Technology for X-Informatics
Kmeans and MapReduce Parallelism

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Big Data Ecosystem in One Sentence

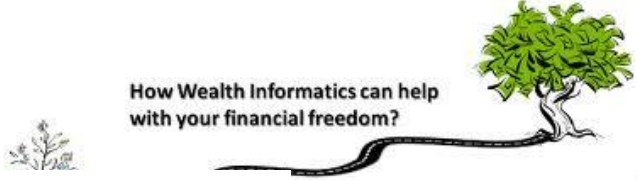
Use Clouds running Data Analytics Collaboratively processing Big Data to solve problems in X-Informatics (or e-X)

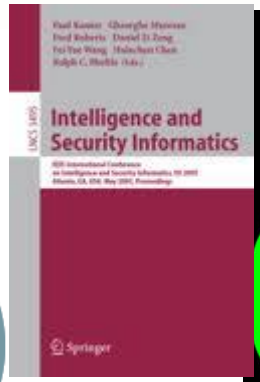
X = Astronomy, Biology, Biomedicine, Business, Chemistry, Climate, Crisis, Earth Science, Energy, Environment, Finance, Health, Intelligence, Lifestyle, Marketing, Medicine, Pathology, Policy, Radar, Security, Sensor, Social, Sustainability, Wealth and Wellness with more fields (physics) defined implicitly

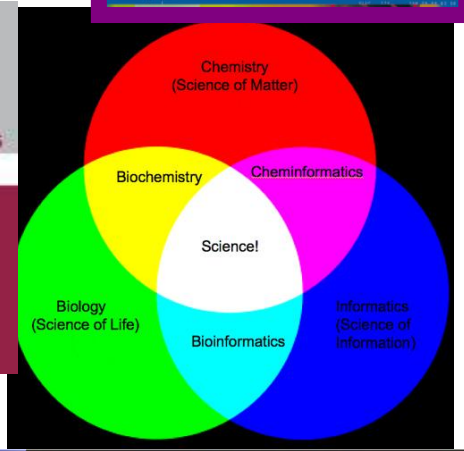
Spans Industry and Science (research)

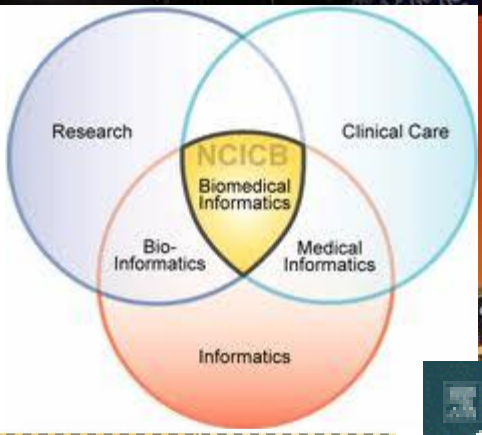
Education: Data Science see recent New York Times articles

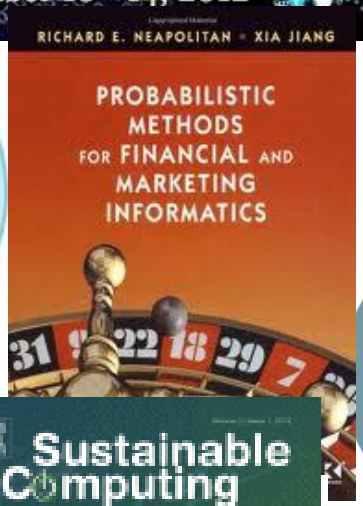
http://datascience101.wordpress.com/2013/04/13/new-york-times-data-science-articles/

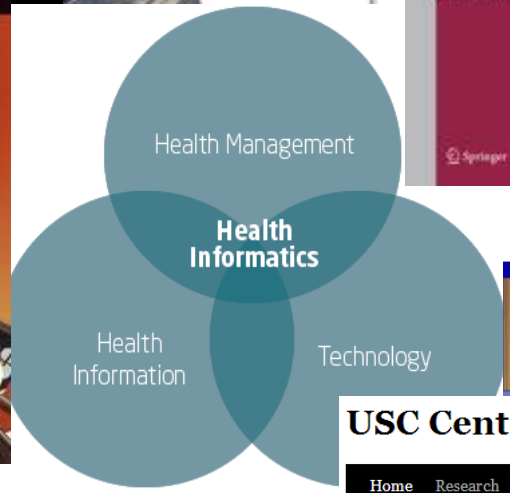


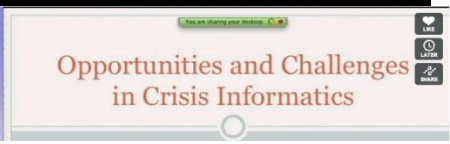


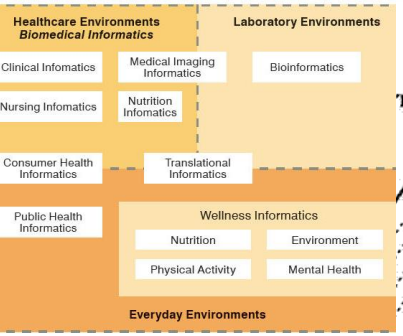


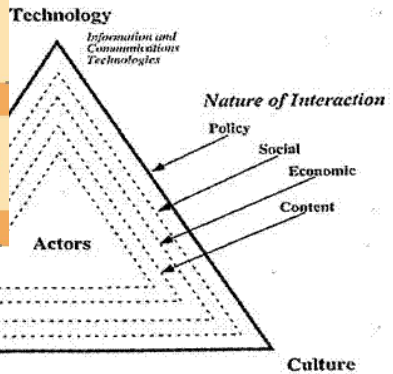




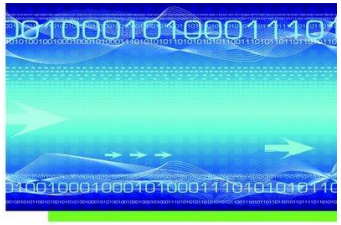








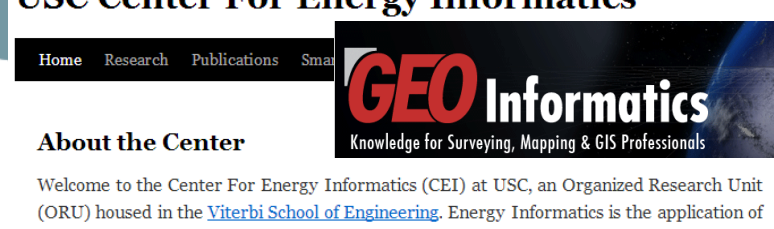
Social Informatics

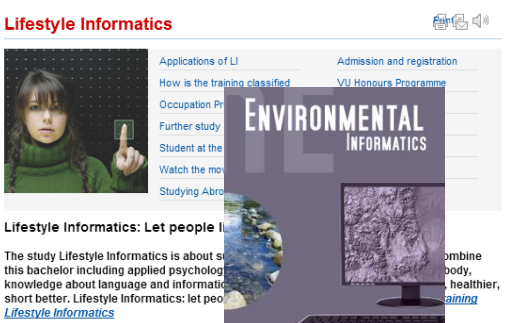


Noelia Penelope Greer (Ed.)

Business Informatics

Information technology, Management,





MapReduce Kmeans in Python

Slightly Changed Sequential version

- We change to allow MapReduce implementation
- Overall iteration over starting positions
  - Initialize Centroids
  - Iterate until converged
    - Call **map** to find association and do first step in find centroids as sum over point vectors and distortion
    - **Reduce** step: Divide summed centers by points in center to get centroid
      - Do other book keeping
      - Delete zero size clusters
    - Check convergence
- Return best solution based on Quality criterion

Parallel MapReduce Version

```
Iseven = np.empty([tot], dtype=bool)
for i in arange(tot):
        Iseven[i] = (i%2 == 0);
obs1 = compress(Iseven, obs, 0)
obs2 = compress(logical_not(Iseven), obs, 0)

avg_dist = []
diff = thresh+1.
while diff > thresh:
        #
        if Parallelism == 1:
                code_book, NumPointsinClusters, distortsum, distortmax, NumPoints  = Kmeans_map(obs, code_book)
        if Parallelism == 2:
                # Can be Parallel Map Operations
                code_book1, NumPointsinClusters1, distortsum1, distortmax1, NumPoints1  = Kmeans_map(obs1, code_book)
                code_book2, NumPointsinClusters2, distortsum2, distortmax2, NumPoints2  = Kmeans_map(obs2, code_book)
                #
                #       Following are 4 Reduction Operations
                #       Note maps include local reductions
                code_book = np.add( code_book1, code_book2)
                NumPointsinClusters = np.add( NumPointsinClusters1, NumPointsinClusters2)
                distortsum = distortsum1 + distortsum2
                distortmax = np.maximum(distortmax1, distortmax2)
                NumPoints = NumPoints1 +  NumPoints2
        #
        code_book = compress(np.greater(NumPointsinClusters, 0), code_book, 0)
        #       remove code_books that didn't have any members
        #
        j = 0
        nc = code_book.shape[0]
        for i in arange(nc):
                if NumPointsinClusters[i] > 0:
                        code_book[j,:] = code_book[j,:] / NumPointsinClusters[i]
                        j = j + 1
```

Map

Reduce

Map for Kmeans

```
def Kmeans_map(obs, code_book):
        No = obs.shape[0]
        nc = code_book.shape[0]
        # nc is current number of clusters (may decrease if zero clusters last iteration)
        #
        #compute membership and distances between obs and code_book
        obs_code, distort = vq(obs, code_book)
        distortsum = np.sum(distort)
        distortmax = np.amax(distort)
        #
        # vq returns an indexing array obs_code mapping rows of obs (the points) to code_book (the centroids)
        # distort is an array of length No that has difference between observation and chosen centroid
        # vq stands for vector quantization and is provided in SciPy
        #
        VectorDimension = obs.shape[1]
        NewCode_Book = np.zeros([nc, VectorDimension])
        NumPointsinClusters = np.zeros([nc])
        for i in arange(nc):
                #               Loop over clusters labelled with i
                cell_members = compress(equal(obs_code, i), obs, 0)
                NumPointsinClusters[i] = cell_members.shape[0]
                #               Extract Points in this Cluster; extract points whose quantization label is i
                #
                NewCode_Book[i] = np.sum(cell_members, 0)
                #               Calculate centroid of i'th cluster
        return NewCode_Book, NumPointsinClusters, distortsum, distortmax, No
```

- This routine takes Points in obs and Centroids in code_book and associates each point with nearest centroid
- It calculates Non normalized centroids (sum over vectors in cluster), Number of points in each cluster and convergence measures (mean and max of distance between points and centers)

Comments!

- Extension to P-way parallelism simple
  - Divide data into P parts
  - Run P separate maps with each having all centers
  - Sum (or max) P versions of center sums, Point sums, convergence criterion in Reduce
- Maps can run in parallel
- Reduce would run in a single process except for large levels of parallelism
- Sequential code uses mean directly not sums
- Parallel code does center sums and
- Divides by total number of points in Reduce