

MAT 101: Exam 1
Spring — 2024
02/21/2024
85 Minutes

Name: _____

Write your name on the appropriate line on the exam cover sheet. This exam contains 11 pages (including this cover page) and 10 questions. Check that you have every page of the exam. Answer the questions in the spaces provided on the question sheets. Be sure to answer every part of each question and show all your work. If you run out of room for an answer, continue on the back of the page — being sure to indicate the problem number.

Question	Points	Score
1	10	
2	10	
3	10	
4	10	
5	10	
6	10	
7	10	
8	10	
9	10	
10	10	
Total:	100	

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1. (10 points) The prime factorization of 852 is $2^2 \cdot 3 \cdot 71$. Freely making use of this fact, complete the following:
- (a) Find the prime factorization of 954.
 - (b) Compute $\gcd(852, 954)$.
 - (c) Compute $\text{lcm}(852, 954)$.

2. (10 points) Showing all your work and simplifying as much as possible, compute the following:

(a) $\frac{2}{3} - \frac{8}{6} + \frac{12}{5}$

(b) $\frac{\frac{20}{21}}{\frac{55}{18}}$

3. (10 points) Showing all your work, simplify the following as much as possible:

$$\frac{(x^3 y^{-3})^3 x^2 y^0}{x^{-3} (y^2)^4}$$

4. (10 points) Showing all your work, simplify the following as much as possible:

$$x^4 y^3 \sqrt[4]{\frac{x^4 y^{-9}}{x^2 y^3}}$$

5. (10 points) Showing all your work, compute the following:

(a) $(15 + 7i) - (14 - 8i)$

(b) $(3 + 9i)(13 - 2i)$

6. (10 points) Showing all your work, compute the following:

(a) 6% of 984

(b) 560 increased by 47%

(c) 0.22 decreased by 22%

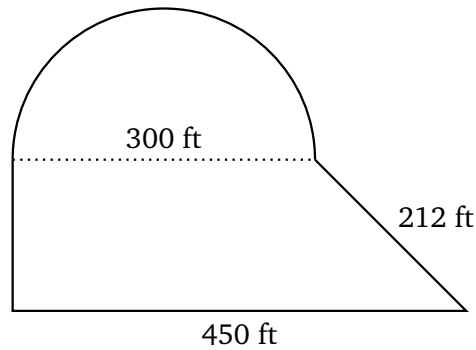
7. (10 points) Below are the grades for a student as well as the course grade components and weights. Noting that the last exam has not occurred, find the student's current course average.

Grade Component	Component Value	Student's Grade
Quizzes	15%	61%
Homework	25%	75%
Exam 1	10%	80%
Exam 2	20%	52%
Exam 3	30%	N/A

8. (10 points) Suppose your overall GPA last semester was 3.433 based on a total of 49 credits. If you expect to receive a GPA this semester of 2.765 based on 16 credits, what would your overall GPA be then?

9. (10 points) You are converting the cost of land in a certain region in the US for a European buyer. If the land cost \$85,000 per acre, what is this in Euros per square kilometer? [$\$1.08 = \text{€}1$; $1 \text{ acre} = 43,560 \text{ sq. ft}$; $1 \text{ m}^2 = 10.7638 \text{ ft}^2$]

10. (10 points) Surveillance satellites have taken images of a newly constructed building. The arial view of the roof and its dimensions are shown below.



- (a) Assuming the 'upper' portion of this region is a semicircle, find the area of the roof of this building.
- (b) Assuming the outer walls are perfectly perpendicular with the ground from top to bottom and that the building is 77 ft tall, find the volume of the building.