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MATH 111-I

Spring 2025

Quiz 6

Problem 1: Showing all your work, factor the following:

(a) $2x^2 + 4x - 48$

(b) $4x^2 - 25$

(c) $2x^2 - 5x - 3$

(a) First, observe that we can factor out 2: $2x^2 + 4x - 48 = 2(x^2 + 2x - 24)$. We need to find factors of -24 that add to 2. Therefore, we have...

	<u>-24</u>	
$1 \cdot -24$		-23
$-1 \cdot 24$		23
$2 \cdot -12$		-10
$-2 \cdot 12$		10
$3 \cdot -8$		-5
$-3 \cdot 8$		5
$4 \cdot -6$		-2
<u>$-4 \cdot 6$</u>		<u>2</u>

$$2x^2 + 4x - 48 = 2(x^2 + 2x - 24) = 2(x - 4)(x + 6)$$

(b) This is a difference of perfect squares: $a^2 - b^2 = (a - b)(a + b)$. We have $a = 2x$, so that $a^2 = (2x)^2 = 4x^2$, and $b = 5$, so that $b^2 = 25$. But then...

$$4x^2 - 25 = (2x - 5)(2x + 5)$$

(c) We find that $ac = 2 \cdot -3 = -6$. We need to find factors of -6 that add to $b = -5$. But then...

	<u>-6</u>	
<u>$1 \cdot -6$</u>		<u>-5</u>
$-1 \cdot 6$		5
$2 \cdot -3$		-1
$-2 \cdot 3$		1

$$2x^2 - 5x - 3 = 2x^2 + x - 6x - 3 = x(2x + 1) - 3(2x + 1) = (2x + 1)(x - 3)$$

Problem 2: Without explicitly attempting to factor $x^2 + 5x + 3$, explain why it cannot factor ‘nicely.’

We know that a quadratic function factors if and only if the discriminant is a perfect square. The discriminant of a quadratic function $ax^2 + bx + c$ is $D = b^2 - 4ac$. We know for $x^2 + 5x + 3$ that $D = 5^2 - 4(1)3 = 25 - 12 = 13$. But $\sqrt{13} \approx 3.60555$ is not a perfect square. Therefore, $x^2 + 5x + 3$ cannot factor ‘nicely.’