MAT 108: Exam 3
Spring – 2022
05/11/2022
85 Minutes

Name:	

Write your name on the appropriate line on the exam cover sheet. This exam contains 10 pages (including this cover page) and 9 questions. Check that you have every page of the exam. Answer the questions in the spaces provided on the question sheets. Be sure to answer every part of each question and show all your work. If you run out of room for an answer, continue on the back of the page — being sure to indicate the problem number.

Question	Points	Score
1	16	
2	8	
3	10	
4	10	
5	10	
6	10	
7	10	
8	13	
9	13	
Total:	100	

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1. A student is given a set of data points on an exam to for which they are to create a linear regression. Suppose that the points are (-2,1), (0,5), (2,3), and (4,5). Their computation of the least square regression line is shown below. Unfortunately, they spilled coffee on their work, obscuring some of the numbers.

(a) (7 points) Recompute (i)–(vii) for the student and place your answers in the appropriate space below.

$$\overline{x} = (\mathbf{i})$$

$$\overline{y} = \frac{1+5+3+5}{4} = \frac{14}{4} = 3.5$$

$$s_x^2 = \frac{1}{3} \cdot 20 \approx 6.6667 \Longrightarrow s_x \approx 2.582$$

$$s_y^2 = (\mathbf{i}\mathbf{i}) \Longrightarrow s_y = (\mathbf{i}\mathbf{i}\mathbf{i})$$

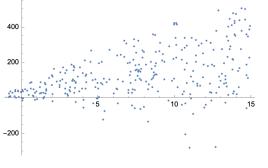
x	y	$x_i - \overline{x}$	$(x_i - \overline{x})^2$	$y_i - \overline{y}$	$(y_i - \overline{y})^2$	$\frac{x_i - \overline{x}}{s_x}$	$\frac{y_i - \overline{y}}{s_y}$	$\frac{x_i - \overline{x}}{s_x} \cdot \frac{y_i - \overline{y}}{s_y}$
-2	1	(iv)	9	-2.5	6.25	-1.1619	-1.3056	1.517
0	5	-1	1	1.5	2.25	-0.3873	0.7833	-0.3034
2	3	1	1	-0.5	(v)	0.3873	-0.2611	-0.1011
4	5	3	9	1.5	2.25	1.1619	0.7833	(vi)
		Sum:	(vii)	Sum:	11		Sum:	2.0226

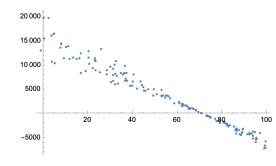
$$(i) =$$
 $(v) =$ $(ii) =$ $(vi) =$ $(vii) =$ $(vii) =$ $(vii) =$

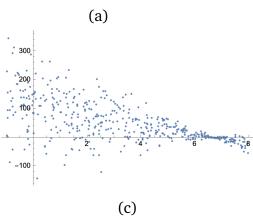
- (b) (5 points) Compute r^2 for the student. Based on this value, explain to the student whether the least square regression line is a 'good' model.
- (c) (4 points) Given that the resulting linear regression is $\hat{y} = 0.5x + 3$, find the predicted value for x = 2 and its corresponding residual for the student.

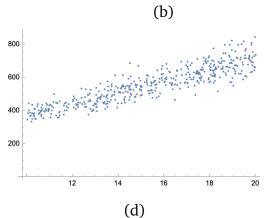
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2. (8 points) The same student from Problem 1 also had to compute the regression coefficient, R, for several different data sets. Unfortunately, they dropped their papers—separating the data from the computed R value. Match the dataset to the most likely regression coefficient for the student.









(i)
$$R = -0.9831$$

(ii) _____:
$$R = -0.6050$$

(iii) _____:
$$R = 0.4635$$

(iv) ____:
$$R = 0.9032$$

- 3. Suppose A, B, and C are events in a finite probability space. Suppose P(A)=0.40, P(B)=0.20, P(C)=0.30, P(A and B)=0, and P(B and C)=0.05.
 - (a) (2 points) Assuming A and C are independent, compute P(A and C).

(b) (2 points) Still assuming that A and C are independent, find P(A or C).

(c) (2 points) Are A and B disjoint events? Explain.

(d) (2 points) Are A and B independent events? Explain.

(e) (2 points) Find $P(B \mid C)$.

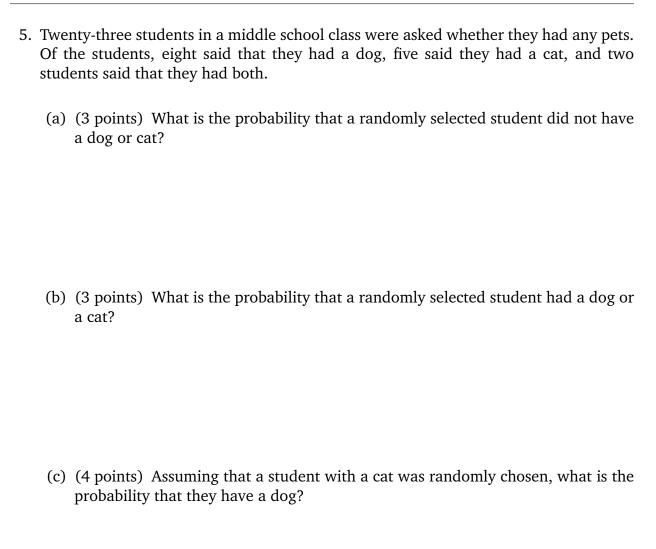
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4. Students across various STEM majors at local colleges were surveyed to determine whether they preferred Netflix, Hulu, Disney+, or HBO Max. The results are shown below.

	Biology	Chemistry	Computer Science	Physics	Mathematics	Total
Netflix	3	7	14	4	8	36
Hulu	6	13	12	3	7	41
Disney+	15	4	1	4	2	26
HBO Max	10	2	5	2	1	20
Total	34	26	32	13	18	123

- (a) (2 points) What is the probability that a randomly selected student was a Physics major that preferred Disney+?
- (b) (2 points) What is the probability that a randomly selected student preferred Hulu?
- (c) (2 points) What is the probability that a randomly selected student preferred Netflix or was a Chemistry major?
- (d) (2 points) What is the probability that a Biology or Computer Science major preferred Netflix?
- (e) (2 points) What is the probability that a student that preferred HBO Max was a Mathematics major?

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6. When it comes to 'fine' Mexican dining, people agree the two best options are Chipotle or Moe's. One survey suggested 80% of people prefer Chipotle to Moe's. However of those surveyed, only 40% of people that went to Chipotle had a good experience whereas 60% of Moe's customers had a good experience.

(a)	(3 points)	What i	is the	probability	that	a	randomly	selected	person	had	a	good
	experience	at Chi	potle (or Moe's?								

(b) (3 points) What is the probability that a randomly selected person either preferred Moe's or had a bad experience at Chipotle?

(c) (4 points) What is the probability that a person that did not have a good experience had it at Chipotle?

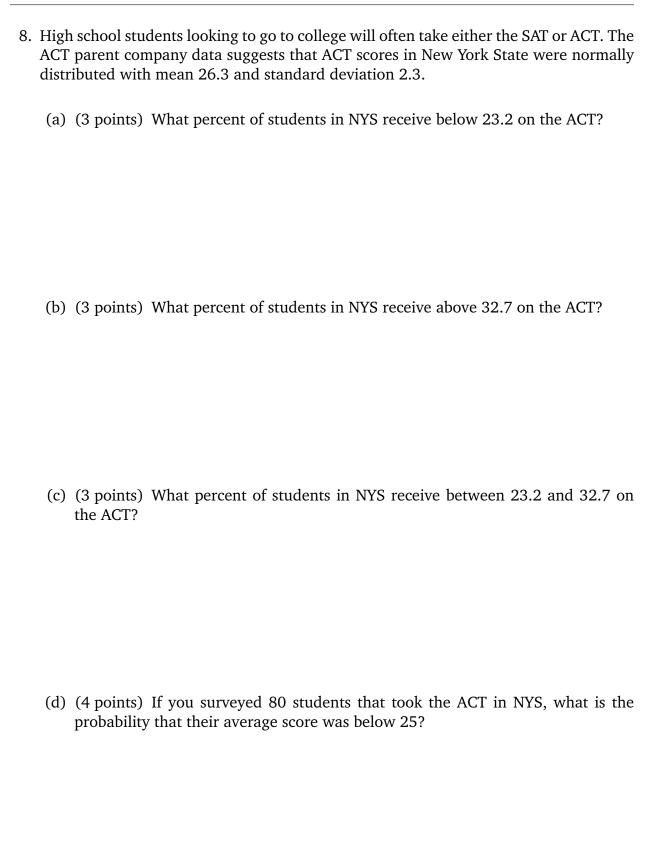
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7. "Step right up," yells a clown at a carnival. "Try your luck and see if fortune favors you today!" You walk up to the booth. The clown explains that you can pay \$1 to try your luck at a dice rolling game. If you roll either a one, two, three, or four, you win nothing. If you roll a five, you receive \$0.50. However, if you roll a six, then you win \$5.

(a) (7 points) Compute the amount, on average, you can expect to win playing this game.

(b) (3 points) In the long run, should you play this game? Explain your reasoning using your computation in (a).

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9.	There are a plethora of quick dining options in the United States. A recent survey approximates that 1 in 5 people have been to a Sonic drive-in. Suppose that ten people are randomly surveyed.					
	(a)	(3 points) before?	What is the probability that exactly three of them had been to a Sonic			
	(b)	(3 points) before?	What is the probability that less than four of them had been to a Sonic			
	(c)	(3 points) before?	What is the probability that at least one of them had been to a sonic			
	(d)	imate the p	Using the normal approximation to the binomial distribution, approxorobability that if 300 people were surveyed that less than fifty of them to a Sonic before?			