

Name: \_\_\_\_\_

MATH 101

Fall 2023

HW 9: Due 10/30

*“Mathematics is the most beautiful and  
most powerful creation of human spirit.”  
– Stefan Banach*

**Problem 1.** (10pt) Values for several functions are given in the table below.

$x$	-3	-2	-1	0	1	2	3
$f(x)$	4	8	-1	5	-3	0	-2
$g(x)$	1	6	0	-6	-7	-3	1
$h(x)$	-4	0	3	5	10	3	9

Given the data above, compute the following:

(a)  $(h + g)(-2) =$

(b)  $(f - g)(0) =$

(c)  $(5h)(1) =$

(d)  $\left(\frac{h}{f}\right)(1) =$

(e)  $g(-3)h(3) =$

(f)  $g(-1 - f(3)) =$

(g)  $(h \circ g)(2) =$

(h)  $(g \circ h)(2) =$

(i)  $(f \circ g)(-1) =$

(j)  $(h \circ g \circ f)(1) =$

**Problem 2.** (10pt) Suppose  $f(x)$  and  $g(x)$  are the functions given below.

$$f(x) = 2x - 3$$

$$g(x) = x^2 + 2x - 1$$

Compute the following:

(a)  $f(5) =$

(b)  $g(-2) =$

(c)  $f(0) - 3g(2) =$

(d)  $(f - g)(x) =$

(e)  $(fg)(x) =$

(f)  $\left(\frac{f}{g}\right)(x) =$

(g)  $(f \circ g)(0) =$

(h)  $(g \circ f)(0) =$

(i)  $(f \circ g)(x) =$

(j)  $(g \circ f)(x) =$

**Problem 3.** (10pt) Let  $f(x)$  be the function given by  $f(x) = 3x - 7$ .

- (a) Find a value in the range of  $f$ . Be sure to justify why the value is in the range.
- (b) Compute  $f(4)$ . Is  $(4, 1)$  on the graph of  $f$ ? Explain.
- (c) Is there an  $x$  such that  $f(x) = 11$ ? Explain.
- (d) Is  $1 \in f^{-1}(3)$ ? Explain.
- (e) Assuming  $f^{-1}$  exists, what is  $f(f^{-1}(\pi))$  and  $f^{-1}(f(\sqrt{2}))$ ?