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**MATH 108** 

Spring 2024 "[Waitress] Aww, honey there are other fish in the sea. [Sally] I don't wanna hear the specials, lady!"

HW 3: Due 01/31

— Waitress & Sally Solomon, Third Rock from the Sun

**Problem 1.** (10pts) Suppose that the CPI in 2023 was approximately 290.503. According to the US Bureau of Labor Statistics, the current CPI is 300.728.

- (a) Find the inflation rate from 2023 to 2024.
- (b) If the inflation rate in (a) continues from 2024 to 2025, estimate the cost of a good next year that costs \$69.99 this year,
- (c) If the inflation rate in (a) remains constant each year, what will the increase in prices be from 2024 to 2030? What percent more will goods cost in 2030 than 2024?

## Solution.

(a) Because the current CPI is greater than the CPI last year, we know there has been inflation. We know also that the inflation rate is...

$$\left| \frac{\text{Current CPI}}{\text{Former CPI}} - 1 \right| = \left| \frac{300.728}{290.503} - 1 \right| = |1.03519757 - 1| = 0.03519757$$

Therefore, the inflation rate was 3.52%.

(b) If we want to compute N increased or decreased by a %, we compute  $N \cdot (1 \pm \%_d)$ , where  $\%_d$  is the percentage written as a decimal and we choose '+' if it is a percentage increase and choose '-' if it is a percentage decrease. Assuming an inflation rate of 3.52%, we expect a percentage increase of 3.52%. But then, assuming a constant inflation rate, we approximate that the cost of the good next year will be...

$$\$69.99(1+0.0352) = \$69.99(1.0352) = \$72.4536 \approx \$72.45$$

(c) If we apply the same percentage increase or decrease n times in a row, we multiply by  $(1 \pm \%_d)$  a total of n times. Therefore, if we want to compute N increased or decreased by a % a total of n times, we compute  $P(1 + \%_d)^n$ . But then the  $(1 + \%_d)^n$  factor represents the percentage increase or decrease resulting from applying a percentage increase/decrease of  $\%_d$  a total of n times. Assuming a constant inflation rate of 3.52% over the six years from 2024 to 2030, we have...

$$(1+0.0352)^6 = (1.0352)^6 = 1.230681 = 1+0.230681$$

Therefore, we can recognize this as representing a 23.07% increase, i.e. prices will increase 23.07% from 2024 to 2030.

**Problem 2.** (10pts) Patrick runs a chard stand. Chard being...chard, Patrick needs to take out a loan to help pay for dancers to advertise his product at the local farmer's market to drive up sales. The local bank offers a simple discount note for \$5,600 over a period of 8 months at 8.7% annual interest.

- (a) What is the maturity for this simple discount note?
- (b) What is the discount for this note?
- (c) What is the interest Patrick pays on this loan?
- (d) How much does Patrick receive from the bank?
- (e) At the end of the 8 months, how much does Patrick owe the bank?

## Solution.

- (a) The maturity for a simple discount note is the requested loan amount. Therefore, the maturity is M = \$5,600.
- (b) The discount for a simple discount note is the interest paid (up-front) on the loan. But this is...

$$D = Mrt = \$5,600(0.087) \frac{\$}{12} = \$324.80$$

- (c) The interest paid on the loan is the discount on the note. But from (b), we know that this is \$324.80.
- (d) Patrick receives the full maturity minus the discount (interest) that is paid up-front. Therefore, the amount received (the proceeds) are...

$$P = M - D = \$5,600 - \$324.80 = \$5,275.20$$

(e) Patrick only ever has to pay back the amount borrowed plus interest. However, the interest (discount) is paid up-front. Therefore, at the end of the 8 months, Patrick need only pay back the amount borrowed—\$5,600.