

**Check-In 01/14.** (*True/False*) The vector  $\mathbf{u} = \langle 2, -1, 0 \rangle$  is a unit vector.

**Solution.** The statement is *false*. We know a unit vector has length 1. We know if  $\mathbf{v} = \langle x_1, x_2, \dots, x_n \rangle$ , then  $\|\mathbf{v}\| = \sqrt{x_1^2 + x_2^2 + \dots + x_n^2}$ . But then  $\|\mathbf{u}\| = \|\langle 2, -1, 0 \rangle\| = \sqrt{2^2 + (-1)^2 + 0^2} = \sqrt{4 + 1 + 0} = \sqrt{5} \neq 1$ . Therefore,  $\mathbf{u}$  is not a unit vector.

**Check-In 01/16.** (*True/False*) Suppose that  $\mathbf{u}, \mathbf{v} \in \mathbb{R}^n$ . If  $\mathbf{u} \cdot \mathbf{v} = 0$ , then either  $\mathbf{u} = \mathbf{0}$  or  $\mathbf{v} = \mathbf{0}$ . Furthermore,  $\mathbf{u} \perp \mathbf{v}$ .

**Solution.** The statement is *false*. If  $\mathbf{u} \cdot \mathbf{v} = 0$ , it is true that  $\mathbf{u}$  and  $\mathbf{v}$  are perpendicular (so long as neither of them are nonzero). Furthermore, if  $\mathbf{u}$  and  $\mathbf{v}$  are perpendicular, then  $\mathbf{u} \cdot \mathbf{v} = 0$ . However, if  $\mathbf{u} \cdot \mathbf{v} = 0$ , it need not be the case that  $\mathbf{u}$  and  $\mathbf{v}$  are zero. For instance, if  $\mathbf{u} = \langle 1, 0, \dots, 0 \rangle$  and  $\mathbf{v} = \langle 0, 1, 0, \dots, 0 \rangle$ , then  $\mathbf{u} \cdot \mathbf{v} = 1(0) + 0(1) + 0(0) + \dots + 0(0) = 0$  but neither  $\mathbf{u}$  nor  $\mathbf{v}$  are zero. Furthermore, it is impossible that  $\mathbf{u} = \mathbf{0}$  or  $\mathbf{v} = \mathbf{0}$ . Both  $\mathbf{u}, \mathbf{v}$  are *vectors* while 0 is a scalar.