Quiz 1. True/False: Both $12 = 3 \cdot 4$ and $12 = 2^2 \cdot 3$ are prime factorizations of 12.

Solution. The statement is *false*. A factorization of an integer n is a product of integers that yields n. For instance, if n=100, then $n=1\cdot 100, 10\cdot 10, 5\cdot 20, \ldots$ are all factorizations of 100. A prime factorization is a factorization where all the numbers in the product are primes or powers of primes. [If n is prime, we allow n=n to be the prime factorization, i.e. the 'empty' product.] Then in the instance of n=100, the factorizations $5\cdot 20$ cannot be a prime factorization because 20 is not prime. In the given problem, $12=3\cdot 4$ is *not* a prime factorization because 4 is not prime $(4=2\cdot 2)$, while $12=2^2\cdot 3$ is a prime factorization because we have written 12 as a product of (powers of) primes. By the Fundamental Theorem of Arithmetic, every integer greater than 1 is either prime or can be written uniquely (up to order, e.g. $6=2\cdot 3=3\cdot 2$) as a product of primes.

Quiz 2. True/False:
$$gcd(2^{50} \cdot 3^{60} \cdot 7^{40}, 2^{30} \cdot 3^{70} \cdot 5^{90}) = 2^{30} \cdot 3^{60} \cdot 5^{90} \cdot 7^{40}$$

Solution. The statement is *false*. If one wishes to compute $\gcd(a,b)$, one can compute the prime factorizations of a,b and find the product of the primes appearing in *both* prime factorizations of a,b, each to the smaller of the prime powers involved in the factorizations of a,b. For instance, if we wanted to compute $\gcd(2520,74844) = \gcd(2^3 \cdot 3^2 \cdot 5^1 \cdot 7, 2^2 \cdot 3^5 \cdot 7 \cdot 11)$, observe that the primes occurring both are 2,3,7. The smallest power for each is 2,2,1, respectively. Therefore, $\gcd(2520,74844) = \gcd(2^3 \cdot 3^2 \cdot 5^1 \cdot 7, 2^2 \cdot 3^5 \cdot 7 \cdot 11) = 2^2 \cdot 3^2 \cdot 7^1 = 252$. In the given problem, while the smallest power of each prime was chosen, *every* prime was used rather than just the primes both factorizations have in common.

Quiz 3. True/False: We compute the reduced result of (3/7)/(45/56) as follows:

$$\frac{\frac{3}{7}}{\frac{45}{56}} = \frac{3}{7} \cdot \frac{56}{45} = \frac{3 \cdot 56}{7 \cdot 45} = \frac{168}{315}$$

Solution. The statement is *false*. While the given answer is equal to the reduced answer, the given answer is not reduced (for instance, the numerator and denominator are both divisible by 3). Therefore, the statement is false. Remember, one should always cancel wherever possible *before* 'multiplying straight across' in multiplication of rational numbers:

$$\frac{\frac{3}{7}}{\frac{45}{56}} = \frac{3}{7} \cdot \frac{56}{45} = \frac{3^{1}}{7^{1}} \cdot \frac{56^{8}}{\cancel{45}^{15}} = \frac{1}{1} \cdot \frac{8}{15} = \frac{1 \cdot 8}{1 \cdot 15} = \frac{8}{15}$$

Quiz 4. *True/False*:

$$\frac{xy^4z^3}{z^{-3}\sqrt{x^2y^4}} = \frac{1}{\sqrt{x}}$$

Solution. The statement is *false*. We can simplify this expression as follows:

$$\frac{xy^4z^3}{z^{-3}\sqrt{x^2y^4}} = \frac{xy^4z^3}{z^{-3}(x^{2/2}y^{4/2})} = \frac{xy^4z^3}{z^{-3}xy^2} = \frac{xy^4z^3z^3}{xy^2} = \frac{y^4z^6}{y^2} = y^2z^6$$

Quiz 5. True/False: To compute 560 increased by 160%, one computes 560(2.60) = 1456.

Solution. The statement is *true*. To compute a percentage increase/decrease of a number N, we compute $N(1 \pm \%_d)$, where N is the number, $\%_d$ is the percentage written as a decimal, and where we choose '+' if it is a percentage increase and '-' if it is a percentage decrease. So here, we compute...

$$N(1 \pm \%_d) = 560(1 + 1.60) = 560(2.60) = 1456$$

Quiz 6. *True/False*: Suppose a course has three exams: two prelims and a final exam. The final exam is worth twice as much as any of the other exams. If a student receives an 85%, 89%, and 81% on the prelims and final exam, respectively, then their exam average is $85\% \left(\frac{1}{4}\right) + 89\% \left(\frac{1}{4}\right) + 81\% \left(\frac{1}{2}\right) = 84\%$.

Solution. The statement is *true*. We know that the weighted average is \sum value · weight. If the first exam is worth 1 part of the exam grade, the second must be worth 1 part and the final exam must be worth 2 parts (because it needs to be worth twice as much as either of the other two). Then the exam grade is split into 1 + 1 + 2 = 4 parts, which the first exam worth 1/4 th of the grade, the second worth 1/4 th of the grade, and the last worth 2/4 = 1/2 the grade. But then we have...

$$\sum \text{value} \cdot \text{weight} = 85\% \cdot \frac{1}{4} + 89\% \cdot \frac{1}{4} + 81\% \cdot \frac{1}{2} = 21.25\% + 22.25\% + 40.5\% = 84\%$$

Quiz 7. True/False: The acceleration towards Earth due to gravitational attraction is approximately 9.8 m/s². To convert this to feet per hour, you need to multiply 9.8 m/s² by $60^2/0.3048 \approx 11811.0236$. [1 ft = 0.3048 m]

Solution. The statement is *false*. To perform the conversion, we have...

which gives us...

$$9.8 \cdot 60 \cdot 60 \cdot 60 \cdot 60 / 0.3048 = 9.8 \cdot 60^4 / 0.3048 \; \text{ft/hr}^2 \approx 16692913.38 \; \text{ft/hr}^2$$

So we need multiply by $60^4/0.3048$, not $60^2/0.3048$. The given computation only converts one units of seconds to hours, leaving one unit of seconds unconverted. Therefore, the given answer is really $9.8 \text{ m/s}^2 \cdot 60^2/0.3048 \approx 11811.0236 \text{ ft/(s} \cdot \text{hr)}$.