Quiz 1. *True/False*: The number 1 is prime.

Solution. The statement is *false*. A prime number is an integer greater than 1 that can only be factored as the product of one and itself. So for example, the integer 11 is prime because we can only factor 11 as $11 = 1 \cdot 11$. However, the integer 12 is not prime because we can write $12 = 2 \cdot 6$, neither of which are 1 or 12.

Quiz 2. *True/False*: $gcd(2^3 \cdot 3 \cdot 5, 2 \cdot 3^2 \cdot 7) = 2^3 \cdot 3^2 \cdot 5 \cdot 7$.

Solution. The statement is *false*. Remember given a prime factorization of the numbers, we find the gcd by choosing the *smallest* powers of each prime that appears in the factorizations. So we should have $gcd(2^3 \cdot 3 \cdot 5, 2 \cdot 3^2 \cdot 7) = 2 \cdot 3$. Instead, the largest power of each prime that appears in the factorizations was chosen which is how we compute the lcm. Therefore, we have $lcm(2^3 \cdot 3 \cdot 5, 2 \cdot 3^2 \cdot 7) = 2^3 \cdot 3^2 \cdot 5 \cdot 7$.

Quiz 3. True/False: $\sqrt[3]{2^8 \cdot 3^3 \cdot 5^1 \cdot 7^5} = 2^2 \cdot 3^1 \cdot 7\sqrt[3]{2^2 \cdot 5^1 \cdot 7^2}$

Solution. The statement is *true*. There are two ways to think about this. First, we should write out the numbers and group them into threes and pull out/leave the terms appropriately:

Alternatively, we can use division. We know that 8/3 is 2 with remainder 2, 3/3 is 1 with remainder 0, 1/3 is 0 with remainder 1, and 5/3 is 1 with remainder 2. So we can pull out two 3's with 2 remaining, one 3 with 0 remaining, no 5's with 1 remaining, and two 7's with 2 remaining, which gives:

 $\sqrt[3]{2^8 \cdot 3^3 \cdot 5^1 \cdot 7^5} = 2^2 \cdot 3^1 \cdot 7\sqrt[3]{2^2 \cdot 5^1 \cdot 7^2}$

Quiz 4. *True/False*: 68 increased by 119% is 68(1.19).

Solution. The statement is *false*. To find 119% of 68, we would multiply 68 by the percent written as a decimal. This would be 68(1.19). However, to increase or decrease a number by a percentage, we compute the number $\#(1\pm\%)$, where we add if we are increasing, subtract if we are decreasing, # is the number, and % is the percentage written as a decimal. So to increase 68 by 119%, we need to compute 68(1+1.19)=68(2.19).

Quiz 5. *True/False*: If f(x) = 3x + 5 and g(x) = 1 - 2x, then $(f \circ g)(1) = 8$.

Solution. The statement is *false*. Recall that $(f \circ g)(1) = f(g(1))$. First, we compute g(1): g(1) = 1 - 2(1) = 1 - 2 = -1. Then we need to compute f(g(1)) = f(-1). We have f(-1) = 3(-1) + 5 = -3 + 5 = 2.

Quiz 6. True/False: The point (1, -3) is on the graph of f(x) = x - 3.

Solution. The statement is *false*. We have the point (x, y) = (1, -3). If this point is on the graph of f(x), then these x and y satisfy the equation for f(x). We can check this:

$$f(x) = x - 3$$
$$-3 = 1 - 3$$
$$-3 \neq -2$$

Therefore, the point (1, -3) is not on the graph of f(x). Alternatively, if x = 1, then the corresponding point on the graph of f(x) would have y-value f(1) = 1 - 3 = -2. Then the point (1, -2) is on the graph of f(x). But then (1, -3) is not on the graph of f(x).

Quiz 7. True/False: The graph of the solutions to 2x - 6y = 9 is a line.

Solution. The statement is *true*. The graph of the set of solutions to an equation of the form Ax + By = C is a line. Here we have A = 2, B = -6, and C = 9. Notice also we can solve for y:

$$2x - 6y = 9$$

$$-6y = -2x + 9$$

$$y = \frac{-2}{-6}x + \frac{9}{-6}$$

$$y = \frac{1}{3}x - \frac{3}{2}$$

The function $f(x) = \frac{1}{3}x - \frac{3}{2}$ is a linear function, whose graph must be a line.

Quiz 8. True/False: The line through (-1,5) with slope 3 is y=3x+8.

Solution. The statement is *true*. We know that the line contains the (-1,5) and has slope 3, i.e. m=3. Then we have

$$y = mx + b$$

$$y = 3x + b$$

$$5 = 3(-1) + b$$

$$5 = -3 + b$$

$$b = 8$$

Therefore, the equation of the line is y = 3x + 8.

Quiz 9. *True/False*: A function cannot have two *y*-intercepts.

Solution. The statement is *true*. If a function had two y-intercepts, then there would be two points on the graph of the function on the y-axis. But then the function would fail the vertical line test—which is impossible because it is a function.

Quiz 10. True/False: 47 increased by 16% is 47(0.16).

Solution. The statement is *false*. There are two ways to do this: first, we can use the percent increase/decrease formula; that is, if we want to increase/decrease a number by a percentage, we use the formula $\#(1\pm\%)$, where # is the number, % is the percentage written as a decimal, and we choose + if we are increasing the number and - if we are decreasing the number. So in our case, we have 47(1+0.16)=47(1.16). The other method is to find the amount of increase/decrease and then add/subtract this to our original number, respectively. We want to find 16% of 47, which is 47(0.16). Then we increase, i.e. add, this to our original number, so we have 47+47(0.16)=47(1.16).

Quiz 11. True/False: The vertex of the quadratic function $y = (x+2)^2 - 3$ is the point (2, -3).

Solution. The statement is *false*. The x-coordinate of the vertex is the x-value that makes the square term zero. In this case, x=-2 would make $(x+2)^2$ zero. Then we would be left with y=-3, which is the y-coordinate of the vertex. Therefore, the vertex is (-2,-3). Alternatively, the 'proper' vertex form of a quadratic function is y=A(x-B)+C. The vertex is (B,C). Writing the 'proper' vertex form of the quadratic function $y=(x+2)^2-3$, we have $y=(x--2)^2+(-3)$. Therefore, the vertex form is (-2,-3). Finally, one could expand this out: $y=(x+2)^2-3=(x^2+4x+4)-3=x^2+4x+1$. The x-coordinate of the vertex is $x=\frac{-b}{2a}=\frac{-4}{2(1)}=-2$. Then the y-coordinate of the vertex is $y(-2)=(-2)^2+4(-2)+1=4-8+1=-3$. Therefore, the vertex is (-2,-3).

Quiz 12. True/False: $x^2 - 4x - 5 = (x+1)(x-5)$

Solution. The statement is true. One way of seeing this would be to expand (x+1)(x-5),

$$(x+1)(x-5) = x^2 - 5x + x - 5 = x^2 - 4x - 5.$$

Alternatively, we can factor the polynomial $x^2 - 4x - 5$. First, we find the factors of 5, which are only 1, 5. Because the 5 is negative, the factors must have opposite signs.

$$1, -5: -4$$

 $-1, 5: 4$

We want these signed factors to add to -4. Therefore, we want 'factors' 1, -5. Therefore,

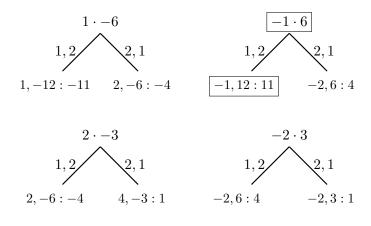
$$x^2 - 4x - 5 = (x+1)(x-5)$$

Quiz 13. True/False: $2x^2 + 11x - 6 = (2x - 1)(x + 6)$

Solution. The statement is *true*. There are two approaches: first, we can simply expand the right side and show that this is equal to the left side,

$$(2x-1)(x+6) = 2x^2 + 12x - x - 6 = 2x^2 + 11x - 6$$

Alternatively, we can factor the polynomial on the left side and show that it is the same as the given factorization of the right side,



Therefore,

$$2x^2 + 11x - 6 = (2x - 1)(x + 6)$$

Quiz 14. True/False: The vertical asymptotes of
$$f(x) = \frac{(x-1)(x+3)}{(x-1)(x+5)}$$
 are $x=1$ and $x=-5$.

Solution. The statement is *false*. We first find the domain. The domain of a rational function is where the denominator is not 0. The denominator is 0 if (x-1)(x+5)=0. But then x-1=0, i.e. x=1, or x+5=0, i.e. x=-5. Therefore, the domain is all real numbers such that $x\neq -5, 1$. We can then cancel any common factors in the numerator and denominator. Then

$$\frac{(x-1)(x+3)}{(x-1)(x+5)} = \frac{\cancel{(x-1)}(x+3)}{\cancel{(x-1)}(x+5)} = \frac{x+3}{x+5}$$

The vertical asymptotes are then the values where the denominator vanishes in this reduced function. But then x + 5 = 0, i.e. x = -5. Therefore, the only vertical asymptote is x = -5.

Quiz 15. True/False: To add $\frac{5}{x+1}$ and $\frac{x}{(x+1)^2}$, one would use the common denominator of x+1.

Solution. The statement is *false*. The common denominator should be the least common multiple of the two denominators. The first expression has a single factor of x + 1, whereas the second expression has two factors of x + 1. Therefore, the least common denominator would be $(x + 1)^2$.

Quiz 16. *True/False*: There is no function with domain all reals and a vertical asymptote at x = 1.

Solution. The statement is *true*. Any x-value which corresponds to a vertical asymptote cannot be in the domain of the function. So if x=1 were a vertical asymptote, then x=1 is not in the domain for the function. But then the domain cannot be all real numbers.