

**Quiz 1. True/False:** The function  $f(x) = 9 - 5x$  is a linear function with slope 5 and  $y$ -intercept 9.

**Solution.** The statement is *false*. We know a function of the form  $f(x) = mx + b$  is a linear function with slope  $m$  and  $y$ -intercept  $b$ . Because we have  $f(x) = 9 - 5x = -5x + 9$ , we have  $m = -5$ , i.e. slope  $-5$ , and  $y$ -intercept 9, i.e.  $(0, 9)$ . But then the slope is  $-5$ , not the given value of 5.

**Quiz 2. True/False:** If  $f(x) = 2x - 1$  and  $g(x) = 3 - x$ , then  $(f \circ g)(0) = f(0)g(0) = -1 \cdot 3 = -3$ .

**Solution.** The statement is *false*. First, note that  $f(0) = 2(0) - 1 = -1$ ,  $g(0) = 3 - 0 = 3$ , and  $f(3) = 2(3) - 1 = 6 - 1 = 5$ . What was given was function multiplication, i.e. what was computed was  $(fg)(0) = f(0)g(0) = -1 \cdot 3 = -3$ . What was originally written was function composition. We have  $(f \circ g)(0) = f(g(0)) = f(3) = 5$ .

**Quiz 3. True/False:** Compared to the graph of  $f(x)$ , the graph of  $5 - 3f(x + 2)$  is stretched by a factor of 3, then shifted to the right by 2 and up by 5.

**Solution.** The statement is *false*. We know that  $f(x + 2)$  is the graph of  $f(x)$  shifted 2 to the *left*. The graph of  $-3f(x + 2)$  is then the graph of  $f(x)$  shifted two to the left, stretched by a factor of 3, and reflected across the  $x$ -axis. Finally, the graph of  $5 - 3f(x + 2)$  is the graph of  $f(x)$  shifted two to the left, stretched by a factor of 3, reflected across the  $x$ -axis, then shifted upwards by 5.

**Quiz 4. True/False:** The function  $f(x) = 4(5^{-x})$  is a concave up, decreasing, exponential function.

**Solution.** The statement is *true*. A function of the form  $f(x) = Ab^x$  is an exponential function. We can summarize whether  $f(x)$  is increasing or decreasing and concave up or down as follows: But

	$0 < b < 1$	$b > 1$
$A > 0$	Decreasing, Concave Up	Increasing, Concave Up
$A < 0$	Increasing, Concave Down	Decreasing, Concave Down

we have  $f(x) = 4(5^{-x}) = 4(5^{-1})^x = 4\left(\frac{1}{5}\right)^x$ . Therefore,  $f(x)$  is exponential with  $A = 4 > 0$  and  $0 < b = \frac{1}{5} < 1$ . Therefore,  $f(x)$  is a decreasing, concave up, exponential function.

**Quiz 5. True/False:** The function  $f(x) = 5(2^{1-2x})$  is equal to the function  $g(x) = 10\left(\frac{1}{4}\right)^x$ .

**Solution.** The statement is *true*. Observe that we have...

$$f(x) = 5(2^{1-2x}) = 5 \cdot 2^1 \cdot 2^{-2x} = 10 \cdot 2^{-2x} = 10(2^{-2})^x = 10\left(\frac{1}{2^2}\right)^x = 10\left(\frac{1}{4}\right)^x = g(x)$$