

CP-Reference

Contents

1	Template	4
2	Data Structures	4
2.1	Centroid Decomposition	4
2.2	DSU	6
2.3	EERTREE	7
2.4	Fenwick 2d	10
2.5	Fenwick	10
2.6	LCA o1 minimal	11
2.7	LCA	11
2.8	Mo (Saad)	12
2.9	Mo Algorithm	13
2.10	Mo on trees	14
2.11	MonoQueue Anas	17
2.12	MonoQueue	18
2.13	Ordered Set	19
2.14	Saad HLD	19
2.15	Sack	22
2.16	SparseTable	23
2.17	Sqrt Decomposition	24
2.18	Treap	25
2.19	Two SAT	28
2.20	TwoSAT F	30
2.21	Segment Tree	31
2.21.1	Extended Segment Tree	31
2.21.2	KST Lazy	33
2.21.3	KST Simple	34
2.21.4	Persistent Basic	36
2.21.5	Persistent Segment Tree (Anas)	37
2.21.6	PST Kareem	37
2.21.7	PST Path Kareem	38
2.21.8	RST Lazy	40
2.21.9	RST simple	41
2.21.10	Segment Tree with lazy	42
2.21.11	SparseSegmentTree(setBinary-sum Range)	44
2.21.12	SparseSegmentTree(xor-sum Range)	46
3	Flows	47
3.1	Dinic Reda get min cut edges	47
3.2	Dinic Reda with scaling	47

3.3	Dinic Reda	49
3.4	Edmonds Karp	51
3.5	Hopcroft Karp	52
3.6	Hungarian	53
3.7	Max Bipartite Matching	55
3.8	MCMF	56
3.9	Push Relable	58
4	Geometry	60
4.1	Areas	60
4.2	Basic Funcs	60
4.3	ConvexHull	63
4.4	CosineRule	64
4.5	Defines 3D	64
4.6	Defines and Point all	65
4.7	Defines and Point simple	66
4.8	Helpers 3D	67
4.9	Intersections	69
4.10	Lattice Points	70
4.11	Polygon Centroid	70
4.12	some Properties of Regular polygons	70
5	Graph	71
5.1	Articulation Points Kareem	71
5.2	Articulation Points Reda	71
5.3	Bellmanford	72
5.4	Bridges Kareem	73
5.5	Bridges Reda	74
5.6	Euler tour	75
5.7	Tarjan SCC Reda	75
6	Math	76
6.1	Combinatorics	76
6.2	Equations	77
6.3	Fast Power	78
6.4	Gauss Xor	78
6.5	Gauss	80
6.6	Linear Diophantine Equation CRT	84
6.7	Lucus Theorem	84
6.8	Matrix power	85
6.9	MillerRabin	86
6.10	Mobius Function	87
6.11	NCR Preprocessing	88
6.12	Phi	88

6.13	Sieve w e5wato	89
6.14	SieveUpTo1e9	90
6.15	SumRangeDivisors	92
6.16	FFT w e5wato	92
6.16.1	FFT Iterative	92
6.16.2	FFT MOD	93
6.16.3	FFT string Matching	94
6.16.4	FFT	96
6.16.5	FWHT	97
6.16.6	NTT Time-Shift	98
6.16.7	NTT	101
7	Misc	102
7.1	Base Conversion	102
7.2	BuiltIn functions	103
7.3	CheckTime	104
7.4	CompareFunction for ds	104
7.5	DP digits	104
7.6	DP SOS Kareem	105
7.7	Generate All Submasks	106
7.8	Li-Chao	106
7.9	LIS Onlogn	107
7.10	misereNim	107
7.11	Next element	107
7.12	Random	109
7.13	Ternary search	109
7.14	VectorHasher	110
7.15	XOR basis Range	110
7.16	XOR basis	112
7.17	Xor from 1 to n	112
8	Problem codes	112
8.1	Lca Persistant code problem	112
8.2	Line Sweep Mostafa Saad	116
9	Strings	120
9.1	Aho Corasick	120
9.2	Anas Suffix Array	121
9.3	Hashing Kareem	123
9.4	Hashing	124
9.5	KMP	125
9.6	Manacher	126
9.7	Saad Trie	126
9.8	Suffix Automation	128

9.9	Trie 1d vector	130
9.10	Trie pointers	131
9.11	Z algorithm	131

1 Template

```
#include<bits/stdc++.h> //3alHady | ft. Reda , AbdoSa3d , Kareem
```

```
using namespace std;

#define all(v) v.begin(),v.end()
#define ll long long
#define endl "\n"

void solve()
{

}

signed
main()
{
    cin.tie(0)->sync_with_stdio(false);

    int t = 1;
    //cin >> t;
    while (t--)
        solve();

}
```

2 Data Structures

2.1 Centroid Decomposition

```
class centroid_decomposition {
    vector<bool> centroidMarked;
    vector<int> size;

    void dfsSize(int node, int par) {
        size[node] = 1;
        for (int ch : adj[node])
            if (ch != par && !centroidMarked[ch]) {
                dfsSize(ch, node);
                size[node] += size[ch];
            }
    }

    int getCenter(int node, int par, int size_of_tree) {
        for (int ch : adj[node]) {
            if (ch == par || centroidMarked[ch]) continue;
            if (size[ch] * 2 > size_of_tree) return getCenter(ch, node, size_of_tree);
        }
    }
}
```

```

    return node;
}

int getCentroid(int src) {
    dfsSize(src, -1);
    int centroid = getCenter(src, -1, size[src]);
    centroidMarked[centroid] = true;
    return centroid;
}

int decomposeTree(int root) {
    root = getCentroid(root);
    solve(root);
    for (int ch : adj[root]) {
        if (centroidMarked[ch]) continue;
        int centroid_of_subtree = decomposeTree(ch);
        // note: root and centroid_of_subtree probably not have a direct edge in
        // adj          // centroidTree[root].push_back(centroid_of_subtree);
        // centroidParent[centroid_of_subtree] = root;    }
    return root;
}

void calc(int node, int par) {
    // TO-DO
    for (int ch : adj[node])
        if (ch != par && !centroidMarked[ch]) calc(ch, node);
}

void add(int node, int par) {
    // TO-DO
    for (int ch : adj[node])
        if (ch != par && !centroidMarked[ch]) add(ch, node);
}

void remove(int node, int par) {
    // TO-DO
    for (int ch : adj[node])
        if (ch != par && !centroidMarked[ch]) remove(ch, node);
}

void solve(int root) {
    // add root
    for (int ch : adj[root])
        if (!centroidMarked[ch]) {
            calc(ch, root);
            add(ch, root);
        }
    // TO-DO //remove root
    for (int ch : adj[root])
        if (!centroidMarked[ch]) remove(ch, root);
}

public:

```

```

int n, root;
vector<vector<int>> adj, centroidTree;
vector<int> centroidParent;

centroid_decomposition(vector<vector<int>> &adj) : adj(adj) {
    n = (int)adj.size() - 1;
    size = vector<int>(n + 1);
    centroidTree = vector<vector<int>>(n + 1);
    centroidParent = vector<int>(n + 1, -1);
    centroidMarked = vector<bool>(n + 1);
    root = decomposeTree(1);
}
};

```

2.2 DSU

Minimal

```

struct DSU {
    std::vector<int> p;
    DSU(int n): p(n) { std::iota(p.begin(), p.end(), 0); }
    int find(int x) { return p[x]==x ? x : p[x]=find(p[x]); }
    void unite(int a, int b){ p[find(a)] = find(b); }
};

```

```

struct DSU {
    vector<int> rank, parent, size;
    vector<vector<int>> component;
    int forsets;

    DSU(int n) {
        size = rank = parent = vector<int>(n + 1, 1);
        component = vector<vector<int>>(n + 1);
        forsets = n;
        for (int i = 0; i <= n; i++) {
            parent[i] = i;
            component[i].push_back(i);
        }
    }

    int find_set(int v) {
        if (v == parent[v])
            return v;
        return parent[v] = find_set(parent[v]);
    }

    void link(int par, int node) {
        parent[node] = par;
        size[par] += size[node];
        for (const int &it: component[node])
            component[par].push_back(it);
        component[node].clear();
        if (rank[par] == rank[node])

```

```

        rank[par]++;
        forsets--;
    }

    bool union_sets(int v, int u) {
        v = find_set(v), u = find_set(u);
        if (v != u) {
            if (rank[v] < rank[u])
                swap(v, u);
            link(v, u);
        }
        return v != u;
    }

    bool same_set(int v, int u) {
        return find_set(v) == find_set(u);
    }

    int size_set(int v) {
        return size[find_set(v)];
    }
};

```

2.3 EERTREE

```

/* @brief Palindromes in Dequeby adamant*/
#define PROBLEM "https://judge.yosupo.jp/problem/palindromes_in_deque"
#pragma GCC optimize("Ofast,unroll-loops")
#pragma GCC target("tune=native")
#include <bits/stdc++.h>
using namespace std;

template<int sigma = 26, char mch = 'a'>
struct eertree {
    eertree(size_t q) {
        q += 2;
        cnt = len = par = qlink = vector(q, 0);
        to.resize(q);
        link.resize(q);
        ranges::fill(link[0], 1);
        qlink[0] = 1;
        len[1] = -1;
    }

    template<bool back = 1>
    static int get(auto const &d, size_t idx) {
        if (idx >= size(d)) { return -1; } else { return back ? rbegin(d)[idx]
↪ : d[idx]; }
    }

    template<bool back = 1>
    static void push(auto &d, auto c) { back ? d.push_back(c) :
↪ d.push_front(c); }

```

```

template<bool back = 1>
static void pop(auto &d) { back ? d.pop_back() : d.pop_front(); }

template<bool back = 1>
void add_letter(char c) {
    c -= mch;
    push<back>(s, c);
    int pre = get<back>(states, 0);
    int last = make_to<back>(pre, c);
    active += !(cnt[last]++);
    int D = 2 + len[pre] - len[last];
    while (D + len[pre] <= len[last]) {
        pop<back>(states);
        if (!empty(states)) {
            pre = get<back>(states, 0);
            D += get<back>(diffs, 0);
            pop<back>(diffs);
        } else { break; }
    }
    if (!empty(states)) { push<back>(diffs, D); }
    push<back>(states, last);
}

template<bool back = 1>
void pop_letter() {
    int last = get<back>(states, 0);
    active -= (--cnt[last]);
    pop<back>(states);
    pop<back>(s);
    array cands = {pair{qlink[last], len[last] - len[qlink[last]]},
↪ pair{par[last], 0}};
    for (auto [state, diff]: cands) {
        if (empty(states)) {
            states = {state};
            diffs = {diff};
        } else {
            int D = get<back>(diffs, 0) - diff;
            int pre = get<back>(states, 0);
            if (D + len[state] > len[pre]) {
                push<back>(states, state);
                pop<back>(diffs);
                push<back>(diffs, D);
                push<back>(diffs, diff);
            }
        }
    }
    pop<back>(diffs);
}

void add_letter(char c, bool back) { back ? add_letter<1>(c) :
↪ add_letter<0>(c); }
void pop_letter(bool back) { back ? pop_letter<1>() : pop_letter<0>(); }
int distinct() { return active; }

```



```

    template<bool back = 1>
    int maxlen() { return len[get<back>(states, 0)]; }

private:
    vector<array<int, sigma> > to, link;
    vector<int> len, qlink, par, cnt;
    deque<char> s;
    deque<int> states = {0}, diffs;
    int sz = 2, active = 0;

    template<bool back = 1>
    int make_to(int last, int c) {
        if (c != get<back>(s, len[last] + 1)) { last = link[last][c]; }
        if (!to[last][c]) {
            int u = to[link[last][c]][c];
            qlink[sz] = u;
            link[sz] = link[u];
            link[sz][get<back>(s, len[u])] = u;
            len[sz] = len[last] + 2;
            par[sz] = last;
            to[last][c] = sz++;
        }
        return to[last][c];
    }
};

void solve() {
    int q;
    cin >> q;
    eertree me(q);
    for (int i = 0; i < q; i++) {
        int t;
        cin >> t;
        if (t / 2) { me.pop_letter(t % 2); } else {
            char c;
            cin >> c;
            me.add_letter(c, t % 2);
        }
        cout << me.distinct() << ' ' << me.maxlen<0>() << ' ' << me.maxlen<1>()
        << "\n";
    }
}

signed main() {
    ios::sync_with_stdio(0);
    cin.tie(0);
    int t = 1;
    while (t--) { solve(); }
}

```

2.4 Fenwick 2d

```
template <typename T>
class FenwickTree2D {
public:
    vector<vector<T>> tree;
    int n, m;
    void init(int n, int m) {
        tree.assign(n + 2, vector<T>(m + 2, 0));
        this->n = n;
        this->m = m;
    }
    T merge(T &x, T &y) { return x + y; }
    void update(int x, int y, T val) {
        for (; x <= n; x += x & -x) {
            for (int z = y; z <= m; z += z & -z) {
                tree[x][z] = merge(tree[x][z], val);
            }
        }
    }
    T getPrefix(int x, int y) {
        if (x <= 0) return 0;
        T ret = 0;
        for (; x; x -= x & -x) {
            for (int z = y; z; z -= z & -z) {
                ret = merge(ret, tree[x][z]);
            }
        }
        return ret;
    }
    T getSquare(int xl, int yl, int xr, int yr) {
        return getPrefix(xr, yr) + getPrefix(xl - 1, yl - 1) -
            getPrefix(xr, yl - 1) - getPrefix(xl - 1, yr);
    }
};
```

2.5 Fenwick

```
struct fenwik_tree
{
    int n;
    vector<int> fen;
    fenwik_tree(int _n)
    {
        fen = vector<int>(_n + 1);
        n = _n;
    }
    int sum(int p)
    {
        int s = 0;
        while (p >= 1) s += fen[p], p -= p & -p;
        return s;
    }
    int sum(int l, int r)
```

```

{
    return sum(r) - (l > 1 ? sum(l - 1) : 0);
}
void add(int p, int x)
{
    while (p <= n) fen[p] += x, p += p & -p;
}
};

```

2.6 LCA o1 minimal

```

vector<int> dep(n), in(n), out(n), seq, pa(n, -1);

auto dfs = [&](auto &&self, int u) -> void {
    in[u] = seq.size();
    seq.push_back(u);
    for (auto v : G[u])
        if (v != pa[u]) {
            pa[v] = u, dep[v] = dep[u] + 1;
            self(self, v);
        }
    out[u] = seq.size();
};
seq.reserve(n);
dfs(dfs, 0);

const int M = __lg(n);
vector dp(M + 1, vector<int>(n));
auto cmp = [&](int a, int b) { return dep[a] < dep[b] ? a : b; };

dp[0] = seq;
for (int i = 0; i < M; i++)
    for (int j = 0; j + (2 << i) <= n; j++)
        dp[i + 1][j] = cmp(dp[i][j], dp[i][j + (1 << i)]);

auto lca = [&](int a, int b) {
    if (a == b) return a;
    a = in[a] + 1, b = in[b] + 1;
    if (a > b) swap(a, b);
    int h = __lg(b - a);
    return pa[cmp(dp[h][a], dp[h][b - (1 << h)])];
};

```

2.7 LCA

```

const int LG = 20;
const int N = 1e6 + 10;
int up[N][LG], lvl[N];
vector<vector<int>> G;
class LCA{
public:
    LCA(){
        dfs(1, 0);
    }
};

```

```

}
void dfs(int u, int p){
    up[u][0] = p;
    for(int j = 1; j < LG; j++){
        up[u][j] = up[up[u][j-1]][j-1];
    }
    for(auto&v : G[u]){
        if(v == p) continue;
        lvl[v] = lvl[u] + 1;
        dfs(v, u);
    }
}
int kthAncestor(int u, int k){
    for(int j = LG-1; j >= 0; j--){
        if(k >> j & 1){
            u = up[u][j];
        }
    }
    return u;
}
int lca(int u, int v){
    if(lvl[u] < lvl[v]) swap(u, v);
    int d = lvl[u] - lvl[v];
    u = kthAncestor(u, d);
    if(u == v) return u;
    for(int j = LG-1; j >= 0; j--){
        if(up[u][j] != up[v][j]){
            u = up[u][j];
            v = up[v][j];
        }
    }
    return up[u][0];
}
int dist(int u, int v){
    return lvl[u] + lvl[v] - 2*lvl[lca(u, v)];
}
};

```

2.8 Mo (Saad)

```

const int N = 1e5 + 5;
vector<int> v(N);
int root;
struct query {
    int l, r, idx;
    bool operator<(query& oth) const {
        if (l / root == oth.l / root) return r < oth.r;
        return l < oth.l;
    }
};
vector<query> ask;
vector<ll> ans(N);
ll cur;
int n, q, l = 0, r = -1;

```

```

struct MO {
    void add(int idx) {}
    void remove(int idx) {}
    void change(int idx) {
        while (r < ask[idx].r) {
            r++;
            add(r);
        }
        while (r > ask[idx].r) {
            remove(r);
            r--;
        }
        while (l > ask[idx].l) {
            l--;
            add(l);
        }
        while (l < ask[idx].l) {
            remove(l);
            l++;
        }
        ans[ask[idx].idx] = cur;
    }
};

void solve() {
    cin >> n >> q;
    ask = vector<query>(q);
    root = sqrt(q) + 1;
    for (int i = 0; i < n; i++) cin >> v[i];
    for (int i = 0; i < q; i++)
        cin >> ask[i].l >> ask[i].r, --ask[i].l, --ask[i].r, ask[i].idx = i;
    sort(all(ask));
    MO mo;
    for (int i = 0; i < q; i++) mo.change(i);
    for (int i = 0; i < q; i++) cout << ans[i] << endl;
}

```

2.9 Mo Algorithm

```

int sqrtN; //use a constant value
struct query {
    int l, r, qindx, block;
    query() {}
    query(int l, int r, int qindx) : l(l), r(r), qindx(qindx), block(l / sqrtN) {}
    ↪ bool operator <(const query& q) {
        if (block != q.block) return block < q.block;
        return (block & 2 == 0 ? r < q.r : r > q.r);
    }
};

vector<query> q;
int curL, curR, ans;
void add(int indx);
void remove(int indx);

```

```

void solve(int l, int r) {
    while (curL > l) add(--curL);
    while (curR < r) add(++curR);
    while (curL < l) remove(curL++);
    while (curR > r) remove(curR--);
}
vector<int> MO() {
    vector<int> rt(q.size());
    ans = 0;
    curL = 1; curR = 0;
    add(0);
    sort(q.begin(), q.end());
    for (auto it : q) {
        solve(it.l, it.r);
        rt[it.qindx] = ans;
    }
    return rt;
}

```

2.10 Mo on trees

```

// mex on path
vector<vector<int>> adj;
int root;
const int N = 2e5 + 5;
const int LG = 20;
int in[N], out[N], vis[N], lvl[N], frq[N], V[N], vertex[2 * N], up[N][LG];
class MEX {
private:
    bitset<N + 1> mex;
    vector<int> cnt;
public:
    MEX() {
        mex.set();
        cnt.assign(N + 1, 0);
    }

    void add(int x) {
        if (++cnt[x] == 1) {
            mex[x] = false;
        }
    }

    void remove(int x) {
        if (--cnt[x] == 0) {
            mex[x] = true;
        }
    }

    int get_mex() {
        return mex._Find_first();
    }
};

```

```

MEX mx;
struct MoOnTree {
    int n, timer;

    MoOnTree(int n) { //base 1
        n *= 2;
        n += 5;
        this->n = n;
        timer = 0;
        dfs(1, 0);
    }

    void dfs(int u, int p) {
        in[u] = ++timer;
        vertex[timer] = u;
        up[u][0] = p;
        for (int j = 1; j < LG; j++) {
            up[u][j] = up[up[u][j - 1]][j - 1];
        }
        for (auto &v: adj[u]) {
            if (v == p) continue;
            lvl[v] = lvl[u] + 1;
            dfs(v, u);
        }
        out[u] = ++timer;
        vertex[timer] = u;
    }

    int lca(int u, int v) {
        if (lvl[u] < lvl[v]) swap(u, v);
        int k = lvl[u] - lvl[v];
        for (int j = 0; j < LG; j++) {
            if (k >> j & 1) {
                u = up[u][j];
            }
        }
        if (u == v) return u;
        for (int j = LG - 1; j >= 0; j--) {
            if (up[u][j] != up[v][j]) {
                u = up[u][j];
                v = up[v][j];
            }
        }
        return up[u][0];
    }

    struct query {
        int l, r, id, lca;
        query(int l, int r, int id, int lca) : l(l), r(r), id(id), lca(lca) {}

        bool operator<(query &oth) const {
            if (l / root == oth.l / root)
                return r < oth.r;
        }
    };
};

```

```

        return l < oth.l;
    }
};

vector<query> ask;

void addQuery(int u, int v, int id) {
    if (in[u] > in[v]) swap(u, v);
    int lc = lca(u, v);
    int l = (u == lc ? in[u] : out[u]), r = in[v];
    if (u == lc) lc = -1;
    ask.emplace_back(l, r, id, lc);
}

void add(int u) {
    mx.add(V[u]);
}

void remove(int u) {
    mx.remove(V[u]);
}

void modify(int idx, int d, bool node = false) { // node = false -> idx =
→ timer, true -> idx = node
    if (!idx) return;
    int u = (node ? idx : vertex[idx]);
    frq[u] += d;
    if (frq[u] & 1) add(u);
    else remove(u);
}

vector<ll> process() {
    vector<ll> ans(ask.size());
    sort(all(ask));
    int l = 0, r = -1;
    for (auto &query: ask) {
        while (r < query.r) {
            r++;
            modify(r, 1);
        }
        while (r > query.r) {
            modify(r, -1);
            r--;
        }
        while (l > query.l) {
            l--;
            modify(l, 1);
        }
        while (l < query.l) {
            modify(l, -1);
            l++;
        }
        if (~query.lca) modify(query.lca, 1, 1);
    }
}

```



```

        ans[query.id] = mx.get_mex();
        if (~query.lca)modify(query.lca, -1, 1);
    }
    return ans;
}
};

int n, q;

void init() {
    for (int i = 0; i <= n; i++)in[i] = out[i] = vis[i] = lvl[i] = frq[i] =
    ↪ V[i] = 0;
    for (int i = 0; i <= 2 * n; i++)vertex[i] = 0;
    adj = vector<vector<int>>(n + 1);
    frq[0] = 1;
}

void solve() {
    cin >> n >> q;
    init();
    root = sqrtl(2 * n) + 5;
    for (int i = 1; i <= n; i++){
        cin >> V[i];
        if(V[i] >= n + 5)V[i] = n + 5;
    }
    for (int i = 1; i < n; i++) {
        int a, b;
        cin >> a >> b;
        adj[a].push_back(b);
        adj[b].push_back(a);
    }
    MoOnTree MO(n);
    for (int id = 0; id < q; id++) {
        int a, b;
        cin >> a >> b;
        MO.addQuery(a, b, id);
    }
    vector<ll> ans = MO.process();
    for (auto &it: ans){
        cout<<it-1<<endl;
    }
}

```

2.11 MonoQueue Anas

```

template <class T>
struct Mono_queue {
    stack<pair<T, T>> pop_st, push_st;

    void push_to_stack(stack<pair<T, T>> &st, const T &val) {
        st.emplace(val, st.empty() ? val : max(val, st.top().second));
    }

    void push(const T &val) {

```

```

        push_to_stack(push_st, val);
    }

    void move() {
        if (!pop_st.empty()) return;
        while (!push_st.empty()) {
            push_to_stack(pop_st, push_st.top().first);
            push_st.pop();
        }
    }

    void pop(){
        move();
        pop_st.pop();
    }

    bool empty() const{
        return pop_st.empty() && push_st.empty();
    }

    int size() const{
        return pop_st.size() + push_st.size();
    }

    T get_max() const {
        if (pop_st.empty())
            return push_st.top().second;
        if (push_st.empty())
            return pop_st.top().second;
        return max(push_st.top().second, pop_st.top().second);
    }
};

```

2.12 MonoQueue

```

class MQ {
private:
    deque<pair<int, ll>> dq;
public:
    void push(int idx, ll x) {
        while (!dq.empty() && dq.back().second >= x) {
            dq.pop_back();
        }
        dq.push_back({idx, x});
    }

    ll get(int idx, int k) {
        while (!dq.empty() && idx - dq.front().first > k) dq.pop_front();
        if (dq.empty()) return 1e9;
        return dq.front().second;
    }
};

```

2.13 Ordered Set

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template<typename key>
using ordered_set = tree<key, null_type, less<key>, rb_tree_tag,
    ↪ tree_order_statistics_node_update>;

// order_of_key(k) : It returns to the number of items that are strictly
    ↪ smaller than our item k in  $O(\log n)$  tme.
// find_by_order(k): It returns to an iterator to the kth element (counting
    ↪ from zero) in the set in  $O(\log n)$  tme.
// To find the first element k must be zero.
```

2.14 Saad HLD

```
const int N = 1e4 + 5;
int sz[N], head[N];
vector<int>heavy(N, -1);
vector<int>seq, idx(N);
vector<vector<pair<int, int>>>v(N);
int val[N];
int depth[N];
int n;
template<typename T>
class segment_tree {//1-based
#define LEFT (idx<<1)
#define RIGHT (idx<<1|1)
#define MID ((start+end)>>1)
    int n;
    vector<T> tree;
    vector<T> lazy;

    T merge(const T& left, const T& right) {
        return max(left, right);
    }

    inline void pushup(int idx) {
        tree[idx] = merge(tree[LEFT], tree[RIGHT]);
    }

    void build(int idx, int start, int end) {
        if (start == end)
            return;
        build(LEFT, start, MID);
        build(RIGHT, MID + 1, end);
        pushup(idx);
    }

    void build(int idx, int start, int end, const vector<T>& arr) {
        if (start == end) {
            tree[idx] = arr[start];
            return;
        }
        build(LEFT, start, MID, arr);
        build(RIGHT, MID + 1, end, arr);
        pushup(idx);
    }
};
```

```

    }
    build(LEFT, start, MID, arr);
    build(RIGHT, MID + 1, end, arr);
    pushup(idx);
}

T query(int idx, int start, int end, int from, int to) {
    if (from <= start && end <= to)
        return tree[idx];
    if (to < start || from > end) return 0;
    return merge(query(LEFT, start, MID, from, to), query(RIGHT, MID + 1,
↪ end, from, to));
}

void update(int idx, int start, int end, int lq, int rq,
    const T& val) {
    if (rq < start || end < lq)
        return;
    if (lq <= start && end <= rq) {
        tree[idx] = val;
        return;
    }

    update(LEFT, start, MID, lq, rq, val);
    update(RIGHT, MID + 1, end, lq, rq, val);
    pushup(idx);
}

public:
    segment_tree(int n) : n(n), tree(n << 2), lazy(n << 2) {}

    segment_tree(const vector<T>& v) {
        n = v.size() - 1;
        tree = vector<T>(n << 2);
        lazy = vector<T>(n << 2);
        build(1, 1, n, v);
    }

    T query(int l, int r) {
        return query(1, 1, n, l, r);
    }

    void update(int l, int r, const T& val) {
        update(1, 1, n, l, r, val);
    }

    #undef LEFT
    #undef RIGHT
    #undef MID
};

void dfsSz(int node, int par)

```

```

{
    int mx = 0;
    sz[node] = 1;
    for (auto it : v[node])
    {
        if (it.first == par)continue;
        dfsSz(it.first, node);
        val[it.first] = it.second;

        if (sz[it.first] > mx)mx = sz[it.first], heavy[node] = it.first;
        sz[node] += sz[it.first];
    }
}
int p[N];
void dfs(int node, int par, int h)
{
    p[node] = par;
    head[node] = h;
    idx[node] = seq.size();
    seq.push_back(node);

    depth[node] = depth[par] + 1;
    if (~heavy[node])
        dfs(heavy[node], node, h);
    for (auto it : v[node])
    {
        if (it.first == par || heavy[node] == it.first)continue;
        dfs(it.first, node, it.first);
    }
}
segment_tree<int> st(0);
int query(int a, int b) {
    int res = 0;
    for (; head[a] != head[b]; b = p[head[b]]) {
        if (depth[head[a]] > depth[head[b]])
            swap(a, b);
        int cur_heavy_path_max = st.query(idx[head[b]], idx[b]);
        res = max(res, cur_heavy_path_max);
    }
    if (depth[a] > depth[b])
        swap(a, b);
    if (a != b)
    {
        int last_heavy_path_max = st.query(idx[a] + 1, idx[b]);
        res = max(res, last_heavy_path_max);
    }
    return res;
}
void solve()
{
    seq.push_back(-1);
    cin >> n;
    vector<pair<int, int>>edges(n);

```

```

heavy = vector<int>(n + 1, -1);
for (int i = 1; i < n; i++)
{
    int x, y, c;
    cin >> x >> y >> c;
    edges[i] = { x, y };
    v[x].push_back({ y, c });
    v[y].push_back({ x, c });
}
dfsSz(1, -1);
dfs(1, N - 1, 1);
st = segment_tree<int>(n+1);
for (int i = 2; i <= n; i++)
    st.update(idx[i], idx[i], val[i]);
while (true)
{
    string q;
    cin >> q;
    if (q == "DONE")
    {
        seq.clear();
        for (int i = 1; i <= n; i++)
            v[i].clear();
        return;
    }
    if (q == "CHANGE")
    {
        int id, val;
        cin >> id >> val;
        int a = edges[id].first;
        int b = edges[id].second;
        if (p[a] == b) swap(a, b);
        st.update(idx[b], idx[b], val);
    }
    else
    {
        int a, b;
        cin >> a >> b;
        cout << query(a, b) << endl;
    }
}
}

```

2.15 Sack

```

vector<int> *vec[maxn];
int cnt[maxn];
void dfs(int v, int p, bool keep){
    int mx = -1, bigChild = -1;
    for(auto u : g[v])
        if(u != p && sz[u] > mx)
            mx = sz[u], bigChild = u;
}

```

```

for(auto u : g[v])
    if(u != p && u != bigChild)
        dfs(u, v, 0);
if(bigChild != -1)
    dfs(bigChild, v, 1), vec[v] = vec[bigChild];
else
    vec[v] = new vector<int> ();
vec[v]->push_back(v);
cnt[ col[v] ]++;
for(auto u : g[v])
    if(u != p && u != bigChild)
        for(auto x : *vec[u]){
            cnt[ col[x] ]++;
            vec[v] -> push_back(x);
        }
//now cnt[c] is the number of vertices in subtree of vertex v that has
↪ color c.
// note that in this step *vec[v] contains all of the subtree of vertex v.
if(keep == 0)
    for(auto u : *vec[v])
        cnt[ col[u] ]--;
}

int cnt[maxn];
void dfs(int v, int p, bool keep){
    int mx = -1, bigChild = -1;
    for(auto u : g[v])
        if(u != p && sz[u] > mx)
            mx = sz[u], bigChild = u;
    for(auto u : g[v])
        if(u != p && u != bigChild)
            dfs(u, v, 0); // run a dfs on small childs and clear them from cnt
    if(bigChild != -1)
        dfs(bigChild, v, 1); // bigChild marked as big and not cleared from
↪ cnt
    for(auto u : g[v])
        if(u != p && u != bigChild)
            for(int p = st[u]; p < ft[u]; p++)
                cnt[ col[ ver[p] ] ]++;
    cnt[ col[v] ]++;
    //now cnt[c] is the number of vertices in subtree of vertex v that has
↪ color c. You can answer the queries easily.
    if(keep == 0)
        for(int p = st[v]; p < ft[v]; p++)
            cnt[ col[ ver[p] ] ]--;
}

```

2.16 SparseTable

```

template<typename T>
struct sparseTable {
    vector<vector<T>> table;
    vector<int> lg;

```

```

int n, maxLog;
sparseTable(vector<ll> &v) {
    n = v.size();
    lg.resize(n + 1);
    for (int i = 2; i <= n; ++i) lg[i] = lg[i / 2] + 1;
    maxLog = lg[n] + 1;
    table.resize(n, vector<T>(maxLog));
    for (int i = 0; i < n; i++) {
        table[i][0] = v[i];
    }
    for (int j = 1; j < maxLog; j++) {
        for (int i = 0; i <= n - (1 << j); i++) {
            table[i][j] = min(table[i][j - 1], table[i + (1 << (j - 1))][j
↪ - 1]);
        }
    }
}

T query(int l, int r) {
    assert(l <= r);
    int j = lg[r - l + 1];
    return min(table[l][j], table[r - (1 << j) + 1][j]);
}

T query2(int l, int r) {
    T mn = 2e9;
    for (int i = maxLog; i >= 0; i--) {
        if ((1 << i) <= r - l + 1) {
            mn = min(mn, table[l][i]);
            l += 1 << i;
        }
    }
    return mn;
}
};

```

2.17 Sqrt Decomposition

```

int root = (int)sqrt(n + .0) + 1;
vector<int> v(n), bucket(root);
for (int i = 0; i < n; ++i)
    bucket[i / root] += v[i];

while (q--) {
    int l, r;
    int sum = 0;
    int c_l = l / root, c_r = r / root;
    if (c_l == c_r)
        for (int i = l; i <= r; ++i)
            sum += v[i];
    else {
        for (int i = l, end = (c_l + 1) * root - 1; i <= end; ++i)
            sum += v[i];
        for (int i = c_l + 1; i <= c_r - 1; ++i)
            sum += bucket[i];
        for (int i = c_r * root; i <= r; ++i)

```



```

        sum += v[i];
    }
}

```

2.18 Treap

```

enum DIR
{
    L, R
};

template<typename T>
struct cartesian_tree
{
    static cartesian_tree<T>* sentinel;
    T key;
    int priority = 0, size = 0;
    bool reverse = false;
    cartesian_tree* child[2];
    cartesian_tree* parent;
    cartesian_tree()
    {
        key = T();
        priority = 0;
        child[L] = child[R] = parent = this;
    }
    cartesian_tree(const T& x, int y) :
        key(x), priority(y)
    {
        size = 1;
        child[L] = child[R] = sentinel;
        parent = sentinel;
    }
    void push_down()
    {
        if (!reverse)
            return;
        reverse = 0;
        child[L]->doReverse();
        child[R]->doReverse();
    }
    void doReverse()
    {
        reverse ^= 1;
        swap(child[L], child[R]);
    }
    void push_up()
    {
        if (child[L] != sentinel) child[L]->parent = this;
        if (child[R] != sentinel) child[R]->parent = this;
        size = child[L]->size + child[R]->size + 1;
    }
};

```

```

template<typename T>
cartesian_tree<T>* cartesian_tree<T>::sentinel = new cartesian_tree<T>();

template<typename T, template<typename> class cartesian_tree>
class implicit_treap
{ //1 based
    typedef cartesian_tree<T> node;
    typedef cartesian_tree<T>* nodeptr;
#define emptyNode cartesian_tree<T>::sentinel
    nodeptr root;

    void split(nodeptr root, nodeptr& l, nodeptr& r, int firstXElment)
    {
        if (root == emptyNode)
        {
            l = r = emptyNode;
            return;
        }
        root->push_down();
        if (firstXElment <= root->child[L]->size)
        {
            split(root->child[L], l, root->child[L], firstXElment);
            r = root;
        }
        else
        {
            split(root->child[R], root->child[R], r,
                firstXElment - root->child[L]->size - 1);
            l = root;
        }
        root->push_up();
    }

    nodeptr merge(nodeptr l, nodeptr r)
    {
        l->push_down();
        r->push_down();
        if (l == emptyNode || r == emptyNode)
            return (l == emptyNode ? r : l);
        if (l->priority > r->priority)
        {
            l->child[R] = merge(l->child[R], r);
            l->push_up();
            return l;
        }
        r->child[L] = merge(l, r->child[L]);
        r->push_up();
        return r;
    }

    vector<nodeptr> split_range(int s, int e)
    { // [x<s, s<=x<=e, e<x]
        nodeptr l, m, r, tmp;

```

```

    split(root, l, tmp, s - 1);
    split(tmp, m, r, e - s + 1);
    return { l, m, r };
}
map<T, nodeptr> mp;
public:
implicit_treap() :
    root(emptyNode)
{
}
int size()
{
    return root->size;
}
void insert(int pos, const T& key)
{
    nodeptr tmp = new node(key, rand());
    nodeptr l, r;
    split(root, l, r, pos - 1);
    root = merge(merge(l, tmp), r);
}
void push_back(const T& value)
{
    nodeptr tmp = new node(value, rand());
    mp[value] = tmp;
    root = merge(root, tmp);
}
T getByIndex(int pos)
{
    vector<nodeptr> tmp = split_range(pos, pos);
    nodeptr l = tmp[0], m = tmp[1], r = tmp[2];
    T rt = m->key;
    root = merge(merge(l, m), r);
    return rt;
}
void erase(int pos)
{
    vector<nodeptr> tmp = split_range(pos, pos);
    nodeptr l = tmp[0], m = tmp[1], r = tmp[2];
    delete m;
    root = merge(l, r);
}
void cyclic_shift(int s, int e)
{
    //to the right
    vector<nodeptr> tmp = split_range(s, e);
    nodeptr l = tmp[0], m = tmp[1], r = tmp[2];
    nodeptr first, second;
    split(m, first, second, e - s);
    root = merge(merge(merge(l, second), first), r);
}
void reverse_range(int s, int e)

```

```

{
    vector<nodeptr> tmp = split_range(s, e);
    nodeptr l = tmp[0], m = tmp[1], r = tmp[2];
    m->doReverse();
    root = merge(merge(l, m), r);
}
node range_query(int s, int e)
{
    vector<nodeptr> tmp = split_range(s, e);
    nodeptr l = tmp[0], m = tmp[1], r = tmp[2];
    node rt = *m;
    root = merge(merge(l, m), r);
}
int getIndexByValue(const T& value)
{
    nodeptr cur = mp[value];

    vector<nodeptr> path;
    path.push_back(cur);
    while (cur != root)
    {
        cur = cur->parent;
        path.push_back(cur);
    }

    for (int i = path.size() - 1; i >= 0; i--)
        path[i]->push_down();
    for (auto& it : path)
        it->push_up();

    cur = mp[value];
    int cnt = cur->child[L]->size + 1;
    while (cur != root)
    {
        nodeptr par = cur->parent;
        if (par->child[R] == cur) cnt += par->child[L]->size + 1;
        cur = par;
    }
    return cnt;
}
};
implicit_treap<int, cartesian_tree> tr;

```

2.19 Two SAT

//SCC

```

vector<vector<int>> adj, scc;
vector<int> dfs_num, dfs_low, compId;
vector<bool> inStack;
stack<int> stk;
int timer;
void dfs(int node) {
    dfs_num[node]=dfs_low[node]=++timer;

```

```

stk.push(node);
inStack[node]=1;
for(int child : adj[node])
    if(!dfs_num[child]) {
        dfs(child);
        dfs_low[node]=min(dfs_low[node], dfs_low[child]);
    }
    else if(inStack[child])
        dfs_low[node]=min(dfs_low[node], dfs_num[child]);

//can be dfs_low[node] = min(dfs_low[node], dfs_low[child]);

if(dfs_low[node]==dfs_num[node]) {
    scc.push_back(vector<int>());
    int v=-1;
    while(v!=node) {
        v=stk.top();
        stk.pop();
        inStack[v]=0;
        scc.back().push_back(v);
        compId[v]=scc.size()-1;
    }
}
}

void SCC() {
    timer=0;
    dfs_num=dfs_low=compId=vector<int>(adj.size());
    inStack=vector<bool>(adj.size());
    scc=vector<vector<int>>();
    for(int i=1; i<adj.size(); i++)
        if(!dfs_num[i]) dfs(i);
}

int n;
int Not(int x) {
    return (x>n ? x-n : x+n);
}

void addEdge(int a, int b) {
    adj[Not(a)].push_back(b);
    adj[Not(b)].push_back(a);
}

void add_xor_edge(int a, int b) {
    addEdge(Not(a), Not(b));
    addEdge(a, b);
}

// this should be fixed
bool _2SAT(vector<int>& value) {
    SCC();
    for(int i=1; i<=n; i++)
        if(compId[i]==compId[Not(i)])
            return false;
    vector<int> assign(scc.size(), -1);
    for(int i=0; i<scc.size(); i++)
        if(assign[i]==-1) {

```

```

        assign[i]=true;
        assign[compId[Not(scc[i].back())]]=false;
    }
    for(int i=1; i<=n; i++)
        value[i]=assign[compId[i]];
    return true;
}
// to this but needs testing
bool _2SAT(vector<int> &value) {
    SCC();
    for (int i = 1; i <= n; i++)
        if (compId[i] == compId[Not(i)]) return false;

    value.assign(n + 1, 0);
    // Tarjan gives components in reverse topological order if you index by
    // discovery
    // Using the standard rule:    for (int i = 1; i <= n; i++)
        value[i] = (compId[i] > compId[Not(i)]);
    return true;
}

```

2.20 TwoSAT F

```

class two_sat
{
public:
    two_sat(int n) : answer(n, -1), start(2 * n + 1)
    {
    }
    void add_or_clause(int x, bool valx, int y, bool valy)
    {
        x = x * 2 + valx;
        y = y * 2 + valy;
        edges.push_back({ x ^ 1, y });
        edges.push_back({ y ^ 1, x });
        ++start[x ^ 1];
        ++start[y ^ 1];
    }
    pair<bool, vector<int>> solve()
    {
        for (int i = 0; i + 1 < start.size(); ++i)
        { start[i + 1] += start[i]; }
        proc();
        tos.resize(edges.size());
        for (const auto& p : edges)
        { tos[start[p.first]++] = p.second; }
        proc();
        for (int i = 0; i < answer.size(); ++i)
        {
            if (answer[i] == -1)
            {
                lastv.clear();
                if (!dfs(2 * i))
                {

```

```

        for (int v : lastv)
        { answer[v] = -1; }
        if (!dfs(2 * i + 1))
        { return { false, {} }; }
    }
}
return { true, answer };
}
private:
void proc()
{
    for (int i = start.size() - 1; i; --i)
    { start[i] = start[i - 1]; }
    start[0] = 0;
}
bool dfs(int v)
{
    lastv.push_back(v / 2);
    answer[v / 2] = v % 2;
    for (int i = start[v]; i < start[v + 1]; ++i)
    {
        const int to = tos[i];
        if ((answer[to / 2] != -1 && answer[to / 2] != to % 2) || (answer[to / 2]
↪ == -1 && !dfs(to)))
        { return false; }
    }
    return true;
}
vector<int> answer, lastv, start, tos;
vector<pair<int, int>> edges;
};

```

2.21 Segment Tree

2.21.1 Extended Segment Tree

```

struct segtree {
    segtree *left = nullptr, *right = nullptr;
    int mx = 0;

    segtree(int val = 0) :
        mx(val) {

    }

    void extend() {
        if (left == nullptr) {
            left = new segtree();
            right = new segtree();
        }
    }

    void pushup() {
        mx = max(left->mx, right->mx);
    }
};

```

```

    }

    ~segtree() {
        if (left == nullptr) return;
        delete left;
        delete right;
    }
};

class extended_segment_tree {
#define MID ((start+end)>>1)

    void update(segtree *root, int start, int end, int pos, int val) {
        if (pos < start || end < pos)
            return;
        if (start == end) {
            root->mx = max(root->mx, val);
            return;
        }
        root->extend();
        update(root->left, start, MID, pos, val);
        update(root->right, MID + 1, end, pos, val);
        root->pushup();
    }

    int query(segtree *root, int start, int end, int l, int r) {
        if (root == nullptr || r < start || end < l)
            return 0;
        if (l <= start && end <= r)
            return root->mx;
        return max(query(root->left, start, MID, l, r),
                    query(root->right, MID + 1, end, l, r));
    }

public:
    int start, end;
    segtree *root;

    extended_segment_tree() {
    }

    ~extended_segment_tree() {
        delete root;
    }

    extended_segment_tree(int start, int end) : start(start), end(end) {
        root = new segtree();
    }

    void update(int pos, int val) {
        update(root, start, end, pos, val);
    }
}

```



```

int query(int l, int r) {
    return query(root, start, end, l, r);
}

```

```

#undef MID
};

```

2.21.2 KST Lazy

```

class SegTreeLazy {
private:
#define outofrange s>r || e<l
#define inrange s>=l && e<=r
#define lchild p<<1, s, (s+e)/2
#define rchild p<<1|1, (s+e)/2+1, e

    struct Node {
        ll val, lz;

        Node(ll x = 0) {
            val = x;
            lz = 0;
        }
    };

    Node merge(const Node &a, const Node &b) {
        Node temp;
        temp.val = a.val + b.val;
        return temp;
    }

    void build(int p, int s, int e, const vector<ll> &A) {
        if (s == e) {
            seg[p].val = A[s];
            return;
        }
        build(lchild, A);
        build(rchild, A);
        seg[p] = merge(seg[p << 1], seg[p << 1 | 1]);
    }

    void prop(int p, int s, int e) {
        if (seg[p].lz) {
            seg[p].val += (e - s + 1) * seg[p].lz;
            if (s != e) {
                seg[p << 1].lz += seg[p].lz;
                seg[p << 1 | 1].lz += seg[p].lz;
            }
            seg[p].lz = 0;
        }
    }

    void update(int p, int s, int e, int l, int r, ll val) {

```

```

    prop(p, s, e);
    if (outofrange) return;
    if (inrange) {
        seg[p].lz += val;
        prop(p, s, e);
        return;
    }
    update(lchild, l, r, val);
    update(rchild, l, r, val);
    seg[p] = merge(seg[p << 1], seg[p << 1 | 1]);
}

ll def = {0};

ll query(int p, int s, int e, int l, int r) {
    prop(p, s, e);
    if (outofrange) return def;
    if (inrange) {
        return seg[p].val;
    }
    return query(lchild, l, r) + query(rchild, l, r);
}

vector<Node> seg;
int n;
public:
    SegTreeLazy(const vector<ll> &A) {
        int size = 1;
        while (size < sz(A)) size <<= 1;
        n = sz(A);
        seg.resize(size << 1);
        build(1, 0, n - 1, A);
    }

    void update(int l, int r, ll val) {
        update(1, 0, n - 1, l, r, val);
    }

    ll query(int l, int r) {
        return query(1, 0, n - 1, l, r);
    }
};

```

2.21.3 KST Simple

```

class SegTree {
private:
    #define outofrange s>r || e<l
    #define inrange s>=l && e<=r
    #define lchild p<<1, s, (s+e)/2
    #define rchild p<<1|1, (s+e)/2+1, e

    struct Node {
        ll val;

```

```

    Node(ll x = 0) {
        val = x;
    }

};

Node merge(const Node &a, const Node &b) {
    Node temp;
    temp.val = a.val + b.val;
    return temp;
}

void build(int p, int s, int e, const vector<ll> &A) {
    if (s == e) {
        seg[p].val = A[s];
        return;
    }
    build(lchild, A);
    build(rchild, A);
    seg[p] = merge(seg[p << 1], seg[p << 1 | 1]);
}

void update(int p, int s, int e, int idx, ll val) {
    if (s > idx || e < idx) return;
    if (s == e) {
        seg[p].val += val;
        return;
    }
    update(lchild, idx, val);
    update(rchild, idx, val);
    seg[p] = merge(seg[p << 1], seg[p << 1 | 1]);
}

ll def = {0};

ll query(int p, int s, int e, int l, int r) {
    if (outofrange) return def;
    if (inrange) {
        return seg[p].val;
    }
    return query(lchild, l, r) + query(rchild, l, r);
}

vector<Node> seg;
int n;
public:
SegTree(const vector<ll> &A) {
    int size = 1;
    while (size < sz(A)) size <<= 1;
    n = sz(A);
    seg.resize(size << 1);
    build(1, 0, n - 1, A);
}

```

```

    }

    void update(int idx, ll val) {
        update(1, 0, n - 1, idx, val);
    }

    ll query(int l, int r) {
        return query(1, 0, n - 1, l, r);
    }
};

```

2.21.4 Persistent Basic

```

struct Node {
    Node *ls{}, *rs{};
    int sum{};
} pool[int(1e6)];

int top;
Node *null = pool + 0;

void reset() {
    top = 1;
    null->sum = 0;
    null->ls = null->rs = null;
}

Node *newNode() {
    auto p = pool + (top++);
    *p = *null;
    return p;
}

// x is position to insert
Node *add(Node *p, int l, int r, int x) {
    auto np = newNode();
    *np = *p;
    np->sum++;
    if (r - l == 1) {
        return np;
    }
    int m = (l + r) / 2;
    if (x < m) {
        np->ls = add(p->ls, l, m, x);
    } else {
        np->rs = add(p->rs, m, r, x);
    }
    return np;
}

void solve() {
    int n;
    const int C = (int)1E5;
    vector<Node *> root(n);
}

```

```

// when add, w is position on seg you want to add
// root[v] = add(root[u], 1, C + 1, w); auto Find = [u](Node *a, Node *b,
↪ int k) {
    int l = 1, r = C + 1;    while (r - l > 1) {        int m = (l + r) / 2;
↪ int cnt = a->ls->sum - b->ls->sum;        if (cnt >= k) {            a = a->ls;
↪         b = b->ls;            r = m;        } else {            k -= cnt;            a =
↪ a->rs;            b = b->rs;            l = m;        }        }        return l;    };
}

```

2.21.5 Persistent Segment Tree (Anas)

```

struct Node;
extern Node *emp;
struct Node {
    Node *left, *right;
    int val;
    Node() {
        left = right = this;
        val = 0;
    }
    Node(int val, Node *L = emp, Node *R = emp) : val(val), left(L), right(R) {}
};
Node *emp = new Node();
const int N = 2e5 + 5, MAX = 2e5 + 5;
Node *seg[N] = {emp};
Node *insert(Node *root, int start, int end, int idx) {
    if (idx > end || idx < start)
        return root;
    if (start == end) {
        return new Node(root->val + 1);
    }
    int mid = start + end >> 1;
    Node *L = insert(root->left, start, mid, idx);
    Node *R = insert(root->right, mid + 1, end, idx);
    return new Node(L->val + R->val, L, R);
}
int query(Node *L, Node *R, int start, int end, int k) {
    if (end <= k)
        return 0;
    if (start > k)
        return R->val - L->val;
    int mid = start + end >> 1;
    return query(L->left, R->left, start, mid, k) +
           query(L->right, R->right, mid + 1, end, k);
}

```

2.21.6 PST Kareem

```

struct Node {
    Node *left, *right;
    ll val;

    Node(ll val) : left(nullptr), right(nullptr), val(val) {}
}

```

```

Node(Node *l, Node *r) : left(l), right(r), val(l->val + r->val) {}
};

struct PST {
    int n;
    vector<Node*>roots;
    Node *build(int s, int e) {
        if (s == e) {
            return new Node(0);
        }
        return new Node(build(s, (s + e) / 2), build((s + e) / 2 + 1, e));
    }

    Node *update(Node *prev, int s, int e, int idx, ll val) {
        if (s == e) {
            return new Node(val);
        }
        int mid = (s + e) / 2;
        if (idx <= mid) {
            return new Node(update(prev->left, s, mid, idx, val), prev->right);
        } else {
            return new Node(prev->left, update(prev->right, mid + 1, e, idx,
↪ val));
        }
    }

    ll get(Node *cur, int s, int e, int l, int r) {
        if (s > r || e < l) return 0;
        if (s >= l && e <= r) return cur->val;
        return get(cur->left, s, (s + e) / 2, l, r) + get(cur->right, (s + e) /
↪ 2 + 1, e, l, r);
    }

    PST(int n) : n(n){
        roots.push_back(build(0,n-1));
    }
    void update(int k, int idx, ll x){
        roots[k] = update(roots[k], 0, n - 1, idx, x);
    }
    ll get(int k,int l,int r){
        return get(roots[k],0,n-1,l,r);
    }
    void makeCopy(int k){
        roots.push_back(roots[k]);
    }
};

```

2.21.7 PST Path Kareem

// values on nodes

```

struct Node {
    Node *left, *right;
    ll frq, sum;
    Node(ll frq, ll sum) : left(nullptr), right(nullptr), frq(frq), sum(sum) {}
}

```

```

    Node(Node *l, Node *r) : left(l), right(r), frq(l->frq + r->frq),
    ↪ sum(l->sum + r->sum) {}

};

struct PST {
private:
    int n;
    vector<Node *> roots;

    Node *build(int s, int e) {
        if (s == e) {
            return new Node(0ll, 0ll);
        }
        return new Node(build(s, (s + e) / 2), build((s + e) / 2 + 1, e));
    }

    Node *update(Node *prev, int s, int e, int idx, ll val) {
        if (s == e) {
            //cout<<"HI ";cout<<idx<<' '<<val<<' '<<(prev->frq)<<'
            ↪ '<<(prev->sum)<<endl;
            return new Node(1 + prev->frq, val + prev->sum);
        }
        int mid = (s + e) / 2;
        if (idx <= mid) {
            return new Node(update(prev->left, s, mid, idx, val), prev->right);
        } else {
            return new Node(prev->left, update(prev->right, mid + 1, e, idx,
            ↪ val));
        }
    }

    //kth element
    ll getKth(Node *u, Node *v, Node *lc, Node *upLc, int s, int e, ll k) {
        if (s == e) return s;
        int lVal = u->left->frq + v->left->frq - upLc->left->frq -
        ↪ lc->left->frq;
        if (lVal >= k) {
            return getKth(u->left, v->left, lc->left, upLc->left, s, (s + e) /
            ↪ 2, k);
        }
        return getKth(u->right, v->right, lc->right, upLc->right, (s + e) / 2 +
        ↪ 1, e, k - lVal);
    }

    pair<ll, ll> merge(const pair<ll, ll> &a, const pair<ll, ll> &b) {
        return {a.first + b.first, a.second + b.second};
    }

    // number of elements, sum of them in range
    pair<ll, ll> getRange(Node *u, Node *v, Node *lc, Node *upLc, int s, int e,
    ↪ int l, int r) {
        if (s > r || e < 1) return {0, 0};
        if (s >= 1 && e <= r) {

```

```

        return {u->frq + v->frq - (upLc->frq) - lc->frq, u->sum + v->sum -
↪ (upLc->sum) - lc->sum};
    }
    return merge(getRange(u->left, v->left, lc->left, upLc->left, s, (s +
↪ e) / 2, l, r),
        getRange(u->right, v->right, lc->right, upLc->right, (s +
↪ e) / 2 + 1, e, l, r));
}

public:
    PST(int n) : n(n) {
        roots = vector<Node *>(n);
        roots[0] = build(0, n - 1);
    }

    void update(int u, int par, int idx, ll val) {
        roots[u] = update(roots[par], 0, n - 1, idx, val);
    }
    //kth element
    ll getKth(int u, int v, int lc, int upLC, ll k) {
        return getKth(roots[u], roots[v], roots[lc], roots[upLC], 0, n - 1, k);
    }
    // number of elements, sum of them in range
    pair<ll, ll> getRange(int u, int v, int lc, int upLc, int l, int r) {
        return getRange(roots[u], roots[v], roots[lc], roots[upLc], 0, n - 1,
↪ l, r);
    }
};

```

2.21.8 RST Lazy

```

#define outofrange l > e || s > r
#define inrange l <= s && e <= r
#define lchild p * 2, s, (s+e)/2
#define rchild p * 2 + 1, (s+e)/2 + 1, e

const int mod = 1e9 + 7;
static const int N = 3e5 + 500;
// if needed more than one thingy or complex merging
struct W
{
    int sum, sum2;
    int lz;
    W operator+(W he) const
    {
        // up
        return { (sum + he.sum) % mod, (sum2 + he.sum2) % mod, 0 };
    }

    void prop(int len)
    {
        // prop lazy
        lz %= mod;
        sum2 += lz * lz % mod * len + 2 * sum * lz;
    }
};

```



```

        sum += len * lz;
        sum2 %= mod;
        sum %= mod;
        lz = 0;
    }
};
W seg[4 * N], def = { 0 };
int n, l, r, val;

void dostuff(int p, int s, int e)
{
    // down
    if (s != e)
        seg[p * 2].lz += seg[p].lz, seg[p * 2 + 1].lz += seg[p].lz;
    seg[p].prop(e - s + 1);
}
void update(int p = 1, int s = 1, int e = n)
{
    dostuff(p, s, e);
    if (outofrange) return;
    if (inrange)
    {
        seg[p].lz += val;
        dostuff(p, s, e);
        return;
    }
    update(lchild), update(rchild);
    seg[p] = seg[p * 2] + seg[p * 2 + 1];
}

W get(int p = 1, int s = 1, int e = n)
{
    dostuff(p, s, e);
    if (outofrange)
        return def;
    if (inrange)
        return seg[p];
    return get(lchild) + get(rchild);
}

```

2.21.9 RST simple

```

#define outofrange l > e || s > r
#define inrange l <= s && e <= r
#define lchild p * 2, s, (s+e)/2
#define rchild p * 2 + 1, (s+e)/2 + 1, e

static const int N = 3e5 + 500;
// if needed more than one thingy or complex merging
struct W
{
    int sum, mx, mn;
    W operator+(W he) const
    {

```

```

    return { sum + he.sum, max(mx, he.mx), min(mn, he.mn) };
}
};
W seg[4 * N], def = { 0 }, val;
int n, l, r;

void update(int p = 1, int s = 1, int e = n)
{
    if (outofrange) return;
    if (inrange)
    {
        seg[p] = val;
        return;
    }
    update(lchild), update(rchild);
    seg[p] = seg[p * 2] + seg[p * 2 + 1];
}
W get(int p = 1, int s = 1, int e = n)
{
    if (outofrange)
        return def;
    if (inrange)
        return seg[p];
    return get(lchild) + get(rchild);
}

```

2.21.10 Segment Tree with lazy

Segment tree lazy

```

/*
for efficient memory (2*n)
#define LEFT (idx+1)
#define MID ((start+end)>>1)
#define RIGHT (idx+((MID-start+1)<<1))
*/
template<typename T>
class segment_tree { // 1-based
#define LEFT (idx<<1)
#define RIGHT (idx<<1|1)
#define MID ((start+end)>>1)
    int n;
    vector<T> tree;
    vector<T> lazy;

    T merge(const T &left, const T &right) {

    }

    inline void pushdown(int idx, int start, int end) {
        if (lazy[idx] == 0)
            return;
        //update tree[idx] with lazy[idx]
        tree[idx] += lazy[idx];
        if (start != end) {

```

```

        lazy[LEFT] += lazy[idx];
        lazy[RIGHT] += lazy[idx];
    }
    //clear lazy
    lazy[idx] = 0;
}

inline void pushup(int idx) {
    tree[idx] = merge(tree[LEFT], tree[RIGHT]);
}

void build(int idx, int start, int end) {
    if (start == end)
        return;
    build(LEFT, start, MID);
    build(RIGHT, MID + 1, end);
    pushup(idx);
}

void build(int idx, int start, int end, const vector<T> &arr) {
    if (start == end) {
        tree[idx] = arr[start];
        return;
    }
    build(LEFT, start, MID, arr);
    build(RIGHT, MID + 1, end, arr);
    pushup(idx);
}

T query(int idx, int start, int end, int from, int to) {
    pushdown(idx, start, end);
    if (from <= start && end <= to)
        return tree[idx];
    if (to <= MID)
        return query(LEFT, start, MID, from, to);
    if (MID < from)
        return query(RIGHT, MID + 1, end, from, to);
    return merge(query(LEFT, start, MID, from, to),
        query(RIGHT, MID + 1, end, from, to));
}

void update(int idx, int start, int end, int lq, int rq,
    const T &val) {
    pushdown(idx, start, end);
    if (rq < start || end < lq)
        return;
    if (lq <= start && end <= rq) {
        lazy[idx] += val; //update lazy
        pushdown(idx, start, end);
        return;
    }
    update(LEFT, start, MID, lq, rq, val);
    update(RIGHT, MID + 1, end, lq, rq, val);
}

```

```

        pushup(idx);
    }

public:
    segment_tree(int n) : n(n), tree(n << 2), lazy(n << 2) {
    }

    segment_tree(const vector<T> &v) {
        n = v.size() - 1;
        tree = vector<T>(n << 2);
        lazy = vector<T>(n << 2);
        build(1, 1, n, v);
    }

    T query(int l, int r) {
        return query(1, 1, n, l, r);
    }

    void update(int l, int r, const T &val) {
        update(1, 1, n, l, r, val);
    }

#undef LEFT
#undef RIGHT
#undef MID
};

```

2.21.11 SparseSegmentTree(setBinary-sum Range)

```

#include <bits/stdc++.h>
using namespace std;

class SparseSegtree {
private:
    struct Node {
        int freq = 0;
        int lazy = 0;
        Node *left = nullptr;
        Node *right = nullptr;
    };
    Node *root = new Node;
    const int n;

    int comb(int a, int b) { return a + b; }

    void apply(Node *cur, int len, int val) {
        if (val == 1) {
            (cur->lazy) = val;
            (cur->freq) = len * val;
        }
    }

    void push_down(Node *cur, int l, int r) {
        if ((cur->left) == nullptr) { (cur->left) = new Node; }
    }

```

```

    if ((cur->right) == nullptr) { (cur->right) = new Node; }
    int m = (l + r) / 2;
    apply(cur->left, m - 1 + 1, cur->lazy);
    apply(cur->right, r - m, cur->lazy);
}

void range_set(Node *cur, int l, int r, int ql, int qr, int val) {
    if (qr < l || ql > r) { return; }
    if (ql <= l && r <= qr) {
        apply(cur, r - l + 1, val);
    } else {
        push_down(cur, l, r);
        int m = (l + r) / 2;
        range_set(cur->left, l, m, ql, qr, val);
        range_set(cur->right, m + 1, r, ql, qr, val);
        (cur->freq) = comb((cur->left)->freq, (cur->right)->freq);
    }
}

int range_sum(Node *cur, int l, int r, int ql, int qr) {
    if (qr < l || ql > r) { return 0; }
    if (ql <= l && r <= qr) { return cur->freq; }
    push_down(cur, l, r);
    int m = (l + r) / 2;
    return comb(range_sum(cur->left, l, m, ql, qr),
                range_sum(cur->right, m + 1, r, ql, qr));
}

public:
SparseSegtree(int n) : n(n) {}

void range_set(int ql, int qr, int val) { range_set(root, 0, n - 1, ql, qr,
↵ val); }

int range_sum(int ql, int qr) { return range_sum(root, 0, n - 1, ql, qr); }
};

int main() {
    int query_num;
    cin >> query_num;
    const int RANGE_SIZE = 1e9;
    SparseSegtree st(RANGE_SIZE + 1);

    int c = 0;
    for (int i = 0; i < query_num; i++) {
        int type, x, y;
        cin >> type >> x >> y;
        if (type == 1) {
            c = st.range_sum(x + c, y + c);
            cout << c << '\n';
        } else if (type == 2) {
            st.range_set(x + c, y + c, 1);
        }
    }
}

```

```

}
}

```

2.21.12 SparseSegmentTree(xor-sum Range)

```

class SparseSegtree {
private:
    struct Node {
        int freq = 0;
        bool lazy = 0;
        Node *left = nullptr;
        Node *right = nullptr;
    };
    Node *root = new Node;
    const int n;

    int comb(int a, int b) { return a + b; }

    void apply(Node *cur, int len, int val) {
        if(val == 1){
            (cur->lazy) ^= val;
            cur->freq = len - cur->freq;
        }
    }

    void push_down(Node *cur, int l, int r) {
        if ((cur->left) == nullptr) { (cur->left) = new Node; }
        if ((cur->right) == nullptr) { (cur->right) = new Node; }
        int m = (l + r) / 2;
        apply(cur->left, m - l + 1, cur->lazy);
        apply(cur->right, r - m, cur->lazy);
        cur->lazy = 0;
    }

    void flip_range(Node *cur, int l, int r, int ql, int qr, int val) {
        if (qr < l || ql > r) { return; }
        if (ql <= l && r <= qr) {
            apply(cur, r - l + 1, val);
        } else {
            push_down(cur, l, r);
            int m = (l + r) / 2;
            flip_range(cur->left, l, m, ql, qr, val);
            flip_range(cur->right, m + 1, r, ql, qr, val);
            (cur->freq) = comb((cur->left)->freq, (cur->right)->freq);
        }
    }

    int range_sum(Node *cur, int l, int r, int ql, int qr) {
        if (qr < l || ql > r) { return 0; }
        if (ql <= l && r <= qr) { return cur->freq; }
        push_down(cur, l, r);
        int m = (l + r) / 2;
        return comb(range_sum(cur->left, l, m, ql, qr),
                    range_sum(cur->right, m + 1, r, ql, qr));
    }
}

```

```

    }

public:
    SparseSegtree(int n) : n(n) {}

    void flip_range(int ql, int qr, int val) { flip_range(root, 0, n - 1, ql,
↪ qr, val); }

    int range_sum(int ql, int qr) { return range_sum(root, 0, n - 1, ql, qr); }
};

```

3 Flows

3.1 Dinic Reda get min cut edges

```

void dfs2(int u, int par) {
    if (reached[u])
        return;
    reached[u] = 1;
    for (int i = 0; i < (int) g[u].size(); i++) {
        edge &e = g[u][i];

        if (par == e.to) continue;
        if (e.flow == e.w) continue;
        dfs2(e.to, u);
    }
}

vector<ii > get_cut(int _s, int _t) {
    max_flow(_s, _t);
    reached = vector<int>(n);
    dfs2(s, -1);
    vector<ii > ret;
    for (int u = s; u <= t; u++) {
        if (reached[u]) {
            for (int i = 0; i < (int) g[u].size(); i++) {
                edge &e = g[u][i];
                if (!reached[e.to]) {
                    ret.push_back({u, e.to});
                }
            }
        }
    }
    return ret;
}

```

3.2 Dinic Reda with scaling

Dinic with capacity scaling runs in:

$O(V * E * \log C)$

where

* V = number of vertices

* E = number of edges

```

* C = maximum edge capacity.

const ll inf = 1LL << 61;

struct Dinic {
    struct edge {
        int to, rev;
        ll flow, w;
        int id;
    };
    int n, s, t, mxid;
    vector<int> d, flow_through, done;
    vector<vector<edge>> g;

    Dinic() {}

    Dinic(int _n) {
        n = _n + 10;
        mxid = 0;
        g.resize(n);
    }

    void add_edge(int u, int v, ll w, int id = -1) {
        edge a = {v, (int)g[v].size(), 0, w, id};
        edge b = {u, (int)g[u].size(), 0, w, -2}; // for bidirectional edges
        ↪ cap(b) = w
        g[u].emplace_back(a);
        g[v].emplace_back(b);
        mxid = max(mxid, id);
    }

    bool bfs(ll scale) {
        d.assign(n, -1);
        d[s] = 0;
        queue<int> q;
        q.push(s);
        while (!q.empty()) {
            int u = q.front();
            q.pop();
            for (auto &e : g[u]) {
                int v = e.to;
                if (d[v] == -1 && e.flow < e.w && e.w >= scale) {
                    d[v] = d[u] + 1;
                    q.push(v);
                }
            }
        }
        return d[t] != -1;
    }

    ll dfs(int u, ll flow, ll scale) {
        if (u == t) return flow;
        for (int &i = done[u]; i < (int)g[u].size(); i++) {

```



```

        edge &e = g[u][i];
        if (e.w < scale || e.flow >= e.w) continue;
        int v = e.to;
        if (d[v] == d[u] + 1) {
            ll nw = dfs(v, min(flow, e.w - e.flow), scale);
            if (nw > 0) {
                e.flow += nw;
                g[v][e.rev].flow -= nw;
                return nw;
            }
        }
    }
    return 0;
}

ll max_flow(int _s, int _t) {
    s = _s;
    t = _t;
    ll flow = 0;

    // Determine the maximum capacity in the graph
    ll scale = 1;
    for (int i = 0; i < n; i++) {
        for (const auto &e : g[i]) {
            scale = max(scale, e.w);
        }
    }

    // Apply scaling
    for (scale = (scale + 1) / 2; scale > 0; scale /= 2) {
        while (bfs(scale)) {
            done.assign(n, 0);
            while (ll nw = dfs(s, inf, scale)) flow += nw;
        }
    }

    flow_through.assign(mxid + 10, 0);
    for (int i = 0; i < n; i++)
        for (auto e : g[i])
            if (e.id >= 0)
                flow_through[e.id] = e.flow;

    return flow;
}
};

```

3.3 Dinic Reda

```

struct Dinic
{
    struct edge
    {
        int to, rev;
        ll flow, w;
    };

```

```

    int id;
};
int n, s, t, mxid;
vector<int> d, flow_through, done;
vector<vector<edge>> g;

Dinic()
{
}

Dinic(int _n)
{
    n = _n + 10;
    mxid = 0;
    g.resize(n);
}

void add_edge(int u, int v, ll w, int id = -1)
{
    edge a = { v, (int)g[v].size(), 0, w, id };
    edge b = { u, (int)g[u].size(), 0, 0, -2 }; //for bidirectional edges cap(b)
    ↪ = w
    g[u].emplace_back(a);
    g[v].emplace_back(b);
    mxid = max(mxid, id);
}

bool bfs()
{
    d.assign(n, -1);
    d[s] = 0;
    queue<int> q;
    q.push(s);
    while (!q.empty())
    {
        int u = q.front();
        q.pop();
        for (auto& e : g[u])
        {
            int v = e.to;
            if (d[v] == -1 && e.flow < e.w) d[v] = d[u] + 1, q.push(v);
        }
    }
    return d[t] != -1;
}

ll dfs(int u, ll flow)
{
    if (u == t) return flow;
    for (int& i = done[u]; i < (int)g[u].size(); i++)
    {
        edge& e = g[u][i];
        if (e.w <= e.flow) continue;
    }
}

```

```

    int v = e.to;
    if (d[v] == d[u] + 1)
    {
        ll nw = dfs(v, min(flow, e.w - e.flow));
        if (nw > 0)
        {
            e.flow += nw;
            g[v][e.rev].flow -= nw;
            return nw;
        }
    }
}
return 0;
}

ll max_flow(int _s, int _t)
{
    s = _s;
    t = _t;
    ll flow = 0;
    while (bfs())
    {
        done.assign(n, 0);
        while (ll nw = dfs(s, inf)) flow += nw;
    }
    flow_through.assign(mxid + 10, 0);
    for (int i = 0; i < n; i++) for (auto e : g[i]) if (e.id >= 0)
    ↪ flow_through[e.id] = e.flow;
    return flow;
}

};

void solve()
{
    int n, m;
    cin >> n >> m;
    Dinic F(n);
    for (int i = 0; i < m; ++i)
    {
        int a, b, c;
        cin >> a >> b >> c;
        F.add_edge(a, b, c);
    }
    cout << F.max_flow(1, n) << endl;
}

```

3.4 Edmonds Karp

```

//O( V * E * E)
#define INF 0x3f3f3f3f3f3f3fLL
int n;
int capacity[101][101];

```

```

int getPath(int src, int dest, vector<int> &parent) {
    parent = vector<int>(n + 1, -1);
    queue<pair<int, int>> q;
    q.push({src, INF});
    while (q.size()) {
        int cur = q.front().first, flow = q.front().second;
        q.pop();

        if (cur == dest) return flow;
        for (int i = 1; i <= n; i++)
            if (parent[i] == -1 && capacity[cur][i]) {
                parent[i] = cur;
                q.push({i, min(flow, capacity[cur][i])});
                if (i == dest) return q.back().second;
            }
    }
    return 0;
}

int Edmonds_Karp(int source, int sink) {
    int max_flow = 0;
    int new_flow = 0;
    vector<int> parent(n + 1, -1);
    while (new_flow = getPath(source, sink, parent)) {
        max_flow += new_flow;
        int cur = sink;
        while (cur != source) {
            int prev = parent[cur];
            capacity[prev][cur] -= new_flow;
            capacity[cur][prev] += new_flow;
            cur = prev;
        }
    }
    return max_flow;
}

```

3.5 Hopcroft Karp

```

//Hopcroft-Karp algorithm for maximum bipartite matching
//O(sqrt(V) * E)
struct Hopcroft_Karp { //1-based
#define NIL 0
#define INF INT_MAX
    int n, m;
    vector<vector<int>> adj;
    vector<int> rowAssign, colAssign, dist;
    bool bfs() {
        queue<int> q;
        dist = vector<int>(adj.size(), INF);
        for (int i = 1; i <= n; i++)
            if (rowAssign[i] == NIL) {
                dist[i] = 0;
                q.push(i);
            }
        while (!q.empty()) {

```

```

    int cur = q.front();
    q.pop();
    if (dist[cur] >= dist[NIL]) break;
    for (auto& nxt : adj[cur]) {
        if (dist[colAssign[nxt]] == INF) {
            dist[colAssign[nxt]] = dist[cur] + 1;
            q.push(colAssign[nxt]);
        }
    }
}
return dist[NIL] != INF;
}
bool dfs(int i) {
    if (i == NIL)
        return true;
    for (int j : adj[i]) {
        if (dist[colAssign[j]] == dist[i] + 1 && dfs(colAssign[j])) {
            colAssign[j] = i;
            rowAssign[i] = j;
            return true;
        }
    }
    dist[i] = INF;
    return false;
}
Hopcroft_Karp(int n, int m)
: n(n), m(m), adj(n + 1), rowAssign(n + 1), colAssign(m + 1) {
}
void addEdge(int u, int v) {
    adj[u].push_back(v);
}
int maximum_bipartite_matching() {
    int rt = 0;
    while (bfs()) {
        for (int i = 1; i <= n; i++)
            if (rowAssign[i] == NIL && dfs(i))
                rt++;
    }
    return rt;
}
};

```

3.6 Hungarian

```

// n^3 or something
// nodes are 0-based /* There are n workers and n tasks. You know exactly
→ how much you need to pay each worker to perform one or another task. You
→ also know that every worker can only perform one task. Your goal is to
→ assign each worker some a task, while minimizing your expenses. */

// fill vector a with costs // if you want maximizie final cost then you will
→ multiply edges cost with -1 // this algorithm works only on bipartite
→ graph // the maximum matching must equal to n template<typename T>
class hungarian

```

```

{
public:
    int n;
    int m;
    vector<vector<T> > a;
    vector<T> u;
    vector<T> v;
    vector<int> pa;
    vector<int> pb;
    vector<int> way;
    vector<T> minv;
    vector<bool> used;
    T inf;
    hungarian(int _n, int _m) : n(_n), m(_m)
    {
        assert(n <= m);
        a = vector<vector<T> >(n, vector<T>(m));
        u = vector<T>(n + 1);
        v = vector<T>(m + 1);
        pa = vector<int>(n + 1, -1);
        pb = vector<int>(m + 1, -1);
        way = vector<int>(m, -1);
        minv = vector<T>(m);
        used = vector<bool>(m + 1);
        inf = numeric_limits<T>::max();
    }
    inline void add_row(int i)
    {
        fill(minv.begin(), minv.end(), inf);
        fill(used.begin(), used.end(), false);
        pb[m] = i;
        pa[i] = m;
        int j0 = m;
        do
        {
            used[j0] = true;
            int i0 = pb[j0];
            T delta = inf;
            int j1 = -1;
            for (int j = 0; j < m; j++)
            {
                if (!used[j])
                {
                    T cur = a[i0][j] - u[i0] - v[j];

                    if (cur < minv[j])
                    {
                        minv[j] = cur;
                        way[j] = j0;
                    }
                    if (minv[j] < delta)
                    {
                        delta = minv[j];

```

```

        j1 = j;
    }
}
for (int j = 0; j <= m; j++)
{
    if (used[j])
    {
        u[pb[j]] += delta;
        v[j] -= delta;
    }
    else
    {
        minv[j] -= delta;
    }
}
j0 = j1;
} while (pb[j0] != -1);
do
{
    int j1 = way[j0];
    pb[j0] = pb[j1];
    pa[pb[j0]] = j0;
    j0 = j1;
} while (j0 != m);
}
inline T current_score()
{
    return -v[m];
}
inline T solve()
{
    for (int i = 0; i < n; i++)
    {
        add_row(i);
    }
    return current_score();
}
};

```

3.7 Max Bipartite Matching

```

//O(E*V)
vector<vector<int>> adj;
vector<int> rowAssign, colAssign, vis; //make vis array instance of vector
int test_id;

bool canMatch(int i) {
    if (vis[i] == test_id) return false;
    vis[i] = test_id;
    for (int j: adj[i])
        if (colAssign[j] == -1) {
            colAssign[j] = i;
            rowAssign[i] = j;
        }
}

```

```

        return true;
    }
    for (int j: adj[i])
        if (canMatch(colAssign[j])) {
            colAssign[j] = i;
            rowAssign[i] = j;
            return true;
        }
    return false;
}
// O(rows * edges) //number of operation could be strictly less than order
↳ (1e5*1e5->AC)
int maximum_bipartite_matching(int rows, int cols) {
    int maxFlow = 0;
    rowAssign = vector<int>(rows, -1);
    colAssign = vector<int>(cols, -1);
    vis = vector<int>(rows);
    for (int i = 0; i < rows; i++) {
        test_id++;
        if (canMatch(i)) maxFlow++;
    }
    vector<pair<int, int>> matches;
    for (int j = 0; j < cols; j++)
        if (~colAssign[j]) matches.push_back({colAssign[j], j});
    return maxFlow;
}

```

3.8 MCMF

```

struct MCMF //0-based
{
    struct edge
    {
        int from, to, cost, cap, flow, backEdge;
        edge()
        {
            from = to = cost = cap = flow = backEdge = 0;
        }
        edge(int from, int to, int cost, int cap, int flow, int backEdge) :
            from(from), to(to), cost(cost), cap(cap), flow(flow),
            backEdge(
                backEdge)
        {
        }
    };
    bool operator<(const edge& other) const
    {
        return cost < other.cost;
    }
};
int n, src, dest;
vector<vector<edge>> adj;

const int OO = 1e9;
MCMF(int n, int src, int dest) : n(n), src(src), dest(dest), adj(n)

```



```

{
}
void addEdge(int u, int v, int cost, int cap)
{
    edge e1 = edge(u, v, cost, cap, 0, adj[v].size());
    edge e2 = edge(v, u, -cost, 0, 0, adj[u].size());
    adj[u].push_back(e1);
    adj[v].push_back(e2);
}
pair<int, int> minCostMaxFlow()
{
    int maxFlow = 0, cost = 0;
    while (true)
    {
        vector<pair<int, int>> path = spfa();
        if (path.empty())
            break;
        int new_flow = 0;
        for (auto& it : path)
        {
            edge& e = adj[it.first][it.second];
            new_flow = min(new_flow, e.cap - e.flow);
        }
        for (auto& it : path)
        {
            edge& e = adj[it.first][it.second];
            e.flow += new_flow;
            cost += new_flow * e.cost;
            adj[e.to][e.backEdge].flow -= new_flow;
        }
        maxFlow += new_flow;
    }
    return { maxFlow, cost };
}
enum visit
{
    finished, in_queue, not_visited
};
vector<pair<int, int>> spfa()
{
    vector<int> dis(n, 0), prev(n, -1), from_edge(n), state(n,
        not_visited);
    deque<int> q;
    dis[src] = 0;
    q.push_back(src);
    while (!q.empty())
    {
        int u = q.front();

        q.pop_front();
        state[u] = finished;
        for (int i = 0; i < adj[u].size(); i++)

```

```

    {
        edge e = adj[u][i];
        if (e.flow >= e.cap || dis[e.to] <= dis[u] + e.cost)
            continue;
        dis[e.to] = dis[u] + e.cost;
        prev[e.to] = u;
        from_edge[e.to] = i;
        if (state[e.to] == in_queue)
            continue;
        if (state[e.to] == finished
            || (!q.empty() && dis[q.front()] > dis[e.to]))
            q.push_front(e.to);
        else
            q.push_back(e.to);
        state[e.to] = in_queue;
    }
}
if (dis[dest] == 00)
    return {};
vector<pair<int, int>> path;
int cur = dest;
while (cur != src)
{
    path.push_back({ prev[cur], from_edge[cur] });
    cur = prev[cur];
}
reverse(path.begin(), path.end());
return path;
}
};

```

3.9 Push Relabel

*// $v^2 * \text{sqrt_root}(E)$*

#define sz(x) x.size()

```

struct PushRelabel
{
    struct Edge
    {
        int dest, back;
        ll f, c;
    };
    vector<vector<Edge>> g;
    vector<ll> ec;
    vector<Edge*> cur;
    vector<vi> hs;
    vi H;

    PushRelabel(int n) : g(n), ec(n), cur(n), hs(2 * n), H(n)
    {
    }
}

```

```

void addEdge(int s, int t, ll cap, ll rcap = 0)
{
    if (s == t) return;
    g[s].push_back({ t, sz(g[t]), 0, cap });
    g[t].push_back({ s, sz(g[s]) - 1, 0, rcap });
}

void addFlow(Edge& e, ll f)
{
    Edge& back = g[e.dest][e.back];
    if (!ec[e.dest] && f) hs[H[e.dest]].push_back(e.dest);
    e.f += f;
    e.c -= f;
    ec[e.dest] += f;
    back.f -= f;
    back.c += f;
    ec[back.dest] -= f;
}

ll calc(int s, int t)
{
    int v = sz(g);
    H[s] = v;
    ec[t] = 1;
    vi co(2 * v);
    co[0] = v - 1;
    for (int i = 0; i < v; i++)
        cur[i] = g[i].data();
    for (Edge& e : g[s]) addFlow(e, e.c);

    for (int hi = 0;;)
    {
        while (hs[hi].empty()) if (!hi--) return -ec[s];
        int u = hs[hi].back();
        hs[hi].pop_back();
        while (ec[u] > 0) // discharge u
        if (cur[u] == g[u].data() + sz(g[u]))
        {
            H[u] = 1e9;
            for (Edge& e : g[u])
                if (e.c && H[u] > H[e.dest] + 1)
                    H[u] = H[e.dest] + 1, cur[u] = &e;
            if (++co[H[u]], !--co[hi] && hi < v)
                for (int i = 0; i < v; i++)
                    if (hi < H[i] && H[i] < v)
                        --co[H[i]], H[i] = v + 1;
            hi = H[u];
        }
        else if (cur[u]->c && H[u] == H[cur[u]->dest] + 1)
            addFlow(*cur[u], min(ec[u], cur[u]->c));
        else ++cur[u];
    }
}

```

```

    }

    bool leftOfMinCut(int a)
    {
        return H[a] >= sz(g);
    }
};

```

4 Geometry

4.1 Areas

```

ld areaOfTri(P a, P b, P c){
    return abs((vec(a, b)^vec(a, c)) / 2.0);
}

ld triArea(ot A, ot B, ot C){
    ld s = (A + B + C) * 0.5;
    return sqrt(s * (s - A) * (s - B) * (s - C));
}

//Area of a Triangle Formula in Coordinate Geometry
//If (x1, y1), (x2, y2), and (x3, y3) are the three vertices of a triangle on
→ the coordinate plane, then //its area is calculated by the formula
 //(1/2) |x1(y2 - y3) + x2(y3 - y1) + x3(y1 - y2)|

// tested
ld areaOfPolygon(vector<P> p){
    ot area = 0;
    for(int i = 1; i < p.size() - 1; i++)
        area += vec(p[0], p[i])^vec(p[0], p[i + 1]);
    return abs(area / 2.0);
}

```

4.2 Basic Funcs

```

bool collinear(P a, P b, P c)
{
    return (vec(a, b) ^ vec(a, c)) == 0;
}

**get acute directed angle from a to b**
// tested
ld gda(P a, P b)
{
    ld ang = abs(angle(a) - angle(b));
    ang = min(ang, 2 * PI - ang);
    return ang * ((a ^ b) > 0 ? 1 : -1);
}

// get's X given a line and y
ld getX(P a, P b, ll y) {
    ld slope = (b.y - a.y) / (b.x - a.x);
    return a.x + (y - a.y) / slope;
}

```

```

}

//tested
ld linePointDis(P l1, P l2, P p)
{
    ot area = abs(vec(p, l1) ^ vec(p, l2));
    ld base = len(vec(l1, l2));
    return area / base;
}

ld segmentPointDis(P a, P b, P p){
    P ab = vec(a,b), ap = vec(a,p);
    ld ab2 = ab*ab; // dot
    if (ab2 < eps) return len(vec(p,a)); // degenerate segment
    ld t = max<ld>(0, min<ld>(1, (ap*ab)/ab2));
    P proj = { a.x + ab.x*t, a.y + ab.y*t };
    return len(vec(p, proj));
}

struct cmp
{
    P about;
    cmp(P c)
    {
        about = c;
    }
    bool operator()(const P& a, const P& b) const
    {
        ld cr = vec(about, a) ^ vec(about, b);
        if (fabs(cr) < eps)
            return a < b;
        return cr > 0;
    }
};

void sortAntiClockWise(vector<P>& pnts)
{
    P mn(*min_element(all(pnts)));
    sort(pnts.begin(), pnts.end(), cmp(mn));
}

inline bool pibb(P const& a, P const& b1, P const& b2)
{
    return a.x >= min(b1.x, b2.x) &&
        a.x <= max(b1.x, b2.x) &&
        a.y >= min(b1.y, b2.y) &&
        a.y <= max(b1.y, b2.y);
}

bool lineIntersection(P p1, P p2, P p3, P p4, P& sec)
{
    ld denom = (p1.x - p2.x) * (p3.y - p4.y) - (p1.y - p2.y) * (p3.x - p4.x);

```

```

    if (abs(denom) < eps)
        return false;

    ld t = ((p1.x - p3.x) * (p3.y - p4.y) - (p1.y - p3.y) * (p3.x - p4.x)) /
↪   denom;

    sec = p1 + vec(p1, p2) * t;

    return true;
}

bool segmentsIntersection(P l1, P l2, P k1, P k2, P& sec)
{
    if (lineIntersection(l1, l2, k1, k2, sec))
    {
        if (pibb(sec, l1, l2) && pibb(sec, k1, k2))
            return true;
        return false;
    }
    return false;
}

bool isPointOnSegment(P const& a, P const& l1, P const& l2)
{
    return collinear(a, l1, l2) && pibb(a, l1, l2);
}

P getCircleCenter(P A, P B, P C) {
    if (isCollinear(A, B, C)) {
        collinear = true;
        return {0, 0};
    }
    collinear = false;
    ld D = 2 * (A.x * (B.y - C.y) + B.x * (C.y - A.y) + C.x * (A.y - B.y));
    ld Ux = ((A.x * A.x + A.y * A.y) * (B.y - C.y) + (B.x * B.x + B.y * B.y) *
↪   (C.y - A.y) + (C.x * C.x + C.y * C.y) * (A.y - B.y)) / D;
    ld Uy = ((A.x * A.x + A.y * A.y) * (C.x - B.x) + (B.x * B.x + B.y * B.y) *
↪   (A.x - C.x) + (C.x * C.x + C.y * C.y) * (B.x - A.x)) / D;
    return {Ux, Uy};
}

bool issquare(P a, P b, P c, P d)
{
    if (a == b || a == c || a == d || b == c || b == c || c == d)
        return false;

    vector<ld> ds = {
        a.dis(b), a.dis(c), a.dis(d),
        b.dis(c), b.dis(d), c.dis(d)
    };
    sort(all(ds));
    return ds[0] > 0 &&
        abs(ds[2] - ds[3]) < 1e-8 &&
        abs(ds[0] - ds[1]) < 1e-8 &&

```

```

        abs(ds[1] - ds[2]) < 1e-8 &&
        abs(ds[4] - ds[5]) < 1e-8;
    }

P reflectPoint(P a, P b, P p) {
    P ab = vec(a, b), ap = vec(a, p);
    ld ab2 = ab * ab; // dot(ab, ab)
    if (ab2 < eps) return p; // degenerate line -> nothing to reflect
    // projection parameter on the INFINITE line (no clamp!)
    ld t = (ap * ab) / ab2;
    P proj = {a.x + ab.x * t, a.y + ab.y * t};
    // reflected point: proj + (proj - p)
    P r = {2 * proj.x - p.x, 2 * proj.y - p.y};
    return r;
}

```

4.3 ConvexHull

```

void convexHull(vector<P> p, vector<P>& hull)
{
    sort(all(p), [&](P& a, P& b)
    {
        if (a.x != b.x)
            return a.x < b.x;
        return a.y < b.y;
    });
    if (p.size() == 1)
    {
        hull.push_back(p[0]);
        return;
    }
    for (int rep = 0; rep < 2; rep++)
    {
        int s = hull.size();
        for (int i = 0; i < p.size(); i++)
        {
            while (hull.size() >= s + 2)
            {
                P p1 = hull.end()[-2];
                P p2 = hull.end()[-1];
                if ((vec(p1, p2) ^ vec(p1, p[i])) < -eps)
                    break;

                hull.pop_back();
            }
            hull.push_back(p[i]);
        }
        reverse(all(p));
        hull.pop_back();
    }
}

```

4.4 CosineRule

```
c^2 = a^2 + b^2 - 2ab * cos(C)
a^2 = b^2 + c^2 - 2bc * cos(A)
b^2 = a^2 + c^2 - 2ac * cos(B)

cos(C) = (a^2 + b^2 - c^2) / (2ab)
cos(A) = (b^2 + c^2 - a^2) / (2bc)
cos(B) = (a^2 + c^2 - b^2) / (2ac)
```

```
C = cos^(-1) [(a^2 + b^2 - c^2) / (2ab)]
A = cos^(-1) [(b^2 + c^2 - a^2) / (2bc)]
B = cos^(-1) [(a^2 + c^2 - b^2) / (2ac)]
```

4.5 Defines 3D

```
// 3D geometry (compact, ACPC-friendly)

#define ot long long
#define ld long double
#define sq(x) ((x)*(x))

const ld eps = 1e-12L;
const ld PI = acosl(-1.0L);

struct P3 {
    ld x, y, z;

    void read() { std::cin >> x >> y >> z; }

    P3 operator + (P3 const& o) const { return {x + o.x, y + o.y, z + o.z}; }
    P3 operator - (P3 const& o) const { return {x - o.x, y - o.y, z - o.z}; }
    void operator += (P3 const& o) { x += o.x; y += o.y; z += o.z; }
    void operator -= (P3 const& o) { x -= o.x; y -= o.y; z -= o.z; }

    P3 operator * (ld k) const { return {x * k, y * k, z * k}; }
    P3 operator / (ld k) const { return {x / k, y / k, z / k}; }
    friend P3 operator * (ld k, P3 a) { return a * k; }

    // dot
    ld operator * (P3 const& o) const { return x * o.x + y * o.y + z * o.z; }

    // cross
    P3 operator ^ (P3 const& o) const {
        return { y * o.z - z * o.y, z * o.x - x * o.z, x * o.y - y * o.x };
    }

    ld norm2() const { return (*this) * (*this); }
    ld len() const { return sqrtl(norm2()); }

    P3 unit() const {
        ld l = len();
        return (l < eps ? P3{0, 0, 0} : (*this) / l);
    }
}
```



```

}

// Rodrigues rotation: rotate this vector around 'axis' (through origin)
↪ by 'ang' radians
P3 rotate(P3 axis, ld ang) const {
    axis = axis.unit();
    if (axis.len() < eps) return *this;
    ld c = cosl(ang), s = sinl(ang);
    ↪ return (*this) * c + (axis ^ (*this)) * s + axis * ((axis * (*this)) *
    ↪ (1 - c));
}
};

```

4.6 Defines and Point all

```

#define ot long long
#define ld long double
#define sq(x) ((x)*(x))
#define eps 1e-8
#define angle(a) (atan2((a).y, (a).x))
#define slope(p) (((p).y)/((p).x))
#define vec(a, b) ((b)-(a))
#define len(v) (hypotl((v).y, (v).x))

struct P
{
    ot x, y;
    void read()
    {
        cin >> x >> y;
    }

    bool operator==(P const& he) const
    {
        return x == he.x && y == he.y;
    }
    P operator-(P const& he) const
    {
        return { x - he.x, y - he.y };
    }

    P operator+(P const& he) const
    {
        return { x + he.x, y + he.y };
    }
    void operator--(P const& he)
    {
        x -= he.x, y -= he.y;
    }
    void operator+=(P const& he)
    {
        x += he.x, y += he.y;
    }
    // scalar multiplication

```

```

P operator*(ot val) const
{
    return { x * val, y * val };
}

// cross product
ot operator^(P const& he) const
{
    return x * he.y - y * he.x;
}
// dot product = x1x2+y1y2 = |a|*|b|*cos(theta)
ot operator*(P const& he) const
{
    return x * he.x + y * he.y;
}
//angle in radians
P rotate(ot angle) const
{
    ot cos_theta = cos(angle);
    ot sin_theta = sin(angle);
    return { x * cos_theta - y * sin_theta, x * sin_theta + y * cos_theta };
}
};

```

```

struct Line {
    ld a, b, c;
};

```

```

Line lineFromVector(P p, P v) {
    Line L;
    L.a = v.y;
    L.b = -v.x;
    L.c = v.x * p.y - v.y * p.x;

    ld norm = sqrt(L.a * L.a + L.b * L.b);
    if (norm > 1e-12) L.a /= norm, L.b /= norm, L.c /= norm;

    // (optional) make a unique orientation
    if (L.a < 0 || (abs(L.a) < 1e-12 && L.b < 0))
        L.a = -L.a, L.b = -L.b, L.c = -L.c;

    return L;
}

```

4.7 Defines and Point simple

```

#define ot long long
#define ld long double
#define eps 1e-8
#define vec(a, b) ((b)-(a))
#define len(v) (hypotl((v).y, (v).x))

struct P

```

```

{
    ot x, y;
    void read()
    {
        cin >> x >> y;
    }
    P operator-(P const& he) const
    {
        return { x - he.x, y - he.y };
    }
    // cross product
    ot operator^(P const& he) const
    {
        return x * he.y - y * he.x;
    }
};

```

4.8 Helpers 3D

```
#define vec3(a,b) ((b)-(a))
```

```
ld dis(P3 a, P3 b) { return vec3(a, b).len(); }
```

```
// scalar triple product: a · (b × c)
```

```
ld mixed(P3 a, P3 b, P3 c) { return a * (b ^ c); }
```

```

bool collinear(P3 a, P3 b, P3 c){
    P3 ab = vec3(a,b), ac = vec3(a,c);
    return (ab ^ ac).len() <= eps * ab.len() * ac.len();
}

```

```

bool collinear(P3 a, P3 b, P3 c){
    P3 ab = vec3(a,b), ac = vec3(a,c);
    return (ab ^ ac).len() <= eps * ab.len() * ac.len();
}

```

```

bool coplanar(P3 a, P3 b, P3 c, P3 d){
    P3 ab=vec3(a,b), ac=vec3(a,c), ad=vec3(a,d);
    return fabs1(mixed(ab,ac,ad)) <= eps * ab.len() * ac.len() * ad.len();
}

```

```

bool coplanar(P3 a, P3 b, P3 c, P3 d){
    P3 ab=vec3(a,b), ac=vec3(a,c), ad=vec3(a,d);
    return fabs1(mixed(ab,ac,ad)) <= eps * ab.len() * ac.len() * ad.len();
}

```

```

ld triArea(P3 a, P3 b, P3 c) {
    return (vec3(a, b) ^ vec3(a, c)).len() / 2;
}

```

```

ld tetraVol(P3 a, P3 b, P3 c, P3 d) {
    return fabs1(mixed(vec3(a, b), vec3(a, c), vec3(a, d))) / 6;
}

```

```
// projection of p onto infinite line (a,b)
```

```

P3 projPointLine(P3 p, P3 a, P3 b) {
    P3 ab = vec3(a, b);
    ld ab2 = ab * ab;
    if (ab2 < eps) return a;
    ld t = (vec3(a, p) * ab) / ab2;
    return a + ab * t;
}

ld linePointDis(P3 a, P3 b, P3 p) {
    P3 ab = vec3(a, b), ap = vec3(a, p);
    ld den = ab.len();
    if (den < eps) return ap.len();
    return (ab ^ ap).len() / den;
}

ld segmentPointDis(P3 a, P3 b, P3 p) {
    P3 ab = vec3(a, b), ap = vec3(a, p);
    ld ab2 = ab * ab;
    if (ab2 < eps) return ap.len();
    ld t = (ap * ab) / ab2;
    t = std::max<ld>(0, std::min<ld>(1, t));
    return dis(p, a + ab * t);
}

ld pointPlaneDis(P3 p, P3 A, P3 B, P3 C) {
    P3 n = (vec3(A, B) ^ vec3(A, C));
    ld den = n.len();
    if (den < eps) return 0;
    return fabs1(vec3(A, p) * n) / den;
}

// projection of p onto plane (A,B,C)
P3 projPointPlane(P3 p, P3 A, P3 B, P3 C) {
    P3 n = (vec3(A, B) ^ vec3(A, C));
    ld nn = n * n;
    if (nn < eps) return p;
    ld t = (vec3(A, p) * n) / nn;
    return p - n * t;
}

// reflection of p across plane (A,B,C)
P3 reflectPointPlane(P3 p, P3 A, P3 B, P3 C) {
    P3 q = projPointPlane(p, A, B, C);
    return q * 2 - p;
}

ld angle3(P3 a, P3 b) { // [0, pi]
    ld la = a.len(), lb = b.len();
    if (la < eps || lb < eps) return 0;
    ld cs = (a * b) / (la * lb);
    cs = std::max<ld>(-1, std::min<ld>(1, cs));

```

```

    return acos1(cs);
}

// line (p1,p2) with plane (A,B,C) -> unique intersection point in 'sec'
bool linePlaneIntersection(P3 p1, P3 p2, P3 A, P3 B, P3 C, P3& sec) {
    P3 v = vec3(p1, p2);
    P3 n = (vec3(A, B) ^ vec3(A, C));
    ld denom = n * v;
    if (fabs1(denom) < eps) return false; // parallel or in-plane -> no unique
    ↪ hit
    ld t = (n * (A - p1)) / denom;
    sec = p1 + v * t;
    return true;
}

// segment [p1,p2] with plane (A,B,C) -> unique intersection in 'sec'
bool segmentPlaneIntersection(P3 p1, P3 p2, P3 A, P3 B, P3 C, P3& sec) {
    P3 v = vec3(p1, p2);
    P3 n = (vec3(A, B) ^ vec3(A, C));
    ld denom = n * v;
    if (fabs1(denom) < eps) return false;
    ld t = (n * (A - p1)) / denom;
    if (t < -eps || t > 1 + eps) return false;
    sec = p1 + v * t;
    return true;
}

// point-in-triangle in 3D (accepts points slightly off-plane within eps)
bool pointInTriangle(P3 p, P3 A, P3 B, P3 C) {
    P3 n = (vec3(A, B) ^ vec3(A, C));
    ld nl = n.len();
    if (nl < eps) return false; // degenerate triangle
    if (fabs1(vec3(A, p) * n) > eps * nl) return false; // not on plane

    P3 v0 = vec3(A, C), v1 = vec3(A, B), v2 = vec3(A, p);
    ld d00 = v0 * v0, d01 = v0 * v1, d11 = v1 * v1;
    ld d20 = v2 * v0, d21 = v2 * v1;
    ld denom = d00 * d11 - d01 * d01;
    if (fabs1(denom) < eps) return false;

    ld u = (d11 * d20 - d01 * d21) / denom;
    ld v = (d00 * d21 - d01 * d20) / denom;
    return u >= -eps && v >= -eps && u + v <= 1 + eps;
}

```

4.9 Intersections

// two segments

*// To check if two segments intersect we will use the * signed area of the ABC
 ↪ triangle. This can be derived * from the cross product of the vectors AB
 ↪ and AC.*

```

bool intersect(Segment a, Segment b)
{
    Point p1 = { a.xi, a.yi }, p2 = { a.xf, a.yf }, p3 = { b.xi, b.yi }, p4 = {
    ↪ b.xf, b.yf };

    return ((p4 - p1) ^ (p2 - p1)) * ((p2 - p1) ^ (p3 - p1)) >= 0 &&
        ((p2 - p3) ^ (p4 - p3)) * ((p4 - p3) ^ (p1 - p3)) >= 0 &&
        max(p1.x, p2.x) >= min(p3.x, p4.x) && max(p3.x, p4.x) >= min(p1.x, p2.x)
    ↪ &&
        max(p1.y, p2.y) >= min(p3.y, p4.y) && max(p3.y, p4.y) >= min(p1.y, p2.y);
}

```

4.10 Lattice Points

```

long long getLatticeBoundaryPoints(vector<P>& p)
{
    long long boundary = 0;
    p.push_back(p[0]);
    for (int i = 0; i < p.size() - 1; i++)
    {
        P a = vec(p[i], p[i + 1]);
        boundary += __gcd(abs((int)a.x), abs((int)a.y));
    }
    p.pop_back();
    return boundary;
}

long long getLatticeInsidePoints(vector<P>& p)
{
    return (getAreat2(p) - getLatticeBoundaryPoints(p)) / 2 + 1;
}

```

4.11 Polygon Centroid

```

P getCentroid(vector<P>& p)
{
    ld x, y;
    long long tarea = 0;
    x = 0;
    y = 0;
    for (int i = 1; i < p.size() - 2; i++)
    {
        long long area = (vec(p[0], p[i]) ^ vec(p[0], p[i + 1]));
        x += area * ((p[0].x + p[i].x + p[i + 1].x) / 3.0);
        y += area * ((p[0].y + p[i].y + p[i + 1].y) / 3.0);
        tarea += area;
    }
    x /= tarea;
    y /= tarea;
    return { x, y };
}

```

4.12 some Properties of Regular polygons

Properties of Regular polygons

Some of the properties of regular polygons are listed below.

All the sides of a regular polygon are equal
 All the interior angles are equal
 The perimeter of a regular polygon with n sides is equal to the n times of a
 → side measure.
 The sum of all the interior angles of a simple n -gon or regular polygon = $(n - 2) \times 180^\circ$
 → $2) \times 180^\circ$
 The number of diagonals in a polygon with n sides = $n(n - 3)/2$
 The number of triangles formed by joining the diagonals from one corner of a
 → polygon = $n - 2$
 The measure of each interior angle of n -sided regular polygon = $[(n - 2) \times 180^\circ] / n$
 → $180^\circ / n$
 The measure of each exterior angle of an n -sided regular polygon = $360^\circ / n$

area of regular polygon = $((l^2) * n) / (4 \tan(\pi/n))$
 l is the side length

n is the number of sides

5 Graph

5.1 Articulation Points Kareem

```

//undirected
vector<int>adj[N];
int dfn[N],low[N];
set<int>points;
int cnt;
void articulationPoint(int node, int parent){
    dfn[node] = low[node] = ++cnt;
    int childs = 0;
    for(auto&ch : adj[node]){
        if(ch == parent)continue;
        if(dfn[ch] == -1){
            articulationPoint(ch, node);
            low[node] = min(low[node],low[ch]);
            if(dfn[node]<=low[ch]&& ~parent)points.insert(node);
            childs++;
        }else{
            low[node] = min(low[node],dfn[ch]);
        }
    }
    if(childs > 1 && parent == -1)points.insert(node);
}

```

5.2 Articulation Points Reda

```

#define vi vector<int>
#define vvi vector<vector<int>>
#define vsi vector<set<int>>
//SCC

```

```

vvi G;
vi dnum, dlow, pr;
set<int> arc_point;

int dfsroot, cntroot, id, n;
void articulation_points(int node)
{
    if (dnum[node] != -1) return;
    dnum[node] = dlow[node] = ++id;
    for (auto u : G[node])
    {
        if (dnum[u] == -1)
        {
            pr[u] = node;
            articulation_points(u);
            if (dnum[node] <= dlow[u])
                if (node == dfsroot)
                    cntroot++;
                else
                    arc_point.insert(node);
            dlow[node] = min(dlow[node], dlow[u]);
        }
        else if (u != pr[node])
        {
            dlow[node] = min(dlow[node], dnum[u]);
        }
    }
}

void solve()
{
    dlow = pr = vi(n + 1);
    dnum = vi(n + 1, -1);
    id = 0;
    arc_point.clear();
    G = vvi(n + 1);
    // input graph
    for (int i = 0; i < n; i++)
    {
        dfsroot = i;
        cntroot = 0;
        articulation_points(i);
        if (cntroot > 1)
            arc_point.insert(i);
    }
}

```

5.3 Bellmanford

```

struct edge {
    int from, to, weight;

    edge() { from = to = weight = 0; }

    edge(int from, int to, int weight) :

```



```

        from(from), to(to), weight(weight) {
    }

    bool operator<(const edge &other) const {
        return weight > other.weight;
    }
};

vector<edge> edgeList;

//O(V*E)
void bellmanford(int n, int src, int dest = -1) {
    vector<int> dis(n + 1, oo), prev(n + 1, -1);
    dis[src] = 0;
    bool negativeCycle = false;
    int last = -1, tmp = n;
    while (tmp--) {
        last = -1;
        for (edge e: edgeList)
            if (dis[e.to] > dis[e.from] + e.weight) {
                dis[e.to] = dis[e.from] + e.weight;
                prev[e.to] = e.from;
                last = e.to;
            }
        if (last == -1)
            break;
        if (tmp == 0)
            negativeCycle = true;
    }
    if (last != -1) {
        for (int i = 0; i < n; i++)
            last = prev[last];
        vector<int> cycle;
        for (int cur = last; cur != last || cycle.size() > 1; cur =
            prev[cur])
            cycle.push_back(cur);
        reverse(cycle.begin(), cycle.end());
    }
    vector<int> path;
    while (dest != -1) {
        path.push_back(dest);
        dest = prev[dest];
    }
    reverse(path.begin(), path.end());
}

```

5.4 Bridges Kareem

```

//undirected
vector<int>adj[N];
int dfn[N],low[N],timer;
void bridges(int node,int parent){
    dfn[node] = low[node] = ++timer;
    for(auto&ch : adj[node]){

```

```

    if(ch == parent)continue;
    if(dfn[ch] == -1){
        bridges(ch,node);
        low[node] = min(low[node],low[ch]);
        if(dfn[node] < low[ch]){
            // is_bridge
        }
    }else{
        low[node] = min(low[node],dfn[ch]);
    }
}
}

```

5.5 Bridges Reda

```

vsi G;
vi dn, dlow, pr;
int id = 0, n;
set<pair<int, int>> out;
void bridges(int node)
{
    if (dn[node] != -1)
        return;
    dn[node] = dlow[node] = ++id;
    for (auto u : G[node])
    {
        if (dn[u] == -1)
        {
            pr[u] = node;
            bridges(u);
            if (dn[node] < dlow[u])
                out.insert({ min(node, u), max(node, u) });
            dlow[node] = min(dlow[node], dlow[u]);
        }
        else if (u != pr[node])
        {
            dlow[node] = min(dlow[node], dn[u]);
        }
    }
}

void solve()
{
    out.clear();
    dlow = vi(n + 1);
    dn = pr = vi(n + 1, -1);
    G = vsi(n + 1);
    // input graph
    for (int i = 0; i < n; i++)if (dn[i] == -1)bridges(i);
    // out -> set with all bridges
}

```

5.6 Euler tour

```
void euler(vector<vector<int>> &adjMax, vector<int> &ret,
           int n, int i, bool isDirected = false)
{
    for (int j = 0; j < n; j++)
    {
        if (adjMax[i][j])
        {
            adjMax[i][j]--;
            if (!isDirected)
                adjMax[j][i]--;
            euler(adjMax, ret, n, j, isDirected);
        }
    }
    ret.push_back(i);
}
```

5.7 Tarjan SCC Reda

//TARJAN

```
#define vi vector<int>
#define vvi vector<vector<int>>
#define usi vector<set<int>>
//SCC
int n, m;
vvi G;
vi dn, dlow, onstack;
stack<int> st;
int id;
void tarjan(int node)
{
    if (~dn[node]) return;
    ++id;
    dn[node] = dlow[node] = id;
    onstack[node] = 1;
    st.push(node);
    for (auto u : G[node])
    {
        if (dn[u] == -1)
        {
            tarjan(u);
            dlow[node] = min(dlow[node], dlow[u]);
        }
        if (onstack[u])
            dlow[node] = min(dlow[node], dlow[u]);
    }
    if (dlow[node] == dn[node])
    {
        int u = -1;
        while (u != node)
        {
            u = st.top();
        }
    }
}
```

```

        st.pop();
        onstack[u] = 0;
        dlow[u] = dlow[node];
    }
}
}
void solve()
{
    cin >> n >> m;
    st = stack<int>();
    G = vvi(n + 1);
    id = 0;
    dn = vi(n + 2, -1);
    onstack = dlow = vi(n + 2);

    // input graph
    for (int i = 1; i <= n; i++) if (dn[i] == -1) tarjan(i);
    // same dlow value means on same cycle
}

```

6 Math

6.1 Combinatorics

```

/*
 *  $nCr = n! / ((n-r)! * r!)$ 
 *  $nCr(n, r) = nCr(n, n-r)$ 
 *  $nPr = n! / (n-r)!$ 
 *  $nPr(circle) = nPr / r$ 
 *  $nCr(n, r) = pascal[n][r]$ 
 *  $catalan[n] = nCr(2n, n) / (n+1)$ 
 */
ull nCr(int n, int r) {
    if (r > n)
        return 0;
    r = max(r, n - r);
    ull ans = 1, div = 1, i = r + 1;
    while (i <= n) {
        ans *= i++;
        ans /= div++;
    }
    return ans;
}

ull nPr(int n, int r) {
    if (r > n)
        return 0;
    ull p = 1, i = n - r + 1;
    while (i <= n)
        p *= i++;
    return p;
}

```

```

// return catalan number n-th using dp  $O(n^2)$ //max = 35 then overflow
vector<ull> catalanNumber(int n) {
    vector<ull> catalan(n + 1);
    catalan[0] = catalan[1] = 1;
    for (int i = 2; i <= n; i++) {
        ull &rt = catalan[i];
        for (int j = 0; j < n; j++)
            rt += catalan[j] * catalan[n - j - 1];
    }
    return catalan;
}

// count number of paths in matrix n*m // go to right or down only
ull countNumberOfPaths(int n, int m) {
    return nCr(n + m - 2, n - 1);
}

```

6.2 Equations

```

//  $(a^n) \% p = \text{result}$ , return minimum n
int getPower(int a, int result, int mod) {
    int sq = sqrt(mod);
    map<int, int> mp;
    ll r = 1;
    for (int i = 0; i < sq; i++) {
        if (mp.find(r) == mp.end())
            mp[r] = i;
        r = (r * a) % mod;
    }
    ll tmp = modInverse(r, mod);
    ll cur = result;
    for (int i = 0; i <= mod; i += sq) {
        if (mp.find(cur) != mp.end())
            return i + mp[cur];
        cur = (cur * tmp) % mod; //val/(a^sq)
    }
    return INF;
}

// need testing
// return  $a^1 + a^2 + a^3 + \dots + a^k$ 
ll sumPower(ll a, ll k, int mod) {
    if (k == 1) return a % mod;
    ll half = sumPower(a, k / 2, mod);
    ll p = half * power(a, k / 2, mod) % mod;
    p = (p + half) % mod;
    if (k & 1) p = (p + power(a, k, mod)) % mod;
    return p;
}

// same function but faster (not tested)
int calci_xpi(int x, int n)
{
    int p1 = fix(fix(x * (1 - (modInv(Bpow(x, n)))))) * modInv((x - 1) * (x -
    ↪ 1)));
    int p2 = fix(n * fix(modInv((x - 1) * Bpow(x, n))));
}

```

```

    return fix(p1 - p2);
}
//return sum of sequence a, a+x , a+2x .... b(not tested)
ll sumSequence(ll a, ll b, ll x) {
    a = ((a + x - 1) / x) * x;
    b = (b / x) * x;
    return (b + a) * (b - a + x) / (2 * x);
}

```

6.3 Fast Power

```

ll fpow(ll x, ll n, int mod) {
    if (n == 0) return 1 % mod;
    if (n == 1) return x % mod;
    ll ans = fpow(x, n / 2, mod);
    ans = ans * ans % mod;
    if (n & 1) ans = ans * (x % mod) % mod;
    return ans;
}

// iterative
ll fpow(ll x, ll k, ll mod) {
    ll res = 1;
    for (x %= mod; k; k >>= 1, x = x * x % mod)
        if (k & 1) res = res * x % mod;
    return res;
}

// minimal
ll fast(ll b, ll e){
    if(!e) return 1;
    return fast(b * b % mod, e >> 1) * ((e&1) ? b : 1) % mod;
}

ll modInverse(ll b, ll mod) { // if mod is Prime
    return power(b, mod - 2, mod);
}
**if mod is not Prime,gcd(a,b) must be equal 1
ll modInverse(ll b, ll mod) {
    return power(b, phi_function(mod) - 1, mod);
}

```

6.4 Gauss Xor

```

// problem link : https://codeforces.com/gym/101908/problem/M
const int N = 2005;

class Gauss {
    const int INF = 2;
    const double EPS = 1E-9;
public:
    //this code finds lexicographically largest solution

```

```

//n is number of eq ,m is number of variables
// xor gauss (mod 2)
//  $x_1 \wedge (\neg x_2) \wedge (x_3) = 1 \rightarrow (x_1 \wedge (1 \wedge x_2) \wedge x_3 = 1) \quad (x_1 \wedge x_2 \wedge x_3 = 0)$ 
int gauss(vector<bitset<N>> a, int n, int m, bitset<N> &ans) {
    vector<int> where(m, -1);
    // to make it minimum lexicographically Three Modifications
    // Modification 1: reverse col iteration ( left to right)
    for (int col = m - 1, row = 0; col >= 0 && row < n; col--) {
        for (int i = row; i < n; ++i) {
            if (a[i][col]) {
                swap(a[i], a[row]);
                break;
            }
        }
        if (!a[row][col])
            continue;

        where[col] = row;

        for (int i = 0; i < n; ++i) {
            if (i != row && a[i][col])
                a[i] ^= a[row]; // XOR the rows
        }
        ++row;
    }

    ans.reset();
    //Modification 2: reverse i iteration (right to left)
    for (int i = 0; i < m; ++i) {
        if (where[i] != -1) {
            int r = where[i];
            bool sum = 0;
            for (int j = 0; j < i; ++j) {
                sum ^= (a[r][j] & ans[j]);
            }
            ans[i] = (a[r][m] ^ sum);
        } else {
            // Modification 3 : if is free set it to 0
            ans[i] = 1;
        }
    }

    for (int i = 0; i < n; ++i) {
        bool sum = 0;
        for (int j = 0; j < m; ++j)
            sum ^= (ans[j] & a[i][j]); // XOR the known values
        if (sum != a[i][m])
            return 0; // No solution
    }

    for (int i = 0; i < m; ++i)
        if (where[i] == -1)
            return INF; // Infinite solutions

```

```

        return 1; // Unique solution
    }
};

void solve() {
    int n, m;
    cin >> n >> m;
    vector<bitset<N>> a(n);
    for (int i = 0; i < n; i++) a[i].set(m);
    cin.ignore();
    for (int i = 0; i < n; i++) {
        string s;
        getline(cin, s);
        s.pop_back();
        if (i + 1 < n) {
            s.pop_back();
            s.pop_back();
            s.pop_back();
            s.pop_back();
        }
        s.erase(s.begin());
        stringstream ss(s);
        while (ss >> s) {
            if (s == "or") continue;
            if (s == "not") a[i].flip(m);
            else {
                int num = stoi(s.substr(1)) - 1;
                a[i].flip(num);
            }
        }
    }

    Gauss gs;
    bitset<N> ans;
    int rt = gs.gauss(a, n, m, ans);
    if (rt == 0) cout << "impossible\n";
    else {
        for (int i = 0; i < m; i++) {
            if (ans[i]) cout << "T";
            else cout << "F";
        }
        LL;
    }
}

```

6.5 Gauss

```

class Gauss {
    const int INF = 2;
    const double EPS = 1E-9;
public:
    int gauss(vector<vector<double> > a, vector<double> &ans) {
        int n = (int) a.size();
    }
}

```



```

    int m = (int) a[0].size() - 1;

    vector<int> where(m, -1);
    for (int col = 0, row = 0; col < m && row < n; ++col) {
        int sel = row;
        for (int i = row; i < n; ++i)
            if (abs(a[i][col]) > abs(a[sel][col]))
                sel = i;
        if (abs(a[sel][col]) < EPS)
            continue;
        for (int i = col; i <= m; ++i)
            swap(a[sel][i], a[row][i]);
        where[col] = row;

        for (int i = 0; i < n; ++i)
            if (i != row) {
                double c = a[i][col] / a[row][col];
                for (int j = col; j <= m; ++j)
                    a[i][j] -= a[row][j] * c;
            }
        ++row;
    }

    ans.assign(m, 0);
    for (int i = 0; i < m; ++i)
        if (where[i] != -1)
            ans[i] = a[where[i]][m] / a[where[i]][i];
    for (int i = 0; i < n; ++i) {
        double sum = 0;
        for (int j = 0; j < m; ++j)
            sum += ans[j] * a[i][j];
        if (abs(sum - a[i][m]) > EPS)
            return 0;
    }

    for (int i = 0; i < m; ++i)
        if (where[i] == -1)
            return INF;
    return 1;
}

int gaussWithMod(vector<vector<ll>> a, vector<ll> &ans, ll p) {
    int n = (int) a.size();
    int m = (int) a[0].size() - 1;

    vector<int> where(m, -1);
    for (int col = 0, row = 0; col < m && row < n; ++col) {
        int sel = row;
        for (int i = row; i < n; ++i)
            if (a[i][col] > a[sel][col])
                sel = i;
        if (a[sel][col] == 0)
            continue;

```

```

    for (int i = col; i <= m; ++i)
        swap(a[sel][i], a[row][i]);
    where[col] = row;

    ll inv = modInverse(a[row][col], p);
    for (int i = 0; i < n; ++i) {
        if (i != row && a[i][col] != 0) {
            ll c = a[i][col] * inv % p;
            for (int j = col; j <= m; ++j) {
                a[i][j] = (a[i][j] - a[row][j] * c % p + p) % p;
            }
        }
    }
    ++row;
}

ans.assign(m, 0);
for (int i = 0; i < m; ++i)
    if (where[i] != -1) {
        ll inv = modInverse(a[where[i]][i], p);
        ans[i] = (a[where[i]][m] * inv) % p;
    }

for (int i = 0; i < n; ++i) {
    ll sum = 0;
    for (int j = 0; j < m; ++j)
        sum = (sum + ans[j] * a[i][j]) % p;
    if (sum != a[i][m])
        return 0; // No solution
}

for (int i = 0; i < m; ++i)
    if (where[i] == -1)
        return INF; // Infinite solutions

return 1; // Unique solution
}

int gauss(vector<bitset<N>> a, int n, int m, bitset<N> &ans) {
    vector<int> where(m, -1);
    for (int col = 0, row = 0; col < m && row < n; ++col) {
        for (int i = row; i < n; ++i) {
            if (a[i][col]) {
                swap(a[i], a[row]);
                break;
            }
        }
        if (!a[row][col])
            continue;

        where[col] = row;

```

```

        for (int i = 0; i < n; ++i) {
            if (i != row && a[i][col])
                a[i] ^= a[row]; // XOR the rows
        }
        ++row;
    }

    ans.reset();
    for (int i = 0; i < m; ++i)
        if (where[i] != -1)
            ans[i] = a[where[i]][m];

    for (int i = 0; i < n; ++i) {
        bool sum = 0;
        for (int j = 0; j < m; ++j)
            sum ^= (ans[j] & a[i][j]); // XOR the known values
        if (sum != a[i][m])
            return 0; // No solution
    }

    for (int i = 0; i < m; ++i)
        if (where[i] == -1)
            return INF; // Infinite solutions

    return 1; // Unique solution
}

int compute_rank(vector<vector<double>> A) {
    int n = A.size();
    int m = A[0].size();

    int rank = 0;
    vector<bool> row_selected(n, false);
    for (int i = 0; i < m; ++i) {
        int j;
        for (j = 0; j < n; ++j) {
            if (!row_selected[j] && abs(A[j][i]) > EPS)
                break;
        }
        if (j != n) {
            ++rank;
            row_selected[j] = true;
            for (int p = i + 1; p < m; ++p)
                A[j][p] /= A[j][i];
            for (int k = 0; k < n; ++k) {
                if (k != j && abs(A[k][i]) > EPS) {
                    for (int p = i + 1; p < m; ++p)
                        A[k][p] -= A[j][p] * A[k][i];
                }
            }
        }
    }
}

```

```

    return rank;
}
};

```

6.6 Linear Diophantine Equation CRT

```

ll exgcd(ll a,ll b, ll &x, ll &y){
    if (a<0||b<0){
        ll g=exgcd(abs(a),abs(b),x,y);
        if (a<0)x*=-1;
        if (b<0)y*=-1;
        return g;
    }
    if (b == 0){
        x=1,y=0;
        return a;
    }
    ll g= exgcd(b,a%b,y,x);
    y-=(a/b)*x;
    return g;
}
ll ldioaph(ll a,ll b, ll c,ll &x,ll &y, bool &found){
    ll g=exgcd(a,b,x,y);
    if (c%g){
        found=false;
        return g;
    }
    found=true;
    x*=c/g;
    y*=c/g;
    return g;
}
pair<ll,ll>CRT(const vector<ll>&a, const vector<ll>&m){
    ll rem=a[0],mod=m[0];
    int n=a.size();
    for (int i=1;i<n;i++){
        ll x,y;
        bool found=0;
        ll g= ldioaph(mod,-m[i],a[i]-rem,x,y,found);

        if (!found)
            return {-1,-1};
        rem+=mod*x;
        mod=mod/g*m[i];
        rem=(rem%mod+mod)%mod;
    }
    return {rem,mod};
}

```

6.7 Lucas Theorem

```

int N = 1e6 + 3, mod = 1e6 + 3;
// pre in O(mod),

```

```

struct combi
{
    int n;
    vector<int> facts, finvs, invs;
    combi(int _n) : n(_n), facts(_n), finvs(_n), invs(_n)
    {
        facts[0] = finvs[0] = 1;
        invs[1] = 1;
        for (int i = 2; i < n; i++)
        {
            invs[i] = 1LL * invs[mod % i] * (mod - mod / i) % mod;
        }
        for (int i = 1; i < n; i++)
        {
            facts[i] = 1LL * facts[i - 1] * i % mod;
            finvs[i] = 1LL * finvs[i - 1] * invs[i] % mod;
        }
    }
    inline int ncr(int x, int y)
    {
        if (y > x || y < 0) return 0;
        return 1LL * facts[x] * finvs[y] % mod * finvs[x - y] % mod;
    }
};

combi C(N);
// Computes nCr % mod using Lucas' Theorem when mod is a prime
int lucas(ll n, ll r)
{
    if (r > n) return 0;
    if (n < mod) return C.ncr(n, r);
    return 1LL * lucas(n / mod, r / mod) * lucas(n % mod, r % mod) % mod;
}

```

6.8 Matrix power

```

// const int M = 2;
// typedef array<array<int, M>, M> matrix;

int mod = 1e9+7;
class matrix{
public:
    vector<vector<ll>>>v;
    int n;
    matrix(int sz1){
        n = sz1;
        v = vector<vector<ll>>>(n, vector<ll>(n));
    }
    matrix operator *(const matrix&a){
        matrix res(n);
        for(int i=0;i<n;i++){
            for(int k=0;k<n;k++){
                //if(v[i][k] == 0)continue;
                for(int j=0;j<n;j++){
                    res.v[i][j] += v[i][k] * a.v[k][j];
                }
            }
        }
    }
};

```

```

        res.v[i][j]%=mod;
    }
}
return res;
}
void ones(){
    for(int i=0;i<n;i++)v[i][i] = 1;
}
};
matrix mpow(matrix a,ll k){
    matrix ans(a.n);
    ans.ones();
    while(k){
        if(k&1){
            ans = ans*a;
        }
        a = a*a;
        k>>=1;
    }
    return ans;
}

```

6.9 MillerRabin

```

// n < 4,759,123,141      3 : 2, 7, 61
// n < 1,122,004,669,633  4 : 2, 13, 23, 1662803
// n < 3,474,749,660,383  6 : pirmses <= 13
// n < 2^64               7 :
// 2, 325, 9375, 28178, 450775, 9780504, 1795265022
// Make sure testing integer is in range [2, n-2] if
//The largest known gap between consecutive primes 1e9 is 282, 1e12 1132
using u64 = uint64_t;
using u128 = __uint128_t;
u64 binpower(u64 base, u64 e, u64 mod) {
    u64 result = 1;
    base %= mod;
    while (e) {
        if (e & 1)
            result = (u128) result * base % mod;
        base = (u128) base * base % mod;
        e >>= 1;
    }
    return result;
}
bool check_composite(u64 n, u64 a, u64 d, int s) {
    u64 x = binpower(a, d, n);
    if (x == 1 || x == n - 1)
        return false;
    for (int r = 1; r < s; r++) {
        x = (u128) x * x % n;
        if (x == n - 1)
            return false;
    }
}

```

```

    return true;
}
bool MillerRabin(u64 n) { // returns true if n is prime, else returns false.
    if (n < 2)
        return false;

    int r = 0;
    u64 d = n - 1;
    while ((d & 1) == 0) {
        d >>= 1;
        r++;
    }

    for (int a: {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37}) {
        if (n == a)
            return true;
        if (check_composite(n, a, d, r))
            return false;
    }
    return true;
}

```

6.10 Mobius Function

```

const int N = 2e6 + 10, MOD = 1e9 + 7;
int mob[N];
bool prime[N];
void mobius() {
    // fix this ya 3amy @abdosa3d
    memset(mob, 1, sizeof mob);
    memset(prime + 2, 1, sizeof(prime) - 2);
    mob[0] = 0;
    mob[2] = -1;
    for (int i = 4; i < N; i += 2) {
        // fix this too
        mob[i] *= (i & 3) ? -1 : 0;
        prime[i] = 0;
    }
    for (int i = 3; i < N; i += 2)
        if (prime[i]) {
            mob[i] = -1;
            for (int j = 2 * i; j < N; j += i) {
                mob[j] *= (j % (1LL * i * i)) ? -1 : 0;
                prime[j] = 0;
            }
        }
}

```

```

const int N = 4e7 + 10;
char mu[N];
vector<bool> comp(N);

void mobius_linear() {

```

```

vector<int> ps;
ps.reserve(N / 10);
mu[1] = 1;
for (int i = 2; i < N; ++i) mu[i] = 0; // optional, will be set

for (int i = 2; i < N; ++i) {
    if (!comp[i]) {
        ps.push_back(i);
        mu[i] = -1;
    }
    for (int p: ps) {
        long long v = 1LL * i * p;
        if (v >= N) break;
        comp[v] = true;
        if (i % p == 0) {
            mu[v] = 0;
            break;
        } // square divides
        mu[v] = -mu[i];
    }
}
}

```

6.11 NCR Preprocessing

```

const int N = 1e6 + 100;
const int mod = 1e9 + 7;
ll fact[N];
ll inv[N]; //mod inverse for i
ll invfact[N]; //mod inverse for i!
void factInverse() {
    fact[0] = inv[1] = fact[1] = invfact[0] = invfact[1] = 1;
    for (long long i = 2; i < N; i++) {
        fact[i] = (fact[i - 1] * i) % mod;
        inv[i] = mod - (inv[mod % i] * (mod / i) % mod);
        invfact[i] = (inv[i] * invfact[i - 1]) % mod;
    }
}

ll nCr(int n, int r) {
    if (r > n) return 0;
    return (((fact[n] * invfact[r]) % mod) * invfact[n - r]) %
        mod;
}

```

6.12 Phi

```

const int N=1e6+5;
int phi[N];
void pre(){
    for (int i=0;i<N;i++)
        phi[i]=i;
    for (int i=2;i<N;i++){

```



```

        if (phi[i]==i){
            for (int j=i;j<N;j+=i)
                phi[j]-=phi[j]/i;
        }
    }

}

11 phi(ll n){
    ll p_to_k, relative_primes=1;
    for (ll i=2,d=1;i*i<=n;i+=d,d=2){
        if (!(n%i)){
            p_to_k=1;
            while(!(n%i)){
                p_to_k*=i,n/=i;
            }
            relative_primes*=(p_to_k/i)*(i-1);

        }

    }
    if (n!=1){
        relative_primes*=(n-1);
    }
    return relative_primes;
}

11 phi(ll n) {
    ll result = n;
    for (ll i = 2; i * i <= n; i++) {
        if (n % i == 0) {
            while (n % i == 0)
                n /= i;
            result -= result / i;
        }
    }
    if (n > 1)
        result -= result / n;
    return result;
}

```

6.13 Sieve w e5wato

```

get prime factors using sieve (less than sqrt(n))
vector<int> prime_fact(int n)
{
    vector<int>temp;
    for (int i = 0;primes[i] * 1LL * primes[i] <= n;i++)
    {
        while (n % primes[i] == 0)
            temp.push_back(primes[i]), n /= primes[i];
    }
    if (n > 1)temp.push_back(n);
    return temp;
}

```

```

}

segmented_sieve --> get primes in range ex(1e9:1e9+1e6) o[(r-1)*loglog(r)+
↪ o(sieve)]
r
const int N=1e5+5;
bool composite[N];
void segmented_sieve()
{
    for(auto i:primes)
    {
        for(int j=max(i*i,(1+i-1)/i*i);j<=r;j+=i)
            composite[j-1]=1; //
    }
    if(1==1)composite[0]=1;
}

//Linear Sieve
const int N = 1e7;
int lpf[N + 1];
vector<int> prime;

void sieve() {
    for (int i = 2; i <= N; i++) {
        if (lpf[i] == 0) {
            lpf[i] = i;
            prime.push_back(i);
        }
        for (int j: prime) {
            if (j > lpf[i] || 1LL * i * j > N)break;
            lpf[i * j] = j;
        }
    }
}

```

6.14 SieveUpTo1e9

```

//about 5e7 primes up to 1e9
vector<int> sieve(const int N = int(1e9), const int Q = 17, const int L = 1 <<
↪ 15) {
    static const int rs[] = {1, 7, 11, 13, 17, 19, 23, 29};
    struct P {
        P(int p) : p(p) {}
        int p;
        int pos[8];
    };
    auto approx_prime_count = [](const int N) -> int {
        return N > 60184 ? N / (log(N) - 1.1) : max(1., N / (log(N) - 1.11)) +
↪ 1;
    };
    const int v = sqrt(N), vv = sqrt(v);
    vector<bool> isp(v + 1, true);
    for (int i = 2; i <= vv; ++i)
        if (isp[i]) {

```

```

        for (int j = i * i; j <= v; j += i)
            isp[j] = false;
    }
    const int rsize = approx_prime_count(N + 30);
    vector<int> primes = {2, 3, 5};
    int psize = 3;
    primes.resize(rsize);
    vector<P> sprimes;
    size_t pbeg = 0;
    int prod = 1;
    for (int p = 7; p <= v; ++p) {
        if (!isp[p]) continue;
        if (p <= Q) prod *= p, ++pbeg, primes[psize++] = p;
        auto pp = P(p);
        for (int t = 0; t < 8; ++t) {
            int j = (p <= Q) ? p : p * p;
            while (j % 30 != rs[t]) j += p << 1;
            pp.pos[t] = j / 30;
        }
        sprimes.push_back(pp);
    }
    vector<unsigned char> pre(prod, 0xFF);
    for (size_t pi = 0; pi < pbeg; ++pi) {
        auto pp = sprimes[pi];
        const int p = pp.p;
        for (int t = 0; t < 8; ++t) {
            const unsigned char m = ~(1 << t);
            for (int i = pp.pos[t]; i < prod; i += p) pre[i] &= m;
        }
    }
    const int block_size = (L + prod - 1) / prod * prod;
    vector<unsigned char> block(block_size);
    unsigned char *pblock = block.data();
    const int M = (N + 29) / 30;
    for (int beg = 0; beg < M; beg += block_size, pblock += block_size) {
        int end = min(M, beg + block_size);
        for (int i = beg; i < end; i += prod) {
            copy(pre.begin(), pre.end(), pblock + i);
        }
        if (beg == 0) pblock[0] &= 0xFE;
        for (size_t pi = pbeg; pi < sprimes.size(); ++pi) {
            auto &pp = sprimes[pi];
            const int p = pp.p;
            for (int t = 0; t < 8; ++t) {
                int i = pp.pos[t];
                const unsigned char m = ~(1 << t);
                for (; i < end; i += p) pblock[i] &= m;
                pp.pos[t] = i;
            }
        }
        for (int i = beg; i < end; ++i) {
            for (int m = pblock[i]; m > 0; m &= m - 1) {
                primes[psize++] = i * 30 + rs[__builtin_ctz(m)];
            }
        }
    }

```

```

    }
}
assert(psize <= rsize);
while (psize > 0 && primes[psize - 1] > N)--psize;
primes.resize(psize);
return primes;
}

```

6.15 SumRangeDivisors

```

// return sum of divisors for all number from 1 to n //O(n)
ll sumRangeDivisors(int n) {
    ll ans = 0;

    for (int x = 1; x <= n; x++)
        ans += (n / x) * x;
    return ans;
}
// calc 1e9 in 42ms, can calc more but need big integer
ll sumRangeDivisors(ll x) {
    ll ans = 0, left = 1, right;
    for (; left <= x; left = right + 1) {
        right = x / (x / left);
        ans += (x / left) * (left + right) * (right - left + 1) / 2;
    }
    return ans;
}

```

6.16 FFT w e5wato

6.16.1 FFT Iterative

```

const double PI = acos(-1);
typedef complex<double> cd;

void fft(vector<cd> &a, bool invert) {
    int n = a.size();
    // bit reversal permutation
    for (int i = 0, j = 0; i < n; i++) {
        if (i < j) swap(a[i], a[j]);
        int bit = n >> 1;
        for (; j & bit; bit >>= 1) j ^= bit;
        j ^= bit;
    }
    for (int ln = 2; ln <= n; ln <= 1) {
        double angle = 2 * PI / ln;
        cd wln(cos(angle), sin(angle) * (invert ? -1 : 1));
        for (int j = 0; j < n; j += ln) {
            cd w(1);
            for (int i = 0; i < ln / 2; i++) {
                cd temp = a[i + j];
                a[i + j] = a[i + j] + w * a[i + j + ln / 2];
                a[i + j + ln / 2] = temp - w * a[i + j + ln / 2];
            }
        }
    }
}

```

```

        w *= wln;
        if (invert) {
            a[i + j] /= 2;
            a[i + j + ln / 2] /= 2;
        }
    }
}
}
}
vector<ll> mul(vector<ll> &a, vector<ll> &b) {
    int n = 1;
    while (n < a.size() + b.size()) n <<= 1;
    vector<cd> fa(all(a)), fb(all(b));
    fa.resize(n);
    fb.resize(n);
    fft(fa, 0);
    fft(fb, 0);
    for (int i = 0; i < n; i++) {
        fa[i] *= fb[i];
    }
    fft(fa, 1);
    vector<ll> res(n);
    for (int i = 0; i < n; i++) {
        res[i] = round(fa[i].real());
    }
    return res;
}

```

6.16.2 FFT MOD

```

#define rep(aa, bb, cc) for(int aa = bb; aa < cc; aa++)
#define sz(a) (int)a.size()
#define vi vector<int>
typedef complex<double> C;
typedef vector<double> vd;
void fft(vector<C> &a) {
    int n = sz(a), L = 31 - __builtin_clz(n);
    static vector<complex<long double>> R(2, 1);
    static vector<C> rt(2, 1); // (~10% faster if double)
    for (static int k = 2; k < n; k *= 2) {
        R.resize(n);
        rt.resize(n);
        auto x = polar(1.0L, acos(-1.0L) / k);
        rep(i, k, 2 * k) rt[i] = R[i] = i & 1 ? R[i / 2] * x : R[i / 2];
    }
    vi rev(n);
    rep(i, 0, n) rev[i] = (rev[i / 2] | (i & 1) << L) / 2;
    rep(i, 0, n) if (i < rev[i]) swap(a[i], a[rev[i]]);
    for (int k = 1; k < n; k *= 2)
        for (int i = 0; i < n; i += 2 * k)
            rep(j, 0, k) {
                // C z = rt[j+k] * a[i+j+k]; // (25% faster if hand-rolled)
                // include-line
            }
    }
}

```

```

        auto x = (double *) &rt[j + k], y = (double *) &a[i + j + k];
        ↪        // exclude-line
        C z(x[0] * y[0] - x[1] * y[1], x[0] * y[1] + x[1] * y[0]);
        ↪        // exclude-line
        a[i + j + k] = a[i + j] - z;
        a[i + j] += z;
    }
}

template<int M>
vi convMod(const vi &a, const vi &b) {
    if (a.empty() || b.empty()) return {};
    vi res(sz(a) + sz(b) - 1);
    int B = 32 - __builtin_clz(sz(res)), n = 1 << B, cut = int(sqrt(M));
    vector<C> L(n), R(n), outs(n), outl(n);
    rep(i, 0, sz(a)) L[i] = C((int) a[i] / cut, (int) a[i] % cut);
    rep(i, 0, sz(b)) R[i] = C((int) b[i] / cut, (int) b[i] % cut);
    fft(L), fft(R);
    rep(i, 0, n) {
        int j = -i & (n - 1);
        outl[j] = (L[i] + conj(L[j])) * R[i] / (2.0 * n);
        outs[j] = (L[i] - conj(L[j])) * R[i] / (2.0 * n) / 1i;
    }
    fft(outl), fft(outs);
    rep(i, 0, sz(res)) {
        ll av = int64_t(real(outl[i]) + .5), cv = int64_t(imag(outs[i]) + .5);
        ll bv = int64_t(imag(outl[i]) + .5) + int64_t(real(outs[i]) + .5);
        res[i] = ((av % M * cut + bv) % M * cut + cv) % M;
    }
    return res;
}

```

6.16.3 FFT string Matching

```

using cd = complex<double>;
const double PI = acos(-1), eps = 5e-4; // If you get a wrong answer you can
↪ change the eps lower of higher till you pass

void fft(vector<cd> &a, bool invert) {
    int n = a.size();

    for (int i = 1, j = 0; i < n; i++) {
        int bit = n >> 1;
        for (; j & bit; bit >>= 1)
            j ^= bit;
        j ^= bit;

        if (i < j)
            swap(a[i], a[j]);
    }

    for (int len = 2; len <= n; len <<= 1) {
        double ang = 2 * PI / len * (invert ? -1 : 1);
        cd wlen(cos(ang), sin(ang));
    }
}

```

```

        for (int i = 0; i < n; i += len) {
            cd w(1);
            for (int j = 0; j < len / 2; j++) {
                cd u = a[i+j], v = a[i+j+len/2] * w;
                a[i+j] = u + v;
                a[i+j+len/2] = u - v;
                w *= wlen;
            }
        }
    }

    if (invert) {
        for (cd & x : a)
            x /= n;
    }
}

vector<cd> multiply(vector<cd> const& a, vector<cd> const& b) {
    vector<cd> fa(a.begin(), a.end()), fb(b.begin(), b.end());
    int n = 1;
    while (n < (int)a.size() + (int)b.size())
        n <= 1;
    fa.resize(n);
    fb.resize(n);

    fft(fa, false);
    fft(fb, false);
    for (int i = 0; i < n; i++)
        fa[i] *= fb[i];
    fft(fa, true);

    return fa;
}

void solve(int tc) {

    string s, patt; cin >> s >> patt;
    int n = (int)s.length(), m = (int)patt.length();

    vector<cd> poly1(n), poly2(m);

    for (int i = 0; i < n; ++i) {
        double angle = 2*PI*(s[i]-'a')/26;
        poly1[i] = cd(cos(angle), sin(angle));
    }
    for (int i = 0; i < m; ++i) {
        if(patt[m-i-1] == '*') poly2[i] = cd(0,0);
        else {
            double angle = 2*PI*(patt[m-i-1]-'a')/26;
            poly2[i] = cd(cos(angle), -sin(angle));
        }
    }
}

```

```

vector<cd> ans = multiply(poly1, poly2);
int wild_cnt = (int)count(patt.begin(), patt.end(), '*');

int tot = 0;
vector<int> pos;
for (int i = 0; i < n; ++i) {
    if(fabs(ans[m-1+i].real() - (m - wild_cnt)) < eps &&
↪   fabs(ans[m-1+i].imag()) < eps) {
        ++tot;
        pos.push_back(i);
    }
}

cout << tot << "\n";
for(auto & p : pos) cout << p << " ";
cout << "\n";
}

```

6.16.4 FFT

```

const double PI = acos(-1);
typedef complex<double> cd;
void fft(vector<cd>&a, bool invert){
    int n = a.size();
    if(n == 1)return;
    vector<cd>a0(n/2),a1(n/2);
    for(int i=0;i<n;i++){
        a0[i] = a[i*2];
        a1[i] = a[i*2+1];
    }
    fft(a0,invert);
    fft(a1,invert); //  $a(x) = a_0(x^2) + x * a_1(x^2)$ 
    double angle = 2*PI/n * (invert ? -1 : 1);
    cd w = 1, wn(cos(angle),sin(angle));
    for(int i=0;i<n/2;i++){
        a[i] = a0[i] + w * a1[i];
        a[i + n/2] = a0[i] - w * a1[i];
        w*= wn;
        if(invert){
            a[i]/=2;
            a[i + n/2]/=2;
        }
    }
}

vector<ll> multiply(vector<ll>&a,vector<ll>&b){
    int n = 1;
    while(n < sz(a) + sz(b))n<=1;
    vector<cd>fa(all(a)),fb(all(b));
    fa.resize(n);
    fb.resize(n);
    fft(fa,0);
    fft(fb,0);
    for(int i=0;i<n;i++){

```



```

        fa[i]*=fb[i];
    }
    fft(fa,1);
    vector<ll>res(n);
    for(int i=0;i<n;i++){
        res[i] = round(fa[i].real());
    }
    return res;
}

```

6.16.5 FWHT

```

const int mod = 1e9 + 7;

int POW(long long n, long long k) {
    int ans = 1 % mod;
    n %= mod;
    if (n < 0) n += mod;
    while (k) {
        if (k & 1) ans = (long long) ans * n % mod;
        n = (long long) n * n % mod;
        k >>= 1;
    }
    return ans;
}

const int inv2 = (mod + 1) >> 1;
#define M (1 << 20)
#define OR 0
#define AND 1
#define XOR 2

struct FWHT {
    int P1[M], P2[M];

    void wt(int *a, int n, int flag = XOR) {
        if (n == 0) return;
        int m = n / 2;
        wt(a, m, flag);
        wt(a + m, m, flag);
        for (int i = 0; i < m; i++) {
            int x = a[i], y = a[i + m];
            if (flag == OR) a[i] = x, a[i + m] = (x + y) % mod;
            if (flag == AND) a[i] = (x + y) % mod, a[i + m] = y;
            if (flag == XOR) a[i] = (x + y) % mod, a[i + m] = (x - y + mod) %
↪ mod;
        }
    }

    void iwt(int *a, int n, int flag = XOR) {
        if (n == 0) return;
        int m = n / 2;
        iwt(a, m, flag);
        iwt(a + m, m, flag);
    }
}

```

```

        for (int i = 0; i < m; i++) {
            int x = a[i], y = a[i + m];
            if (flag == OR) a[i] = x, a[i + m] = (y - x + mod) % mod;
            if (flag == AND) a[i] = (x - y + mod) % mod, a[i + m] = y;
            if (flag == XOR) a[i] = 1LL * (x + y) * inv2 % mod, a[i + m] = 1LL
↪ * (x - y + mod) * inv2 % mod;
            // replace inv2 by >>1 if not required
        }
    }

vector<int> multiply(int n, vector<int> A, vector<int> B, int flag = XOR) {
    assert(__builtin_popcount(n) == 1);
    A.resize(n);
    B.resize(n);
    for (int i = 0; i < n; i++) P1[i] = A[i];
    for (int i = 0; i < n; i++) P2[i] = B[i];
    wt(P1, n, flag);
    wt(P2, n, flag);
    for (int i = 0; i < n; i++) P1[i] = 1LL * P1[i] * P2[i] % mod;
    iwt(P1, n, flag);
    return vector<int>(P1, P1 + n);
}

vector<int> pow(int n, vector<int> A, long long k, int flag = XOR) {
    assert(__builtin_popcount(n) == 1);
    A.resize(n);
    for (int i = 0; i < n; i++) P1[i] = A[i];
    wt(P1, n, flag);
    for (int i = 0; i < n; i++) P1[i] = POW(P1[i], k);
    iwt(P1, n, flag);
    return vector<int>(P1, P1 + n);
}
} t;

```

6.16.6 NTT Time-Shift

```

const ll mod = (119 << 23) + 1, root = 3; // = 998244353
// For  $p < 2^{30}$  there is also e.g.  $5 << 25$ ,  $7 << 26$ ,  $479 << 21$ 
// and  $483 << 21$  (same root). The last two are  $> 10^9$ .
ll modpow(ll b, ll e) {
    ll ans = 1;
    for (; e; b = b * b % mod, e /= 2)
        if (e & 1) ans = ans * b % mod;
    return ans;
}

// Primitive Root of the mod of form  $2^a * b + 1$ 
int generator() {
    vector<int> fact;
    int phi = mod - 1, n = phi;
    for (int i = 2; i * i <= n; ++i)
        if (n % i == 0) {
            fact.push_back(i);
            while (n % i == 0)

```

```

        n /= i;
    }
    if (n > 1)
        fact.push_back(n);

    for (int res = 2; res <= mod; ++res) {
        bool ok = true;
        for (size_t i = 0; i < fact.size() && ok; ++i)
            ok &= modpow(res, phi / fact[i]) != 1;
        if (ok) return res;
    }
    return -1;
}

ll modpow(ll b, ll e, ll m) {
    ll ans = 1;
    for (; e; b = b * b % m, e /= 2)
        if (e & 1) ans = ans * b % m;
    return ans;
}

void ntt(vector<ll> &a) {
    int n = (int) a.size(), L = 31 - __builtin_clz(n);
    static vector<ll> rt(2, 1); // erase the static if you want to use two
    ↪ moduli;
    for (static int k = 2, s = 2; k < n; k *= 2, s++) { // erase the static if
    ↪ you want to use two moduli;
        rt.resize(n);
        ll z[] = {1, modpow(root, mod >> s, mod)};
        for (int i = k; i < 2 * k; ++i) rt[i] = rt[i / 2] * z[i & 1] % mod;
    }
    vector<int> rev(n);
    for (int i = 0; i < n; ++i) rev[i] = (rev[i / 2] | (i & 1) << L) / 2;
    for (int i = 0; i < n; ++i) if (i < rev[i]) swap(a[i], a[rev[i]]);
    for (int k = 1; k < n; k *= 2) {
        for (int i = 0; i < n; i += 2 * k) {
            for (int j = 0; j < k; ++j) {
                ll z = rt[j + k] * a[i + j + k] % mod, &ai = a[i + j];
                a[i + j + k] = ai - z + (z > ai ? mod : 0);
                ai += (ai + z >= mod ? z - mod : z);
            }
        }
    }
}

vector<ll> conv(const vector<ll> &a, const vector<ll> &b) {
    if (a.empty() || b.empty()) return {};
    int s = (int) a.size() + (int) b.size() - 1, B = 32 - __builtin_clz(s), n =
    ↪ 1 << B;
    int inv = modpow(n, mod - 2, mod);
    vector<ll> L(a), R(b), out(n);
    L.resize(n), R.resize(n);
    ntt(L), ntt(R);

```

```

    for (int i = 0; i < n; ++i) out[-i & (n - 1)] = (ll) L[i] * R[i] % mod *
↪ inv % mod;
    ntt(out);
    return {out.begin(), out.begin() + s};
}

vector<ll> polyPow(vector<ll> a, ll k) {
    vector<ll> ans = {1};
    while (k) {
        if (k & 1) {
            ans = conv(ans, a);
        }
        k >>= 1;
        a = conv(a, a);
    }
    return ans;
}

const int N = 1e6 + 100;
ll fact[N];
ll inv[N]; //mod inverse for i
ll invfact[N]; //mod inverse for i!
//call factInverse
void factInverse() {
    fact[0] = inv[1] = fact[1] = invfact[0] = invfact[1] = 1;
    for (long long i = 2; i < N; i++) {
        fact[i] = (fact[i - 1] * i) % mod;
        inv[i] = mod - (inv[mod % i] * (mod / i) % mod);
        invfact[i] = (inv[i] * invfact[i - 1]) % mod;
    }
}
//t(x) -> t(x + k) or t(x - k)
vector<ll> shift(const vector<ll> &p, ll k) {
    k %= mod;
    k += mod;
    k %= mod;

    ll n = p.size();
    vector<ll> p1(n), p2(n);
    for (int i = 0; i < n; ++i) {
        p1[i] = fact[i] * p[i] % mod;
    }

    ll curr = 1;
    for (int i = 0; i < n; ++i) {
        p2[n - i - 1] = invfact[i] * curr % mod;
        curr = curr * k % mod;
    }

    vector<ll> res = conv(p1, p2);

    vector<ll> ans;
    for (int i = n - 1; i < res.size(); ++i) {

```

```

        ans.push_back(res[i] * invfact[i - (n - 1)] % mod);
    }

    return ans;
}

```

6.16.7 NTT

```

const ll mod = (119 << 23) + 1, root = 3; // = 998244353
// For p < 2^30 there is also e.g. 5 << 25, 7 << 26, 479 << 21
// and 483 << 21 (same root). The last two are > 10^9.
ll modpow(ll b, ll e) {
    ll ans = 1;
    for (; e; b = b * b % mod, e /= 2)
        if (e & 1) ans = ans * b % mod;
    return ans;
}

// Primitive Root of the mod of form 2^a * b + 1
int generator() {
    vector<int> fact;
    int phi = mod - 1, n = phi;
    for (int i = 2; i * i <= n; ++i)
        if (n % i == 0) {
            fact.push_back(i);
            while (n % i == 0)
                n /= i;
        }
    if (n > 1)
        fact.push_back(n);

    for (int res = 2; res <= mod; ++res) {
        bool ok = true;
        for (size_t i = 0; i < fact.size() && ok; ++i)
            ok &= modpow(res, phi / fact[i]) != 1;
        if (ok) return res;
    }
    return -1;
}

ll modpow(ll b, ll e, ll m) {
    ll ans = 1;
    for (; e; b = b * b % m, e /= 2)
        if (e & 1) ans = ans * b % m;
    return ans;
}

void ntt(vector<ll> &a) {
    int n = (int) a.size(), L = 31 - __builtin_clz(n);
    static vector<ll> rt(2, 1); // erase the static if you want to use two
    ↪ moduli;
    for (static int k = 2, s = 2; k < n; k *= 2, s++) { // erase the static if
    ↪ you want to use two moduli;
        rt.resize(n);

```

```

    ll z[] = {1, modpow(root, mod >> s, mod)};
    for (int i = k; i < 2 * k; ++i) rt[i] = rt[i / 2] * z[i & 1] % mod;
}
vector<int> rev(n);
for (int i = 0; i < n; ++i) rev[i] = (rev[i / 2] | (i & 1) << L) / 2;
for (int i = 0; i < n; ++i) if (i < rev[i]) swap(a[i], a[rev[i]]);
for (int k = 1; k < n; k *= 2) {
    for (int i = 0; i < n; i += 2 * k) {
        for (int j = 0; j < k; ++j) {
            ll z = rt[j + k] * a[i + j + k] % mod, &ai = a[i + j];
            a[i + j + k] = ai - z + (z > ai ? mod : 0);
            ai += (ai + z >= mod ? z - mod : z);
        }
    }
}

vector<ll> conv(const vector<ll> &a, const vector<ll> &b) {
    if (a.empty() || b.empty()) return {};
    int s = (int) a.size() + (int) b.size() - 1, B = 32 - __builtin_clz(s), n =
↪ 1 << B;
    int inv = modpow(n, mod - 2, mod);
    vector<ll> L(a), R(b), out(n);
    L.resize(n), R.resize(n);
    ntt(L), ntt(R);
    for (int i = 0; i < n; ++i) out[-i & (n - 1)] = (ll) L[i] * R[i] % mod *
↪ inv % mod;
    ntt(out);
    return {out.begin(), out.begin() + s};
}

ll CRT(ll a, ll m1, ll b, ll m2) {
    __int128 m = m1 * m2;
    ll ans = a * m2 % m * modpow(m2, m1 - 2, m1) % m + m1 * b % m * modpow(m1,
↪ m2 - 2, m2) % m;
    return ans % m;
}

```

7 Misc

7.1 Base Conversion

```

string letters = "0123456789ABCDEF";

int toInt(char c)
{
    return letters.find(c);
}

int FromAnyBasetoDecimal(string in, int base)
{
    int res = 0;
    for (int i = 0; i < in.size(); ++i)

```

```

        res *= base, res += toInt(in[i]);
    return res;
}

string FromDecimaltoAnyBase(int number, int base)
{
    if (number == 0)
        return "0";
    string res = "";
    for (; number; number /= base)
        res = letters[number % base] + res;
    return res;
}

string toNegativeBase(int n, int negBase)
{
    if (n == 0)
        return "0";
    string ans = "";
    while (n != 0)
    {
        int rem = n % negBase;
        n /= negBase;
        if (rem < 0)
        {
            rem += (-negBase);
            n += 1;
        }
        ans += to_string(rem);
    }
    reverse(all(ans));
    return ans;
}

void print(int x)
{
    if (x <= 1)
    {
        cout << x;
        return;
    }
    print(x >> 1);
    cout << (x & 1);
}

```

7.2 BuiltIn functions

```

11 mxb(11 x)
{
    if (!x)
        return x;
    return 1LL << (63 - __builtin_clzll(x));
}
// count leading zeros
__builtin_clzll(x)

```

```
// count on bits
__builtin_popcountll(x)

// to get lowbit (x&-x)
```

7.3 CheckTime

```
auto start = chrono::high_resolution_clock::now();
// code    auto stop = chrono::high_resolution_clock::now();
auto duration = chrono::duration_cast<chrono::nanoseconds>(stop - start);
cerr << "Time taken : " << ((ld)duration.count()) / ((ld)1e9) << " s" << endl;
```

7.4 CompareFunction for ds

```
class comp {
public:
    bool operator()(T a, T b){
        if(cond){
            return true;
        }
        return false;
    }
};

priority_queue<data_type, container, comparator> ds;
```

7.5 DP digits

```
int n;
vector<int>v1, v2;
ll dp[20][2][2];
ll fun(int idx, bool l, bool r)
{
    if (idx == n)return 1;
    ll& ret = dp[idx][l][r];
    if (~ret)return ret;
    ret = 0;
    int lim1 = l? 0 : v1[idx];
    int lim2 = r? 9 : v2[idx];

    for (int i = lim1; i <= lim2; i++)
    {
        bool temp1 = i > v1[idx];
        bool temp2 = i < v2[idx];
        ret += fun(idx + 1, l|temp1, r|temp2);
    }
    return ret;
}
void solve()
{
    memset(dp, -1, sizeof dp);
```



```

ll x, y;
cin >> x >> y;
while (x)v1.push_back(x % 10), x /= 10;
while (y)v2.push_back(y % 10), y /= 10;
while (v1.size() < v2.size())v1.push_back(0);
while (v2.size() < v1.size())v2.push_back(0);
reverse(all(v1));
reverse(all(v2));
n = v1.size();
cout << fun(0, 0, 0, 0) << endl;
v1.clear();
v2.clear();
}

```

7.6 DP SOS Kareem

```

const int LG = 22;
const int M = 1 << LG;

// subset contribute to its superset
void forward1(vector<ll>&dp) {
    for (int bt = 0; bt < LG; ++bt) {
        for (int m = 0; m < M; ++m) {
            if (m >> bt & 1){
                dp[m] += dp[m ^ (1 << bt)];
            }
        }
    }
}

// superset contribute to its subset
void forward2(vector<ll>&dp) {
    for (int bt = 0; bt < LG; ++bt) {
        for (int m = M - 1; m >= 0; m--) {
            if (m >> bt & 1){
                dp[m ^ (1 << bt)] += dp[m];
            }
        }
    }
}

// remove subset contribution from superset
void backward1(vector<ll>&dp) {
    for (int bt = 0; bt < LG; bt++){
        for (int m = M - 1; m >= 0; m--){
            if (m >> bt & 1){
                dp[m] -= dp[m ^ (1 << bt)];
            }
        }
    }
}

// remove superset contribution from subset
void backward2(vector<ll> &dp) {

```

```

    for (int bt = 0; bt < LG; bt++){
        for (int m = 0; m < M; m++){
            if (m >> bt & 1){
                dp[m ^ (1 << bt)] -= dp[m];
            }
        }
    }
}

```

7.7 Generate All Submasks

```

void genAllSubmask(int mask) {
    for (int subMask = mask;; subMask = (subMask - 1) & mask) {
//code
        if (subMask == 0)
            break;
    }
}

```

7.8 Li-Chao

```

const int LC_N = (int)1e6 + 1;
const long long LC_INF = (long long)1e17;
vector<array<long long,2>> lc_tree(4 * LC_N, {0, LC_INF});

long long f_line(const array<long long,2>& line, int x) {
    return line[0] * x + line[1];
}

void lc_insert(array<long long,2> line, int lo = 1, int hi = LC_N, int i = 1) {
    int m = (lo + hi) / 2;
    bool left = f_line(line, lo) < f_line(lc_tree[i], lo);
    bool mid = f_line(line, m) < f_line(lc_tree[i], m);

    if (mid) swap(lc_tree[i], line);
    if (hi - lo == 1) return;

    if (left != mid)
        lc_insert(line, lo, m, 2 * i);
    else
        lc_insert(line, m, hi, 2 * i + 1);
}

long long lc_query(int x, int lo = 1, int hi = LC_N, int i = 1) {
    int m = (lo + hi) / 2;
    long long curr = f_line(lc_tree[i], x);

    if (hi - lo == 1) return curr;

    if (x < m)
        return min(curr, lc_query(x, lo, m, 2 * i));
    else
        return min(curr, lc_query(x, m, hi, 2 * i + 1));
}

```

7.9 LIS Onlogn

```
int LIS(const vector<int> &v) {
    vector<int> lis(v.size());//put value less than zero if needed
    int l = 0;
    for (int i = 0; i < sz(v); i++) {
        int idx = lower_bound(lis.begin(), lis.begin() + l, v[i]) - lis.begin();
        if (idx == l)
            l++;
        lis[idx] = v[i];
    }
    return l;
}
```

7.10 misereNim

```
string misereNim(const vector<int>& heaps) {
    int ones = 0;
    int moreThanOne = 0;
    int nimSum = 0;

    for (int h : heaps) {
        if (h == 1) ones++;
        else moreThanOne++;
        nimSum ^= h;
    }

    if (moreThanOne == 0) {
        // All heaps are 1
        return (ones % 2 == 0 ? "Win" : "Lose");
    } else if (moreThanOne == 1) { // remove this condition @saad
        // One heap > 1
        return (ones % 2 == 1 ? "Win" : "Lose");
    } else {
        // General case
        return (nimSum == 0 ? "Lose" : "Win");
    }
}
```

7.11 Next element

```
int n;
const int N = 1e5+5;
vector<int>v(N);
//
vector<int>next_mx()
{
    stack<int>st;
    st.push(n + 1);
    vector<int>suf;
    v[n + 1] = 2e9;
    for (int i = n; i > 0; i--)
    {
        while (v[i] >= v[st.top()])st.pop();
        suf.push_back(st.top());
    }
}
```

```

        st.push(i);
    }
    suf.push_back(0);
    reverse(all(suf));
    return suf;
}

vector<int>next_mn()
{
    stack<int>st;
    st.push(n + 1);
    vector<int>suf;
    v[n + 1] = -2e9;
    for (int i = n; i > 0; i--)
    {
        while (v[i] <= v[st.top()])st.pop();
        suf.push_back(st.top());
        st.push(i);
    }
    suf.push_back(0);
    reverse(all(suf));
    return suf;
}

vector<int>prev_mx()
{
    vector<int>pre;
    stack<int>st;
    pre.push_back(0);
    st.push(0);
    v[0] = 2e9;
    for (int i = 1; i <= n; i++)
    {
        while (v[i] >= v[st.top()])st.pop();
        pre.push_back(st.top());
        st.push(i);
    }
    return pre;
}

vector<int>prev_mn()
{
    vector<int>pre;
    stack<int>st;
    pre.push_back(0);
    st.push(0);
    v[0] = -2e9;
    for (int i = 1; i <= n; i++)
    {
        while (v[i] <= v[st.top()])st.pop();
        pre.push_back(st.top());
        st.push(i);
    }
}

```

```
    return pre;
}
```

7.12 Random

```
#include <random>

static random_device rd;
static mt19937 gen(rd());

int randomgen(int x)
{
    uniform_int_distribution<> dis(0, x - 1);
    int rndnum = dis(gen);
    return rndnum;
}

#include <chrono>
#include <random>

//write this line once in top
mt19937_64 rng(chrono::steady_clock::now().time_since_epoch().count() *
               ((uint64_t) new char | 1));

// use this instead of rand()
template<typename T>
T Rand(T low, T high) {
    return uniform_int_distribution<T>(low, high)(rng);
}
```

7.13 Ternary search

```
// 1 d ternary search

bool can(int mid) {}
int ternary_search(int l, int r)
{
    int ans;
    while (l <= r)
    {
        int mid1 = l + (r - l) / 3;
        int mid2 = r - (r - l) / 3;
        if (can(mid1) > can(mid2)) ans=mid1, r = mid2;
        else ans=mid2, l = mid1;
    }
    return ans;
}

// 2d, beware if dealing with double remove the +-1
double get(int row, int mid);
double ans = 1e18;
double ternary1(int row)
{
    int l = -1e9 - 5, r = 1e9 + 5, mid1, mid2;
```

```

double res;
while (l <= r) {
    mid1 = l + (r - l) / 3;
    mid2 = r - (r - l) / 3;
    double res1 = get(row, mid1);
    double res2 = get(row, mid2);
    if (res1 > res2)
        l = mid1 + 1, res = res2;
    else
        r = mid2 - 1, res = res1;
}
return res;
}
void ternary2()
{
    int l = -1e9 - 5, r = 1e9 + 5, mid1, mid2;
    while (l <= r) {
        mid1 = l + (r - l) / 3;
        mid2 = r - (r - l) / 3;
        double res1 = ternary1(mid1);
        double res2 = ternary1(mid2);
        if (res1 > res2)
        {
            ans = min(ans, res2);
            l = mid1 + 1;
        }
        else
        {
            ans = min(ans, res1);
            r = mid2 - 1;
        }
    }
}
}

```

7.14 VectorHasher

```

struct VectorHasher {
    int operator()(const vector<int> &V) const {
        int hash = V.size();
        for(auto &i : V) {
            hash ^= i + 0x9e3779b9 + (hash << 6) + (hash >> 2);
        }
        return hash;
    }
};

```

unordered_map<vector <int> , int, VectorHasher> used;

7.15 XOR basis Range

```

const int LOG = 21;
struct Basis {

```

```

int basis[LOG];
int lst_idx[LOG];
int sz;

Basis() {
    sz = 0;
    for (int i = LOG - 1; i >= 0; --i) {
        basis[i] = 0;
        lst_idx[i] = -1;
    }
}

void insert(int x, int idx) {
    for (int i = LOG - 1; i >= 0; --i) {
        if ((x & (1ll << i)) == 0) continue;
        if (lst_idx[i] < idx)
        {
            swap(x, basis[i]);
            swap(lst_idx[i], idx);
            ++sz;
        }
        x ^= basis[i];
    }
}

int get_max(int l) {
    int ans = 0;
    for (int i = LOG - 1; i >= 0; --i) {
        if (basis[i] && !(ans & (1ll << i)) && lst_idx[i] >= l)
            ans ^= basis[i];
    }
    return ans;
}

};

void solve()
{
    Basis B = Basis();
    int n; cin >> n;
    vector<Basis> arr(n);
    for (int i = 0; i < n; ++i) {
        int x; cin >> x;
        B.insert(x, i);
        arr[i] = B;
    }

    int q; cin >> q;
    while (q--)
    {
        int l, r; cin >> l >> r;
        l--, r--;
        cout << arr[r].get_max(l) << endl;
    }
}

```

```
}
```

7.16 XOR basis

```
const int d=31;
int basis[d];
int sz;
bool insertVector(int mask) {
    for (ll i = d-1; i>=0; i--){
        if ((mask & 1<< i) == 0) continue;
        if (!basis[i]) {
            basis[i] = mask;
            sz++;
            return true;
        }
        mask ^= basis[i];
    }
    return false;
}
```

7.17 Xor from 1 to n

```
//xor from 1 to x
ll getXor(ll x) {
    if (x % 4 == 0) return x;
    if (x % 4 == 1) return 1;
    if (x % 4 == 2) return x + 1;
    return 0;
}
```

8 Problem codes

8.1 Lca Persistant code problem

```
#include<bits/stdc++.h> //Silence / ft. Reda , AbdoSa3d , Nourhan
```

```
using namespace std;
```

```
#define all(v) v.begin(),v.end()
#define ll long long
#define endl "\n"
```

```
struct Node
{
    Node* ls{}, * rs{};
    int sum{};
} pool[int(1e6)];
int top;
Node* null = pool + 0;
vector<Node*> rot;
void reset()
{
    top = 1;
```



```

    null->sum = 0;
    null->ls = null->rs = null;
}
Node* newNode()
{
    auto p = pool + (top++);
    *p = *null;
    return p;
}

// x is postion to insert
Node* add(Node* p, int l, int r, int x)
{
    auto np = newNode();
    *np = *p;
    np->sum++;
    if (r - l == 1)
    {
        return np;
    }
    int m = (l + r) / 2;
    if (x < m)
    {
        np->ls = add(p->ls, l, m, x);
    }
    else
    {
        np->rs = add(p->rs, m, r, x);
    }
    return np;
}

int R = 1e5 + 1;
int const N = 1e5 + 5, M = 20;
int dp[N][M + 1];
int lvl[N], n;
vector<vector<pair<int, int>>> G;

void dfs(int u, int par)
{
    dp[u][0] = par;
    for (auto [i, w] : G[u])
    {
        if (i != par)
        {
            lvl[i] = lvl[u] + 1;
            rot[i] = add(rot[u], 1, R, w);
            dfs(i, u);
        }
    }
}

int lca(int u, int v)

```

```

{
    if (lvl[u] > lvl[v]) swap(u, v);
    for (int i = M; i >= 0; i--)
        if (lvl[v] - (1 << i) >= lvl[u])
            v = dp[v][i];

    if (u == v) return v;
    for (int i = M; i >= 0; i--)
    {
        int cu = dp[u][i], cv = dp[v][i];
        if (min(cu, cv) != -1 && cu != cv)
            u = cu, v = cv;
    }
    return dp[u][0];
}

void solve()
{
    reset();
    cin >> n;
    rot = vector<Node*>(n + 1);
    G = vector<vector<pair<int, int>>>(n + 1);
    rot[1] = null;
    for (int i = 1; i < n; i++)
    {
        int u, v, w;
        cin >> u >> v >> w;
        G[u].push_back({ v, w });
        G[v].push_back({ u, w });
    }
    dfs(1, -1);
    for (int i = 1; i <= M; i++)
    {
        for (int j = 1; j <= n; j++)
        {
            int u = dp[j][i - 1];
            if (u == -1) dp[j][i] = -1;
            else dp[j][i] = dp[u][i - 1];
        }
    }
    auto get = [&](int a, int b, int c, int k)
    {
        int l = 1, r = R;
        Node* at = rot[a];
        Node* bt = rot[b];
        Node* pt = rot[c];
        while (r - l > 1)
        {
            int sum = at->ls->sum + bt->ls->sum - 2 * pt->ls->sum;
            if (sum >= k)
            {
                at = at->ls;
                bt = bt->ls;
            }
        }
    }
}

```

```

        pt = pt->ls;
        r = (r + 1) / 2;
    }
    else
    {
        k -= sum;
        at = at->rs;
        bt = bt->rs;
        pt = pt->rs;
        l = (r + 1) / 2;
    }
}
return l;
};

int q;
cin >> q;
cout << fixed << setprecision(1);
while (q--)
{
    int a, b;
    cin >> a >> b;
    int c = lca(a, b);
    int cnt = lvl[a] + lvl[b] - 2 * lvl[c];
    if (cnt & 1)
    {
        int x = get(a, b, c, cnt / 2 + 1);
        cout << x * 1.0 << endl;
    }
    else
    {
        int x = get(a, b, c, cnt / 2);
        int y = get(a, b, c, cnt / 2 + 1);
        cout << (x + y) / 2.0 << endl;
    }
}

int
main()
{
    cin.tie(0)->sync_with_stdio(0);

    int t = 1;
    cin >> t;
    while (t--)
        solve();
}

```

8.2 Line Sweep Mostafa Saad

```
/*
 *
 * Created on: Oct 29, 2016
 * Author: mostafa saad
 *
 *
 * tested on timus_1469_no_smoking
 * http://acm.timus.ru/problem.aspx?space=1&num=1469
 */

#include <iostream>
#include <cmath>
#include <complex>
#include <cassert>
#include <bits/stdc++.h>
using namespace std;

const double PI = acos(-1.0);
const double EPS = 1e-8;

int dcmp(double a, double b) {
    return fabs(a - b) <= EPS ? 0 : a < b ? -1 : 1;
}

typedef complex<int> point;

#define X real()
#define Y imag()
#define angle(a) (atan2((a).imag(), (a).real()))
#define vec(a,b) ((b)-(a))
#define same(p1,p2) (dp(vec(p1,p2),vec(p1,p2)) < EPS)
#define dp(a,b) ((conj(a)*(b)).real()) // a*b cos(T), if
↪ zero -> prep
#define cp(a,b) ((conj(a)*(b)).imag()) // a*b sin(T), if
↪ zero -> parallel
#define length(a) (hypot((a).imag(), (a).real()))
#define normalize(a) (a)/length(a)
#define rotate0(p,ang) ((p)*exp(point(0,ang)))
#define rotateA(p,ang,about) (rotate0(vec(about,p),ang)+about)
#define reflect0(v,m) (conj((v)/(m))*(m))

point reflect(point p, point p0, point p1) {
    point z = p - p0, w = p1 - p0;
    return conj(z / w) * w + p0; // Reflect point p1 around p0p1
}

#define all(v) ((v).begin()), ((v).end())
#define sz(v) ((int)((v).size()))
#define clr(v, d) memset(v, d, sizeof(v))
#define rep(i, v) for(int i=0;i<sz(v);++i)
#define lp(i, n) for(int i=0;i<(int)(n);++i)
#define lpi(i, j, n) for(int i=(j);i<(int)(n);++i)
```

```

#define lpd(i, j, n) for(int i=(j);i>=(int)(n);--i)

int ccw(point a, point b, point c) {
    point v1(b - a), v2(c - a);
    double t = cp(v1, v2);

    if (t > +EPS)
        return +1;
    if (t < -EPS)
        return -1;
    if (v1.X * v2.X < -EPS || v1.Y * v2.Y < -EPS)
        return -1;
    if (norm(v1) < norm(v2) - EPS)
        return +1;
    return 0;
}

bool intersect(point p1, point p2, point p3, point p4) {
    // special case handling if a segment is just a point
    bool x = (p1 == p2), y = (p3 == p4);
    if (x && y)
        return p1 == p3;
    if (x)
        return ccw(p3, p4, p1) == 0;
    if (y)
        return ccw(p1, p2, p3) == 0;

    return ccw(p1, p2, p3) * ccw(p1, p2, p4) <= 0 && ccw(p3, p4, p1) * ccw(p3,
↪ p4, p2) <= 0;
}

////////////////////////////////////

bool operator <(point &a, point &b) {
    if (dcmp(a.X, b.X) != 0)
        return dcmp(a.X, b.X) < 0;
    return dcmp(a.Y, b.Y) < 0;
}

struct segment {
    point p, q;
    int seg_idx;

    segment() {seg_idx = -1;}
    segment(point p_, point q_, int seg_idx_) {
        if (q_ < p_)
            swap(p_, q_);
        p = p_, q = q_, seg_idx = seg_idx_;
    }

    double CY(int x) const {
        if (dcmp(p.X, q.X) == 0)
            return p.Y; // horizontal
    }
}

```

```

    double t = 1.0 * (x - p.X)/(q.X - p.X);
    return p.Y + (q.Y - p.Y)*t;
}
// operator< is very tricky and can cause 100 WAs.
bool operator<(const segment& rhs) const {
    if(same(p, rhs.p) && same(q, rhs.q))
        return false;

    int maxX = max(p.X, rhs.p.X);
    int yc = dcmp(CY(maxX), rhs.CY(maxX));

    if (yc == 0) // critical condition
        return seg_idx < rhs.seg_idx;
    return yc < 0;
}
};

////////////////////////////////////

int ENTRY = +1, EXIT = -1;          // entry types
const int MAX_SEGMENTS = 50000 + 9;
const int MAX_EVENTS = MAX_SEGMENTS * 2;

struct event {
    point p;
    int type, seg_idx;
    // smaller X first. If tie: ENTRY event first. Last on smaller Y
    bool operator <(const event & rhs) const {
        if (dcmp(p.X, rhs.p.X) != 0)
            return dcmp(p.X, rhs.p.X) < 0;
        if (type != rhs.type)
            return type > rhs.type;
        return dcmp(p.Y, rhs.p.Y) < 0;
    }
};

int n;
segment segments[MAX_SEGMENTS];
event events[MAX_EVENTS];
set<segment> sweepSet;
typedef set<segment>::iterator ITER;

////////////////////////////////////

bool intersectSeg(ITER seg1Iter, ITER seg2Iter) {
    if (seg1Iter == sweepSet.end() || seg2Iter == sweepSet.end())
        return false;
    return intersect(seg1Iter->p, seg1Iter->q, seg2Iter->p, seg2Iter->q);
}

ITER after(ITER cur) {
    return cur == sweepSet.end() ? sweepSet.end() : ++cur;
}

```

```

}

ITER before(ITER cur) {
    return cur == sweepSet.begin() ? sweepSet.end() : --cur;
}

void FoundIntersection(int i, int j) {
    printf("%d %d\n", i + 1, j + 1);
}

void bentleyOttmann_lineSweep() {    // O( (k+n) logn )
    // Prepare events
    lp(i, n)
    {
        events[2*i] = {segments[i].p, ENTRY, i};
        events[2*i+1] = {segments[i].q, EXIT, i};
    }
    sort(events, events+2*n);

    lp(i, 2*n) {
        if (events[i].type == ENTRY) {
            auto status = sweepSet.insert(segments[events[i].seg_idx]);
            ITER cur = status.first, below = before(cur), above = after(cur);

            if(!status.second) {
                FoundIntersection(cur->seg_idx, events[i].seg_idx); // Duplicate
            } else {
                if(intersectSeg(cur, above))
                    FoundIntersection(cur->seg_idx, above->seg_idx);
                if(intersectSeg(cur, below))
                    FoundIntersection(cur->seg_idx, below->seg_idx);
            }
        } else {
            ITER cur = sweepSet.find(segments[events[i].seg_idx]);

            if(cur == sweepSet.end())
                continue; // e.g. Duplicate

            ITER below = before(cur), above = after(cur);

            if(intersectSeg(above, below))
                FoundIntersection(above->seg_idx, below->seg_idx);
            sweepSet.erase(cur);
        }
    }
}

////////////////////////////////////

int main() {
#ifdef ONLINE_JUDGE
    freopen("test.txt", "rt", stdin);
#endif

```

```

    int x, y;

    cin >> n;
    lp(i, n)
    {
        cin >> x >> y;        point p1 = point(x, y);
        cin >> x >> y;        point p2 = point(x, y);

        segments[i] = segment(p1, p2, i);
    }
    bentleyOttmann_lineSweep();

    return 0;
}

```

9 Strings

9.1 Aho Corasick

```

struct aho_corasick{
    struct trie_node {

        vector<int> pIdxs; //probably take memory limit
        map<char, int> next;
        int fail;
        trie_node() : fail(0) {}
        bool have_next(char ch) {
            return next.find(ch) != next.end();
        }
        int &operator[](char ch) {
            return next[ch];
        }
    };
    vector<trie_node> t;
    vector<string> patterns;
    vector<int> end_of_pattern;
    vector<vector<int>> adj;
    int insert(const string &s, int patternIdx) {
        int root = 0;
        for (const char &ch: s) {
            if (!t[root].have_next(ch)) {
                t.push_back(trie_node());
                t[root][ch] = t.size() - 1;
            }
            root = t[root][ch];
        }
        t[root].pIdxs.push_back(patternIdx);
        return root;
    }
    int next_state(int cur, char ch) {
        while (cur > 0 && !t[cur].have_next(ch))
            cur = t[cur].fail;
    }
}

```



```

        if (t[cur].have_next(ch))
            return t[cur][ch];
        return 0;
    }
    void buildAhoTree() {
        queue<int> q;
        for (auto &child: t[0].next)
            q.push(child.second);
        while (!q.empty()) {
            int cur = q.front();
            q.pop();
            for (auto &child: t[cur].next) {
                int k = next_state(t[cur].fail, child.first);
                t[child.second].fail = k;
                vector<int> &idxs = t[child.second].pIdxs;
                //dp[child.second] = max(dp[child.second], dp[k]);
                idxs.insert(idxs.end(), all(t[k].pIdxs));
                q.push(child.second);
            }
        }
    }
    void buildFailureTree() {
        adj = vector<vector<int>>(t.size());
        for (int i = 1; i < t.size(); i++)
            adj[t[i].fail].push_back(i);
    }
    aho_corasick(const vector<string> &_patterns) {
        t.push_back(trie_node());
        patterns = _patterns;
        end_of_pattern = vector<int>(patterns.size());
        for (int i = 0; i < patterns.size(); i++)
            end_of_pattern[i] = insert(patterns[i], i);
        buildAhoTree();
        //buildFailureTree();
    }
    vector<vector<int>> match(const string &str) {
        int k = 0;
        vector<vector<int>> rt(patterns.size());
        for (int i = 0; i < str.size(); i++) {
            k = next_state(k, str[i]);
            for (auto &it: t[k].pIdxs)
                rt[it].push_back(i);
        }
        return rt;
    }
};

```

9.2 Anas Suffix Array

```

struct SuffixArray {
    const static int alpha = 128, LOG = 20;
    vector<int> suf, order, newOrder, lcp, logs;
    vector<vector<int>> table;

```

```

string s;
int n;

SuffixArray(const string& _s) : n(sz(_s) + 1), s(_s) {
    s += ' ';
    suf = order = newOrder = vector<int>(n);
    vector<int> bucket_idx(n), newOrder(n), new_suf(n);
    vector<int> prev(n), head(alpha, -1);

    auto getOrder = [&](const int& a) -> int {
        return a < n ? order[a] : 0;
    };

    for (int i = 0; i < n; i++) {
        prev[i] = head[s[i]];
        head[s[i]] = i;
    }
    for (int i = 0, buc = -1, idx = 0; i < alpha; i++) {
        if(head[i] == -1) continue;
        bucket_idx[++buc] = idx;
        for (int j = head[i]; ~j; j = prev[j]){
            suf[idx++] = j; order[j] = buc;
        }
    }

    for (int len = 1; order[suf[n - 1]] != n - 1; len <= 1) {
        auto comp = [&](const int &a, const int &b) -> bool {
            if (order[a] != order[b]) return order[a] < order[b];
            return getOrder(a + len) < getOrder(b + len);
        };
        for (int i = 0; i < n; i++) {
            int j = suf[i] - len;
            if(j < 0) continue;
            new_suf[bucket_idx[order[j]]++] = j;
        }
        for(int i = 1; i < n; i++){
            suf[i] = new_suf[i];
            bool newGroup = comp(suf[i - 1], suf[i]);
            newOrder[suf[i]] = newOrder[suf[i - 1]] + newGroup;
            if(newGroup){
                bucket_idx[newOrder[suf[i]]] = i;
            }
        }
        order = newOrder;
    }

    lcp = vector<int>(n);
    int k = 0;
    for (int i = 0; i < n - 1; i++) {
        int pos = order[i];
        int j = suf[pos - 1];
        while (s[i + k] == s[j + k]) k++;
        lcp[pos] = k;
    }
}

```

```

        k = max(0, k - 1);
    }
    buildTable();
}

void buildTable() {
    table = vector<vector<int>>(n + 1, vector<int>(LOG));
    logs = vector<int>(n + 1);
    logs[1] = 0;
    for (int i = 2; i <= n; i++)
        logs[i] = logs[i >> 1] + 1;
    for (int i = 0; i < n; i++) {
        table[i][0] = lcp[i];
    }
    for (int j = 1; j <= logs[n]; j++) {
        for (int i = 0; i <= n - (1 << j); i++) {
            table[i][j] = min(table[i][j - 1], table[i + (1 << (j - 1))][j
↪ - 1]);
        }
    }
}

int LCP(int i, int j) {
    if (i == j) return n - i - 1;
    int l = order[i], r = order[j];
    if (l > r) swap(l, r);
    l++;
    int sz = logs[r - l + 1];
    return min(table[l][sz], table[r - (1 << sz) + 1][sz]);
}

int LCP_Order(int l, int r){
    if (l == r) return n-suf[l]-1;
    if (l > r) swap(l, r);
    l++;
    int sz = logs[r - l + 1];
    return min(table[l][sz], table[r - (1 << sz) + 1][sz]);
}

int compare_substrings(int l1, int r1, int l2, int r2) {
    int k = min({LCP(l1, l2), r1 - l1 + 1, r2 - l2 + 1});
    l1 += k; l2 += k;
    if (l1 > r1 && l2 > r2) return 0;
    if (l1 > r1) return -1;
    if (l2 > r2) return 1;
    return (s[l1] > s[l2] ? 1 : -1);
}
};

```

9.3 Hashing Kareem

```

class Hashing {
    const ll MOD = (1ll << 61) - 1;

```

```

    vector<ll> p, h;
    static ll base;
public:
    Hashing(const string &a) {
        p = h = vector<ll>(a.size() + 1);
        p[0] = 1;
        for (int i = 0; i < a.size(); i++) {
            p[i+1] = (__int128_t) p[i] * base % MOD;
            h[i+1] = ((__int128_t) h[i] * base + a[i]) % MOD;
        }
    }
    ll getHash(int l, int r) { //base 0
        return ((h[r + 1] - (__int128_t) h[l] * p[r - l + 1] % MOD) + MOD)%MOD;
    }
};
ll rng(ll l = (1ll << 40), ll r = (1ll << 60)) {
    static std::mt19937 gen(
        std::chrono::steady_clock::now().time_since_epoch().count());
    return std::uniform_int_distribution<long long>(l, r)(gen);
}
ll Hashing::base = rng();

```

9.4 Hashing

```

const int N = 1e5 + 5, MOD1 = 1e9 + 7, MOD2 = 1e9 + 9;
int pw1[N], inv1[N], pw2[N], inv2[N], BASE;

bool isPrime(int x) {
    for (int i = 2; i * i <= x; i++) {
        if (x % i == 0) return 0;
    }
    return x > 1;
}

int fix(ll x, int M) {
    return (x % M + M) % M;
}

int fpow(int a, int b, int mod) {
    if (!b) return 1;
    int ret = fpow(a, b >> 1, mod);
    ret = fix(1ll * ret * ret, mod);
    if (b & 1) ret = fix(1ll * ret * a, mod);
    return ret;
}

void init() {
    static bool done = false;
    if (done) return;
    done = true;

    mt19937_64 rng(chrono::steady_clock::now().time_since_epoch().count());
    uniform_int_distribution<int> dist(257, 10007);
    do{

```

```

    BASE = dist(rng);
}while (!isPrime(BASE));

pw1[0] = inv1[0] = pw2[0] = inv2[0] = 1;
int iv1 = fpow(BASE, MOD1 - 2, MOD1);
int iv2 = fpow(BASE, MOD2 - 2, MOD2);
for (int i = 1; i < N; ++i) {
    pw1[i] = fix(1ll * pw1[i - 1] * BASE, MOD1);
    pw2[i] = fix(1ll * pw2[i - 1] * BASE, MOD2);
    inv1[i] = fix(1ll * inv1[i - 1] * iv1, MOD1);
    inv2[i] = fix(1ll * inv2[i - 1] * iv2, MOD2);
}
}

struct Hash {
    vector<pair<int, int>> pre;

    Hash(const string &s) {
        init();
        pre.assign(sz(s) + 1, {0, 0});
        for (int i = 0; i < sz(s); i++) {
            pre[i + 1] = make_pair(fix(1ll * pw1[i] * s[i] + pre[i].first,
↪ MOD1),
                                fix(1ll * pw2[i] * s[i] + pre[i].second,
↪ MOD2));
        }
    }

    pair<int, int> getRange(int l, int r) const { // 0-based
        return make_pair(fix(1ll * inv1[l] * (pre[r + 1].first - pre[l].first),
↪ MOD1),
                        fix(1ll * inv2[l] * (pre[r + 1].second -
↪ pre[l].second), MOD2));
    }
};

```

9.5 KMP

```

//KMP
vector<int>KMP(const string&s){
    int n = sz(s);
    vector<int>fail(n);
    for(int i = 1; i < n; i++){
        int j = fail[i-1];
        while(j && s[i] != s[j]){
            j = fail[j-1];
        }
        if(s[i] == s[j])j++;
        fail[i] = j;
    }
    return fail;
}

```

9.6 Manacher

```
vector<int> manacher_odd(string s) {
    int n = s.size();
    s = "$" + s + "^";
    vector<int> p(n + 2);
    int l = 1, r = 1;
    for(int i = 1; i <= n; i++) {
        p[i] = max(0, min(r - i, p[l + (r - i)]));
        while(s[i - p[i]] == s[i + p[i]]) {
            p[i]++;
        }
        if(i + p[i] > r) {
            l = i - p[i], r = i + p[i];
        }
    }
    return vector<int>(begin(p) + 1, end(p) - 1);
}

vector<int> manacher(string s) {
    string t;
    for(auto c: s) {
        t += string("#") + c;
    }
    auto res = manacher_odd(t + "#");
    return vector<int>(begin(res) + 1, end(res) - 1);
}

// Returns vector `d2` where d2[i] is the max radius of even-length
// palindrome centered between s[i-1] and s[i]
vector<int> manacher_even(const string &s) {
    int n = s.size();
    vector<int> d2(n); // For even-length palindromes
    int l = 0, r = -1;

    for (int i = 0; i < n; ++i) {
        int k = (i > r) ? 0 : min(d2[l + r - i + 1], r - i + 1);

        while (i - k - 1 >= 0 && i + k < n && s[i - k - 1] == s[i + k])
            ++k;

        d2[i] = k;
        if (i + k - 1 > r) {
            l = i - k;
            r = i + k - 1;
        }
    }

    return d2;
}
```

9.7 Saad Trie

```
struct trie
{
```

```

trie* nxt[26]{};
bool endOfWord = false;
void insert(const string& s)
{
    trie* current = this;
    for (auto ch : s)
    {
        int i = ch - 'a';
        if (current->nxt[i] == nullptr) current->nxt[i] = new trie;
        current = current->nxt[i];
    }
    current->endOfWord = true;
}
bool search(const string& s)
{
    trie* current = this;
    for (auto ch : s)
    {
        int i = ch - 'a';
        if (current->nxt[i]==nullptr)return false;
        current = current->nxt[i];
    }
    return current->endOfWord;
}
};

```

```

struct trie
{
    trie* nxt[2]{};
    void insert(int val)
    {
        trie* current = this;
        for (int i=30;i>=0;i--)
        {
            bool bit = val >> i & 1;
            if (current->nxt[bit] == nullptr) current->nxt[bit] = new trie;
            current = current->nxt[bit];
        }
    }
    int search(int val)
    {
        int ans = 0;
        trie* current = this;
        for (int i = 30;i >= 0;i--)
        {
            bool bit = val >> i & 1;
            if (current->nxt[!bit] == nullptr)
                current = current->nxt[bit];
            else
                ans += (1 << i), current=current->nxt[!bit];
        }
    }
};

```

```

    }
    return ans;
}
};

```

9.8 Suffix Automation

```

struct suffix_automaton {
    struct state {
        int len, link = 0, cnt = 0;
        bool terminal = false, is_clone = false;
        map<char, int> next;
        state(int len = 0) : len(len) {}
        bool have_next(char ch) {
            return next.find(ch) != next.end();
        }
        void clone(const state &other, int nlen) {
            len = nlen;
            next = other.next;
            link = other.link;
            is_clone = true;
        }
    };
};
vector<state> st;
int last = 0;
suffix_automaton() {
    st.push_back(state());
    st[0].link = -1;
}
suffix_automaton(const string &s) : suffix_automaton() {
    for (char ch: s)
        extend(ch);
    for (int cur = last; cur > 0; cur = st[cur].link)
        st[cur].terminal = true;
}
void extend(char c) {

    int cur = st.size();
    st.push_back(state(st[last].len + 1));
    st[cur].cnt = 1;
    int p = last;
    last = cur;
    while (p != -1 && !st[p].have_next(c)) {
        st[p].next[c] = cur;
        p = st[p].link;
    }
    if (p == -1)
        return;
    int q = st[p].next[c];
    if (st[p].len + 1 == st[q].len) {
        st[cur].link = q;
        return;
    }
    int clone = st.size();

```



```

    st.push_back(state());
    st[clone].clone(st[q], st[p].len + 1);
    while (p != -1 && st[p].next[c] == q) {
        st[p].next[c] = clone;
        p = st[p].link;
    }
    st[q].link = st[cur].link = clone;
}
void calc_number_of_occurrences() {
    vector<vector<int>> lvl(st[last].len + 1);
    for (int i = 1; i < st.size(); i++)
        lvl[st[i].len].push_back(i);
    for (int i = st[last].len; i >= 0; i--)
        for (auto cur: lvl[i])
            st[st[cur].link].cnt += st[cur].cnt;
}
vector<ll> dp;
ll Count(int cur) //count number of paths
{
    ll &rt = dp[cur];
    if (rt)
        return rt;
    rt = 1;
    for (auto ch: st[cur].next)
        rt += Count(ch.second);
    return rt;
}
string kth_substring(ll k) //1-based,different substring,0 = ""
{
    assert(k <= Count(0));
    string rt;
    int cur = 0;
    while (k > 0) {
        for (auto ch: st[cur].next) {
            if (Count(ch.second) < k)
                k -= Count(ch.second);
            else {
                rt += ch.first;
                cur = ch.second;
                k--;
                break;
            }
        }
    }
    return rt;
}
string longest_common_substring(const string &t) {
    int cur = 0, l = 0, mx = 0, idx = 0;
    for (int i = 0; i < t.size(); i++) {
        while (cur > 0 && !st[cur].have_next(t[i])) {
            cur = st[cur].link;
            l = st[cur].len;
        }
    }
}

```

```

    }
    if (st[cur].have_next(t[i])) {
        cur = st[cur].next[t[i]];
        l++;
    }
    if (l > mx) {
        mx = l;
        idx = i;
    }
}
return t.substr(idx - mx + 1, mx);
}
};

```

9.9 Trie 1d vector

```

class Trie{
private:
    struct Node{
        map<char,int>mp;
        int leaf;
        bool have_next(char c){
            return mp.find(c)!=mp.end();
        }
        int& operator[](char c){
            return mp[c];
        }
        Node(){
            leaf = 0;
        }
    };
public:
    vector<Node>v;
    Trie(){
        v.push_back(Node());
    }
    void update(const string&s,int op){
        int cur = 0;
        for(auto&ch : s){
            if(!v[cur].have_next(ch)){
                v.push_back(Node());
                v[cur][ch] = v.size() - 1;
            }
            cur = v[cur][ch];
        }
        v[cur].leaf+=op;
    }
    int count(const string&s){
        int cur = 0;
        for(auto&it: s){
            if(!v[cur].have_next(it)){
                return 0;
            }
            cur = v[cur][it];
        }
    }
};

```

```

    }
    return v[cur].leaf;
}
};

```

9.10 Trie pointers

```

class Trie{
private:

    struct Node{
        map<char, Node*> mp;
        int c;
        Node(){
            c = 0;
        }
    };
    Node* root;
    void destroy(Node* cur){
        for(auto&it : cur->mp){
            destroy(it.second);
        }
        delete cur;
    }
public:
    Trie(){
        root = new Node;
    }
    ~Trie(){
        destroy(root);
    }
    void update(const string&s, int op){
        Node* tmp = root;
        for(auto&it : s){
            if(tmp->mp.count(it) == 0){
                tmp->mp[it] = new Node;
            }
            tmp = tmp->mp[it];
            tmp->c += op;
        }
    }
};

```

9.11 Z algorithm

```

/* z[i] equal the length of the longest substring starting from s[i]
   which is also a prefix of s */
vector<int> z_algo(string s) {
    int n = s.size();
    vector<int> z(n);
    z[0] = n;
    for (int i = 1, L = 1, R = 1; i < n; i++) {
        int k = i - L;

```

```

        if (z[k] + i >= R) {
            L = i;
            R = max(R, i);
            while (R < n && s[R - L] == s[R]) R++;
            z[i] = R - L;
        } else z[i] = z[k];
    }
    return z;
}

// z_function kareem
vector<int> z_function(const string&s){
    int n = s.size();
    vector<int> z(n);
    int l = 0, r = 0;
    for(int i = 1; i < n; i++){
        if(i < r){
            z[i] = min(r - i, z[i - l]);
        }
        while(i + z[i] < n && s[i + z[i]] == s[z[i]])
            z[i]++;
        if(i + z[i] > r){
            l = i;
            r = i + z[i];
        }
    }
    return z;
}

```