





**A3 Formulas.** Standard equations.

- paraboloid:  $z = x^2 + y^2$  
- saddle:  $z = x^2 - y^2$  
- 1-sheeted hyperboloid:  $x^2 + y^2 - z^2 = 1$  
- 2-sheeted hyperboloid:  $-x^2 - y^2 + z^2 = 1$  
- ellipsoid:  $x^2 + y^2 + z^2 = 1$  
- double-cone:  $z^2 = x^2 + y^2$  

**Integral Formulas.**

- $\int \frac{1}{1+t^2} dt = \arctan t + C$
- $\int \frac{1}{\sqrt{1-t^2}} dt = \arcsin t + C$
- $\int \frac{1}{t} dt = \ln |t| + C$

**Trig Identities.**

- power reduction:  $\cos^2 \theta = \frac{1}{2} + \frac{1}{2} \cos 2\theta$   
 $\sin^2 \theta = \frac{1}{2} - \frac{1}{2} \cos 2\theta$
- double angle:  $\sin 2\theta = 2 \sin \theta \cos \theta$   
 $\cos 2\theta = \cos^2 \theta - \sin^2 \theta$

**A1 Formulas.**

- $\vec{v} \cdot \vec{w} = \|\vec{v}\| \|\vec{w}\| \cos \theta$
- $\|\vec{v} \times \vec{w}\| = \|\vec{v}\| \|\vec{w}\| \sin \theta = [\text{parallelogram area}]$
- $|\vec{v} \cdot (\vec{w} \times \vec{r})| = [\text{parallelepiped volume}]$
- $\text{proj}_{\vec{v}}(\vec{w}) = \left( \frac{\vec{v} \cdot \vec{w}}{\vec{v} \cdot \vec{v}} \right) \vec{v}$
- $\text{comp}_{\vec{v}}(\vec{w}) = \frac{\vec{v} \cdot \vec{w}}{\|\vec{v}\|}$

**A2 Formulas.**

- distance from point **B** to plane  $\mathcal{P}$  with normal  $\vec{n}$ :  
 $\frac{|\vec{AB} \cdot \vec{n}|}{\|\vec{n}\|}$  where **A** is on  $\mathcal{P}$
- distance from point **B** to line  $\ell$  with direction  $\vec{v}$ :  
 $\frac{\|\vec{AB} \times \vec{v}\|}{\|\vec{v}\|}$  where **A** is on  $\ell$

