

MATH 141: Exam 1

Name: \_\_\_\_\_

Fall —, 2025

09/19/2025

50 Minutes

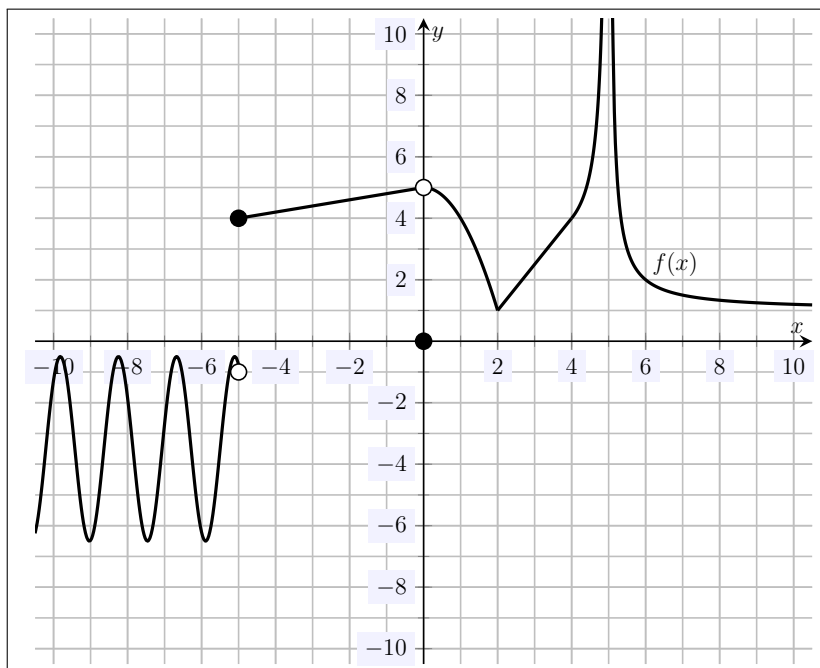
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Write your name on the appropriate line on the exam cover sheet. This exam contains 7 pages (including this cover page) and 5 questions. Check that you have every page of the exam. Answer the questions in the spaces provided on the question sheets. Be sure to answer every part of each question and show all your work. If you run out of room for an answer, continue on the back of the page — being sure to indicate the problem number. At no during the exam may you use l'Hôpital's rule. *Solutions which make use of l'Hôpital's rule will receive no credit.*

Question	Points	Score
1	20	
2	20	
3	20	
4	20	
5	20	
Total:	100	

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1. (20 points) Use the plot of the function  $f(x)$  shown below to answer the following questions—if a given limit does not exist, simply write ‘DNE’:



(a)  $\lim_{x \rightarrow -\infty} f(x) =$

(b)  $\lim_{x \rightarrow -5^-} f(x) =$

(c)  $\lim_{x \rightarrow -5^+} f(x) =$

(d)  $\lim_{x \rightarrow -5} f(x) =$

(e)  $\lim_{x \rightarrow 0^-} f(x) =$

(f)  $\lim_{x \rightarrow 0^+} f(x) =$

(g)  $\lim_{x \rightarrow 0} f(x) =$

(h)  $\lim_{x \rightarrow 5} f(x) =$

(i)  $\lim_{x \rightarrow \infty} f(x) =$

- (j) Give an  $x$ -value such that  $f(x)$  is continuous but not differentiable at  $x$ .

2. (20 points) Showing all your work, compute the limits below. You may *not* use l'Hôpital's to compute any limits.

(a)  $\lim_{x \rightarrow 2^+} \frac{x - 4}{x - 2}$

(b)  $\lim_{n \rightarrow \infty} \frac{10n^2 + 3n - 5}{7 - n^2}$

(c)  $\lim_{x \rightarrow \infty} \left(1 + \frac{3}{x}\right)^{2x}$

(d)  $\lim_{h \rightarrow 0} \frac{2 - \sqrt{h+4}}{h}$

3. (20 points) Let  $f(x)$  be the piecewise function given below.

$$f(x) = \begin{cases} x + 1, & x < 1 \\ 2x - 3, & x \geq 1 \end{cases}$$

(a) Find  $f(1)$ .

(b) Completely justifying your answer, compute  $\lim_{x \rightarrow 1} f(x)$ .

(c) Explain why  $f(x)$  is not continuous at  $x = 1$ . Justify your answer in terms of the definition of continuity.

(d) Classify the type of discontinuity  $f(x)$  has at  $x = 1$ . Be sure to justify your answer.

4. (20 points) Use the definition of the derivative to find  $f'(-3)$ , where  $f(x) = x^2 + 2x$ . *Do not* use the definition of the derivative to find  $f'(x)$  and then evaluate at  $x = -3$ . You will not receive any credit for using any derivative 'shortcut' rules, although you may check your answer with them. You may *not* use l'Hôpital's to compute any limits.

5. (20 points) Showing all your work, compute the following but *do not simplify your results*:

(a)  $\frac{d}{dx} \left( \sqrt[7]{x^9} + \frac{1}{x^4} + 9^x + \arcsin(x) \right)$

(b)  $\frac{d}{dx} (\cos^3(5x))$

(c)  $\frac{d}{dx} (e^x \cot(x) \ln(x))$

(d)  $\frac{d}{dx} \left( \frac{\sec x}{3x - x^2} \right)$