Quiz 1. *True/False*: Prunella is trying to find the cardinality of the set $\{1, 2, 1, 4, 1, 8\}$. She counts how many numbers are in the set and finds that there are six numbers. Therefore, the cardinality of the set is 6.

Solution. The statement is *false*. The cardinality (or 'size') of a set is the number of elements in a set. However, the order of elements of a set does not matter nor do repeats within a set. Therefore, the set $\{1,2,1,4,1,8\}$ is the same as the set $\{1,2,4,8\}$. The cardinality of this set is clearly 4. We may then more clearly define the cardinality of a set to be the number of *distinct* elements of a set. Prunella is mistaken believing that the repeated 1s count towards the cardinality.

Quiz 2. *True/False*: If A is a set with 5 elements and B is a set with 3 elements, then A-B is a set with 2 elements.

Solution. The statement is *false*. It may be possible for some sets. For instance, if $A = \{a, b, c, d, e\}$ and $B = \{a, c, e\}$, then $A - B = \{b, d\}$. Then |A| = 5, |B| = 3, and |A - B| = 2. However, this is not true for *all* sets. For instance, if $A = \{a, b, c, d, e\}$ and $B = \{-5, 6, \text{nice'}\}$, then $A - B = \{a, b, c, d, e\}$. But then in this case, |A| = 5, |B| = 3, and |A - B| = 5. The cardinality of A - B depends on how many elements of A have been 'removed' because they were elements of A. This could be 1, 2, or 3 elements depending on the cardinality of $A \cap B$.

Quiz 3. *True/False*: The number of ways of choosing three distinct candle sticks from a collection of five to arrange on a mantle is ${}_5P_3 = 5 \cdot 4 \cdot 3 = 60$ possible choices of arrangements.

Solution. The statement is *true*. We can count this directly. There are 5 possible candlesticks to choose for the far left position. This leaves 4 possible choices for the rightmost candlestick and then finally 3 possible choices for the middle candlestick. But then in total there are $5 \cdot 4 \cdot 3 = 60$ total possible arrangements. Alternatively, we know the number of ways of arranging k objects from a collection of n distinct objects, with repetition not allowed, where the order of the arrangement matters, is given by ${}_{n}P_{k}$. Here, we have n=5 and k=3. But then we know the number of possible arrangements is ${}_{5}P_{3} = \frac{5!}{(5-3)!} = \frac{5!}{2!} = \frac{5 \cdot 4 \cdot 3 \cdot 2 \cdot 1}{2 \cdot 1} = 5 \cdot 4 \cdot 3 = 60$.

Quiz 4. *True/False*: The number of possible ways of guessing the correct answers to a 10 question True/False exam is $_{10}C_{10}$.

Solution. The statement is *false*. We know that the order of the answer choices matters. We know also that $_{10}C_{10}$ represents a combination. For combinations, order is unimportant. Therefore, it is highly unlikely (but not strictly speaking impossible) that $_{10}C_{10}$ gives the correct count. We know each question has 2 possible answers. One must answer the first question, and the second, and the third, etc. There are 10 questions. Therefore, there are $2 \cdot 2 \cdot \cdots \cdot 2 = 2^{10} = 1024$ total possible number of ways of answering (guessing) the answers for this collection of 10 true/false questions.

Quiz 5. *True/False*: Harriet lives In Alkonost, AZ. There it is sunny 90% of the time. Harriet is planning her weekend. She can expect that there is a $0.90 \cdot 0.90 = 0.81$ probability, i.e. 81% chance, that it is sunny both days.

Solution. The statement is *false*. If A and B are events, then we know that $P(A \text{ and } B) = P(A) \cdot P(B)$, if A and B are independent. Recall two events are independent if and only if the occurrence or non-occurrence of an event changes the probability that the other event occurs/does not occur. If A and B are not independent, it may not be true that $P(A \text{ and } B) = P(A) \cdot P(B)$. Let A be the event that it is sunny on Saturday and B be the event that it is sunny on Sunday. Clearly, A and B are not independent events. For instance, if it is sunny/rainy one day, it is more/less likely to be sunny/rainy the next. Therefore, it may not be the case that there is a $0.90 \cdot 0.90 = 0.81$ probability, i.e. 81% chance, that it is sunny both days. Generally, $P(A \text{ and } B) = P(A)P(B \mid A) = P(B)P(A \mid B)$, whether or not A and B are independent.

Quiz 6. *True/False*: At a community college, 45% of students have some experience with Excel, 55% of students have some experience with Word, and 70% of students have experience with at least one of them. Therefore, 15% of students have experience only with Excel.

Solution. The statement is true. If A and B are events, we know that $P(A \text{ or } B) = P(A) + P(B) - P(A \cap B)$. But then we know that P(Excel or Word) = P(Excel) + P(Word) - P(Excel & Word). But then we have 0.70 = 0.45 + 0.55 - P(Excel & Word). Then 0.70 = 1.00 - P(Excel & Word) so that P(Excel & Word) = 0.30. Finally, because every person that knows Excel either knows word or does not (and these are mutually exclusive), we know that 0.45 = P(Excel) = P(Only Excel) + P(Excel and Word) = P(Only Excel) + 0.30. But this shows that P(Only Excel) = 0.15. Therefore, 15% of students have experience only with Excel.

Quiz 7. *True/False*: One can use a histogram to give the number of people enjoying certain film genres.

Ouiz 8. True/False: Both mean and median are measures of center for data.

Quiz 9. *True/False*: If the standard deviation of a set of data is 0, then it must be that every number in the data set is the same.

Quiz 10. *True/False*: Suppose you plot a normal distribution with mean μ and standard deviation σ , i.e. $N(\mu, \sigma)$. If you were to plot a normal distribution with smaller mean but larger standard deviation, this distribution would be located 'to the left' and would be 'wider' than the original distribution.

Quiz 11. *True/False*: If three lines intersect, they are concurrent lines.

Quiz 12. *True/False*: There exists a right triangle with external angle 30°.

Quiz 13. True/False: An acute triangle has only one acute angle.

Quiz 14. True/False: Two geometric figures are congruent if and only if they have the same area.

Quiz 15. True/False: Suppose you have a triangle, $\triangle ABC$, such that the sides \overline{AB} , \overline{BC} , and \overline{AC} are such that $|\overline{AB}| < |\overline{BC}| < |\overline{AC}|$. Then we have $|\overline{AB}|^2 + |\overline{BC}|^2 = |\overline{AC}|^2$.