR RCT WAS SPECIFIED AS ZERO *****
END

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GEO 1680
GEO 1690
GEO 1700
GEO 1710
GEO 1720
GEO 1730
GEO 1740
GEO 1750
GEO 1760
GEO 1770
GEO 1780
GEO 1790
GEO 1800
GEO 1810
GEO 1820
GEO 1830
GEO 1840
GEO 1850
GEO 1860
GEO 1870
GEO 1880
GEO 1890
GEO 1900
GEO 1910
GEO 1920
GEO 1930
GEO 1940
GEO 1950
GEO 1960
GEO 1970
GEO 1980
GEO 1990
GEO 2000
GEO 2010
GEO 2020
GEO 2030
GEO 2040
GEO 2050
GEO 2060
GEO 2070
GEO 2080
GEO 2090
GEO 2100
GEO 2110
GEO 2120
GEO 2130
GEO 2140
GEO 2150
GEO 2160
GEO 2170
GEO 2180
GEO 2190
GEO 2200
GEO 2210
GEO 2220
GEO 2230
GEO 2240
GEO 2250
GEO 2260
GEO 2270
GEO 2280
GEO 2290
GEO 2300
GEO 2310
GEO 2320
GEO 2330
GEO 2340
GEO 2350
GEO 2360
GEO 2370
GEO 2380
GEO 2390
GEO 2400

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60	YH(L)=RT1+(XT1-X)*TAN(ANI)	GCB 840
	NXNY(L)=TAN(ANI)	GCB 850
	GO TO 100	GCB 860
C		GCB 870
70	YH(L)=RT+RCT*(1,0-COS(ASIN((XT-X)/RCT)))	GCB 880
	NXNY(L)=(XT-X)/(RCT+RT-YH(L))	GCB 890
	GO TO 100	GCB 900
C		GCB 910
80	YH(L)=RT+RCT*(1,0-COS(ASIN((X-XT)/RCT)))	GCB 920
	NXNY(L)=(XT-X)/(RCT+RT-YH(L))	GCB 930
	GO TO 100	GCB 940
C		GCB 950
90	YH(L)=RT2+(X-XT2)*TAN(ANE)	GCB 960
	NXNY(L)=-TAN(ANE)	GCB 970
C		GCB 980
100	YCB(L)=2,0*RTCB-YH(L)	GCB 990
	NXNYCB(L)=-NXNY(L)	GCB 1000
	IF (YCB(L),GE,0,0) GO TO 110	GCB 1010
	YCB(L)=0,0	GCB 1020
	NXNYCB(L)=0,0	GCB 1030
110	CONTINUE	GCB 1040
	GO TO 200	GCB 1050
C		GCB 1060
C	GENERAL CENTERBODY CASE = INPUT CENTERBODY COORDINATES ONLY	GCB 1070
C		GCB 1080
120	PRINT 220	GCB 1090
	IF (IUI,EQ,1) PRINT 270, IINTCB,IDIFCB	GCB 1100
	IF (IUI,EQ,2) PRINT 280, IINTCB,IDIFCB	GCB 1110
	L1=LMAX+1	GCB 1120
	IP=1	GCB 1130
	DO 130 L=1,LMAX	GCB 1140
	XCB(L)=XICB+DX*(L-1)	GCB 1150
	CALL MTLUP (XCB(L),YCB(L),IINTCB,NCBPTS,NCBPTS,1,IP,XCBI,YCBI)	GCB 1160
130	CONTINUE	GCB 1170
	LDUM=NCBPTS	GCB 1180
	IF (LMAX,GT,NCBPTS) LDUM=LMAX	GCB 1190
	DO 150 L=1,LDUM	GCB 1200
	IF (L,GT,LMAX) GO TO 140	GCB 1210
	SLOPE=DIF(L,IDIFCB,LMAX,XCB,YCB)	GCB 1220
	NXNYCB(L)=-SLOPE	GCB 1230
	IF (YCB(L),GE,0,0) GO TO 140	GCB 1240
	YCB(L)=0,0	GCB 1250
	NXNYCB(L)=0,0	GCB 1260
	SLOPE=-NXNYCB(L)	GCB 1270
140	IF (L,LE,NCBPTS,AND,L,LE,LMAX) PRINT 310, L,XCBI(L),YCBI(L),XCB(L),	GCB 1280
	YCB(L),SLOPE	GCB 1290
	IF (L,GT,NCBPTS,AND,L,LE,LMAX) PRINT 320, L,XCB(L),YCB(L),SLOPE	GCB 1300
	IF (L,LE,NCBPTS,AND,L,GT,LMAX) PRINT 330, L,XCBI(L),YCBI(L)	GCB 1310
150	CONTINUE	GCB 1320
	GO TO 200	GCB 1330
C		GCB 1340
C	GENERAL CENTERBODY CASE = INPUT CENTERBODY COORDINATES AND SLOPES	GCB 1350
C		GCB 1360
160	PRINT 220	GCB 1370
	IF (IUI,EQ,1) PRINT 290	GCB 1380
	IF (IUI,EQ,2) PRINT 300	GCB 1390
	DO 180 L=1,LMAX	GCB 1400
	XCB(L)=XICB+DX*(L-1)	GCB 1410
	IF (YCB(L),GE,0,0) GO TO 170	GCB 1420
	YCB(L)=0,0	GCB 1430
	NXNYCB(L)=0,0	GCB 1440
170	SLOPE=-NXNYCB(L)	GCB 1450
	PRINT 340, L,XCB(L),YCB(L),SLOPE	GCB 1460
180	CONTINUE	GCB 1470
	GO TO 200	GCB 1480
C		GCB 1490
190	PRINT 350	GCB 1500
	IERR=1	GCB 1510
	RETURN	GCB 1520
C		GCB 1530
200	IF (IUI,EQ,1) RETURN	GCB 1540
	DO 210 L=1,LMAX	GCB 1550
	YCB(L)=YCB(L)/2,54	GCB 1560
210	CONTINUE	GCB 1570
	XICB=XICB/2,54	GCB 1580
	XECB=XECB/2,54	GCB 1590
	DX=UX/2,54	GCB 1600
	RETURN	GCB 1610
C		GCB 1620
C	FORMAT STATEMENTS	GCB 1630
C		GCB 1640

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220  FORMAT (1H1) GCB 1650
230  FORMAT (1H0,20X,52HA CYLINDRICAL CENTERBODY HAS BEEN SPECIFIED BY GCB 1660
1XICB=F8,4,12H (IN), RICB=F8,4,16H (IN), AND XECB=F8,4,5H (IN)) GCB 1670
240  FORMAT (1H0,20X,52HA CYLINDRICAL CENTERBODY HAS BEEN SPECIFIED BY GCB 1680
1XICB=F8,4,12H (CM), RICB=F8,4,16H (CM), AND XECB=F8,4,5H (CM)) GCB 1690
250  FORMAT (1H0,20X,62HA CIRCULAR-ARC, CONICAL CENTERBODY HAS BEEN SPEGCB 1700
1CIFIED BY XICB=F8,4,5H (IN),7H, RICB=F8,4,6H (IN),,/,21X,5HRTCB=GCB 1710
2,F8,4,7H (IN),,5HXECB=F8,4,5H (IN),8H, RCICB=F8,4,5H (IN),8H, RGC 1720
3CTCB=F8,4,5H (IN),9H, ANGICB=F6,2,7H (DEG),,/,21X,11HAND ANGECB=GCB 1730
4,F6,2,8H (DEG),,29HTHE COMPUTED VALUES ARE XTCB=F8,4,5H (IN),10HGC 1740
5 AND RECB=F8,4,6H (IN),) GCB 1750
260  FORMAT (1H0,20X,62HA CIRCULAR-ARC, CONICAL CENTERBODY HAS BEEN SPEGCB 1760
1CIFIED BY XICB=F8,4,5H (CM),7H, RICB=F8,4,6H (CM),,/,21X,5HRTCB=GCB 1770
2,F8,4,7H (CM),,5HXECB=F8,4,5H (CM),8H, RCICB=F8,4,5H (CM),8H, RGC 1780
3CTCB=F8,4,5H (CM),9H, ANGICB=F6,2,7H (DEG),,/,21X,11HAND ANGECB=GCB 1790
4,F6,2,8H (DEG),,29HTHE COMPUTED VALUES ARE XTCB=F8,4,5H (CM),10HGC 1800
5 AND RECB=F8,4,6H (CM),) GCB 1810
270  FORMAT (1H0,20X,76HA GENERAL CENTERBODY HAS BEEN SPECIFIED BY THE GCB 1820
1FOLLOWING PARAMETERS, IINTCB=I1,9H, IDIFCB=I1,1H,,/,22X,1HL,10XGCB 1830
2,8HXCBI(IN),10X,8HYCBI(IN),9X,7HXCBI(IN),10X,7HYCBI(IN),11X,5HSLOPE,GCB 1840
3/) GCB 1850
280  FORMAT (1H0,20X,76HA GENERAL CENTERBODY HAS BEEN SPECIFIED BY THE GCB 1860
1FOLLOWING PARAMETERS, IINTCB=I1,9H, IDIFCB=I1,1H,,/,22X,1HL,10XGCB 1870
2,8HXCBI(CM),10X,8HYCBI(CM),9X,7HXCBI(CM),10X,7HYCBI(CM),11X,5HSLOPE,GCB 1880
3/) GCB 1890
290  FORMAT (1H0,20X,68HA GENERAL CENTERBODY HAS BEEN SPECIFIED BY THE GCB 1900
1FOLLOWING PARAMETERS,,/,22X,1HL,11X,7HXCBI(IN),10X,7HYCBI(IN),11X,5GCB 1910
2HSLOPE,/) GCB 1920
300  FORMAT (1H0,20X,68HA GENERAL CENTERBODY HAS BEEN SPECIFIED BY THE GCB 1930
1FOLLOWING PARAMETERS,,/,22X,1HL,11X,7HXCBI(CM),10X,7HYCBI(CM),11X,5GCB 1940
2HSLOPE,/) GCB 1950
310  FORMAT (1H,20X,I2,7X,F10,4,7X,F10,4,7X,F10,4,7X,F10,4,7X,F10,4) GCB 1960
320  FORMAT (1H,20X,I2,41X,F10,4,7X,F10,4,7X,F10,4) GCB 1970
330  FORMAT (1H,20X,I2,7X,F10,4,7X,F10,4) GCB 1980
340  FORMAT (1H,20X,I2,7X,F10,4,7X,F10,4,7X,F10,4) GCB 1990
350  FORMAT (1H0,48H***** RCICB OR RCTCB WAS SPECIFIED AS ZERO ***** GCB 2000
END GCB 2010

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C	SUBROUTINE MTLUP(X,Y,M,N,MAX,NTAB,I,VARI,VARD)	MTL	10
C	*****	MTL	20
C	*****	MTL	30
C	THIS SUBROUTINE IS CALLED BY SUBROUTINE GEOM TO INTERPOLATE FOR	MTL	40
C	EQUALLY SPACED NOZZLE WALL COORDINATES FOR THE TABULAR INPUT	MTL	50
C	CASE, SUBROUTINE MTLUP WAS TAKEN FROM THE NASA-LANGLEY PROGRAM	MTL	60
C	LIBRARY. THE DATE OF THIS VERSION IS 09-12-69,	MTL	70
C	*****	MTL	80
C	*****	MTL	90
C	*****	MTL	100
C	MODIFICATION OF LIBRARY INTERPOLATION SUBROUTINE FTUP	MTL	110
C	MULTIPLE TABLE LOOK-UP ON ONE INDEPENDENT VARIABLE TABLE	MTL	120
C	USES AN EXTERNAL INTERVAL POINTER (I) TO START SEARCH	MTL	130
C	I LESS THAN 0 WILL CHECK MONOTONICITY	MTL	140
C		MTL	150
C	DIMENSION VARI(1), VARD(MAX,1), Y(1), V(3), YY(2)	MTL	160
C	LOGICAL EX	MTL	170
C		MTL	180
C	IF (M,EQ,0) GO TO 170	MTL	190
C	IF (N,LE,1) GO TO 170	MTL	200
C	EX=.F.	MTL	210
C	IF (I,GE,0) GO TO 60	MTL	220
C	IF (N,LT,2) GO TO 60	MTL	230
C		MTL	240
C	MONOTONICITY CHECK	MTL	250
C		MTL	260
C	IF (VARI(2)-VARI(1)) 20,20,40	MTL	270
C		MTL	280
C	ERROR IN MONOTONICITY	MTL	290
C		MTL	300
C	K=LOC(VARI(1))	MTL	310
10	PRINT 190, J,K,(VARI(J),J=1,N)	MTL	320
C	STOP	MTL	330
C		MTL	340
C	MONOTONIC DECREASING	MTL	350
C		MTL	360
C	DO 30 J=2,N	MTL	370
20	IF (VARI(J)-VARI(J-1)) 30,10,10	MTL	380
C	CONTINUE	MTL	390
30	GO TO 60	MTL	400
C		MTL	410
C	MONOTONIC INCREASING	MTL	420
C		MTL	430
40	DO 50 J=2,N	MTL	440
C	IF (VARI(J)-VARI(J-1)) 10,10,50	MTL	450
50	CONTINUE	MTL	460
C		MTL	470
C	INTERPOLATION	MTL	480
C		MTL	490
60	IF (I,LE,0) I=1	MTL	500
C	IF (I,GE,N) I=N-1	MTL	510
C		MTL	520
C	LOCATE I INTERVAL (X(I),LE,X,LT,X(I+1))	MTL	530
C		MTL	540
C	IF ((VARI(I)-X)*(VARI(I+1)-X)) 100,100,70	MTL	550
C		MTL	560
C	IN GIVES DIRECTION FOR SEARCH OF INTERVALS	MTL	570
C		MTL	580
70	IN=SIGN(1,0,(VARI(I+1)-VARI(I))*(X-VARI(I)))	MTL	590
C		MTL	600
C	IF X OUTSIDE ENDPOINTS, EXTRAPOLATE FROM END INTERVAL	MTL	610
C		MTL	620
80	IF ((I+IN),LE,0) GO TO 90	MTL	630
C	IF ((I+IN),GE,N) GO TO 90	MTL	640
C	I=I+IN	MTL	650
C	IF ((VARI(I)-X)*(VARI(I+1)-X)) 100,100,80	MTL	660
C		MTL	670
C	EXTRAPOLATION	MTL	680
C		MTL	690
90	EX=.T.	MTL	700
100	IF (M,EQ,2) GO TO 120	MTL	710
C		MTL	720
C	FIRST ORDER	MTL	730
C		MTL	740
C	DO 110 NT=1,NTAB	MTL	750
110	Y(NT)=(VARD(I,NT)*(VARI(I+1)-X)-VARD(I+1,NT)*(VARI(I)-X))/(VARI(I+1)-VARI(I))	MTL	760
C	IF (EX) I=I+IN	MTL	770
C	RETURN	MTL	780
C		MTL	790
C	SECOND ORDER	MTL	800
C		MTL	810
C		MTL	820
C		MTL	830

120	IF (N,EQ,2) GO TO 10	MTL	840
	IF (I,EQ,(N-1)) GO TO 140	MTL	850
	IF (I,EQ,1) GO TO 130	MTL	860
C		MTL	870
C	PICK THIRD POINT	MTL	880
C		MTL	890
	SK=VARI(I+1)-VARI(I)	MTL	900
	IF ((SK*(X-VARI(I-1))),LT,(SK*(VARI(I+2)-X))) GO TO 140	MTL	910
130	L=I	MTL	920
	GO TO 150	MTL	930
140	L=I-1	MTL	940
150	V(1)=VARI(L)-X	MTL	950
	V(2)=VARI(L+1)-X	MTL	960
	V(3)=VARI(L+2)-X	MTL	970
	DO 160 NT=1,NTAB	MTL	980
	YY(1)=(VARD(L,NT)*V(2)-VARD(L+1,NT)*V(1))/(VARI(L+1)-VARI(L))	MTL	990
	YY(2)=(VARD(L+1,NT)*V(3)-VARD(L+2,NT)*V(2))/(VARI(L+2)-VARI(L+1))	MTL	1000
160	Y(NT)=(YY(1)*V(3)+YY(2)*V(1))/(VARI(L+2)-VARI(L))	MTL	1010
	IF (EX) I=I+IN	MTL	1020
	RETURN	MTL	1030
C		MTL	1040
C	ZERO ORDER	MTL	1050
C		MTL	1060
170	DO 180 NT=1,NTAB	MTL	1070
180	Y(NT)=VARD(1,NT)	MTL	1080
	RETURN	MTL	1090
C		MTL	1100
190	FORMAT (1H1,49H TABLE BELOW OUT OF ORDER FOR MTLUP AT POSITION ,1	MTL	1110
	15,/31H X TABLE IS STORED IN LOCATION ,06,/(8G15,8))	MTL	1120
	END	MTL	1130

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C      FUNCTION DIF (L,M,NP,VARI,VARD)
C      *****
C      THIS FUNCTION IS CALLED BY SUBROUTINE GEOM TO CALCULATE THE
C      NOZZLE WALL SLOPE FOR THE TABULAR INPUT CASE. FUNCTION DIF WAS
C      TAKEN FROM THE NASA-LANGLEY PROGRAM LIBRARY. THE DATE OF THIS
C      VERSION IS 08-01-68.
C      *****
C      THIS FUNCTION SUBPROGRAM FINDS THE DERIVATIVE AT A GIVEN POINT,
C      L, FOR THE DESIRED X AND Y IN A GIVEN TABLE. THE N-POINT
C      LAGRANGIAN FORMULA IS USED WHERE N IS ODD.
C      L = INTEGER, THE POINT OF X AND Y AT WHICH DERIVATIVE IS FOUND
C      M = INTEGER, 1-5, TO DETERMINE THE POINT FORMULA, N, N=2*M+1
C      NP = INTEGER, THE NUMBER OF POINTS IN TABLE OF VARIABLES
C      VARI = ARRAY OF INDEPENDENT VARIABLE, X, VARI(NP)
C      VARD = ARRAY OF DEPENDENT VARIABLE, Y, VARD(NP)
C
C      DIMENSION VARI(NP), VARD(NP), X(11), Y(11)
C      DIF=77700000000000000000000000000000
C      IF (M,LT,1) RETURN
C      N=2*M+1
C      IF (M,GT,5.OR,N,GT,NP) RETURN
C      M1=M+1
C      M2=NP-M+1
C      K=L
C      IF (L,LE,M1.OR,N,GE,M2) GO TO 10
C      K=M1
C      IF (L,LT,M2) GO TO 10
C      K=L-(NP-N)
10     MX=L-K
C      DO 20 J=1,N
C      MJ=MX+J
C      X(J)=VARI(MJ)
20     Y(J)=VARD(MJ)
C      A=1,
C      B=0,
C      C=0,
C      DO 40 J=1,N
C      IF (J,EQ,K) GO TO 40
C      P=1,
C      DO 30 I=1,N
C      IF (I,EQ,J) GO TO 30
C      P=P*(X(J)-X(I))
30     CONTINUE
C      T=X(K)-X(J)
C      B=B+Y(J)/(P*T)
C      A=A*T
C      C=C+1,/T
C      CONTINUE
C      DIF=A*B+Y(K)*C
C      RETURN
C      END
C

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	SUBROUTINE ONEDIM	ONE	10
C		ONE	20
C	*****	ONE	30
C		ONE	40
C	THIS SUBROUTINE CALCULATES THE 1-D INITIAL-DATA SURFACE	ONE	50
C		ONE	60
C	*****	ONE	70
C		ONE	80
	COMMON /AV/ IAV,CAV,NST,SMP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81,	ONE	90
	1,21),QPT(81,21)	ONE	100
	COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)	ONE	110
	COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RO(81,21,2)	ONE	120
	COMMON /CNTRLC/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAM1,GAONE	ONE	130
	1M2,L1,L2,L3,M1,M2,DX,DY,DT,N,N1,N3,NASM,IYEL,ICAR,NID,LJET,JFLAG,ONE	ONE	140
	2IERR,IUI,IUD,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TCONE	ONE	150
	3,LC,PLOW,ROLOW	ONE	160
	COMMON /GENTRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCT,ANGI,ANGE,XN(81),ONE	ONE	170
	1YH(81),XHI(81),YHI(81),NXNY(81),NMPTS,IINT,IDIF,LT,NDIM	ONE	180
	COMMON /GCB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,RECB,RCICB,RCTCB,ANGICBONE	ONE	190
	1,ANGEGB,XCB(81),YCB(81),XCB1(81),YCB1(81),NXNYCB(81),NCBPTS,IINTCBONE	ONE	200
	2,IDIFCB,LECB	ONE	210
	COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASSI,MASST,THRUST,NONE	ONE	220
	1STAG	ONE	230
	REAL MN3,NXNY,MASSI,MASST,NXNYCB,MASSE	ONE	240
C		ONE	250
	MN3=0.01	ONE	260
	IF (NID,EQ,-1.OR,NID,GT,2) MN3=2.0	ONE	270
	GRGAS=1.0/(RGAS*G)	ONE	280
	NXCK=0	ONE	290
	ACOE=2.0/(GAMMA+1.0)	ONE	300
	BCOE=(GAMMA-1.0)/(GAMMA+1.0)	ONE	310
	CCOE=(GAMMA+1.0)/2.0/(GAMMA-1.0)	ONE	320
	IF (NID,LT,0) GO TO 20	ONE	330
C		ONE	340
C	OVERALL LOOP	ONE	350
C		ONE	360
	IF (NGCB,NE,0) GO TO 10	ONE	370
	RSTAR=RT	ONE	380
	RSTARS=RT*RT	ONE	390
	GO TO 20	ONE	400
10	RSTAR=YH(LT)-YCB(LT)	ONE	410
	RSTARS=YH(LT)**2-YCB(LT)**2	ONE	420
20	DO 130 L=1,LMAX	ONE	430
	IF (L,EQ,1.AND,NID,EQ,-1) GO TO 130	ONE	440
	IF (L,EQ,1.AND,NID,GT,2) GO TO 130	ONE	450
	X=X1+DX*(L-1)	ONE	460
	IF (NID,LT,0) GO TO 50	ONE	470
	IF (NGCB,NE,0) GO TO 30	ONE	480
	IF (X,LT,XT) GO TO 50	ONE	490
	IF (X,GT,XT) GO TO 40	ONE	500
	MN3=1.0	ONE	510
	GO TO 100	ONE	520
30	IF (L,LT,LT) GO TO 50	ONE	530
	IF (L,GT,LT) GO TO 40	ONE	540
	MN3=1.0	ONE	550
	GO TO 100	ONE	560
40	IF (NXCK,EQ,1) GO TO 50	ONE	570
	IF (NID,EQ,1.OR,NID,EQ,3) MN3=1.1	ONE	580
	IF (NID,EQ,2.OR,NID,EQ,4) MN3=0.9	ONE	590
	NXCK=1	ONE	600
50	IF (NDIM,EQ,1) GO TO 60	ONE	610
	RAD=YH(L)-YCB(L)	ONE	620
	ARATIO=RAD/RSTAR	ONE	630
	GO TO 70	ONE	640
60	RADS=YH(L)**2-YCB(L)**2	ONE	650
	ARATIO=RADS/RSTARS	ONE	660
		ONE	670
C		ONE	680
C	NEWTON-RAPHSON ITERATION LOOP	ONE	690
C		ONE	700
70	DO 90 ITER=1,20	ONE	710
	ABM=ACOE+BCOE*MX3*MX3	ONE	720
	ABMC=ABM*CCOE	ONE	730
	FM=ABMC/MN3*ARATIO	ONE	740
	FPM=ABMC*(2.0*BCOE*CCOE/ABM-1.0/(MN3*MX3))	ONE	750
	OMN3=MN3	ONE	760
	MN3=OMN3-FM/FPM	ONE	770
	IF (MN3,GT,1.0.AND,OMN3,LT,1.0) MN3=0.99	ONE	780
	IF (MN3,LT,1.0.AND,OMN3,GT,1.0) MN3=1.01	ONE	790
	IF (MN3,GE,0.0) GO TO 80	ONE	800
	MN3=-MN3	ONE	810
	GO TO 90	ONE	820
80	IF (ABS(MN3-OMN3)/OMN3,LE,0.0005) GO TO 100	ONE	830
90	CONTINUE	ONE	840
	PRINT 140, L	ONE	850

C		ONE	850
C	FILL IN 2-D ARRAYS LOOP	ONE	860
C		ONE	870
100	DEM=1.0+GAM2*MN3*MN3	ONE	880
	DEMP=DEM**GAM1	ONE	890
	DNXNY=(NXNY(L)-NXNYCB(L))/M1	ONE	900
	DO 120 M=1,HMAX	ONE	910
	P(L,M,1)=PT(M)/DEMP	ONE	920
	TEMP=TT(M)/DEM	ONE	930
	RO(L,M,1)=P(L,M,1)*GRGAS/TEMP	ONE	940
	Q=MN3*SQRT(GAMMA*P(L,M,1)/RO(L,M,1))	ONE	950
	DN=NXNYCB(L)+DNXNY*(M-1)	ONE	960
	DNS=DN*DN	ONE	970
	IF (DNS.EQ.0.0) GO TO 110	ONE	980
	SIGN=1.0	ONE	990
	IF (DN.GT.0.0) SIGN=-1.0	ONE	1000
	U(L,M,1)=Q/SQRT(1.0+DNS)	ONE	1010
	V(L,M,1)=SIGN*Q/SQRT(1.0+1.0/DNS)	ONE	1020
	GO TO 120	ONE	1030
110	U(L,M,1)=Q	ONE	1040
	V(L,M,1)=0.0	ONE	1050
120	CONTINUE	ONE	1060
130	CONTINUE	ONE	1070
	RETURN	ONE	1080
C		ONE	1090
140	FORMAT (1H0,10X,93H***** THE 1-D SOLUTION FOR THE INITIAL=DATA SUR	ONE	1100
	FACE FAILED TO CONVERGE IN 20 ITERATIONS AT L=,12,6H *****)	ONE	1110
	END	ONE	1120

C	SUBROUTINE MAP(IP,L,M,AL,BE,DE,LD1,AL1,BE1,DE1)	MAP	10
C	*****	MAP	20
C	*****	MAP	30
C	THIS SUBROUTINE CALCULATES THE MAPPING FUNCTIONS	MAP	40
C	*****	MAP	50
C	*****	MAP	60
C	*****	MAP	70
	COMMON /AV/ JAV,CAV,NST,SMP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81,21),QPT(81,21)	MAP	80
	1,21),QPT(81,21)	MAP	90
	COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)	MAP	100
	COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RO(81,21,2)	MAP	110
	COMMON /CNTRLC/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RCAS,GAH1,GAMAP	MAP	120
	1M2,L1,L2,L3,M1,M2,DX,DY,DT,N,N1,N3,NASH,IVEL,ICHAR,NID,LJET,JFLAG,MAP	MAP	130
	21ERR,IUI,IUO,DXR,DYR,LD,HD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TCHAP	MAP	140
	3,LC,PLOW,HOLOW	MAP	150
	COMMON /GENTRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCI,ANGI,ANGE,XW(81),MAP	MAP	160
	1YH(81),XWI(81),YHI(81),NXNY(81),NHPTS,IINT,IDIF,LI,NDIM	MAP	170
	COMMON /GCB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,RECB,RCICB,RCTCB,ANGICBMAP	MAP	180
	1,ANGEGB,XCB(81),YCB(81),XCB1(81),YCB1(81),NXNYCB(81),NCBPTS,IINTCBMAP	MAP	190
	2,IDIFCB,LECB	MAP	200
	COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASSI,MASST,THRUST,NMAP	MAP	210
	1STAG	MAP	220
	REAL MN3,NXNY,MASST,MASST,NXNYCB,MASSE	MAP	230
C		MAP	240
	BE=1.0/(YH(L)-YCB(L))	MAP	250
	IF (IP,EQ,0) RETURN	MAP	260
	Y=(M-1)*DY	MAP	270
	AL=BE*(NXNYCB(L)+Y*(NXNY(L)-NXNYCB(L)))	MAP	280
	DE=-BE*Y*XWI(L)	MAP	290
	IF (IP,EQ,1) RETURN	MAP	300
	BE=1.0/(YH(LD1)-YCB(LD1))	MAP	310
	AL1=BE1*(NXNYCB(LD1)+Y*(NXNY(LD1)-NXNYCB(LD1)))	MAP	320
	DE1=-BE1*Y*XWI(LD1)	MAP	330
	RETURN	MAP	340
	END	MAP	350
		MAP	360

```

SUBROUTINE MASFLO(ISURF)
C
C *****
C THIS SUBROUTINE CALCULATES THE INITIAL=DATA OR SOLUTION SURFACE
C MASS FLOW AND THRUST
C *****
C
COMMON /AV/ IAV,CAV,NST,SMP,LS9,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81,
1,21),QPT(81,21)
COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)
COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RO(81,21,2)
COMMON /CNTRL/ LMAX,HMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAM1,GAM2,
1M2,L1,L2,L3,M1,M2,DX,DY,DT,N,N1,N3,NASM,IVEL,ICHAR,NID,LJET,JFLAG,
2IERR,IUI,IUO,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TCMA
3,LC,PLOW,ROLOW
COMMON /GENTRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCT,ANGI,ANGE,XW(81),
1YH(81),XWI(81),YHI(81),NXNY(81),NMPTS,IINT,IDIF,LT,NDIM
COMMON /GCB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,RECB,RCICB,RCTCB,ANGICBMA
1,ANGEGB,XCB(81),YCB(81),XCB1(81),YCB1(81),NXNYCB(81),NCBPTS,IINTCBMA
2,IDIFCB,LECB
COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASSI,MASST,THRUST,NMA
1STAG
REAL MN3,NXNY,MASST,MASST,NXNYCB,MASSE
C
LC2=LC*LC
LDUM=LMAX*1
IF (LT,EQ,LMAX) LT=LMAX*1
IF (JFLAG,NE,0) LDUM=LJET*1
IF (ISURF,EQ,1,OR,NID,EQ,0) GO TO 30
C
C CALCULATE THE MASS FLOW AND THRUST FOR THE 1-D INITIAL=DATA
C SURFACE
C
IF (NDIM,EQ,1) GO TO 10
AREAI=(YH(1)-YCB(1))/LC2
AREAT=(YH(LT)-YCB(LT))/LC2
AREAE=(YH(LDUM)-YCB(LDUM))/LC2
GO TO 20
10 AREAI=3.141593*(YH(1)**2-YCB(1)**2)/LC2
AREAT=3.141593*(YH(LT)**2-YCB(LT)**2)/LC2
AREAE=3.141593*(YH(LDUM)**2-YCB(LDUM)**2)/LC2
20 VHI=SQRT(U(1,1,1)**2+V(1,1,1)**2)
VMT=SQRT(U(LT,1,1)**2+V(LT,1,1)**2)
VME=SQRT(U(LDUM,1,1)**2+V(LDUM,1,1)**2)
MASSI=RO(1,1,1)*VHI*AREAI*G
MASST=RO(LT,1,1)*VMT*AREAT*G
MASSE=RO(LDUM,1,1)*VME*AREAE*G
THRUST=RO(LDUM,1,1)*U(LDUM,1,1)**2*AREAE
RETURN
C
C CALCULATE THE MASS FLOW AND THRUST FOR THE 2-D INITIAL=DATA
C AND SOLUTION SURFACES
C
30 MASSI=0.0
MASST=0.0
MASSE=0.0
THRUST=0.0
DYI=DY*(YH(1)-YCB(1))
DYT=DY*(YH(LT)-YCB(LT))
DYE=DY*(YH(LDUM)-YCB(LDUM))
ND=1
IF (ISURF,EQ,1) ND=N3
DO 60 M=1,M1
RADI=(M-1)*DYI+YCB(1)
RADT=(M-1)*DYT+YCB(LT)
RADE=(M-1)*DYE+YCB(LDUM)
IF (NDIM,EQ,1) GO TO 40
AREAI=DYI/LC2
AREAT=DYT/LC2
AREAE=DYE/LC2
GO TO 50
40 AREAI=3.141593*((RADI+DYI)**2-RADI**2)/LC2
AREAT=3.141593*((RADT+DYT)**2-RADT**2)/LC2
AREAE=3.141593*((RADE+DYE)**2-RADE**2)/LC2
50 ROUI=(RO(1,M,ND)*U(1,M,ND)+RO(1,M+1,ND)*U(1,M+1,ND))*0.5
ROUT=(RO(LT,M,ND)*U(LT,M,ND)+RO(LT,M+1,ND)*U(LT,M+1,ND))*0.5
ROUE=(RO(LDUM,M,ND)*U(LDUM,M,ND)+RO(LDUM,M+1,ND)*U(LDUM,M+1,ND))*0.5
1,5 ROU2E=(RO(LDUM,M,ND)*U(LDUM,M,ND)**2+RO(LDUM,M+1,ND)*U(LDUM,M+1,NDMA
810

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1)**2)*0.5
MASSI=MASSI+ROUI*AREAI*G
MASTT=MASTT+ROUT*AREAT*G
MASSE=MASSE+ROUE*AREAE*G
THRUST=THRUST+ROUZE*AREAE
60 CONTINUE
RETURN
END

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MAS 820
MAS 830
MAS 840
MAS 850
MAS 860
MAS 870
MAS 880
MAS 890

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SUBROUTINE PLOT(TITLE,T,NP)
C
C *****
C THIS SUBROUTINE PLOTS THE VELOCITY VECTORS AND DEPENDENT VARIABLE
C CONTOUR PLOTS
C *****
C
C DIMENSION CQ(81,21), CON(9), XCO(4), YCO(4), TITLE(8)
COMMON /AV/ JAV,CAV,NST,SMP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81,
1,21),QPT(81,21)
COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)
COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RO(81,21,2)
COMMON /CNTRLC/ LMAX,HMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAM1,CAPLT
1M2,L1,L2,L3,M1,M2,DX,DY,DT,N,N1,N3,NASM,IYEL,ICAR,NID,LJET,JFLAG,PLT
2IERR,IUI,IUO,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TCPLT
3,LC,PLOW,ROLOW
COMMON /GEMTRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCT,ANGI,ANGE,XW(81),
1YW(81),XWI(81),YWI(81),NXNY(81),NWPTS,IINT,IDI,LT,NDIM
COMMON /GCB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,RECB,RCICB,RCITCB,ANGICB,PLT
1,ANGEGB,XCB(81),YCB(81),XCB1(81),YCB1(81),NXNYCB(81),NCBPTS,IINTCB,PLT
2,IDI,FCB,LECB
COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASSI,MASST,THRUST,NPLT
1STAG
REAL MN3,NXNY,MASSI,MASST,NXNYCB,MASSE
C
C GENERATE THE VELOCITY VECTOR PLOT
C
ND=N3
IF (N.EQ.0) ND=1
CALL GETQ (4LKJBN,JNM)
XL=XI
XR=XE
YT=YW(1)
YB=YCB(1)
DO 10 L=2,LMAX
YT=AMAX1(YT,YW(L))
YB=AMIN1(YB,YCB(L))
10 CONTINUE
VV=0.9*DX
FIYB=916.0
XD=(XR-XL)/(YT-YB)
FIR=(1022.0-1022.0/FLOAT(L1)-1.0)/900.0
IF(XD.LE.FIR) GO TO 20
FIXL=0.0
FIXR=1022.0-1022.0/FLOAT(L1)-1.0
FIYT=916.0-FIXR/XD
GO TO 30
20 FIXL=511.0-450.0*XD
FIXR=511.0+450.0*XD
FIYT=16.0
30 XCONV=(FIXR-FIXL)/(XR-XL)
YCONV=(FIYT-FIYB)/(YT-YB)
VMAX=0.0
DO 40 L=1,LMAX
DO 40 M=1,MMAX
VMAX=AMAX1(VMAX,ABS(U(L,M,ND)),ABS(V(L,M,ND)))
40 CONTINUE
IF (VMAX.LT.1.0E-10) GO TO 60
DROU=VV/VMAX
CALL ADV (1)
DO 50 L=1,LMAX
IX1=FIXL+(FLOAT(L-1)*DX)*XCONV
DY=(YW(L)-YCB(L))/FLOAT(MMAX-1)
DO 50 M=1,MMAX
IY1=FIYB+(YCB(L)+FLOAT(M-1)*DY-YB)*YCONV
IX2=FIXL+(FLOAT(L-1)*DX+U(L,M,ND)*DROU)*XCONV
IY2=FIYB+(YCB(L)+FLOAT(M-1)*DY+V(L,M,ND)*DROU)*YCONV
CALL DRV (IX1,IY1,IX2,IY2)
CALL PLT (IX1,IY1,16)
50 CONTINUE
CALL LINCNT (59)
WRITE (7,410)
WRITE (7,350)JNM,TITLE,NP,T
C
C GENERATE THE CONTOUR PLOTS
C
60 I=0
70 I=I+1
GO TO (80,100,120,140,340), I
80 DO 90 L=1,LMAX
90 DO 90 M=1,MMAX
CQ(L,M)=RU(L,M,ND)*G

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90	CONTINUE	PLT	850
	GO TO 160	PLT	860
100	DO 110 L=1,LMAX	PLT	870
	DO 110 M=1,MMAX	PLT	880
	CQ(L,M)=P(L,M,ND)/PC	PLT	890
110	CONTINUE	PLT	900
	GO TO 160	PLT	910
120	DO 130 L=1,LMAX	PLT	920
	DO 130 M=1,MMAX	PLT	930
	CQ(L,M)=P(L,M,ND)/RO(L,M,ND)/RGAS/G=TC	PLT	940
130	CONTINUE	PLT	950
	GO TO 160	PLT	960
140	DO 150 L=1,LMAX	PLT	970
	DO 150 M=1,MMAX	PLT	980
	CQ(L,M)=SQRT((U(L,M,ND)**2+V(L,M,ND)**2)/(GAMMA*P(L,M,ND)/RO(L,M,NPLT	PLT	990
	ID)))	PLT	1000
150	CONTINUE	PLT	1010
160	QMN=1,OE06	PLT	1020
	QMX=QMN	PLT	1030
	DO 170 L=1,LMAX	PLT	1040
	DO 170 M=1,MMAX	PLT	1050
	QMN=AMIN1(CQ(L,M),QMN)	PLT	1060
	QMX=AMAX1(CQ(L,M),QMX)	PLT	1070
170	CONTINUE	PLT	1080
	XX=QMX-QMN	PLT	1090
	DQ=0,1+XX	PLT	1100
	DO 180 K=1,9	PLT	1110
	CON(K)=QMN+(FLOAT(K))*DQ	PLT	1120
180	CONTINUE	PLT	1130
	K=9	PLT	1140
	CALL ADV (1)	PLT	1150
	CALL LINCNT (59)	PLT	1160
	GO TO (190,200,210,220), I	PLT	1170
190	WRITE (7,360)	PLT	1180
	GO TO 230	PLT	1190
200	WRITE (7,370)	PLT	1200
	GO TO 230	PLT	1210
210	WRITE (7,380)	PLT	1220
	GO TO 230	PLT	1230
220	WRITE (7,390)	PLT	1240
230	WRITE (7,400)QMN,QMX,CON(1),CON(K),DQ	PLT	1250
	WRITE (7,350)JNM,TITLE,NP,T	PLT	1260
	DO 320 L=2,LMAX	PLT	1270
	DY=(YM(L-1)-YCB(L-1))/FLOAT(MMAX-1)	PLT	1280
	DY1=(YM(L)-YCB(L))/FLOAT(MMAX-1)	PLT	1290
	DO 320 M=2,MMAX	PLT	1300
	NN=0	PLT	1310
	DO 320 KK=1,K	PLT	1320
	K1=K2=K3=K4=0	PLT	1330
	IF (CQ(L-1,M-1),LE,CON(KK)) K1=1	PLT	1340
	IF (CQ(L,M-1),LE,CON(KK)) K2=1	PLT	1350
	IF (CQ(L-1,M),LE,CON(KK)) K3=1	PLT	1360
	IF (CQ(L,M),LE,CON(KK)) K4=1	PLT	1370
	IF (K1+K2+K3+K4,NE,0) GO TO 320	PLT	1380
	IF (K1+K2+K3+K4,EQ,0) GO TO 320	PLT	1390
	IF (NN,NE,0) GO TO 240	PLT	1400
	NN=1	PLT	1410
	XCO(1)=XI+FLOAT(L-2)*DX	PLT	1420
	XCO(2)=XCO(1)+DX	PLT	1430
	XCO(3)=XCO(1)	PLT	1440
	XCO(4)=XCO(2)	PLT	1450
	YCO(1)=YCB(L-1)+FLOAT(M-2)*DY	PLT	1460
	YCO(2)=YCB(L)+FLOAT(M-2)*DY	PLT	1470
	YCO(3)=YCB(L-1)+FLOAT(M-1)*DY	PLT	1480
	YCO(4)=YCB(L)+FLOAT(M-1)*DY	PLT	1490
240	LL=0	PLT	1500
	IF (K1+K3,NE,1) GO TO 250	PLT	1510
	IC1=1 \$ IC2=3 \$ LP1=L-1 \$ MP1=M-1 \$ LP2=L-1 \$ MP2=M	PLT	1520
	ASSIGN 250 TO KR1	PLT	1530
	GO TO 280	PLT	1540
250	IF (K1+K2,NE,1) GO TO 260	PLT	1550
	IC1=1 \$ IC2=2 \$ LP1=L-1 \$ MP1=M-1 \$ LP2=L \$ MP2=M-1	PLT	1560
	ASSIGN 260 TO KR1	PLT	1570
	GO TO 280	PLT	1580
260	IF (K2+K4,NE,1) GO TO 270	PLT	1590
	IC1=2 \$ IC2=4 \$ LP1=L \$ MP1=M-1 \$ LP2=L \$ MP2=M	PLT	1600
	ASSIGN 270 TO KR1	PLT	1610
	GO TO 280	PLT	1620
270	IF (K3+K4,NE,1) GO TO 320	PLT	1630
	IC1=3 \$ IC2=4 \$ LP1=L-1 \$ MP1=M \$ LP2=L \$ MP2=M	PLT	1640
	ASSIGN 320 TO KR1	PLT	1650

280	LL=LL+1	PLT 1660
	XX=(CON(KK)-CQ(LP1,MP1))/(CQ(LP2,MP2)-CQ(LP1,MP1))	PLT 1670
	IF (LL.EQ,2) GO TO 290	PLT 1680
	IX1=FIXL+(XCO(IC1)+XX*(XCO(IC2)-XCO(IC1))-XL)*XCONV	PLT 1690
	IY1=FIYB+(YCO(IC1)+XX*(YCO(IC2)-YCO(IC1))-YB)*YCONV	PLT 1700
	GO TO KR1,(250,260,270,320)	PLT 1710
290	IX2=FIXL+(XCO(IC1)+XX*(XCO(IC2)-XCO(IC1))-XL)*XCONV	PLT 1720
	IY2=FIYB+(YCO(IC1)+XX*(YCO(IC2)-YCO(IC1))-YB)*YCONV	PLT 1730
	CALL DRV (IX1,IY1,IX2,IY2)	PLT 1740
	IF (KK,NE,1) GO TO 300	PLT 1750
	CALL PLT (IX1,IY1,35)	PLT 1760
300	IF (KK,NE,K) GO TO 310	PLT 1770
	CALL PLT (IX1,IY1,24)	PLT 1780
310	LL=0	PLT 1790
	IF (LP2,NE,L) GO TO 320	PLT 1800
	IF (MP2,NE,M=1) GO TO 320	PLT 1810
	GO TO 260	PLT 1820
320	CONTINUE	PLT 1830
C		PLT 1840
C	DRAW THE GEOMETRY CONTOURS	PLT 1850
C		PLT 1860
	DO 330 L=2,LMAX	PLT 1870
	IX1=FIXL+(FLOAT(L-2)*DX)*XCONV	PLT 1880
	IX2=FIXL+(FLOAT(L-1)*DX)*XCONV	PLT 1890
	IY1=FIYB+(YCB(L-1)-YB)*YCONV	PLT 1900
	IY2=FIYB+(YCB(L)-YB)*YCONV	PLT 1910
	IY3=FIYB+(YH(L-1)-YB)*YCONV	PLT 1920
	IY4=FIYB+(YH(L)-YB)*YCONV	PLT 1930
	CALL DRV (IX1,IY1,IX2,IY2)	PLT 1940
	CALL DRV (IX1,IY3,IX2,IY4)	PLT 1950
330	CONTINUE	PLT 1960
	GO TO 70	PLT 1970
340	CONTINUE	PLT 1980
	DY=1,0/FLOAT(MMAX=1)	PLT 1990
	CALL ADV (1)	PLT 2000
	RETURN	PLT 2010
C		PLT 2020
350	FORMAT (1H ,A10,4X,0A10,2X,2HN=,I4,2X,2HT=,1PE10,4,4H SEC)	PLT 2030
360	FORMAT (1H ,7HDENSITY)	PLT 2040
370	FORMAT (1H ,8HPPRESSURE)	PLT 2050
380	FORMAT (1H ,11HTEMPERATURE)	PLT 2060
390	FORMAT (1H ,11HMACH NUMBER)	PLT 2070
400	FORMAT (1H ,10HLOW VALUE=,1PE11,4,2X,11HHIGH VALUE=,E11,4,2X,12HLOPLT 2080	
	1H CONTOUR=,E11,4,2X,13HHIGH CONTOUR=,E11,4,2X,14HDELTA CONTOUR=,E1PLT 2090	
	21,4)	PLT 2100
410	FORMAT (1H ,16HVELOCITY VECTOR8)	PLT 2110
	END	PLT 2120

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C      SUBROUTINE SHOCK(IPASS)                                SHO  10
C      *****                                                SHO  20
C      THIS SUBROUTINE CALCULATES THE LOCAL ARTIFICIAL VISCOSITY TERMS    SHO  30
C      FOR SHOCK COMPUTATIONS                                         SHO  40
C      *****                                                SHO  50
C      COMMON /AV/ IAV,CAV,NST,SMP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81,21),OPT(81,21) SHO  60
C      1,21),OPT(81,21)                                             SHO  70
C      COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)                     SHO  80
C      COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RO(81,21,2) SHO  90
C      COMMON /CNTRL/ LMAX,MMAX,NMAX,NPRINT,TCNV,FDT,GAMMA,RGAS,GAMI,GASHO 100
C      1M2,L1,L2,L3,M1,M2,DX,DY,DT,N,N1,N3,NASH,IVEL,ICHAR,NID,LJET,JFLAG,SHO 110
C      2IERR,IUI,IUD,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TCSHO 120
C      3,LC,PLOW,ROLOW                                              SHO 130
C      COMMON /GEMTRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCI,ANGI,ANGE,XW(81),SHO 140
C      1YH(81),XHI(81),YHI(81),NXNY(81),NHPIS,IINT,IDIF,LT,NDIM     SHO 150
C      COMMON /GCB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,RECB,RCICB,RCTCB,ANGICB,SHO 160
C      1,ANGEGB,XCB(81),YCB(81),XCB1(81),YCB1(81),NXNYCB(81),NCBPS,IINTCB,SHO 170
C      2,IDIFCB,LECB                                              SHO 180
C      COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASST,THRUST,NSHO 190
C      1STAG                                                        SHO 200
C      REAL MN3,NXNY,MASST,MASST,NXNYCB,MASSE                      SHO 210
C      GO TO (10,160), IPASS                                         SHO 220
C      CALCULATE LOCAL ARTIFICIAL VISCOSITY FOR SHOCK COMPUTATIONS    SHO 230
C      IF (N,NE,1) GO TO 30                                           SHO 240
C      NC=0                                                           SHO 250
C      RG=RGAS*G                                                       SHO 260
C      CTA1=1,0=CTA                                                  SHO 270
C      DO 20 L=1,LMAX                                                 SHO 280
C      DO 20 M=1,MMAX                                                 SHO 290
C      QUT(L,M)=0,0                                                  SHO 300
C      QVT(L,M)=0,0                                                  SHO 310
C      OPT(L,M)=0,0                                                  SHO 320
C      20 CONTINUE                                                    SHO 330
C      30 ROUM=CAV*DT*DX*DY*2,0                                       SHO 340
C      NC=NC+1                                                         SHO 350
C      NLINE=0                                                         SHO 360
C      IF (NC,NE,NPRINT) GO TO 40                                     SHO 370
C      PRINT 200                                                       SHO 380
C      PRINT 190, N,PC                                                SHO 390
C      DO 150 L=LSS,L1                                                SHO 400
C      DO 150 M=1,MMAX                                                 SHO 410
C      LMD2=LD*(M-1)+LMD1                                             SHO 420
C      LMMD2=LD*(M-2)+LMD1                                             SHO 430
C      LMPD2=LD*M+LMD1                                                SHO 440
C      LMN1=L+LMD2                                                    SHO 450
C      LP=L+1+LMD2                                                    SHO 460
C      LM=L+1+LMD2                                                    SHO 470
C      MP=L+LMPD2                                                      SHO 480
C      MM=L+LMMD2                                                      SHO 490
C      LPMP=L+1+LMPD2                                                 SHO 500
C      LPMH=L+1+LMMD2                                                 SHO 510
C      LMMP=L+1+LMPD2                                                 SHO 520
C      LMMH=L+1+LMMD2                                                 SHO 530
C      CALL MAP (1,L,M,AL,BE,DE,LD1,AL1,BE1,DE1)                    SHO 540
C      CHECK TO SEE IF THE DIVERGENCE OF THE VELOCITY IS NEGATIVE    SHO 550
C      UX=0,5*(U(LP)-U(LM))*DXR                                       SHO 560
C      IF (M,EQ,1) GO TO 50                                           SHO 570
C      IF (M,EQ,MMAX) GO TO 60                                         SHO 580
C      UY=0,5*(U(MP)-U(MM))*DYR                                       SHO 590
C      VY=0,5*(V(MP)-V(MM))*DYR                                       SHO 600
C      GO TO 70                                                        SHO 610
C      50 UY=(U(MP)-U(LMN1))*DYR                                       SHO 620
C      VY=(V(MP)-V(LMN1))*DYR                                       SHO 630
C      GO TO 70                                                        SHO 640
C      60 UY=(U(LMN1)-U(MM))*DYR                                       SHO 650
C      VY=(V(LMN1)-V(MM))*DYR                                       SHO 660
C      70 DIV=UX+AL*UY+BE*VY                                           SHO 670
C      IF (DIV,LT,0,0) GO TO 80                                       SHO 680
C      QUT(L,M)=0,0                                                  SHO 690
C      QVT(L,M)=0,0                                                  SHO 700
C      OPT(L,M)=0,0                                                  SHO 710
C      GO TO 150                                                       SHO 720

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80	OQUT=QUT(L,M)	3HO	830
	OQVT=QVT(L,M)	3HO	840
	OQPT=QPT(L,M)	3HO	850
	UX1=(U(LMN1)-U(LM))*DXR	3HO	860
	UX2=(U(LP)-U(LMN1))*DXR	3HO	870
	VX1=(V(LMN1)-V(LM))*DXR	3HO	880
	VX2=(V(LP)-V(LMN1))*DXR	3HO	890
	TM=P(LM)/(RO(LM)*RG)	3HO	900
	T=P(LMN1)/(RO(LMN1)*RG)	3HO	910
	TP=P(LP)/(RO(LP)*RG)	3HO	920
	TX1=(T-TM)*DXR	3HO	930
	TX2=(TP-T)*DXR	3HO	940
	LDUM=L-1	3HO	950
	CALL MAP (1,LDUM,M,ALM,BEM,DE,LD1,AL1,BE1,DE1)	3HO	960
	LDUM=L+1	3HO	970
	CALL MAP (1,LDUM,M,ALP,BEP,DE,LD1,AL1,BE1,DE1)	3HO	980
	BE1=0.5*(BEM+BE)	3HO	990
	BE2=0.5*(BEP+BE)	3HO	1000
	AL1=0.5*(ALM+AL)	3HO	1010
	AL2=0.5*(ALP+AL)	3HO	1020
	IF (M,EQ,1) GO TO 90	3HO	1030
	IF (M,EQ,MMAX) GO TO 100	3HO	1040
C		3HO	1050
C	CALCULATE THE INTERIOR POINT QUANTITIES	3HO	1060
C		3HO	1070
	UY1=0.25*(U(MP)+U(LMMP)-U(MM)-U(LMMH))*DYR	3HO	1080
	UY2=0.25*(U(MP)+U(LPMP)-U(MM)-U(LPMH))*DYR	3HO	1090
	VY1=0.25*(V(MP)+V(LMMP)-V(MM)-V(LMMH))*DYR	3HO	1100
	VY2=0.25*(V(MP)+V(LPMP)-V(MM)-V(LPMH))*DYR	3HO	1110
	UX3=0.25*(U(LP)+U(LPMH)-U(LM)-U(LMMH))*DXR	3HO	1120
	UX4=0.25*(U(LP)+U(LPMP)-U(LM)-U(LMMP))*DXR	3HO	1130
	VX3=0.25*(V(LP)+V(LPMH)-V(LM)-V(LMMH))*DXR	3HO	1140
	VX4=0.25*(V(LP)+V(LPMP)-V(LM)-V(LMMP))*DXR	3HO	1150
	VY3=(V(LMN1)-V(MM))*DYR	3HO	1160
	VY4=(V(MP)-V(LMN1))*DYR	3HO	1170
	UY3=(U(LMN1)-U(MM))*DYR	3HO	1180
	UY4=(U(MP)-U(LMN1))*DYR	3HO	1190
	THY=P(MM)/(RO(MM)*RG)	3HO	1200
	TPY=P(MP)/(RO(MP)*RG)	3HO	1210
	TMM=P(LMMH)/(RO(LMMH)*RG)	3HO	1220
	TMP=P(LMMP)/(RO(LMMP)*RG)	3HO	1230
	TPM=P(LPMH)/(RO(LPMH)*RG)	3HO	1240
	TPP=P(LPMP)/(RO(LPMP)*RG)	3HO	1250
	TY1=0.25*(TPY+TMP-THY-TMM)*DYR	3HO	1260
	TY2=0.25*(TPP+TPY-TPM-THY)*DYR	3HO	1270
	TX3=0.25*(TP+TPM-TM-TMM)*DXR	3HO	1280
	TX4=0.25*(TPP+TP-TMP-TM)*DXR	3HO	1290
	TY3=(T-THY)*DYR	3HO	1300
	TY4=(TPY-T)*DYR	3HO	1310
	MDUM=M-1	3HO	1320
	CALL MAP (1,L,MDUM,ALMY,BEMY,DE,LD1,AL1,BE1,DE1)	3HO	1330
	MDUM=M+1	3HO	1340
	CALL MAP (1,L,MDUM,ALPY,BEPY,DE,LD1,AL1,BE1,DE1)	3HO	1350
	BE3=0.5*(BEMY+BE)	3HO	1360
	BE4=0.5*(BEPY+BE)	3HO	1370
	AL3=0.5*(ALMY+AL)	3HO	1380
	AL4=0.5*(ALPY+AL)	3HO	1390
	GO TO 110	3HO	1400
C		3HO	1410
C	CALCULATE THE CENTERLINE POINT QUANTITIES	3HO	1420
C		3HO	1430
90	UY1=0.5*(U(MP)+U(LMMP)-U(LMN1)+U(LM))*DYR	3HO	1440
	VY1=0.5*(V(MP)+V(LMMP)-V(LMN1)+V(LM))*DYR	3HO	1450
	UY2=0.5*(U(LPMP)+U(MP)-U(LP)-U(LMN1))*DYR	3HO	1460
	VY2=0.5*(V(LPMP)+V(MP)-V(LP)-V(LMN1))*DYR	3HO	1470
	UX3=VX3=UX4=VX4=0.0	3HO	1480
	THEW=ATAN(-NXNYCB(L))	3HO	1490
	THE=ATAN(V(MP)/U(MP))	3HO	1500
	VMAG=SQRT(U(MP)*U(MP)+V(MP)*V(MP))	3HO	1510
	RTHE=2.0*THEW-THE	3HO	1520
	UR=VMAG*COS(RTHE)	3HO	1530
	VR=VMAG*SIN(RTHE)	3HO	1540
	UY3=(U(LMN1)-UR)*DYR	3HO	1550
	VY3=(V(LMN1)-VR)*DYR	3HO	1560
	UY4=(U(MP)-U(LMN1))*DYR	3HO	1570
	VY4=(V(MP)-V(LMN1))*DYR	3HO	1580
	TPY=P(MP)/(RO(MP)*RG)	3HO	1590
	TMP=P(LMMP)/(RO(LMMP)*RG)	3HO	1600
	TPP=P(LPMP)/(RO(LPMP)*RG)	3HO	1610
	TY1=0.0	3HO	1620
	TY2=0.0	3HO	1630
	TX4=0.25*(TPP+TP-TMP-TM)*DXR	3HO	1640

	TX3=TX4	SHO 1650
	TY4=(TPY-T)*DYR	SHO 1660
	TY3=-TY4	SHO 1670
	BE3=BE	SHO 1680
	AL3=AL	SHO 1690
	MDUM=M+1	SHO 1700
	CALL MAP (1,L,MDUM,AL4,BE4,DE,LD1,AL1,BE1,DE1)	SHO 1710
	GO TO 110	SHO 1720
C		SHO 1730
C	CALCULATE THE WALL POINT QUANTITIES	SHO 1740
C		SHO 1750
100	UY1=0.5*(U(LMN1)+U(LM)-U(MM)-U(LMMM))*DYR	SHO 1760
	VY1=0.5*(V(LMN1)+V(LM)-V(MM)-V(LMMM))*DYR	SHO 1770
	UY2=0.5*(U(LP)+U(LMN1)-U(LPMM)-U(MM))*DYR	SHO 1780
	VY2=0.5*(V(LP)+V(LMN1)-V(LPMM)-V(MM))*DYR	SHO 1790
	UX3=VX3=UX4=VX4=0.0	SHO 1800
	UY3=(U(LMN1)-U(MM))*DYR	SHO 1810
	VY3=(V(LMN1)-V(MM))*DYR	SHO 1820
	THEW=ATAN(-NXNY(L))	SHO 1830
	THE=ATAN(V(MM)/U(MM))	SHO 1840
	VMAG=SQRT(U(MM)*U(MM)+V(MM)*V(MM))	SHO 1850
	RTHE=2.0*THEW+THE	SHO 1860
	UR=VMAG*COS(RTHE)	SHO 1870
	VR=VMAG*8IN(RTHE)	SHO 1880
	UY4=(UR-U(LMN1))*DYR	SHO 1890
	VY4=(VR-V(LMN1))*DYR	SHO 1900
	TPM=P(LPMM)/(RO(LPMM)*RG)	SHO 1910
	TMYP=P(MM)/(RO(MM)*RG)	SHO 1920
	TMM=P(LMMM)/(RO(LMMM)*RG)	SHO 1930
	TY1=0.0	SHO 1940
	TY2=0.0	SHO 1950
	TX3=0.25*(TP+TPM-TM+TMM)*DXR	SHO 1960
	TX4=TX3	SHO 1970
	TY3=(T-TMY)*DYR	SHO 1980
	TY4=-TY3	SHO 1990
	MDUM=M+1	SHO 2000
	CALL MAP (1,L,MDUM,AL3,BE3,DE,LD1,AL1,BE1,DE1)	SHO 2010
	BE4=BE	SHO 2020
	AL4=AL	SHO 2030
C		SHO 2040
110	UXY1=UX1+AL1*UY1	SHO 2050
	UXY2=UX2+AL2*UY2	SHO 2060
	UXY3=UX3+AL3*UY3	SHO 2070
	UXY4=UX4+AL4*UY4	SHO 2080
	UXY12=0.5*(UX1+UX2+AL3*UY3+AL4*UY4)	SHO 2090
	VXY1=VX1+AL1*VY1	SHO 2100
	VXY2=VX2+AL2*VY2	SHO 2110
	VXY3=VX3+AL3*VY3	SHO 2120
	VXY4=VX4+AL4*VY4	SHO 2130
	VXY12=0.5*(VX1+VX2+AL3*VY3+AL4*VY4)	SHO 2140
	BUY1=BE1*UY1	SHO 2150
	BUY2=BE2*UY2	SHO 2160
	BUY3=BE3*UY3	SHO 2170
	BUY4=BE4*UY4	SHO 2180
	BUY34=0.5*(BUY3+BUY4)	SHO 2190
	BVY1=BE1*VY1	SHO 2200
	BVY2=BE2*VY2	SHO 2210
	BVY3=BE3*VY3	SHO 2220
	BVY4=BE4*VY4	SHO 2230
	BVY34=0.5*(BVY3+BVY4)	SHO 2240
	TXY1=TX1+AL1*TY1	SHO 2250
	TXY2=TX2+AL2*TY2	SHO 2260
	TXY3=TX3+AL3*TY3	SHO 2270
	TXY4=TX4+AL4*TY4	SHO 2280
C		SHO 2290
C	CALCULATE THE ARTIFICIAL VISCOSITY COEFFICIENTS	SHO 2300
C		SHO 2310
	DIV=UXY12+BYY34	SHO 2320
	VID=VXY12+BUY34	SHO 2330
	RLA=XLA*RDUM*ABS(DIV)/BE	SHO 2340
	RMU=XMU*RDUM*ABS(VID)/BE	SHO 2350
	RK=RMU*GAM1*RG/RKMU	SHO 2360
	RLP2M=RLA+2.0*RMU	SHO 2370
	RLA2=2.0*RLA	SHO 2380
	RMU2=2.0*RMU	SHO 2390
	RLPM=RLA+RMU	SHO 2400
	UETA=0.0	SHO 2410
	VETA=0.0	SHO 2420
	PETA=0.0	SHO 2430
	PCTA=0.0	SHO 2440
	IF (NDIM,EO,0) GO TO 130	SHO 2450

```

C
C
C      CALCULATE THE AXISYMMETRIC TERMS
C
C      IF (M, EQ, 1, AND, YCB(L), EQ, 0, 0) GO TO 120
C      Y=FLOAT(M-1)*DY/BE+YCB(L)
C      VB=V(LMN1)
C      UVT= (RLPM*VXY12+RMU*BUY34)/Y
C      VVT=RLP2M*(BYY34-VB/Y)/Y
C      PVT= (RLP2M*VB*VB/Y+RLA2*VB*(BYY34+UXY12))/Y
C      PCT= RK*0.5*(BE4*TY4+BE3*TY3)/Y
C      DUVT=RLPM*BE*(VXY4-VXY3)*DYR+RMU*BE*(BUY4-BUY3)*DYR
C      DVVT=RLP2M*0.5*BE*(BYY4-BYY3)*DYR
C      DPVT= (RLP2M+RLA2)*BYY34*BYY34+RLA2*BYY34*UXY12
C      DPCT= RK*BE*(BE4*TY4+BE3*TY3)*DYR
C      IF (ABS(UVT), GT, ABS(DUVT)) UVT=DUVT
C      IF (ABS(VVT), GT, ABS(DVVT)) VVT=DVVT
C      IF (ABS(PVT), GT, ABS(DPVT)) PVT=DPVT
C      IF (ABS(PCT), GT, ABS(DPCT)) PCT=DPCT
C      GO TO 130
120  UVT=RLPM*BE*(VXY4-VXY3)*DYR+RMU*BE*(BUY4-BUY3)*DYR
C      VVT=RLP2M*0.5*BE*(BYY4-BYY3)*DYR
C      PVT= (RLP2M+RLA2)*BYY34*BYY34+RLA2*BYY34*UXY12
C      PCT= RK*BE*(BE4*TY4+BE3*TY3)*DYR
C
C      CALCULATE THE ARTIFICIAL VISCOSITY TERMS
C
C
130  OUT(L, M)= (RLP2M*(UXY2-UXY1)+RLA*(BYY2-BYY1))*DXR+AL*(RLP2M*(UXY4-UXY3)+RLA*(BYY4-BYY3))*DYR+RMU*BE*(VXY4+BUY4-VXY3-BUY3)*DYR+UVT
C      OUT(L, M)=RMU*(VXY2+BUY2-VXY1-BUY1)*DXR+RMU*AL*(VXY4+BUY4-VXY3-BUY3)*DYR+VVT
C      )+DYR*BE*(RLA*(UXY4-UXY3)+RLP2M*(BYY4-BYY3))*DYR+VVT
C      OPT(L, M)=RO(LMN1)*(GAMMA=1, 0)*(RLP2M*(UXY12+UXY12+BYY34+BYY34)+RMU*0
C      1*(VXY12+VXY12+BUY34+BUY34)+RLA2*UXY12+BYY34+RMU2*BUY34+VXY12+RK*(
C      2*XY2-XY1)*DXR+AL*(TXY4-TXY3)*DYR+BE*(BE4*TY4+BE3*TY3)*DYR)+PVT+PSHO
C      3CTA)
C      OUT(L, M)=CTA*OUT(L, M)+CTA1*OOUT
C      OVT(L, M)=CTA*OVT(L, M)+CTA1*OOVT
C      OPT(L, M)=CTA*OPT(L, M)+CTA1*OOPT
C
C
C      PRINT THE ARTIFICIAL VISCOSITY TERMS
C
C
C      IF (NC, NE, NPRINT) GO TO 150
C      NLINE=NLINE+1
C      IF (NLINE, LT, 55) GO TO 140
C      PRINT 200
C      PRINT 100, N, PC
C      NLINE=1
140  OPT(L, M)=OPT(L, M)/PC
C      PRINT 100, L, M, OUT(L, M), OVT(L, M), OPT(L, M)
C      OPT(L, M)=OPT(L, M)*PC
150  CONTINUE
C      IF (NC, EQ, NPRINT) NC=0
C      RETURN
C
C      SMOOTH THE FLOW VARIABLES IF REQUESTED
C
C
160  IF (SMP, LT, 0, 0, OR, SMP, GE, 1, 0) RETURN
C      SMP4=.25*(1, 0=SMP)
C      DO 170 L=2, L1
C      U(L, MMAX, N3)=SMP4*(U(L-1, MMAX, N3)+U(L+1, MMAX, N3)+2, 0*U(L, M1, N3))+SSHO
C      1MP*U(L, MMAX, N3)
C      V(L, MMAX, N3)=U(L, MMAX, N3)*NXNY(L)
C      P(L, MMAX, N3)=SMP4*(P(L-1, MMAX, N3)+P(L+1, MMAX, N3)+2, 0*P(L, M1, N3))+SSHO
C      1MP*P(L, MMAX, N3)
C      RO(L, MMAX, N3)=SMP4*(RO(L-1, MMAX, N3)+RO(L+1, MMAX, N3)+2, 0*RO(L, M1, N3))+SSHO
C      1)+SMP*RO(L, MMAX, N3)
C      U(L, 1, N3)=SMP4*(U(L-1, 1, N3)+U(L+1, 1, N3)+2, 0*U(L, 2, N3))+SMP*U(L, 1, N3)
C      13)
C      V(L, 1, N3)=U(L, 1, N3)*NXNYCB(L)
C      P(L, 1, N3)=SMP4*(P(L-1, 1, N3)+P(L+1, 1, N3)+2, 0*P(L, 2, N3))+SMP*P(L, 1, N3)
C      13)
C      RO(L, 1, N3)=SMP4*(RO(L-1, 1, N3)+RO(L+1, 1, N3)+2, 0*RO(L, 2, N3))+SMP*RO(L, 1, N3)
C      1L, 1, N3)
C      DO 170 M=2, M1
C      LMD2=L0*(M-1)+LMD3
C      LMD2=L0*(M-2)+LMD3
C      LMD2=L0*M+LMD3
C      LMN3=L+LMD2
C      LP=L+1+LMD2
C      LM=L+1+LMD2
C      MP=L+LMD2
C      MM=L+LMD2
C      U(LMN3)=SMP4*(U(LM)+U(LP)+U(MM)+U(MP))+SMP*U(LMN3)
C      V(LMN3)=SMP4*(V(LM)+V(LP)+V(MM)+V(MP))+SMP*V(LMN3)

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	P(LMN3)=SMP4*(P(LH)+P(LP)+P(HH)+P(HP))+SMP*P(LMN3)	8MO 3290
	RO(LMN3)=SMP4*(RO(LH)+RO(LP)+RO(HH)+RO(HP))+SMP*RO(LMN3)	8MO 3300
170	CONTINUE	8MO 3310
	RETURN	8MO 3320
C		8MO 3330
180	FORMAT (1H,5X,2I5,3F14,4)	8MO 3340
190	FORMAT (1H,63HLOCAL ARTIFICIAL VISCOSITY PARAMETERS FOR SHOCK CALC8MO 3350	
	ULATION8, N=14,5H (PC=,F5,1,1H),//,10X,1HL,4X,1HM,10X,3HQUT,11X,3H8MO 3360	
	2QVT,11X,3HQPT,/) 8MO 3370	
200	FORMAT (1H1)	8MO 3380
	END	8MO 3390

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SUBROUTINE INTER
C
C *****
C THIS SUBROUTINE CALCULATES THE INTERIOR MESH POINTS
C *****
C
COMMON /AV/ IAV,CAV,NST,SNP,LSS,CTA,XMU,XLA,RKMU,OUT(81,21),QVT(81,21),QPT(81,21)
COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)
COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RO(81,21,2)
COMMON /CNTRLC/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAM1,GAINT
1M2,L1,L2,L3,M1,M2,DX,DY,DT,N,N1,N3,NASH,IYEL,ICHAR,NID,LJET,JFLAG,INT
2IERR,IUI,IUD,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TCINT
3,LC,PLOW,ROLOW
COMMON /GEMTRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCT,ANGI,ANGE,XH(81),INT
1YH(81),XHI(81),YHI(81),NXNY(81),NWPTS,IINT,IDIF,LT,NDIM
COMMON /GCB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,RECB,RCICB,RCYCB,ANGICB,INT
1,ANGECB,XCB(81),YCB(81),XCB1(81),YCB1(81),NXNYCB(81),NCBPTS,IINTCB,INT
2,IDIFCB,LECB
COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASST,THRUST,NINT
1STAG
REAL MN3,NXNY,MASST,MASST,NXNYCB,MASSE
C
C ATERM=0.0
C IF (ICHAR,EQ,2) GO TO 40
C
C COMPUTE THE TENTATIVE SOLUTION AT T+DT
C
MDUM=1
IF (NGCB,NE,0) MDUM=2
DO 30 L=2,LMAX
DO 30 M=MDUM,M1
CALL MAP (1,L,M,AL,BE,DE,LD1,AL1,BE1,DE1)
LMD2=LD*(M-1)
LMN1=L+LMD2+LMD1
LMN3=L+LMD2+LMD3
L1MN1=L-1+LMD2+LMD1
LM1N1=L+LD*(M-2)+LMD1
UB=U(LMN1)
VB=V(LMN1)
PB=P(LMN1)
ROB=RO(LMN1)
ASB=GAMMA*PB/ROB
IF (M,NE,1) GO TO 10
DUDX=(UB-U(L1MN1))*DXR
DPDX=(PB-P(L1MN1))*DXR
DRODX=(ROB-RO(L1MN1))*DXR
DVDY=(4.0*V(L,2,N1)-V(L,3,N1))*0.5*DYR
V(LMN3)=0.0
C
URHS=UB*DUDX+DPDX/ROB
RORHS=-UB*DRODX+ROB*DUDX-(1+NDIM)*ROB*BE+DVDY
PRHS=-UB*DPDX+ASB*(RORHS+UB*DRODX)
GO TO 20
10 IF (NDIM,EQ,1) ATERM=ROB*VB/((M-1)*DY/BE+YCB(L))
UVB=UB*AL+VB*BE+DE
DUDX=(UB-U(L1MN1))*DXR
DVDX=(VB-V(L1MN1))*DXR
DPDX=(PB-P(L1MN1))*DXR
DRODX=(ROB-RO(L1MN1))*DXR
DUDY=(UB-U(LMN1))*DYR
DVDY=(VB-V(LMN1))*DYR
DPDY=(PB-P(LMN1))*DYR
DRODY=(ROB-RO(LMN1))*DYR
C
URHS=-UB*DUDX+UVB*DUDY-(DPDX+AL*DPDY)/ROB
VRHS=-UB*DVDX+UVB*DVDY-BE*DPDY/ROB
RORHS=-UB*DRODX+UVB*DRODY-ROB*(DUDX+AL*DUDY+RE+DVDY)=ATERM
PRHS=-UB*DPDX+UVB*DPDY+ASB*(RORHS+UB*DRODX+UVB*DRODY)
V(LMN3)=V(LMN1)+VRHS*DT
20 U(LMN3)=U(LMN1)+URHS*DT
P(LMN3)=P(LMN1)+PRHS*DT
RO(LMN3)=RO(LMN1)+RORHS*DT
IF (P(LMN3),LE,0.0) P(LMN3)=PLOW*PC
IF (RO(LMN3),LE,0.0) RO(LMN3)=ROLOW/G
30 CONTINUE
RETURN
C
C COMPUTE THE FINAL SOLUTION AT T+DT
C

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40	MDUM=1	INT 830
	IF (NGCB,NE,0) MDUM=2	INT 840
	DO 70 L=2,L1	INT 850
	DO 70 M=MDUM,M1	INT 860
	CALL MAP (1,L,M,AL,BE,DE,LD1,AL1,BE1,DE1)	INT 870
	LMD2=LD*(M=1)	INT 880
	LMN1=L+LMD2+LMD1	INT 890
	LMN3=L+LMD2+LMD3	INT 900
	L1MN3=L+1+LMD2+LMD3	INT 910
	LM1N3=L+LD*M+LMD3	INT 920
	UB=U(LMN3)	INT 930
	VB=V(LMN3)	INT 940
	PB=P(LMN3)	INT 950
	ROB=RO(LMN3)	INT 960
	ASB=GAMMA*PB/ROB	INT 970
	IF (M,NE,1) GO TO 50	INT 980
	DUDX=(U(L1MN3)-UB)*DXR	INT 990
	OPDX=(P(L1MN3)-PB)*DXR	INT 1000
	DRODX=(RO(L1MN3)-ROB)*DXR	INT 1010
	DVDY=(4,0*V(L,2,N3)-V(L,3,N3))*0.5*DYR	INT 1020
	V(LMN3)=0,0	INT 1030
C	URHS=-UB*DUDX+OPDX/ROB	INT 1040
	RORHS=-UB*DRODX-ROB*DUDX-(1+NDIM)*ROB*BE*DVDY	INT 1050
	PRHS=-UB*OPDX+ASB*(RORHS+UB*DRODX)	INT 1060
	GO TO 60	INT 1070
50	IF (NDIM,EQ,1) ATERM=ROB*VB/((M=1)*DY/BE+YCB(L))	INT 1080
	UVB=UB*AL+VB*BE+DE	INT 1090
	DUDX=(U(L1MN3)-UB)*DXR	INT 1100
	DYDX=(V(L1MN3)-VB)*DXR	INT 1110
	DPDX=(P(L1MN3)-PB)*DXR	INT 1120
	DRODX=(RO(L1MN3)-ROB)*DXR	INT 1130
	DUDY=(U(LM1N3)-UB)*DYR	INT 1140
	DYDY=(V(LM1N3)-VB)*DYR	INT 1150
	DPDY=(P(LM1N3)-PB)*DYR	INT 1160
	DRODY=(RO(LM1N3)-ROB)*DYR	INT 1170
C	URHS=-UB*DUDX-UVB*DUDY-(DPDX+AL*DPDY)/ROB	INT 1180
	VRHS=-UB*DYDX-UVB*DYDY-BE*DPDY/ROB	INT 1190
	RORHS=-UB*DRODX-UVB*DRODY-ROB*(DUDX+AL*DUDY+BE*DVDY)+ATERM	INT 1200
	PRHS=-UB*DPDX-UVB*DPDY+ASB*(RORHS+UB*DRODX+UVB*DRODY)	INT 1210
	V(LMN3)=(V(LMN1)+V(LMN3)+VRHS*DT)*0.5	INT 1220
60	U(LMN3)=(U(LMN1)+U(LMN3)+URHS*DT)*0.5	INT 1230
	P(LMN3)=(P(LMN1)+P(LMN3)+PRHS*DT)*0.5	INT 1240
	RO(LMN3)=(RO(LMN1)+RO(LMN3)+RORHS*DT)*0.5	INT 1250
	IF (P(LMN3),LE,0,0) P(LMN3)=PLOW*PC	INT 1260
	IF (RO(LMN3),LE,0,0) RO(LMN3)=ROLOW/G	INT 1270
	IF (IAV,EQ,0) GO TO 70	INT 1280
C		INT 1290
C	ADD THE ARTIFICIAL VISCOSITY FOR SHOCK CALCULATIONS	INT 1300
C		INT 1310
	U(LMN3)=U(LMN3)+QUT(L,M)	INT 1320
	V(LMN3)=V(LMN3)+QVT(L,M)	INT 1330
	IF (M,EQ,1) V(LMN3)=0,0	INT 1340
	P(LMN3)=P(LMN3)+QPT(L,M)	INT 1350
70	CONTINUE	INT 1360
	RETURN	INT 1370
	END	INT 1380
		INT 1390
		INT 1400

```

SUBROUTINE WALL
C
C *****
C
C THIS SUBROUTINE CALCULATES THE BOUNDARY MESH POINTS AT THE NOZZLE
C WALL, EXHAUST JET BOUNDARY, AND CENTERBODY
C *****
C
COMMON /AV/ IAV,CAV,NST,SMP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81,21),QPT(81,21)
COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)
COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RO(81,21,2)
COMMON /CNTRLC/ LMAX,MMAX,NMAX,NPRINT,TCONV,PDT,GAMMA,RGAS,GAM1,GAMWAL
1M2,L1,L2,L3,M1,M2,DX,DY,DT,N,N1,N3,NA8M,IVEL,ICHR,N1D,LJET,JFLAG,WAL
2IERR,IUI,IUO,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TCWAL
3,LC,PLOW,HOLDH
COMMON /GEMTRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCT,ANGI,ANGE,XW(81),
1YW(81),XWI(81),YWI(81),NXNY(81),NWPIS,IINT,IDIF,LT,NDIM
COMMON /GCB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,RECB,RCICB,RCTCB,ANGICBWAL
1,ANGECB,XCB(81),YCB(81),XCB1(81),YCB1(81),NXNYCB(81),NCBPTS,IINTCBWAL
2,IDIFCB,LECB
COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASSI,MASST,THRUST,NWAL
1STAG
REAL MN3,NXNY,MASSI,MASST,NXNYCB,MASSE
C
IF (N,EQ,1) DELY=0.005
XWID=0.0
IF (IB,EQ,1) GO TO 10
Y1=0.0 3 Y3=0.0 3 MDUM=1 3 MDUM1=2 3 SIGN=-1.0
GO TO 20
10 Y1=1.0 3 Y3=1.0 3 MDUM=MMAX 3 MDUM1=M1 3 SIGN=1.0
20 ATERM2=0.0
ATERM3=0.0
LDUM=LMAX
IF (ICHR,EQ,2) LDUM=L1
LMDM=LD*(MDUM-1)
LMDM1=LD*(MDUM1-1)
DYS=SIGN*DYR
DO 350 L=2,LDUM
LMN1=L+LMDM+LMD1
LMN3=L+LMDM+LMD3
LM1N1=L+LMDM1+LMD1
L1MN1=L-1+LMDM+LMD1
L1MN3=L-1+LMDM+LMD3
L1M1N1=L-1+LMDM1+LMD1
IF (JFLAG,EQ,0) GO TO 50
IF (IB,EQ,2) GO TO 50
C
XWID=XWI(L)
IF (ICHR,EQ,1) GO TO 30
C
C USE THE DUMMY ARRAYS TO MANIPULATE THE ONE-SIDED SOLUTIONS
C
IF (L,NE,LJET=2) GO TO 30
U(L,MN3)=UD(3)
V(L,MN3)=VD(3)
P(L,MN3)=PD(3)
RO(L,MN3)=ROD(3)
GO TO 50
30 IF (L,NE,LJET=1) GO TO 40
IF (ICHR,EQ,1) UOLD=U(LMN1)
U(LMN1)=UD(1)
V(LMN1)=VD(1)
P(LMN1)=PD(1)
RO(LMN1)=ROD(1)
GO TO 50
40 IF (L,NE,LJET) GO TO 50
U(L1MN1)=UD(2)
V(L1MN1)=VD(2)
P(L1MN1)=PD(2)
RO(L1MN1)=ROD(2)
C
50 U1=U(LMN1)
V1=V(LMN1)
P1=P(LMN1)
RO1=RO(LMN1)
U2=U1
V2=V1
A1=SQRT(GAMMA*P1/RO1)
A2=A1
IF (ICHR,EQ,2) GO TO 60
WAL 10
WAL 20
WAL 30
WAL 40
WAL 50
WAL 60
WAL 70
WAL 80
WAL 90
WAL 100
WAL 110
WAL 120
WAL 130
WAL 140
WAL 150
WAL 160
WAL 170
WAL 180
WAL 190
WAL 200
WAL 210
WAL 220
WAL 230
WAL 240
WAL 250
WAL 260
WAL 270
WAL 280
WAL 290
WAL 300
WAL 310
WAL 320
WAL 330
WAL 340
WAL 350
WAL 360
WAL 370
WAL 380
WAL 390
WAL 400
WAL 410
WAL 420
WAL 430
WAL 440
WAL 450
WAL 460
WAL 470
WAL 480
WAL 490
WAL 500
WAL 510
WAL 520
WAL 530
WAL 540
WAL 550
WAL 560
WAL 570
WAL 580
WAL 590
WAL 600
WAL 610
WAL 620
WAL 630
WAL 640
WAL 650
WAL 660
WAL 670
WAL 680
WAL 690
WAL 700
WAL 710
WAL 720
WAL 730
WAL 740
WAL 750
WAL 760
WAL 770
WAL 780
WAL 790
WAL 800
WAL 810
WAL 820

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	U3=U1	HAL	830
	V3=V1	HAL	840
	P3=P1	HAL	850
	R03=R01	HAL	860
	A3=A1	HAL	870
	GO TO 70	HAL	880
60	U3=U(LMN3)	HAL	890
	V3=V(LMN3)	HAL	900
	P3=P(LMN3)	HAL	910
	R03=R0(LMN3)	HAL	920
	A3=SQRT(GAMMA*P3/R03)	HAL	930
C		HAL	940
C	CALCULATE THE PROPERTY INTERPOLATING POLYNOMIAL COEFFICIENTS	HAL	950
C		HAL	960
70	BU=(U1-U(LM1N1))*DYS	HAL	970
	BV=(V1-V(LM1N1))*DYS	HAL	980
	BP=(P1-P(LM1N1))*DYS	HAL	990
	BRO=(R01-R0(LM1N1))*DYS	HAL	1000
	CU=U1-BU*Y3	HAL	1010
	CV=V1-BV*Y3	HAL	1020
	CP=P1-BP*Y3	HAL	1030
	CRO=R01-BRO*Y3	HAL	1040
C		HAL	1050
C	CALCULATE THE CROSS DERIVATIVE INTERPOLATING POLYNOMIAL	HAL	1060
C	COEFFICIENTS	HAL	1070
C		HAL	1080
	DU=(U1-U(L1MN1))*DXR	HAL	1090
	DV=(V1-V(L1MN1))*DXR	HAL	1100
	DP=(P1-P(L1MN1))*DXR	HAL	1110
	DRO=(R01-R0(L1MN1))*DXR	HAL	1120
	DU1=(U(LM1N1)-U(L1M1N1))*DXR	HAL	1130
	DV1=(V(LM1N1)-V(L1M1N1))*DXR	HAL	1140
	DP1=(P(LM1N1)-P(L1M1N1))*DXR	HAL	1150
	DRO1=(R0(LM1N1)-R0(L1M1N1))*DXR	HAL	1160
	BDU=(DU-DU1)*DYS	HAL	1170
	BDV=(DV-DV1)*DYS	HAL	1180
	BDP=(DP-DP1)*DYS	HAL	1190
	BDRO=(DRO-DRO1)*DYS	HAL	1200
	CDU=DU-BDU*Y3	HAL	1210
	CDV=DV-BDV*Y3	HAL	1220
	CDP=DP-BDP*Y3	HAL	1230
	CDRO=DRO-BDRO*Y3	HAL	1240
C		HAL	1250
C	CALCULATE Y2	HAL	1260
C		HAL	1270
	CALL MAP (1,L,MDUM,AL,BE,DE,LD1,AL1,BE1,DE1)	HAL	1280
	AL9=SQRT(AL*AL+BE*BE)	HAL	1290
	UV3=U3*AL+V3*BE+DE	HAL	1300
	AL2=AL	HAL	1310
	DO 90 ILL=1,3	HAL	1320
	UV2=U2*AL2+V2*BE+DE	HAL	1330
	Y2=Y3=(UV2+SIGN*AL9*A2+UV3+SIGN*AL9*A3)*DT*0.5	HAL	1340
C		HAL	1350
C	INTERPOLATE FOR THE PROPERTIES	HAL	1360
C		HAL	1370
	U2=BU*Y2+CU	HAL	1380
	V2=BV*Y2+CV	HAL	1390
	P2=BP*Y2+CP	HAL	1400
	R02=BRO*Y2+CRO	HAL	1410
	AL2=Y2*AL	HAL	1420
	AD=GAMMA*P2/R02	HAL	1430
	IF (AD,GT,0.0) GO TO 80	HAL	1440
	PRINT 360, N,L,MDUM	HAL	1450
	IERR=1	HAL	1460
	RETURN	HAL	1470
80	A2=SQRT(AD)	HAL	1480
90	CONTINUE	HAL	1490
C		HAL	1500
C	INTERPOLATE FOR THE CROSS DERIVATIVES	HAL	1510
C		HAL	1520
	DU1=DU	HAL	1530
	DV1=DV	HAL	1540
	DP1=DP	HAL	1550
	DRO1=DRO	HAL	1560
	DU2=BDU*Y2+CDU	HAL	1570
	DV2=BDV*Y2+CDV	HAL	1580
	DP2=BDP*Y2+CDP	HAL	1590
	DRO2=BDRO*Y2+CDRO	HAL	1600
C		HAL	1610
C	CALCULATE THE PSI TERMS	HAL	1620
C		HAL	1630
	IF (NDIM,EG,0) GO TO 110	HAL	1640

	IF (IB,EQ,2) GO TO 100	WAL 1650
	ATERM2=RO2*V2/(YCB(L)+Y2/BE)	WAL 1660
	GO TO 110	WAL 1670
100	ATERM2=RO2*V2/(YCB(L)+Y2/BE)	WAL 1680
	IF (IAV,EQ,0) GO TO 110	WAL 1690
	ATDS=RO2*V(L,2,N1)*DYR*BE	WAL 1700
	IF (ABS(ATERM2),GT,ARS(ATDS)) ATERM2=ATDS	WAL 1710
C		WAL 1720
110	PSI21=U1*DU1-DP1/RO1	WAL 1730
	PSI31=U1*DV1	WAL 1740
	PSI41=U1*DP1+A1*A1*U1*DR01	WAL 1750
	PSI12=U2*DH02-RO2*DU2-ATERM2	WAL 1760
	PSI22=U2*DU2-DP2/RO2	WAL 1770
	PSI32=U2*DV2	WAL 1780
	PSI42=U2*DP2+A2*A2*U2*DR02	WAL 1790
	IF (ICHR,EQ,1) GO TO 150	WAL 1800
C		WAL 1810
C	CALCULATE THE CROSS DERIVATIVES AT THE SOLUTION POINT	WAL 1820
C		WAL 1830
	IF (JFLAG,EQ,0) GO TO 120	WAL 1840
	IF (IB,EQ,2) GO TO 120	WAL 1850
	IF (L,EQ,2) GO TO 120	WAL 1860
	IF (L,NE,LJET=1) GO TO 120	WAL 1870
	IF (ILJET,EQ,2) GO TO 120	WAL 1880
	GO TO 130	WAL 1890
120	DU3=(U(L1MN3)-U3)*DXR	WAL 1900
	DV3=(V(L1MN3)-V3)*DXR	WAL 1910
	DP3=(P(L1MN3)-P3)*DXR	WAL 1920
	DR03=(RO(L1MN3)-RO3)*DXR	WAL 1930
	GO TO 140	WAL 1940
130	DU3=(U3-U(L=1,MDUM,N3))*DXR	WAL 1950
	DV3=(V3-V(L=1,MDUM,N3))*DXR	WAL 1960
	DP3=(P3-P(L=1,MDUM,N3))*DXR	WAL 1970
	DR03=(RO3-RO(L=1,MDUM,N3))*DXR	WAL 1980
C		WAL 1990
C	ENTER THE EXHAUST JET ITERATION LOOP	WAL 2000
C		WAL 2010
140	IF (JFLAG,EQ,0) GO TO 150	WAL 2020
	IF (IB,EQ,2) GO TO 150	WAL 2030
	IF (L,LT,LJET) GO TO 150	WAL 2040
	YW(L)=YW(L)	WAL 2050
	UDUM=U(LMN3)	WAL 2060
	VDUM=V(LMN3)	WAL 2070
	PDUM=P(LMN3)	WAL 2080
	RODUM=RO(LMN3)	WAL 2090
150	DO 200 NJ=1,10	WAL 2100
	IF (ICHR,EQ,1) GO TO 250	WAL 2110
	IF (JFLAG,EQ,0) GO TO 210	WAL 2120
	IF (IB,EQ,2) GO TO 210	WAL 2130
	IF (L,LT,LJET) GO TO 210	WAL 2140
	IF (NJ,EQ,1) GO TO 200	WAL 2150
	IF (NJ,GT,2) GO TO 180	WAL 2160
160	YWOLD=YW(L)	WAL 2170
	POLD=P(LMN3)	WAL 2180
	IF (P(LMN3),LT,PE) GO TO 170	WAL 2190
	YW(L)=YW(L)+DELY	WAL 2200
	GO TO 190	WAL 2210
170	YW(L)=YW(L)-DELY	WAL 2220
	GO TO 190	WAL 2230
180	IF (P(LMN3),EQ,POLD) GO TO 160	WAL 2240
	DYDP=(YW(L)-YWOLD)/(P(LMN3)-POLD)	WAL 2250
	YWNEW=YW(L)+DYDP*(PE-P(LMN3))	WAL 2260
	YWOLD=YW(L)	WAL 2270
	POLD=P(LMN3)	WAL 2280
	YW(L)=YWNEW	WAL 2290
190	IF (YW(L),LT,(0.98*YWOLD)) YW(L)=0.98*YWOLD	WAL 2300
	IF (YW(L),GT,(1.02*YWOLD)) YW(L)=1.02*YWOLD	WAL 2310
200	NXNY(L)=(YW(L)-YW(L-1))*DXR	WAL 2320
	XWI(L)=(YW(L)-YWI(L))/DT	WAL 2330
	XWID=XWI(L)	WAL 2340
	CALL MAP (1,L,MMAX,AL,BE,DE,LD1,AL1,BE1,DE1)	WAL 2350
	ALS=SQRT(AL*AL+BE*BE)	WAL 2360
	U(LMN3)=UDUM	WAL 2370
	V(LMN3)=VDUM	WAL 2380
	P(LMN3)=PDUM	WAL 2390
	RO(LMN3)=RODUM	WAL 2400
C		WAL 2410
C	CALCULATE THE PSI TERMS AT THE SOLUTION POINT	WAL 2420
C		WAL 2430
210	IF (NDIM,EQ,0) GO TO 240	WAL 2440
	IF (IB,EQ,2) GO TO 220	WAL 2450
	ATERM3=RO3*V3/(YCB(L)+1.0/BE)	WAL 2460
	GO TO 240	WAL 2470

220	IF (YCB(L),EQ,0,0) GO TO 230	WAL 2480
	ATERM3=RO3*V3/YCB(L)	WAL 2490
	IF (JAV,EQ,0) GO TO 240	WAL 2500
	ATDS=RO3*V(L,2,N3)*DYR*BE	WAL 2510
	IF (ABS(ATERM3),GT,ABS(ATDS)) ATERM3=ATDS	WAL 2520
	GO TO 240	WAL 2530
230	ATERM3=RO3*V(L,2,N3)*DYR*BE	WAL 2540
C		WAL 2550
240	PSI13=-U3*DR03+RO3*DU3-ATERM3	WAL 2560
	PSI23=-U3*DU3-DP3/RO3	WAL 2570
	PSI33=-U3*DV3	WAL 2580
	PSI43=-U3*DP3+A3*A3*U3*DR03	WAL 2590
C		WAL 2600
C	CALCULATE THE COMPATIBILITY EQUATION COEFFICIENTS	WAL 2610
C		WAL 2620
250	ABR=NXNY(L)	WAL 2630
	IF (I8,EQ,2) ABR=NXNYCB(L)	WAL 2640
	ALB=0,5*(AL2+AL)/ALS	WAL 2650
	BEB=BE/ALS	WAL 2660
	A1B=(A1+A3)*0,5	WAL 2670
	A2B=(A2+A3)*0,5	WAL 2680
	RO1B=(RO1+RO3)*0,5	WAL 2690
	RO2B=(RO2+RO3)*0,5	WAL 2700
	IF (ICHR,EQ,1) GO TO 260	WAL 2710
	PSI21B=(PSI21+PSI23)*0,5	WAL 2720
	PSI31B=(PSI31+PSI33)*0,5	WAL 2730
	PSI41B=(PSI41+PSI43)*0,5	WAL 2740
	PSI12B=(PSI12+PSI13)*0,5	WAL 2750
	PSI22B=(PSI22+PSI23)*0,5	WAL 2760
	PSI32B=(PSI32+PSI33)*0,5	WAL 2770
	PSI42B=(PSI42+PSI43)*0,5	WAL 2780
	GO TO 270	WAL 2790
260	PSI21B=PSI21	WAL 2800
	PSI31B=PSI31	WAL 2810
	PSI41B=PSI41	WAL 2820
	PSI12B=PSI12	WAL 2830
	PSI22B=PSI22	WAL 2840
	PSI32B=PSI32	WAL 2850
	PSI42B=PSI42	WAL 2860
C		WAL 2870
C	SOLVE THE COMPATIBILITY EQUATIONS FOR U,V,P, AND RO	WAL 2880
C		WAL 2890
270	U(LMN3)=(U(LMN1)-ABR*(V(LMN1)-XWID)+(PSI21B-ABR*PSI31B)*DT)/(1,0+ABR)	WAL 2900
	1BR*ABR)	WAL 2910
	V(LMN3)=U(LMN3)+ABR*XWID	WAL 2920
	P(LMN3)=P2-SIGN*RO2B*A2B*(ALB*(U(LMN3)-U2)+BEB*(V(LMN3)-V2))+(PSI41B-ABR*PSI42B)*DT	WAL 2930
	12B*A2B*A2B*PSI12B+SIGN*RO2B*A2B*(ALB*PSI22B+BEB*PSI32B)*DT	WAL 2940
	IF (P(LMN3),LE,0,0) P(LMN3)=PLOW*PC	WAL 2950
	RO(LMN3)=RO(LMN1)+(P(LMN3)-P(LMN1)-PSI41B*DT)/(A1B*A1B)	WAL 2960
	IF (RO(LMN3),LE,0,0) RO(LMN3)=ROLOW/G	WAL 2970
	IF (JAV,EQ,0) GO TO 280	WAL 2980
C		WAL 2990
C	ADD THE ARTIFICIAL VISCOSITY FOR SHOCK CALCULATIONS	WAL 3000
C		WAL 3010
	IF (ICHR,EQ,1) GO TO 280	WAL 3020
	U(LMN3)=U(LMN3)+(QUT(L,MDUM)+ABR*QVT(L,MDUM))/(1,0+ABR*ABR)	WAL 3030
	V(LMN3)=U(LMN3)*ABR	WAL 3040
	P(LMN3)=P(LMN3)+QPT(L,MDUM)	WAL 3050
C		WAL 3060
280	IF (JFLAG,EQ,0) GO TO 350	WAL 3070
	IF (I8,EQ,2) GO TO 350	WAL 3080
	IF (L,LT,LJET=1) GO TO 350	WAL 3090
	IF (L,EQ,LJET=1) GO TO 300	WAL 3100
	IF (ICHR,EQ,1) GO TO 350	WAL 3110
	DELP=ABS((P(LMN3)-PE)/PE)	WAL 3120
	IF (DELP,LE,0,001) GO TO 350	WAL 3130
290	CONTINUE	WAL 3140
	GO TO 350	WAL 3150
C		WAL 3160
C	SOLVE THE COMPATIBILITY EQUATIONS FOR THE DOWNSTREAM SIDE OF THE	WAL 3170
C	NOZZLE WALL EXIT POINT	WAL 3180
C		WAL 3190
300	UD(3)=U(LMN3)	WAL 3200
	VD(3)=V(LMN3)	WAL 3210
	PD(3)=P(LMN3)	WAL 3220
	ROD(3)=RO(LMN3)	WAL 3230
	PD(4)=PE	WAL 3240
	XH1=SQRT((UD(3)*UD(3)+VD(3)*VD(3))/(GAMMA*PD(3)/ROD(3)))	WAL 3250
	DUMD=1,0+GAM2*XH1*XH1	WAL 3260
	TD=PD(3)/ROD(3)/RGAS/G	WAL 3270
	TTD=TD*DUMD	WAL 3280
	IF (PE,GT,PD(3),AND,XH1,GE,1,0) GO TO 310	WAL 3290
	TTD=TD*DUMD	WAL 3300

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      IF (PE,GT,PD(3),AND,XM1,GE,1,0) GO TO 310
      PTD=PD(3)*DUMD**GAM1
      ROD(4)=ROD(3)*(PE/PD(3))** (1,0/GAMMA)
      GO TO 320
310  PRD=PE/PD(3)
      GAMD=(GAMMA+1,0)/(GAMMA-1,0)
      ROD(4)=ROD(3)*(GAMD*PRD+1,0)/(PRD+GAMD)
320  TE=PE/ROD(4)/RGAS/G
      XMACH=SQRT((TTD/TE+1,0)/GAM2)
      SS=SQRT(GAMMA*PE/ROD(4))
      VMAG=XMACH*SS
      UD(4)=VMAG/SQRT(1,0+NXNY(LJET)*NXNY(LJET))
      VD(4)=UD(4)*NXNY(LJET)
C
C      AVERAGE THE J-SIDED MACH NOS FOR THE INTERIOR POINT CALCULATIONS
C
      XM2=SQRT((UD(4)*UD(4)+VD(4)*VD(4))/(GAMMA*PD(4)/ROD(4)))
      IF (XM1,GE,1,0) GO TO 350
      XMB=(XM1+XM2)/2,0
      IF (XMB,GE,1,0) GO TO 330
      DPL=1,0
      DPR=1,0
      GO TO 340
330  DPL=XM2+1,0
      DPR=1,0-XM1
      XMB=1,0
340  DPLR=DPR+DPL
      DUM=1,0+GAM2*XMB*XMB
      TEMP=TTD/DUM
      P(LMN3)=PTD/DUM**GAM1
      RO(LMN3)=P(LMN3)/(RGAS*TEMP*G)
      QA=SQRT(2,0*GAM1*(RGAS*TTD*G-P(LMN3)/RO(LMN3)))
      DNXY=(DPR*NXNY(LJET)+DPL*NXNY(L))/DPLR
      U(LMN3)=QA/SQRT(1,0+DNXY*DNXY)
      V(LMN3)=-U(LMN3)*DNXY
      IF (ICAR,EQ,1) GO TO 350
      UD(1)=UD(3)
      VD(1)=VD(3)
      PD(1)=PD(3)
      ROD(1)=ROD(3)
      UD(2)=UD(4)
      VD(2)=VD(4)
      PD(2)=PD(4)
      ROD(2)=ROD(4)
350  CONTINUE
      IF (JFLAG,EQ,0) RETURN
      IF (IB,EQ,2) RETURN
      IF (ICAR,EQ,1) RETURN
      U(LJET-1,MMAX,N1)=UOLD
      YH(LMAX)=YH(LMAX)
      YH(LMAX)=2,0*YH(L1)-YH(L2)
      NXNY(LMAX)=- (YH(LMAX)-YH(L1))*DXR
      XH(LMAX)=(YH(LMAX)-YH(LMAX))/DT
      DELY=ABS(YH(LJET)-YH(LJET))
      IF (DELY,EQ,0,0) DELY=0,0001
      RETURN
C
360  FORMAT (1H0,61H***** A NEGATIVE SQUARE ROOT OCCURED IN SUBROUTINE
1WALL AT N=,I4,4H, L=,I2,8H, AND M=,I2,6H ***** )
      END

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WAL 3310
WAL 3320
WAL 3330
WAL 3340
WAL 3350
WAL 3360
WAL 3370
WAL 3380
WAL 3390
WAL 3400
WAL 3410
WAL 3420
WAL 3430
WAL 3440
WAL 3450
WAL 3460
WAL 3470
WAL 3480
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WAL 3650
WAL 3660
WAL 3670
WAL 3680
WAL 3690
WAL 3700
WAL 3710
WAL 3720
WAL 3730
WAL 3740
WAL 3750
WAL 3760
WAL 3770
WAL 3780
WAL 3790
WAL 3800
WAL 3810
WAL 3820
WAL 3830
WAL 3840
WAL 3850
WAL 3860
WAL 3870
WAL 3880
WAL 3890
WAL 3900

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C	SUBROUTINE INLET	INL	10
C	*****	INL	20
C	*****	INL	30
C	THIS SUBROUTINE CALCULATES THE BOUNDARY MESH POINTS AT THE NOZZLE	INL	40
C	INLET FOR SUBSONIC FLOW	INL	50
C	*****	INL	60
C	*****	INL	70
C	*****	INL	80
C	*****	INL	90
C	COMMON /AV/ IAV,CAV,NST,SMP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81	INL	100
C	1,21),QPT(81,21)	INL	110
C	COMMON /ONESTD/ UD(4),VD(4),PD(4),ROD(4)	INL	120
C	COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RO(81,21,2)	INL	130
C	COMMON /CNTRLC/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAMI,GAINL	INL	140
C	1M2,L1,L2,L3,M1,M2,DX,DY,DT,N,N1,N3,NASM,IVEL,ICHAR,N1D,LJET,JFLAG,INL	INL	150
C	2IERR,IUI,IUD,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TCINL	INL	160
C	3,LC,PLOH,ROLOW	INL	170
C	COMMON /GEMTRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCI,ANGI,ANGE,XW(81),INL	INL	180
C	1YN(81),XWI(81),YWI(81),NXNY(81),NWPTS,IINT,IDIF,LT,NDIM	INL	190
C	COMMON /GCB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,RECB,RCICB,RCTCB,ANGICBINL	INL	200
C	1,ANGECB,XCB(81),YCB(81),XCB1(81),YCB1(81),NXNYCB(81),NCBPTS,IINTCBINL	INL	210
C	2,IDIFCB,LECB	INL	220
C	COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASS,MASSI,MASST,THRUST,NINL	INL	230
C	1STAG	INL	240
C	REAL MN3,NXNY,MASSI,MASST,NXNYCB,MASS	INL	250
C	GRGB=GAMMA*RGAS*G	INL	260
C	X3=XI	INL	270
C	ATERM2=0.0	INL	280
C	ATERM3=0.0	INL	290
C	DO 100 ICHAR=1,2	INL	300
C	DO 100 M=1,MMAX	INL	310
C	LMN1=1+LD*(M-1)+LMD1	INL	320
C	LMN3=1+LD*(M-1)+LMD3	INL	330
C	L1MN1=2+LD*(M-1)+LMD1	INL	340
C	L1M1N1=2+LD*(M-2)+LMD1	INL	350
C	L1M1N1=1+LD*(M-2)+LMD1	INL	360
C	L1M1N3=1+LD*(M-2)+LMD3	INL	370
C	CALL MAP (2,1,M,AL,BE,DE,2,AL1,BE1,DE1)	INL	380
C	U2=U(LMN1)	INL	390
C	A2=SQRT(GAMMA*P(LMN1)/RO(LMN1))	INL	400
C	IF (ICHAR,EQ,2) GO TO 10	INL	410
C	U(LMN3)=U2	INL	420
C	V(LMN3)=V(LMN1)	INL	430
C	A3=A2	INL	440
C	*****	INL	450
C	*****	INL	460
C	CALCULATE THE PROPERTY INTERPOLATING POLYNOMIAL COEFFICIENTS	INL	470
C	*****	INL	480
C	*****	INL	490
10	BU=(U(L1MN1)-U(LMN1))*DXR	INL	500
	BV=(V(L1MN1)-V(LMN1))*DXR	INL	510
	BP=(P(L1MN1)-P(LMN1))*DXR	INL	520
	BRO=(RO(L1MN1)-RO(LMN1))*DXR	INL	530
	BYCB=(YCB(2)-YCB(1))*DXR	INL	540
	BAL=(AL1-AL)*DXR	INL	550
	BBE=(BE1-BE)*DXR	INL	560
	CU=U(1,M,N1)-BU*X3	INL	570
	CV=V(1,M,N1)-BV*X3	INL	580
	CP=P(1,M,N1)-BP*X3	INL	590
	CRO=RO(1,M,N1)-BRO*X3	INL	600
	CYCB=YCB(1)-BYCB*X3	INL	610
	CAL=AL-BAL*X3	INL	620
	CBE=BE-BBE*X3	INL	630
C	*****	INL	640
C	CALCULATE THE CROSS DERIVATIVE INTERPOLATING POLYNOMIAL	INL	650
C	COEFFICIENTS	INL	660
C	*****	INL	670
C	IF (M,EQ,1) GO TO 20	INL	680
	DU=(U(L1MN1)-U(L1M1N1))*DYR	INL	690
	DV=(V(L1MN1)-V(L1M1N1))*DYR	INL	700
	DP=(P(L1MN1)-P(L1M1N1))*DYR	INL	710
	DRO=(RO(L1MN1)-RO(L1M1N1))*DYR	INL	720
	DU1=(U(LMN1)-U(L1M1N1))*DYR	INL	730
	DV1=(V(LMN1)-V(L1M1N1))*DYR	INL	740
	DP1=(P(LMN1)-P(L1M1N1))*DYR	INL	750
	DRO1=(RO(LMN1)-RO(L1M1N1))*DYR	INL	760
	GO TO 40	INL	770
20	IF (NGCB,NE,0) GO TO 30	INL	780
	DU=0.0	INL	790
	DV=V(2,2,N1)*DYR	INL	800
	DP=0.0	INL	810
	DRO=0.0	INL	820
	DU1=0.0	INL	830
	DV1=V(1,2,N1)*DYR	INL	840

	DP1=0.0	INL 840
	DRO1=0.0	INL 850
	GO TO 40	INL 860
30	DU=(U(2,2,N1)-U(2,1,N1))*DYP	INL 870
	DV=(V(2,2,N1)-V(2,1,N1))*DYP	INL 880
	DP=(P(2,2,N1)-P(2,1,N1))*DYP	INL 890
	DRO=(RO(2,2,N1)-RO(2,1,N1))*DYP	INL 900
	DU1=(U(1,2,N1)-U(1,1,N1))*DYP	INL 910
	DV1=(V(1,2,N1)-V(1,1,N1))*DYP	INL 920
	DP1=(P(1,2,N1)-P(1,1,N1))*DYP	INL 930
	DRO1=(RO(1,2,N1)-RO(1,1,N1))*DYP	INL 940
40	BDU=(DU-DU1)*DXR	INL 950
	BDV=(DV-DV1)*DXR	INL 960
	BDP=(DP-DP1)*DXR	INL 970
	BDRO=(DRO-DRO1)*DXR	INL 980
	CDU=DU1-BDU*X3	INL 990
	CDV=DV1-BDV*X3	INL 1000
	CDP=DP1-BDP*X3	INL 1010
	CDRO=DRO1-BDRO*X3	INL 1020
C		INL 1030
C	CALCULATE X2	INL 1040
C		INL 1050
	IF (ICAR, EQ, 2) A3=SQRT(GAMMA*P(LMN3)/RO(LMN3))	INL 1060
	DO 50 IL=1,2	INL 1070
	X2=X3-(U(1,M,N3)-A3+U2-A2)*0.5*DT	INL 1080
C		INL 1090
C	INTERPOLATE FOR THE PROPERTIES	INL 1100
C		INL 1110
	U2=BU*X2+CU	INL 1120
	P2=BP*X2+CP	INL 1130
	RO2=BR0*X2+CRO	INL 1140
	A2=SQRT(GAMMA*P2/RO2)	INL 1150
50	CONTINUE	INL 1160
	V2=BV*X2+CV	INL 1170
	YCB2=BYCB*X2+CYCB	INL 1180
	AL2=BAL*X2+CAL	INL 1190
	BE2=BBE*X2+CBE	INL 1200
	UV2=U2*AL2+V2*BE2	INL 1210
C		INL 1220
C	INTERPOLATE FOR THE CROSS DERIVATIVES	INL 1230
C		INL 1240
	DU2=BDU*X2+CDU	INL 1250
	DV2=BDV*X2+CDV	INL 1260
	DP2=BDP*X2+CDP	INL 1270
	DRO2=BDRO*X2+CDRO	INL 1280
C		INL 1290
C	CALCULATE THE PSI TERMS	INL 1300
C		INL 1310
	IF (NDIM, EQ, 0) GO TO 70	INL 1320
	IF (M, EQ, 1, AND, NGCB, EQ, 0) GO TO 60	INL 1330
	ATERM2=RO2*V2/(DY*(M=1)/BE2+YCB2)	INL 1340
	GO TO 70	INL 1350
60	ATERM2=RO2*BE2*DV2	INL 1360
70	PSI12=-UV2*DRO2-RO2*AL2*DU2-RO2*BE2*DV2-ATERM2	INL 1370
	PSI22=-UV2*DU2-AL2*DP2/RO2	INL 1380
	PSI42=-UV2*DP2+A2*A2*UV2*DRO2	INL 1390
	IF (ICAR, EQ, 1) GO TO 130	INL 1400
C		INL 1410
C	CALCULATE THE CROSS DERIVATIVES AT THE SOLUTION POINT	INL 1420
C		INL 1430
	IF (M, EQ, 1, AND, NGCB, EQ, 0) GO TO 80	INL 1440
	IF (M, EQ, MMAX) GO TO 90	INL 1450
	DU3=(U(LMN3)-U(LMN3))*DYP	INL 1460
	DV3=(V(LMN3)-V(LMN3))*DYP	INL 1470
	DP3=(P(LMN3)-P(LMN3))*DYP	INL 1480
	DRO3=(RO(LMN3)-RO(LMN3))*DYP	INL 1490
	GO TO 100	INL 1500
80	DU3=0.0	INL 1510
	DV3=V(1,2,N3)*DYP	INL 1520
	DP3=0.0	INL 1530
	DRO3=0.0	INL 1540
	GO TO 100	INL 1550
90	DU3=(U(1,MMAX,N3)-U(1,M1,N3))*DYP	INL 1560
	DV3=(V(1,MMAX,N3)-V(1,M1,N3))*DYP	INL 1570
	DP3=(P(1,MMAX,N3)-P(1,M1,N3))*DYP	INL 1580
	DRO3=(RO(1,MMAX,N3)-RO(1,M1,N3))*DYP	INL 1590
C		INL 1600
C	CALCULATE THE PSI TERMS AT THE SOLUTION POINT	INL 1610
C		INL 1620
100	IF (NDIM, EQ, 0) GO TO 120	INL 1630
	IF (M, EQ, 1, AND, NGCB, EQ, 0) GO TO 110	INL 1640
	ATERM3=RO(LMN3)*V(LMN3)/(DY*(M=1)/BE+YCB(1))	INL 1650
	GO TO 120	INL 1660

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110 ATERM3=RO(LMN3)*BE*DV3 INL 1670
120 UV3=U(LMN3)*AL+V(LMN3)*BE INL 1680
PSI13=UV3*DR03=RO(LMN3)*AL*DU3=RO(LMN3)*BE*DV3-ATERM3 INL 1690
PSI23=UV3*DU3=AL*DP3/RO(LMN3) INL 1700
PSI43=UV3*DP3+A3*A3*UV3*DR03 INL 1710
GO TO 140 INL 1720
130 PSI23=PSI22 INL 1730
PSI43=PSI42 INL 1740
PSI13=PSI12 INL 1750
C INL 1760
C SOLVE THE COMPATIBILITY EQUATIONS FOR U,V,P, AND RO INL 1770
C INL 1780
140 MN3=SQRT(U(LMN3)*U(LMN3)+V(LMN3)*V(LMN3))/A3 INL 1790
T2=P2/(RO2*RGAS*G) INL 1800
PSI1B=(PSI12+PSI13)*0.5 INL 1810
PSI2B=(PSI22+PSI23)*0.5 INL 1820
PSI4B=(PSI42+PSI43)*0.5 INL 1830
GPSI1B=GAMMA*PSI1B INL 1840
THETA=TAN(THETA(M)) INL 1850
UCORR=0.5+0.5/SQRT(1.0+THETA*TTHETA) INL 1860
C INL 1870
DO 160 ITER=1,20 INL 1880
DEM=(1.0+GAM2*MN3*MN3) INL 1890
P(LMN3)=PT(M)/(DEM**GAM1) INL 1900
T3=TT(M)/DEM INL 1910
PB=(P2+P(LMN3))*0.5 INL 1920
RTB=RGAS*(T2+T3)*0.5*G INL 1930
U(LMN3)=U2+DT*PSI2B+(P(LMN3)-P2*(PSI4B+RTB*GPSI1B)*DT)*SQRT(RTB/GA INL 1940
1 MMA)/PB INL 1950
U(LMN3)=U(LMN3)*UCORR INL 1960
V(LMN3)=V(LMN3)*TTHETA INL 1970
OMN3=MN3 INL 1980
MN3=SQRT((U(LMN3)*U(LMN3)+V(LMN3)*V(LMN3))/(T3*GRGB)) INL 1990
IF (OMN3.NE.0.0) GO TO 150 INL 2000
IF (ABS(MN3-OMN3).LE.0.0001) GO TO 170 INL 2010
GO TO 160 INL 2020
150 IF (ABS((MN3-OMN3)/OMN3).LE.0.001) GO TO 170 INL 2030
160 CONTINUE INL 2040
C INL 2050
PRINT 190, M,N INL 2060
170 RO(LMN3)=P(LMN3)/(RGAS*T3*G) INL 2070
180 CONTINUE INL 2080
RETURN INL 2090
C INL 2100
190 FORMAT (1H0,58H***** THE SOLUTION FOR NOZZLE ENTRANCE BOUNDARY POIN INL 2110
INT ( 1,,I2,1H,,I4,43H) FAILED TO CONVERGE IN 20 ITERATIONS ***** INL 2120
END INL 2130

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30	DU=(U(LMAX,2,N1)-U(LMAX,1,N1))*DYS	EXI	840
	DV=(V(LMAX,2,N1)-V(LMAX,1,N1))*DYS	EXI	850
	DP=(P(LMAX,2,N1)-P(LMAX,1,N1))*DYS	EXI	860
	DRO=(RO(LMAX,2,N1)-RO(LMAX,1,N1))*DYS	EXI	870
	DU1=(U(L1,2,N1)-U(L1,1,N1))*DYS	EXI	880
	DV1=(V(L1,2,N1)-V(L1,1,N1))*DYS	EXI	890
	DP1=(P(L1,2,N1)-P(L1,1,N1))*DYS	EXI	900
	DRO1=(RO(L1,2,N1)-RO(L1,1,N1))*DYS	EXI	910
40	BDU=(DU-DU1)*DXR	EXI	920
	BDV=(DV-DV1)*DXR	EXI	930
	BDP=(DP-DP1)*DXR	EXI	940
	BDRO=(DRO-DRO1)*DXR	EXI	950
	CDU=DU-BDU*X3	EXI	960
	CDV=DV-BDV*X3	EXI	970
	CDP=DP-BDP*X3	EXI	980
	CDRO=DRO-BDRO*X3	EXI	990
C		EXI	1000
C	CALCULATE X1 AND X2	EXI	1010
C		EXI	1020
	IF (ICAR, EQ, 2) A3=SQRT(GAMMA*P(LMAX,M,N3)/RO(LMAX,M,N3))	EXI	1030
	DO 50 IL=1,2	EXI	1040
	X1=X3-(U(LMAX,M,N3)+U1)*0.5*DT	EXI	1050
	X2=X3-(U(LMAX,M,N3)+A3+U2+A2)*0.5*DT	EXI	1060
C		EXI	1070
C	INTERPOLATE FOR THE PROPERTIES	EXI	1080
C		EXI	1090
	U1=BU*X1+CU	EXI	1100
	U2=BU*X2+CU	EXI	1110
	P2=BP*X2+CP	EXI	1120
	RO2=BR0*X2+CRO	EXI	1130
	A2=SQRT(GAMMA*P2/RO2)	EXI	1140
50	CONTINUE	EXI	1150
	V1=BV*X1+CV	EXI	1160
	P1=BP*X1+CP	EXI	1170
	RO1=BR0*X1+CRO	EXI	1180
	YCB1=BYCB*X1+CYCB	EXI	1190
	AL1=BAL*X1+CAL	EXI	1200
	BE1=BBE*X1+CBE	EXI	1210
	DE1=BDE*X1+CDE	EXI	1220
	UV1=U1*AL1+V1*BE1+DE1	EXI	1230
	A1=SQRT(GAMMA*P1/RO1)	EXI	1240
	V2=BV*X2+CV	EXI	1250
	YCB2=BYCB*X2+CYCB	EXI	1260
	AL2=BAL*X2+CAL	EXI	1270
	BE2=BBE*X2+CBE	EXI	1280
	DE2=BDE*X2+CDE	EXI	1290
	UV2=U2*AL2+V2*BE2+DE2	EXI	1300
C		EXI	1310
C	INTERPOLATE FOR THE CROSS DERIVATIVES	EXI	1320
C		EXI	1330
	DV1=BDV*X1+CDV	EXI	1340
	DP1=BDP*X1+CDP	EXI	1350
	DRO1=BDRO*X1+CDRO	EXI	1360
	DU2=BDU*X2+CDU	EXI	1370
	DV2=BDV*X2+CDV	EXI	1380
	DP2=BDP*X2+CDP	EXI	1390
	DRO2=BDRO*X2+CDRO	EXI	1400
C		EXI	1410
C	CALCULATE THE PSI TERMS	EXI	1420
C		EXI	1430
	IF (NDIM, EQ, 0) GO TO 70	EXI	1440
	IF (M, EQ, 1, AND, LECB, NE, LMAX) GO TO 60	EXI	1450
	ATERM1=RO1*V1/(DY*(M-1)/BE1+YCB1)	EXI	1460
	ATERM2=RO2*V2/(DY*(M-1)/BE2+YCB2)	EXI	1470
	GO TO 70	EXI	1480
60	ATERM1=RO1*BE1*DV1	EXI	1490
	ATERM2=RO2*BE2*DV2	EXI	1500
70	PSI31=-UV1*DV1+BE1*DP1/RO1	EXI	1510
	PSI41=-UV1*DP1+A1*A1*UV1*DRO1	EXI	1520
	PSI12=-UV2*DRO2-RO2*AL2*DU2-RO2*BE2*DV2+ATERM2	EXI	1530
	PSI22=-UV2*DU2+AL2*DP2/RO2	EXI	1540
	PSI42=-UV2*DP2+A2*A2*UV2*DRO2	EXI	1550
	IF (ICAR, EQ, 1) GO TO 130	EXI	1560
C		EXI	1570
C	CALCULATE THE CROSS DERIVATIVES AT THE SOLUTION POINT	EXI	1580
C		EXI	1590
	IF (M, EQ, 1, AND, LECB, NE, LMAX) GO TO 80	EXI	1600
	IF (M, EQ, MMAX) GO TO 90	EXI	1610
	DU3=(U(LMAX,M+1,N3)-U(LMAX,M,N3))*DYS	EXI	1620
	DV3=(V(LMAX,M+1,N3)-V(LMAX,M,N3))*DYS	EXI	1630
	DP3=(P(LMAX,M+1,N3)-P(LMAX,M,N3))*DYS	EXI	1640
	DRO3=(RO(LMAX,M+1,N3)-RO(LMAX,M,N3))*DYS	EXI	1650
	GO TO 100	EXI	1660

80	DU3=0.0	EXI 1670
	DV3=V(LMAX,2,N3)*DYR	EXI 1680
	DP3=0.0	EXI 1690
	DRO3=0.0	EXI 1700
	GO TO 100	EXI 1710
90	DU3=(U(LMAX,MMAX,N3)-U(LMAX,M1,N3))*DYR	EXI 1720
	DV3=(V(LMAX,MMAX,N3)-V(LMAX,M1,N3))*DYR	EXI 1730
	DP3=(P(LMAX,MMAX,N3)-P(LMAX,M1,N3))*DYR	EXI 1740
	DRO3=(RO(LMAX,MMAX,N3)-RO(LMAX,M1,N3))*DYR	EXI 1750
C		EXI 1760
C	CALCULATE THE PSI TERMS AT THE SOLUTION POINT	EXI 1770
C		EXI 1780
100	IF (NDIM,EQ,0) GO TO 120	EXI 1790
	IF (M,EQ,1,AND,LECB,NE,LMAX) GO TO 110	EXI 1800
	ATERM3=RO(LMAX,M,N3)*V(LMAX,M,N3)/(DY*(M-1)/BE+YCB(LMAX))	EXI 1810
	GO TO 120	EXI 1820
110	ATERM3=RO(LMAX,1,N3)*BE*DV3	EXI 1830
120	UV3=U(LMAX,M,N3)*AL+V(LMAX,M,N3)*BE+DE	EXI 1840
	PSI13=-UV3*DRO3-RO(LMAX,M,N3)*(AL*DU3+BE*DV3)-ATERM3	EXI 1850
	PSI23=-UV3*DU3-AL*DP3/RO(LMAX,M,N3)	EXI 1860
	PSI33=-UV3*DV3-BE*DP3/RO(LMAX,M,N3)	EXI 1870
	PSI43=-UV3*DP3+A3*A3*UV3*DRO3	EXI 1880
C		EXI 1890
C	CALCULATE THE COMPATIBILITY EQUATION COEFFICIENTS	EXI 1900
C		EXI 1910
130	IF (ICHR,EQ,1) GO TO 140	EXI 1920
	PSI31B=(PSI31+PSI33)*0.5	EXI 1930
	PSI41B=(PSI41+PSI43)*0.5	EXI 1940
	PSI12B=(PSI12+PSI13)*0.5	EXI 1950
	PSI22B=(PSI22+PSI23)*0.5	EXI 1960
	PSI42B=(PSI42+PSI43)*0.5	EXI 1970
	GO TO 150	EXI 1980
140	PSI31B=PSI31	EXI 1990
	PSI41B=PSI41	EXI 2000
	PSI12B=PSI12	EXI 2010
	PSI22B=PSI22	EXI 2020
	PSI42B=PSI42	EXI 2030
C		EXI 2040
C	SOLVE THE COMPATIBILITY EQUATIONS FOR U,V,P, AND RO	EXI 2050
C		EXI 2060
150	P(LMAX,M,N3)=PE	EXI 2070
	RO(LMAX,M,N3)=RO1+2.0*(P(LMAX,M,N3)-P1-DT*PSI41B)/(A3*A3+A1*A1)	EXI 2080
	U(LMAX,M,N3)=U2+((PSI42B+(RO2+RO(LMAX,M,N3))*(A2+A3)*PSI22B/4.0+(A2+A3)*PSI12B/2.0)*DT*(P(LMAX,M,N3)-P2))/(RO2+RO(LMAX,M,N3))	EXI 2090
	2*(A2+A3)*4.0	EXI 2100
	V(LMAX,M,N3)=V1+DT*PSI31B	EXI 2110
160	CONTINUE	EXI 2120
	V(LMAX,MMAX,N3)=-U(LMAX,MMAX,N3)*NXNY(LMAX)	EXI 2130
	V(LMAX,1,N3)=-U(LMAX,1,N3)*NXNYCB(LMAX)	EXI 2140
	IF (JFLAG,EQ,0) RETURN	EXI 2150
	V(LMAX,MMAX,N3)=V(LMAX,MMAX,N3)+XNT(LMAX)	EXI 2160
	RETURN	EXI 2170
	END	EXI 2180
		EXI 2190