

MAT 100: Exam 1
Fall – 2021
10/20/2021
85 Minutes

Name: _____

Write your name on the appropriate line on the exam cover sheet. This exam contains 13 pages (including this cover page) and 15 questions. Check that you have every page of the exam. Answer the questions in the spaces provided on the question sheets. Be sure to answer every part of each question and show all your work.

Question	Points	Score
1	8	
2	8	
3	8	
4	6	
5	6	
6	4	
7	4	
8	6	
9	8	
10	6	
11	6	
12	4	
13	10	
14	8	
15	8	
Total:	100	

1. (8 points) Compute the following:

(a) $4 + 4 - 5 \cdot 0 + 1 - 1 =$

(b) $12/4 \cdot 3 - 1 =$

(c) $-5 - 6 + 2 \cdot 3^2 =$

(d) $10/5 - 6(3 - 4)^3 =$

2. (8 points) Simplify the following, being sure to have no negative exponents in your expression.

(a) $\frac{x^{-6}}{x^{-3}} =$

(b) $\frac{(xy^2)^2}{x^2y^3} =$

(c) $\frac{x^6y^{-3}}{x^3y^2} =$

(d) $\left(\frac{y^3}{x^2}\right)^{-2} =$

3. (8 points) Compute the following, being sure to simplify your answer completely:

(a) $4 + \frac{1}{5} =$

(b) $\frac{3}{10} - \frac{5}{4} =$

(c) $\frac{6}{35} \cdot \frac{7}{15} =$

(d) $\frac{-\frac{7}{5}}{\frac{21}{10}} =$

4. (6 points) Write a mathematical expression that computes the following:

(a) 33% of 48

(b) 92% of 172

(c) 121% of 16

5. (6 points) Write a mathematical expression that computes the following:

(a) 71 decreased by 90%

(b) 88 increased by 30%

(c) 55 increased by 190%

6. (4 points) Convert the following decimal numbers to scientific notation:

(a) $7400 =$

(b) $0.002 =$

7. (4 points) Convert the following numbers in scientific notation to decimal notation:

(a) $8.0 \cdot 10^{-6} =$

(b) $1.65 \cdot 10^3 =$

8. (6 points) Find the prime factorizations of the following integers:

(a) $210 =$

(b) $125 =$

(c) $88 =$

9. (8 points) Compute the following:

(a) $\gcd(14, 21) =$

(b) $\text{lcm}(6, 20) =$

(c) $\gcd(252, 9720) = \gcd(2^2 \cdot 3^2 \cdot 7, 2^3 \cdot 3^5 \cdot 5) =$

(d) $\text{lcm}(252, 9720) = \text{lcm}(2^2 \cdot 3^2 \cdot 7, 2^3 \cdot 3^5 \cdot 5) =$

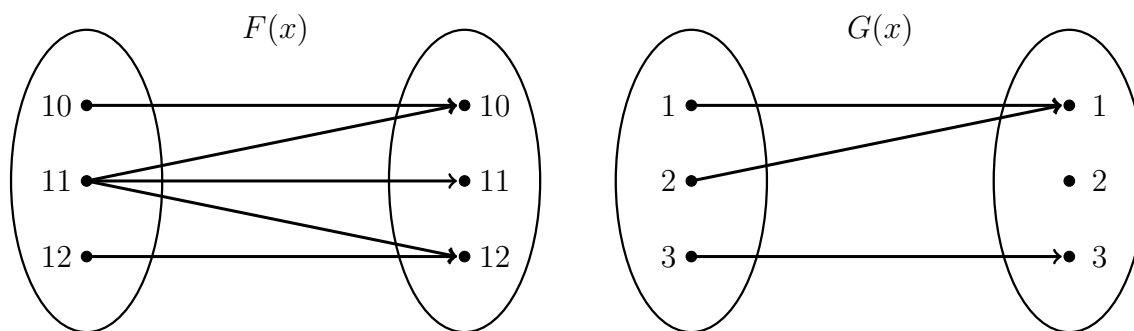
10. (6 points) Simplify the following as much as possible:

(a) $\sqrt{50} =$

(b) $\sqrt{80} =$

(c) $\sqrt[3]{2^2 \cdot 3^6 \cdot 5} =$

11. (6 points) Consider the following relations below:



x	$H(x)$	x	$J(x)$
1	1	5	-1
2	2	6	-2
3	3	7	-3
4	4	8	-4
1	5	9	-6

$$K(x) := 0.782x - 1283$$

$$L(x) := 2x(x^2 + 1)(x^4 + 1)$$

Determine if each of the relations given above is a function. If the relation is a function, write 'T' (True) and if the relation is *not* a function, write 'F' (False):

(a) _____: $F(x)$

(b) _____: $G(x)$

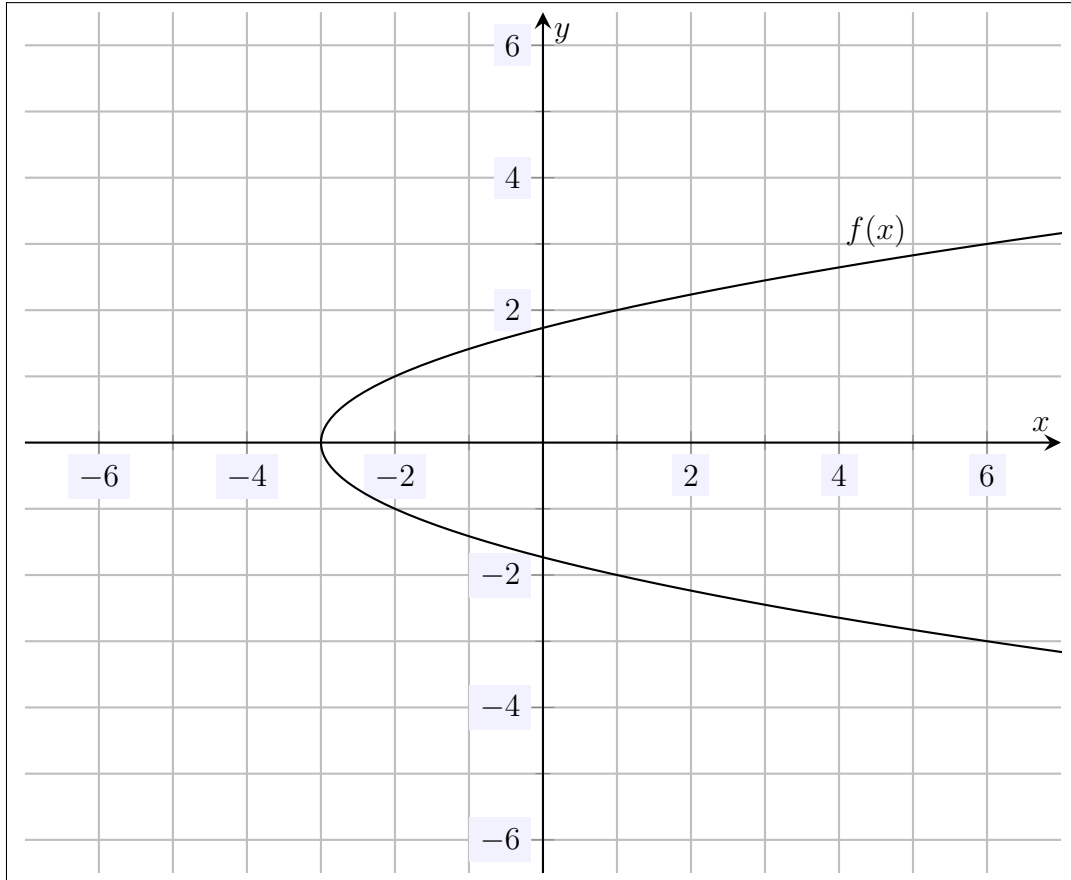
(c) _____: $H(x)$

(d) _____: $J(x)$

(e) _____: $K(x)$

(f) _____: $L(x)$

12. (4 points) Consider the relation plotted below.



(a) Is the relation plotted above a function? Explain.

(b) Does the relation above have an inverse function? Explain.

13. (10 points) Consider the functions given in the table below.

x	0	1	2	3	4
$f(x)$	1	4	0	-2	6
$g(x)$	2	3	5	5	7

Compute the following:

(a) $g(3) =$

(b) $g(2) - f(3) =$

(c) $f(0)g(1) =$

(d) $(f + g)(4) =$

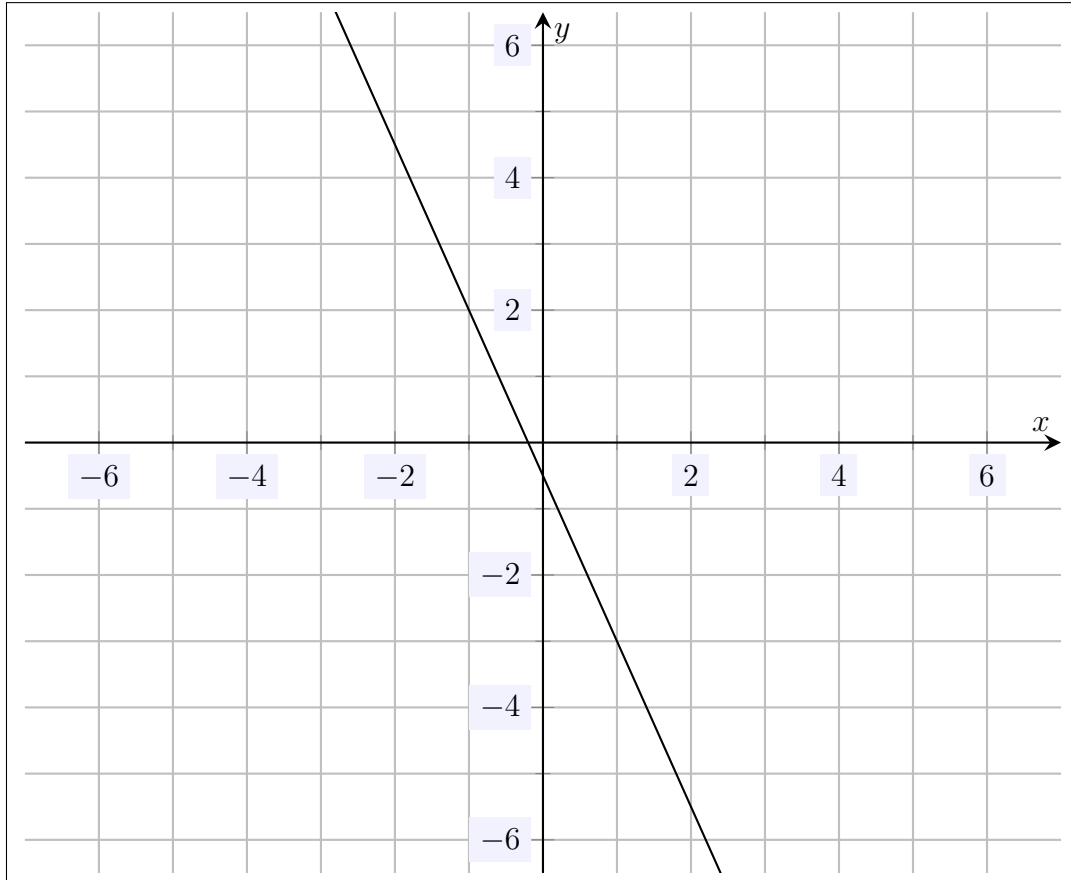
(e) $(f \circ g)(1) =$

(f) $(g \circ f)(1) =$

(g) x -intercept of $f(x)$:

(h) y -intercept of $g(x)$:

14. (8 points) Find the equation of the line shown below:



15. (8 points) Find the equation of the line that is perpendicular to the line $y = \frac{1}{2}x + 1$ that passes through the point $(2, 1)$.