**Problem 1.** (10pt) Let  $A=\{2,6,8,10\}$ , B be the set of nonnegative even numbers that are at most 10, and C be the set of perfect squares less than 10. Define  $f:A\to\mathbb{Z}$  and  $g:B\setminus C\to\mathbb{Z}$  via  $x\to \frac{15(x+8)}{x}$  and  $x\mapsto \frac{5(x^2-16x+88)}{4}$ , respectfully. Fully justifying your answer, determine whether  $f\equiv g$ .

**Problem 2.** (10pt) Define the following real-valued functions:

$$f(x) = 2x - 1$$
  $j(x) = \frac{x - 1}{x + 2}$   
 $g(x) = x^2 + x + 1$   $k(x) = \sin(\pi x)$   
 $h(x) = x2^x$   $\ell(x) = 1 - x^2$ 

Showing all your work, for each of the following, either compute the function at the specified value or find a general rule for the given function operation:

- (a) (f+g)(0)
- (b)  $(j \ell)(2)$
- (c) (gk)(5)
- (d)  $\left(\frac{f}{j}\right)$  (3)
- (e)  $(h \circ k)(1)$
- (f)  $(2f + \ell)(x)$
- (g) (fg)(x)
- (h)  $\left(\frac{h}{f}\right)(x)$
- (i)  $(k \circ \ell)(x)$
- (j)  $(\ell \circ g \circ f)(x)$

**Problem 3.** (10pt) Let  $f: \mathbb{R} \to \mathbb{R}$  be given by  $x \mapsto x^2 + 4x - 5$ .

- (a) Determine f(-5).
- (b) Compute f([0,1]).
- (c) Is  $16 \in \operatorname{im} f$ ? Explain.
- (d) Determine  $f^{-1}(0)$ .
- (e) Find the domain, codomain, and range for f(x).

**Problem 4.** (10pt) Being sure to justify your answer, complete the following:

- (a) Let  $f: \mathbb{R} \to \mathbb{R}$  be given by  $f(x) = 5 x^2$ . Is f an increasing function? Explain. Is f a decreasing function? Explain.
- (b) Let  $g: \mathbb{R} \to \mathbb{R}$  be given by g(x) = 5x 8. Is g a positive function? Explain. Is g a negative function? Explain.
- (c) Let g be as in (b) and define  $A=[2,\infty)$  and  $B=(-\infty,0)$ . Is  $g\big|_A$  a positive function? Explain. Is  $g\big|_B$  a negative function? Explain.
- (d) Let  $h: \mathbb{R} \to \mathbb{R}$  be given by...

$$h(x) = \begin{cases} 1 - x, & x < 2\\ 3x + 5, & x \ge 2 \end{cases}$$

Find the largest possible interval  $S\subseteq\mathbb{R}$  such that  $h|_S$  is a nondecreasing function. Is h monotone on S? Is h strictly monotone on S?