

MAT 101: Exam 1
Winter – 2021
01/07/2021
85 Minutes

Name: _____

Write your name on the appropriate line on the exam cover sheet. This exam contains 14 pages (including this cover page) and 15 questions. Check that you have every page of the exam. Answer the questions in the spaces provided on the question sheets. Be sure to answer every part of each question and show all your work.

Question	Points	Score
1	6	
2	6	
3	8	
4	8	
5	8	
6	6	
7	6	
8	6	
9	6	
10	6	
11	6	
12	6	
13	6	
14	6	
15	10	
Total:	100	

1. (6 points) Showing all your work, compute the following:

(a) $84 + 84 - 16 \cdot 0 + 12$

(b) $12/6 - 3(4 - 6)^3$

(c) $6 + 10/5 \cdot 2 - 7$

2. (6 points) Find the prime factorization of each of the following integers:

(a) 120

(b) 17

(c) 51

3. (8 points) Find the following:

(a) $\gcd(10, 15)$

(b) $\text{lcm}(10, 15)$

(c) $\gcd(2^3 \cdot 3^2 \cdot 5, 2^2 \cdot 3 \cdot 7)$

(d) $\text{lcm}(2^3 \cdot 3^2 \cdot 5, 2^2 \cdot 3 \cdot 7)$

4. (8 points) Showing all your work and being sure to simplify as much as possible, compute the following:

(a) $\frac{5}{6} - \frac{3}{8}$

(b) $\frac{3}{5} - \frac{7}{2}$

(c) $\frac{10}{18} \cdot \frac{6}{25}$

(d) $\frac{\frac{14}{15}}{\frac{21}{10}}$

5. (8 points) Simplify the following as much as possible, being sure to have no negative exponents in your expression:

(a) $\frac{x^3 y^3 z}{xy^6 z^{-2}}$

(b) $\left(\frac{(xy^2)^3}{x^5 y} \right)^{-1}$

(c) $\left(\frac{x^{-2}}{y^{-3}} \right)^5$

(d) $\frac{15x^{-3}y^2}{5xy}$

6. (6 points) Simplify the following as much as possible:

(a) $\sqrt{45}$

(b) $\sqrt[3]{24}$

(c) $\sqrt[4]{2^8 \cdot 3^9 \cdot 5^4 \cdot 7}$

7. (6 points) Convert the following numbers from scientific to decimal notation:

(a) $1.5 \cdot 10^0$

(b) $4.35 \cdot 10^{-3}$

(c) $6.7 \cdot 10^5$

8. (6 points) Convert the following numbers from decimal to scientific notation:

(a) 0.0004

(b) 5.4

(c) 1540000

9. (6 points) Convert $0.181818\overline{18}$ from a decimal to a fraction.

10. (6 points) Showing all your work, compute the following:

(a) 35% of 68

(b) 50% of 19.4

(c) 131% of 46

11. (6 points) Showing all your work, compute the following:

(a) 650 increased by 40%

(b) 84 decreased by 45%

(c) 93 increased by 160%

12. (6 points) A gas pump takes 1.6 minutes to pump 12 gallons of gas. Assuming the rate at which the pump works remains constant, find how long it will take to pump 26 gallons of gas.

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13. (6 points) Convert 23 gallons per square foot to liters per square inches. [1 gallon = 3.79 liters; 12 inches = 1 foot.]

14. (6 points) Suppose you invest \$970 in an account which earns 5% annual interest compounded monthly. Find the amount of money in the account after 6 years. Be sure to give the formula for the interest at time t and to show all your work.

15. (10 points) Suppose $f(x)$ and $g(x)$ are functions whose values are given in the table below.

x	-4	-1	0	1	3	5
$f(x)$	0	4	8	-1	7	4
$g(x)$	-2	-6	-3	7	2	3

Compute the following:

(a) $g(1)$

(b) $(f + g)(-1)$

(c) $(fg)(5)$

(d) $(f \circ g)(5)$

(e) $(g \circ f)(1)$