Name:	
MATH 308	"Some mathematicians feel that combinatorial analysis is not a branch of mathematics but rather a collection of clever but unrelated tricks."
Fall 2022 HW 17: Due 12/06	
11W 17. Due 12/00	– Frank Harary

**Problem 1.** (10pt) Suppose there are 8 appetizers, 15 entrées, and 6 desserts available at a restaurant. Using the multiplication principle or the addition principle, answer the following:

- (a) How many ways can you order either an appetizer, entrées, or dessert? [Ans: 29]
- (b) How many ways can you order a meal, i.e. appetizer, entrées, and dessert. [Ans: 720]
- (c) How many ways can you order either an appetizer and an entrée, or an appetizer and a dessert? [Ans: 168]

**Problem 2.** (10pt) Using the theory of permutations, showing all your work, and fully justifying your reasoning, compute the following:

- (a) The number of possible ways 15 people can finish a race, assuming that ties are not possible. [Ans: 1,307,674,368,000]
- (b) The number of possible president, vice president, secretary, and treasurer that can be elected from 486 people, assuming no individual can hold more than one role. [Ans: 55,102,398,120]
- (c) The number of possible passwords using 12 characters, assuming a character can be a digit or uppercase/lowercase letter. [Ans: 3,226,266,762,397,899,821,056]
- (d) The number of distinct possible arrangements of the letters of the word 'syzygy.' [Ans: 120]

**Problem 3.** (10pt) Using the theory of combinations, showing all your work, and fully justifying your reasoning, compute the following:

- (a) How many ways are there to choose a committee of 6 people from a collection of 20 people? [Ans: 38,760]
- (b) How many 6 card hands can be dealt from a deck of 52 cards? [Ans: 20,358,520]
- (c) How many ways are there to select any four bills from a jar containing a large number of \$1, \$5, \$10, \$20, \$50, and \$100 bills? [Ans: 70]
- (d) How many nonnegative solutions  $(x_1, x_2, x_3, x_4, x_5)$  are there to the equation  $x_1 + x_2 + x_3 + x_4 + x_5 = 100$ ? [Ans: 4,598,126]

**Problem 4.** (10pt) Showing all your work and fully justifying your reasoning, answer the following:

- (a) How many ways can the word 'frustrating' be arranged so that there are 4 letters between the 'u" and 'g'? [Ans: 1,088,640]
- (b) How many ways can you choose a committee of 10 people with a designated representative for the committee from a collection of 50 people? [Ans: 102,722,781,700]
- (c) If 50 people are broken up into groups by assigning to them to 4 rooms with 35 seats each, does one of the rooms have to have at least 13 people? Does one of the rooms have to have at least 23 empty seats?
- (d) If you have a jury pool consisting of 14 men and 16 women, how many juries can be formed consisting of 5 men and 7 women? [Ans: 22,902,880]