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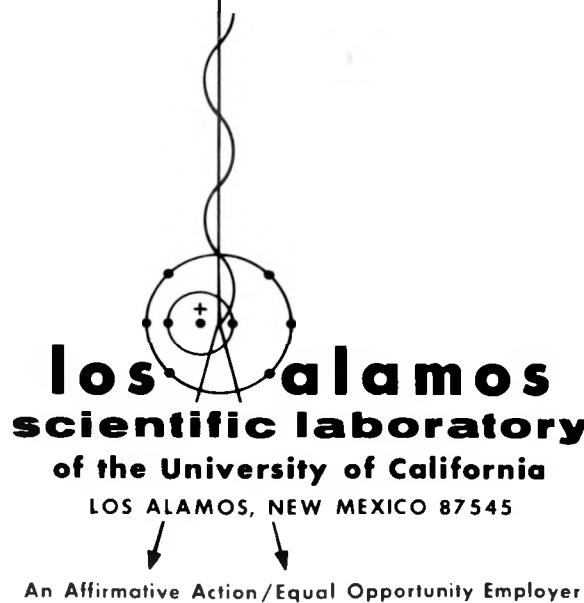
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NAP: A Computer Program for the Computation of Two-Dimensional, Time-Dependent, Inviscid Nozzle Flow

by

Michael C. Cline



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NAP: A COMPUTER PROGRAM FOR THE
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ABSTRACT

A computer program, NAP, is presented for calculating inviscid, steady, and unsteady flow in two-dimensional and axisymmetric nozzles. Interior mesh points are computed using the MacCormack finite-difference scheme, while a characteristic scheme is used to calculate the boundary mesh points. An explicit artificial viscosity term is included for shock computations. The fluid is assumed to be a perfect gas. This method was used to compute the steady flow in a 45°-15° conical, converging-diverging nozzle, a 15° conical, converging nozzle, and a 10° conical, plug nozzle. The numerical solution agreed well with the experimental data. In contrast to previous time-dependent methods for calculating steady flows, the computational times were < 1 min on a CDC 6600 computer.

I. BASIC DESCRIPTION OF THE METHOD

A. Introduction

The equations of motion governing steady, inviscid flow are of a mixed type: hyperbolic in the supersonic region and elliptic in the subsonic region. These mathematical difficulties may be removed by using the "time-dependent" method, in which the flow is assumed to be unsteady or time-dependent. Then the governing equations are hyperbolic in both subsonic and supersonic regions. The steady-state solution may be obtained as the asymptotic solution for large time. This time-dependent technique has been used to compute steady converging-diverging nozzle flows (reported in Refs. 1-6), and it has also been used to compute steady converging nozzle flows (see Refs. 4 and 7). The results of those calculations are mainly good, but the computational times are rather large. In addition, although the computer program of Ref. 6 included a centerbody and those of Refs. 4 and 7 included the exhaust jet, none of the above codes is able to calculate both, that is, plug nozzles.

The object of this research was to develop a production-type computer program capable of solving steady converging, converging-diverging, and plug two-dimensional nozzle flows in computational times of < 1 min on a CDC 6600 computer. Such a program would be able to solve unsteady flows as well.

B. Literature Review

The following is a discussion of the methods used in Refs. 1 through 7. The first paragraph deals with the computation of the interior mesh points; the next three paragraphs are concerned with the boundary mesh points.

Prozan (see Ref. 1), Wehofer and Moger,⁴ and Laval⁵ used variations of the two-step Lax-Wendroff scheme to compute the interior mesh points. Migdal et al.³ and Brown and Ozcan⁷ employed the original one-step Lax-Wendroff scheme, but with the equations of motion in nonconservation form. Serra⁶ applied the original Lax-Wendroff scheme with the equations of motion in conservation form. To stabilize their schemes, Laval and Serra used artificial viscosity terms in their difference equations. Wehofer and

Moger reset the stagnation conditions along each streamline, reset the mass flow at each axial location, and smoothed the subsonic portion of the flow after each time step.

To compute the nozzle inlet mesh points, Prozan (in Ref. 1) assumed the inlet flow to be uniform. Wehofer and Moger assumed only that the pressure was radially uniform at the inlet. Migdal et al. and Brown and Ozcan mapped the inlet to minus infinity after Moretti,⁸ thus allowing the static conditions to be set equal to the stagnation conditions. Laval used extrapolation of the interior mesh points to determine the inlet mesh points, while Serra employed a characteristic scheme.

Prozan (in Ref. 1), Wehofer and Moger, Laval, and Brown and Ozcan used an extrapolation technique to compute the wall mesh points. Migdal et al. employed a characteristic scheme after Moretti⁸ to compute the wall mesh points, while Serra applied a reflection technique. For the converging nozzle problem to be properly posed, an exhaust jet calculation must be included. Wehofer and Moger used an extrapolation procedure to compute the exhaust jet boundary mesh points, while Brown and Ozcan employed a characteristic scheme after Moretti.⁸

All of the above authors used extrapolation to compute the exit mesh points when the flow was supersonic, since any errors incurred would be swept out of the mesh. Serra employed a characteristic scheme when the exit flow was subsonic.

C. Choice of a Method

The lengthy computational times associated with time-dependent calculations are usually caused by inefficient numerical schemes or poor treatment of boundaries, resulting in the requirement for excessively fine computational meshes (see Refs. 8 and 9). A technique for a much more efficient calculation of the interior and boundary mesh points will be discussed here.

The computation of steady flows by a time-dependent method differs from ordinary initial-value problems in that the initial data and much of the transient solution have a negligible effect on the final or steady solution. Therefore, accuracy is important only for the asymptotic state, and special attention to intermediate efficiency will result in reasonable computational times. For this reason, interior mesh points can be computed by using a very

efficient finite-difference scheme, as opposed to those less efficient finite-difference or characteristic schemes that achieve high accuracy at every step.

In the class of finite-difference schemes, the two-step methods such as the MacCormack¹⁰ and the two-step Lax-Wendroff schemes¹¹ are more efficient than the original Lax-Wendroff scheme,¹¹ especially if the governing equations are in conservation form. Moretti¹² showed that using the equations of motion in conservation form decreased efficiency and ease of programming while only slightly increasing the accuracy of shock calculations. The use of an explicit artificial viscosity term for shock-free flows also decreases efficiency and was shown to be physically unjustified.¹² In addition, such increases in the numerical dissipation can often destroy the weak shock structure of transonic flows. Therefore, the MacCormack scheme with the equations of motion in nonconservation form is used to calculate the interior mesh points. An explicit artificial viscosity term was included for shock computations only. Remember that the implicit dissipation always present as an effect of truncation terms assures numerical stability for the shock-free flow results.

The boundary mesh points, while making up only a small part of the total mesh points, must be handled most accurately,⁸ because of the flow-field's sensitivity to precise boundary geometry. Moretti⁸ and Abbott⁹ showed that reflection, extrapolation, and one-sided difference techniques for computing solid wall boundaries give poor results and should be avoided. Therefore, the wall and centerbody mesh points are computed using a characteristic scheme. A characteristic scheme is also used to calculate the exhaust jet boundary mesh points.

In the case of the nozzle inlet mesh points for subsonic flow, the use of extrapolation techniques and the assumption of one-dimensional flow presume the form of the solution and in many cases are physically unjustified. On the other hand, a characteristic scheme could be used to calculate the inlet mesh points. While the stagnation pressure and temperature are assumed to remain constant at the inlet in a characteristic scheme (not necessarily the case for unsteady flow), this assumption

would appear to be valid for the time-dependent calculation of steady flows. Moretti⁸ recommends mapping the inlet to minus infinity, thus allowing the static conditions to be set equal to the stagnation conditions. In theory, this appears to be the best approach, but it should be kept in mind that the infinite physical plane must be replaced by a finite computational plane. Also, this technique requires additional mesh points upstream of the nozzle inlet. It is not presently resolved as to whether the characteristic scheme approach used by Serra or the mapping-to-minus-infinity approach suggested by Moretti⁸ and employed by Migdal et al. and Brown and Ozcan is the best technique. To reduce the total number of mesh points to be computed, a characteristic scheme is used to compute the inlet mesh points. For supersonic flow, the inlet mesh points are set equal to specified values of velocity, pressure, and density, because in a supersonic stream the downstream conditions do not propagate upstream.

Extrapolation is used to compute the exit mesh points when the flow is supersonic, since any errors incurred will be swept out of the mesh, and a characteristic scheme is employed when the flow is subsonic.

D. Equations of Motion

The appropriate nonconservation form of equations for two-dimensional, inviscid, isentropic, rotational flow are

$$\rho_t + u\rho_x + v\rho_y + \rho u_x + \rho v_y + \epsilon p v/y = 0, \quad (1)$$

$$u_t + uu_x + vu_y + p_x/\rho = 0, \quad (2)$$

$$v_t + uv_x + vv_y + p_y/\rho = 0, \quad (3)$$

$$p_t + u\rho_x + v\rho_y - a^2(\rho_t + u\rho_x + v\rho_y) = 0, \quad (4)$$

where ρ is the density, u is the axial velocity, v is the radial velocity, p is the pressure, a is the local speed of sound, t is the time, x and y are the axial and radial coordinates, and the subscripts denote partial differentiation. The symbol ϵ is 0 for planar flow and 1 for axisymmetric flow.

The physical (x,y) plane is mapped into a rectangular computational plane (ζ,η) by the following coordinate transformation:

$$\zeta = x; \quad \eta = \frac{y - y_c(x)}{y_w(x,t) - y_c(x)}; \quad \tau = t, \quad (5)$$

where $y_w(x,t)$ denotes the nozzle wall and exhaust jet boundary radius as a function of x and t and $y_c(x)$ denotes the nozzle centerbody radius as a function of x . These mapping functions must be single-valued functions of the x coordinate. In the (ζ,η,τ) coordinate system Eqs. (1) through (4) become

$$\rho_\tau + u\rho_\zeta + \bar{v}\rho_\eta + \rho u_\zeta + \rho \alpha u_\eta + \rho \beta v_\eta + \epsilon p v / (y_c + \eta/\beta) = 0, \quad (6)$$

$$u_\tau + uu_\zeta + \bar{v}u_\eta + p_\zeta/\rho + \alpha p_\eta/\rho = 0, \quad (7)$$

$$v_\tau + uv_\zeta + \bar{v}v_\eta + \beta p_\eta/\rho = 0, \quad (8)$$

$$p_\tau + u\rho_\zeta + \bar{v}\rho_\eta - a^2(\rho_\tau + u\rho_\zeta + \bar{v}\rho_\eta) = 0, \quad (9)$$

where

$$\begin{aligned} \beta &= \frac{1}{y_w - y_c}; \quad \alpha = -\beta \frac{\partial y_c}{\partial x} - \eta \beta \left(\frac{\partial y_w}{\partial x} - \frac{\partial y_c}{\partial x} \right); \\ \delta &= -\eta \beta \frac{\partial y_w}{\partial t}, \end{aligned} \quad (10)$$

$$\bar{v} = \alpha u + \beta v + \delta. \quad (11)$$

The fluid is assumed to be thermally and calorically perfect; that is, a constant ratio of specific heats is assumed.

For shock computations, an artificial viscosity model of the form suggested by von Neumann-Richtmyer¹¹ is used. This model, which has a term corresponding to all the viscous and thermal conduction terms in the Navier-Stokes equations, is shown below.

$$\begin{aligned} [\text{RHS Eq. (21)}] &= (\lambda + 2\mu) \frac{\partial}{\partial x} \left(\frac{\partial u}{\partial x} \right) + \lambda \frac{\partial}{\partial x} \left(\frac{\partial v}{\partial y} \right) \\ &\quad + \mu \frac{\partial}{\partial y} \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right) \\ &\quad + \frac{\epsilon}{y} \left[(\lambda + \mu) \frac{\partial v}{\partial x} + \mu \frac{\partial u}{\partial y} \right], \end{aligned} \quad (12)$$

$$\begin{aligned}
[\text{RHS Eq. (3)}] &= (\lambda + 2\mu) \frac{\partial}{\partial y} \left(\frac{\partial u}{\partial x} \right) + \lambda \frac{\partial}{\partial y} \left(\frac{\partial v}{\partial y} \right) \\
&\quad + \mu \frac{\partial}{\partial x} \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right) + \frac{\varepsilon(\lambda + 2\mu)}{y} \left(\frac{\partial v}{\partial y} - \frac{v}{y} \right), \\
&\quad (13)
\end{aligned}$$

$$\begin{aligned}
[\text{RHS Eq. (4)}] &= \rho(\gamma - 1) \left\{ (\lambda + 2\mu) \left[\left(\frac{\partial u}{\partial x} \right)^2 + \left(\frac{\partial v}{\partial y} \right)^2 \right] \right. \\
&\quad + \mu \left[\left(\frac{\partial u}{\partial y} \right)^2 + \left(\frac{\partial v}{\partial x} \right)^2 \right] + 2\lambda \frac{\partial u}{\partial x} \frac{\partial v}{\partial y} \\
&\quad + 2\mu \frac{\partial u}{\partial y} \frac{\partial v}{\partial x} + k \left[\frac{\partial}{\partial x} \left(\frac{\partial T}{\partial x} \right) + \frac{\partial}{\partial y} \left(\frac{\partial T}{\partial y} \right) \right. \\
&\quad \left. + \frac{\varepsilon v}{y} \left[(\lambda + 2\mu) \frac{v}{y} + 2\lambda \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) \right. \right. \\
&\quad \left. \left. + \frac{k}{v} \frac{\partial T}{\partial y} \right] \right\}, \\
&\quad (14)
\end{aligned}$$

$$\lambda = 2c c_\lambda \Delta x \Delta y \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right),$$

$$\mu = 2c c_\mu \Delta x \Delta y \left(\frac{\partial v}{\partial x} + \frac{\partial u}{\partial y} \right),$$

$$k = \frac{\mu \gamma R}{(\gamma - 1) Pr},$$

where c , c_λ , and c_μ are nondimensional quantities that specify the distribution and amount of smoothing, γ is the ratio of specific heats, R is the gas constant, Δx and Δy are the axial and radial mesh spacing, and Pr is the Prandtl number.

In the (ζ, η, τ) coordinate system Eqs. (12) through (14) become

$$\begin{aligned}
[\text{RHS Eq. (7)}] &= (\lambda + 2\mu) \left(\frac{\partial}{\partial \zeta} + \alpha \frac{\partial}{\partial \eta} \right) \left(\frac{\partial u}{\partial \zeta} + \alpha \frac{\partial u}{\partial \eta} \right) \\
&\quad + \lambda \left(\frac{\partial}{\partial \zeta} + \alpha \frac{\partial}{\partial \eta} \right) \left(\beta \frac{\partial v}{\partial \eta} \right) + \mu \beta \frac{\partial}{\partial \eta} \left(\beta \frac{\partial u}{\partial \eta} \right. \\
&\quad \left. + \frac{\partial v}{\partial \zeta} + \alpha \frac{\partial v}{\partial \eta} \right) + \frac{\varepsilon}{\bar{n}} \left[(\lambda + \mu) \left(\frac{\partial v}{\partial \zeta} \right. \right. \\
&\quad \left. \left. + \alpha \frac{\partial v}{\partial \eta} \right) + \mu \beta \frac{\partial u}{\partial \eta} \right], \\
&\quad (15)
\end{aligned}$$

$$\begin{aligned}
[\text{RHS Eq. (8)}] &= (\lambda + 2\mu) \beta \frac{\partial}{\partial \eta} \left(\frac{\partial u}{\partial \zeta} + \alpha \frac{\partial u}{\partial \eta} \right) + \lambda \beta \frac{\partial}{\partial \eta} \left(\beta \frac{\partial v}{\partial \eta} \right. \\
&\quad \left. + \mu \left(\frac{\partial}{\partial \zeta} + \alpha \frac{\partial}{\partial \eta} \right) \left(\beta \frac{\partial u}{\partial \eta} + \frac{\partial v}{\partial \zeta} + \alpha \frac{\partial v}{\partial \eta} \right) \right. \\
&\quad \left. + \frac{\varepsilon(\lambda + 2\mu)}{\bar{n}} \left(\beta \frac{\partial v}{\partial \eta} - \frac{v}{\bar{n}} \right) \right], \\
&\quad (16)
\end{aligned}$$

$$\begin{aligned}
[\text{RHS Eq. (9)}] &= \rho(\gamma - 1) \left\{ (\lambda + 2\mu) \left[\left(\frac{\partial u}{\partial \zeta} + \alpha \frac{\partial u}{\partial \eta} \right)^2 \right. \right. \\
&\quad \left. \left. + \left(\beta \frac{\partial v}{\partial \eta} \right)^2 \right] + \mu \left[\left(\beta \frac{\partial u}{\partial \eta} \right)^2 + \left(\frac{\partial v}{\partial \zeta} + \alpha \frac{\partial v}{\partial \eta} \right)^2 \right] \right. \\
&\quad \left. + 2\lambda \left(\frac{\partial u}{\partial \zeta} + \alpha \frac{\partial u}{\partial \eta} \right) \left(\beta \frac{\partial v}{\partial \eta} \right) \right. \\
&\quad \left. + 2\mu \left(\beta \frac{\partial u}{\partial \eta} \right) \left(\frac{\partial v}{\partial \zeta} + \alpha \frac{\partial v}{\partial \eta} \right) + k \left[\left(\frac{\partial}{\partial \zeta} \right. \right. \right. \\
&\quad \left. \left. \left. + \alpha \frac{\partial}{\partial \eta} \right) \left(\frac{\partial T}{\partial \zeta} + \alpha \frac{\partial T}{\partial \eta} \right) + \beta \frac{\partial}{\partial \eta} \left(\beta \frac{\partial T}{\partial \eta} \right) \right] \right. \\
&\quad \left. + \frac{\varepsilon v}{\bar{n}} \left[(\lambda + 2\mu) \frac{v}{\bar{n}} + 2\lambda \left(\frac{\partial u}{\partial \zeta} + \alpha \frac{\partial u}{\partial \eta} \right. \right. \right. \\
&\quad \left. \left. \left. + \beta \frac{\partial v}{\partial \eta} \right) + \frac{k}{v} \beta \frac{\partial T}{\partial \eta} \right] \right\}, \\
&\quad (17)
\end{aligned}$$

$$\lambda = 2c c_\lambda \Delta \zeta \frac{\Delta \eta}{\beta} \left(\frac{\partial u}{\partial \zeta} + \alpha \frac{\partial u}{\partial \eta} + \beta \frac{\partial v}{\partial \eta} \right),$$

$$\mu = 2c c_\mu \Delta \zeta \frac{\Delta \eta}{\beta} \left(\frac{\partial v}{\partial \zeta} + \alpha \frac{\partial v}{\partial \eta} + \beta \frac{\partial u}{\partial \eta} \right),$$

where $\bar{n} = y_c + n/\beta$, and y_c = centerbody radius. These terms are nonzero only when the divergence of the velocity is negative.

E. Numerical Method

The computational plane is divided into five sets of mesh points: interior, inlet, exit, wall and centerbody, and exhaust jet boundary.

1. Interior Mesh Points. The interior mesh points are computed using the MacCormack scheme, a second-order, noncentered, two-step, finite-difference scheme. Backward differences are used on the first step; forward differences are used on the second. The governing equations are left in non-conservation form. An explicit artificial viscosity term is used for shock computations. Centerline mesh points are computed by enforcing symmetry of the flow. For example, the finite-difference equations for Eq. (1) for planar flow ($\epsilon = 0$) and no artificial viscosity are

$$\begin{aligned} \bar{\rho}_{L,M}^{N+1} &= \bar{\rho}_{L,M}^N - \left[u_{L,M}^N \left(\frac{\bar{\rho}_{L,M}^N - \bar{\rho}_{L-1,M}^N}{\Delta x} \right) \right. \\ &\quad + v_{L,M}^N \left(\frac{\bar{\rho}_{L,M}^N - \bar{\rho}_{L,M-1}^N}{\Delta y} \right) \\ &\quad + \bar{\rho}_{L,M}^N \left(\frac{u_{L,M}^N - u_{L-1,M}^N}{\Delta x} \right) \\ &\quad \left. + \bar{\rho}_{L,M}^N \left(\frac{v_{L,M}^N - v_{L,M-1}^N}{\Delta y} \right) \right] \Delta t , \end{aligned} \quad (18)$$

$$\begin{aligned} \bar{\rho}_{L,M}^{N+1} &= 0.5 \left\{ \bar{\rho}_{L,M}^N + \bar{\rho}_{L,M}^{N+1} - \left[\bar{u}_{L,M}^{N+1} \left(\frac{\bar{\rho}_{L+1,M}^{N+1} - \bar{\rho}_{L,M}^{N+1}}{\Delta x} \right) \right. \right. \\ &\quad + \bar{v}_{L,M}^{N+1} \left(\frac{\bar{\rho}_{L,M+1}^{N+1} - \bar{\rho}_{L,M}^{N+1}}{\Delta y} \right) \\ &\quad + \bar{\rho}_{L,M}^{N+1} \left(\frac{\bar{u}_{L+1,M}^{N+1} - \bar{u}_{L,M}^{N+1}}{\Delta x} \right) \\ &\quad \left. \left. + \bar{\rho}_{L,M}^{N+1} \left(\frac{\bar{v}_{L,M+1}^{N+1} - \bar{v}_{L,M}^{N+1}}{\Delta y} \right) \right] \Delta t \right\} , \end{aligned} \quad (19)$$

where L and M denote axial and radial mesh points, respectively, N denotes the time step, and the bar denotes values calculated on the first step. A complete description of the method is given in Ref. 10.

2. Inlet Mesh Points. The inlet mesh points for subsonic flow are computed using a second-order, reference-plane characteristic scheme. In this

scheme, the partial derivatives with respect to n are computed in the initial-value and solution surfaces using noncentered differencing as in the MacCormack scheme. These approximations to the derivatives with respect to n are then treated as forcing terms and the resulting system of equations is solved in the $n = \text{constant}$ reference planes using a two-independent-variable, characteristic scheme. The characteristic relations for the $n = \text{constant}$ reference planes are derived in Appendix A. The boundary condition is the specification of the stagnation temperature and stagnation pressure. The use of a reference-plane characteristic scheme requires the specification of inlet flow angle as an additional boundary condition. The inlet flow angle can be approximately determined from the nozzle geometry. The equations relating the total and static conditions are

$$p_T/p = [1 + (\gamma - 1) M^2/2]^{Y/(\gamma-1)} , \quad (20)$$

$$T_T/T = 1 + (\gamma - 1) M^2/2 , \quad (21)$$

where γ is the ratio of specific heats, M is the Mach number, T is the temperature, and the subscript T denotes the total conditions.

The characteristic relations relating the interior flow to the nozzle inlet flow are Eq. (A-43) in Appendix A and can be written as

$$\begin{aligned} dp - \rho adu &= (\psi_4 + a^2 \psi_1 - \rho a \psi_2) d\tau \\ \text{for } d\xi &= (u-a) d\tau , \end{aligned} \quad (22)$$

where the top equation is called the compatibility equation and the bottom equation is called the characteristic curve equation. The ψ terms (see Appendix A) represent the derivatives in the n direction. Equation (22) may be written in finite-difference form by first replacing the differentials by differences along the characteristic curve. Next, the coefficients are either evaluated in the initial-value plane (first step) or considered to be the average of the coefficients evaluated in both the initial-value and solution planes (second step). Finally, the ψ terms are treated as follows: on the first step the coefficients and derivatives, using backward differences, are evaluated in the initial-

value plane; on the second and final step the coefficients and derivatives, now using forward differences, are evaluated in the solution plane and then averaged with the ψ terms from the first step. Equations (20), (21), and (22), along with the inlet flow angle and the equation of state $p = \rho RT$, where R is the gas constant, form a system of five equations for the five variables u , v , p , ρ , and T .

A brief description of the unit processes of this scheme is given below. The intersection of the characteristic curve through the solution point with the initial-value line in the $n = \text{constant}$ plane is determined by solving the characteristic curve equation. The coefficient $u-a$ is evaluated in the initial-value plane. The dependent variables and derivatives in the ψ terms are calculated at the intersection point using linear interpolation. Next, the compatibility equation, along with Eqs. (20) and (21) and the equation of state, are used to calculate the variables at the solution point. An iterative solution of these equations is required. Thus the first step has been used to compute all inlet mesh points. In the second step, the characteristic curve equation is solved again. Now the coefficient $u-a$ is the average of the values in the initial-value plane and the first-step solution plane. Again, linear interpolation is used to obtain the variables at the intersection point. Finally, the compatibility equation, now with averaged coefficients and ψ terms, is used along with Eqs. (20) and (21) and the equation of state to determine the final solution.

A reference-plane characteristic scheme was chosen over a bicharacteristic scheme because the increased accuracy of a bicharacteristic scheme seemed not to be worth the increased computational time for time-dependent flows.

For supersonic flow, the inlet mesh points are set equal to specified values of velocity, pressure, and density.

3. Exit Mesh Points. For subsonic flow, a reference-plane characteristic scheme similar to the inlet scheme is used. The exit pressure is specified. The characteristic relations relating the interior flow to the nozzle exit flow are Eqs. (A-41), (A-42), and (A-44). These equations can be written as

$$\left. \begin{aligned} dp - a^2 dp &= \psi_4 d\tau \\ dv &= \psi_3 d\tau \end{aligned} \right\} \quad \text{for } d\xi = u d\tau , \quad (23)$$

$$dp + \rho adu = (\psi_4 + a^2 \psi_1 + \rho a \psi_2) d\tau \quad (24)$$

$$dp + \rho adu = (\psi_4 + a^2 \psi_1 + \rho a \psi_2) d\tau \quad (25)$$

These equations are written in finite-difference form in the same manner as was done for the nozzle inlet scheme. Equations (23), (24), and (25), along with the exit pressure condition, form a system of four equations for the variables u , v , p , and ρ .

For supersonic flow, the exit mesh points are computed using linear extrapolation.

4. Wall and Centerbody Mesh Points. The wall and centerbody mesh points are also computed using a reference-plane characteristic scheme. In this scheme, the derivatives with respect to ξ are approximated, and the resulting system of equations is solved in the $\xi = \text{constant}$ reference planes. The characteristic relations for the $\xi = \text{constant}$ reference planes are given in Appendix B. The wall and centerbody contours and therefore their slopes are specified. The boundary condition is given by

$$v = u \tan \theta + \frac{\partial y_w}{\partial t} , \quad (26)$$

where θ is the local wall or centerbody angle.

The characteristic relations relating the interior flow to the flow at the nozzle wall are Eqs. (B-15), (B-16), and (B-18) in Appendix B. These equations are

$$\beta du - \alpha dv = (\beta \psi_2 - \alpha \psi_3) dt \quad (27)$$

$$\left. \begin{aligned} dp - a^2 dp &= \psi_4 dt \\ dp + \rho adu/\alpha^* + \rho \beta adv/\alpha^* &= (\psi_4 + a^2 \psi_1 \right. \quad (28)$$

$$\left. + \rho a \psi_2/\alpha^* + \rho \beta a \psi_3/\alpha^* \right) \text{ for } d\eta = (\bar{v} + \alpha^* a) dt . \quad (29)$$

These equations are written in finite-difference form in the same manner as was done for the nozzle inlet scheme. Equations (26), (27), (28), and (29) form a system of four equations for the four variables u , v , p , and ρ .

5. Exhaust Jet Boundary Mesh Points. The exhaust jet boundary mesh points are computed by the wall routine such that the pressure boundary condition

$$p = p_{\text{ambient}} \quad (30)$$

is satisfied. This is accomplished by first assuming the shape of the jet boundary and then using the wall routine to calculate the pressure. Next, the jet boundary location is slightly changed and a second pressure is computed. By use of an interpolation procedure, a new jet boundary location is determined. This interpolation-extrapolation procedure is then repeated at each point until the jet boundary pressure and the ambient pressure agree within some specified tolerance.

When an exhaust jet calculation is made, the nozzle wall exit lip mesh point becomes a singularity and, therefore, is treated by a special procedure. First, an upstream solution is computed at the exit mesh point, using the flow tangency condition as the boundary condition and backward ζ differences in both the initial-value and solution planes. Next, a downstream solution is calculated, using Eq. (30) as the boundary condition and the total conditions calculated from the upstream mesh point. The upstream solution is used when computing wall mesh points upstream of the exit mesh point, whereas the downstream solution is used when computing downstream wall mesh points. A third exit mesh point solution to be used for interior mesh point calculation is determined as follows. When the upstream solution is subsonic, the two solution Mach numbers are averaged such that the averaged Mach number is less than or equal to one. This Mach number is then used to calculate the exit mesh point solution to be used to compute the interior mesh points. When the upstream solution is supersonic, the upstream solution is used to calculate the interior mesh points.

6. Step Size. The step size Δt is controlled by the well-known Courant or C-F-L condition which can be expressed as

$$\Delta t \leq 1/[(V + a) (1/\Delta x^2 + 1/\Delta y^2)^{1/2}] , \quad (31)$$

where V is the velocity magnitude. Using Eqs. (5)

and (10), Eq. (31) can be written as

$$\Delta t \leq A/[(V + a) (1/\Delta \zeta^2 + \beta^2/\Delta \eta^2)^{1/2}] , \quad (32)$$

where the coefficient A was determined from actual calculations and varied between 0.4 and 1.6 depending on the geometry of the flow in question.

F. Overall Program

The nozzle inlet flow, as well as the flow leaving the nozzle, may be either subsonic or supersonic. The flow may contain variations in stagnation temperature and stagnation pressure from streamline to streamline. The nozzle wall and centerbody geometries may be either one of two analytical contours or a completely general tabular contour. The program is capable of calculating the exhaust jet boundary for subsonic or supersonic flow. The initial data may be read in or calculated internally by the program. The internally computed data are calculated assuming one-dimensional, steady, isentropic flow with area change. The program output includes the coordinates, velocities, pressure, density, Mach number, temperature, mass flow, and axial thrust in both English and metric units.

G. Results and Discussion

The results presented here have been published in Ref. 13. The CDC 6600 computational times represent the central processor time not including compilation. So that these results can be compared with those of other investigators, the following table of relative machine speeds is given.

Computer	Relative Machine Speed
IBM 7094	0.1
IBM 360/50	0.1
IBM 360/65	0.3
IBM 360/75	0.5
Univac 1108	0.5
CDC 6600	1.0

These relative speeds were obtained from Refs. 14 and 15 and are only rough estimates because values may vary considerably depending on the compiler and machine configuration. In each case, the one-dimensional values computed internally by the program were the initial data. When the relative change in axial velocity in the throat and downstream regions was less than a prescribed convergence tolerance, the flow was assumed to have reached steady state. The convergence tolerance was found

to be a function of the mesh spacing, flow speed, and nozzle geometry. For the results presented here, a convergence tolerance of 0.003% was used for flows without exhaust jet calculations; 0.005% for flows with exhaust jet calculations.

The present method was used to compute the steady-state solution for flow in the 45° - 15° conical, converging-diverging nozzle shown in Fig. 1a. The Mach number contours and wall pressure ratio are shown in Fig. 2. Although the code works with English and metric units, the units in the original publication of the experimental data (English) were used here. The experimental data are those of Cuffel et al.² The computed discharge coefficient is 0.983, compared with the experimental value of 0.985. The 21×8 computational mesh required 301 time planes and a computational time of 35 s. There is good agreement with the experimental data. This case was also

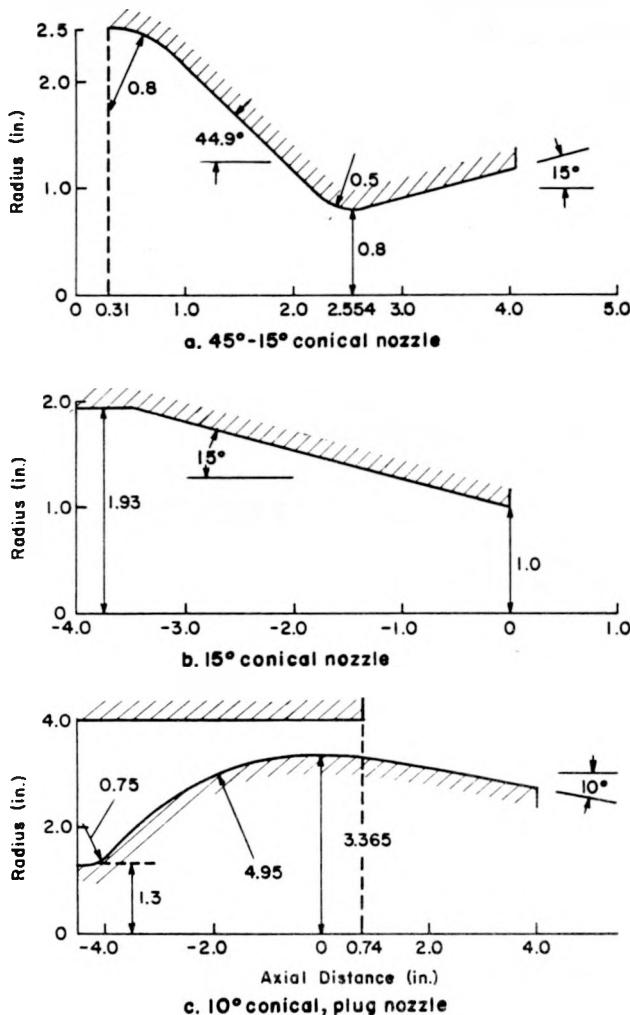


Fig. 1. Nozzle geometries.

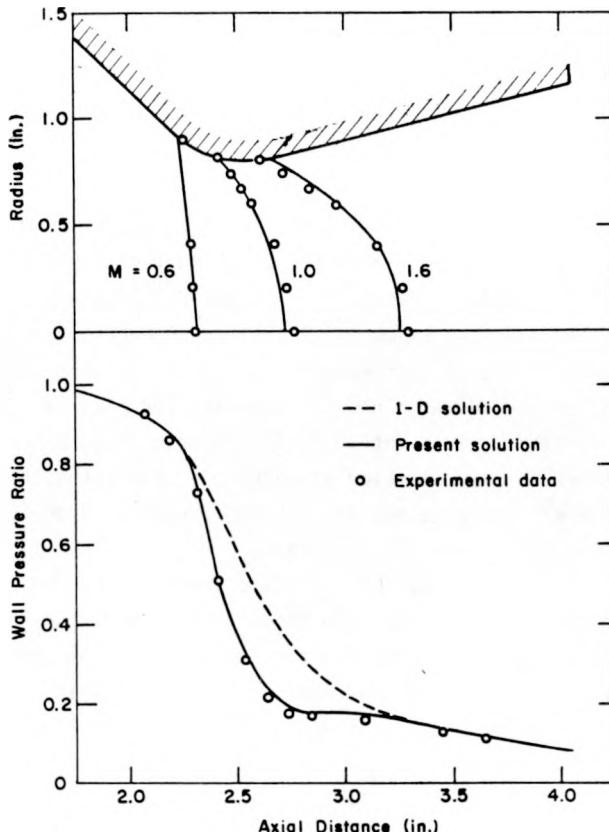


Fig. 2. Mach number contours (above) and wall pressure ratio for 45° - 15° conical nozzle.

solved by Prozan (see Ref. 2), Migdal, Laval, and Serra. The details of Prozan's computation were not reported by Cuffel et al., but Saunders reported a time of 45 min on a CDC 3200 (23×11 mesh) for computing the flow in a nozzle with a large radius of curvature. Migdal et al. reported a computational time of less than 5 min on an IBM 350/75; Laval reported a computational time on the order of 2 h on an IBM 360/50 (61×21 mesh); and Serra reported a computational time of 80 min on a Univac 1108 (3000 mesh points). This case was also solved by Prozan and Kooker,¹⁶ using a relaxation scheme to solve the steady, irrotational equations of motion. Their computational time was 5 to 10 min on an IBM 7094 (21×11 mesh).

The present method was also used to compute the steady-state flow in a 15° conical, converging nozzle. The nozzle geometry is shown in Fig. 1b. The Mach number contours and wall pressure ratio for a nozzle pressure ratio of 2.0 are shown in Fig. 3. The experimental data are those of Thornock.¹⁷ The computed discharge coefficient is 0.957, compared

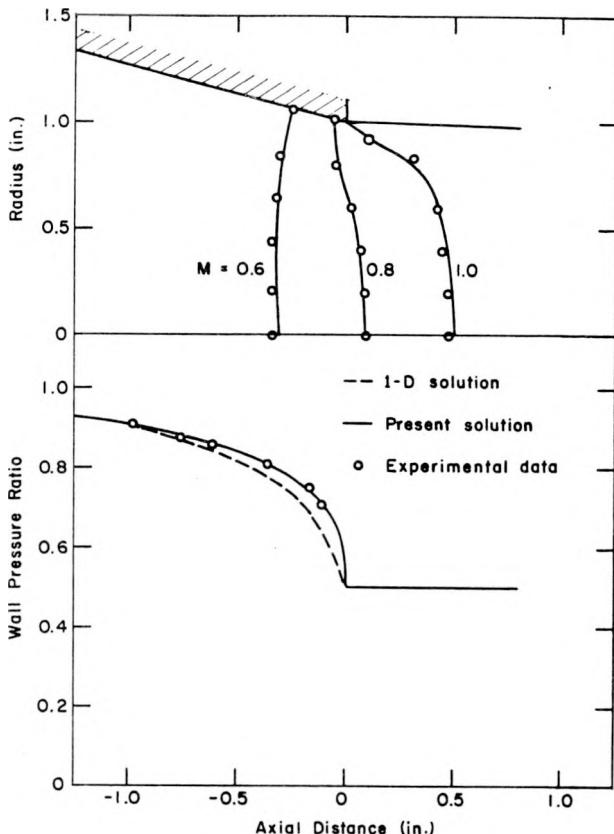


Fig. 3. Mach number contours (above) and wall pressure ratio for 15° conical nozzle.

with the experimental value of 0.960. The 23×7 computational mesh required 249 time planes and a computational time of 29 s. There is good agreement with the experimental data. This case was also solved by Wehofer and Moger and Brown and Ozcan. Wehofer and Moger's solution for a pressure ratio of 2 required over 2 h on an IBM 360/50 (47×11 mesh); Brown and Ozcan's results required 17 min on an IBM 360/65 (20×6 mesh).

Finally, the present method was used to calculate the flow in a 10° conical, plug nozzle. The nozzle geometry is shown in Fig. 1c. The Mach number contours and plug pressure ratio for a nozzle pressure ratio of 3.29 are shown in Fig. 4. The experimental data are those of Bresnahan and Johns.¹⁸ The 31×6 computational mesh required 327 time planes and a computational time of 52 s. Again, there is good agreement with the experimental data. The author is unaware of any other time-dependent analyses of plug nozzles.

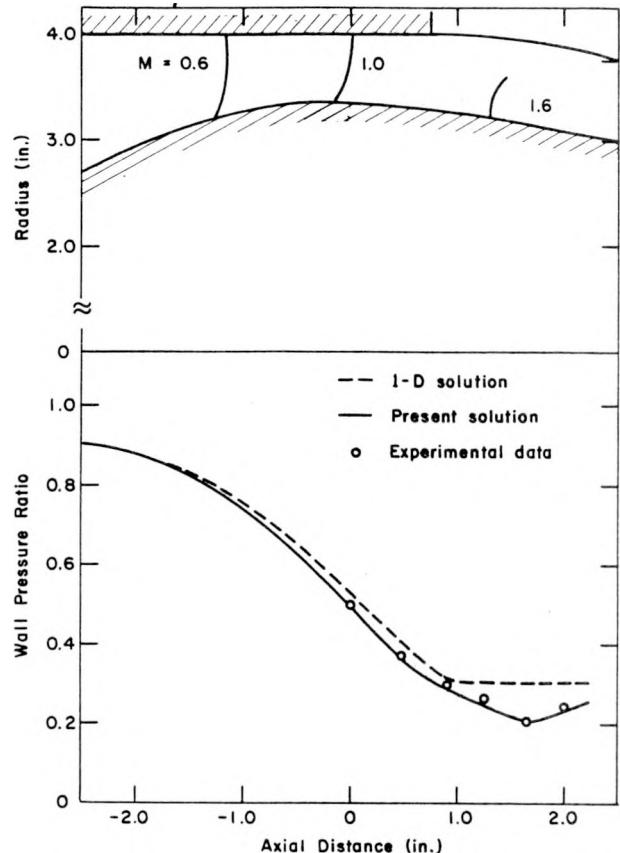


Fig. 4. Mach number contours (above) and plug pressure ratio for 10° conical plug nozzle.

H. Concluding Remarks

A method of computing nozzle flows has been presented. A production-type computer program capable of solving a wide variety of nozzle flows has been developed. The program's accuracy was demonstrated by computing the steady flow in a 45° - 15° conical, converging-diverging nozzle, a 15° conical, converging nozzle, and a 10° conical, plug nozzle. The < 1-min computational time for these steady flows is considerably faster than for any of the earlier time-dependent techniques.

II. DESCRIPTION AND USE OF THE NAP PROGRAM

A. Subroutine Description

The computer program consists of one program, one function, and twelve subroutines.

1. Program MAIN. Program MAIN initiates a run by reading in the input data. Next, the program title, abstract, and input data descriptions are printed. The program then calls subroutines GEØM and GEØMCB to calculate the nozzle geometry. The

input data are then converted to the internal units. If requested, program MAIN calls subroutine ONEDIM to calculate the one-dimensional, initial-value surface. Program MAIN then prints the initial-value surface, which includes a mass flow and thrust calculation made by subroutine MASFLØ. Next, subroutine PLØT is called and it plots the data on film. The final part of MAIN consists of the time-step loop, which performs the following operations: calculates the next time-step size; calls subroutine INTER to compute the interior mesh points; calls subroutine WALL to compute the wall mesh points; calls subroutine INLET to compute the inlet mesh points for subsonic flow; calls subroutine EXITT to compute the exit mesh points for subsonic flow; calls subroutine MASFLØ to compute the mass flow and thrust; prints the solution surface; calls subroutine PLØT to plot the data on film; checks the solution for its convergence to the steady-state solution; and punches the last solution plane on cards for restart.

2. Subroutine GEØM. Subroutine GEØM calculates the nozzle-wall coordinates and slopes for four different wall geometries: a constant area duct, a circular-arc, conical nozzle, and two tabular input nozzles. In the case of the first tabular nozzle, a completely general set of wall coordinates is input. Subroutine GEØM then calls subroutine MTLUP, which interpolates for equally spaced coordinates. Next, subroutine GEØM calls function DIF, which calculates the slopes of the equally spaced coordinates. For the second tabular nozzle, equally spaced coordinates and slopes are read in.

3. Subroutine GEØMCB. Subroutine GEØMCB calculates the nozzle centerbody coordinates and slopes for four different centerbody geometries and is the same as subroutine GEØM.

4. Subroutine MTLUP. Subroutine MTLUP was taken from the NASA Langley program library. The date of this version is 9-12-69. This subroutine is called by subroutines GEØM and GEØMCB to interpolate the nozzle-wall and centerbody coordinates for equally spaced coordinates.

5. Function DIF. Function DIF was also taken from the NASA Langley program library. The date of this version is 8-1-68. This function is called by subroutines GEØM and GEØMCB to calculate the slopes of the nozzle-wall and centerbody coordinates.

6. Subroutine ONEDIM. Subroutine ONEDIM is called by program MAIN to compute the one-dimension-

al, isentropic, initial-value surface. A Newton-Raphson scheme is used to calculate the Mach number for the area ratios, which are determined from the nozzle geometry.

7. Subroutine MAP. Subroutine MAP calculates the mapping functions that map the physical plane to a rectangular computational plane. Therefore, this subroutine is called before each mesh point is calculated.

8. Subroutine MASFLØ. Subroutine MASFLØ is called by program MAIN to calculate the mass flow and thrust for the initial-value and solution surfaces. This subroutine uses the trapezoidal rule to evaluate the mass flow and thrust integrals.

9. Subroutine PLØT. Subroutine PLØT produces velocity vector plots, and contours of density, pressure, temperature, and Mach number plots using the SC-4020 microfilm recorder. English units are used for the contour values. This subroutine uses five LASL system routines: GETQ, ADV, LINCNT, PLT, and DRV. GETQ obtains the job identification label. ADV advances the film. LINCNT indexes a specified horizontal line on each frame. PLT and DRV plot a plus sign at a specified point and draw a vector between two specified points, respectively. If this program is used on non-LASL computers, these five routines will have to be replaced by their respective counterparts on another computing system.

10. Subroutine SHØCK. Subroutine SHØCK calculates the artificial viscosity for shock computations. The artificial viscosity model is a quadratic viscosity after von Neumann-Richtmyer and has a term corresponding to all the viscous and thermal-conduction terms in the Navier-Stokes equations. In addition, this subroutine adds numerical smoothing to stabilize the calculations for very nonuniform initial-data surfaces or to accelerate the convergence to steady state.

11. Subroutine INTER. Subroutine INTER is called by program MAIN to calculate the interior mesh points. The technique used by this subroutine is the MacCormack, second-order, finite-difference scheme.

12. Subroutine WALL. Subroutine WALL is called by program MAIN to compute the wall, centerbody, and exhaust jet boundary mesh points. This subroutine uses a second-order, reference-plane characteristic scheme and also controls the inter-

pulation process for locating the exhaust jet boundary.

13. Subroutine INLET. Subroutine INLET is called by program MAIN to compute the inlet mesh points for subsonic flow. A second-order, reference-plane characteristic scheme is employed by subroutine INLET.

14. Subroutine EXITT. Subroutine EXITT is called by program MAIN to calculate the exit mesh points when the flow is subsonic. It uses a second-order, reference-plane characteristic scheme.

B. Input Data Description

The program input data is entered by a title card and five namelists. The namelists are CNTRL, IVS, GEMTRY, GCBL, and BC. The title card and each namelist are discussed below. The program will continue reading in data decks and executing them until a file mark is encountered. After each data deck is executed, the default values for the input data are restored before the next data deck is read in.

1. Title Card. The first card of each data deck is a title card consisting of 80 alphanumeric characters which identify the job. This card must always be the first card of the data deck, even if no information is specified on the card. The five namelists must appear in the order in which they are discussed below.

2. Namelist CNTRL. This namelist inputs the parameters that control the overall logic of the program.

LMAX	An integer specifying the number of mesh points in the X or axial direction (81 maximum). No default value is specified.
MMAX	An integer specifying the number of mesh points in the Y or radial direction (21 maximum). No default value is specified.
NMAX	An integer specifying the maximum number of time steps. For NMAX = 0, only the initial-data surface is computed and printed (provided NPRINT > 0). The default value is 0.
NPRINT	An integer specifying the amount of output desired. For NPRINT = N, every Nth solution plane, plus the initial-data and final solution planes, are printed. For NPRINT = -N, every Nth solution plane, plus the final solution plane, are print-

ed. For NPRINT = 0, only the final solution plane is printed. The default value is 0.

TC0NV	Specifies the axial velocity steady-state convergence tolerance in percent. If less than or equal to zero, the convergence is not checked. The default is 0.0.
FDT	A parameter that premultiplies the allowable C-F-L time step. It is desirable to use as large a value of FDT as possible without causing the computation to become unstable. Values as large as 1.6 have been used successfully for shock-free flows, while values of 0.4 to 0.6 are required for flows with shocks. The default value is 1.0.
GAMMA	Denotes the ratio of specific heats. The default value is 1.4.
RGAS	Denotes the gas constant in lbf-ft/lbm-°R if English units are used, or J/kg-°K if metric units are used. The default value is 53.35.
TSTOP	Specifies the physical time, in seconds, at which the computations will be stopped. The default value is 1.0.
IAV	An integer which, if nonzero, requests the addition of a local artificial viscosity to stabilize calculations in the vicinity of a shock. The value of FDT must be reduced to ~0.6. The default value for IAV is 0.
IUI	An integer specifying the type of units to be used for the input quantities. If IUI equals 1, English units are assumed; if equal to 2, metric units are assumed. In using any default values, make sure the values correspond to the proper units. The default value is 1.
IU0	Same as IUI except for output quantities. If IU0 equals 3, both English and metric units are printed. The default value is 1.
IPUNCH	An integer which, if nonzero, punches the last solution plane on cards for restart. The default value is 0.
NPLOT	An integer which, if greater than or equal to zero, plots both velocity vectors and contours of density, pressure,

	temperature, and Mach number on a SC-4020 microfilm recorder. For NPLOT = N, all Nth solution planes, plus the initial-data and final solution plane, are plotted. For NPLOT = 0, only the final solution plane is plotted. The default value is -1.		model. A nondimensional value is used. The default value is 0.2.
NST	An integer denoting the time step at which a small amount of numerical smoothing is stopped. This smoothing may be required to stabilize the calculations for very nonuniform initial-data surfaces. Some initial smoothing caused subsonic flows to reach steady state faster, but this was not the case for transonic and supersonic flows. The default value is 0 (no smoothing). When using the restart option, make sure NST is set equal to zero.	XLA	Denotes the coefficient c_λ in the equation for λ in the artificial viscosity model. A nondimensional value is used. The default value is 1.0.
	The remaining parameters in namelist CNTRL are less important than the parameters given above. For most nozzle flows, these remaining parameters can be left at their default values.	RKMU	Denotes the Prandtl number for the fluid used in the artificial viscosity model. The default value is 0.7.
NASM	An integer specifying which part of the flowfield is tested for steady-state convergence. For NASM = 0, the entire flowfield is tested. For NASM = 1, the transonic and supersonic (throat region to exit) regions are tested. The default value is 1.	CTA	Denotes the amount of time-averaging for the artificial viscosity. For CTA = 1.0, the values at the current time step are used. For CTA = 0.0, the values at the previous time step are used. For CTA between 0.0 and 1.0, a linear average is used. The default value is 0.5.
NAME	An integer which, when nonzero, causes the five namelists to be printed in addition to the regular output. The default value is 0.	LSS	An integer specifying the axial mesh point at which the addition of the artificial viscosity will begin. The default value is 2.
NC0NVI	An integer specifying how many times the convergence tolerance TC0NV must be satisfied on consecutive time steps before the solution is considered to have converged. The default value is 1.	PL0W	If the pressure becomes negative during a calculation, it is set equal to PL0W (psia). The default value is 0.01 psia.
IUNIT	An integer which, when equal to zero, causes the program to use either English or metric units (see IUI and IU0). For IUNIT equal to 1, a nondimensional set of units is used. The default value is 0.	R0L0W	If the density becomes negative during a calculation, it is set equal to R0L0W (lbm/ft^3). The default value is 0.0001 lbm/ft^3 .
CAV	Denotes the artificial viscosity premultiplier c in the equations for λ and μ . The default value is 4.0.	SMP	A parameter controlling the amount of smoothing (provided NST ≠ 0). The dependent variables are smoothed by the following formula:
XMU	Denotes the coefficient c_μ in the equation for μ in the artificial viscosity		$u_{L,M} = \text{SMP} * u_{L,M} + (1.0 - \text{SMP}) * (u_{L+1,M} + u_{L,M+1} + u_{L-1,M} + u_{L,M-1}) / 4.0$ The default value is 0.95.
			3. Namelist IVS. This namelist specifies the flow variables for the initial-data surface.
NID			An integer specifying the type of initial-data surface desired. For NID = 0, a two-dimensional, initial-data surface is read in. A value of U, V, P, and R0 (discussed below) must be read in for all L = 1 to LMAX and M = 1 to MMAX mesh points. For NID ≠ 0, a one-dimensional data surface is computed internally.

The following combinations are possible:

N1D = -2	subsonic	see RSTAR and RSTARS
N1D = -1	supersonic	
N1D = 1	subsonic-sonic-supersonic	No
N1D = 2	subsonic-sonic-subsonic	additional
N1D = 3	supersonic-sonic-supersonic	data is
N1D = 4	supersonic-sonic-subsonic	needed

The default value is 1.

U(L,M,1) An array denoting the X or axial direction velocity component in ft/s or m/s. For N1D = 0, U(L,M,1) must be input for L = 1 to LMAX and M = 1 to MMAX. For N1D ≠ 0, U(L,M,1) is not input. No default values are specified.

V(L,M,1) An array denoting the Y or radial direction velocity component in ft/s or m/s. See U(L,M,1) for additional information. No default values are specified.

P(L,M,1) An array denoting the pressure in psia or kPa. See U(L,M,1) for additional information. No default values are specified.

R0(L,M,1) An array denoting the density in lbm/ft^3 or kg/m^3 . See U(L,M,1) for additional information. No default values are specified.

RSTAR, RSTARS If N1D = -1 or -2, either RSTAR for planar or RSTARS for axisymmetric flow must be input. RSTAR is the area per unit depth, in inches or cm, where the Mach number is unity. RSTARS is the area divided by π , in in^2 or cm^2 , where the Mach number is unity. No default values are specified.

If the restart option is to be used, the initial run must have been made with IPUNCH ≠ 0 in CNTRL, thereby causing a new IVS deck to be punched. The new IVS replaces the one used in the initial run and includes two additional parameters, NSTART and TSTART, which denote, respectively, the time step and physical time where the solution was restarted.

When N1D ≠ 0, the initial data is calculated using one-dimensional, isentropic theory. However, the axial and radial velocity components are adjusted while keeping the magnitude constant and satisfying the flow angle. The flow angles are linearly interpolated between the slope of the wall

and centerbody.

4. Namelist GEMTRY. This namelist specifies the parameters that define the nozzle-wall contour.		
NDIM	An integer denoting the flow geometry. For NDIM = 0, two-dimensional, planar flow is assumed, and for NDIM = 1, axisymmetric flow is assumed. The default value is 1.	
NGEOM	An integer specifying one of four different nozzle-wall geometries. A discussion of these four cases follows the definitions of the additional parameters in this namelist. No default value is specified. The axial coordinate, in inches or cm, of the nozzle-wall inlet. No default value is specified.	
XI	The axial coordinate, in inches or cm, of the nozzle-wall inlet. No default value is specified.	
RI	The radial coordinate, in inches or cm, of the nozzle-wall inlet. No default value is specified.	
RT	The radial coordinate, in inches or cm, of the nozzle-wall throat. No default value is specified.	
XE	The axial coordinate, in inches or cm, of the nozzle-wall exit. No default value is specified.	
RCI	The radius of curvature, in inches or cm, of the nozzle-wall inlet. No default value is specified.	
RCT	The radius of curvature, in inches or cm, of the nozzle-wall throat. No default value is specified.	
ANGI	The angle, in degrees, of the converging section. No default value is specified.	
ANGE	The angle, in degrees, of the diverging section. No default value is specified.	
XWI	A one-dimensional array of nonequally spaced axial coordinates in inches or cm. No default values are specified.	
YWI	A one-dimensional array of radial coordinates, in inches or cm, corresponding to the axial coordinates in array XWI. No default values are specified.	
NWPTS	An integer specifying the number of entries in arrays XWI and YWI. The maximum value is 81. No default value is specified.	
IINT	An integer specifying the order of interpolation used. The maximum value is 2. The default value is 1.	

IDIF An integer specifying the order of differentiation used. The maximum value is 5. The default value is 1.

YW A one-dimensional array of radial coordinates, in inches or cm, which correspond to LMAX equally spaced axial coordinates. No default values are specified.

NXNY A one-dimensional array (floating point) of the negative of the wall slopes corresponding to the elements of YW. No default values are specified.

JFLAG An integer which, when nonzero, denotes that an exhaust jet calculation is to be carried out. The default value is 0.

LJET An integer specifying the first mesh point of the exhaust jet boundary. For example, if the nozzle wall ends at the 10th axial mesh point, LJET = 11. The program assumes that the nozzle always ends at a mesh point. No default value is specified.

The following is a discussion of the four different wall geometries considered by this program.

a. Constant area duct (NGEOM = 1). The parameters XI, RI (radius of the duct), and XE must be specified.

b. Circular-arc, conical nozzle wall (NGEOM = 2). The geometry for this case is shown in Fig. 5. The parameters XI, RI, RT, XE, RCI, RCT, ANGI, and ANGE are specified. The axial coordinate of the throat and the radius of the exit are computed internally.

c. General nozzle wall (NGEOM = 3). An arbitrary nozzle-wall contour is specified by tabular input. NWPTS axial and radial coordinate pairs are specified by the arrays XWI and YWI, respectively. For good accuracy, one coordinate pair should be the nozzle throat. The tabular data need not be equally

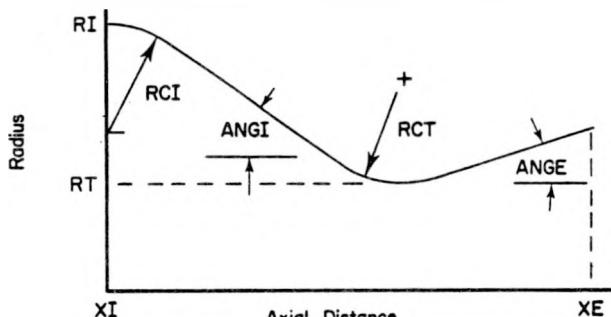


Fig. 5. Circular-arc, conical nozzle-wall geometry.

spaced. From the specified values of NWPTS, XWI, YWI, IINT, and IDIF, the program uses IINT-order interpolation to obtain LMAX equally spaced nozzle-wall contour points. Next, IDIF-order differentiation is used to obtain the nozzle-wall slope at these LMAX points.

d. General nozzle wall (NGEOM = 4). An arbitrary nozzle-wall contour is specified by tabular input. LMAX radial coordinates and the negative of their slopes are specified by the arrays YW and NXNY, respectively. These radial coordinates correspond to the LMAX equally spaced, axial mesh points. Therefore, XI and XE are input instead of each axial coordinate. For good accuracy, one pair of coordinates should be the nozzle throat.

5. Namelist GCBL. This namelist specifies the parameters that define the nozzle centerbody geometry. If no centerbody is present, this namelist is left blank but must still be present in the data deck.

NGCB An integer which, when nonzero, specifies one of four different centerbody geometries. A discussion of these four cases will follow the definitions of the additional parameters in this namelist. The default value is 0.

RICB The radial coordinate, in inches or cm, of the centerbody inlet. No default value is specified.

RTCB The radial coordinate, in inches or cm, of the centerbody maximum radius. No default value is specified.

RCICB The radius of curvature, in inches or cm, of the centerbody inlet. No default value is specified.

RCTCB The radius of curvature, in inches or cm, of the centerbody maximum radius. No default value is specified.

ANGICB The angle, in degrees, of the converging section. No default value is specified.

ANGECB The angle, in degrees, of the diverging section. No default value is specified.

XCBI A one-dimensional array of nonequally spaced axial coordinates in inches or cm. No default values are specified.

YCBI A one-dimensional array of radial coordinates, in inches or cm, corresponding to the axial coordinates in array XCBI. No default value are specified.

NCBPTS	An integer specifying the number of entries in arrays XCBI and YCBI. The maximum value is 81. No default value is specified.
IINTCB	An integer specifying the order of interpolation used. The maximum value is 2. The default value is 1.
IDIFCB	An integer specifying the order of differentiation used. The maximum value is 5. The default value is 1.
YCB	A one-dimensional array of radial coordinates, in inches or cm, which correspond to LMAX equally spaced axial coordinates. No default values are specified.
NXNYCB	A one-dimensional array (floating point) of the negative of the centerbody slopes corresponding to the elements of YCB. No default values are specified.

The following is a discussion of the four different centerbody geometries considered by this program.

- a. Cylindrical centerbody (NGCB = 1). The parameter RICB (radius of the centerbody) must be specified.
- b. Circular-arc, conical centerbody (NGCB = 2). The geometry for this case is shown in Fig. 6. The parameters RICB, RTCB, RCICB, RCTCB, ANGICB, and ANGEBCB are specified. The axial coordinate of the maximum radius and the radius of the exit are computed internally.

c. General centerbody (NGCB = 3). An arbitrary centerbody contour is specified by tabular input. NCBPTS axial and radial coordinate pairs are specified by the arrays XCBI and YCBI, respectively. The tabular data need not be equally spaced. From the specified values of NCBPTS, XCBI, YCBI, IINTCB, and IDIFCB, the program uses IINTCB-

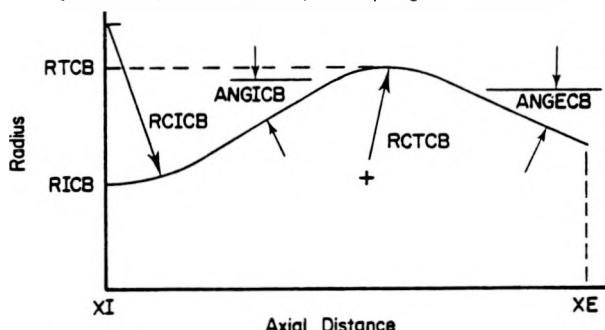


Fig. 6. Circular-arc, conical nozzle centerbody geometry.

order interpolation to obtain LMAX equally spaced centerbody contour points. Next, IDIFCB-order differentiation is used to obtain the centerbody slope at these LMAX points.

d. General centerbody (NGCB = 4). An arbitrary centerbody contour is specified by tabular input. LMAX radial coordinates and the negative of their slopes are specified by the arrays YCB and NXNYCB, respectively. These radial coordinates correspond to the LMAX equally spaced, axial mesh points.

6. Namelist BC. This namelist specifies the flow variables for the nozzle inlet and exit computational boundaries.

NSTAG	An integer which, when nonzero, denotes that variable total pressure PT, variable total temperature TT, and variable flow angle THETA (all discussed below) across the nozzle inlet have been specified. If NSTAG ≠ 0, then a value for PT, TT, and THETA must be specified at the M = 1 to MMAX points even if one or two of the variables are constant. If NSTAG = 0, only the first value for each of the three arrays needs to be specified. The default value is 0.
PT(M)	A one-dimensional array denoting the stagnation pressure, in psia or kPa, across the nozzle inlet. No default values are specified.
TT(M)	A one-dimensional array denoting the stagnation temperature, in °F or °C, across the nozzle inlet. No default values are specified.
THETA(M)	A one-dimensional array denoting the flow angle, in degrees, across the nozzle inlet. The default value is THETA(1) = 0.0, which is meaningful only when NSTAG = 0.
PE	The pressure, in psia or kPa to which the nozzle is exiting. This pressure is used to compute the nozzle exit conditions when the flow is subsonic and the exhaust jet boundary location when an exhaust jet calculation is requested. The default value is 14.7.
ISUPER	An integer which, when nonzero, specifies that the inlet flow is supersonic. For this case the boundary condition is the

	specification of the variables UI, VI, PI, and R θ I discussed below. The default value is 0.	mass flow (MASSI), and the exit mass flow (MASSE). For planar flow the mass flow units are lbm/in-s or kg/in-s and the thrust units are lb _f /in. or newtons/in. When the initial-data surface is the one-dimensional solution calculated by the program, the mass flow and thrust values are also the one-dimensional values, even though the velocity components are not.
UI(M)	A one-dimensional array denoting the axial velocity, in ft/s or m/s, across the nozzle inlet. This array, as well as the arrays VI, PI, and R θ I below, start with the centerline or centerbody value and end with the wall value. No default values are specified.	
VI(M)	Same as UI, except radial velocity.	
PI(M)	Same as UI, except pressure in psia or kPa.	
R θ I(M)	Same as UI, except density in lbm/ft ³ or kg/m ³ .	

The present version of this program allows for a maximum of 81 axial and 21 radial mesh points. To increase or decrease the maximum number of mesh points, the dimensions of the arrays QUT, QVT, and QPT in common AV, the arrays U,V,P, and R θ in common S θ LUTN, the arrays XW, YW, NXNY, XWI, and YWI in common GEMTRY, the arrays XCB, YCB, NXNYCB, XCBI, and YCBI in common GCB, the arrays PT, TT, and THETA in common BCC, the arrays UI, VI, PI and R θ I in program MAIN, the arrays YW and NXNY in subroutine GE θ MCB, and the array CQ in subroutine PL θ T must be changed to the desired values. In addition, card MAI 2950 must be changed such that LD and MD correspond to the new maximum axial and radial mesh points respectively.

C. Output Description

Program output consists of printed output, film plots, and punched cards for restart. The program has no options to output any results on magnetic tapes. For all computer-printed figures, the number zero has a slash through it, while the typed text has a slash through the letter 0.

The first page (or first two pages in the tabular input nozzle case), of output includes the program title, abstract, list of control parameters, fluid model, flow geometry, nozzle geometry, and boundary conditions.

Following the title page is the initial-data surface. This data is either data that has been input or a one-dimensional solution that has been computed by the program. All units are given. At the bottom of the initial-data surface is the mass flow at the minimum cross section (MASS), the thrust (THRUST) due to the exit momentum only, the inlet

mass flow (MASSI), and the exit mass flow (MASSE). For planar flow the mass flow units are lbm/in-s or kg/in-s and the thrust units are lb_f/in. or newtons/in. When the initial-data surface is the one-dimensional solution calculated by the program, the mass flow and thrust values are also the one-dimensional values, even though the velocity components are not. After the initial-data surface has been printed, the solution surfaces are printed. These surfaces have the same format as the initial-data surface. Each solution surface gives the flowfield for a certain value of time. As many solution planes as desired are printed by varying the input data. If the artificial viscosity option is used, a page of artificial viscosity parameters is printed before each solution plane. Also, film plots are made for each requested time step. When the computation is stopped because the flow has satisfied the convergence tolerance, the physical time equals TST θ P, or the maximum number of time steps has been reached, the final solution plane is always printed and plotted. As in the case of the initial-data surface, the mass flow and thrust are printed below the solution surface. The thrust calculation includes only the exit momentum.

D. Sample Calculations

1. Case No. 1 - Converging-Diverging Nozzle.

The nozzle geometry for this case is shown in Fig. 1a, and results are shown in Fig. 2. The data deck and printed output are presented in Figs. 7 and 8, respectively.

a. Namelist CNTRL. This case used a 21x8 mesh; therefore, LMAX = 21 and MMAX = 8. The maximum number of time steps NMAX is set equal to 400. The convergence tolerance TC θ NV is set equal to 0.003. The step-size premultiplier FDT is set equal to 1.6. The additional parameters are left equal to their default values.

b. Namelist IVS. A one-dimensional, subsonic-sonic-supersonic, initial-data surface was computed by the program; therefore, no input is required.

c. Namelist GEMTRY. For this case, the nozzle wall is a conical, converging-diverging nozzle; therefore, NGE θ M = 2. The axial location of the inlet XI equals 0.31 in., the radius of the inlet RI equals 2.5 in., the radius of the throat RT equals 0.8 in., and the axial location of the exit XE equals 4.05 in. The radius of curvature of the inlet RCI

```
CASE NO. 1 - CONVERGING-DIVERGING NOZZLE (45 DEG INLET, 15 DEG EXIT)
SCNTRL LMAX=21,MMAX=8,NMAX=400,TCONV=0.003,FDT=1.6      $
SIVS   3
SGEMTRY NGEOH=2,XI=0.31,RI=2.5,RT=0.8,XE=4.05,RCI=0.8,RCT=0.5,ANGI=44.88,
ANGE=15.0      3
SGCBL   3
$BC PT=70.0,TT=80.0      3
```

Fig. 7. Case No. 1 data deck.

NAP, A COMPUTER PROGRAM FOR THE COMPUTATION OF TWO-DIMENSIONAL, TIME-DEPENDENT, INVISCID NOZZLE FLOW
BY MICHAEL C. CLINE, T-3 - LOS ALAMOS SCIENTIFIC LABORATORY

PROGRAM ABSTRACT =

THE EQUATIONS OF MOTION FOR TWO-DIMENSIONAL, TIME DEPENDENT, INVISCID FLOW IN A NOZZLE ARE SOLVED USING THE SECOND-ORDER, MACCORMACK, FINITE-DIFFERENCE SCHEME. THE FLUID IS ASSUMED TO BE A PERFECT GAS. ALL BOUNDARY CONDITIONS ARE COMPUTED USING A SECOND-ORDER, REFERENCE PLANE CHARACTERISTIC SCHEME. THE STEADY STATE SOLUTION IS OBTAINED AS THE ASYMPTOTIC SOLUTION FOR LARGE TIME. THE NOZZLES MAY BE EITHER CONVERGING, CONVERGING-DIVERGING, OR PLUG GEOMETRIES.

JOB TITLE =

CASE NO. 1 - CONVERGING-DIVERGING NOZZLE (45 DEG INLET, 15 DEG EXIT)

CONTROL PARAMETERS =

```
LMAX=21 MMAX= 8 NMAX= 400 NPRINT= 0 TCONV= .003 FDT=1.60 NSTAG=0 NASM=1 IUNIT=0
IUI=1 IUD=1 IEX=1 NCONVIS= 1 TSTOP=1.00000 NDE= 1 NPLT= -1 IPUNCH=0 ISUPER=0
IAV=0 CAV= 5.0 XMU=1.00 XLA=0.00 RKMU= .50 CTA= .50 LSS= 2 SMP= ,95 NST= 0
```

FLUID MODEL =

THE RATIO OF SPECIFIC HEATS, GAMMA =1.4000 AND THE GAS CONSTANT, R = 53,3500 (FT-LBF/LBM-R)

FLOW GEOMETRY =

AXISYMMETRIC FLOW HAS BEEN SPECIFIED

NOZZLE GEOMETRY =

A CIRCULAR-ARC, CONICAL NOZZLE HAS BEEN SPECIFIED BY XI= ,3100 (IN), RI= 2.5000 (IN), RT= ,8000 (IN), XE= 4.0500 (IN), RCI= ,8000 (IN), RCT= ,5000 (IN), ANGI= 44.88 (DEG), AND ANGE= 15.00 (DEG). THE COMPUTED VALUES ARE XT= 2.5540 (IN) AND RE= 1.1832 (IN).

BOUNDARY CONDITIONS =

PT= 70.0000 (PSIA) T1= 80.0000 (F) THETA= 0.0000 (DEG) PE= 14.7000 (PSIA)

```
N= 10
N= 20
N= 30
N= 40
N= 50
N= 60
N= 70
N= 80
N= 90
N= 100
N= 110
N= 120
N= 130
```

Fig. 8. Case No. 1 output.

N# 140
N# 150
N# 160
N# 170
N# 180
N# 190
N# 200
N# 210
N# 220
N# 230
N# 240
N# 250
N# 260
N# 270
N# 280
N# 290
N# 300

Fig. 8 (cont)

SOLUTION SURFACE NO. 301 - TIME = .00162916 SECONDS (DELTA T = .00000541)

L	M	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBM/FT ³)	Q (FPS)	MACH NO	T (F)
1	1	.3100	0.0300	144.3320	-0.0000	69.2160	.347087	144.3320	.1269	78.2651
1	2	.3100	.3571	141.7219	-0.0000	69.2440	.347187	141.7219	.1246	78.3272
1	3	.3100	.7143	128.2883	-0.0000	69.3801	.347675	128.2883	.1128	78.6293
1	4	.3100	1.0710	109.3612	-0.0000	69.5491	.348279	109.3612	.0961	79.0040
1	5	.3100	1.4286	86.4350	-0.0000	69.7181	.348884	86.4350	.0759	79.3778
1	6	.3100	1.7857	62.2730	-0.0000	69.8536	.349368	62.2730	.0547	79.6771
1	7	.3100	2.1429	39.9999	-0.0000	69.9396	.349675	39.9999	.0351	79.8668
1	8	.3100	2.5000	19.8533	-0.0000	69.9851	.349838	19.8533	.0174	79.9672
2	1	.4970	0.0000	146.0691	0.0000	69.2904	.347208	146.0691	.1284	78.5319
2	2	.4970	.3540	143.4827	-4.4481	69.3196	.347388	143.5516	.1262	78.6038
2	3	.4970	.7000	130.0260	-8.4555	69.4507	.347845	130.3006	.1145	78.9123
2	4	.4970	1.0619	110.9310	-10.9369	69.6135	.348395	111.4688	.0979	79.3234
2	5	.4970	1.4159	87.8029	-11.7973	69.7741	.348920	88.5919	.0778	79.7545
2	6	.4970	1.7699	63.3199	-10.8059	69.8959	.349328	64.2353	.0564	80.0651
2	7	.4970	2.1239	40.7250	-8.3105	69.9730	.349708	41.5643	.0365	80.0739
2	8	.4970	2.4778	20.2377	-4.8653	70.0063	.349850	20.8143	.0183	80.1108
3	1	.6840	0.0000	153.2228	0.0000	69.1441	.346842	153.2228	.1347	78.0858
3	2	.6840	.3439	150.4176	-8.0795	69.1721	.346941	150.6344	.1325	78.1501
3	3	.6840	.6878	136.5817	-15.2234	69.2963	.347379	137.4275	.1208	78.4365
3	4	.6840	1.0317	116.4617	-19.6710	69.4572	.347946	118.1113	.1038	78.8078
3	5	.6840	1.3755	92.1280	-21.2109	69.6187	.348556	94.5382	.0831	79.1154
3	6	.6840	1.7194	66.2422	-19.7190	69.7494	.349177	69.1149	.0607	79.1672
3	7	.6840	2.0633	42.2740	-15.8931	69.8388	.349479	45.1628	.0397	79.3988
3	8	.6840	2.4072	21.3548	-11.2935	69.8902	.349784	24.1572	.0212	79.3180
4	1	.8710	0.0000	165.0230	0.0000	69.0375	.346366	165.0230	.1451	77.9945
4	2	.8710	.3243	161.8471	-12.7268	69.0718	.346482	162.3467	.1428	78.0821
4	3	.8710	.6487	148.1388	-24.0734	69.2124	.346970	150.0021	.1319	78.4187
4	4	.8710	.9739	127.6638	-31.8727	69.4034	.347638	131.5824	.1156	78.8667
4	5	.8710	1.2973	102.9220	-35.8430	69.6042	.348388	108.9846	.0957	79.2632
4	6	.8710	1.6217	76.1942	-35.2481	69.7817	.348968	83.9523	.0737	79.7398
4	7	.8710	1.9460	51.5053	-32.0512	69.9154	.349415	68.6636	.0532	80.0812
4	8	.8710	2.2703	29.4211	-28.9397	70.0166	.349804	41.2688	.0362	81.4995
5	1	1.0580	0.0000	184.0563	0.0000	68.7930	.345583	184.0563	.1628	77.3041
5	2	1.0580	.2977	180.4888	-16.5732	68.8270	.345704	181.2481	.1595	77.3811
5	3	1.0580	.5955	167.0840	-31.6930	68.9608	.346189	170.0632	.1496	77.6716
5	4	1.0580	.8932	146.2731	-42.9213	69.1497	.346899	152.4403	.1341	78.0406
5	5	1.0580	1.1989	120.6574	-49.3831	69.3592	.347728	130.3722	.1146	78.3850
5	6	1.0580	1.4887	92.4029	-49.9827	69.5637	.348495	105.0170	.0923	78.7833
5	7	1.0580	1.7864	66.3897	-46.6519	69.7342	.349073	81.0763	.0712	79.2094
5	8	1.0580	2.0841	45.6459	-45.4552	69.8646	.351093	64.4183	.0567	77.2645
6	1	1.2450	0.0000	208.6485	0.0000	68.3644	.343931	208.6485	.1838	76.5209
6	2	1.2450	.2711	204.5468	-20.3330	68.4076	.344081	205.5549	.1810	76.6265
6	3	1.2450	.5423	191.1932	-39.2038	68.5551	.344612	195.1712	.1718	76.9548
6	4	1.2450	.8134	169.6280	-54.0883	68.7762	.345419	178.0522	.1567	77.4270
6	5	1.2450	1.0845	142.5697	-63.7640	69.0343	.346336	156.1792	.1374	78.0158
6	6	1.2450	1.3557	111.6738	-65.9052	69.3100	.347214	129.8432	.1141	78.7985
6	7	1.2450	1.6260	83.9892	-64.4311	69.5343	.348057	105.0563	.0930	79.2339
6	8	1.2450	1.8979	60.8833	-60.6288	69.8047	.348123	89.9223	.0753	81.2287
7	1	1.4320	0.0000	244.4324	0.0000	67.8755	.342319	244.4324	.2155	75.1934
7	2	1.4320	.2445	239.7789	-25.3265	67.9268	.342507	241.1127	.2126	75.3031
7	3	1.4320	.4891	226.5992	-49.2547	68.0787	.343078	231.8906	.2044	75.6076
7	4	1.4320	.7336	204.3100	-69.2211	68.3138	.343971	215.7177	.1901	76.8607
7	5	1.4320	.9781	174.9460	-82.8765	68.6031	.345044	193.5836	.1705	76.6578
7	6	1.4320	1.2226	140.4528	-87.7474	68.9166	.346251	165.6098	.1458	77.2313

Fig. 8 (cont)

SOLUTION SURFACE NO. 301 - TIME = .00162916 SECONDS (DELTA T = .00000541)

L	M	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBH/FT ³)	G (FPS)	MACH NO	T (F)
7	7	1.4320	1.4672	107.5088	-85.8497	69.2024	.347372	137.6427	.1211	77.7176
7	8	1.4320	1.7117	79.2457	-78.9145	69.5794	.349485	111.8364	.0984	77.3792
8	1	1.6190	0.0000	289.8529	0.0000	66.7858	.338237	289.8529	.2561	72.9549
8	2	1.6190	.2179	284.0910	-28.5977	66.9547	.338482	286.1237	.2528	73.1195
8	3	1.6190	.4359	271.8205	-56.1340	67.0230	.339096	277.5561	.2451	73.4932
8	4	1.6190	.6538	248.8184	-80.3206	67.2999	.340096	261.4613	.2308	74.1227
8	5	1.6190	.8717	217.0973	-98.7450	67.6666	.341368	238.4991	.2103	75.0325
8	6	1.6190	1.0896	178.2156	-108.4309	68.1022	.342872	208.6098	.1838	76.1139
8	7	1.6190	1.3076	139.1469	-110.3320	68.5385	.344469	177.5810	.1563	77.0468
8	8	1.6190	1.5255	103.3920	-102.9598	69.3680	.345942	145.9131	.1279	81.2318
9	1	1.8060	0.0000	353.4364	0.0000	65.5800	.334082	353.4364	.3132	69.8416
9	2	1.8060	.1913	348.2441	-34.5414	65.6636	.334394	349.9529	.3101	70.0227
9	3	1.8060	.3826	336.6731	-68.5580	65.8359	.335051	343.5825	.3043	70.3717
9	4	1.8060	.5740	314.9155	-100.6910	66.1349	.336185	330.6213	.2927	70.9827
9	5	1.8060	.7653	282.8929	-128.3042	66.5481	.337729	310.6290	.2748	71.8578
9	6	1.8060	.9566	240.3598	-147.2737	67.8482	.339698	281.8907	.2491	72.7483
9	7	1.8060	1.1479	192.7554	-154.1167	67.6139	.341812	246.2463	.2174	73.9216
9	8	1.8060	1.3393	133.7156	-133.1567	68.7510	.346700	188.7076	.1664	75.2460
10	1	1.9930	0.0000	436.8635	0.0000	62.9419	.324223	436.8635	.3893	63.9988
10	2	1.9930	.1647	432.1713	-35.7768	63.0217	.324508	433.6496	.3864	64.1953
10	3	1.9930	.3294	423.3175	-71.8588	63.1559	.324995	429.8775	.3822	64.5243
10	4	1.9930	.4942	404.2725	-107.9751	63.4802	.325878	418.4434	.3725	65.1589
10	5	1.9930	.6589	373.7684	-142.2246	63.7957	.327237	399.9133	.3556	66.2076
10	6	1.9930	.8236	328.4187	-171.8434	64.2934	.329012	370.6682	.3292	67.4514
10	7	1.9930	.9883	264.4666	-185.0507	65.0844	.331075	322.7626	.2862	69.3341
10	8	1.9930	1.1530	173.9843	-172.3608	65.8445	.333145	244.2672	.2157	73.4752
11	1	2.1000	0.0000	549.3454	0.0000	59.7185	.312647	549.3454	.4935	55.5636
11	2	2.1000	.1381	546.9007	-38.8068	59.7792	.312892	548.2758	.4925	55.6838
11	3	2.1000	.2762	543.1126	-79.2687	59.8393	.313169	548.8669	.4930	55.7461
11	4	2.1000	.4144	534.6434	-124.1219	59.9824	.313805	548.8623	.4929	55.9318
11	5	2.1000	.5525	518.7335	-174.8851	60.2570	.314978	547.4206	.4914	56.3641
11	6	2.1000	.6906	491.7599	-234.3386	60.7072	.316985	544.7407	.4888	56.9273
11	7	2.1000	.8287	440.5535	-301.6778	61.5756	.320739	540.5643	.4844	58.1852
11	8	2.1000	.9668	392.7055	-391.1038	61.5951	.321452	554.2664	.4972	57.1991
12	1	2.3670	0.0000	703.1835	0.0000	53.3954	.280589	703.1835	.6419	39.4042
12	2	2.3670	.1195	705.4581	-30.2450	53.2708	.288114	706.1062	.6448	39.8606
12	3	2.3670	.2389	711.9606	-62.2785	52.9060	.286719	714.6793	.6533	38.0537
12	4	2.3670	.3584	724.0761	-98.6945	52.2435	.284195	730.7714	.6692	36.1859
12	5	2.3670	.4779	742.4033	-142.4451	51.1951	.288222	756.0238	.6945	33.1228
12	6	2.3670	.5974	769.8530	-199.6792	49.5354	.274167	795.3273	.7347	27.6732
12	7	2.3670	.7168	806.1904	-274.0574	47.0968	.266002	851.4989	.7946	17.8985
12	8	2.3670	.8363	926.4913	-373.6663	40.8628	.242460	999.0058	.9555	-5.1008
13	1	2.5540	0.0000	867.9594	0.0000	45.7225	.250957	867.9594	.8111	16.5731
13	2	2.5540	.1143	873.9191	-18.6820	45.4031	.257720	874.1188	.8177	15.5161
13	3	2.5540	.2266	887.6345	-37.8442	44.6459	.254760	888.4409	.8333	13.0183
13	4	2.5540	.3429	914.6763	-56.5003	43.2240	.249189	916.4197	.8640	8.1917
13	5	2.5540	.4571	958.2606	-72.0883	40.8916	.239920	961.0287	.9140	.0397
13	6	2.5540	.5714	1029.4131	-84.1867	37.0759	.224347	1032.8498	.9976	+13.9336
13	7	2.5540	.6857	1148.3074	-75.4358	38.8928	.197584	1150.7826	1.1425	-37.8082
13	8	2.5540	.8000	1368.1926	-0.0522	22.7786	.157750	1368.1926	1.4137	-70.2496
14	1	2.7410	0.0000	1057.9041	0.0000	36.0264	.210543	1057.9041	1.0231	+15.8489
14	2	2.7410	.1189	1067.8182	0.8614	35.4940	.216255	1067.8292	1.0349	-16.9857
14	3	2.7410	.2370	1089.2563	11.4080	34.3251	.211179	1089.3160	1.0609	-21.2789
14	4	2.7410	.3560	1130.3124	26.9803	32.2010	.201817	1130.6344	1.1114	-29.3362

Fig. 8 (cont)

SOLUTION SURFACE NO. 301 - TIME = .00162916 SECONDS (DELTA T = .00000541)

L	M	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBM/FT ³)	Q (FPS)	MACH NO	T (F)
14	5	2.7410	.4757	1193.1032	59.7158	28.9781	.187128	1194.5967	1.1919	-42.0154
14	6	2.7410	.5946	1286.8774	125.7866	24.3779	.165031	1293.8103	1.3210	-61.2883
14	7	2.7410	.7135	1418.7214	259.2371	18.2527	.133085	1442.2116	1.5291	-89.8075
14	8	2.7410	.8325	1505.1920	403.3150	13.9588	.108703	1558.2894	1.7074	-113.3946
15	1	2.9280	0.0000	1229.8892	0.0000	27.4208	.179803	1229.8892	1.2364	-48.2460
15	2	2.9280	.1261	1240.8800	32.2297	26.0007	.177122	1241.2985	1.2516	-50.6718
15	3	2.9280	.2522	1263.7031	67.2349	25.6518	.171356	1265.4904	1.2843	-55.9399
15	4	2.9280	.3782	1305.5670	116.1644	23.5457	.161098	1310.7247	1.3462	-65.4968
15	5	2.9280	.5043	1363.5225	186.1417	20.6584	.146475	1376.1675	1.4380	-79.3179
15	6	2.9280	.6304	1430.6074	283.8963	17.2910	.128325	1462.4280	1.5657	-96.9372
15	7	2.9280	.7565	1495.9417	379.2887	14.3497	.111752	1543.2763	1.6910	-113.4100
15	8	2.9280	.8826	1523.8676	408.1040	13.2341	.104698	1576.7956	1.7414	-118.8190
16	1	3.1150	0.0000	1379.6124	0.0000	20.5366	.146067	1379.6124	1.4447	-80.5066
16	2	3.1150	.1532	1389.4600	57.2871	20.0520	.143567	1390.6493	1.4611	-83.0081
16	3	3.1150	.2665	1409.1488	116.9047	19.0318	.138250	1413.9898	1.4964	-88.4294
16	4	3.1150	.3997	1443.4828	190.1003	17.3330	.129183	1455.9477	1.5607	-97.8448
16	5	3.1150	.5330	1485.3850	276.8617	15.2534	.117647	1510.9669	1.6476	-110.0416
16	6	3.1150	.6662	1525.9339	367.4331	13.2773	.106148	1569.5483	1.7425	-122.3815
16	7	3.1150	.7994	1549.1994	421.6142	12.1092	.098925	1605.5458	1.8819	-129.6003
16	8	3.1150	.9327	1556.6257	417.0966	11.9976	.097596	1611.5375	1.8055	-128.4656
17	1	3.3020	0.0000	1507.1046	0.0000	15.3430	.118416	1587.1046	1.6440	-110.2754
17	2	3.3020	.1404	1514.6529	77.2857	14.9337	.116398	1516.6234	1.6597	-112.5417
17	3	3.3020	.2808	1529.1232	155.3746	14.2210	.112077	1536.9967	1.6942	-117.5164
17	4	3.3020	.4212	1552.9446	242.7868	13.0110	.105050	1571.8086	1.7537	-125.6938
17	5	3.3020	.5616	1577.6060	331.4854	11.7860	.097193	1612.0556	1.8239	-134.9123
17	6	3.3020	.7020	1595.3473	493.6915	10.7335	.091068	1645.6305	1.8821	-141.8784
17	7	3.3020	.8424	1597.4021	431.4681	10.4723	.089155	1654.6318	1.8956	-142.9533
17	8	3.3020	.9828	1597.3052	427.9967	10.5899	.089340	1653.6520	1.8859	-140.0558
18	1	3.4890	0.0000	1612.0423	0.0000	11.5688	.096652	1612.0423	1.8295	-136.9232
18	2	3.4890	.1476	1616.9281	91.6926	11.3298	.095191	1619.5259	1.8433	-138.7643
18	3	3.4890	.2951	1625.8324	182.2494	10.8049	.091980	1636.0152	1.8742	-142.9296
18	4	3.4890	.4427	1639.4993	276.0081	10.0197	.087043	1662.4818	1.9240	-149.2947
18	5	3.4890	.5902	1649.7370	350.9217	9.3866	.082402	1688.3296	1.9726	-155.1532
18	6	3.4890	.7378	1651.7627	412.3465	8.9842	.080145	1702.4548	1.9965	-157.4273
18	7	3.4890	.8853	1641.7622	427.9168	9.1505	.081014	1696.6129	1.9813	-154.8662
18	8	3.4890	1.0329	1636.9946	439.1673	9.2411	.081065	1696.8121	1.9733	-152.3077
19	1	3.6760	0.0000	1704.0260	0.0000	8.8149	.079430	1704.0260	2.0085	-160.4557
19	2	3.6760	.1547	1706.2877	101.0366	8.6716	.078480	1709.2764	2.0191	-161.7878
19	3	3.6760	.3074	1709.9698	198.9763	8.3402	.076304	1721.5868	2.0445	-164.9760
19	4	3.6760	.4641	1714.2779	293.1834	7.8684	.073245	1739.1680	2.0800	-169.3052
19	5	3.6760	.6189	1712.3564	365.8767	7.6060	.071250	1751.0084	2.1043	-171.8626
19	6	3.6760	.7736	1701.0635	403.9740	7.6934	.071703	1749.1524	2.0967	-170.3935
19	7	3.6760	.9283	1685.4753	420.4454	8.0075	.073602	1737.1245	2.0679	-166.3468
19	8	3.6760	1.0830	1682.1090	450.7198	7.9878	.073040	1741.4474	2.0677	-164.8157
20	1	3.8630	0.0000	1766.6661	0.0000	6.9239	.066761	1766.8681	2.1542	-180.0643
20	2	3.8630	.1619	1767.1843	105.9000	6.8519	.066250	1770.3558	2.1615	-180.8484
20	3	3.8630	.3237	1767.0745	206.8870	6.6633	.064921	1779.1443	2.1805	-182.9639
20	4	3.8630	.4856	1765.0631	297.6374	6.4524	.063380	1789.9821	2.2020	-185.2113
20	5	3.8630	.6475	1755.9466	360.1684	6.4495	.063276	1792.5037	2.2045	-184.8822
20	6	3.8630	.8094	1740.1859	391.2931	6.7291	.065123	1783.6360	2.1787	-181.8971
20	7	3.8630	.9712	1723.3741	415.9469	7.8217	.066976	1772.8593	2.1499	-177.0232
20	8	3.8630	1.1331	1719.3424	460.6964	6.9351	.065991	1779.9942	2.1559	-176.3486
21	1	4.0500	0.0000	1629.7062	-0.0000	5.0329	.054092	1629.7062	2.3553	-208.8585
21	2	4.0500	.1690	1620.9810	110.7794	5.0322	.054012	1631.4345	2.3559	-208.5265

Fig. 8 (cont)

SOLUTION SURFACE NO. 301 - TIME = .00162916 SECONDS (DELTA T = .00000541)

L	M	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBM/FT ³)	Q (FPS)	MACH NO	T (F)
21	3	4.0500	.3381	1824.1799	214.7978	4.9865	.053538	1836.7827	2.3632	-208.6011
21	4	4.0500	.5071	1815.8484	302.0914	5.0164	.053515	1840.8054	2.3607	-206.9819
21	5	4.0500	.6761	1799.5367	354.4601	5.2938	.055301	1834.1141	2.3278	-201.6568
21	6	4.0500	.8451	1778.5083	378.6123	5.7648	.058542	1818.3617	2.2752	-194.2070
21	7	4.0500	1.0142	1761.2728	411.4485	6.0368	.060351	1808.6933	2.2456	-190.0439
21	8	4.0500	1.1832	1756.5757	478.6731	5.8824	.058942	1818.5410	2.2603	-190.6220

MASS# 3.1653 (LBM/SEC) THRUST# 172.3716 (LBF) MASSI# 3.3454 MASSE# 3.1829

equals 0.8 in., while the radius of curvature of the throat RCT equals 0.5 in. The angle of the converging section ANGI equals 44.88° , while the angle of the diverging section is 15° . No other input is required.

d. Namelist GCBL. This nozzle has no centerbody, and no input is required.

e. Namelist BC. The total pressure PT equals 70 psia and the total temperature TT equals 80°F . No other input is required.

2. Case No. 2 - Converging Nozzle. The nozzle geometry for this case is shown in Fig. 1b and results are shown in Fig. 3. The data deck and printed output are presented in Figs. 9 and 10, respectively.

a. Namelist CNTRL. This case uses a 23×7 mesh; therefore, LMAX = 23 and MMAX = 7. The maximum number of time steps NMAX is set equal to 400. The convergence tolerance TC δ NV is set equal to 0.005. The step-size premultiplier FDT is set equal to 1.4. The additional parameters are left equal to their default values.

b. Namelist IVS. No input is required because a one-dimensional, subsonic-sonic-supersonic, initial-data surface was computed by the program.

c. Namelist GEMTRY. For this case, the nozzle is a conical converging nozzle and either the NGE \varnothing M = 3 or 4 option could be used. For this case, the NGE \varnothing M = 4 option was chosen; therefore, the YW and NXNY arrays must be input. The axial location of the inlet XI equals -3.6 in. and the axial location of the exit XE equals 0.8 in. Since an exhaust jet calculation is required for convergent sonic nozzles, JFLAG is set equal to 1. The nozzle ends at the 19th axial mesh point; therefore, LJET is set equal to 20. The values of YW and NXNY for L = 20 to 23 are an initial guess of the shape of the exhaust jet. No other input is required.

d. Namelist GCBL. This nozzle has no centerbody, and no input is required.

e. Namelist BC. The total pressure PT equals 25.0 psia, the total temperature TT equals 180.0°F , and the ambient pressure to which the jet is exiting PE is 12.5 psia. No other input is required.

3. Case No. 3 - Converging-Diverging, Plug Nozzle. The nozzle geometry for this case is shown in Fig. 1c and results are shown in Fig. 4. The data deck and printed output are presented in Figs. 11 and 12, respectively.

a. Namelist CNTRL. This case used a 31 by 6 mesh; therefore, LMAX = 31 and MMAX = 6. The maximum number of time steps NMAX is set equal to 400. The convergence tolerance TC δ NV is set equal to 0.005. The step-size premultiplier FDT is set equal to 1.6. The additional parameters are left equal to their default values.

b. Namelist IVS. A one-dimensional subsonic-sonic-supersonic, initial-data surface was computed by the program; therefore, no input is required.

c. Namelist GEMTRY. For this case, the nozzle wall is a constant area duct; therefore, NGE \varnothing M is set equal to 1. The axial location of the inlet XI and exit XE are equal to -4.44 and 2.96 in., respectively. The duct radius RI is 4.0 in. Since an exhaust jet calculation is required for plug nozzles, JFLAG is set equal to 1. The duct ends at the 22nd mesh point; therefore, LJET is set equal to 23. The NGE \varnothing M = 1 option specifies a constant radius as the initial guess of the shape of the exhaust jet. No other input is required.

d. Namelist GCBL. For this case, the nozzle centerbody is a conical, converging-diverging nozzle; therefore, NGCB = 2. The radii of the inlet RICB and throat RCTCB sections are 1.3 and 3.365 in., respectively. The radii of curvature of the inlet RCICB and throat RCTCB sections are 0.75 and 4.95 in., respectively. The angles of the inlet ANGICB and exit ANGECB sections are 45.0° and 10.0° , respectively. No other input is required.

e. Namelist BC. The total pressure PT equals 100.0 psia, the total temperature TT equals 70.0°F , and the ambient pressure to which the nozzle is exiting PE is 30.4 psia. No other input is required.

ACKNOWLEDGMENT

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REFERENCES

1. L. M. Saunders, "Numerical Solution of the Flow Field in the Throat Region of a Nozzle," Brown Engineering Co. report BSVD-P-66-TN-001 (NASA CR 82601) (August 1966).
2. R. F. Cuffel, L. H. Back, and P. F. Massier, "Transonic Flow-Field in a Supersonic Nozzle with Small Throat Radius of Curvature," AIAA J. 7, 1364-1366 (July 1969).

```
CASE NO. 2 = CONVERGING NOZZLE (15 DEG INLET, PT/PE=2,0)
$CNTRL LMAX=23,MMAX=7,NMAX=480,TCONV=0.005,FDT=1.4    3
$IVS   3
$GEOMTRY NGEOH=4,XI=3,6,XE=0,8,JFLAG=1,LJET=20,
YH=1,93,1,91103,1,85744,1,80385,1,75026,1,69667,1,64308,1,58949,1,5359,
1,48231,1,42872,1,37513,1,32154,1,26795,1,21436,1,16077,1,10718,1,05359,
1,0,1,01,1,02,1,03,1,04,
NXNY=0,0,18+0,26795,4+0,05    3
$CCBL   3
$BC PT=25,0,TT=180,0,PE=12,5    3
```

Fig. 9. Case No. 2 data deck.

NAP, A COMPUTER PROGRAM FOR THE COMPUTATION OF TWO-DIMENSIONAL, TIME-DEPENDENT, INVISCID NOZZLE FLOW
BY MICHAEL C. CLINE, T-3 - LOS ALAMOS SCIENTIFIC LABORATORY

PROGRAM ABSTRACT =

THE EQUATIONS OF MOTION FOR TWO-DIMENSIONAL, TIME DEPENDENT, INVISCID FLOW IN A NOZZLE ARE SOLVED USING THE SECOND-ORDER, MACCORMACK, FINITE-DIFFERENCE SCHEME. THE FLUID IS ASSUMED TO BE A PERFECT GAS. ALL BOUNDARY CONDITIONS ARE COMPUTED USING A SECOND-ORDER, REFERENCE PLANE CHARACTERISTIC SCHEME. THE STEADY STATE SOLUTION IS OBTAINED AS THE ASYMPTOTIC SOLUTION FOR LARGE TIME. THE NOZZLES MAY BE EITHER CONVERGING, CONVERGING-DIVERGING, OR PLUG GEOMETRIES.

JOB TITLE =

CASE NO. 2 - CONVERGING NOZZLE (15 DEG INLET, PT/PE=2.0)

CONTROL PARAMETERS =

```
LMAX=23  MMAX= 7   NMAX= 400  NPRINT=  0   TCONV=.005  FDT=1.40  NSTAG=0      NASM=1    IUNIT=0
IUI=1    IUU=1    IEX=1    NCONV= 1   TSTOP=1.00000  NDE= 1   NPLOT= -1   IPUNCH=0  ISUPER=0
IAV=0    CAV= 5.0   XMU=1.00   XLA=0.00   RKMU=.50    CTA=.50   LSS= 2     SMP=.95  NST=  0
```

FLUID MODEL =

THE RATIO OF SPECIFIC HEATS, GAMMA =1.4000 AND THE GAS CONSTANT, R = 53,3500 (FT-LBF/LBM-R)

FLOW GEOMETRY =

AXISYMMETRIC FLOW HAS BEEN SPECIFIED

Fig. 10. Case No. 2 output.

NOZZLE GEOMETRY -

A GENERAL NOZZLE HAS BEEN SPECIFIED BY THE FOLLOWING PARAMETERS, XT= -.0000 (IN), RT= 1.0000 (IN),

L	XW (IN)	YW (IN)	SLOPE
1	-3.6000	1.9300	.0000
2	-3.4000	1.9110	.2680
3	-3.2000	1.8574	.2680
4	-3.0000	1.8038	.2680
5	-2.8000	1.7503	.2680
6	-2.6000	1.6967	.2680
7	-2.4000	1.6431	.2680
8	-2.2000	1.5895	.2680
9	-2.0000	1.5359	.2680
10	-1.8000	1.4823	.2680
11	-1.6000	1.4287	.2680
12	-1.4000	1.3751	.2680
13	-1.2000	1.3215	.2680
14	-1.0000	1.2679	.2680
15	-.8000	1.2144	.2680
16	-.6000	1.1608	.2680
17	-.4000	1.1072	.2680
18	-.2000	1.0536	.2680
19	0.0000	1.0000	.2680
20	.2000	1.0100	.0500
21	.4000	1.0200	.0500
22	.6000	1.0300	.0500
23	.8000	1.0400	.0500

AN EXHAUST JET CALCULATION HAS BEEN REQUESTED, THE NOZZLE ENDS AT X= -.0000 (IN), THE MESH POINTS L= 20 TO L= 23 ARE AN INITIAL APPROXIMATION TO THE EXHAUST JET BOUNDARY.

BOUNDARY CONDITIONS -

PT= 25.0000 (PSIA) TT= 180.0000 (F) THETA= 0.0000 (DEG) PE= 12.5000 (PSIA)

N# 10
N# 20
N# 30
N# 40
N# 50
N# 60
N# 70
N# 80
N# 90
N# 100
N# 110
N# 120
N# 130
N# 140
N# 150
N# 160
N# 170
N# 180
N# 190
N# 200
N# 210
N# 220
N# 230
N# 240
N# 250

Fig. 10 (cont)

SOLUTION SURFACE NO. 250 - TIME = .00158712 SECONDS (DELTA T = .00000638)

L.	M.	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBM/FT ³)	W (FPS)	MACH NO	T (F)
1	1	-3.6000	0.0000	218.2506	-0.0000	24.4617	.103809	218.2506	.1765	176.0323
1	2	-3.6000	.3217	216.3467	-0.0000	24.4710	.103837	216.3467	.1750	176.1012
1	3	-3.6000	.6433	211.0650	-0.0000	24.4963	.103914	211.0650	.1707	176.2889
1	4	-3.6000	.9650	202.4249	-0.0000	24.5363	.104035	202.4249	.1637	176.5859
1	5	-3.6000	1.2867	189.9110	-0.0000	24.5914	.104202	189.9110	.1535	176.9940
1	6	-3.6000	1.6083	174.1160	-0.0000	24.6561	.104398	174.1160	.1407	177.4720
1	7	-3.6000	1.9300	164.5359	-0.0000	24.6934	.104510	164.5359	.1329	177.7474
2	1	-3.4000	0.0000	220.5038	0.0000	24.4990	.103923	220.5038	.1783	176.3022
2	2	-3.4000	.3185	218.7400	-4.0464	24.5109	.103960	218.7783	.1769	176.3904
2	3	-3.4000	.6370	213.8199	-8.2875	24.5001	.104048	213.9805	.1730	176.6059
2	4	-3.4000	.9555	205.9606	-13.4604	24.5896	.104198	206.4000	.1668	176.9704
2	5	-3.4000	1.2740	194.7161	-20.0002	24.6637	.104423	195.7611	.1582	177.5146
2	6	-3.4000	1.5925	188.9249	-29.6254	24.7622	.104722	183.3343	.1480	178.2341
2	7	-3.4000	1.9110	174.0626	-46.6401	24.8416	.104960	180.2029	.1454	178.8254
3	1	-3.2000	0.0000	227.1668	0.0000	24.4463	.103763	227.1668	.1838	175.9150
3	2	-3.2000	.3096	225.7720	-5.3792	24.4543	.103787	225.8360	.1827	175.9741
3	3	-3.2000	.6191	221.6900	-10.9482	24.4738	.103846	221.9601	.1795	176.1190
3	4	-3.2000	.9287	215.5644	-17.4423	24.5049	.103941	216.2689	.1749	176.3485
3	5	-3.2000	1.2383	207.0481	-25.0312	24.5548	.104092	208.5557	.1686	176.7162
3	6	-3.2000	1.5479	198.1668	-35.7006	24.6088	.104257	201.3569	.1627	177.1105
3	7	-3.2000	1.8574	198.2077	-53.1097	24.6476	.104374	205.1997	.1658	177.3994
4	1	-3.0000	0.0000	235.6639	0.0000	24.4175	.103676	235.6639	.1907	175.6968
4	2	-3.0000	.3006	234.4539	-7.3429	24.4250	.103699	234.5689	.1898	175.7526
4	3	-3.0000	.6013	230.8325	-14.8498	24.4423	.103752	231.3097	.1871	175.8806
4	4	-3.0000	.9019	225.5461	-23.0375	24.4701	.103836	226.7196	.1834	176.0856
4	5	-3.0000	1.2026	218.3708	-31.7397	24.5143	.103971	220.6654	.1784	176.4092
4	6	-3.0000	1.5032	211.9665	-43.1284	24.5537	.104092	216.3096	.1749	176.6889
4	7	-3.0000	1.8038	212.2437	-56.8707	24.6007	.104231	219.7309	.1776	177.0544
5	1	-2.8000	0.0000	247.5469	0.0000	24.3459	.103458	247.5469	.2004	175.1670
5	2	-2.8000	.2917	246.5466	-8.7738	24.3526	.103479	246.7027	.1997	175.2168
5	3	-2.8000	.5834	243.3623	-17.7079	24.3666	.103521	244.0057	.1975	175.3216
5	4	-2.8000	.8751	236.7445	-27.0514	24.3904	.103594	240.2721	.1944	175.4974
5	5	-2.8000	1.1660	232.8556	-37.0282	24.4250	.103699	235.7813	.1988	175.7524
5	6	-2.8000	1.4585	227.6809	-48.4235	24.4573	.103798	232.7812	.1883	175.9860
5	7	-2.8000	1.7503	228.6649	-61.2708	24.5005	.103929	236.7314	.1914	176.3066
6	1	-2.6000	0.0000	261.7128	0.0000	24.2648	.103213	261.7128	.2119	174.5560
6	2	-2.6000	.2828	260.8302	-10.1521	24.2709	.103232	261.0277	.2114	174.6021
6	3	-2.6000	.5656	257.8653	-20.3801	24.2848	.103274	258.6694	.2094	174.7047
6	4	-2.6000	.8483	253.6428	-30.8959	24.3073	.103343	255.5175	.2069	174.8705
6	5	-2.6000	1.1311	248.3621	-41.6794	24.3390	.103440	251.8351	.2038	175.1021
6	6	-2.6000	1.4139	243.7055	-53.3241	24.3676	.103529	249.5492	.2020	175.3015
6	7	-2.6000	1.6967	244.3368	-65.4700	24.4135	.103665	252.9561	.2047	175.6627
7	1	-2.4000	0.0000	278.6913	0.0000	24.1552	.102879	278.6913	.2258	173.7395
7	2	-2.4000	.2738	271.8506	-11.4203	24.1616	.102899	278.0932	.2253	173.7883
7	3	-2.4000	.5477	275.0155	-22.8667	24.1760	.102942	275.9645	.2236	173.8962
7	4	-2.4000	.8215	270.9450	-34.4379	24.1995	.103014	273.1248	.2213	174.0711
7	5	-2.4000	1.0954	265.9299	-46.0672	24.2306	.103189	269.8906	.2186	174.3033
7	6	-2.4000	1.3692	261.3584	-57.9952	24.2601	.103199	267.7156	.2168	174.5205
7	7	-2.4000	1.6431	261.2947	-70.0139	24.3087	.103348	270.5122	.2190	174.8742
8	1	-2.2000	0.0000	298.2684	0.0000	24.0233	.102479	298.2684	.2419	172.7423
8	2	-2.2000	.2649	297.4346	-12.6689	24.0303	.102500	297.7043	.2414	172.7947
8	3	-2.2000	.5298	294.5968	-25.3010	24.0464	.102549	295.6813	.2398	172.9156
8	4	-2.2000	.7947	290.4766	-37.9156	24.0724	.102629	292.9407	.2375	173.1089
8	5	-2.2000	1.0597	285.5788	-50.3370	24.1059	.102732	289.7842	.2349	173.3559

Fig. 10 (cont)

SOLUTION SURFACE NO. 250 - TIME = .00158212 SECONDS (DELTA T = .00000638)

L	M	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBH/FT3)	Q (FPS)	MACH NO	T (F)
8	6	-2.2000	1.3246	280.4825	-62.7287	24.1385	.102833	287.4114	.2329	173.5864
8	7	-2.2000	1.5895	279.4577	-74.8807	24.1921	.102992	289.3160	.2344	174.0116
9	1	-2.0000	0.0000	320.7490	0.0000	23.8619	.101985	320.7490	.2604	171.5322
9	2	-2.0000	.2560	319.8654	-13.9317	23.8697	.102009	320.1687	.2599	171.5911
9	3	-2.0000	.5120	316.9519	-27.7697	23.8881	.102065	318.1661	.2582	171.7312
9	4	-2.0000	.7679	312.6118	-41.4462	23.9180	.102156	315.3473	.2559	171.9570
9	5	-2.0000	1.0239	307.1939	-54.7331	23.9557	.102271	312.0317	.2531	172.2427
9	6	-2.0000	1.2799	301.6978	-67.7192	23.9939	.102587	309.2046	.2508	172.5310
9	7	-2.0000	1.5359	299.5372	-80.2610	24.0541	.102574	310.1038	.2514	172.9667
10	1	-1.8000	0.0020	346.3661	0.0000	23.6682	.101395	346.3661	.2815	170.0524
10	2	-1.8000	.2471	345.3925	-15.2419	23.6768	.101421	345.7286	.2810	170.1177
10	3	-1.8000	.4941	342.3345	-30.3344	23.6978	.101486	343.6758	.2793	170.2769
10	4	-1.8000	.7412	337.6399	-45.1344	23.7321	.101591	340.6432	.2767	170.5347
10	5	-1.8000	.9882	331.7133	-59.3789	23.7754	.101724	336.9860	.2737	170.8565
10	6	-1.8000	1.2353	325.4397	-73.1379	23.8208	.101866	333.5568	.2708	171.1825
10	7	-1.8000	1.4823	321.9512	-86.2668	23.8898	.102071	333.3085	.2705	171.7416
11	1	-1.6000	0.0000	375.5134	0.0000	23.4324	.100671	375.5134	.3056	168.2648
11	2	-1.6000	.2381	374.4108	-16.6154	23.4421	.100700	374.7873	.3050	168.3393
11	3	-1.6000	.4762	371.1009	-33.0393	23.4659	.100773	372.6485	.3032	168.5224
11	4	-1.6000	.7144	366.0622	-49.0830	23.5053	.100894	369.3381	.3005	168.8245
11	5	-1.6000	.9525	359.5270	-64.4590	23.5554	.101047	365.2597	.2970	169.2101
11	6	-1.6000	1.1906	352.3245	-79.1683	23.6098	.101213	361.1097	.2936	169.6314
11	7	-1.6000	1.4287	347.3365	-93.0688	23.6904	.101465	359.5893	.2922	170.2123
12	1	-1.4000	0.0010	408.9079	0.0000	23.1479	.099799	408.9079	.3334	166.0546
12	2	-1.4000	.2292	407.6655	-18.1308	23.1585	.099832	408.0685	.3327	166.1365
12	3	-1.4000	.4584	404.2326	-36.0390	23.1845	.099912	405.8359	.3308	166.3361
12	4	-1.4000	.6876	398.6307	-53.4933	23.2283	.100047	402.2039	.3278	166.6697
12	5	-1.4000	.9168	391.3549	-70.1610	23.2850	.100224	397.5943	.3239	167.0972
12	6	-1.4000	1.1459	383.0706	-86.0187	23.3495	.100426	392.6096	.3197	167.5669
12	7	-1.4000	1.3751	376.3341	-100.8387	23.4443	.100707	389.6098	.3171	168.3548
13	1	-1.2000	0.0000	447.1313	0.0000	22.7906	.098693	447.1313	.3653	163.2986
13	2	-1.2000	.2203	445.7369	-19.6613	22.8027	.098730	446.1704	.3645	163.3940
13	3	-1.2000	.4405	442.1427	-39.1094	22.8313	.098819	443.8690	.3626	163.6186
13	4	-1.2000	.6608	436.0959	-58.1395	22.8806	.098971	439.9543	.3593	164.0057
13	5	-1.2000	.8810	428.1243	-76.4190	22.9464	.099173	434.8911	.3550	164.5264
13	6	-1.2000	1.1013	418.6672	-93.7621	23.0238	.099408	429.0379	.3500	165.1462
13	7	-1.2000	1.3215	409.9834	-109.8551	23.1400	.099777	424.4462	.3461	165.9803
14	1	-1.0000	0.0000	491.8170	0.0000	22.3572	.097356	491.8170	.4030	159.8453
14	2	-1.0000	.2113	490.2796	-21.5428	22.3701	.097396	490.7527	.4021	159.9470
14	3	-1.0000	.4226	486.6123	-42.8966	22.3991	.097487	488.4994	.4002	160.1742
14	4	-1.0000	.6340	480.2180	-63.8922	22.4504	.097647	484.4498	.3967	160.5728
14	5	-1.0000	.8453	471.4310	-84.0395	22.5213	.097870	478.8631	.3920	161.1150
14	6	-1.0000	1.0566	460.5844	-103.1474	22.6094	.098150	471.9930	.3861	161.7650
14	7	-1.0000	1.2677	449.1457	-120.3486	22.7455	.098553	464.9899	.3800	162.9506
15	1	-.8000	0.0000	543.6828	0.0000	21.7821	.095555	543.6828	.4471	155.2834
15	2	-.8000	.2024	542.0487	-22.9703	21.7965	.095600	542.5352	.4461	155.4009
15	3	-.8000	.4048	538.4690	-45.8802	21.8258	.095691	540.4200	.4443	155.6414
15	4	-.8000	.6072	531.9002	-68.7134	21.8802	.095860	536.3202	.4008	156.0874
15	5	-.8000	.8096	522.6432	-91.1922	21.9695	.096107	530.5392	.4358	156.7555
15	6	-.8000	1.0120	510.3910	-112.8464	22.0651	.096426	522.7172	.4291	157.6460
15	7	-.8000	1.2144	496.5545	-133.0518	22.2581	.097051	514.0711	.4215	159.0362
16	1	-.6000	0.0000	605.7994	0.0000	21.0913	.093395	605.7994	.5005	149.5466
16	2	-.6000	.1935	604.2591	-25.2777	21.1046	.093437	604.7876	.4997	149.6538
16	3	-.6000	.5869	601.2402	-50.6770	21.1282	.093513	603.3722	.4984	149.8407

Fig. 10 (cont)

SOLUTION SURFACE NO. 259 - TIME = .00158212 SECONDS (DELTA T = .00000638)

L	M	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBM/FT ³)	Q (FPS)	MACH NO	T (F)
16	4	-.6000	.5804	595.4506	-76.5530	21.1741	.093661	600.3513	.4958	150.2000
16	5	-.6000	.7738	586.3424	-102.2688	21.2470	.093898	595.1943	.4913	150.7570
16	6	-.6000	.9673	573.5778	-128.0177	21.3467	.094228	587.6905	.4848	151.4746
16	7	-.6000	1.1608	553.1442	-148.2150	21.5507	.094828	572.6572	.4717	153.4126
17	1	-.4000	0.0000	679.9293	0.0000	20.1120	.090272	679.9293	.5656	141.3566
17	2	-.4000	.1845	678.6968	-25.3110	20.1200	.090297	679.1686	.5649	141.4296
17	3	-.4000	.3691	676.8210	-51.0818	20.1274	.090319	678.7459	.5646	141.5005
17	4	-.4000	.5536	672.4041	-77.9199	20.1488	.090384	676.9038	.5629	141.7062
17	5	-.4000	.7381	664.7553	-106.3046	20.1967	.090527	673.2015	.5596	142.1826
17	6	-.4000	.9226	649.7730	-136.1958	20.2636	.090717	663.8933	.5516	142.9160
17	7	-.4000	1.1072	627.9869	-168.2691	20.7049	.092179	650.1400	.5386	146.2742
18	1	-.2000	0.0000	767.7202	0.0000	18.9623	.086583	767.7202	.6441	131.1364
18	2	-.2000	.1756	767.7318	-26.9237	18.9591	.086574	768.2037	.6446	131.0940
18	3	-.2000	.3512	768.7246	-55.0030	18.9365	.086506	770.6898	.6468	130.8548
18	4	-.2000	.5268	770.0819	-86.4261	18.9007	.086403	774.9165	.6506	130.4457
18	5	-.2000	.7024	770.7476	-121.8434	18.8823	.086372	780.3190	.6553	130.0779
18	6	-.2000	.8780	774.0238	-175.1882	18.7029	.085858	793.6018	.6676	127.9712
18	7	-.2000	1.0536	731.2056	-195.9265	19.2978	.087683	756.9999	.6336	134.0480
19	1	.0000	0.0000	881.7838	0.0000	17.2847	.081080	881.7838	.7499	115.4064
19	2	.0000	.1667	884.8922	-21.7872	17.2351	.080919	885.1603	.7531	114.8961
19	3	.0000	.3333	892.4690	-44.5059	17.1095	.080509	893.5780	.7611	113.6201
19	4	.0000	.5000	907.4413	-69.5616	16.8712	.079729	910.1036	.7768	111.1565
19	5	.0000	.6667	929.8310	-95.3880	16.5257	.078596	934.7109	.8004	107.5206
19	6	.0000	.8333	970.9132	-136.3203	15.7535	.076019	980.4337	.8457	99.3511
19	7	.0000	1.0000	1016.1021	-147.6067	15.2398	.074031	1026.7674	.8886	95.6104
20	1	.2000	0.0000	1001.4017	0.0000	15.3667	.074543	1001.4017	.8660	96.4174
20	2	.2000	.1659	1006.6100	-10.2280	15.2797	.074239	1086.6620	.8713	95.5332
20	3	.2000	.3310	1018.5216	-20.1734	15.0807	.073541	1018.7213	.8833	93.5037
20	4	.2000	.4977	1041.5218	-28.0663	14.7043	.072212	1041.8999	.9066	89.6199
20	5	.2000	.6637	1074.2768	-28.0371	14.1890	.070371	1074.6638	.9397	84.2341
20	6	.2000	.8296	1138.3593	-48.2369	13.1441	.066588	1139.8782	1.0067	72.7999
20	7	.2000	.9955	1193.2730	-26.9502	12.4972	.064252	1193.5773	1.0626	64.9985
21	1	.4000	0.0000	1999.4854	0.0000	13.7553	.068831	1099.4854	.9657	79.4089
21	2	.4000	.1659	1103.1248	-1.2130	13.6961	.068616	1103.1255	.9695	78.7672
21	3	.4000	.3317	1111.2973	-2.4019	13.5634	.068134	1111.2999	.9780	77.3249
21	4	.4000	.4976	1125.6585	-2.0971	13.3319	.067290	1125.6623	.9930	74.7738
21	5	.4000	.6634	1140.3012	.7380	13.1058	.066459	1140.3014	1.0083	72.2436
21	6	.4000	.8293	1163.6872	-5.5522	12.7467	.065140	1163.6873	1.0329	68.1722
21	7	.4000	.9951	1190.9668	-2.0159	12.4998	.064260	1190.9685	1.0603	65.0239
22	1	.6000	0.0000	1161.1336	0.0000	12.7426	.065154	1161.1336	1.0309	67.8962
22	2	.6000	.1660	1162.4664	1.8530	12.7227	.065079	1162.4678	1.0323	67.6732
22	3	.6000	.3320	1165.5589	3.5348	12.6768	.064908	1165.5642	1.0356	67.1596
22	4	.6000	.4980	1170.6776	4.7717	12.5978	.064612	1170.6873	1.0410	66.2712
22	5	.6000	.6640	1173.8592	7.0631	12.5493	.064427	1173.8804	1.0444	65.7481
22	6	.6000	.8299	1178.9652	7.5425	12.5091	.064270	1178.9893	1.0493	65.3489
22	7	.6000	.9959	1192.3993	4.7125	12.4965	.064249	1192.4086	1.0616	64.9867
23	1	.8000	0.0000	1222.7818	-0.0000	11.7299	.061477	1222.7818	1.0992	55.0064
23	2	.8000	.1661	1221.8079	4.9190	11.7494	.061543	1221.8178	1.0980	55.3043
23	3	.8000	.3322	1219.8205	9.4775	11.7902	.061682	1219.8573	1.0955	55.9309
23	4	.8000	.4984	1215.6967	12.4405	11.8637	.061934	1215.7603	1.0987	57.8332
23	5	.8000	.6645	1207.4172	13.4183	11.9936	.062396	1207.4918	1.0814	58.8296
23	6	.8000	.8306	1194.2432	15.6371	12.2716	.063399	1194.3456	1.0659	62.4479
23	7	.8000	.9967	1193.8317	4.7182	12.4934	.064238	1193.8410	1.0629	64.9495

MASS= 1.5757 (LB/M SEC) THRUST= 44.7800 (LBF) MASSI= 1.5915 MASSE= 1.5757

Fig. 10 (cont)

```
CASE NO. 3 = CONVERGING-DIVERGING, PLUG NOZZLE (10 DEG CONE, PT/PE=3.29)
SCNTRL LMAX=31,MMAX=6,NMAX=400,TCONV=0,005,FDT=1.6    S
37VS   S
SGEMTRY NGEOM=1,XI=-4,440,XE=2,9600,RJ=4,0,JFLAG=1,LJET=23    S
SGCBL NGCB=2,RICB=1,3,RTC=3,365,RCICB=0,75,RCTCB=4,95,
ANGICB=45,0,ANGECB=10,0    S
SBC PT=100,0,TT=70,0,PE=30,4    S
```

Fig. 11. Case No. 3 data deck.

NAP, A COMPUTER PROGRAM FOR THE COMPUTATION OF TWO-DIMENSIONAL, TIME-DEPENDENT, INVISCID NOZZLE FLOW
BY MICHAEL C. CLINE, I-3 - LOS ALAMOS SCIENTIFIC LABORATORY

PROGRAM ABSTRACT -

THE EQUATIONS OF MOTION FOR TWO-DIMENSIONAL, TIME DEPENDENT, INVISCID FLOW IN A NOZZLE ARE SOLVED USING THE SECOND-ORDER, MACCORMACK, FINITE-DIFFERENCE SCHEME. THE FLUID IS ASSUMED TO BE A PERFECT GAS. ALL BOUNDARY CONDITIONS ARE COMPUTED USING A SECOND-ORDER, REFERENCE PLANE CHARACTERISTIC SCHEME. THE STEADY STATE SOLUTION IS OBTAINED AS THE ASYMPTOTIC SOLUTION FOR LARGE TIME. THE NOZZLES MAY BE EITHER CONVERGING, CONVERGING-DIVERGING, OR PLUG GEOMETRIES.

JOB TITLE -

CASE NO. 3 - CONVERGING-DIVERGING, PLUG NOZZLE (10 DEG CONE, PT/PE=3,29)

CONTROL PARAMETERS -

```
LMAX=31  MMAX= 6  NMAX= 400  NPRINT=  0  TCONV= .005  FDT=1.60  NSTAG=0  NASM=1  IUNIT=0
IUI=1  IUD=1  IEX=1  NCONVI= 1  TSTOP=1.00000  NID= 1  NPLOT= -1  IPUNCH=0  ISUPER=0
IAV=0  CAV= 5.0  XMU=1.00  XLA=0.00  RKMU= ,50  CTA= ,50  LSS= 2  SMP= ,95  NST=  0
```

FLUID MODEL -

THE RATIO OF SPECIFIC HEATS, GAMMA =1.4000 AND THE GAS CONSTANT, R = 53.3500 (FT-LBF/LBM-R)

FLOW GEOMETRY -

AXISYMMETRIC FLOW HAS BEEN SPECIFIED

NOZZLE GEOMETRY -

A CONSTANT AREA DUCT HAS BEEN SPECIFIED BY XI= -4,4400 (IN), RI= 4,0000 (IN), AND XE= 2,9600 (IN)

AN EXHAUST JET CALCULATION HAS BEEN REQUESTED. THE NOZZLE ENDS AT X= ,7400 (IN). THE MESH POINTS L= 23 TO L= 31 ARE AN INITIAL APPROXIMATION TO THE EXHAUST JET BOUNDARY.

A CIRCULAR-ARC, CONICAL CENTERBODY HAS BEEN SPECIFIED BY XICB= -4,4400 (IN), RICB= 1,3000 (IN), RTCB= 3.3650 (IN), XECB= 2,9600 (IN), RCICB= ,7500 (IN), RCTCB= 4,9500 (IN), ANGICB= 45.00 (DEG), AND ANGECB= 10.00 (DEG). THE COMPUTED VALUES ARE XTCB= -,0140 (IN) AND RECB= 2,9170 (IN).

BOUNDARY CONDITIONS -

PT= 100.0000 (PSIA) TT= 70.0000 (F) THETA= 0.0000 (DEG) PE= 30,4000 (PSIA)

NE	10
NE	20
NE	30
NE	40
NE	50
NE	60
NE	70
NE	80

Fig. 12. Case No. 3 output.

N= 90
N= 100
N= 110
N= 120
N= 130
N= 140
N= 150
N= 160
N= 170
N= 180
N= 190
N= 200
N= 210
N= 220
N= 230
N= 240
N= 250
N= 260
N= 270
N= 280
N= 290
N= 300
N= 310
N= 320
N= 330
N= 340

Fig. 12 (cont)

SOLUTION SURFACE NO. 345 - TIME = .00237634 SECONDS (DELTA T = .00000691)

L	M	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBM/FT ³)	Q (FP9)	MACH NO	T (F)
1	1	-4.4400	1.3000	109.4812	-0.0000	99.3430	.506883	109.4812	.0971	69.0027
1	2	-4.4400	1.8400	106.0169	-0.0000	99.3831	.507029	106.0169	.0940	69.0638
1	3	-4.4400	2.3800	212.9815	-0.0000	97.5259	.500243	212.9815	.1894	66.2199
1	4	-4.4400	2.9200	236.6861	-0.0000	96.9532	.498143	236.6861	.2107	65.3351
1	5	-4.4400	3.4600	276.8857	-0.0000	95.8470	.494076	276.8857	.2468	63.6156
1	6	-4.4400	4.0000	273.4428	-0.0000	95.9570	.494481	273.4428	.2437	63.7873
2	1	-4.1933	1.3417	107.4307	37.4142	99.2108	.506393	113.7593	.1009	68.8098
2	2	-4.1933	1.8734	104.0377	29.6151	99.2062	.506362	108.1707	.0960	68.8175
2	3	-4.1933	2.4050	214.2242	22.0820	97.4455	.499962	215.3593	.1915	66.0820
2	4	-4.1933	2.9367	237.1094	13.9520	96.9338	.498071	237.5195	.2114	65.3056
2	5	-4.1933	3.4683	277.6715	7.3298	95.8509	.494092	277.7683	.2476	63.6205
2	6	-4.1933	4.0000	274.0878	0.0000	95.9535	.494468	274.0878	.2443	63.7824
3	1	-3.9467	1.4851	112.9896	98.6735	98.7348	.504664	150.0103	.1332	68.0751
3	2	-3.9467	1.9881	119.2811	55.7369	99.1459	.506168	131.6609	.1168	68.6990
3	3	-3.9467	2.4911	230.3713	50.8948	97.1220	.498801	235.9263	.2099	65.5554
3	4	-3.9467	2.9940	245.1004	28.8405	96.7471	.497390	246.7914	.2197	65.0115
3	5	-3.9467	3.4970	264.0488	15.6501	95.6688	.493423	284.4796	.2537	63.3345
3	6	-3.9467	4.0000	279.0134	0.0000	95.8206	.493979	279.0134	.2487	63.5740
4	1	-3.7000	1.7293	133.0260	133.0260	97.9867	.501924	188.1272	.1672	66.9351
4	2	-3.7000	2.1835	152.2549	70.3057	98.2987	.503055	167.7834	.1490	67.4243
4	3	-3.7000	2.6376	251.8800	69.9268	96.4944	.496505	261.4141	.2328	64.5736
4	4	-3.7000	3.0917	258.5497	37.0252	96.2556	.495578	261.1873	.2327	64.2546
4	5	-3.7000	3.5459	293.1525	20.9197	95.3831	.492369	293.8988	.2622	62.8874
4	6	-3.7000	4.0000	287.4930	0.0000	95.5579	.493011	287.4930	.2564	63.1645
5	1	-3.4533	1.9750	165.0872	159.4938	97.2086	.499081	229.5475	.2042	65.7285
5	2	-3.4533	2.3800	189.7552	88.9515	97.4650	.500033	209.5695	.1864	66.1113
5	3	-3.4533	2.7850	274.8965	86.3530	95.8902	.494289	287.3773	.2562	63.6267
5	4	-3.4533	3.1900	275.5988	45.2297	95.7240	.493625	279.2655	.2490	63.4220
5	5	-3.4533	3.5950	305.6406	25.4583	95.0148	.491013	306.7070	.2738	62.3076
5	6	-3.4533	4.0000	330.2397	0.0000	95.1903	.491657	300.2397	.2679	62.5870
6	1	-3.2067	2.1978	205.2745	173.2552	96.0735	.494909	268.6183	.2394	63.9703
6	2	-3.2067	2.5582	229.6718	104.0684	96.2531	.495595	252.1495	.2247	64.2229
6	3	-3.2067	2.9187	297.7834	94.9364	95.0783	.491294	312.5506	.2790	62.3581
6	4	-3.2067	3.2791	296.9780	50.8483	94.9696	.490842	301.2929	.2689	62.2412
6	5	-3.2067	3.6396	321.7514	27.9020	94.4542	.488941	322.9590	.2885	61.4256
6	6	-3.2067	4.0000	317.4202	0.0000	94.6142	.489529	317.4202	.2835	61.6822
7	1	-2.9600	2.3929	246.1173	182.2747	94.9109	.490626	306.2642	.2734	62.1473
7	2	-2.9600	2.7143	267.6866	117.9731	95.0919	.491347	292.5299	.2611	62.3756
7	3	-2.9600	3.0357	323.2732	100.9577	94.2213	.488127	338.6709	.3027	61.0076
7	4	-2.9600	3.3571	321.5757	56.3837	94.1319	.487751	326.4813	.2918	60.9145
7	5	-2.9600	3.6786	341.9079	29.8608	93.7507	.486340	343.2094	.3069	60.3106
7	6	-2.9600	4.0000	338.8474	0.0000	93.8859	.486837	338.8474	.3030	60.5294
8	1	-2.7133	2.5642	289.9157	188.6100	93.5079	.485435	345.8682	.3094	59.9300
8	2	-2.7133	2.8514	307.9821	127.0301	93.7199	.486292	333.4952	.2983	60.1912
8	3	-2.7133	3.1385	353.1446	104.0948	93.1129	.484817	368.1668	.3296	59.2511
8	4	-2.7133	3.4257	350.7214	60.2814	93.0513	.483748	355.8642	.3186	59.1957
8	5	-2.7133	3.7128	367.0750	30.9629	92.7906	.482778	368.3786	.3299	58.7817
8	6	-2.7133	4.0000	365.0832	0.0000	92.9035	.483193	365.0832	.3269	58.9667
9	1	-2.4667	2.7146	335.9522	191.6407	91.9380	.479603	386.7687	.3469	57.4175
9	2	-2.4667	2.9717	350.4988	134.3668	92.1960	.480650	375.3716	.3365	57.7394
9	3	-2.4667	3.2288	387.1967	105.6010	91.7925	.479105	401.3389	.3600	57.1358
9	4	-2.4667	3.4859	384.1126	63.0205	91.7586	.478944	389.2481	.3492	57.1185
9	5	-2.4667	3.7429	397.2721	31.6727	91.5882	.478304	398.5327	.3576	56.8485
9	6	-2.4667	4.0000	396.0271	0.0000	91.6830	.478654	396.0271	.3553	57.0061

Fig. 12 (cont)

SOLUTION SURFACE NO. 345 = TIME = .00237634 SECONDS (DELTA T = .00000691)

L	M	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBH/FT3)	W (FPS)	MACH NO	T (F)
10	1	-2.2200	2.8463	385.7795	192.0533	90.0749	.472645	430.9412	.3876	54.3954
10	2	-2.2200	3.0770	396.9902	137.6490	90.3795	.473882	420.1767	.3778	54.7871
10	3	-2.2200	3.3078	426.5248	105.6109	90.1440	.472945	439.4053	.3952	54.4635
10	4	-2.2200	3.5385	422.6905	64.3804	90.1463	.472923	427.5654	.3845	54.5002
10	5	-2.2200	3.7693	433.1660	31.9255	90.0516	.472562	434.3409	.3907	54.3518
10	6	-2.2200	4.0000	432.3408	0.0000	90.1354	.472872	432.3408	.3888	54.4940
11	1	-1.9733	2.9607	440.1175	189.7053	87.8573	.464311	479.2614	.4326	50.7368
11	2	-1.9733	3.1666	448.0872	138.0339	88.2164	.465769	468.8662	.4230	51.2182
11	3	-1.9733	3.3764	471.3597	104.1647	88.1287	.465373	482.7320	.4356	51.1456
11	4	-1.9733	3.5843	466.6714	64.4745	88.1745	.465519	471.1042	.4250	51.2510
11	5	-1.9733	3.7921	474.8778	31.7414	88.1431	.465393	475.9374	.4294	51.2060
11	6	-1.9733	4.0000	474.2174	0.0000	88.2221	.465686	474.2174	.4278	51.3423
12	1	-1.7267	3.0593	500.0783	184.4158	85.1723	.454142	532.9986	.4833	46.2146
12	2	-1.7267	3.2474	504.7398	135.5893	85.6008	.455882	522.6344	.4736	46.6202
12	3	-1.7267	3.4356	522.3541	101.1329	85.6519	.456001	532.0542	.4820	46.9892
12	4	-1.7267	3.6237	516.6715	63.2783	85.7507	.456353	520.5320	.4715	47.1831
12	5	-1.7267	3.8119	522.8704	31.0492	85.7759	.456442	523.7915	.4744	47.2336
12	6	-1.7267	4.0000	522.1891	0.0000	85.8554	.456738	522.1891	.4729	47.3748
13	1	-1.4800	3.1429	566.2529	175.5815	81.9333	.441756	592.8501	.5405	40.6179
13	2	-1.4800	3.3143	567.4408	130.0717	82.4540	.443870	582.1578	.5304	41.4001
13	3	-1.4800	3.4858	579.7939	96.2310	82.6443	.444521	587.7255	.5352	41.8215
13	4	-1.4800	3.6572	572.9430	60.6967	82.8076	.445125	576.1491	.5245	42.1299
13	5	-1.4800	3.8286	577.3073	29.7520	82.8869	.445422	578.0735	.5262	42.2757
13	6	-1.4800	4.0000	576.4726	0.0000	82.9705	.445737	576.4726	.5246	42.4267
14	1	-1.2333	3.2125	639.0676	162.4290	78.0504	.426727	659.3865	.6054	33.6883
14	2	-1.2333	3.3700	636.5520	121.0465	78.6926	.429342	647.9589	.5943	34.7195
14	3	-1.2333	3.5275	643.9203	89.0877	79.0292	.430567	650.0539	.5958	35.4213
14	4	-1.2333	3.6850	635.7200	56.5499	79.2706	.431485	638.2302	.5847	35.8779
14	5	-1.2333	3.8425	638.3532	27.7308	79.4040	.431995	638.9553	.5852	36.1254
14	6	-1.2333	4.0000	637.2739	0.0000	79.4949	.432340	637.2739	.5835	36.2970
15	1	-.9867	3.2685	718.4278	143.9795	73.4700	.408725	732.7132	.6786	25.1849
15	2	-.9867	3.4148	711.9765	107.8925	74.2675	.411994	720.1048	.6660	26.5599
15	3	-.9867	3.5611	714.5835	79.2171	74.7626	.413865	718.9610	.6642	27.5894
15	4	-.9867	3.7074	704.8565	50.5751	75.0970	.415164	706.6686	.6524	28.2372
15	5	-.9867	3.8537	705.8355	24.8312	75.2871	.415905	706.2721	.6518	28.6006
15	6	-.9867	4.0000	704.4402	0.0000	75.3868	.416293	704.4402	.6500	28.7919
16	1	-.7400	3.3115	803.7732	119.1784	68.1821	.387547	812.5607	.7687	14.8693
16	2	-.7400	3.4492	793.2104	89.8965	69.1705	.391649	798.2882	.7458	16.7076
16	3	-.7400	3.5869	791.2734	66.3987	69.8382	.394253	794.0294	.7408	16.1298
16	4	-.7400	3.7246	779.9013	42.4700	70.2801	.396011	781.0568	.7280	19.0199
16	5	-.7400	3.8623	779.2786	20.8999	70.5298	.397005	779.5588	.7262	19.5177
16	6	-.7400	4.0000	777.5410	0.0000	70.6408	.397439	777.5410	.7242	19.7486
17	1	-.4933	3.3417	893.9432	86.9769	62.2513	.363220	898.1644	.8519	2.6020
17	2	-.4933	3.4734	879.1927	66.3566	63.4636	.368344	881.6933	.8340	5.0490
17	3	-.4933	3.6050	873.0032	49.2059	64.3169	.371780	874.3888	.8254	6.9467
17	4	-.4933	3.7367	859.9066	31.9340	64.8781	.374068	860.4994	.8113	8.1395
17	5	-.4933	3.8683	857.7794	15.7672	65.1907	.375342	857.9243	.8083	8.7992
17	6	-.4933	4.0000	855.6361	0.0000	65.3116	.375837	855.6361	.8059	9.0498
18	1	-.2467	3.3595	987.1818	46.4557	55.8187	.336086	988.2743	.9522	-11.7118
18	2	-.2467	3.4876	968.3785	36.6601	57.2806	.342422	969.0721	.9303	-8.4827
18	3	-.2467	3.6157	958.2832	28.1325	58.3275	.346782	958.6961	.9179	-6.8113
18	4	-.2467	3.7438	943.5326	18.7218	59.0161	.349673	943.7183	.9020	-4.4493
18	5	-.2467	3.8719	939.9736	9.3489	59.3931	.351253	940.0201	.8976	-3.6020
18	6	-.2467	4.0000	937.6150	0.0000	59.5321	.351811	937.6150	.8950	-3.2594

Fig. 12 (cont)

SOLUTION SURFACE NO. 345 - TIME = .00237634 SECONDS (DELTA T = .00000691)

L	M	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBM/FT ³)	Q (FPS)	MACH NO	T (F)
19	1	.00000	3.3650	1081.4350	-3.0549	49.1261	.306824	1081.4393	1.0612	-27.8336
19	2	.00001	3.4920	1058.8194	.3966	50.8497	.314533	1058.8195	1.0340	-23.6353
19	3	.00000	3.6190	1045.3491	2.5186	52.0884	.319889	1045.3522	1.0172	-20.4885
19	4	.00000	3.7460	1029.0488	2.6347	52.9016	.323416	1029.0521	.9990	-18.4954
19	5	.00000	3.8730	1024.3133	1.4601	53.3412	.325514	1024.3143	.9932	-17.4236
19	6	.00000	4.0000	1020.9992	0.0000	53.4719	.325911	1020.9992	.9897	-17.1525
20	1	.2467	3.3581	1173.1244	-61.8584	42.3494	.276131	1174.7541	1.1778	-46.0380
20	2	.2467	3.4865	1148.0302	-42.2793	44.3423	.285382	1148.8084	1.1403	-40.6080
20	3	.2467	3.6149	1132.0781	-26.9501	45.7752	.291831	1132.3988	1.1227	-36.6236
20	4	.2467	3.7433	1114.2692	-15.5124	46.7326	.296129	1114.3772	1.1014	-34.0414
20	5	.2467	3.8716	1107.7929	-6.9782	47.2613	.298489	1107.8149	1.0932	-32.6288
20	6	.2467	4.0000	1107.0192	0.0000	47.5041	.299451	1107.0192	1.0913	-31.8133
21	1	.4933	3.3389	1269.0032	-130.7462	35.7235	.244355	1275.7208	1.3101	-65.3967
21	2	.4933	3.4711	1238.3914	-93.2116	37.9196	.255030	1241.8944	1.2646	-58.6706
21	3	.4933	3.6034	1219.8855	-62.9528	39.5784	.262856	1221.5088	1.2360	-53.5867
21	4	.4933	3.7356	1200.0219	-39.8646	40.7549	.268366	1200.6576	1.2097	-50.0979
21	5	.4933	3.8678	1193.6524	-20.1323	41.3780	.271285	1193.8222	1.2002	-48.3097
21	6	.4933	4.0000	1179.4275	0.0000	41.3454	.271483	1179.4275	1.1867	-48.9338
22	1	.7400	3.3072	1331.6916	-205.2378	30.9496	.220443	1347.4142	1.4120	-81.0462
22	2	.7400	3.4458	1305.5170	-155.2045	32.8860	.230385	1314.7103	1.3663	-74.7132
22	3	.7400	3.5843	1288.8579	-111.5273	34.4362	.238202	1293.6743	1.3360	-69.7912
22	4	.7400	3.7229	1272.2609	-71.9720	35.4028	.243148	1274.2950	1.3113	-66.9984
22	5	.7400	3.8614	1267.2158	-32.7531	35.8114	.245264	1267.6390	1.3026	-65.8919
22	6	.7400	4.0000	1266.7778	0.0000	35.2207	.241585	1286.7778	1.3233	-66.4902
23	1	.9867	3.2649	1383.2720	-243.9082	27.2685	.201293	1404.6112	1.4984	-94.3544
23	2	.9867	3.4123	1374.5314	-187.5136	28.2471	.206581	1387.2628	1.4731	-98.9272
23	3	.9867	3.5596	1374.0087	-128.3918	28.8864	.209959	1380.0740	1.4609	-88.6462
23	4	.9867	3.7070	1372.0843	-67.7226	29.0913	.210905	1373.7546	1.4524	-87.6901
23	5	.9867	3.8543	1375.5143	-12.7883	29.2328	.211388	1375.5738	1.4524	-86.7353
23	6	.9867	4.0016	1355.3965	9.0228	30.4018	.217243	1355.4266	1.4227	-82.2707
24	1	1.2333	3.2214	1434.0378	-252.8596	24.1425	.184583	1456.1601	1.5809	-106.9657
24	2	1.2333	3.3752	1436.4195	-196.1252	24.5272	.186714	1449.7469	1.5706	-105.4328
24	3	1.2333	3.5291	1402.6305	-135.8278	24.8334	.188222	1449.0107	1.5664	-103.8817
24	4	1.2333	3.6829	1429.7078	-89.7732	25.6828	.192670	1432.5235	1.5486	-100.2039
24	5	1.2333	3.8367	1397.4981	-69.4626	27.0136	.203959	1399.2234	1.4878	-91.9200
24	6	1.2333	3.9985	1354.6985	-61.0675	30.3938	.217202	1356.0742	1.4234	-82.2982
25	1	1.4800	3.1779	1401.9167	-261.3019	21.3229	.168627	1504.7777	1.6616	-118.6924
25	2	1.4800	3.3359	1482.1869	-207.8316	21.7522	.171088	1496.6810	1.6481	-116.8278
25	3	1.4800	3.4939	1474.3214	-165.8729	22.0291	.177072	1483.6231	1.6224	-112.0096
25	4	1.4800	3.6519	1433.9630	-149.1645	25.1620	.189852	1441.7004	1.5549	-102.2670
25	5	1.4800	3.8098	1392.5720	-137.2705	27.8314	.204048	1399.3228	1.4877	-91.8457
25	6	1.4800	3.9678	1349.1683	-124.2698	30.4025	.217246	1354.8794	1.4221	-82.2663
26	1	1.7267	3.1344	1509.8281	-266.2235	20.0212	.161484	1533.1197	1.7096	-125.3505
26	2	1.7267	3.2942	1499.4577	-251.5096	20.6565	.165113	1520.4047	1.6878	-122.3211
26	3	1.7267	3.4540	1403.9559	-241.1145	22.8440	.177299	1483.6789	1.6230	-112.2279
26	4	1.7267	3.6137	1417.7407	-227.3863	25.5073	.191743	1435.8471	1.5457	-100.9358
26	5	1.7267	3.7735	1380.4098	-207.8969	27.9914	.204894	1395.9772	1.4830	-91.2585
26	6	1.7267	3.9333	1342.5048	-187.8490	30.4071	.217269	1355.5834	1.4228	-82.2483
27	1	1.9733	3.0909	1459.0269	-257.2658	22.5791	.175554	1481.5348	1.6221	-112.8446
27	2	1.9733	3.2505	1447.6522	-284.2170	22.7877	.176792	1475.2885	1.6135	-112.0919
27	3	1.9733	3.4101	1421.8776	-293.0628	24.3402	.185340	1451.7650	1.5730	-105.5272
27	4	1.9733	3.5696	1394.0753	-279.9659	26.1367	.195040	1421.9095	1.5251	-90.2955
27	5	1.9733	3.7292	1365.8397	-260.7981	28.2135	.206032	1390.5157	1.4754	-90.3841
27	6	1.9733	3.8888	1334.1585	-240.7433	30.4107	.217288	1355.7051	1.4229	-82.2369

Fig. 12 (cont)

SOLUTION SURFACE NO. 345 - TIME = .00237634 SECONDS (DELTA T = .00000691)

L	M	X (IN)	Y (IN)	U (FPS)	V (FPS)	P (PSIA)	RHO (LBM/FT ³)	Q (FPS)	MACH NO	T (F)
28	1	2.2200	3.0475	1410.7945	-248.7612	25.4098	.192169	1432.5583	1.5469	=103.1005
28	2	2.2200	3.2047	1406.2072	-302.8893	25.0046	.189801	1438.4577	1.5561	=104.4101
28	3	2.2200	3.3620	1391.8446	-333.8577	25.5297	.192227	1431.3254	1.5421	=101.5240
28	4	2.2200	3.5193	1370.4248	-334.0730	26.7231	.198370	1410.5562	1.5090	=96.3879
28	5	2.2200	3.6766	1346.7431	-320.5242	28.5479	.207844	1384.3600	1.4667	=89.2631
28	6	2.2200	3.8339	1317.7933	-293.3750	30.3985	.217221	1350.0549	1.4170	=82.2726
29	1	2.4667	3.0040	1291.9779	-227.8106	32.9470	.231216	1311.9087	1.3646	=75.3852
29	2	2.4667	3.1572	1303.0941	-283.3728	31.6862	.224897	1333.5495	1.3950	=79.7104
29	3	2.4667	3.3104	1313.7524	-335.5893	30.4038	.218006	1355.9372	1.4256	=83.5673
29	4	2.4667	3.4637	1313.3000	-362.5924	29.0082	.214542	1362.4354	1.4352	=84.9830
29	5	2.4667	3.6169	1309.8925	-363.4159	30.1072	.215866	1359.3710	1.4292	=83.5434
29	6	2.4667	3.7702	1315.1981	-339.5192	30.3952	.217210	1358.3149	1.4257	=82.2946
30	1	2.7133	2.9605	1194.3369	-210.5938	40.0065	.264795	1212.7615	1.2251	=52.1976
30	2	2.7133	3.1101	1210.9114	-238.5102	38.6329	.258294	1234.1772	1.2530	=56.2885
30	3	2.7133	3.2598	1240.8253	-278.4410	36.0241	.245565	1271.6827	1.3037	=64.0377
30	4	2.7133	3.4095	1267.3081	-314.9771	33.3000	.232040	1305.8638	1.3535	=72.6441
30	5	2.7133	3.5591	1293.9764	-334.6486	31.3972	.222419	1336.5495	1.3968	=78.9811
30	6	2.7133	3.7088	1306.3885	-325.0857	30.3957	.217212	1346.2286	1.4130	=82.2909
31	1	2.9600	2.9170	1096.6960	-193.3771	47.0660	.298373	1113.6143	1.1009	=30.2290
31	2	2.9600	3.0631	1118.7287	-193.6476	45.5797	.291692	1135.3648	1.1278	=30.2301
31	3	2.9600	3.2092	1167.8982	-221.2927	41.6444	.273125	1188.6785	1.1953	=48.4494
31	4	2.9600	3.3552	1221.3161	-267.3618	36.7919	.249537	1250.2381	1.2785	=62.0356
31	5	2.9600	3.5013	1278.0603	-305.8814	32.6871	.228973	1314.1543	1.3657	=74.6800
31	6	2.9600	3.6474	1297.5788	-322.8935	30.3963	.217213	1337.1503	1.4035	=82.2872

MASS= 33.9930 (LBM/SEC) THRUST= 1353.5464 (LBF) MASSI= 34.5377 MASSE= 33.8257

SEJ

Fig. 12 (cont)

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APPENDIX A

ETA CONSTANT REFERENCE PLANE CHARACTERISTIC RELATIONS

I. EQUATIONS OF MOTION

The equations of motion, Eqs. (6) through (9), can be written as

$$\rho_{\tau} + up_{\zeta} + pu_{\zeta} = -\bar{v}\rho_{\eta} - \rho au_{\eta} - \rho\beta v_{\eta} - \epsilon\rho v\beta/\eta, \quad (A-1)$$

$$u_{\tau} + uu_{\zeta} + p_{\zeta}/\rho = -\bar{v}u_{\eta} - \alpha p_{\eta}/\rho, \quad (A-2)$$

$$v_{\tau} + uv_{\zeta} = -\bar{v}v_{\eta} - \beta p_{\eta}/\rho, \quad (A-3)$$

$$p_{\tau} + up_{\zeta} - a^2 (\rho_{\tau} + up_{\zeta}) = -\bar{v}p_{\eta} + a^2 \bar{v}\rho_{\eta}. \quad (A-4)$$

$$\psi_1 = -\bar{v}\rho_{\eta} - \rho au_{\eta} - \rho\beta v_{\eta} - \epsilon\rho v\beta/\eta, \quad (A-5)$$

$$\psi_2 = -\bar{v}u_{\eta} - \alpha p_{\eta}/\rho, \quad (A-6)$$

$$\psi_3 = -\bar{v}v_{\eta} - \beta p_{\eta}/\rho, \quad (A-7)$$

$$\psi_4 = -\bar{v}p_{\eta} + a^2 \bar{v}\rho_{\eta}, \quad (A-8)$$

Eqs. (A-1) through (A-4) become

$$\rho_{\tau} + up_{\zeta} + pu_{\zeta} = \psi_1, \quad (A-9)$$

$$u_{\tau} + uu_{\zeta} + p_{\zeta}/\rho = \psi_2, \quad (A-10)$$

Letting

$$v_\tau + uv_\zeta = \psi_3, \quad (A-11)$$

$$p_\tau + up_\zeta - a^2 p_\tau - a^2 u p_\zeta = \psi_4. \quad (A-12)$$

II. CHARACTERISTIC CURVES

A linear combination of the equations of motion can be formed by multiplying Eqs. (A-9) through (A-12) by ℓ_i , $i = 1, 2, 3, 4$, respectively, and then summing them. This linear combination can be written as

$$\begin{aligned} & \ell_1 (p_\tau + up_\zeta + pu_\zeta - \psi_1) \\ & + \ell_2 (u_\tau + uu_\zeta + p_\zeta/p - \psi_2) + \ell_3 (v_\tau + uv_\zeta - \psi_3) \\ & + \ell_4 (p_\tau + up_\zeta - a^2 p_\tau - a^2 u p_\zeta - \psi_4) = 0. \end{aligned} \quad (A-13)$$

Rearrangement of Eq. (A-13) yields

$$\begin{aligned} & (u\ell_1 - a^2 u\ell_4) p_\zeta + (\ell_1 - a^2 \ell_4) p_\tau + (\rho\ell_1 + u\ell_2) u_\zeta \\ & + \ell_2 u_\tau + u\ell_3 v_\zeta + \ell_3 v_\tau + (\ell_2/p + u\ell_4) p_\zeta + \ell_4 p_\tau \\ & = \ell_1 \psi_1 + \ell_2 \psi_2 + \ell_3 \psi_3 + \ell_4 \psi_4. \end{aligned} \quad (A-14)$$

The following set of vectors can be defined, where the components are the coefficients of the partial derivatives in Eq. (A-14).

$$W_1 = (u\ell_1 - a^2 u\ell_4, \ell_1 - a^2 \ell_4), \quad (A-15)$$

$$W_2 = (\rho\ell_1 + u\ell_2, \ell_2), \quad (A-16)$$

$$W_3 = (u\ell_3, \ell_3), \quad (A-17)$$

$$W_4 = (\ell_2/p + u\ell_4, \ell_4). \quad (A-18)$$

Therefore, Eq. (A-14) can be written as

$$\begin{aligned} & d_{W_1} p + d_{W_2} u + d_{W_3} v + d_{W_4} p \\ & = \ell_1 \psi_1 + \ell_2 \psi_2 + \ell_3 \psi_3 + \ell_4 \psi_4, \end{aligned} \quad (A-19)$$

where $d_{W_i} \rho$ is defined as the derivative of ρ in the direction of the vector W_i , etc.

A question is now posed: Can the ℓ_i , $i = 1, 2, 3, 4$, be chosen such that the vectors W_j , $j = 1, 2, 3, 4$, would be linearly dependent or, in other words, would lie in one direction. If such ℓ_i do exist, the curve which contains the vectors W_j is called the characteristic curve, its normal N is called the characteristic normal, and Eq. (A-19) is called the compatibility equation. Therefore, if $N = (N_\zeta, N_\tau)$ is the characteristic normal in the $\zeta-\tau$ plane, N and W_j are related by

$$N \cdot W_j = 0 \quad (j = 1, 2, 3, 4). \quad (A-20)$$

When Eq. (A-20) is expanded,

$$(u\ell_1 - a^2 u\ell_4) N_\zeta + (\ell_1 - a^2 \ell_4) N_\tau = 0, \quad (A-21)$$

$$(\rho\ell_1 + u\ell_2) N_\zeta + \ell_2 N_\tau = 0, \quad (A-22)$$

$$u\ell_3 N_\zeta + \ell_3 N_\tau = 0, \quad (A-23)$$

$$(\ell_2/p + u\ell_4) N_\zeta + \ell_4 N_\tau = 0. \quad (A-24)$$

In matrix form, Eqs. (A-21) through (A-24) become

$$\left| \begin{array}{cccc} uN_\zeta + N_\tau & 0 & 0 & -a^2(uN_\zeta + N_\tau) \\ pN_\zeta & uN_\zeta + N_\tau & 0 & 0 \\ 0 & 0 & uN_\zeta + N_\tau & 0 \\ 0 & N_\zeta/p & 0 & uN_\zeta + N_\tau \end{array} \right| \left| \begin{array}{c} \ell_1 \\ \ell_2 \\ \ell_3 \\ \ell_4 \end{array} \right| = 0. \quad (A-25)$$

Equation (A-25) is a system of homogeneous equations. For Eq. (A-25) to have a nontrivial solution, the coefficient matrix must be singular; in other words, its determinant must equal zero. Setting the determinant equal to zero yields

$$(uN_\zeta + N_\tau)^2 [(uN_\zeta + N_\tau)^2 - a^2 N_\zeta^2] = 0. \quad (A-26)$$

Setting the first factor of Eq. (A-26) equal to zero yields

$$uN_\zeta + N_T = 0 . \quad (A-27)$$

Setting the second factor of Eq. (A-26) equal to zero yields

$$uN_\zeta + N_T = \pm aN_\zeta . \quad (A-28)$$

Noting that $d\zeta/d\tau = -N_T/N_\zeta$, Eqs. (A-27) and (A-28) can be written as

$$d\zeta/d\tau = u , \quad (A-29)$$

$$d\zeta/d\tau = u \mp a . \quad (A-30)$$

Equation (A-29) represents the projection of the flow pathlines on the $\eta = \text{constant}$ planes. Equation (A-30) represents the projection of the Mach cones on the $\eta = \text{constant}$ planes.

III. SOLUTION FOR THE ℓ_i

If the compatibility equation (A-19) is to be used, the arbitrary parameters ℓ_i must be evaluated in the following manner. Consider first the characteristic curve given by Eq. (A-27). Substituting Eq. (A-27) into Eq. (A-25) yields

$$\begin{vmatrix} 0 & 0 & 0 & 0 \\ \rho N_\zeta & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & N_\zeta/\rho & 0 & 0 \end{vmatrix} \begin{vmatrix} \ell_1 \\ \ell_2 \\ \ell_3 \\ \ell_4 \end{vmatrix} = 0 . \quad (A-31)$$

Since the rank of the coefficient matrix of Eq. (A-31) is two, there are two independent solutions for ℓ_i . From Eq. (A-31),

$$\ell_1 = \ell_2 = 0, \ell_3 \text{ and } \ell_4 \text{ are arbitrary.} \quad (A-32)$$

Therefore, two possible solutions are

$$\ell_1 = \ell_2 = \ell_3 = 0, \ell_4 = 1 , \quad (A-33)$$

$$\ell_1 = \ell_2 = \ell_4 = 0, \ell_3 = 1 . \quad (A-34)$$

Consider next the characteristic curve given by Eq. (A-28). Substituting Eq. (A-28) into Eq. (A-25) yields

$$\begin{vmatrix} \pm aN_\zeta & 0 & 0 & \mp a^3 N_\zeta \\ \rho N_\zeta & \pm aN_\zeta & 0 & 0 \\ 0 & 0 & \pm aN_\zeta & 0 \\ 0 & N_\zeta/\rho & 0 & \pm aN_\zeta \end{vmatrix} \begin{vmatrix} \ell_1 \\ \ell_2 \\ \ell_3 \\ \ell_4 \end{vmatrix} = 0 . \quad (A-35)$$

Since the rank of the coefficient matrix of Eq. (A-35) is three, there is only one independent solution for ℓ_i . From Eq. (A-35),

$$\ell_3 = 0, \ell_1 = a^2 \ell_4, \ell_2 = \mp \rho a \ell_4 . \quad (A-36)$$

Therefore, one possible solution is

$$\ell_1 = a^2, \ell_2 = \mp \rho a, \ell_3 = 0, \ell_4 = 1 . \quad (A-37)$$

IV. COMPATIBILITY EQUATIONS

Substituting Eqs. (A-33) and (A-34) into Eq. (A-14) yields

$$p_T + up_\zeta - a^2 (\rho_T + up_\zeta) = \psi_4 , \quad (A-38)$$

$$v_T + uv_\zeta = \psi_3 . \quad (A-39)$$

Substituting Eq. (A-37) into Eq. (A-14) yields

$$\begin{aligned} a^2(\rho_T + up_\zeta + pu_\zeta - \psi_1) \mp \rho a (u_T + uu_\zeta + p_\zeta/\rho - \psi_2) \\ + p_T + up_\zeta - a^2 (\rho_T + up_\zeta) - \psi_4 = 0 . \end{aligned} \quad (A-40)$$

Equations (A-38) through (A-40) can be written as

$$dp - a^2 dp = \psi_4 d\tau \quad \left. \begin{array}{l} \text{for } d\zeta = u dt , \\ dv = \psi_3 dt \end{array} \right\} \quad (A-41)$$

$$dv = \psi_3 dt \quad (A-42)$$

$$dp - \rho adu = (\psi_4 + a^2 \psi_1 - \rho a \psi_2) dt \quad \left. \begin{array}{l} \text{for } d\zeta = (u-a)dt , \\ dp + \rho adu = (\psi_4 + a^2 \psi_1 + \rho a \psi_2) dt \end{array} \right\} \quad (A-43)$$

$$dp + \rho adu = (\psi_4 + a^2 \psi_1 + \rho a \psi_2) dt \quad \left. \begin{array}{l} \text{for } d\zeta = (u+a)dt . \\ \text{for } d\zeta = (u+a)dt . \end{array} \right\} \quad (A-44)$$

APPENDIX B
ZETA CONSTANT REFERENCE PLANE CHARACTERISTIC RELATIONS

I. EQUATIONS OF MOTION

The equations of motion, Eqs. (6) through (9), can be written as

$$\rho_{\tau} + \bar{v}\rho_{\eta} + \rho\alpha u_{\eta} + \rho\beta v_{\eta} = -up_{\zeta} - \rho u_{\zeta} - \epsilon\rho v\beta/\eta , \quad (B-1)$$

$$u_{\tau} + \bar{v}u_{\eta} + \alpha p_{\eta}/\rho = -uu_{\zeta} - p_{\zeta}/\rho , \quad (B-2)$$

$$v_{\tau} + \bar{v}v_{\eta} + \beta p_{\eta}/\rho = -uv_{\zeta} , \quad (B-3)$$

$$p_{\tau} + \bar{v}p_{\eta} - a^2(\rho_{\tau} + \bar{v}\rho_{\eta}) = -up_{\zeta} + a^2up_{\zeta} . \quad (B-4)$$

Letting

$$\psi_1 = -up_{\zeta} - \rho u_{\zeta} - \epsilon\rho u\beta/\eta , \quad (B-5)$$

$$\psi_2 = -uu_{\zeta} - p_{\zeta}/\rho , \quad (B-6)$$

$$\psi_3 = -uv_{\zeta} , \quad (B-7)$$

$$\psi_4 = -up_{\zeta} + a^2up_{\zeta} , \quad (B-8)$$

Eqs. (B-1) through (B-4) become

$$\rho_{\tau} + \bar{v}\rho_{\eta} + \rho\alpha u_{\eta} + \rho\beta v_{\eta} = \psi_1 , \quad (B-9)$$

$$u_{\tau} + \bar{v}u_{\eta} + \alpha p_{\eta}/\rho = \psi_2 , \quad (B-10)$$

$$v_{\tau} + \bar{v}v_{\eta} + \beta p_{\eta}/\rho = \psi_3 , \quad (B-11)$$

$$p_{\tau} + \bar{v}p_{\eta} - a^2(\rho_{\tau} + \bar{v}\rho_{\eta}) = \psi_4 . \quad (B-12)$$

II. CHARACTERISTIC CURVES

Following the development of Appendix A, the characteristic curves can be shown to be

$$d\eta/d\tau = \bar{v} , \quad (B-13)$$

$$d\eta/d\tau = \bar{v} + \alpha^*a , \quad (B-14)$$

$$\text{where } \alpha^* = (\alpha^2 + \beta^2)^{1/2} .$$

III. COMPATIBILITY EQUATIONS

Again, following the development of Appendix A, the compatibility equations can be shown to be

$$\beta du - \alpha dv = (\beta\psi_2 - \alpha\psi_3)d\tau \quad \left. \begin{array}{l} \\ \end{array} \right\} \text{for } d\eta = \bar{v}d\tau , \quad (B-15)$$

$$dp - a^2dp = \psi_4d\tau \quad \left. \begin{array}{l} \\ \end{array} \right\} \quad (B-16)$$

$$\begin{aligned} dp - \rho\alpha adu/\alpha^* - \rho\beta adv/\alpha^* &= (\psi_4 + a^2\psi_1 \\ - \rho\alpha a\psi_2/\alpha^* - \rho\beta a\psi_3/\alpha^*)d\tau \quad \text{for } d\eta = (\bar{v} - \alpha^*a)d\tau \end{aligned} \quad (B-17)$$

$$\begin{aligned} dp + \rho\alpha adu/\alpha^* + \rho\beta adv/\alpha^* &= (\psi_4 + a^2\psi_1 \\ + \rho\alpha a\psi_2/\alpha^* + \rho\beta a\psi_3/\alpha^*)d\tau \quad \text{for } d\eta = (\bar{v} + \alpha^*a)d\tau \end{aligned} \quad (B-18)$$

APPENDIX C
FORTRAN IV LISTING OF THE NAP PROGRAM

LASL Identification: LP-0537

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PROGRAM MAIN(INPUT,OUTPUT,FILM,PUNCH,TAPES=INPUT,TAPE6=OUTPUT,
1TAPE7=FILM)                                MAI 10
C                                              MAI 20
C                                              MAI 30
C                                              MAI 40
C                                              MAI 50
C                                              MAI 60
C                                              MAI 70
C                                              MAI 80
C                                              MAI 90
C                                              MAI 100
C                                              MAI 110
C                                              MAI 120
C                                              MAI 130
C                                              MAI 140
C                                              MAI 150
C                                              MAI 160
C                                              MAI 170
C                                              MAI 180
C                                              MAI 190
C                                              MAI 200
C                                              MAI 210
C                                              MAI 220
C                                              MAI 230
C                                              MAI 240
C                                              MAI 250
C                                              MAI 260
C                                              MAI 270
C                                              MAI 280
C                                              MAI 290
C                                              MAI 300
C                                              MAI 310
C                                              MAI 320
C                                              MAI 330
C                                              MAI 340
C                                              MAI 350
C                                              MAI 360
C                                              MAI 370
C                                              MAI 380
C                                              MAI 390
C                                              MAI 400
C                                              MAI 410
C                                              MAI 420
C                                              MAI 430
C                                              MAI 440
C                                              MAI 450
C                                              MAI 460
C                                              MAI 470
C                                              MAI 480
C                                              MAI 490
C                                              MAI 500
C                                              MAI 510
C                                              MAI 520
C                                              MAI 530
C                                              MAI 540
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C                                              MAI 570
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C                                              MAI 620
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C                                              MAI 720
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C                                              MAI 740
C                                              MAI 750
C                                              MAI 760
C                                              MAI 770
C                                              MAI 780
C                                              MAI 790
C                                              MAI 800
C                                              MAI 810
C                                              MAI 820
C                                              MAI 830
C
C ***** NAP, A COMPUTER PROGRAM FOR THE COMPUTATION OF TWO-DIMENSIONAL,
C ***** TIME-DEPENDENT, INVISCID NOZZLE FLOW ***** MAI 40
C
C ***** BY MICHAEL C. CLINE, T-3 ***** MAI 50
C ***** LOS ALAMOS SCIENTIFIC LABORATORY ***** MAI 60
C
C ***** PROGRAM ABSTRACT ***** MAI 70
C
C ***** THE EQUATIONS OF MOTION FOR TWO-DIMENSIONAL, TIME DEPENDENT,
C ***** INVISCID FLOW IN A NOZZLE ARE SOLVED USING THE SECOND-ORDER,
C ***** MACCORMACK, FINITE-DIFFERENCE SCHEME. THE FLUID IS ASSUMED TO BE
C ***** A PERFECT GAS. ALL BOUNDARY CONDITIONS ARE COMPUTED USING A
C ***** SECOND-ORDER, REFERENCE PLANE CHARACTERISTIC SCHEME. THE STEADY
C ***** STATE SOLUTION IS OBTAINED AS THE ASYMPTOTIC SOLUTION FOR LARGE
C ***** TIME. THE NOZZLES MAY BE EITHER CONVERGING, CONVERGING-DIVERGING,
C ***** OR PLUG GEOMETRIES. ***** MAI 80
C
C ***** DIMENSION TITLE(8), UI(21), VI(21), PI(21), ROI(21) ***** MAI 90
C ***** COMMON /AV/ IAV,CAV,NST,8MP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81,21) ***** MAI 100
C ***** 1,21),QPT(81,21) ***** MAI 110
C ***** COMMON /ONESID/ U(4),VD(4),PD(4),ROD(4) ***** MAI 120
C ***** COMMON /SOLUTH/ U(81,21,2),V(81,21,2),P(81,21,2),R0(81,21,2) ***** MAI 130
C ***** COMMON /CNTRL/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAMI,GAMAI ***** MAI 140
C 1M2,L1,L2,L3,M1,M2,DX,DY,DT,N,N1,N3,NASM,IVEL,ICHAR,NID,LJET,JFLAG,MAI 150
C 2IERR,IUI,IUO,DXR,DYR,L0,MD,LMD1,LMD3,IB,RSTAR,RSTAR8,NPLOT,G,PC,TCHAI ***** MAI 160
C 3,LC,PL0W,ROL0W ***** MAI 170
C ***** COMMON /GEMTRYC/ NGEOM,XI,RI,XT,RE,RCI,RCT,ANGI,ANGE,XH(81),MAI 180
C 1YH(81),XWI(81),YWI(81),NXNY(81),NWPPTS,IINT,IDIF,LT,NDIM ***** MAI 190
C ***** COMMON /GCBL/ NGCB,XICB,RICB,XTCB,RTCB,XECB,REC,B,RCICB,RCTCB,ANGICBMAI 200
C 1,ANGECB,XCB(81),YCB(81),XCB(81),YCB(81),NXNYCB(81),NCBPTS,IINTCBMAI 210
C 2,IDIFCB,LECB ***** MAI 220
C ***** COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASST,MASSI,THRUST,NMAI 230
C 1$TAG ***** MAI 240
C ***** REAL MN3,NXNY,MASSE,MASST,NXNYCB,MASSE ***** MAI 250
C ***** NAMELIST /CNTRL/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,TSTOP,GAMMA,RGAS,MAI 260
C 1NASM,NAME,NCONVI,NST,IUI,IUO,SMP,IPUNCH,IAV,CAV,NPLOT,IE,X,LSS,CTA,MAI 270
C 2XMU,XLA,RKMU,IUNIT,PL0W,ROL0W ***** MAI 280
C ***** NAMELIST /IVS/ U,V,P,RO,NID,NSTART,TSTART,RSTAR,RSTAR8 ***** MAI 290
C ***** NAMELIST /GEMTRY/ NDIM,XI,RI,RT,XE,RCI,RCT,ANGI,ANGE,NGEOM,XWI,YWI,MAI 300
C 1,NWPPTS,IINT,IDIF,LJET,JFLAG,NXNY,YH ***** MAI 310
C ***** NAMELIST /GCBL/ NGCB,RICB,XTCB,RTCB,RCICB,RCTCB,ANGICB,ANGEBCB,YCB,NXNYCBMAI 320
C 1B,XCB(81),NCBPTS,IINTCB,IDIFCB ***** MAI 330
C ***** NAMELIST /BC/ PT,TT,THETA,PE,N$TAG,ISUPER,UI,VI,PI,ROI ***** MAI 340
C
C ***** READ IN DATA ***** MAI 350
C
C 10  TCONV=0,0 S FDT=1,0 S TSTOP=1,0 S NASH=1 S NSTAG=0 S NAME=0 ***** MAI 360
C 1PUNCH=0 S NGCB=0 S IINTCB=1 S IDIFCB=1 S NSTART=0 S TSTART=0,0 ***** MAI 370
C 1IINT=1 S IDIF=1 S NMAX=0 S NPRINT=0 S GAMMA=1,4 S RGAS=53,35 ***** MAI 380
C 1NID=1 S NDIM=1 S THETA(1)=0,0 S PE=14,7 S NST=0 S N=0 S IE=1 ***** MAI 390
C 1NCONVI=1 S IERR=0 S JFLAG=0 S IUI=1 S IUO=1 S SMP=0,95 S ISUPER=0 ***** MAI 400
C 1AV=0 S CAV=4,0 S NPLOT=-1 S G=32,174 S PC=144,0 S TC=460,0 ***** MAI 410
C 1LC=12,0 S IUNIT=0 S LS9=2 S CTA=0,5 S XMU=0,2 S XLA=1,0 ***** MAI 420
C 1RKMU=0,7 S PL0W=0,01 S ROL0W=0,0001 S RSTAR=0,0 S RSTAR8=0,0 ***** MAI 430
C 1READ 650, TITLE ***** MAI 440
C 1IF (EOF,5) GO TO 30 ***** MAI 450
C 20  STOP ***** MAI 460
C 30  READ (5,CNTRL) ***** MAI 470
C 30  READ (5,IVS) ***** MAI 480
C 30  READ (5,GEMTRY) ***** MAI 490
C 30  READ (5,GCBL) ***** MAI 500
C 30  READ (5,BC) ***** MAI 510
C 30  IF (NAME,EQ,A) GO TO 40 ***** MAI 520
C 30  WRITE (6,CNTRL) ***** MAI 530
C 30  WRITE (6,IVS) ***** MAI 540
C 30  WRITE (6,GEMTRY) ***** MAI 550
C 30  WRITE (6,GCBL) ***** MAI 560
C 30  WRITE (6,BC) ***** MAI 570
C
C ***** PRINT INPUT DATA ***** MAI 580
C
C 40  PRINT 660 ***** MAI 590
C 40  PRINT 690 ***** MAI 600
C 40  PRINT 680 ***** MAI 610
C 40  PRINT 700 ***** MAI 620
C 40  PRINT 670 ***** MAI 630

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PRINT 710, TITLE
PRINT 670
PRINT 720
NPRINT=ABS(FLOAT(NPRINT))
PRINT 730, LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,NSTAG,NASM,IUNIT,IUI,IUMAI
10,IEI,NCONVI,TSTOP,N1D,NPLOT,IPUNCH,ISUPER,IAV,CAV,XMU,XLA,RKMU,CTMAI
2A,LSS,SMP,NST
PRINT 670
IF (IUI,EQ,1) PRINT 740, GAMMA,RGAS
IF (IUI,EQ,2) PRINT 750, GAMMA,RGAS
PRINT 670
PRINT 780
IF (NDIM,EO,0) PRINT 790
IF (NDIM,EO,1) PRINT 800
C
C   CALCULATE THE NOZZLE RADIUS AND NORMAL
C
PRINT 670
CALL GEOM
IF (IERR,NE,0) GO TO 10
DY=1.0/FLOAT(MMAX-1)
IF (NCGB,NE,0) GO TO 60
RICB=0.0
RTCB=0.0
DO 50 L=1,LMAX
YCB(L)=0.0
NXNYCB(L)=0.0
50 CONTINUE
GO TO 90
60 XICB=XI
XECB=XE
CALL GEOMCB
LT=1 S XI=XICB S XE=XECB
YO=0.0
DO 80 L=1,LMAX
IF (NDIM,EO,0) Y=YW(L)-YCB(L)
IF (NDIM,EO,1) Y=YW(L)**2-YCB(L)**2
IF (Y,GT,0.0) GO TO 70
PRINT 920
GO TO 10
70 IF (Y,LT,YO) LT=L
YO=Y
80 CONTINUE
90 IF (NSTAG,NE,0) GO TO 110
DO 100 M=2,MMAX
PT(M)=PT(1)
TT(M)=TT(1)
THETA(M)=THETA(1)
100 CONTINUE
PRINT 670
IF (IUI,EQ,1) PRINT 760, PT(1),TT(1),THETA(1),PE
IF (IUI,EQ,2) PRINT 770, PT(1),TT(1),THETA(1),PE
GO TO 130
110 PRINT 660
IF (IUI,EQ,1) PRINT 890, PE
IF (IUI,EQ,2) PRINT 900, PE
DO 120 M=1,MMAX
PRINT 910, M,PT(M),TT(M),THETA(M)
120 CONTINUE
C
C   CONVERT METRIC UNITS TO ENGLISH UNITS
C
130 IF (IUI,EO,1) GO TO 180
RSTAR=RSTAR/2.54
RSTAR3=RSTAR/6.4516
RGAS=RGAS/5.38032
DO 140 M=1,MMAX
PT(M)=PT(M)/6.8948
TT(M)=(TT(M)+40.0)*9.0/5.0=40.0
140 CONTINUE
PE=PE/6.8948
IF (ISUPER,EO,0) GO TO 160
DO 150 M=1,MMAX
UI(M)=UI(M)/0.3048
VI(M)=VI(M)/0.3048
PI(M)=PI(M)/6.8948
ROI(M)=ROI(M)/16.02
150 CONTINUE
160 IF (NID,NE,0) GO TO 180
IF (NSTART,NE,0) GO TO 180
DO 170 L=1,LMAX
DO 170 M=1,MMAX
U(L,M,1)=U(L,M,1)/0.3048

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V(L,M,1)=V(L,M,1)/0.3048          MAI 1670
P(L,M,1)=P(L,M,1)/6.8948          MAI 1680
RO(L,M,1)=RO(L,M,1)/16.02          MAI 1690
170
C
C   CONVERT INPUT DATA UNITS TO INTERNAL UNITS
C
180   IF (IUNIT.EQ.0) GO TO 190          MAI 1700
PC=LC=G=1.0                         MAI 1710
TC=0.0                               MAI 1720
190   TCONV=TCONV/100.0                MAI 1730
T=TSTART+LC                         MAI 1740
TSTOP=TSTOP+LC                      MAI 1750
DO 200 L=1,LMAX                     MAI 1760
XN(L)=0.0                            MAI 1770
200
C   CONTINUE
DO 210 M=1,MMAX                     MAI 1780
PT(M)=PT(M)*PC                      MAI 1790
TT(M)=TT(M)+TC                      MAI 1800
THETA(M)=THETA(M)*0.0174533        MAI 1810
210
C   CONTINUE
PE=PE*PC                           MAI 1820
IF (N1D,NE,0) GO TO 230             MAI 1830
DO 220 L=1,LMAX                     MAI 1840
DO 220 M=1,MMAX                     MAI 1850
P(L,M,1)=P(L,M,1)*PC               MAI 1860
RO(L,M,1)=RO(L,M,1)/G              MAI 1870
220
C   CONTINUE
GAM1=GAMMA/(GAMMA+1.0)              MAI 1880
GAM2=(GAMMA+1.0)/2.0                MAI 1890
IF (ISUPER,EQ,0) GO TO 250          MAI 1900
DO 240 M=1,MMAX                     MAI 1910
U(1,M,1)=UI(M)                      MAI 1920
V(1,M,1)=VI(M)                      MAI 1930
230
C   GAMMA=GAMMA/(GAMMA+1.0)
GAM2=(GAMMA+1.0)/2.0
IF (ISUPER,EQ,0) GO TO 250
DO 240 M=1,MMAX
U(1,M,1)=UI(M)
V(1,M,1)=VI(M)
P(1,M,1)=PI(M)*PC
RO(1,M,1)=RO(1,M)/G
U(1,M,2)=U(1,M,1)
V(1,M,2)=V(1,M,1)
P(1,M,2)=P(1,M,1)
RO(1,M,2)=RO(1,M,1)
240
C   CONTINUE
L1=LMAX=1                           MAI 1940
L2=LMAX=2                           MAI 1950
L3=LMAX=3                           MAI 1960
M1=MMAX=1                           MAI 1970
M2=MMAX=2                           MAI 1980
250
C   M=1
IF (N1D,EQ,0) GO TO 260             MAI 1990
C
C   COMPUTE THE 1-D INITIAL-DATA SURFACE
C
CALL ONEDIM                          MAI 2000
IF (IERR,NE,0) GO TO 10              MAI 2010
C
C   COMPUTE THE INITIAL-SURFACE MASS FLOW AND THRUST
C
260   IF (NPRINT.GT.0) GO TO 270          MAI 2020
NPRINT=NPRINT                         MAI 2030
GO TO 340                            MAI 2040
270   CALL MASFLO (0)                  MAI 2050
C
C   CALCULATE AND PRINT THE INITIAL-VALUE SURFACE
C
DO 330 IU=1,2                         MAI 2060
IF (IU0,EQ,1.AND.IU,EQ,2) GO TO 330          MAI 2070
IF (IU0,EQ,2.AND.IU,FQ,1) GO TO 330          MAI 2080
NLINE=0
PRINT 660
PRINT 810, TSTART,NSTART            MAI 2090
PRINT 820
IF (IU,EQ,1) PRINT 830              MAI 2100
IF (IU,EQ,2) PRINT 840              MAI 2110
PRINT 670
X=X1+DX
DO 300 L=1,LMAX                     MAI 2120
X=X+DX
CALL MAP (0,L,1,AL,BE,DE,LD1,AL1,BE1,DE1)    MAI 2130
DY10=DY/BE
Y=YCB(L)-DY10
DO 300 M=1,MMAX                     MAI 2140
Y=Y+DY10
VELMAG=SORT(U(L,M,1)**2+V(L,M,1)**2)      MAI 2150
XHACH=VELMAG/SQRT(GAMMA*P(L,M,1)/RO(L,M,1))  MAI 2160
PRE3=P(L,M,1)/PC                      MAI 2170

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RHO=RHO(L,M,1)*G          MAI 2500
TEMP=TEMP(L,M,1)/RHO/RGAS=TC   MAI 2510
XP=X          MAI 2520
YP=Y          MAI 2530
UP=U(L,M,1)      MAI 2540
VP=V(L,M,1)      MAI 2550
IF (IU,EQ,1) GO TO 260      MAI 2560
XP=XP+2,54        MAI 2570
YP=YP+2,54        MAI 2580
UP=UP+0,3048      MAI 2590
VP=VP+0,3048      MAI 2600
PRES=PRES+6,8948     MAI 2610
RHO=RHO+16,02        MAI 2620
VELMAG=VELMAG+0,3048     MAI 2630
TEMP=(TEMP+40,0)*5,0/9,0-40,0  MAI 2640
280 NLINE=NLINE+1          MAI 2650
IF (NLINE,LT,55) GO TO 290      MAI 2660
PRINT 660          MAI 2670
PRINT 810, TSTART,NSTART      MAI 2680
PRINT 820          MAI 2690
IF (IU,EQ,1) PRINT 830      MAI 2700
IF (IU,EQ,2) PRINT 840      MAI 2710
PRINT 670          MAI 2720
NLINE=1          MAI 2730
PRINT 850, L,M,XP,YP,UP,VP,PRES,RHO,VELMAG,XMACH,TEMP  MAI 2740
300 CONTINUE          MAI 2750
IF (IU,EQ,2) GO TO 310      MAI 2760
PRINT 870, MASST,THRUST,MASSI,MASSE      MAI 2770
GO TO 320          MAI 2780
310 MASST=MASST+0,4536      MAI 2790
MASSI=MASSI+0,4536      MAI 2800
MASSE=MASSE+0,4536      MAI 2810
THRUST=THRUST+4,4477      MAI 2820
PRINT 880, MASST,THRUST,MASSI,MASSE      MAI 2830
320 IF (IU0,NE,3) GO TO 340      MAI 2840
330 CONTINUE          MAI 2850
340 IF (NPLOT,LE,0) GO TO 350      MAI 2860
CALL PLOT (TITLE,TSTART,NSTART)      MAI 2870
PRINT 1030, NSTART      MAI 2880
350 IF (NMAX,EQ,0) GO TO 10      MAI 2890
C
C   INITIALIZE THE TIME STEP INTEGRATION LOOP PARAMETERS  MAI 2900
C
N1=1 S N3=2 S DQM=0,0 S NS=0 S NCONV=0 S NC=0 S LDUM=1 S NPC=0  MAI 2930
DXR=1,0/DX S DYR=1,0/DY S DXRS=DXR*DXR S DYRS=DYR*DYR  MAI 2940
LD=81 S MD=21 S LMD=LD*MD  MAI 2950
IF (NASH,NE,0,AND,LT,NE,1) LDUM=LT=1  MAI 2960
NPD=0  MAI 2970
IF (JFLAG,EQ,0) GO TO 360  MAI 2980
UD(1)=U(LJET-1,MMAX,N1)  MAI 2990
VD(1)=V(LJET-1,MMAX,N1)  MAI 3000
PD(1)=P(LJET-1,MMAX,N1)  MAI 3010
ROD(1)=RO(LJET-1,MMAX,N1)  MAI 3020
UD(2)=UD(1)  MAI 3030
VD(2)=VD(1)  MAI 3040
PD(2)=PD(1)  MAI 3050
ROD(2)=ROD(1)  MAI 3060
MAI 3070
C
C   ENTER THE TIME STEP INTERGRATION LOOP  MAI 3080
C
360 DO 580 N=1,NMAX  MAI 3090
NPD=NPD+1  MAI 3100
IF (NPD,NE,10) GO TO 370  MAI 3110
NP=N+NSTART  MAI 3120
PRINT 1040, NP  MAI 3130
NPD=0  MAI 3140
370 CONTINUE  MAI 3150
LMD1=LMD*(N1-1)  MAI 3160
LMD3=LMD*(N3-1)  MAI 3170
MAI 3180
C
C   CALCULATE DELTA T  MAI 3190
C
DO 380 L=1,LMAX  MAI 3200
CALL MAP (0,L,MD,AL,BE,DE,LD1,AL1,BE1,DE1)  MAI 3210
DXDY=DXRS*BE*BE*DYRS  MAI 3220
MAI 3230
DO 380 M=1,MMAX  MAI 3240
LHN1=L+LD*(M-1)+LMD1  MAI 3250
MAI 3260
QS=U(LHN1)+V(LHN1)+V(LHN1)+V(LHN1)  MAI 3270
AS=GAMMA*P(LHN1)/RO(LHN1)  MAI 3280
UPA=SQR(T(QS*DXDY)+SQR(T(AS*DXDY))  MAI 3290
IF (L,EQ,1,AND,M,EQ,1) UPAM=UPA  MAI 3300
IF (UPA,GT,UPAM) UPAM=UPA  MAI 3310

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380  CONTINUE          MAI 3320
DT=FDT/UPAM          MAI 3330
T=T+DT              MAI 3340
IF (T,LE,TSTOP) GO TO 390  MAI 3350
T=T+DT              MAI 3360
DT=TSTOP-T          MAI 3370
T=TSTOP              MAI 3380
C
C DETERMINE IF THE EXIT FLOW IS SUBSONIC OR SUPERSONIC  MAI 3390
C
390  IVEL=0            MAI 3400
IF (QS,GE,A3) IVEL=1  MAI 3410
C
C CALCULATE THE NOZZLE WALL AND INTERIOR MESH POINTS  MAI 3420
C
IF (IAV,NE,0) CALL SHOCK (1)  MAI 3430
ICHR=1               MAI 3440
IB=1                 MAI 3450
CALL INTER           MAI 3460
CALL WALL            MAI 3470
IF (IERR,NE,0) GO TO 10  MAI 3480
IF (NGCB,EQ,0) GO TO 400  MAI 3490
IB=2
CALL WALL            MAI 3500
IF (IERR,NE,0) GO TO 10  MAI 3510
IF (NGCB,EQ,0) GO TO 400  MAI 3520
IB=2
CALL WALL            MAI 3530
IF (IERR,NE,0) GO TO 10  MAI 3540
MAI 3550
400  ICHAR=2            MAI 3560
IB=1                 MAI 3570
CALL INTER           MAI 3580
CALL WALL            MAI 3590
IF (IERR,NE,0) GO TO 10  MAI 3600
IF (NGCB,EQ,0) GO TO 410  MAI 3610
IB=2
CALL WALL            MAI 3620
IF (IERR,NE,0) GO TO 10  MAI 3630
MAI 3640
C
C EXTRAPOLATE THE EXIT MESH POINTS FOR SUPERSONIC FLOW  MAI 3650
C
410  DO 420 M=1,MMAX          MAI 3660
U(LMAX,M,N3)=U(L1,M,N3)+IEX*(U(L1,M,N3)-U(L2,M,N3))  MAI 3670
V(LMAX,M,N3)=V(L1,M,N3)+IEX*(V(L1,M,N3)-V(L2,M,N3))  MAI 3680
P(LMAX,M,N3)=P(L1,M,N3)+IEX*(P(L1,M,N3)-P(L2,M,N3))  MAI 3690
RO(LMAX,M,N3)=RO(L1,M,N3)+IEX*(RO(L1,M,N3)-RO(L2,M,N3))  MAI 3700
IF (P(LMAX,M,N3),GT,0,0,AND,RO(LMAX,M,N3),GT,0,0) GO TO 420  MAI 3710
P(LMAX,M,N3)=P(L1,M,N3)          MAI 3720
RO(LMAX,M,N3)=RO(L1,M,N3)          MAI 3730
MAI 3740
420  CONTINUE          MAI 3750
V(LMAX,MMAX,N3)=U(LMAX,MMAX,N3)*NXNY(LMAX)          MAI 3760
V(LMAX,1,N3)=U(LMAX,1,N3)*NXNYCB(LMAX)          MAI 3770
MAI 3780
C
C CALCULATE THE NOZZLE INLET MESH POINTS  MAI 3790
C
IF (IBUPER,EQ,0) CALL INLET          MAI 3800
MAI 3810
C
C CALCULATE THE NOZZLE EXIT MESH POINTS FOR SUBSONIC FLOW  MAI 3820
C
IF (IVEL,EQ,0) CALL EXITT          MAI 3830
IF (N,LE,NST) CALL SHOCK (2)          MAI 3840
MAI 3850
C
C DETERMINE THE MAXIMUM (DELTA U)/U  MAI 3860
C
IF (TCOMP,LE,0,0) GO TO 440          MAI 3870
DQM=0,0          MAI 3880
MAI 3890
430  DO 430 L=LDMU,LMAX          MAI 3900
DO 430 M=1,MMAX          MAI 3910
MAI 3920
IF (U(L,M,N1),EQ,0,0) GO TO 430  MAI 3930
DQ=AB8((U(L,M,N3)-U(L,M,N1))/U(L,M,N1))  MAI 3940
IF (DQ,GT,DQM) DQM=DQ  MAI 3950
MAI 3960
430  CONTINUE          MAI 3970
MAI 3980
440  NC=NC+1            MAI 3990
NPC=NPC+1          MAI 4000
MAI 4010
IF (DQM,GE,TCOMP) GO TO 450          MAI 4020
NCNCONV=NCNCONV+1          MAI 4030
MAI 4040
450  IF (NCNCONV,EQ,1) NCHECK=N=1  MAI 4050
IF (NCNCONV,GE,NCNCONV) NC=NPRINT  MAI 4060
IF (N,EQ,NMAX) NC=NPRINT          MAI 4070
IF (N,GE,NCHECK+NCNCONV) NCONV=0  MAI 4080
IF (T,EQ,TSTOP) NC=NPRINT          MAI 4090
IF (NC,EQ,NPRINT) GO TO 460          MAI 4100
IF (NPC,EQ,NPLOT) GO TO 550          MAI 4110
GO TO 570          MAI 4120
MAI 4130
C
C COMPUTE THE SOLUTION SURFACE MASS FLOW AND THRUST  MAI 4140
C

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460 ICN=9
IF (JFLAG,EQ,0) GO TO 470
IF (LT,NE,LJET-1) GO TO 470
UDUM=U(LT,MMAX,N3)
RODUM=RO(LT,MMAX,N3)
U(LT,MMAX,N3)=UD(3)
RO(LT,MMAX,N3)=ROD(3)
ICN=1
470 CALL MASFL0 (1)
IF (ICN,EQ,0) GO TO 480
U(LT,MMAX,N3)=UDUM
RO(LT,MMAX,N3)=RODUM
C
C   CALCULATE AND PRINT THE SOLUTION SURFACE
C
480 DO 540 IU=1,2
IF (IU0,EQ,1,AND,IU,EQ,2) GO TO 540
IF (IU0,EQ,2,AND,IU,EQ,1) GO TO 540
NLINE=0
PRINT 660
TIME=T/LC
DTIME=DT/LC
NP=N+NSTART
PRINT 660, NP, TIME, DTIME
PRINT 820
IF (IU,EQ,1) PRINT 830
IF (IU,EQ,2) PRINT 840
PRINT 670
X=XI+DX
DO 510 L=1,LMAX
X=X+DX
CALL MAP (0,L,1,AL,BE,DE,LD1,AL1,BE1,DE1)
DYIO=DY/BE
Y=YCB(L)+DYIO
DO 510 M=1,MMAX
Y=Y+DYIO
VELMAG=SQRT(U(L,M,N3)**2+V(L,M,N3)**2)
XMACH=VELMAG/SQRT(GAMMA*P(L,M,N3)/RO(L,M,N3))
PRESS=P(L,M,N3)/PC
RHO=RO(L,M,N3)*G
TEMP=P(L,M,N3)/RHO/RGAS=TC
XP=X
YP=Y
UP=U(L,M,N3)
VP=V(L,M,N3)
IF (IU,EQ,1) GO TO 490
XP=XP*2.54
YP=YP*2.54
UP=UP*0.3048
VP=VP*0.3048
PRESS=PRESS*0.9948
RHO=RHO*16.02
VELMAG=VELMAG*0.3848
TEMP=(TEMP+40.0)*5.0/9.0=40.0
490 NLINE=NLINE+1
IF (NLINE,LT,55) GO TO 500
PRINT 660
PRINT 860, NP, TIME, DTIME
PRINT 820
IF (IU,EQ,1) PRINT 830
IF (IU,EQ,2) PRINT 840
PRINT 670
NLINE=1
500 PRINT 850, L,M,XP,YP,UP,VP,PRES,RHO,VELMAG,XMACH,TEMP
CONTINUE
510 IF (IU,EQ,2) GO TO 520
PRINT 870, MASST,THRUST,MASST,MASSE
GO TO 530
520 MASST=MASST*0.4536
MASST=MASST*0.4536
MASSE=MASSE*0.4536
THRUST=THRUST*4.4477
PRINT 880, MASST,THRUST,MASST,MASSE
530 IF (IU0,NE,3) GO TO 550
540 CONTINUE
550 IF (NPLOT,LT,0) GO TO 560
TIME=T/LC 9 NP=N+NSTART
CALL PLOT (TITLE,TIME,np)
PRINT 1030, NP
C
C   CHECK FOR CONVERGENCE OF THE STEADY STATE SOLUTION
C

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560 IF (DQM,LT,TCONV) GO TO 590 MAI 4970
IF (T,EQ,TSTOP) GO TO 590 MAI 4980
IF (N,EQ,NMAX) GO TO 590 MAI 4990
IF (NC,EQ,NPRINT) NC=0 MAI 5000
IF (NPC,EQ,NPLOT) NPC=0 MAI 5010
570 CONTINUE MAI 5020
NNN=N1 MAI 5030
N1=N3 MAI 5040
N3=NNN MAI 5050
580 CONTINUE MAI 5060
C MAI 5070
C PUNCH A SIVS NAMELIST FOR RESTART MAI 5080
C MAI 5090
590 IF (NPLOT,GE,0) CALL ADV (10) MAI 5100
IF (IPUNCH,EQ,0) GO TO 10 MAI 5110
DO 600 L=1,LMAX MAI 5120
DO 600 M=1,MMAX MAI 5130
P(L,M,N3)=P(L,M,N3)/PC MAI 5140
R0(L,M,N3)=R0(L,M,N3)*G MAI 5150
600 CONTINUE MAI 5160
PUNCH 930, NP,TIME MAI 5170
DO 610 M=J,MMAX MAI 5180
PUNCH 940, M MAI 5190
PUNCH 950, (U(L,M,N3),L=1,LMAX) MAI 5200
610 CONTINUE MAI 5210
DO 620 M=1,MMAX MAI 5220
PUNCH 960, M MAI 5230
PUNCH 950, (V(L,M,N3),L=1,LMAX) MAI 5240
620 CONTINUE MAI 5250
DO 630 M=1,MMAX MAI 5260
PUNCH 970, M MAI 5270
PUNCH 980, (P(L,M,N3),L=1,LMAX) MAI 5280
630 CONTINUE MAI 5290
DO 640 M=1,MMAX MAI 5300
PUNCH 990, M MAI 5310
PUNCH 1000, (R0(L,M,N3),L=1,LMAX) MAI 5320
640 CONTINUE MAI 5330
PUNCH 1010 MAI 5340
NCARDS=(LMAX/7+2)*MMAX*4+2 MAI 5350
PRINT 1020, NCARDS MAI 5360
GO TO 10 MAI 5370
C MAI 5380
C FORMAT STATEMENTS MAI 5390
C MAI 5400
650 FORMAT (RA10) MAI 5410
660 FORMAT (1H1) MAI 5420
670 FORMAT (1H ) MAI 5430
680 FORMAT (1H0) MAI 5440
690 FORMAT (1H0,15X,10HNNAP, A COMPUTER PROGRAM FOR THE COMPUTATION OFMAI 5450
1 TWO-DIMENSIONAL, TIME-DEPENDENT, INVISCID NOZZLE FLOW, //,37X,59HBMAI 5460
2Y MICHAEL C. CLINE, T-3 - LOS ALAMOS SCIENTIFIC LABORATORY) MAI 5470
700 FORMAT (1H0,10X,18HPROGRAM ABSTRACT //,26X,86HTHE EQUATIONS OF MMAI 5480
10TION FOR TWO-DIMENSIONAL, TIME DEPENDENT, INVISCID FLOW IN A NOZMAI 5490
2LE, //,21X,93HARE SOLVED USING THE SECOND-ORDER, MACCORMACK, FINITE-MAI 5500
3DIFERENCE SCHEME, THE FLUID IS ASSUMED, //,21X,95HTO BE A PERFECT GMAI 5510
4AS, ALL BOUNDARY CONDITIONS ARE COMPUTED USING A SECOND-ORDER, REFMAI 5520
SERENCE PLANE, //,21X,91HCHARACTERISTIC SCHEME, THE STEADY STATE SOLUMMAI 5530
6TION IS OBTAINED AS THE ASYMPTOTIC SOLUTION FOR, //,21X,91HLARGE TIMMAI 5540
7E, THE NOZZLES MAY BE EITHER CONVERGING, CONVERGING-DIVERGING, OR MAI 5550
8PLUG GEOMETRIES,) MAI 5560
710 FORMAT (1H0,10X,11HJOB TITLE //,21X,RA10) MAI 5570
720 FORMAT (1H0,10X,20HCONTROL PARAMETERS ~) MAI 5580
730 FORMAT (1H0,20X,5HLMAX=,I2,2X,5HNMMAX=,I2,3X,5HNMAX=,I4,2X,7HNPRINTMAI 5590
1=,I4,2X,6HTCONV=,F6,3,3X,4HFDT=,F4,2X,6HNSTAG=,I1,5X,5HNA8M=,I1,MAI 5600
2X,6HZUNITE=,I1,/,21X,4HIU1=,I1,4X,4HIUD=,I1,5X,4HIEX=,I1,6X,7HNCONMAI 5610
3VI=,I2,4X,6HTSTOP=,F7,5,2X,4HN1D=,I2,4X,6HNPLT=,I4,2X,7HIPUNCH=,IMAI 5620
41,2X,7HISUPER=,I1,/,21X,4HTAV=,I1,4X,4HCAV=,F4,1,2X,4HXHU=,F4,2,3XMAI 5630
5,4HXLA=,F4,2,5X,5HRKMU=,F5,2,5X,4HCTA=,F4,2,2X,4HLSS=,I2,6X,4H9MP=MAI 5640
6,F4,2,2X,4HNST=,I4) MAI 5650
740 FORMAT (1H0,10X,13HFLUID MODEL //,21X,36HTHE RATIO OF SPECIFIC MMAI 5660
1EATS, GAMMA =,F6,4,26H AND THE GAS CONSTANT, R =,F9,4,15H (FT=LB/MAI 5670
2LBH=R)) MAI 5680
750 FORMAT (1H0,10X,13HFLUID MODEL //,21X,36HTHE RATIO OF SPECIFIC MMAI 5690
1EATS, GAMMA =,F6,4,26H AND THE GAS CONSTANT, R =,F9,4,9H (J/KG*K)MAI 5700
760 FORMAT (1H0,10X,21HBOUNDARY CONDITIONS //,21X,3HPT=,F9,4,7H (PS1MAI 5710
1),5X,3HTT=,F9,4,4H (F),5X,6HTHETA=,F9,4,6H (DEG),5X,3HPE=,F9,4,7HMAI 5720
2 (PS1A)) MAI 5730
770 FORMAT (1H0,10X,21HBOUNDARY CONDITIONS //,21X,3HPT=,F9,4,6H (KPAMAI 5740
1),5X,3HTT=,F9,4,4H (C),5X,6HTHETA=,F9,4,6H (DEG),5X,3HPE=,F9,4,6H MAI 5750
2 (KPA)) MAI 5760
780 FORMAT (1H0,10X,15HFLOW GEOMETRY ~) MAI 5770
790 FORMAT (1H0,20X,47HTWO-DIMENSIONAL, PLANAR FLOW HAS BEEN SPECIFIEDMAI 5780
1) MAI 5790

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800  FORMAT (1H0,20X,36MAXISYMMETRIC FLOW HAS BEEN SPECIFIED)      MAI 5800
810  FORMAT (1H ,30HINITIAL- DATA SURFACE + TIME = ,F10.8,8H SECONDS,4H MAI 5810
     1(N=,I4,1H))                                              MAI 5820
820  FORMAT (1H0,11X,1HL,4X,1HM,9X,1HX,10X,1HY,10X,1HU,11X,1HV,12X,1HP,MAI 5830
     111X,3HRRD,9X,1HQ,11X,4HMACH,8X,1HT)                         MAI 5840
830  FORMAT (1H ,25X,4H(IN),7X,4H(IN),6X,5H(FPS),7X,5H(FPS),7X,6H(P8IA)MAI 5850
     1,6X,9H(LBM/FT3),4X,5H(MPS),10X,2HNO,8X,3H(F))                MAI 5860
840  FORMAT (1H ,25X,4H(CM),7X,4H(CM),6X,5H(MP8),7X,5H(MP8),7X,6H (KPA)MAI 5870
     1,7X,7H(KG/M3),5X,5H(MPS),10X,2HNO,8X,3H(C))                  MAI 5880
850  FORMAT (1H ,7X,215,4F12.4,F13.4,F12.6,3F12.4)                 MAI 5890
860  FORMAT (1H ,20HSOLUTION SURFACE NO.,15,3H = ,7HTIME = ,F10.8,20H SMAI 5900
     1ECONDS (DELTA T = ,F10.8,1H))                                MAI 5910
870  FORMAT (1H0,10X,5HMASS#,F9.4,10H (LBM/SEC),5X,7HTHRUST#,F11.4,6H (MAI 5920
     1LB),5X,6HMASS#,F9.4,5X,6HMASS#,F9.4)                          MAI 5930
880  FORMAT (1H0,10X,5HMASS#,F9.4,9H (KG/SEC),5X,7HTHRUST#,F11.4,10H (NMAI 5940
     1EWTONS),5X,6HMASSI#,F9.4,5X,6HMASS#,F9.4)                     MAI 5950
890  FORMAT (1H0,10X,21HBOUNDARY CONDITIONS = //,22X,1HM,11X,8HPT(P8IA)MAI 5960
     1,10X,5HTT(F),10X,10HTHETA(DEG),10X,3HPE#,F7.3,7H (PSIA),/)    MAI 5970
900  FORMAT (1H0,10X,21HBOUNDARY CONDITIONS = //,22X,1HM,11X,7HPT(KPA),MAI 5980
     112X,5HTT(C),10X,10HTHETA(DEG),10X,3HPE#,F7.3,6H (KPA),/)      MAI 5990
910  FORMAT (1H ,20X,12,10X,F7.2,10X,F7.2,10X,F7.2)                 MAI 6000
920  FORMAT (1H0,78H***** THE RADIUS OF THE CENTERBODY IS LARGER THAN TMAI 6010
     1HE NOZZLE WALL RADIUS *****)                                     MAI 6020
930  FORMAT (1X,1RH5IVS NID=0,NSTART#,14,8H,TSTART#,F14.10,1H,)       MAI 6030
940  FORMAT (1X,4HU(1,,I2,5H,1) *)                                    MAI 6040
950  FORMAT (1X,7(F10.3,1H,))                                         MAI 6050
960  FORMAT (1X,4HV(1,,I2,5H,1) *)                                    MAI 6060
970  FORMAT (1X,4HP(1,,I2,5H,1) *)                                    MAI 6070
980  FORMAT (1X,7(F10.4,1H,))                                         MAI 6080
990  FORMAT (1X,5HRO(1,,I2,5H,1) *)                                    MAI 6090
1000 FORMAT (1X,7(F10.6,1H,))                                         MAI 6100
1010 FORMAT (1X,1H$)                                                 MAI 6110
1020 FORMAT (1H0,27H***** EXPECT APPROXIMATELY ,14,20H PUNCHED CARDS **MAI 6120
     1****)                                                       MAI 6130
1030 FORMAT (1H0,31H***** EXPECT FILM OUTPUT FOR N=,I4,6H *****)    MAI 6140
1040 FORMAT (1H ,2HN#,I4)                                             MAI 6150
     END                                                       MAI 6160

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C          SUBROUTINE GEOM                                GEO  10
C          ***** THIS SUBROUTINE CALCULATES THE NOZZLE RADIUS AND OUTER NORMAL GEO 20
C          ***** GEO 30
C          ***** GEO 40
C          ***** GEO 50
C          ***** GEO 60
C          ***** GEO 70
C          ***** GEO 80
C          ***** GEO 90
C          COMMON /AV/ IAV,CAV,NST,BMP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(B1GEO 100
C          ,21),OPT(81,21)                                GEO 100
C          COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)      GEO 110
C          COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RD(81,21,2)    GEO 120
C          COMMON /CNTRL/ LMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RCAS,GAM1,GAGEO 130
C          IM2,L1,L2,L3,M1,H2,DY,DT,N,N1,N3,NASM,IVEL,ICHAR,NID,LJET,JFLAG,GEO 140
C          ZIERR,IUI,IUO,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TCGEO 150
C          3,LC,PLOW,ROLW                                GEO 160
C          COMMON /GEMTRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCT,ANGI,ANGE,XW(81),GEO 170
C          YW(81),XWI(81),YWI(81),NXNY(81),NNPTS,IINT,IDL,LT,NDIM   GEO 180
C          COMMON /GCB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,RECDB,RCICB,RCTCB,ANGICB GEO 190
C          1,ANGEGB,XCRB(81),YCRB(81),XCB(81),YCB(81),NXNYCB(81),NCBPTS,IINTCB GEO 200
C          2,IDLFCB,LCB                                GEO 210
C          COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASSI,MASSBT,THRUST,NGEO 220
C          1$TAG                                GEO 230
C          REAL MN3,NXNY,MASSI,MASSBT,NXNYCB,MASSE           GEO 240
C          GO TO (10,30,120,170), NGEOM                   GEO 250
C          CONSTANT AREA DUCT CASE                     GEO 260
C          GEO 270
C          GEO 280
C          GEO 290
C          10 PRINT 230                                GEO 300
C          IF (IUI,EQ,1) PRINT 250, XI,RI,XE           GEO 310
C          IF (IUI,EQ,2) PRINT 260, XI,RI,XE           GEO 320
C          LT=LMAX                                GEO 330
C          DX=(XE-XI)/(LMAX-1)                      GEO 340
C          XT=XE                                GEO 350
C          RT=RI                                GEO 360
C          RE=RI                                GEO 370
C          DO 20 L=1,LMAX                          GEO 380
C          YH(L)=RI                                GEO 390
C          NXNY(L)=0,0                            GEO 400
C          CONTINUE                                GEO 410
C          IF (JFLAG,EQ,0) GO TO 210                GEO 420
C          GEO 430
C          XWL=XI+(LJET-2)*DX                      GEO 440
C          IF (IUI,EQ,1) PRINT 370, XWL,LJET,LMAX    GEO 450
C          IF (IUI,EQ,2) PRINT 380, XWL,LJET,LMAX    GEO 460
C          GO TO 210                                GEO 470
C          GEO 480
C          CIRCULAR-ARC, CONICAL NOZZLE CASE        GEO 490
C          GEO 500
C          30 PRINT 230                                GEO 510
C          IF (RCI,EQ,0,0,0,0,0) GO TO 200            GEO 520
C          ANI=ANGI*3.141593/180,0                    GEO 530
C          ANE=ANGE*3.141593/180,0                    GEO 540
C          XTAN=XI+RCI*SIN(ANI)                      GEO 550
C          RTAN=RI+RCI*(COS(ANI)=1,0)                GEO 560
C          RTI=RT=RCT*(COS(ANI)=1,0)                 GEO 570
C          XT1=XTAN+(RTAN-RTI)/TAN(ANI)             GEO 580
C          IF (XT1,GE,XTAN) GO TO 40                  GEO 590
C          XT1=XTAN                                GEO 600
C          RTI=RTAN                                GEO 610
C          XT=XT1+RCT*SIN(ANI)                      GEO 620
C          XT2=XT+RCT*SIN(ANE)                      GEO 630
C          RT2=RT+RCT*(1,0-COS(ANE))               GEO 640
C          RE=RT2+(XE-XT2)*TAN(ANE)                 GEO 650
C          LT=1                                    GEO 660
C          DX=(XE-XI)/(LMAX-1)                      GEO 670
C          IF (IUI,EQ,1) PRINT 270, XI,RI,RT,XE,RCI,RCT,ANGI,ANGE,XT,RE    GEO 680
C          IF (IUI,EQ,2) PRINT 280, XI,RI,RT,XE,RCI,RCT,ANGI,ANGE,XT,RE    GEO 690
C          DO 110 L=1,LMAX                          GEO 700
C          X=XI+(L-1)*DX                           GEO 710
C          IF (X,GE,XI,AND,X,LE,XTAN) GO TO 50       GEO 720
C          IF (X,GT,XTAN,AND,X,LE,XT1) GO TO 60       GEO 730
C          IF (X,GT,XT1,AND,X,LE,XT) GO TO 70        GEO 740
C          IF (X,GT,XT,AND,X,LE,XT2) GO TO 80        GEO 750
C          IF (X,GT,XT2,AND,X,LE,XE) GO TO 90        GEO 760
C          GEO 770
C          50 YH(L)=RI+RCI*(COS(ASIN((X-XI)/RCI))=1,0)    GEO 780
C          NXNY(L)=(X-XI)/(YH(L)-RI+RCI)             GEO 790
C          GO TO 100                                GEO 800
C          GEO 810
C          60 YH(L)=RT1+(XT1-X)*TAN(ANI)              GEO 820
C          NXNY(L)=TAN(ANI)                         GEO 830
C          GO TO 100                                GEO 840

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C
70      YW(L)=RT+RCT*(1.0-COS(ASIN((XT-X)/RCT)))
      NXNY(L)=(XT-X)/(RCT+RT+YW(L))
      GO TO 100
C
80      YW(L)=RT+RCT*(1.0-COS(ASIN((X-XT)/RCT)))
      NXNY(L)=(XT-X)/(RCT+RT-YW(L))
      GO TO 100
C
90      YW(L)=RT2+(X-XT2)*TAN(ANE)
      NXNY(L)=-TAN(ANE)
C
100     IF (L,EQ,1) GO TO 110
      IF (YW(L),LT,YW(LT)) LT=L
110     CONTINUE
      IF (JFLAG,EQ,0) GO TO 210
C
120     XWL=XI+(LJET=2)*DX
      IF (IUI,EQ,1) PRINT 370, XWL,LJET,LMAX
      IF (IUI,EQ,2) PRINT 380, XWL,LJET,LMAX
      GO TO 210
C
C      GENERAL NOZZLE CASE ~ INPUT WALL COORDINATES ONLY
C
120     PRINT 240
      PRINT 230
      XI=XWI(1)
      XE=XWI(NWPTS)
      DX=(XE-XI)/(LMAX=1)
      XW(1)=XI
      XW(LMAX)=XE
      YW(1)=YWI(1)
      YW(LMAX)=YWI(NWPTS)
      RI=YW(1)
      RE=YW(LMAX)
      LT=1
      DO 130 L=2,NWPTS
      IF (YWI(L),LE,YWI(LT)) LT=L
130     CONTINUE
      XT=XWI(LT)
      RT=YWI(LT)
      IF (IUI,EQ,1) PRINT 290, XT,RT,IINT,IDIIF
      IF (IUI,EQ,2) PRINT 300, XT,RT,IINT,IDIIF
      LT=1
      L1=LMAX=1
      IP=1
      DO 140 L=2,L1
      XW(L)=XI+DX*(L-1)
      CALL MTLUP (XW(L),YW(L),IINT,NWPTS,NWPTS,1,IP,XWI,YWI)
      IF (L,EQ,1) GO TO 140
      IF (YWI(L),LE,YWI(LT)) LT=L
140     CONTINUE
      LDUM=NWPTS
      IF (LMAX,GT,NWPTS) LDUM=LMAX
      DO 160 L=1,LDUM
      IF (L,GT,LMAX) GO TO 150
      SLOPE=IDIIF(L,IDIIF,LMAX,XW,YW)
      NXNY(L)=-SLOPE
      IF (L,LE,NWPTS,AND,L,LE,LMAX) PRINT 330, L,XWI(L),YWI(L),XW(L),YW(GEO 1430
$L),SLOPE
      IF (L,GT,NWPTS,AND,L,LE,LMAX) PRINT 340, L,XW(L),YW(L),SLOPE
      IF (L,LE,NWPTS,AND,L,GT,LMAX) PRINT 350, L,XWI(L),YWI(L)
160     CONTINUE
      IF (JFLAG,EQ,0) GO TO 210
C
      IF (IUI,EQ,1) PRINT 370, XW(LJET=1),LJET,LMAX
      IF (IUI,EQ,2) PRINT 380, XW(LJET=1),LJET,LMAX
      GO TO 210
C
C      GENERAL NOZZLE CASE ~ INPUT WALL COORDINATES AND SLOPES
C
170     PRINT 240
      PRINT 230
      DX=(XE-XI)/(LMAX=1)
      RI=YW(1)
      RE=YW(LMAX)
      LT=1
      DO 180 L=2,LMAX
      IF (YWI(L),LE,YWI(LT)) LT=L
180     CONTINUE
      XT=XI+(LT=1)*DX
      RT=YWI(LT)
      IF (IUI,EQ,1) PRINT 310, XT,RT

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      IF (IUI,EQ,2) PRINT 320, XT,RT           GEO 1680
      DO 190 L=1,LMAX                         GEO 1690
      XW(L)=XI+DX*(L-1)                      GEO 1700
      SLOPE=-NXNY(L)                          GEO 1710
      PRINT 360, L,XW(L),YW(L),SLOPE          GEO 1720
190   CONTINUE                                GEO 1730
      IF (JFLAG,EQ,0) GO TO 210               GEO 1740
C
      IF (IUI,EQ,1) PRINT 370, XW(LJET-1),LJET,LMAX    GEO 1750
      IF (IUI,EQ,2) PRINT 380, XW(LJET-1),LJET,LMAX    GEO 1760
      GO TO 210                                GEO 1770
GEO 1780
C
200   PRINT 390                                GEO 1790
      IERR=1                                  GEO 1800
      RETURN                                 GEO 1810
C
210   IF (IUI,EQ,1) RETURN                     GEO 1820
      DO 220 L=1,LMAX                         GEO 1830
      YW(L)=YW(L)/2,54                        GEO 1840
220   CONTINUE                                GEO 1850
      XT=XT/2,54                             GEO 1860
      RT=RT/2,54                             GEO 1870
      IF (NGCB,NE,0) RETURN                   GEO 1880
      XI=XI/2,54 S XE=XE/2,54                 GEO 1890
      DX=DX/2,54                             GEO 1900
      RETURN                                 GEO 1910
GEO 1920
C
C   FORMAT STATEMENTS
C
230   FORMAT (1H0,18X,17HNOZZLE GEOMETRY -)        GEO 1930
240   FORMAT (1H1)                                GEO 1940
250   FORMAT (1H0,20X,46HA CONSTANT AREA DUCT HAS BEEN SPECIFIED BY XI=,GEO 1950
      1F8,4,10H (IN), RI=,F8,4,14H (IN), AND XE=,F8,4,5H (IN))    GEO 1960
260   FORMAT (1H0,20X,46HA CONSTANT AREA DUCT HAS BEEN SPECIFIED BY XI=,GEO 1970
      1F8,4,10H (CM), RI=,F8,4,14H (CM), AND XE=,F8,4,5H (CM))    GEO 1980
270   FORMAT (1H0,20X,56HA CIRCULAR-ARC, CONICAL NOZZLE HAS BEEN SPECIFIED BY XI=,GEO 1990
      1ED BY XI=,F8,4,10H (IN), RI=,F8,4,6H (IN),,/,21X,3HRT=,F8,4,10H (IGEO 2000
      2N), XE=,F8,4,11H (IN), RCI=,F8,4,11H (IN), RCT=,F8,4,12H (IN), ANGGEO 2010
      3I=,F6,2,7H (DEG),,/,21X,9HAND ANGE=,F6,2,35H (DEG), THE COMPUTED VGEOD 2020
      4ALUES ARE XT=,F8,4,13H (IN) AND RE=,F8,4,6H (IN),)           GEO 2030
280   FORMAT (1H0,20X,56HA CIRCULAR-ARC, CONICAL NOZZLE HAS BEEN SPECIFIED BY XI=,GEO 2040
      1ED BY XI=,F8,4,10H (CM), RI=,F8,4,6H (CM),,/,21X,3HRT=,F8,4,10H (GEO 2050
      2M), XE=,F8,4,11H (CM), RCI=,F8,4,11H (CM), RCT=,F8,4,12H (CM), ANGGEO 2060
      3I=,F6,2,7H (DEG),,/,21X,9HAND ANGE=,F6,2,35H (DEG), THE COMPUTED VGEOD 2070
      4ALUES ARE XT=,F8,4,13H (CM) AND RE=,F8,4,6H (CM),)           GEO 2080
290   FORMAT (1H0,20X,68HA GENERAL NOZZLE HAS BEEN SPECIFIED BY THE FOLLOWING PARAMETERS, XT=,F8,4,10H (IN), RT=,F8,4,6H (IN),,/,21X,5HIINGEO 2090
      2T=,I,7H, IDTF=,I,1H,,/,22X,1HL,10X,7HXW(IN),10X,7HYW(IN),11X,GEO 2100
      36HXW(IN),11X,6HYW(IN),12X,5HSLOPE,/ )                      GEO 2110
300   FORMAT (1H0,20X,68HA GENERAL NOZZLE HAS BEEN SPECIFIED BY THE FOLLOWING PARAMETERS, XT=,F8,4,10H (CM), RT=,F8,4,6H (CM),,/,21X,5HIINGEO 2120
      2T=,I,7H, IDTF=,I,1H,,/,22X,1HL,10X,7HXW(CM),10X,7HYW(CM),11X,GEO 2130
      36HXW(CM),11X,6HYW(CM),12X,5HSLOPE,/ )                      GEO 2140
310   FORMAT (1H0,20X,68HA GENERAL NOZZLE HAS BEEN SPECIFIED BY THE FOLLOWING PARAMETERS, XT=,F8,4,10H (IN), RT=,F8,4,6H (IN),,/,22X,1HL,GEO 2150
      2T=,I,7H, IDTF=,I,1H,,/,22X,1HL,10X,7HXW(CM),10X,7HYW(CM),11X,GEO 2160
      36HXW(CM),11X,6HYW(CM),12X,5HSLOPE,/ )                      GEO 2170
320   FORMAT (1H0,20X,68HA GENERAL NOZZLE HAS BEEN SPECIFIED BY THE FOLLOWING PARAMETERS, XT=,F8,4,10H (CM), RT=,F8,4,6H (CM),,/,22X,1HL,GEO 2180
      2T=,I,7H, IDTF=,I,1H,,/,22X,1HL,10X,7HXW(CM),10X,7HYW(CM),11X,GEO 2190
      36HXW(CM),11X,6HYW(CM),12X,5HSLOPE,/ )                      GEO 2200
330   FORMAT (1H ,20X,I2,7X,F10,4,7X,F10,4,7X,F10,4,7X,F10,4)    GEO 2210
340   FORMAT (1H ,20X,I2,4X,F10,4,7X,F10,4,7X,F10,4)              GEO 2220
      211X,6HXW(IN),11X,6HYW(IN),12X,5HSLOPE,/ )                  GEO 2230
350   FORMAT (1H ,20X,I2,7X,F10,4,7X,F10,4)                        GEO 2240
      211X,6HXW(CM),11X,6HYW(CM),12X,5HSLOPE,/ )                  GEO 2250
360   FORMAT (1H ,20X,I2,7X,F10,4,7X,F10,4,7X,F10,4)              GEO 2260
370   FORMAT (1H0,20X,69HAN EXHAUST JET CALCULATION HAS BEEN REQUESTED, GEO 2270
      1 THE NOZZLE ENDS AT X=,F8,4,11H (IN). THE //,21X,14HMESH POINTS L=GEO 2280
      2,I3,6H TO L=,I3,5BH ARE AN INITIAL APPROXIMATION TO THE EXHAUST JET GEO 2290
      3T BOUNDARY.)                                              GEO 2300
380   FORMAT (1H0,20X,69HAN EXHAUST JET CALCULATION HAS BEEN REQUESTED, GEO 2310
      1 THE NOZZLE ENDS AT X=,F8,4,11H (CM). THE //,21X,14HMESH POINTS L=GEO 2320
      2,I3,6H TO L=,I3,5BH ARE AN INITIAL APPROXIMATION TO THE EXHAUST JET GEO 2330
      3T BOUNDARY.)                                              GEO 2340
390   FORMAT (1H0,8UHRRRR RCI OR RCT WAS SPECIFIED AS ZERO *****)    GEO 2350
      END                                     GEO 2360
GEO 2370
GEO 2380
GEO 2390
GEO 2400

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SUBROUTINE GEOMCB                                GCB  10
C
C ***** THIS SUBROUTINE CALCULATES THE CENTERBODY RADIUS AND SLOPE ***** GCB 20
C
C DIMENSION YM(81), NXNY(81)                      GCB 30
C COMMON /AV/ IAV,CAV,NST,SMP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81,GCB 100
1,21),QPT(81,21)                                GCB 40
C COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)        GCB 50
C COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RD(81,21,2) GCB 60
C COMMON /CNTRL/ LMAX,MMAX,NMAX,NPRINT,TCONV,FOT,GAMMA,RGA8,GAMI,GAGCB 140
1M,L1,L2,L3,M1,M2,DY,DT,N,N1,N3,NASM,IVEL,ICHAR,NID,LJET,JFLAG,GCB 150
2IERR,IUI,IUD,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTAR,NPLOT,G,PC,TCGCB 160
3,LC,PLOW,ROLW                                GCB 170
COMMON /GCB/ NGCB,XICB,RTCB,XECB,RECB,RCICB,RCTCB,ANGICB,GCB 180
1,ANGECB,XCB(81),YCB(81),XCB(81),YCB(81),NXNYCB(81),NCBPTS,IINTCB,GCB 190
2,IDIFCB,LECB                                GCB 200
COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MA8SE,MA8SI,MA8ST,THRUST,NGCB 210
1$TAG
REAL MN3,NXNY,MA8SI,MA8ST,NXNYCB,MA8SE                                GCB 220
GCB 230
GCB 240
GCB 250
GCB 260
GCB 270
GCB 280
GCB 290
GCB 300
GCB 310
GCB 320
GCB 330
GCB 340
GCB 350
GCB 360
GCB 370
GCB 380
GCB 390
GCB 400
GCB 410
GCB 420
GCB 430
GCB 440
GCB 450
GCB 460
GCB 470
GCB 480
GCB 490
GCB 500
GCB 510
GCB 520
GCB 530
GCB 540
GCB 550
GCB 560
GCB 570
GCB 580
GCB 590
GCB 600
GCB 610
GCB 620
GCB 630
GCB 640
GCB 650
GCB 660
GCB 670
GCB 680
GCB 690
GCB 700
GCB 710
GCB 720
GCB 730
GCB 740
GCB 750
GCB 760
GCB 770
GCB 780
GCB 790
GCB 800
GCB 810
GCB 820
GCB 830
C
GO TO (10,30,120,160), NGCB
C
CYLINDRICAL CENTERBODY CASE
C
10 IF (IUI,EQ,1) PRINT 230, XICB,RICB,XECB      GCB 300
IF (IUI,EQ,2) PRINT 240, XICB,RICB,XECB      GCB 310
LECB=LMAX
DO 20 L=1,LMAX
YCB(L)=RICB
NXNYCB(L)=0,0
20 CONTINUE
GO TO 200
C
CIRCULAR-ARC, CONICAL CENTERBODY CASE
C
30 XI=XICB
RI=RICB
RT=RTCB
XE=XECB
RCI=RCICB
RCT=RCTCB
ANGI=ANGICB
ANGE=ANGECB
RI=2,0*RT+RI
IF (RCI,EQ,0,0,OR,RCT,EQ,0,0) GO TO 190
ANI=ANGI*3,141593/180,0
ANE=ANGE*3,141593/180,0
XTAN=XI+RCI*SIN(ANI)
RTAN=RI+RCI*(COS(ANI)=1,0)
RT1=RT-RCT*(COS(ANI)=1,0)
XT1=XTAN+(RTAN+RT1)/TAN(ANI)
IF (XT1,GE,XTAN) GO TO 40
XT1=XTAN
RT1=RTAN
40 XT=XT1+RCT*SIN(ANI)
XTCB=XT
XT2=XT+RCT*SIN(ANE)
RT2=RT+RCT*(1,0=COS(ANE))
RE=RT2+(XE=XT2)*TAN(ANE)
RECB=RE
RI=2,0*RT+RI
RE=2,0*RT-RE
IF (IUI,EQ,1) PRINT 250, XI,RI,RT,XE,RCI,RCT,ANGI,ANGE,XT,RE      GCB 680
IF (IUI,EQ,2) PRINT 260, XI,RI,RT,XE,RCI,RCT,ANGI,ANGE,XT,RE      GCB 690
RI=2,0*RT-RI
RE=2,0*RT-RE
DO 110 L=1,LMAX
X=XI+(L-1)*DX
IF (X,GE,XI,AND,X,LE,XTAN) GO TO 50
IF (X,GT,XTAN,AND,X,LE,XT1) GO TO 60
IF (X,GT,XT1,AND,X,LE,XT) GO TO 70
IF (X,GT,XT,AND,X,LE,XT2) GO TO 80
IF (X,GT,XT2,AND,X,LE,XE) GO TO 90
C
50 YM(L)=RI+RCI*(COS(ASIN((X-XI)/RCI))=1,0)
NXNY(L)=(X-XI)/(YM(L)+RI+RCI)
GO TO 100
C

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60      YH(L)=RT1+(XT1-X)*TAN(ANI)          GCB  840
      NXNY(L)=TAN(ANI)                      GCB  850
      GO TO 100                            GCB  860
C
70      YH(L)=RT+RCT*(1,0=COS(ASIN((XT-X)/RCT))) GCB  870
      NXNY(L)=(XT-X)/(RCT+RT=YH(L))        GCB  880
      GO TO 100                            GCB  890
C
80      YH(L)=RT+RCT*(1,0=COS(ASIN((X-XT)/RCT))) GCB  900
      NXNY(L)=(XT-X)/(RCT+RT=YH(L))        GCB  910
      GO TO 100                            GCB  920
C
90      YH(L)=RT2+(X-XT2)*TAN(ANE)          GCB  930
      NXNY(L)=<TAN(ANE)                    GCB  940
C
100     YCB(L)=2,0*RTCB-YH(L)              GCB  950
      NXNYCB(L)=NXNY(L)                   GCB  960
      IF (YCB(L),GE,0,0) GO TO 110        GCB  970
      YCB(L)=0,0                          GCB  980
      NXNYCB(L)=0,0                      GCB  990
110     CONTINUE                           GCB 1000
      GO TO 200                            GCB 1010
C
C      GENERAL CENTERBODY CASE = INPUT CENTERBODY COORDINATES ONLY GCB 1020
C
120     PRINT 220                           GCB 1030
      IF (IUI,EQ,1) PRINT 270, IINTCB, IDIFCB   GCB 1040
      IF (IUI,EQ,2) PRINT 280, IINTCB, IDIFCB   GCB 1050
      L1=LMAX=1                         GCB 1060
      IP=>
      DO 130 L=1,LMAX                  GCB 1070
      XCB(L)=XICB+DX*(L=1)             GCB 1080
      CALL MTLUP (XCB(L),YCB(L),IINTCB,NCBPTS,NCBPTS,1,IP,XCBI,YCBI) GCB 1090
130     CONTINUE                           GCB 1100
      LDUM=NCBPTS                      GCB 1110
      IF (LMAX,GT,NCBPTS) LDUM=LMAX        GCB 1120
      DO 150 L=1,LDUM                  GCB 1130
      IF (L,GT,LMAX) GO TO 140          GCB 1140
      SLOPE=DIF(L, IDIFCB, LMAX, XCB, YCB)  GCB 1150
      NXNYCB(L)=SLOPE                  GCB 1160
      IF (YCB(L),GE,0,0) GO TO 140        GCB 1170
      YCB(L)=0,0                        GCB 1180
      NXNYCB(L)=0,0                      GCB 1190
      SLOPE=-NXNYCB(L)                  GCB 1200
140     IF (L,LE,NCBPTS,AND,L,LE,LMAX) PRINT 310, L,XCBI(L),YCBI(L),XCB(L) GCB 1210
      1,YCBL(L),SLOPE                  GCB 1220
      IF (L,GT,NCBPTS,AND,L,LE,LMAX) PRINT 320, L,XCB(L),YCB(L),SLOPE  GCB 1230
      IF (L,LE,NCBPTS,AND,L,GT,LMAX) PRINT 330, L,XCBI(L),YCBI(L)        GCB 1240
150     CONTINUE                           GCB 1250
      GO TO 200                            GCB 1260
C
C      GENERAL CENTERBODY CASE = INPUT CENTERBODY COORDINATES AND SLOPES GCB 1270
C
160     PRINT 220                           GCB 1280
      IF (IUI,EQ,1) PRINT 290             GCB 1290
      IF (IUI,EQ,2) PRINT 300             GCB 1300
      DO 180 L=1,LMAX                  GCB 1310
      XCB(L)=XICB+DX*(L=1)             GCB 1320
      IF (YCB(L),GE,0,0) GO TO 170        GCB 1330
      YCB(L)=0,0                        GCB 1340
      NXNYCB(L)=0,0                      GCB 1350
      SLOPE=-NXNYCB(L)                  GCB 1360
170     PRINT 340, L,XCB(L),YCB(L),SLOPE  GCB 1370
180     CONTINUE                           GCB 1380
      GO TO 200                            GCB 1390
C
190     PRINT 350                           GCB 1400
      IERR=>
      RETURN                             GCB 1410
C
200     IF (IUI,EQ,1) RETURN             GCB 1420
      DO 210 L=1,LMAX                  GCB 1430
      YCB(L)=YCB(L)/2,54                GCB 1440
210     CONTINUE                           GCB 1450
      XICB=XICB/2,54                  GCB 1460
      XECB=XECB/2,54                  GCB 1470
      DX=DX/2,54                       GCB 1480
      RETURN                             GCB 1490
C
C      FORMAT STATEMENTS                 GCB 1500
C

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220 FORMAT (1H1) GCB 1650
230 FORMAT (1H0,20X,52HA CYLINDRICAL CENTERBODY HAS BEEN SPECIFIED BY GCB 1660
1XICB=F8,4,12H (IN), RICB=F8,4,16H (IN), AND XECB=F8,4,5H (IN)) GCB 1670
240 FORMAT (1H0,20X,52HA CYLINDRICAL CENTERBODY HAS BEEN SPECIFIED BY GCB 1680
1XICB=F8,4,12H (CM), RICB=F8,4,16H (CM), AND XECB=F8,4,5H (CM)) GCB 1690
250 FORMAT (1H0,20X,62HA CIRCULAR-ARC, CONICAL CENTERBODY HAS BEEN SPECIFIED BY GCB 1700
1CIFIED BY XICB=F8,4,5H (IN),7H, RICB=F8,4,6H (IN),,,/21X,5HRTCB=GCB 1710
2,F8,4,7H (IN), ,5HXECB=F8,4,5H (IN),8H, RCICB=F8,4,5H (IN),8H, RGCB 1720
3CTCB=F8,4,5H (IN),9H, ANGICB=F6,2,7H (DEG),,,/21X,11HAND ANGECB=GCB 1730
4,F6,2,8H (DEG), .29HTHE COMPUTED VALUES ARE XTCB=F8,4,5H (IN),10HGC8 1740
5,AND RECB=F8,4,6H (IN),) GCB 1750
260 FORMAT (1H0,20X,62HA CIRCULAR-ARC, CONICAL CENTERBODY HAS BEEN SPECIFIED BY GCB 1760
1CIFIED BY XICB=F8,4,5H (CM),7H, RICB=F8,4,6H (CM),,,/21X,5HRTCB=GCB 1770
2,F8,4,7H (CM), ,5HXECB=F8,4,5H (CM),8H, RCICB=F8,4,5H (CM),8H, RGCB 1780
3CTCB=F8,4,5H (CM),9H, ANGICB=F6,2,7H (DEG),,,/21X,11HAND ANGECB=GCB 1790
4,F6,2,8H (DEG), .29HTHE COMPUTED VALUES ARE XTCB=F8,4,5H (CM),10HGC8 1800
5,AND RECB=F8,4,6H (CM),) GCB 1810
270 FORMAT (1H0,20X,76HA GENERAL CENTERBODY HAS BEEN SPECIFIED BY THE GCB 1820
1FOLLOWING PARAMETERS, IINTCB=I1,9H, IDIFCB=I1,1H,,/22X,IHL,10XGCB 1830
2,8HXCBI(IN),10X,8HYCBI(IN),9X,7HXCBI(IN),10X,7HYCBI(IN),11X,5HSLOPE,GCB 1840
3/) GCB 1850
280 FORMAT (1H0,20X,76HA GENERAL CENTERBODY HAS BEEN SPECIFIED BY THE GCB 1860
1FOLLOWING PARAMETERS, IINTCB=I1,9H, IDIFCB=I1,1H,,/22X,IHL,10XGCB 1870
2,8HXCBI(CM),10X,8HYCBI(CM),9X,7HXCBI(CM),10X,7HYCBI(CM),11X,5HSLOPE,GCB 1880
3/) GCB 1890
290 FORMAT (1H0,20X,68HA GENERAL CENTERBODY HAS BEEN SPECIFIED BY THE GCB 1900
1FOLLOWING PARAMETERS,,/22X,IHL,11X,7HXCBI(IN),10X,7HYCBI(IN),11X,5GCB 1910
2HSLOPE,/ ) GCB 1920
300 FORMAT (1H0,20X,68HA GENERAL CENTERBODY HAS BEEN SPECIFIED BY THE GCB 1930
1FOLLOWING PARAMETERS,,/22X,IHL,11X,7HXCBI(CM),10X,7HYCBI(CM),11X,5GCB 1940
2HSLOPE,/ ) GCB 1950
310 FORMAT (1H ,20X,I2,7X,F10,4,7X,F10,4,7X,F10,4,7X,F10,4,7X,F10,4) GCB 1960
320 FORMAT (1H ,20X,I2,4IX,F10,4,7X,F10,4,7X,F10,4) GCB 1970
330 FORMAT (1H ,20X,I2,7X,F10,4,7X,F10,4) GCB 1980
340 FORMAT (1H ,20X,I2,7X,F10,4,7X,F10,4,7X,F10,4) GCB 1990
350 FORMAT (1H0,48H***** RCICB OR RCTCB WAS SPECIFIED AS ZERO *****) GCB 2000
END GCB 2010

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SUBROUTINE MTLUP(X,Y,M,N,MAX,NTAB,I,VARI,VARD)          MTL 10
C
C ***** THIS SUBROUTINE IS CALLED BY SUBROUTINE GEOM TO INTERPOLATE FOR MTL 20
C EQUALLY SPACED NOZZLE WALL COORDINATES FOR THE TABULAR INPUT MTL 30
C CASE. SUBROUTINE MTLUP WAS TAKEN FROM THE NASA-LANGLEY PROGRAM MTL 40
C LIBRARY. THE DATE OF THIS VERSION IS 09-12-69.           MTL 50
C
C ***** MODIFICATION OF LIBRARY INTERPOLATION SUBROUTINE FTLUP MTL 60
C MULTIPLE TABLE LOOK-UP ON ONE INDEPENDENT VARIABLE TABLE MTL 70
C USES AN EXTERNAL INTERVAL POINTER (I) TO START SEARCH MTL 80
C I LESS THAN 0 WILL CHECK MONOTONICITY                  MTL 90
C
C DIMENSION VARI(1), VARD(MAX,1), Y(1), V(3), YY(2)      MTL 100
C LOGICAL EX                                              MTL 110
C
C IF (M,EQ,0) GO TO 170                                 MTL 120
C IF (N,LE,1) GO TO 170                                 MTL 130
C EX=F,                                                 MTL 140
C IF (I,GE,0) GO TO 60                                 MTL 150
C IF (N,LT,2) GO TO 60                                 MTL 160
C
C MONOTONICITY CHECK                                     MTL 170
C
C IF (VARI(2)-VARI(1)) 20,20,40                      MTL 180
C
C ERROR IN MONOTONICITY                                MTL 190
C
10 K=LOCF(VARI(1))                                     MTL 200
PRINT 190, J,K,(VARI(J),J=1,N)                         MTL 210
STOP                                                    MTL 220
C
C MONOTONIC DECREASING                                MTL 230
C
20 DO 30 J=2,N                                         MTL 240
IF (VARI(J)-VARI(J-1)) 30,10,10                      MTL 250
30 CONTINUE                                              MTL 260
GO TO 60                                               MTL 270
C
C MONOTONIC INCREASING                                MTL 280
C
40 DO 50 J=2,N                                         MTL 290
IF (VARI(J)-VARI(J-1)) 10,10,50                      MTL 300
50 CONTINUE                                              MTL 310
C
C INTERPOLATION                                       MTL 320
C
60 IF (I,LE,0) I=1                                      MTL 330
IF (I,GE,N) I=N-1                                      MTL 340
C
C LOCATE I INTERVAL (X(I),LE,X,LT,X(I+1))            MTL 350
C
C IF ((VARI(I)-X)*(VARI(I+1)-X)) 100,100,70          MTL 360
C
C IN GIVES DIRECTION FOR SEARCH OF INTERVALS        MTL 370
C
70 IN=SIGN(1,0,(VARI(I+1)-VARI(I))*(X-VARI(I)))     MTL 380
C
C IF X OUTSIDE ENDPOINTS, EXTRAPOLATE FROM END INTERVAL MTL 390
C
80 IF (((I+IN),LE,0) GO TO 90                          MTL 400
IF (((I+IN),GE,N) GO TO 90                          MTL 410
I=I+IN                                              MTL 420
IF ((VARI(I)-X)*(VARI(I+1)-X)) 100,100,80          MTL 430
C
C EXTRAPOLATION                                     MTL 440
C
90 EX=T,                                                MTL 450
100 IF (M,EQ,2) GO TO 120                            MTL 460
C
C FIRST ORDER                                       MTL 470
C
110 DO 110 NT=1,NTAB                                    MTL 480
Y(NT)=(VARD(I,NT)*(VARI(I+1)-X)+VARD(I+1,NT)*(VARI(I)-X))/(VARI(I+1)-VARI(I))    MTL 490
111=VARI(I)
IF (EX) I=I+IN                                         MTL 500
RETURN                                                 MTL 510
C
C SECOND ORDER                                     MTL 520
C

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120 IF (N, EQ, 2) GO TO 10
IF (I, EQ, (N-1)) GO TO 140
IF (I, EQ, 1) GO TO 130
C
C   PICK THIRD POINT
C
SK=VARI(I+1)-VARI(I)
IF ((SK*(X-VARI(I-1))),LT,(SK*(VARI(I+2)-X))) GO TO 140
130 L=I
GO TO 150
140 L=I+1
150 V(1)=VARI(L)-X
V(2)=VARI(L+1)-X
V(3)=VARI(L+2)-X
DO 160 NT=1,NTAB
YY(1)=(VARD(L,NT)*V(2)-VARD(L+1,NT)*V(1))/(VARI(L+1)-VARI(L))
YY(2)=(VARD(L+1,NT)*V(3)-VARD(L+2,NT)*V(2))/(VARI(L+2)-VARI(L+1))
Y(NT)=(YY(1)*V(3)+YY(2)*V(1))/(VARI(L+2)-VARI(L))
160 Y(NT)=VARD(1,NT)
IF (EX) I=I+IN
RETURN
C
C   ZERO ORDER
C
170 DO 180 NT=1,NTAB
180 Y(NT)=VARD(1,NT)
RETURN
C
190 FORMAT (1H1,49H TABLE BELOW OUT OF ORDER FOR MTLUP AT POSITION ,I,MTL 1110
15,/31H X TABLE IS STORED IN LOCATION ,06,//(8G15,8))
END

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SUBROUTINE ONEDIM                               ONE   10
C
C ***** THIS SUBROUTINE CALCULATES THE 1-D INITIAL- DATA SURFACE *****      ONE   20
C
C COMMON /AV/ IAV,CAV,NST,SMP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81,ONE   30
1,21),QPT(81,21)                                ONE   40
COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)          ONE   50
COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RD(81,21,2)      ONE   60
COMMON /CNTRL/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAM1,GAONE   70
1M2,L1,L2,L3,M1,M2,DX,DY,DT,N,NI,N3,NASH,IVEL,ICHAR,NID,LJET,JFLAG,ONE   80
2IERR,IUI,IUO,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TCONE   90
3,LC,PLOW,ROLOW                                ONE 100
COMMON /GEMTRY/ NGEOM,XI,RI,XT,XE,RE,RCI,RCT,ANGI,ANGE,XW(81),ONE 110
1YW(81),XWI(81),YWI(81),NXNY(81),NWPTS,IINT,IDIF,LT,NDIM      ONE 120
COMMON /NCGB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,REC8,RCICB,RCTCB,ANGICBONE   130
1,ANGEBCB,XCB(81),YCB(81),XCB(81),YCB(81),NXNYCB(81),NCBPTS,IINTCBONE   140
2,IDIFCB,LECB                                ONE 150
COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASSI,MASST,THRUST,NONE   160
1$TAG
REAL MN3,NXNY,MASSI,MASST,NXNYCB,MA8SE        ONE 170
C
MN3=0.01
IF (NID,EQ,-1,OR,NID,GT,2) MN3=2.0           ONE 180
GRGAS=1.0/(RGAS*G)
NXCK=0
ACOEF=2.0/(GAMMA+1.0)
BCOEF=(GAMMA+1.0)/(GAMMA+1.0)
CCOEF=(GAMMA+1.0)/2.0/(GAMMA+1.0)
IF (N1D,LT,0) GO TO 20                         ONE 190
C
C OVERALL LOOP
C
IF (NGCB,NE,0) GO TO 10
RSTAR=RT
RSTAR=RT*RT
GO TO 20
10 RSTAR=YH(LT)=YCB(LT)
RSTAR=YH(LT)**2-YCB(LT)**2
20 DO 130 L=1,LMAX
IF (L,EQ,1,AND,N1D,EQ,-1) GO TO 130
IF (L,EQ,1,AND,N1D,GT,2) GO TO 130
X=XI+DX*(L-1)
IF (N1D,LT,0) GO TO 50
IF (NGCB,NE,0) GO TO 30
IF (X,LT,XT) GO TO 50
IF (X,GT,XT) GO TO 40
MN3=1.0
GO TO 100
30 IF (L,LT,LT) GO TO 50
IF (L,GT,LT) GO TO 40
MN3=1.0
GO TO 100
40 IF (NXCK,EQ,1) GO TO 50
IF (N1D,EQ,1,OR,N1D,EQ,3) MN3=1.1
IF (N1D,EQ,2,OR,N1D,EQ,4) MN3=0.9
NXCK=1
50 IF (NDJM,EQ,1) GO TO 60
RAD=YH(L)=YCB(L)
ARATIO=RAD/RSTAR
GO TO 70
60 RAD=YH(L)**2-YCB(L)**2
ARATIO=RAD9/RBTARS
C
C NEWTON-RAPHSON ITERATION LOOP
C
70 DO 90 ITER=1,20
ABM=ACOEF+BCOEF+MN3*MN3
ABMC=ABM*CCOEF
FM=ABMC/MN3*ARATIO
FPM=ABMC*(2.0*BCOEF*CCOEF/ABM-1.0/(MN3+MN3))
OMN3=MN3
MN3=OMN3-FM/FPM
IF (MN3,GT,1.0,AND,OMN3,LT,1.0) MN3=0.99
IF (MN3,LT,1.0,AND,OMN3,GT,1.0) MN3=1.01
IF (MN3,GE,0.0) GO TO 80
MN3=MN3
GO TO 90
80 IF (ABS(MN3-OMN3)/OMN3,LE,0.0005) GO TO 100
90 CONTINUE
PRINT 140, L

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```

C      FILL IN 2-D ARRAYS LOOP
C
100  DEM=1,0+GAM2*MN3*MN3          ONE  850
      DEMP=DEM**GAM1                  ONE  860
      DNXNY=(NXNY(L)=NXNYCB(L))/M$    ONE  870
      DO 120 M=1,MMAX                 ONE  880
      P(L,M,1)=PT(M)/DEMP            ONE  890
      TEMP=TT(M)/DEM                ONE  900
      ROCL,M,1)=P(L,M,1)*GRGAS/TEMP  ONE  910
      Q=MN3*SQRT(GAMMA*P(L,M,1)/RO(L,M,1))  ONE  920
      DN=NXNYCB(L)+DNXNY*(M=1)        ONE  930
      DNS=DN*DN                      ONE  940
      IF (DNS,EQ,0,0) GO TO 110      ONE  950
      SIGN=1,0                        ONE  960
      IF (DN,GT,0,0) SIGN=-1,0        ONE  970
      U(L,M,1)=Q/SQRT(1,0+DNS)       ONE  980
      V(L,M,1)=SIGN*Q/SQRT(1,0+1,0/DNS)  ONE  990
      GO TO 120                      ONE 1000
110   U(L,M,1)=Q                  ONE 1010
      V(L,M,1)=0,0                    ONE 1020
120   CONTINUE                     ONE 1030
130   CONTINUE                     ONE 1040
      RETURN                         ONE 1050
C
140   FORMAT (1H0,10X,93H***** THE 1-D SOLUTION FOR THE INITIAL- DATA IS UNONE 1100
      FACE FAILED TO CONVERGE IN 20 ITERATIONS AT L=,I2,6H *****)  ONE 1110
      END                            ONE 1120

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C          SUBROUTINE MAP(IP,L,M,AL,BE,DE,LDI,AL1,BE1,DE$)
C          ***** THIS SUBROUTINE CALCULATES THE MAPPING FUNCTIONS *****
C          ***** COMMON STATEMENT LIST *****
C          COMMON /AV/ TAV,CAV,NST,SMP,LSS,CIA,XMU,XLA,RKMU,QUT(81,21),QVT(81)MAP
C          1,21),OPT(81,21)
C          COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)
C          COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RD(81,21,2)
C          COMMON /CNTRL/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAM1,GAMAP
C          1M2,L1,L2,L3,M1,M2,DX,DY,DT,N,N1,N3,NASM,IVEL,ICHAR,NID,LJET,JFLAG,MAP
C          2IERR,IUI,IUO,DXR,DYR,LD,MD,LMDI,LMD3,IB,RSTAR,R3TARS,NPLOT,G,PC,TCMAP
C          3,LC,PLOW,HOLOW
C          COMMON /GEMTRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCT,ANGI,ANGE,XW(81),MAP
C          1YW(81),XWI(81),NXNY(A1),NWPT8,IINT,IDL,LT,NDIM
C          COMMON /GCB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,RECB,RCICB,RCTCB,ANGICBMAP
C          1,ANGECB,XCB(A1),YCB(81),XCB(81),YCB(81),NXNYCB(81),NCBPTS,IINTCBMAP
C          2,IDLFCB,LECB
C          COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASS,E,MASSI,MASST,THRUST,NMAP
C          1STAG
C          REAL MN3,NXNY,MASSI,MAST,NXNYCB,MASSE
C
C          BE=1.0/(YW(L)-YCB(L))
C          IF (IP,EQ,0) RETURN
C          Y=(M=1)*DY
C          AL=BE*(NXNYCB(L)+Y*(NXNY(L)-NXNYCB(L)))
C          DE=BE*Y*XWI(L)
C          IF (IP,EQ,1) RETURN
C          BE1=1.0/(YW(LDI)-YCB(LD))
C          AL1=BE1*(NXNYCB(LD)+Y*(NXNY(LD)-NXNYCB(LD)))
C          DE1=BE1*Y*XWI(LD)
C          RETURN
C          END

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C          SUBROUTINE MASFL0(ISURF)                                MAS   10
C          ***** THIS SUBROUTINE CALCULATES THE INITIAL=DATA OR SOLUTION SURFACE    MAS  20
C          MASS FLOW AND THRUST                                              MAS  30
C          *****                                                               MAS  40
C          *****                                                               MAS  50
C          *****                                                               MAS  60
C          *****                                                               MAS  70
C          *****                                                               MAS  80
C          *****                                                               MAS  90
C          COMMON /AV/ IAV,CAV,NST,SMP,LSS,CTA,XMU,XLA,RKMU,QUT(B1,21),QVT(B1,MAS 100
1,21),QPT(B1,21)
C          COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)                      MAS 110
C          COMMON /SOLUTN/ U(B1,21,2),V(B1,21,2),P(B1,21,2),RD(B1,21,2)      MAS 120
C          COMMON /CNTRL/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAM1,GAMAS 130
1,M2,L1,L2,L3,M1,M2,DY,DY,DT,N,N1,N3,NASH,IVEL,ICHAR,N1D,LJET,JFLAG,MAS 140
2,IERR,IUI,IUO,DXR,DXR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARs,NPLOT,G,PC,TCHAS 150
3,LC,PLOW,ROLW                                         MAS 160
C          COMMON /GEMTRYC/ NGEDM,XI,RI,XT,RT,XE,RE,RCI,RCT,ANGI,ANGE,XW(B1),MAS 160
1,YH(B1),XWI(B1),YWI(B1),NXNY(B1),NNPTS,JINT,JDIF,LT,NDIM               MAS 170
C          COMMON /GCB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,RECB,RCICB,RCTCB,ANGICBMAS 180
1,ANGEBC,XCB(B1),YCB(B1),XCB(S1),YCB(S1),NXNYCB(B1),NCBPTS,IINTCBMAS 190
2,JDIFCB,LECB                                         MAS 200
C          COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASSI,MASST,THRUST,NMAS 210
1,STAG                                         MAS 220
REAL MN3,NXNY,MASSI,MASST,NXNYCB,MASSE                         MAS 230
C          LC2=LC*LC                                         MAS 240
C          LDUM=LMAX=1                                         MAS 250
C          IF (LT,EQ,LMAX) LT=LMAX=1                           MAS 260
C          IF (JFLAG,NE,0) LDUM=LJET=1                         MAS 270
C          IF (ISURF,EQ,1,OR,N1D,EQ,0) GO TO 30                MAS 280
C          CALCULATE THE MASS FLOW AND THRUST FOR THE 1=D INITIAL=DATA      MAS 290
C          SURFACE                                              MAS 300
C          MAS 310
C          IF (NDIM,EQ,1) GO TO 10                            MAS 320
C          AREA1=(YH(1)-YCB(1))/LC2                          MAS 330
C          AREAT=(YH(LT)-YCB(LT))/LC2                      MAS 340
C          AREAEE=(YH(LDUM)-YCB(LDUM))/LC2                 MAS 350
C          GO TO 20                                         MAS 360
C          10 AREA1=3.141593*(YH(1)**2-YCB(1)**2)/LC2        MAS 370
C          AREAT=3.141593*(YH(LT)**2-YCB(LT)**2)/LC2       MAS 380
C          AREAEE=3.141593*(YH(LDUM)**2-YCB(LDUM)**2)/LC2  MAS 390
C          20 VMI=SQRT(U(1,1,1)**2+V(1,1,1)**2)              MAS 400
C          VMT=SQRT(U(LT,1,1)**2+V(LT,1,1)**2)             MAS 410
C          VME=SQRT(U(LDUM,1,1)**2+V(LDUM,1,1)**2)         MAS 420
C          MASSI=RO(1,1,1)*VMI*AREAI*G                     MAS 430
C          MASST=RO(LT,1,1)*VMT*AREAT*G                   MAS 440
C          MASSE=RO(LDUM,1,1)*VME*AREAEE*G                 MAS 450
C          THRUST=RD(LDUM,1,1)*U(LDUM,1,1)**2*AREAE        MAS 460
C          RETURN                                         MAS 470
C          CALCULATE THE MASS FLOW AND THRUST FOR THE 2=D INITIAL=DATA      MAS 480
C          AND SOLUTION SURFACES                                         MAS 490
C          MAS 500
C          30 MASSI=0,0                                         MAS 510
C          MASST=0,0                                         MAS 520
C          MASSE=0,0                                         MAS 530
C          THRUST=0,0                                         MAS 540
C          DYT=DY*(YH(1)-YCB(1))                           MAS 550
C          DYT=DY*(YH(LT)-YCB(LT))                         MAS 560
C          DYE=DY*(YH(LDUM)-YCB(LDUM))                     MAS 570
C          ND=1
C          IF (ISURF,EQ,1) ND=N3                           MAS 580
C          DO 60 M=1,M1                                     MAS 590
C          RADI=(M-1)*DYI+YCB(1)                         MAS 600
C          RADT=(M-1)*DYT+YCB(LT)                        MAS 610
C          RADE=(M-1)*DYE+YCB(LDUM)                      MAS 620
C          IF (NDIM,EQ,1) GO TO 40                         MAS 630
C          AREA1=DYI/LC2                                    MAS 640
C          AREAT=DYT/LC2                                   MAS 650
C          AREAEE=DYE/LC2                                 MAS 660
C          GO TO 50                                         MAS 670
C          40 AREA1=3.141593*((RADI+DYI)**2-RADI**2)/LC2  MAS 680
C          AREAT=3.141593*((RADT+DYT)**2-RADT**2)/LC2    MAS 690
C          AREAEE=3.141593*((RADE+DYE)**2-RADE**2)/LC2   MAS 700
C          50 ROU1=(RO(1,M,ND)*U(1,M,ND)+RO(1,M+1,ND)*U(1,M+1,ND))*0.5  MAS 710
C          ROUT=(RO(LT,M,ND)*U(LT,M,ND)+RO(LT,M+1,ND)*U(LT,M+1,ND))*0.5  MAS 720
C          ROUE=(RO(LDUM,M,ND)*U(LDUM,M,ND)+RO(LDUM,M+1,ND)*U(LDUM,M+1,ND))*0.5  MAS 730
C          ROU2E=(RO(LDUM,M,ND)*U(LDUM,M,ND)**2+RO(LDUM,M+1,ND)*U(LDUM,M+1,ND))/ND  MAS 740
C          ROU2E=(RO(LDUM,M,ND)*U(LDUM,M,ND)**2+RO(LDUM,M+1,ND)*U(LDUM,M+1,ND))/ND  MAS 750
C          ROU2E=(RO(LDUM,M,ND)*U(LDUM,M,ND)**2+RO(LDUM,M+1,ND)*U(LDUM,M+1,ND))/ND  MAS 760
C          ROU1=(RO(1,M,ND)*U(1,M,ND)+RO(1,M+1,ND)*U(1,M+1,ND))*0.5  MAS 770
C          ROUT=(RO(LT,M,ND)*U(LT,M,ND)+RO(LT,M+1,ND)*U(LT,M+1,ND))*0.5  MAS 780
C          ROUE=(RO(LDUM,M,ND)*U(LDUM,M,ND)+RO(LDUM,M+1,ND)*U(LDUM,M+1,ND))/ND  MAS 790
C          1,5 ROU2E=(RO(LDUM,M,ND)*U(LDUM,M,ND)**2+RO(LDUM,M+1,ND)*U(LDUM,M+1,ND))/ND  MAS 800
C          ROU2E=(RO(LDUM,M,ND)*U(LDUM,M,ND)**2+RO(LDUM,M+1,ND)*U(LDUM,M+1,ND))/ND  MAS 810

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1)*2)*0.5  
MASS1=MASS1+ROU1*AREA1*G  
MASS1=MASS1+ROUT*AREAT*G  
MASS2=MASS2+ROUE*AREA2*G  
THRUST=THRUST+ROU2E*AREA2  
60 CONTINUE  
RETURN  
END
```

MAS	820
MAS	830
MAS	840
MAS	850
MAS	860
MAS	870
MAS	880
MAS	890

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C          SUBROUTINE PLOT(TITLE,T,NP)                               PLT  10
C          ***** THIS SUBROUTINE PLOTS THE VELOCITY VECTORS AND DEPENDENT VARIABLE PLT  20
C          CONTOUR PLOTS                                         PLT  30
C          *****                                                 PLT  40
C          DIMENSION CQ(81,21), CON(9), XCO(4), YCO(4), TITLE(8)      PLT  50
C          COMMON /AV/ JAV,CAV,NBT,SMP,LBS3,CTA,XMU,XLA,RKMU,QVT(81)PLT  60
C          1,21),QPT(81,21)                                         PLT  70
C          COMMON /DNESTD/ UD(4),VD(4),PD(4),ROD(4)                  PLT  80
C          COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RD(81,21,2)    PLT  90
C          COMMON /CNTRL/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAMI,GAPLT 100
C          1M2,L1,L2,L3,M1,M2,DY,DT,N,N1,N3,NASM,IVEL,ICHAR,NID,LJET,JFLAG,PLT 110
C          2IERR,IUI,IUO,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TCPLT 120
C          3,LC,PLOW,ROLON                                         PLT 130
C          COMMON /GEMTRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCT,ANGI,ANGE,XW(81),PLT 140
C          1YN(81),XWI(81),YWI(81),NXNY(81),NWPTS,IINT,IDL,LT,NDIM       PLT 150
C          COMMON /GCB/ NGCB,XICB,RICB,RTCB,XECB,RECBB,RCICB,RCTCB,ANGICBPLT 160
C          1,ANGEGB,XCB(A1),YCB(81),XCB(81),YCB(81),NXNYCB(81),NCBPTS,IINTCBPLT 170
C          2,IDLFCB,LECB                                         PLT 180
C          COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASSI,MASST,THRUST,NPLT 190
C          1STAG                                         PLT 200
C          REAL MN3,NXNY,MASSI,MASST,NXNYCB,MASSE                   PLT 210
C          GENERATE THE VELOCITY VECTOR PLOT                         PLT 220
C          ND=N3                                         PLT 230
C          IF (N,EQ,0) ND=1                                         PLT 240
C          CALL GETQ (4LKJBN,JNM)                                 PLT 250
C          XL=XI                                         PLT 260
C          XR=XE                                         PLT 270
C          YT=YH(1)                                         PLT 280
C          YB=YCB(1)                                         PLT 290
C          DO 10 L=2,LMAX                                     PLT 300
C          YT=AMAX1(YT,YH(L))                                PLT 310
C          YB=AMIN1(YB,YCB(L))                                PLT 320
C          CONTINUE                                         PLT 330
C          VV=0,9*DX                                         PLT 340
C          FIYB=916.0                                         PLT 350
C          XD=(XR-XL)/(YT-YB)                                PLT 360
C          FIR=(1022.0-1022.0/FLOAT(L))-1.0/900.0           PLT 370
C          IF(XD,LE,FIR) GO TO 20                           PLT 380
C          FIXL=0,0                                         PLT 390
C          FIXR=1022.0-1022.0/FLOAT(L)-1.0                 PLT 400
C          FIYT=916.0-FIXR/XD                                PLT 410
C          GO TO 30                                         PLT 420
C          FIXL=511.0-450.0*XD                                PLT 430
C          FIXR=511.0+450.0*XD                                PLT 440
C          FIYT=16.0                                         PLT 450
C          20   XCINV=(FIXR-FIXL)/(XR-XL)                      PLT 460
C          YCINV=(FIYT-FIYB)/(YT-YB)                          PLT 470
C          VMAX=0,0                                         PLT 480
C          DO 40 L=1,LMAX                                     PLT 490
C          DO 40 M=1,MMAX                                     PLT 500
C          VMAX=AMAX1(VMAX,ABS(U(L,M,ND)),ABS(V(L,M,ND)))    PLT 510
C          CONTINUE                                         PLT 520
C          IF (VMAX,LT,1.0E-10) GO TO 60                     PLT 530
C          DROU=VV/VMAX                                     PLT 540
C          CALL ADV (1)                                     PLT 550
C          DO 50 L=1,LMAX                                     PLT 560
C          IX1=FIXL+(FLOAT(L-1)*DX)*XCINV                  PLT 570
C          DY=(YH(L)-YCB(L))/FLOAT(MMAX-1)                  PLT 580
C          DO 50 M=1,MMAX                                     PLT 590
C          IY1=FIYB+(YCB(L)+FLOAT(M-1)*DY-YB)*YCINV        PLT 600
C          IX2=FIXL+(FLOAT(L-1)*DX+U(L,M,ND)*DROU)*XCINV    PLT 610
C          IY2=FIYB+(YCB(L)+FLOAT(M-1)*DY-YB+V(L,M,ND)*DROU)*YCINV    PLT 620
C          CALL DRV (IX1,IY1,IX2,IY2)                        PLT 630
C          CALL PLT (IX1,IY1,16)                            PLT 640
C          50   CONTINUE                                         PLT 650
C          CALL LINCNT (59)                                PLT 660
C          WRITE (7,410)                                     PLT 670
C          WRITE (7,350)JNM,TITLE,NP,T                      PLT 680
C          GENERATE THE CONTOUR PLOTS                      PLT 690
C          60   I=0                                         PLT 700
C          70   I=I+1                                         PLT 710
C          GO TO (80,100,120,140,340), I                  PLT 720
C          DO 90 L=1,LMAX                                     PLT 730
C          DO 90 M=1,MMAX                                     PLT 740
C          CQ(L,M)=R0(L,M,ND)*G                           PLT 750

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90  CONTINUE
GO TO 160
100 DO 110 L=1,LMAX
DO 110 M=1,MMAX
CQ(L,M)=P(L,M,ND)/PC
110 CONTINUE
GO TO 160
120 DO 130 L=1,LMAX
DO 130 M=1,MMAX
CQ(L,M)=P(L,M,ND)/RO(L,M,ND)/RGAS/G=TC
130 CONTINUE
GO TO 160
140 DO 150 L=1,LMAX
DO 150 M=1,MMAX
CQ(L,M)=SQRT((U(L,M,ND)*#2+V(L,M,ND)*#2)/(GAMMA*P(L,M,ND)/RO(L,M,NPLT
1D)))
150 CONTINUE
QMN=1.0E06
QMX=QMN
DO 170 L=1,LMAX
DO 170 M=1,MMAX
QMN=AMIN1(CQ(L,M),QMN)
QMX=AMAX1(CQ(L,M),QMX)
170 CONTINUE
XX=QMX-QMN
DQ=0.1*XX
DO 180 K=1,9
CON(K)=QMN+(FLOAT(K))*DQ
180 CONTINUE
K=9
CALL ADV ()
CALL LINCNT (59)
GO TO (190,200,210,220), I
190 WRITE (7,360)
GO TO 230
200 WRITE (7,370)
GO TO 230
210 WRITE (7,380)
GO TO 230
220 WRITE (7,390)
230 WRITE (7,400) QMN,QMX,CON(),CON(K),DQ
WRITE (7,350) JNM,TITLE,NP,T
DO 320 L=2,LMAX
DY=(YN(L-1)-YCB(L-1))/FLOAT(MMAX=1)
DY1=(YN(L)-YCB(L))/FLOAT(MMAX=1)
DO 320 M=2,MMAX
NN=0
DO 320 KK=1,K
K1=K2=K3=K4=0
IF (CQ(L=1,M=1),LE,CON(KK)) K1=1
IF (CQ(L,M=1),LE,CON(KK)) K2=1
IF (CQ(L=1,M),LE,CON(KK)) K3=1
IF (CQ(L,M),LE,CON(KK)) K4=1
IF (K1+K2+K3+K4,NE,0) GO TO 320
IF (K1+K2+K3+K4,EQ,0) GO TO 320
IF (NN,NE,0) GO TO 240
NN=
XCO(1)=XI+FLOAT(L=2)*DX
XCO(2)=XCO(1)+DX
XCO(3)=XCO(1)
XCO(4)=XCO(2)
YCO(1)=YCB(L-1)+FLOAT(M=2)*DY
YCO(2)=YCB(L)+FLOAT(M=2)*DY1
YCO(3)=YCB(L-1)+FLOAT(M=1)*DY
YCO(4)=YCB(L)+FLOAT(M=1)*DY1
240 LL=0
IF (K1+K3,NE,1) GO TO 250
IC1=1 $ IC2=3 $ LP1=L-1 $ MP1=M=1 $ LP2=L-1 $ MP2=M
ASSIGN 250 TO KRI
GO TO 280
250 IF (K1+K2,NE,1) GO TO 260
IC1=1 $ IC2=2 $ LP1=L-1 $ MP1=M=1 $ LP2=L $ MP2=M
ASSIGN 260 TO KRI
GO TO 280
260 IF (K2+K4,NE,1) GO TO 270
IC1=2 $ IC2=4 $ LP1=L-1 $ MP1=M=1 $ LP2=L $ MP2=M
ASSIGN 270 TO KRI
GO TO 280
270 IF (K3+K4,NE,1) GO TO 320
IC1=3 $ IC2=4 $ LP1=L-1 $ MP1=M $ LP2=L $ MP2=M
ASSIGN 320 TO KRI

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280  LL=LL+1
      XX=(CON(KK)-CQ(LP1,MP1))/(CQ(LP2,MP2)-CQ(LP1,MP1))
      IF (LL,EG,2) GO TO 290
      IX1=FIXL+(XCO(IC1)+XX*(XCO(IC2)-XCO(IC1))-XL)*XCONV
      IY1=FIYB+(YCO(IC1)+XX*(YCO(IC2)-YCO(IC1))-YB)*YCONV
      GO TO KR1,(250,260,270,320)
290  IX2=FIXL+(XCO(IC1)+XX*(XCO(IC2)-XCO(IC1))-XL)*XCONV
      IY2=FIYB+(YCO(IC1)+XX*(YCO(IC2)-YCO(IC1))-YB)*YCONV
      CALL DRV (IX1,IY1,IX2,IY2)
      IF (KK,NE,1) GO TO 300
      CALL PLT (IX1,IY1,35)
300  IF (KK,NE,K) GO TO 310
      CALL PLT (IX1,IY1,24)
310  LL=0
      IF (LP2,NE,L) GO TO 320
      IF (MP2,NE,M-1) GO TO 320
      GO TO 260
320  CONTINUE
C
C   DRAW THE GEOMETRY CONTOURS
C
      DO 330 L=2,LMAX
      IX1=FIXL+(FLOAT(L=2)*DX)*XCONV
      IX2=FIXL+(FLOAT(L=1)*DX)*XCONV
      IY1=FIYB+(YCB(L=1)-YB)*YCONV
      IY2=FIYB+(YCB(L)-YB)*YCONV
      IY3=FIYB+(YM(L=1)-YB)*YCONV
      IY4=FIYB+(YM(L)-YB)*YCONV
      CALL DRV (IX1,IY1,IX2,IY2)
      CALL DRV (IX1,IY3,IX2,IY4)
330  CONTINUE
      GO TO 70
340  CONTINUE
      DY=1.0/FLOAT(MMAX+1)
      CALL ADV (1)
      RETURN
C
350  FORMAT (1H ,A10,4X,8A10,2X,2HN=,I4,2X,2HT=,1PE10,4,4H SEC)    PLT 2030
360  FORMAT (1H ,7HDENSITY)                                              PLT 2040
370  FORMAT (1H ,8HPRESSURE)                                             PLT 2050
380  FORMAT (1H ,11HTEMPERATURE)                                           PLT 2060
390  FORMAT (1H ,11HMACH NUMBER)                                         PLT 2070
400  FORMAT (1H ,10HLOW VALUE=,1PE11,4,2X,11HHIGH VALUE=,E11,4,2X,12HLOWPLT 2080
     1W CONTOUR=,E11,4,2X,13HHIGH CONTOUR=,E11,4,2X,14HDELTA CONTOUR=,E1PLT 2090
     21,4)
410  FORMAT (1H ,16HVELOCITY VECTORS)                                     PLT 2100
      END                                                               PLT 2110
                                                                     PLT 2120

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SUBROUTINE SHOCK(IPASS) SHO 10
C ***** THIS SUBROUTINE CALCULATES THE LOCAL ARTIFICIAL VISCOSITY TERMS SHO 20
C FOR SHOCK COMPUTATIONS SHO 30
C ***** SHO 40
C COMMON /AV/ IAV,CAV,NST,SMP,LSS,CTA,XMU,XLA,RKMU,QUT(B1,21),QVT(B1,21) SHO 50
C /ONESID/ UD(4),VD(4),PD(4),ROD(4) SHO 60
C /SOLUTN/ U(B1,21,2),V(B1,21,2),P(B1,21,2),RO(B1,21,2) SHO 70
C /CNTRL/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAM1,GASHO 80
C 1M2,L1,L2,L3,M1,M2,DX,DY,DT,N,N1,N3,NABM,IVEL,ICHAR,NID,LJET,JFLAG,SHO 90
C 2IERR,IUI,IUD,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TC SHO 100
C 3,LC,PLOW,RODN SHO 110
C /GEMTRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCT,ANG1,ANGE,XW(B1),SHO 120
C YW(B1),XWI(B1),YWI(B1),NXNY(B1),NWPTS,IINT,IDL,LT,NDIM SHO 130
C /GCB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,REC,B,RCICB,RCTCB,ANGICB,SHO 140
C 1,ANGECB,XCB(B1),YCB(B1),XCBI(B1),YCB(B1),NXNYCB(B1),NCBPTS,IINTCB,SHO 150
C 2,IDLFCB,LECB SHO 160
C /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASST,MASST,THRUST,NSH SHO 170
C 1STAG SHO 180
C REAL MN3,NXNY,MASST,MASST,NXNYCB,MASSE SHO 190
C GO TO (10,16A), IPASS SHO 200
C CALCULATE LOCAL ARTIFICIAL VISCOSITY FOR SHOCK COMPUTATIONS SHO 210
C 10 IF (N,NE,1) GO TO 30 SHO 220
C NC=0 SHO 230
C RG=RGAS+G SHO 240
C CTA=1,0=CTA SHO 250
C DO 20 L=1,LMAX SHO 260
C DO 20 M=1,MMAX SHO 270
C QUT(L,M)=0,0 SHO 280
C QVT(L,M)=0,0 SHO 290
C QPT(L,M)=0,0 SHO 300
C 20 CONTINUE SHO 310
C 30 RDUH=CAV*DT*DX*DY*2,0 SHO 320
C NC=NC+1 SHO 330
C NLIN=0 SHO 340
C IF (NC,NE,NPRINT) GO TO 40 SHO 350
C PRINT 200 SHO 360
C PRINT 190, N,PC SHO 370
C 40 DO 150 L=LSS,L1 SHO 380
C DO 150 M=1,MMAX SHO 390
C LMD2=LD*(M-1)+LMD1 SHO 400
C LMM2=LD*(M2)+LMD1 SHO 410
C LMPD2=LD*M+LMD1 SHO 420
C LMN1=L+LMD2 SHO 430
C LP=L+1+LMD2 SHO 440
C LH=L-1+LMD2 SHO 450
C MP=L+LMPD2 SHO 460
C MH=L+LMM2 SHO 470
C LPMP=L+1+LMPD2 SHO 480
C LPMH=L+1+LMM2 SHO 490
C LMNP=L-1+LMPD2 SHO 500
C LMHM=L-1+LMM2 SHO 510
C CALL MAP (1,L,M,AL,BE,DE,LD1,AL1,BE1,DE1) SHO 520
C 50 CHECK TO SEE IF THE DIVERGENCE OF THE VELOCITY IS NEGATIVE SHO 530
C UX=0.5*(U(LP)-U(LH))*DXR SHO 540
C IF (M,EQ,1) GO TO 50 SHO 550
C IF (M,EQ,MMAX) GO TO 60 SHO 560
C UY=0.5*(U(MP)-U(MH))*DYR SHO 570
C VY=0.5*(V(MP)-V(MH))*DYR SHO 580
C GO TO 70 SHO 590
C 50 UY=(U(LMN1)-U(MH))*DYR SHO 600
C VY=(V(LMN1)-V(MH))*DYR SHO 610
C GO TO 70 SHO 620
C 60 UY=(U(LMN1)-U(MM))*DYR SHO 630
C VY=(V(LMN1)-V(MM))*DYR SHO 640
C 70 DIV=UX+AL*UY+BE*VY SHO 650
C IF (DIV,LT,0,0) GO TO 80 SHO 660
C QUT(L,M)=0,0 SHO 670
C QVT(L,M)=0,0 SHO 680
C QPT(L,M)=0,0 SHO 690
C GO TO 150 SHO 700

```

```

80    QQUT=QUT(L,M)
     QQVT=QVT(L,M)
     QOPT=OPT(L,M)
     UX1=(U(LMN1)-U(LM))/DXR
     UX2=(U(LP)-U(LMN1))/DXR
     VX1=(V(LMN1)-V(LM))/DXR
     VX2=(V(LP)-V(LMN1))/DXR
     TM=P(LM)/(RO(LM)*RG)
     TP=P(LMN1)/(RO(LMN1)*RG)
     TP=P(LP)/(RO(LP)*RG)
     TX1=(T-TM)*DXR
     TX2=(TP-T)*DXR
     LDUM=L+1
     CALL MAP (1,LDUM,M,ALM,BEM,DE,LD1,AL1,BE1,DE1)
     LDUM=L+1
     CALL MAP (1,LDUM,M,ALP,BEP,DE,LD1,AL1,BE1,DE1)
     BE1=0,5*(BEM+BE)
     BE2=0,5*(BEP+BE)
     AL1=0,5*(ALM+AL)
     AL2=0,5*(ALP+AL)
     IF (M,EQ,1) GO TO 90
     IF (M,EQ,MMAX) GO TO 100
C
C      CALCULATE THE INTERIOR POINT QUANTITIES
C
     UY1=0,25*(U(MP)+U(LMMP)-U(MH)-U(LMMH))/DYL
     UY2=0,25*(U(MP)+U(LPMP)-U(MH)-U(LPMH))/DYL
     VY1=0,25*(V(MP)+V(LMMP)-V(MH)-V(LMMH))/DYL
     VY2=0,25*(V(MP)+V(LPMP)-V(MH)-V(LPMH))/DYL
     UX3=0,25*(U(LP)+U(LPMH)-U(LM)-U(LMMH))/DXR
     UX4=0,25*(U(LP)+U(LPMP)-U(LM)-U(LMMP))/DXR
     VX3=0,25*(V(LP)+V(LPMP)-V(LM)-V(LMMH))/DXR
     VX4=0,25*(V(LP)+V(LPMH)-V(LM)-V(LMMH))/DXR
     VY3=(V(LMN1)-V(MH))/DYL
     VY4=(V(MP)-V(LMN1))/DYL
     UY3=(U(LMN1)-U(MH))/DYL
     UY4=(U(MP)-U(LMN1))/DYL
     THY=P(MH)/(RO(MH)*RG)
     TPY=P(MP)/(RO(MP)*RG)
     THM=P(LMMH)/(RO(LMMH)*RG)
     TMP=P(LMMP)/(RO(LMMP)*RG)
     TPM=P(LPMM)/(RO(LPMM)*RG)
     TPP=P(LPMP)/(RO(LPMP)*RG)
     TY1=0,25*(TPY+TMP-THY-THM)/DYL
     TY2=0,25*(TPP+TPY+TPM+THY)/DYL
     TX3=0,25*(TP+TPN-TH+THM)/DXR
     TX4=0,25*(TPP+TP+TMP+TM)/DXR
     TY3=(T+THY)/DYL
     TY4=(TPY-T)/DYL
     MDUMHM=1
     CALL MAP (1,L,MDUM,ALHY,BEMY,DE,LD1,AL1,BE1,DE1)
     MDUMHM+1
     CALL MAP (1,L,MDUM,ALPY,BEPY,DE,LD1,AL1,BE1,DE1)
     BE3=0,5*(BEMY+BE)
     BE4=0,5*(BEPY+BE)
     AL3=0,5*(ALHY+AL)
     AL4=0,5*(ALPY+AL)
     GO TO 110
C
C      CALCULATE THE CENTERLINE POINT QUANTITIES
C
90    UY1=0,5*(U(MP)+U(LMMP)-U(LMN1))/DXR
     VY1=0,5*(V(MP)+V(LMMP)-V(LMN1))/DXR
     UX2=0,5*(U(LPMP)+U(MP)-U(LP)-U(LMN1))/DYL
     VY2=0,5*(V(LPMP)+V(MP)-V(LP)-V(LMN1))/DYL
     UX3=VX3=UX4=VX4=0,0
     THE=ATAN(-NXNYCB(L))
     THE=ATAN(V(MP)/U(MP))
     VMAG=SQRT(U(MP)*U(MP)+V(MP)*V(MP))
     RTHE=2,0*THEW-THE
     UR=VMAG*COS(RTHE)
     VR=VMAG*SIN(RTHE)
     UY3=(U(LMN1)-UR)/DYL
     VY3=(V(LMN1)-VR)/DYL
     UY4=(U(MP)-U(LMN1))/DYL
     VY4=(V(MP)-V(LMN1))/DYL
     TPY=P(MP)/(RO(MP)*RG)
     TMP=P(LMMP)/(RO(LMMP)*RG)
     TPP=P(LPMP)/(RO(LPMP)*RG)
     TY1=0,0
     TY2=0,0
     TX4=0,25*(TPP+TP+TMP+TM)/DXR

```

```

TX3=TX4
TY4=(TPY-T)*DYR
TY3=TY4
BE3=BE
AL3=AL
MDUM=MH1
CALL MAP (1,L,MDUM,AL4,BE4,DE,LD1,AL1,BE1,DE1)
GO TO 110
C
C   CALCULATE THE WALL POINT QUANTITIES
C
100 UY1=0,5*(U(LMN1)+U(LM)-U(MH)-U(LMMH))+DYR
    VY1=0,5*(V(LMN1)+V(LM)-V(MH)-V(LMMH))+DYR
    UY2=0,5*(U(LP)+U(LMN1)-U(LPMH)-U(MH))+DYR
    VY2=0,5*(V(LP)+V(LMN1)-V(LPMH)-V(MH))+DYR
    UX3=VX3=UX4=VX4=0,0
    UY3=(U(LMN1)-U(MH))+DYR
    VY3=(V(LMN1)-V(MH))+DYR
    THEW=ATAN(-NXNY(L))
    THE=ATAN(V(MM)/U(MM))
    VMAG=SQRT(U(MM)*U(MM)+V(MM)*V(MM))
    RTHE=2,0*THEW-THE
    UR=VMAG*COS(RTHE)
    VR=VMAG*SIN(RTHE)
    UY4=(UR-U(LMN1))+DYR
    VY4=(VR-V(LMN1))+DYR
    TPM=P(LPMH)/(RO(LPMH)*RG)
    TMY=P(MH)/(RO(MH)*RG)
    TMM=P(LMMH)/(RO(LMMH)*RG)
    TY1=0,0
    TY2=0,0
    TX3=0,25*(TP+TPH+TM+TMM)+DXR
    TX4=TX3
    TY3=(T+THY)*DYR
    TY4=TY3
    MDUM=MH1
    CALL MAP (1,L,MDUM,AL3,BE3,DE,LD1,AL1,BE1,DE1)
    BE4=BE
    AL4=AL
C
S10 UXY1=UX1+AL1*UY1
    UXY2=UX2+AL2*UY2
    UXY3=UX3+AL3*UY3
    UXY4=UX4+AL4*UY4
    UXY12=0,5*(UX1+UX2+AL3*UY3+AL4*UY4)
    VXY1=VX1+AL1*VY1
    VXY2=VX2+AL2*VY2
    VXY3=VX3+AL3*VY3
    VXY4=VX4+AL4*VY4
    VXY12=0,5*(VX1+VX2+AL3*VY3+AL4*VY4)
    BUY1=BE1*UY1
    BUY2=BE2*UY2
    BUY3=BE3*UY3
    BUY4=BE4*UY4
    BUY34=0,5*(BUY3+BUY4)
    BVY1=BE1*VY1
    BVY2=BE2*VY2
    BVY3=BE3*VY3
    BVY4=BE4*VY4
    BVY34=0,5*(BVY3+BVY4)
    TXY1=TX1+AL1*TY1
    TXY2=TX2+AL2*TY2
    TXY3=TX3+AL3*TY3
    TXY4=TX4+AL4*TY4
C
C   CALCULATE THE ARTIFICIAL VISCOSITY COEFFICIENTS
C
DIV=UXY12+BVY34
VID=VXY12+BUY34
RLA=XLAMRDUM*ABS(DIV)/BE
RMU=XMU*RDUM*ABS(VID)/BE
RK=RMU*GAM1*RG/RKMU
RLP2=RLA+2,0*RMU
RLA2=2,0*RLA
RMU2=2,0*RMU
RLPH=RLA+RMU
UVTA=0,0
VVTA=0,0
PVTA=0,0
PCTA=0,0
IF (NDIM,EQ,0) GO TO 130

```

```

C
C      CALCULATE THE AXISYMMETRIC TERMS
C
IF (M,EQ,1,AND,YCB(L),EQ,0,0) GO TO 120
Y=FLOAT(M-1)*DY/BE+YCB(L)
VB=V(LMN1)
UVTA=(RLP2M*(BVY34+VB/Y)/Y
VVTB=RLP2M*(BVY34+VB/Y)/Y
PVTB=RK*0,5*(BE4+TY4+BE3+TY3)/Y
DUVTA=RLP2M*BE*(VXY4-VXY3)*DYL+RMU*BE*(BUY4-BUY3)*DYL
DVVTB=RLP2M*0,5*BE*(BVY4-BVY3)*DYL
DPVTB=(RLP2M+RLA2)*BVY34+BVY34+RLA2*BVY34+UXY12
DPCTA=RK*BE*(BE4+TY4+BE3+TY3)*DYL
IF (ABS(UVTA),GT,ABS(DUVTA)) UVTA=DUVTA
IF (ABS(VVTB),GT,ABS(DVVTB)) VVTB=DVVTB
IF (ABS(PVTB),GT,ABS(DPVTB)) PVTB=DPVTB
IF (ABS(PCTA),GT,ABS(DPCTA)) PCTA=DPCTA
GO TO 130
120 UVTA=RLP2M*BE*(VXY4-VXY3)*DYL+RMU*BE*(BUY4-BUY3)*DYL
VVTB=RLP2M*0,5*BE*(BVY4-BVY3)*DYL
PVTB=(RLP2M+RLA2)*BVY34+BVY34+RLA2*BVY34+UXY12
PCTA=RK*BE*(BE4+TY4+BE3+TY3)*DYL
C
C      CALCULATE THE ARTIFICIAL VISCOSITY TERMS
C
130 QUT(L,M)=(RLP2M*(UXY2+UXY1)+RLA*(BVY2+BVY1))*DXR+AL*(RLP2M*(UXY4+U
SHO 2720
1XY3)+RLA*(BVY4-BVY3))*DYL+RMU*BE*(VXY4+BUY4-VXY3-BUY3)*DYL+UVTA SHO 2730
QVT(L,M)=RMU*(VXY2+BUY2-VXY1+BUY1)*DXR+RMU*AL*(VXY4+BUY4-VXY3-BUY3)
SHO 2740
1)*DYL+BE*(RLA*(UXY4-UXY3)+RLP2M*(BVY4-BVY3))*DYL+VVTA SHO 2750
OPT(L,M)=RO(LMN1)*(GAMMA=1,0)*(RLP2M*(UXY12+UXY12+BVY34+BVY34)+RMU)
SHO 2760
1*(VXY12+UXY12+BUY34+BUY34)+RLA2*UXY12+BVY34+RMU2*BUY34+VXY12+RK*((SHO 2770
2TXY2-TXY1)*DXR+AL*(TXY4-TXY3)*DYL+BE*(BE4+TY4+BE3+TY3)*DYL)+PVTA+PSH
SHO 2780
3CTA) SHO 2790
QUT(L,M)=CTA*QUT(L,M)+CTA1*QOUT SHO 2800
QVT(L,M)=CTA*QVT(L,M)+CTA1*QVVT SHO 2810
OPT(L,M)=CTA*OPT(L,M)+CTA1*QOPT SHO 2820
C
C      PRINT THE ARTIFICIAL VISCOSITY TERMS
C
IF (NC,NE,NPRINT) GO TO 150
NLINE=NLINE+1
IF (NLINE,LT,55) GO TO 140
PRINT 200
PRINT 190, N,PC
NLINE=1
140 OPT(L,M)=OPT(L,M)/PC
PRINT 180, L,M,QUT(L,M),QVT(L,M),OPT(L,M)
OPT(L,M)=OPT(L,M)*PC
150 CONTINUE
IF (NC,EO,NPRINT) NC=0
RETURN
C
C      SMOOTH THE FLOW VARIABLES IF REQUESTED
C
160 IF (SMP,LT,0,0,OR,SMP,GE,1,0) RETURN
SMP4=25*(1,0=SMP)
DO 170 L=2,L1
U(L,MMAX,N3)=SMP4*(U(L-1,MMAX,N3)+U(L+1,MMAX,N3)+2,0+U(L,M1,N3))+SSH
SHO 3040
1MP*U(L,MMAX,N3) SHO 3050
V(L,MMAX,N3)=U(L,MMAX,N3)+NXNY(L)
SHO 3060
P(L,MMAX,N3)=SMP4*(P(L-1,MMAX,N3)+P(L+1,MMAX,N3)+2,0+P(L,M1,N3))+SSH
SHO 3070
1MP*P(L,MMAX,N3) SHO 3080
RO(L,MMAX,N3)=SMP4*(RO(L-1,MMAX,N3)+RO(L+1,MMAX,N3)+2,0+RO(L,M1,N3))
SHO 3090
1)+8MP*RO(L,MMAX,N3) SHO 3100
U(L,1,N3)=SMP4*(U(L-1,1,N3)+U(L+1,1,N3)+2,0+U(L,2,N3))+8MP*U(L,1,N3)
SHO 3110
13) SHO 3120
V(L,1,N3)=U(L,1,N3)+NXNYCB(L)
SHO 3130
P(L,1,N3)=SMP4*(P(L-1,1,N3)+P(L+1,1,N3)+2,0+P(L,2,N3))+8MP*P(L,1,N3)
SHO 3140
13) SHO 3150
RO(L,1,N3)=SMP4*(RO(L-1,1,N3)+RO(L+1,1,N3)+2,0+RO(L,2,N3))+8MP*RO(L,1,N3)
SHO 3160
1L,1,N3) SHO 3170
DO 170 M=2,M1
LMD2=L*(M-1)+LMD3
LMD2=L*(M-2)+LMD3
LMD2=L*M+LMD3
LHN3=L+LMD2
LP=L+1+LMD2
LM=L-1+LMD2
MP=L+LMD2
MM=L+LMD2
U(LHN3)=SMP4*(U(LM)+U(LP)+U(MM)+U(MP))+8MP*U(LHN3)
SHO 3260
V(LHN3)=SMP4*(V(LM)+V(LP)+V(MM)+V(MP))+8MP*V(LHN3)
SHO 3280

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P(LMN3)=8MP4*(P(LM)+P(LP)+P(MM)+P(MP))+8MP*P(LMN3)      SHO 3290
R0(LMN3)=8MP4*(R0(LM)+R0(LP)+R0(MM)+R0(MP))+8MP*R0(LMN3)  SHO 3300
170  CONTINUE                                              SHO 3310
      RETURN                                              SHO 3320
C
180  FORMAT (1H ,5X,2I5,3F14.4)                                SHO 3330
190  FORMAT (1H ,63HLOCAL ARTIFICIAL VISCOSITY PARAMETERS FOR SHOCK CALC SHO 3350
      IULATION8, N=I4,5H (PC=F5.1,IH),//,18X,IHL,4X,1MM,10X,3HQUT,11X,3H SHO 3360
      20VT,11X,3HOPT,/)                                     SHO 3370
200  FORMAT (1H)                                              SHO 3380
      END                                                 SHO 3390

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SUBROUTINE INTER                                INT   10
C                                               INT   20
C                                               INT   30
C                                               INT   40
C                                               INT   50
C                                               INT   60
C                                               INT   70
C                                               INT   80
C                                               INT   90
C                                               INT  100
C                                               INT  110
C                                               INT  120
C                                               INT  130
C                                               INT  140
C                                               INT  150
C                                               INT  160
C                                               INT  170
C                                               INT  180
C                                               INT  190
C                                               INT  200
C                                               INT  210
C                                               INT  220
C                                               INT  230
C                                               INT  240
C                                               INT  250
C                                               INT  260
C                                               INT  270
C                                               INT  280
C                                               INT  290
C                                               INT  300
C                                               INT  310
C                                               INT  320
C                                               INT  330
C                                               INT  340
C                                               INT  350
C                                               INT  360
C                                               INT  370
C                                               INT  380
C                                               INT  390
C                                               INT  400
C                                               INT  410
C                                               INT  420
C                                               INT  430
C                                               INT  440
C                                               INT  450
C                                               INT  460
C                                               INT  470
C                                               INT  480
C                                               INT  490
C                                               INT  500
C                                               INT  510
C                                               INT  520
C                                               INT  530
C                                               INT  540
C                                               INT  550
C                                               INT  560
C                                               INT  570
C                                               INT  580
C                                               INT  590
C                                               INT  600
C                                               INT  610
C                                               INT  620
C                                               INT  630
C                                               INT  640
C                                               INT  650
C                                               INT  660
C                                               INT  670
C                                               INT  680
C                                               INT  690
C                                               INT  700
C                                               INT  710
C                                               INT  720
C                                               INT  730
C                                               INT  740
C                                               INT  750
C                                               INT  760
C                                               INT  770
C                                               INT  780
C                                               INT  790
C                                               INT  800
C                                               INT  810
C                                               INT  820

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***** THIS SUBROUTINE CALCULATES THE INTERIOR MESH POINTS *****

***** COMPUTE THE TENTATIVE SOLUTION AT T+DT *****

***** COMPUTE THE FINAL SOLUTION AT T+DT *****

```

40 MDUM=1
IF (NGCB,NE,0) MDUM=2
DO 70 L=2,L1
DO 70 M=MDUM,M1
CALL MAP (1,L,M,AL,BE,DE,LD1,AL1,BE1,DE1)
LMD2=LMD1
LMN1=L+LMD2+LMD1
LMN3=L+LMD2+LMD3
LMN3=L+LD+M+LMD3
UB=U(LMN3)
VB=V(LMN3)
PB=P(LMN3)
ROB=RO(LMN3)
ASB=GAMMA*PB/RDB
IF (M,NE,1) GO TO 50
DUDX=(U(L1MN3)-UB)*DXR
DPDX=(P(L1MN3)-PB)*DXR
DRODX=(RO(L1MN3)-ROB)*DXR
DVDY=(4.0*V(L,2,N3)-V(L,3,N3))*0.5*DVR
V(LMN3)=0.0
C
URHS=-UB*DUDX-DPDX/ROB
RORHS=-UB*DRODX-ROB*DUDX-(1+NDIM)*ROB*BE*DVDY
PRHS=-UB*DPDX+ASB*(RORHS+UB*DRODX)
GO TO 60
50 IF (NDIM,EQ,1) ATERM=ROB*VB/((M=1)*DY/BE+YCB(L))
UVB=UB*AL+VB*BE+DE
DUDX=(U(L1MN3)-UB)*DXR
DVDX=(V(L1MN3)-VB)*DXR
DPDX=(P(L1MN3)-PB)*DXR
DRODX=(RO(L1MN3)-ROB)*DXR
DUDY=(U(LMN3)-UB)*DVR
DVDY=(V(LMN3)-VB)*DVR
DPDY=(P(LMN3)-PB)*DVR
DRODY=(RO(LMN3)-ROB)*DVR
C
URHS=-UB*DUDX-UVB*DUDY-(DPDX+AL*DPDY)/ROB
VRHS=-UB*DUDX-UVB*DUDY-BE*DPDY/ROB
RORHS=-UB*DRODX-UVB*DRODY=ROB*(DUDX+AL*DUDY+BE*DVDY)=ATERM
PRHS=-UB*DPDX-UVB*DPDY+ASB*(RORHS+UB*DRODX+UVB*DRODY)
V(LMN3)=(V(LMN1)+V(LMN3)+VRHS*DT)*0.5
60 U(LMN3)=(U(LMN1)+U(LMN3)+URHS*DT)*0.5
P(LMN3)=(P(LMN1)+P(LMN3)+PRHS*DT)*0.5
RO(LMN3)=(RO(LMN1)+RO(LMN3)+RORHS*DT)*0.5
IF (P(LMN3),LE,0,0) P(LMN3)=PLDN*PC
IF (RO(LMN3),LE,0,0) RO(LMN3)=ROLDN/G
IF (IAV,EQ,0) GO TO 70
C
C      ADD THE ARTIFICIAL VISCOSITY FOR SHOCK CALCULATIONS
C
U(LMN3)=U(LMN3)+QUT(L,M)
V(LMN3)=V(LMN3)+QVT(L,M)
IF (M,EQ,1) V(LMN3)=0.0
P(LMN3)=P(LMN3)+OPT(L,M)
70 CONTINUE
RETURN
END

```

```

C SUBROUTINE WALL                               HAL 10
C *****                                              HAL 20
C *****                                              HAL 30
C THIS SUBROUTINE CALCULATES THE BOUNDARY MESH POINTS AT THE NOZZLE HAL 50
C WALL, EXHAUST JET BOUNDARY, AND CENTERBODY          HAL 60
C *****                                              HAL 70
C *****                                              HAL 80
C *****                                              HAL 90
C COMMON /AV/ TAV,CAV,NST,SMP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81,21) HAL 100
1,21),QPT(81,21)
COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)          HAL 110
COMMON /SOLUTN/ U(R1,21,2),V(R1,21,2),P(R1,21,2),RD(R1,21,2)          HAL 120
COMMON /CNTRL/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAMI,GAHAL 130
1M2,L1,L2,L3,M1,M2,DY,DT,N,N1,N3,NASH,IVEL,ICHAR,NID,LJET,JFLAG,WAL 140
2IERR,IUI,IUO,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTAR5,NPLOT,G,PC,TCHAL 150
3,LC,PLOW,ROLOW
COMMON /GEMTRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCT,ANGI,ANGE,XW(81),HAL 160
1YW(81),XHI(81),YHI(81),NXNY(R1),NWPTS,IINT,IDI,LT,NDIM          HAL 170
COMMON /GCB/ NGCB,XICB,HICB,XTCB,RTCB,XECB,REC,B,RCICB,RCTCB,ANGICBHAL 180
1,ANGECB,XCB(R1),YCB(81),XCB(81),YCB(81),NXNYCB(81),NCBPTS,IINTCBHAL 190
2,IDI,FCB,LCB
COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASSI,MA8ST,THRUST,NHAL 200
1STAG
REAL MN3,NXNY,MASSI,MA8ST,NXNYCB,MASSE          HAL 210
HAL 220
C IF (N,EQ,1) DELY=0,005                         HAL 230
XHID=0,0                                         HAL 240
IF (IB,EQ,1) GO TO 10                           HAL 250
Y1=0,0 S Y3=0,0 S MDUM1=1 S MDUM1=2 S SIGN=1,0          HAL 260
GO TO 20
10 Y1=1,0 S Y3=1,0 S MDUM=MMAX S MDUM1=M1 S SIGN=1,0          HAL 270
20 ATERM2=0,0                                         HAL 280
ATERM3=0,0                                         HAL 290
LDUM=LMAX                                         HAL 300
IF (ICHAR,EQ,2) LDUM=L1                         HAL 310
LMDM=LD*(MDUM-1)                                HAL 320
LMDM1=LD*(MDUM1-1)                                HAL 330
DYS=SIGN*DYR                                     HAL 340
DO 350 L=2,LDUM                                  HAL 350
LMN1=L+LMDM+LMD1                                HAL 360
LMN3=L+LMDM+LMD3                                HAL 370
LM1N1=L+LMDM1+LMD1                                HAL 380
LM1N1=L-1+LMDM+LMD1                                HAL 390
LM1N3=L+1+LMDM+LMD3                                HAL 400
LM1N1=L-1+LMDM1+LMD1                                HAL 410
IF (JFLAG,EQ,0) GO TO 50                         HAL 420
IF (IB,EQ,2) GO TO 50                           HAL 430
C XHID=XHJ(L)                                     HAL 440
IF (ICHAR,EQ,1) GO TO 30                         HAL 450
C USE THE DUMMY ARRAYS TO MANIPULATE THE ONE-SIDED SOLUTIONS          HAL 460
C
30 IF (L,NE,LJET=2) GO TO 30                      HAL 470
U(L1MN3)=UD(3)                                    HAL 480
V(L1MN3)=VD(3)                                    HAL 490
P(L1MN3)=PD(3)                                    HAL 500
RO(L1MN3)=ROD(3)                                 HAL 510
GO TO 50
30 IF (L,NE,LJET=1) GO TO 40                      HAL 520
IF (ICHAR,EQ,1) UOLD=U(LMN1)                      HAL 530
U(LMN1)=UD(1)                                    HAL 540
V(LMN1)=VD(1)                                    HAL 550
P(LMN1)=PD(1)                                    HAL 560
RO(LMN1)=ROD(1)                                 HAL 570
GO TO 50
40 IF (L,NE,LJET) GO TO 50                        HAL 580
U(L1MN1)=UD(2)                                    HAL 590
V(L1MN1)=VD(2)                                    HAL 600
P(L1MN1)=PD(2)                                    HAL 610
RO(L1MN1)=ROD(2)                                 HAL 620
C
50 U1=U(LMN1)                                     HAL 630
V1=V(LMN1)                                     HAL 640
P1=P(LMN1)                                     HAL 650
RO1=RO(LMN1)                                 HAL 660
U2=U1                                         HAL 670
V2=V1                                         HAL 680
A1=SQRT(GAMMA*P1/RO1)                         HAL 690
A2=A1                                         HAL 700
IF (ICHAR,EQ,2) GO TO 60                         HAL 710
HAL 720
HAL 730
HAL 740
HAL 750
HAL 760
HAL 770
HAL 780
HAL 790
HAL 800
HAL 810
HAL 820

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U3=U1          HAL 830
V3=V1          HAL 840
P3=P1          HAL 850
R03=R01        HAL 860
A3=A1          HAL 870
GO TO 70       HAL 880
60  U3=U(LMN3)  HAL 890
V3=V(LMN3)    HAL 900
P3=P(LMN3)    HAL 910
R03=R0(LMN3)  HAL 920
A3=SQRT(GAMMA*P3/R03)  HAL 930
C
C   CALCULATE THE PROPERTY INTERPOLATING POLYNOMIAL COEFFICIENTS  HAL 940
C
70  BU=(U1-U(LM1N1))*DYS  HAL 950
BV=(V1-V(LM1N1))*DYS  HAL 960
BP=(P1-P(LM1N1))*DYS  HAL 970
BRO=(R01-R0(LM1N1))*DYS  HAL 980
HAL 990
CU=U1-BU*Y3  HAL 1000
CV=V1-BV*Y3  HAL 1010
CP=P1-BP*Y3  HAL 1020
CRO=R01-BRO*Y3  HAL 1030
HAL 1040
C
C   CALCULATE THE CROSS DERIVATIVE INTERPOLATING POLYNOMIAL  HAL 1050
C   COEFFICIENTS  HAL 1060
C
DU=(U1-U(L1MN1))*DXR  HAL 1070
DV=(V1-V(L1MN1))*DXR  HAL 1080
DP=(P1-P(L1MN1))*DXR  HAL 1090
DRO=(R01-R0(L1MN1))*DXR  HAL 1100
HAL 1110
DU1=(U(LM1N1)-U(L1M1N1))*DXR  HAL 1120
DV1=(V(LM1N1)-V(L1M1N1))*DXR  HAL 1130
HAL 1140
DP1=(P(LM1N1)-P(L1M1N1))*DXR  HAL 1150
DRO1=(R0(LM1N1)-R0(L1M1N1))*DXR  HAL 1160
HAL 1170
BDU=(DU-DU1)*DYS  HAL 1180
BDV=(DV-DV1)*DYS  HAL 1190
BDP=(DP-DP1)*DYS  HAL 1200
BDRO=(DRO-DRO1)*DYS  HAL 1210
CDU=DU-BDU*Y3  HAL 1220
CDV=DV-BDV*Y3  HAL 1230
CDP=DP-BDP*Y3  HAL 1240
CDRO=DRO-BDRO*Y3  HAL 1250
HAL 1260
C
C   CALCULATE Y2  HAL 1270
C
CALL MAP (1,L,MDUM,AL,BE,DE,LD1,AL1,BE1,DE1)  HAL 1280
ALS=SORT(AL+AL*BE*BE)  HAL 1290
UV3=U3*AL+V3*BE+DE  HAL 1300
HAL 1310
AL2=AL  HAL 1320
DO 98 ILL=1,3  HAL 1330
UV2=U2*AL2+V2*BE+DE  HAL 1340
Y2=Y3*(UV2+SIGN*ALS*A2+UV3+SIGN*ALS*A3)*DT*0.5  HAL 1350
HAL 1360
C
C   INTERPOLATE FOR THE PROPERTIES  HAL 1370
C
U2=BU*Y2+CU  HAL 1380
V2=BV*Y2+CV  HAL 1390
P2=BP*Y2+CP  HAL 1400
R02=BR0*Y2+CRO  HAL 1410
AL2=Y2*AL  HAL 1420
AD=GAMMA*P2/R02  HAL 1430
IF (AD,GT,0,A) GO TO 80  HAL 1440
PRINT 360, N,L,MDUM  HAL 1450
IERR=1  HAL 1460
RETURN  HAL 1470
80  A2=SQRT(AD)  HAL 1480
CONTINUE  HAL 1490
C
C   INTERPOLATE FOR THE CROSS DERIVATIVES  HAL 1500
C
DU1=DU  HAL 1510
DV1=DV  HAL 1520
DP1=DP  HAL 1530
DRO1=DRO  HAL 1540
HAL 1550
DU2=BDU*Y2+CDU  HAL 1560
DV2=BDV*Y2+CDV  HAL 1570
DP2=BDP*Y2+CDP  HAL 1580
DRO2=BDRO*Y2+CDRO  HAL 1590
HAL 1600
C
C   CALCULATE THE PSI TERMS  HAL 1610
C
IF (NDIM,EQ,A) GO TO 110  HAL 1620
HAL 1630
HAL 1640

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        IF (IB,EQ,2) GO TO 100          HAL 1650
        ATERM2=R02*V2/(YCB(L)+Y2/BE)   HAL 1660
        GO TO 110                      HAL 1670
100    ATERM2=R02*V2/(YCB(L)+Y2/BE)   HAL 1680
        IF (IAV,EQ,0) GO TO 110       HAL 1690
        ATDS=R02*Y(L,2,N1)*DYL*BE     HAL 1700
        IF (ABS(ATERM2),GT,ABS(ATDS)) ATERM2=ATDS   HAL 1710
C
110    PSI21=-U1*DUL=DP1/R01        HAL 1720
        PSI31=-U1*DV1                HAL 1730
        PSI41=-U1*DP1+A1*A1*U1*DRO1  HAL 1740
        PSI122=-U2*DUL2=R02*DUL2-ATERM2  HAL 1750
        PSI22=-U2*DUL2=DP2/R02        HAL 1760
        PSI32=-U2*DV2                HAL 1770
        PSI42=-U2*DP2+A2*A2*U2*DRO2  HAL 1780
        IF (ICHAR,EQ,1) GO TO 150      HAL 1790
C
C    CALCULATE THE CROSS DERIVATIVES AT THE SOLUTION POINT   HAL 1800
C
120    IF (JFLAG,EQ,0) GO TO 120      HAL 1810
        IF (IB,EQ,2) GO TO 120      HAL 1820
        IF (L,EQ,2) GO TO 120      HAL 1830
        IF (L,NE,LJET-1) GO TO 120   HAL 1840
        IF (ILJET,EQ,2) GO TO 120   HAL 1850
        GO TO 130                  HAL 1860
        DU3=(U(L1MN3)-U3)*DXR        HAL 1870
        DV3=(V(L1MN3)-V3)*DXR        HAL 1880
        DP3=(P(L1MN3)-P3)*DXR        HAL 1890
        DRO3=(R0(L1MN3)-R03)*DXR    HAL 1900
        GO TO 140                  HAL 1910
130    DU3=(U3-U(L-1,MDUM,N3))*DXR   HAL 1920
        DV3=(V3-V(L-1,MDUM,N3))*DXR   HAL 1930
        DP3=(P3-P(L-1,MDUM,N3))*DXR   HAL 1940
        DRO3=(R03-R0(L-1,MDUM,N3))*DXR   HAL 1950
C
C    ENTER THE EXHAUST JET ITERATION LOOP                   HAL 1960
C
140    IF (JFLAG,F0,0) GO TO 150      HAL 1970
        IF (IB,EQ,2) GO TO 150      HAL 1980
        IF (L,LT,LJET) GO TO 150      HAL 1990
        YWI(L)=YW(L)
        UDUM=U(LMN3)                HAL 2000
        VDUM=V(LMN3)                HAL 2010
        PDUM=P(LMN3)                HAL 2020
        RODUM=R0(LMN3)              HAL 2030
150    DO 290 NJ=1,10                 HAL 2040
        IF (ICHAR,EQ,1) GO TO 250      HAL 2050
        IF (JFLAG,EQ,0) GO TO 210      HAL 2060
        IF (IB,EQ,2) GO TO 210      HAL 2070
        IF (L,LT,LJET) GO TO 210      HAL 2080
        IF (NJ,EQ,1) GO TO 200      HAL 2090
        IF (NJ,GT,2) GO TO 180      HAL 2100
        YWOLD=YW(L)
        POLD=P(LMN3)                HAL 2110
        IF (P(LMN3),LT,PE) GO TO 170   HAL 2120
        YW(L)=YW(L)+DELY            HAL 2130
        GO TO 190                  HAL 2140
160    YW(L)=YW(L)-DELY            HAL 2150
        GO TO 190                  HAL 2160
170    YW(L)=YW(L)+DELY            HAL 2170
        GO TO 190                  HAL 2180
180    IF (P(LMN3),EQ,POLD) GO TO 160   HAL 2190
        DYDP=(YW(L)-YWOLD)/(P(LMN3)-POLD)  HAL 2200
        YNEW=YW(L)+DYDP*(PE-P(LMN3))    HAL 2210
        YWOLD=YW(L)                  HAL 2220
        POLD=P(LMN3)                HAL 2230
        YW(L)=YNEW                  HAL 2240
190    IF (YW(L),LT,(P,0.98*YWOLD)) YW(L)=0.98*YWOLD  HAL 2250
        IF (YW(L),GT,(1.02*YWOLD)) YW(L)=1.02*YWOLD  HAL 2260
200    NXNY(L)=-(YW(L)-YW(L-1))*DXR    HAL 2270
        XWI(L)=(YW(L)-YWI(L))/DT      HAL 2280
        XWID=XWI(L)                  HAL 2290
        CALL MAP (1,L,MMAX,AL,BE,DE,LD1,AL1,BE1,DE1)  HAL 2300
        ALS=SORT(AL*AL+BE*BE)        HAL 2310
        U(LMN3)=UDUM                HAL 2320
        V(LMN3)=VDUM                HAL 2330
        P(LMN3)=PDUM                HAL 2340
        R0(LMN3)=RODUM              HAL 2350
C
C    CALCULATE THE PSI TERMS AT THE SOLUTION POINT           HAL 2360
C
210    IF (NDIM,EQ,0) GO TO 240      HAL 2370
        IF (IB,EQ,2) GO TO 220      HAL 2380
        ATERM3=R03*V3/(YCB(L)+1.0/BE)  HAL 2390
        GO TO 240                  HAL 2400
        HAL 2410
        HAL 2420
        HAL 2430
        HAL 2440
        HAL 2450
        HAL 2460
        HAL 2470

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220 IF (YCB(L),EQ,0,0) GO TO 230          HAL 2480
      ATERM3=R03*V3/YCB(L)                 HAL 2490
      IF (IAV,EQ,0) GO TO 240              HAL 2500
      ATDS=R03*V(L,2,N3)*DVR*BE           HAL 2510
      IF (ABS(ATERM3),GT,ABS(ATDS)) ATERM3=ATDS
      GO TO 240                           HAL 2520
230 ATERM3=R03*V(L,2,N3)*DVR*BE           HAL 2530
C                                         HAL 2540
C                                         HAL 2550
240 PSI13==U3*DRO3+R03*DUS=ATERM3        HAL 2560
      PSI23==U3*DUS=DP3/R03               HAL 2570
      PSI33==U3*DVS                      HAL 2580
      PSI43==U3*DP3+A3*A3*U3*DRO3        HAL 2590
C                                         HAL 2600
C                                         HAL 2610
C                                         HAL 2620
250 ABR=NXYNY(L)                         HAL 2630
      IF (IB,EQ,2) ABR=NXYNYCB(L)         HAL 2640
      ALB=0.5*(AL2+AL)/ALS               HAL 2650
      BEB=BE/ALS                          HAL 2660
      A1B=(A1+A3)*0.5                   HAL 2670
      A2B=(A2+A3)*0.5                   HAL 2680
      R01B=(R01+R03)*0.5                HAL 2690
      R02B=(R02+R03)*0.5                HAL 2700
      IF (ICHAR,EQ,1) GO TO 260          HAL 2710
      PSI21B=(PSI21+PSI23)*0.5          HAL 2720
      PSI31B=(PSI31+PSI33)*0.5          HAL 2730
      PSI41B=(PSI41+PSI43)*0.5          HAL 2740
      PSI12B=(PSI12+PSI13)*0.5          HAL 2750
      PSI22B=(PSI22+PSI23)*0.5          HAL 2760
      PSI32B=(PSI32+PSI33)*0.5          HAL 2770
      PSI42B=(PSI42+PSI43)*0.5          HAL 2780
      GO TO 270                           HAL 2790
260 PSI21B=PSI21                         HAL 2800
      PSI31B=PSI31                         HAL 2810
      PSI41B=PSI41                         HAL 2820
      PSI12B=PSI12                         HAL 2830
      PSI22B=PSI22                         HAL 2840
      PSI32B=PSI32                         HAL 2850
      PSI42B=PSI42                         HAL 2860
C                                         HAL 2870
C                                         HAL 2880
C                                         HAL 2890
270 U(LMN3)=(U(LMN1)-ABR*(V(LMN1)-XWID)+(PSI21B-ABR*PSI31B)*DT)/(1.0+HAL 2900
      1BR*ABR)                            HAL 2910
      V(LMN3)=-U(LMN3)+ABR*XWID          HAL 2920
      P(LMN3)=P2-SIGN*R02B+A2B*(ALB*(U(LMN3)-U2)+BEB*(V(LMN3)-V2))+(PSI4HAL 2930
      12B+A2B*A2B+PSI12B+SIGN*R02B+A2B*(ALB*PSI22B+BEB*PSI32B))*DT    HAL 2940
      IF (P(LMN3),LE,0,0) P(LMN3)=PLOW*PC          HAL 2950
      RO(LMN3)=RO(LMN1)+(P(LMN3)-P(LMN1)-PSI41B*DT)/(A1B*A1B)          HAL 2960
      IF (RO(LMN3),LE,0,0) RO(LMN3)=ROLOW/G          HAL 2970
      IF (IAV,EQ,0) GO TO 280             HAL 2980
C                                         HAL 2990
C                                         HAL 3000
C                                         HAL 3010
C                                         HAL 3020
      IF (ICHAR,EQ,1) GO TO 280          HAL 3030
      U(LMN3)=U(LMN3)+(QUT(L,MDUM)*ABR*QVT(L,MDUM))/(1.0+ABR*ABR)      HAL 3040
      V(LMN3)=-U(LMN3)*ABR               HAL 3050
      P(LMN3)=P(LMN3)+QPT(L,MDUM)        HAL 3060
C                                         HAL 3070
280 IF (JFLAG,EQ,0) GO TO 350          HAL 3080
      IF (IB,EQ,2) GO TO 350            HAL 3090
      IF (L,LT,LJET-1) GO TO 350          HAL 3100
      IF (L,EQ,LJET-1) GO TO 380          HAL 3110
      IF (ICHAR,EQ,1) GO TO 350          HAL 3120
      DELP=ABS((P(LMN3)-PE)/PE)          HAL 3130
      IF (DELP,LE,0.001) GO TO 350        HAL 3140
290 CONTINUE                           HAL 3150
      GO TO 350                           HAL 3160
C                                         HAL 3170
C                                         HAL 3180
C                                         HAL 3190
300 UD(3)=U(LMN3)                      HAL 3200
      VD(3)=V(LMN3)                      HAL 3210
      PD(3)=P(LMN3)                      HAL 3220
      ROD(3)=RO(LMN3)                    HAL 3230
      PD(4)=PE                           HAL 3240
      XM1=SGRT((UD(3)+UD(3)+VD(3)+VD(3))/(GAMMA*PD(3)/ROD(3)))       HAL 3250
      DUMD=1.0+GAM2*XM1*XM1              HAL 3260
      TD=PD(3)/ROD(3)/RGAS/G           HAL 3270
      TTD=TD*DUMD                        HAL 3280
      IF (PE,GT,PD(3),AND,XM1,GE,1.0) GO TO 310      HAL 3290
      TTD=TD*DUMD                        HAL 3300

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      IF (PE,GT,PD(3),AND,XM1,GE,1,0) GO TO 310          HAL 3310
      PTD=PD(3)*DUMD*GAM1                                HAL 3320
      ROD(4)=ROD(3)*(PE/PD(3))**(1,0/GAMMA)             HAL 3330
      GO TO 320                                           HAL 3340
310   PRD=PE/PD(3)                                         HAL 3350
      GAMD=(GAMMA+1,0)/(GAMMA-1,0)                         HAL 3360
      ROD(4)=ROD(3)*(GAMD*PRD+1,0)/(PRD+GAMD)           HAL 3370
320   TE=PE/ROD(4)/RGAS/G                                 HAL 3380
      XMACH=SQRT((TTD/TE-1,0)/GAM2)                      HAL 3390
      SS=SQRT(GAMMA*PE/ROD(4))                           HAL 3400
      VMAG=XMACH*SS                                     HAL 3410
      UD(4)=VMAG/SQRT(1,0+NXNY(LJET)*NXNY(LJET))       HAL 3420
      VD(4)=UD(4)*NXNY(LJET)                            HAL 3430
C
C   AVERAGE THE 1-SIDED MACH NOS FOR THE INTERIOR POINT CALCULATIONS HAL 3440
C
      XM2=SQRT((UD(4)*UD(4)+VD(4)*VD(4))/(GAMMA*PD(4)/ROD(4))) HAL 3450
      IF (XM1,GE,1,0) GO TO 350                           HAL 3460
      XMB=(XM1+XM2)/2,0                                    HAL 3470
      IF (XMB,GE,1,0) GO TO 330                           HAL 3480
      DPL=1,0                                              HAL 3490
      DPR=1,0                                              HAL 3500
      GO TO 340                                           HAL 3510
330   DPL=XM2=1,0                                         HAL 3520
      DPR=1,0=XM1                                         HAL 3530
      XMB=1,0                                              HAL 3540
340   DPLR=DPR+DPL                                       HAL 3550
      DUM=1,0+GAM2*XMB*XMB                               HAL 3560
      TEMP=TTD/DUM                                       HAL 3570
      P(LMN3)=PTD/DUM*GAM1                             HAL 3580
      RO(LMN3)=P(LMN3)/(RGAS*TEMP*G)                   HAL 3590
      QA=SQRT(2,0*GAM1*(RGAS*TTD*G-P(LMN3)/RO(LMN3))) HAL 3600
      DNXNY=(DPR*NXNY(LJET)+DPL*NXNY(L))/DPLR          HAL 3610
      U(LMN3)=QA/SQRT(1,0+DNXNY*DNXNY)                 HAL 3620
      V(LMN3)=-U(LMN3)*DNXNY                           HAL 3630
      IF (ICHAR,EQ,1) GO TO 350                         HAL 3640
      UD(1)=UD(3)                                         HAL 3650
      VD(1)=VD(3)                                         HAL 3660
      PD(1)=PD(3)                                         HAL 3670
      ROD(1)=ROD(3)                                       HAL 3680
      UD(2)=UD(4)                                         HAL 3690
      VD(2)=VD(4)                                         HAL 3700
      PD(2)=PD(4)                                         HAL 3710
      ROD(2)=ROD(4)                                       HAL 3720
      CONTINUE                                            HAL 3730
350   IF (JFLAG,EQ,0) RETURN                           HAL 3740
      IF (IB,EQ,2) RETURN                               HAL 3750
      IF (ICHAR,EQ,1) RETURN                           HAL 3760
      U(LJET=1,MMAX,N1)=UOLD                          HAL 3770
      YWI(LMAX)=YH(LMAX)                                HAL 3780
      YH(LMAX)=2,0*YH(L1)-YH(L2)                      HAL 3790
      NXNY(LMAX)=(YH(LMAX)-YH(L1))/DXR                HAL 3800
      XWI(LMAX)=(YH(LMAX)-YWI(LMAX))/DT              HAL 3810
      DELY=ABS(YH(LJET)-YWI(LJET))                   HAL 3820
      IF (DELY,EQ,0,0) DELY=0,0001                     HAL 3830
      RETURN                                              HAL 3840
C
360   FORMAT (1HB,6)H***** A NEGATIVE SQUARE ROOT OCCURED IN SUBROUTINE HAL 3850
      !WALL AT N=,I4,4H, L=,I2,8H, AND M=,I2,6H *****          HAL 3860
      END                                                 HAL 3870
                                                HAL 3880
                                                HAL 3890
                                                HAL 3900

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C SUBROUTINE INLET
C ***** THIS SUBROUTINE CALCULATES THE BOUNDARY MESH POINTS AT THE NOZZLE
C INLET FOR SUBSONIC FLOW
C *****
C COMMON /AV/ IAV,CAV,NST,3MP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81
I,21),QPT(81,21)
C COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)
C COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RO(81,21,2)
C COMMON /CNTRL/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAM1,GAINL
1M2,L1,L2,L3,M1,M2,DY,DT,N,N1,N3,NASM,IYEL,ICHAR,NID,LJET,JFLAG,INL
2IERR,IUI,IUD,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TCINL
3,LC,PLOW,ROLW
C COMMON /GEMTRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCT,ANGI,ANGE,XW(81),
1YW(81),XWI(81),YWI(81),NXNY(81),NMPTS,IINT,IDL,LT,NDIM
C COMMON /GCB/ NGCB,XICB,RICB,XTCB,RTCB,XECB,RECB,RCICB,RCTCB,ANGICBINL
1,ANGECB,XCB(81),YCB(81),XCB(81),YCB(81),NXNYCB(81),NCBPTS,IINTCBINL
2,IDLFCB,LECB
C COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASSI,MASST,THRUST,NINL
1$TAG
REAL MN3,NXNY,MASSI,MASST,NXNYCB,MASSE
C GRGB=GAMMA+RGAS*G
X3=XI
ATERM2=0,0
ATERM3=0,0
DO 180 ICHAR=1,2
DO 180 M=1,MMAX
LMN1=1+LD*(M-1)+LMD1
LMN3=1+LD*(M-1)+LMD3
L1MN1=2+LD*(M-1)+LMD1
L1MN1=2+LD*(M-2)+LMD1
LM1N1=1+LD*(M-2)+LMD1
LM1N3=1+LD*M+LMD3
CALL MAP (2,1,M,AL,BE,DE,2,AL1,BE1,DE1)
U2=U(LMN1)
A2=80RT(GAMMA+P(LMN1)/RO(LMN1))
IF (ICHAR,EQ,2) GO TO 10
U(LMN3)=U2
V(LMN3)=V(LMN1)
A3=A2
C CALCULATE THE PROPERTY INTERPOLATING POLYNOMIAL COEFFICIENTS
C
10 BU=(U(L1MN1)-U(LMN1))*DXR
BV=(V(L1MN1)-V(LMN1))*DXR
BP=(P(L1MN1)-P(LMN1))*DXR
BRO=(RO(L1MN1)-RO(LMN1))*DXR
BYCB=(YCB(2)-YCB(1))*DXR
BAL=(AL-AL)*DXR
BBE=(BE-BE)*DXR
CU=U(1,M,N1)-BU*X3
CV=V(1,M,N1)-BV*X3
CP=P(1,M,N1)-BP*X3
CRD=RO(1,M,N1)-BRO*X3
CYCB=YCB(1)-BYCB*X3
CAL=AL-BAL*X3
CBE=BE-BBE*X3
C CALCULATE THE CROSS DERIVATIVE INTERPOLATING POLYNOMIAL
C COEFFICIENTS
C
IF (M,EQ,1) GO TO 20
DU=(U(L1MN1)-U(LMN1))*DYR
DV=(V(L1MN1)-V(LMN1))*DYR
DP=(P(L1MN1)-P(LMN1))*DYR
DRO=(RO(L1MN1)-RO(LMN1))*DYR
DU1=(U(LMN1)-U(LMN1))*DYR
DV1=(V(LMN1)-V(LMN1))*DYR
DP1=(P(LMN1)-P(LMN1))*DYR
DRO1=(RO(LMN1)-RO(LMN1))*DYR
GO TO 40
20 IF (NGCB,NE,0) GO TO 30
DU=0,0
DV=V(2,2,N1)*DYR
DP=0,0
DRO=0,0
DU1=0,0
DV1=V(1,2,N1)*DYR

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      DP1=0,0          INL  840
      DRO1=0,0          INL  850
      GO TO 40          INL  860
50   DU=(U(2,2,N1)-U(2,1,N1))*DYR          INL  870
      DV=(V(2,2,N1)-V(2,1,N1))*DYR          INL  880
      DP=(P(2,2,N1)-P(2,1,N1))*DYR          INL  890
      DRO=(RO(2,2,N1)-RO(2,1,N1))*DYR          INL  900
      DU1=(U(1,2,N1)-U(1,1,N1))*DYR          INL  910
      DV1=(V(1,2,N1)-V(1,1,N1))*DYR          INL  920
      DP1=(P(1,2,N1)-P(1,1,N1))*DYR          INL  930
      DRO1=(RO(1,2,N1)-RO(1,1,N1))*DYR          INL  940
      BDU=(DU+DU1)*DXR          INL  950
      BDV=(DV+DV1)*DXR          INL  960
      BDP=(DP+DP1)*DXR          INL  970
      BDRO=(DRO+DRO1)*DXR          INL  980
      CDU=DU1=BDU*X3          INL  990
      CDV=DV1=BDV*X3          INL 1000
      CDP=DP1=BDP*X3          INL 1010
      CDR0=DRO1=BDRO*X3          INL 1020
C   CALCULATE X2          INL 1030
C
C   IF (ICHAR.EQ.2) A3=SQRT(GAMMA*P(LMN3)/RO(LMN3))
      DO 50 IL=1,2          INL 1040
      X2=X3=(U(1,M,N3)-A3+U2-A2)*B,SADT          INL 1050
C   INTERPOLATE FOR THE PROPERTIES          INL 1060
C
C   U2=BU*X2+CU          INL 1070
      P2=BP*X2+CP          INL 1080
      RO2=BR0*X2+CRO          INL 1090
      A2=SQRT(GAMMA*P2/RO2)          INL 1100
50   CONTINUE          INL 1110
      V2=BV*X2+CV          INL 1120
      YCB2=YCB*X2+CYCB          INL 1130
      AL2=BAL*X2+CAL          INL 1140
      BE2=BBE*X2+CBE          INL 1150
      UV2=U2*AL2+V2*BE2          INL 1160
C   INTERPOLATE FOR THE CROSS DERIVATIVES          INL 1170
C
C   DU2=BDU*X2+CDU          INL 1180
      DV2=BDV*X2+CDV          INL 1190
      DP2=BDP*X2+CDP          INL 1200
      DR02=BDRO*X2+CDRO          INL 1210
C   CALCULATE THE PSI TERMS          INL 1220
C
C   IF (NDIM.EQ.8) GO TO 70          INL 1230
      IF (M.EQ.1.AND.NGCB.EQ.0) GO TO 60          INL 1240
      ATERM2=RO2*V2/(DY*(M-1)/BE2+YCB2)          INL 1250
      GO TO 70          INL 1260
60   ATERM2=RO2*BE2*DV2          INL 1270
70   PSI12*=UV2*DR02*RO2*AL2*DU2=RO2*BE2*DV2=ATERM2          INL 1280
      PSI22*=UV2*DU2*AL2*DP2/RO2          INL 1290
      PSI42*=UV2*DP2*A2*A2*UV2*DR02          INL 1300
      IF (ICHAR.EQ.1) GO TO 130          INL 1310
C   CALCULATE THE CROSS DERIVATIVES AT THE SOLUTION POINT          INL 1320
C
C   IF (M.EQ.1.AND.NGCB.EQ.0) GO TO 80          INL 1330
      IF (M.EQ.MMAX) GO TO 90          INL 1340
      DU3=(U(LM1N3)-U(LMN3))*DYR          INL 1350
      DV3=(V(LM1N3)-V(LMN3))*DYR          INL 1360
      DP3=(P(LM1N3)-P(LMN3))*DYR          INL 1370
      DR03=(RO(LM1N3)-RO(LMN3))*DYR          INL 1380
      GO TO 100          INL 1390
80   DU3=0,0          INL 1400
      DV3=V(1,2,N3)*DYR          INL 1410
      DP3=0,0          INL 1420
      DR03=0,0          INL 1430
      GO TO 100          INL 1440
90   DU3=(U(1,MMAX,N3)-U(1,M1,N3))*DYR          INL 1450
      DV3=(V(1,MMAX,N3)-V(1,M1,N3))*DYR          INL 1460
      DP3=(P(1,MMAX,N3)-P(1,M1,N3))*DYR          INL 1470
      DR03=(RO(1,MMAX,N3)-RO(1,M1,N3))*DYR          INL 1480
      GO TO 100          INL 1490
      INL 1500
100  DU3=0,0          INL 1510
      DV3=V(1,2,N3)*DYR          INL 1520
      DP3=0,0          INL 1530
      DR03=0,0          INL 1540
      GO TO 100          INL 1550
110  DU3=(U(1,MMAX,N3)-U(1,M1,N3))*DYR          INL 1560
      DV3=(V(1,MMAX,N3)-V(1,M1,N3))*DYR          INL 1570
      DP3=(P(1,MMAX,N3)-P(1,M1,N3))*DYR          INL 1580
      DR03=(RO(1,MMAX,N3)-RO(1,M1,N3))*DYR          INL 1590
      INL 1600
C   CALCULATE THE PSI TERMS AT THE SOLUTION POINT          INL 1610
C
C   IF (NDIM.EQ.8) GO TO 120          INL 1620
      IF (M.EQ.1.AND.NGCB.EQ.0) GO TO 110          INL 1630
      ATERM3=RO(LMN3)*V(LMN3)/(DY*(M-1)/BE+YCB(1))          INL 1640
      GO TO 120          INL 1650
      INL 1660

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110 ATERM3=RO(LMN3)*BE*DV3
120 UV3=U(LMN3)*AL+V(LMN3)*BE
PSI13=-UV3*DR03+RO(LMN3)*AL*DU3=RO(LMN3)*BE*DV3=ATERM3
PSI23=-UV3*DU3*AL*DP3/RO(LMN3)
PSI43=-UV3*DP3+A3*A3*UV3*DR03
GO TO 140
130 PSI23=PSI22
PSI43=PSI42
PSI13=PSI12
C
C   SOLVE THE COMPATIBILITY EQUATIONS FOR U,V,P, AND RO
C
140 MN3=SQRT(U(LMN3)*U(LMN3)+V(LMN3)*V(LMN3))/A3
T2=P2/(RO2*RGAS*G)
PSI1B=(PSI12+PSI13)*0.5
PSI2B=(PSI22+PSI23)*0.5
PSI4B=(PSI42+PSI43)*0.5
GPSI1B=GAMMA*PSI1B
TTHETA=TAN(THETA(M))
UCORR=0.5+0.5/SQRT(1.0+TTHETA*TTHETA)
C
DO 160 ITER=1,20
DEM=(1.0+GAM2*MN3*MN3)
P(LMN3)=PT(M)/(DEM*GAM1)
T3=TT(M)/DEM
PB=(P2+P(LMN3))*0.5
RTB=RGAS*(T2+T3)*0.5*G
U(LMN3)=U2+DT*PSI2B+(P(LMN3)-P2*(PSI4B+RTB*GPSI1B)*DT)*SQRT(RTB/GAM1)
IMMA)/PB
U(LMN3)=U(LMN3)*UCORR
V(LMN3)=-U(LMN3)*TTHETA
OMN3=MN3
MN3=SQRT((U(LMN3)*U(LMN3)+V(LMN3)*V(LMN3))/(T3*GRGB))
IF (OMN3,NE,0,0) GO TO 150
IF (ABS(MN3-OMN3),LE,0.0001) GO TO 170
GO TO 160
150 IF (ABS((MN3-OMN3)/OMN3),LE,0.001) GO TO 170
160 CONTINUE
C
PRINT 190, M,N
170 RO(LMN3)=P(LMN3)/(RGAS*T3*G)
180 CONTINUE
RETURN
C
190 FORMAT (1H0,58H***** THE SOLUTION FOR NOZZLE ENTRANCE BOUNDARY POINL 2110
INT ( 1,,12,1H,,14,43H) FAILED TO CONVERGE IN 20 ITERATIONS *****) INL 2120
END INL 2130

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SUBROUTINE EXITT                                EXI  10
C
C
C
C
C THIS SUBROUTINE CALCULATES THE BOUNDARY MESH POINTS AT THE NOZZLE EXIT  50
C EXIT FOR SUBSONIC FLOW                         EXIT  60
C
C
C
C
C
C
COMMON /AV/ IAV,CAV,NST,SMP,LSS,CTA,XMU,XLA,RKMU,QUT(81,21),QVT(81,EXI 100
1,21),QPT(81,21)                                EXI 110
COMMON /ONESID/ UD(4),VD(4),PD(4),ROD(4)        EXI 120
COMMON /SOLUTN/ U(81,21,2),V(81,21,2),P(81,21,2),RO(81,21,2)      EXI 130
COMMON /CNTRL/ LMAX,MMAX,NMAX,NPRINT,TCONV,FDT,GAMMA,RGAS,GAM1,GAEXI 140
1M2,L1,L2,L3,M1,M2,DX,DY,DT,N,N1,N3,NASH,IVEL,ICHAR,NID,LJET,JFLAG,EXI 150
2IERR,IUI,IUO,DXR,DYR,LD,MD,LMD1,LMD3,IB,RSTAR,RSTARS,NPLOT,G,PC,TCEXI 160
3,LC,PLOW,ROLON                                 EXI 170
COMMON /GEMTRYC/ NGEOM,XI,RI,XT,RT,XE,RE,RCI,RCT,ANGI,ANGE,XW(81),EXI 180
1YW(81),XWI(81),YWI(81),NXNY(81),NHPTS,IINT,IDL,LT,NDIM      EXI 190
COMMON /GCB/ NGCB,XICB,RICB,XTCB,RECB,RCICB,RCTCB,ANGICBEXI 200
1,ANGEBC,XCB(R1),YCB(81),XCB(81),YCB(81),NXNYCB(81),NCBPTS,IINTCBEXI 210
2,IDLFCB,LECB                                 EXI 220
COMMON /BCC/ PT(21),TT(21),THETA(21),PE,MASSE,MASSI,MASST,THRUST,NEXI 230
1NSTAG                                         EXI 240
REAL MN3,NXNY,MASSI,MASST,NXNYCB,MASSE          EXI 250
C
X3=XE                                         EXI 260
ATERM1=0,0                                     EXI 270
ATERM2=0,0                                     EXI 280
ATERM3=0,0                                     EXI 290
EXI 300
DO 160 ICHAR=1,2                               EXI 310
DO 160 M=1,MMAX                                EXI 320
CALL MAP (2,LMAX,M,AL,BE,DE,L1,AL1,BE1,DE1)    EXI 330
U1=U(LMAX,M,N1)                                EXI 340
U2=U1                                         EXI 350
A1=SQRT(GAMMA*P(LMAX,M,N1)/RO(LMAX,M,N1))    EXI 360
A2=A1                                         EXI 370
IF (ICHAR,EQ,2) GO TO 10                      EXI 380
U(LMAX,M,N3)=U1                                EXI 390
A3=A1                                         EXI 400
EXI 410
C
C
CALCULATE THE PROPERTY INTERPOLATING POLYNOMIAL COEFFICIENTS   EXI 420
C
C
10 BU=(U(LMAX,M,N1)-U(L1,M,N1))*DXR           EXI 430
BV=(V(LMAX,M,N1)-V(L1,M,N1))*DXR           EXI 440
BP=(P(LMAX,M,N1)-P(L1,M,N1))*DXR           EXI 450
BRD=(RO(LMAX,M,N1)-RO(L1,M,N1))*DXR         EXI 460
BYCB=(YCB(LMAX)-YCB(L1))*DXR                 EXI 470
BAL=(AL-AL1)*DXR                            EXI 480
BBE=(BE-BE1)*DXR                            EXI 490
BDE=(DE-DE1)*DXR                            EXI 500
EXI 510
CU=U(LMAX,M,N1)-BU*X3                        EXI 520
CV=V(LMAX,M,N1)-BV*X3                        EXI 530
CP=P(LMAX,M,N1)-BP*X3                        EXI 540
CRD=RO(LMAX,M,N1)-BRD*X3                     EXI 550
CYCB=YCB(LMAX)-BYCB*X3                       EXI 560
CAL=AL-BAL*X3                                EXI 570
CBE=BE-BBE*X3                                EXI 580
CDE=DE-BDE*X3                                EXI 590
EXI 600
C
C
CALCULATE THE CROSS DERIVATIVE INTERPOLATING POLYNOMIAL   EXI 610
COEFFICIENTS                                         EXI 620
C
C
11 IF (M,EQ,1) GO TO 20                      EXI 630
DU=(U(LMAX,M,N1)-U(LMAX,M=1,N1))*DYR        EXI 640
DV=(V(LMAX,M,N1)-V(LMAX,M=1,N1))*DYR        EXI 650
DP=(P(LMAX,M,N1)-P(LMAX,M=1,N1))*DYR        EXI 660
DRD=(RO(LMAX,M,N1)-RO(LMAX,M=1,N1))*DYR     EXI 670
DU1=(U(L1,M,N1)-U(L1,M=1,N1))*DYR          EXI 680
DV1=(V(L1,M,N1)-V(L1,M=1,N1))*DYR          EXI 690
DP1=(P(L1,M,N1)-P(L1,M=1,N1))*DYR          EXI 700
DRO1=(RO(L1,M,N1)-RO(L1,M=1,N1))*DYR        EXI 710
GO TO 40                                         EXI 720
EXI 730
20 IF (LECB,EQ,LMAX) GO TO 30
DU=0,0                                         EXI 740
DV=V(LMAX,2,N1)*DYR                          EXI 750
DP=0,0                                         EXI 760
DRD=0,0                                         EXI 770
DU1=0,0                                         EXI 780
DV1=V(L1,2,N1)*DYR                          EXI 790
DP1=0,0                                         EXI 800
DRO1=0,0                                         EXI 810
GO TO 40                                         EXI 820
EXI 830

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30    DU=(U(LMAX,2,N1)-U(LMAX,1,N1))*DYR          EXI  840
      DV=(V(LMAX,2,N1)-V(LMAX,1,N1))*DYR          EXI  850
      DP=(P(LMAX,2,N1)-P(LMAX,1,N1))*DYR          EXI  860
      DRO=(RO(LMAX,2,N1)-RO(LMAX,1,N1))*DYR        EXI  870
      DU1=(U(L1,2,N1)-U(L1,1,N1))*DYR            EXI  880
      DV1=(V(L1,2,N1)-V(L1,1,N1))*DYR            EXI  890
      DP1=(P(L1,2,N1)-P(L1,1,N1))*DYR            EXI  900
      DRO1=(RO(L1,2,N1)-RO(L1,1,N1))*DYR          EXI  910
40    BDU=(DU-DU1)*DXR                         EXI  920
      BDV=(DV-DV1)*DXR                         EXI  930
      BDP=(DP-DP1)*DXR                         EXI  940
      BDRO=(DRO-DRO1)*DXR                      EXI  950
      CDU=DU-BDU*X3                          EXI  960
      CDV=DV-BDV*X3                          EXI  970
      CDP=DP-BDP*X3                          EXI  980
      CDRO=DRO-BDRO*X3                      EXI  990
C     CALCULATE X1 AND X2
C
      IF (ICHAR, EQ, 2) A3=SQRT(GAMMA*P(LMAX,M,N3)/RO(LMAX,M,N3))  EXI 1000
      DO 50 IL=1,2
      X1=X3*(U(LMAX,M,N3)+U1)*0.5*DT          EXI 1010
      X2=X3*(U(LMAX,M,N3)+A3+U2+A2)*0.5*DT        EXI 1020
C     INTERPOLATE FOR THE PROPERTIES
C
      U1=BU*X1+CU                      EXI 1030
      U2=BU*X2+CU                      EXI 1040
      P2=BP*X2+CP                      EXI 1050
      RO2=BR0*X2+CRO                    EXI 1060
      A2=SQRT(GAMMA*P2/RO2)             EXI 1070
50    CONTINUE
      V1=BV*X1+CV                      EXI 1080
      P1=BP*X1+CP                      EXI 1090
      RO1=BR0*X1+CRO                    EXI 1100
      YCB1=8YCB*X1+CYCB                EXI 1110
      AL1=BAL*X1+CAL                  EXI 1120
      BE1=BBE*X1+CBE                  EXI 1130
      DE1=BDE*X1+CDE                  EXI 1140
      UV1=U1*AL1+V1*BE1+DE1           EXI 1150
      A1=SQRT(GAMMA*P1/RO1)             EXI 1160
      V2=BV*X2+CV                      EXI 1170
      YCB2=8YCB*X2+CYCB                EXI 1180
      AL2=BAL*X2+CAL                  EXI 1190
      BE2=BBE*X2+CBE                  EXI 1200
      DE2=BDE*X2+CDE                  EXI 1210
      UV2=U2*AL2+V2*BE2+DE2           EXI 1220
      EXI 1230
      A1=SQRT(GAMMA*P1/RO1)             EXI 1240
      V2=BV*X2+CV                      EXI 1250
      YCB2=8YCB*X2+CYCB                EXI 1260
      AL2=BAL*X2+CAL                  EXI 1270
      BE2=BBE*X2+CBE                  EXI 1280
      DE2=BDE*X2+CDE                  EXI 1290
      UV2=U2*AL2+V2*BE2+DE2           EXI 1300
      EXI 1310
C     INTERPOLATE FOR THE CROSS DERIVATIVES
C
      DV1=BDV*X1+CDV                  EXI 1320
      DP1=BDP*X1+CDP                  EXI 1330
      DRO1=BDRO*X1+CDRO                EXI 1340
      DDU2=BDU*X2+CDU                  EXI 1350
      DV2=BDV*X2+CDV                  EXI 1360
      DP2=BDP*X2+CDP                  EXI 1370
      DRD2=BDRO*X2+CDRO                EXI 1380
      EXI 1390
C     CALCULATE THE PSI TERMS
C
      IF (NDIM, EQ, 0) GO TO 70
      IF (M, EQ, 1, AND, LECB, NE, LMAX) GO TO 60
      ATERM1=R01*V1/(DY*(M-1)/BE1+YCB1)      EXI 1400
      ATERM2=R02*V2/(DY*(M-1)/BE2+YCB2)      EXI 1410
      GO TO 70
60    ATERM1=R01*BE1*DV1                EXI 1420
      ATERM2=R02*BE2*DV2                EXI 1430
      PSI31=UV1*DV1*BE1+DP1/R01          EXI 1440
      PSI41=UV1*DP1+A1*A1*UV1+DRO1       EXI 1450
      PSI12=-UV2*DRO2-R02*AL2+DU2-R02*BE2+DV2+ATERM2  EXI 1460
      PSI22=-UV2*DU2+AL2+DP2/R02         EXI 1470
      PSI42=-UV2*DP2+A2*A2*UV2+DRO2       EXI 1480
      IF (ICHAR, EQ, 1) GO TO 130          EXI 1490
70    EXI 1500
      PSI31=UV1*DV1*BE1+DP1/R01          EXI 1510
      PSI41=UV1*DP1+A1*A1*UV1+DRO1       EXI 1520
      PSI12=-UV2*DRO2-R02*AL2+DU2-R02*BE2+DV2+ATERM2  EXI 1530
      PSI22=-UV2*DU2+AL2+DP2/R02         EXI 1540
      PSI42=-UV2*DP2+A2*A2*UV2+DRO2       EXI 1550
      IF (ICHAR, EQ, 1) GO TO 130          EXI 1560
      EXI 1570
C     CALCULATE THE CROSS DERIVATIVES AT THE SOLUTION POINT
C
      IF (M, EQ, 1, AND, LECB, NE, LMAX) GO TO 80
      IF (M, EQ, MMAX) GO TO 90
      DU3=(U(LMAX,M+1,N3)-U(LMAX,M,N3))*DYR        EXI 1580
      DV3=(V(LMAX,M+1,N3)-V(LMAX,M,N3))*DYR        EXI 1590
      DP3=(P(LMAX,M+1,N3)-P(LMAX,M,N3))*DYR        EXI 1600
      DRO3=(RO(LMAX,M+1,N3)-RO(LMAX,M,N3))*DYR        EXI 1610
      GO TO 100                                     EXI 1620
      EXI 1630
      DP3=(P(LMAX,M+1,N3)-P(LMAX,M,N3))*DYR        EXI 1640
      DRO3=(RO(LMAX,M+1,N3)-RO(LMAX,M,N3))*DYR        EXI 1650
      GO TO 100                                     EXI 1660

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80    DU3=0,0          EXI 1670
      DV3=V(LMAX,2,N3)*DYR
      DP3=0,0          EXI 1680
      DRD3=0,0          EXI 1690
      GO TO 100        EXI 1700
90    DU3=(U(LMAX,MMAX,N3)-U(LMAX,M1,N3))*DYR   EXI 1710
      DV3=(V(LMAX,MMAX,N3)-V(LMAX,M1,N3))*DYR   EXI 1720
      DP3=(P(LMAX,MMAX,N3)-P(LMAX,M1,N3))*DYR   EXI 1730
      DRD3=(RO(LMAX,MMAX,N3)-RO(LMAX,M1,N3))*DYR EXI 1740
      EXI 1750
C      CALCULATE THE PSI TERMS AT THE SOLUTION POINT EXI 1760
C      EXI 1770
C      EXI 1780
100   IF (NDIM,EQ,0) GO TO 120        EXI 1790
      IF (M,EQ,1,AND,LECB,NE,LMAX) GO TO 110        EXI 1800
      ATERM3=RO(LMAX,M,N3)*V(LMAX,M,N3)/(DY*(M-1)/BE+YCB(LMAX)) EXI 1810
      GO TO 120        EXI 1820
110   ATERM3=RO(LMAX,1,N3)*BE+DV3          EXI 1830
120   UV3=U(LMAX,M,N3)*AL+V(LMAX,M,N3)*BE+DE          EXI 1840
      PSI13=UV3*DRD3=RO(LMAX,M,N3)*(AL+DU3+BE+DV3)*ATERM3 EXI 1850
      PSI23=UV3*DU3=AL+DP3/RO(LMAX,M,N3)          EXI 1860
      PSI33=UV3*DV3=BE+DP3/RO(LMAX,M,N3)          EXI 1870
      PSI43=UV3*DP3+A3*A3*UV3*DRD3          EXI 1880
      EXI 1890
C      CALCULATE THE COMPATIBILITY EQUATION COEFFICIENTS EXI 1900
C      EXI 1910
130   IF (ICHAR,EQ,1) GO TO 140        EXI 1920
      PSI31B=(PSI31+PSI33)*0.5          EXI 1930
      PSI41B=(PSI41+PSI43)*0.5          EXI 1940
      PSI12B=(PSI12+PSI13)*0.5          EXI 1950
      PSI22B=(PSI22+PSI23)*0.5          EXI 1960
      PSI42B=(PSI42+PSI43)*0.5          EXI 1970
      GO TO 150        EXI 1980
140   PSI31B=PSI31          EXI 1990
      PSI41B=PSI41          EXI 2000
      PSI12B=PSI12          EXI 2010
      PSI22B=PSI22          EXI 2020
      PSI42B=PSI42          EXI 2030
      EXI 2040
C      SOLVE THE COMPATIBILITY EQUATIONS FOR U,V,P, AND RO EXI 2050
C      EXI 2060
150   P(LMAX,M,N3)=PE          EXI 2070
      RO(LMAX,M,N3)=RO1+2,0*(P(LMAX,M,N3)-P1-DT*PSI41B)/(A3+A3+A1+A1) EXI 2080
      U(LMAX,M,N3)=U2+((PSI42B+(RO2+RO(LMAX,M,N3))*(A2+A3)*PSI22B/4,0+(AEXI 2090
      12+A2+A3)*PSI12B/2,0)*DT-(P(LMAX,M,N3)*P2))/(RO2+RO(LMAX,M,N3))/EXI 2100
      2(A2+A3)*4,0          EXI 2110
      V(LMAX,M,N3)=V1+DT*PSI31B          EXI 2120
160   CONTINUE          EXI 2130
      V(LMAX,MMAX,N3)=-U(LMAX,MMAX,N3)*NXNY(LMAX)          EXI 2140
      V(LMAX,1,N3)=-U(LMAX,1,N3)*NXNYCB(LMAX)          EXI 2150
      IF (JFLAG,EQ,0) RETURN          EXI 2160
      V(LMAX,MMAX,N3)=V(LMAX,MMAX,N3)+XW1(LMAX)          EXI 2170
      RETURN          EXI 2180
      END          EXI 2190

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