

Quiz 1. *True/False:* The following is a truth table for $P \rightarrow Q$:

P	Q	$P \rightarrow Q$
T	T	T
T	F	F
F	T	F
F	F	F

Solution. The statement is *false*. The correct truth table should be...

P	Q	$P \rightarrow Q$
T	T	T
T	F	F
F	T	T
F	F	T

One way to think about this is as follows: imagine P is a guarantee. Namely, we promise that if P happens, Q must happen. For instance, P could represent the statement, “You do not tamper with your hardware,” and Q could be the statement, “I will replace your broken computer.” So $P \rightarrow Q$ is then the statement, “If you do not tamper with your hardware, then I will replace your broken computer.” If both P and Q are true, then this should be true—because I promised to replace the computer if you left it alone. If P is true and Q is false, then the statement should be false because I broke my promise. However, my promise holds true whenever P is false. Why? Because you broke our agreement by tampering with the hardware. So while I may or may not replace the computer, my promise has not been broken in either case, i.e. it remains true. In an implication $P \rightarrow Q$, if P is false, then the statement $P \rightarrow Q$ is *always* true.