

Quiz 1. *True/False:* $9/3 + 2(3^2 + 10) - 8 + 4 \cdot 3 = 45$

Solution. The statement is *false*. To see this, we can simply follow the order of operations—using PEMDAS as a guide:

$$9/3 + 2(3^2 + 10) - 8 + 4 \cdot 3 \stackrel{?}{=} 55$$

$$9/3 + 2(9 + 10) - 8 + 4 \cdot 3 \stackrel{?}{=} 55$$

$$9/3 + 2(19) - 8 + 4 \cdot 3 \stackrel{?}{=} 55$$

$$3 + 2(19) - 8 + 4 \cdot 3 \stackrel{?}{=} 55$$

$$3 + 38 - 8 + 4 \cdot 3 \stackrel{?}{=} 55$$

$$3 + 38 - 8 + 12 \stackrel{?}{=} 55$$

$$41 - 8 + 12 \stackrel{?}{=} 55$$

$$33 + 12 \stackrel{?}{=} 55$$

$$45 \neq 55$$

Quiz 2. *True/False:* $\gcd(2^3 \cdot 3 \cdot 5, 2 \cdot 3^2 \cdot 7) = 2^3 \cdot 3^2 \cdot 5 \cdot 7$.

Solution. The statement is *false*. Remember given a prime factorization of the numbers, we find the gcd by choosing the *smallest* powers of each prime that appears in the factorizations. So we should have $\gcd(2^3 \cdot 3 \cdot 5, 2 \cdot 3^2 \cdot 7) = 2 \cdot 3$. Instead, the largest power of each prime that appears in the factorizations was chosen which is how we compute the lcm. Therefore, we have $\text{lcm}(2^3 \cdot 3 \cdot 5, 2 \cdot 3^2 \cdot 7) = 2^3 \cdot 3^2 \cdot 5 \cdot 7$.

Quiz 3. *True/False:* $\frac{\frac{3}{\frac{10}{12}}}{\frac{5}{5}} = \frac{1}{8}$

Solution. The statement is *true*. Note that division by a nonzero number is the same as multiplying by its reciprocal. So we have

$$\frac{\frac{3}{\frac{10}{12}}}{\frac{5}{5}} = \frac{3}{10} \cdot \frac{5}{12} = \frac{3^1}{10^2} \cdot \frac{5^1}{12^4} = \frac{1}{8}$$

One can also rewrite the problem as...

$$\frac{\frac{3}{\frac{10}{12}}}{\frac{5}{5}} = \frac{3}{10} \div \frac{12}{5}$$

But then to divide, we multiply by the reciprocal and proceed as in the solution above.

Quiz 4. True/False: The number $0.\overline{19}$ is rational.

Solution. The statement is *true*. Any real number with a decimal expansion that either terminates or repeats is a rational and hence can be expressed as a/b , where a and b are integers and $b \neq 0$. Moreover, every rational number, i.e. the a/b 's, have a decimal expansion that either terminates or repeats. We can even find a rational expression for $0.\overline{19}$:

$$\begin{array}{rcl} 100r & = & 19.191919191919\dots \\ - \quad r & = & 0.191919191919\dots \\ \hline 99r & = & 19 \end{array}$$

But then $r = 0.\overline{19} = \frac{19}{99}$.

Quiz 5. True/False: $\sqrt[3]{2^8 \cdot 3^3 \cdot 5^1 \cdot 7^5} = 2^2 \cdot 3^1 \cdot 7 \sqrt[3]{2^2 \cdot 5^1 \cdot 7^2}$

Solution. The statement is *true*. There are two ways to think about this. First, we should write out the numbers and group them into threes and pull out/leave the terms appropriately:

$$\sqrt[3]{2^8 \cdot 3^3 \cdot 5^1 \cdot 7^5} = \sqrt[3]{\underbrace{2 \cdot 2 \cdot 2}_{2^3} \cdot \underbrace{2 \cdot 2 \cdot 2}_{2^3} \cdot \underbrace{3 \cdot 3 \cdot 3}_{3^3} \cdot 5 \cdot \underbrace{7 \cdot 7 \cdot 7}_{7^3} \cdot 7 \cdot 7} = 2^2 \cdot 3^1 \cdot 7 \sqrt[3]{2^2 \cdot 5 \cdot 7^2}$$

Alternatively, we can use division. We know that $8/3$ is 2 with remainder 2, $3/3$ is 1 with remainder 0, $1/3$ is 0 with remainder 1, and $5/3$ is 1 with remainder 2. So we can pull out two 3's with 2 remaining, one 3 with 0 remaining, no 5's with 1 remaining, and two 7's with 2 remaining, which gives:

$$\sqrt[3]{2^8 \cdot 3^3 \cdot 5^1 \cdot 7^5} = 2^2 \cdot 3^1 \cdot 7 \sqrt[3]{2^2 \cdot 5^1 \cdot 7^2}$$

Quiz 6. True/False: 57 increased by 127% is $57(1.27)$.

Solution. The statement is *false*. To find 127% of 57, we would multiply 57 by the percent written as a decimal. This would be $57(1.27)$. However, to increase or decrease a number by a percentage, we compute the number $\#(1 \pm \%)$, where we add if we are increasing, subtract if we are decreasing, $\#$ is the number, and $\%$ is the percentage written as a decimal. So to increase 57 by 127%, we need to compute $57(1 + 1.27) = 57(2.27)$.