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MATH 108  
Fall 2023  
HW 3: Due 09/19

*"Money is not the most important thing in the world. Love is. Fortunately, I love money."*

—Jackie Mason

**Problem 1.** (10pt) The CPI in 2022 was approximately 296.071. According to the US Bureau of Labor Statistics, the current CPI is 307.026.

- (a) Find the inflation rate from 2022 to 2023.
- (b) If the inflation rate in (a) continues from 2023 to 2024, estimate the cost of a good next year that costs \$46.99 this year,
- (c) If the inflation rate in (a) remains constant each year what will the increase in prices be from 2023 to 2028?

**Solution.**

- (a) Because the current CPI is greater than the CPI last year, we know there has been inflation. We know also that the inflation rate is...

$$\left| \frac{\text{Current CPI}}{\text{Former CPI}} - 1 \right| = \left| \frac{307.026}{296.071} - 1 \right| = |1.037 - 1| = 0.037$$

Therefore, the inflation rate was 3.7%.

- (b) If we want to compute  $N$  increased or decreased by a %, we compute  $N \cdot (1 \pm \%_d)$ , where  $\%_d$  is the percentage written as a decimal and we choose '+' if it is a percentage increase and choose '-' if it is a percentage decrease. Assuming an inflation rate of 3.7%, we expect a percentage increase of 3.7%. But then, assuming a constant inflation rate, we approximate that the cost of the good next year will be...

$$\$46.99(1 + 0.037) = \$46.99(1.037) = \$48.7286 \approx \$48.73$$

- (c) If we apply the same percentage increase or decrease  $n$  times in a row, we multiply by  $(1 \pm \%_d)$  a total of  $n$  times. Therefore, if we want to compute  $N$  increased or decreased by a % a total of  $n$  times, we compute  $P(1 + \%_d)^n$ . But then the  $(1 + \%_d)^n$  factor represents the percentage increase or decrease resulting from applying a percentage increase/decrease of  $\%_d$  a total of  $n$  times. Assuming a constant inflation rate of 3.7% over the five years from 2023 to 2028, we have...

$$(1 + 0.037)^5 = (1.037)^5 = 1.19920597 = 1 + 0.19920597$$

Therefore, we can recognize this as representing a 19.92% increase, i.e. prices will increase 19.92% from 2023 to 2028.

**Problem 2.** (10pt) Stevie runs a shop that sells hot teas and baked beans. The shop is, surprisingly, not doing well. She decides to take out a simple discount note to pay for some additional advertising in the hopes that it will drive customers to the store. The note the bank offers is \$8,000 for 7 months at 8.3% annual interest.

- (a) What is the maturity for this simple discount note?
- (b) What is the discount for this note?
- (c) What is the interest Stevie pays on this loan?
- (d) How much does Stevie receive from the bank?
- (e) At the end of the 7 months, how much does Stevie owe the bank?

**Solution.**

- (a) The maturity for a simple discount note is the loan amount before the interest is taken. Therefore, the maturity,  $M$ , for this note is \$8,000.
- (b) The discount for a simple discount note is the amount of interest paid on the loan—which is paid up-front. Using a rate of 8.3% annual interest for a period of 7 months, i.e.  $\frac{7}{12}$  years, we have

$$D = Mrt = \$8000 \cdot 0.083 \cdot \frac{7}{12} \approx \$387.33$$

- (c) The interest in a simple discount note is the discount. In (b), we found a discount of \$387.33. Therefore, the interest paid is \$387.33.
- (d) In a simple discount note, one receives the value of maturity after the discount has been applied, i.e. after the interest has been paid. But then, we have...

$$\text{Amount Received} = M - D = \$8000 - \$387.33 = \$7,612.67$$

- (e) In total, Stevie must pay the maturity of the loan plus the discount (the interest). Therefore, a total of  $\$8000 + \$387.33 = \$8387.33$  is paid on the loan. The discount is paid up-front. Therefore, at the end of the 7 months, Stevie need only repay the \$8,000 maturity of the loan.