Name: Cale

Caleb McWhorter — Solutions

"Algebra is the metaphysics of arithmetic."

MATH 308 Fall 2022

HW 16: Due 12/06

−John Ray

Problem 1. (10pt) Let $\mathbf{u}, \mathbf{v} \in \mathbb{R}^4$ be defined by $\mathbf{u} = \begin{pmatrix} 1 \\ 0 \\ -3 \\ 2 \end{pmatrix}$ and $\mathbf{v} = \begin{pmatrix} 4 \\ -1 \\ 6 \\ -5 \end{pmatrix}$. Showing all your

work, compute the following:

- (a) $-6\mathbf{u}$
- (b) $\mathbf{v} \mathbf{u}$
- (c) u + 2v
- (d) $\mathbf{u} \cdot \mathbf{v}$

Problem 2. (10pt) Define matrices A, B, C as follows:

$$A = \begin{pmatrix} 1 & 0 & -4 \\ -2 & 3 & 1 \end{pmatrix}, \qquad B = \begin{pmatrix} 0 & 2 & -2 \\ 5 & 1 & 4 \end{pmatrix}, \qquad C = \begin{pmatrix} 2 & 0 \\ -1 & 6 \\ 5 & 3 \end{pmatrix}$$

Showing all your work, compute the following:

- (a) 4A
- (b) A B
- (c) 3A + B
- (d) AC
- (e) B^T

Problem 3. (10pt) Define matrices A, B, C as follows:

$$A = \begin{pmatrix} 1 & 0 & 2 \\ 0 & -1 & 3 \end{pmatrix}, \qquad B = \begin{pmatrix} 2 & -1 \\ 0 & 3 \end{pmatrix}, \qquad C = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Showing all your work and explaining your reasoning, answer the following:

- (a) What is B^2 ?
- (b) If CA is defined, compute it. If not, explain why.
- (c) What is a_{23} ? What is b_{21} ?
- (d) If M = AC, without explicitly computing AC, what is m_{23} ?

Problem 4. (10pt) If A, B are matrices, is it true $(A+B)^2 = A^2 + 2AB + B^2$? If so, explain why. If not, explain why not.