HUDM6122 Homework 01

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0.1 Exercise 1.1

First, I made a xlsx. version of Table 1.1 to let R read it directly using the package 'readxl". This table is in 10x7 size. The first column is just the index of each observation, so I drop it here. Finally this dataset is in 9x7 size.

One should notice that the sex, depression, and health are categorical variables. The Pearson Correlation Coefficient is used for continuous rather than categorical variables. Therefore, when calculate the correlation matrix we should drop the categorical ones.

Note, there are some parameters need to be set. Since the original dataset contains missing value, I construct the correlation matrix based on all complete observations.

```
> library(readxl)
> table_11 <- read_excel("table_1.1.xlsx")</pre>
> my data \leftarrow table 11[,c(2:7)]
> # drop the discrete vars and use only the complete observations
> my_data_cor <- round(cor(my_data[,c(2,3,6)], use = "complete"),2)
> # the output is rounded in two decimals. Therefore, the correlation matrix is
> my_data_cor
         age
                IQ weight
        1.00 - 0.15
                    -0.12
age
       -0.15 1.00
                     0.75
ΙQ
weight -0.12 0.75
                     1.00
> # the Variance-covariance matrix is
> my_data_cov <- round(cov(my_data[,c(2,3,6)], use = "complete"),2)
> my_data_cov
                    IQ weight
        932.81 -135.74 -74.76
age
ΙQ
       -135.74 884.62 438.21
weight -74.76 438.21 389.29
```

One thing should be noted that when you try different strategies in dealing with the missing data, the results are not the same. Therefore, the argument use = matters here. Based on the discussion on stackflow, use = complete.obs argument will discard the entire row if an NA is present. However, pairwise.complete.obs uses the non-NA values when calculating the correlation between variables.

0.2 Exercise 1.2

Fill the NA with the column's mean, and recalculate the correlation matrix.

```
> # to impute the NA with mean using a for-loop
> for (cols in c(2,3,6)) {
    my_data[,cols][is.na(my_data[,cols])] <- mean(my_data[,cols], na.rm=T)</pre>
+ }
> # create the correlation matrix
> my_data_cor_2 <- round(cor(my_data[,c(2,3,6)]),2)
> my_data_cor_2
         age
                IQ weight
        1.00 -0.14 -0.10
age
             1.00
       -0.14
                     0.52
ΙQ
weight -0.10 0.52
                     1.00
```

0.3 Exercise 1.3

The authors may not clearly say where readers can find the original dataset. After seeing the code underlying in this book's R package MVA, and run this argument demo("Ch-MVA"), one can find the table 1.3's dataset information at the paragraph named code chunk number 5. It is in another package called HSAUR2. First, I draw the normal probability plots of each variable.

```
> # load the Table 1.3's original dataset
> library(HSAUR2)
> # dim(pottery)
> # names(pottery) # the dataset is the same
> # layout(matrix(1:10, nc = 3))
> sapply(colnames(pottery)[1:9], function(x){
+ # use double bracket can directly return the col
+ qqnorm(pottery[[x]], main = x)
+ qqline(pottery[[x]])
+ })
```

\$Al2O3 NULL

\$Fe2O3 NULL

\$MgO NULL

\$CaO NULL

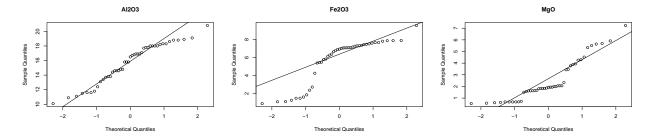
\$Na2O NULL

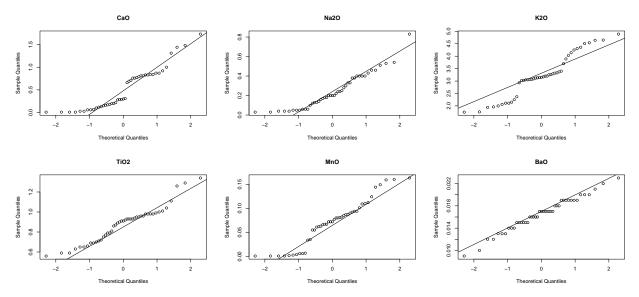
\$K2O NULL

\$TiO2 NULL

\$MnO NULL

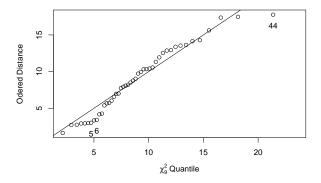
\$BaO NULL





Second, I draw the chi-square plot of the data as followed.

```
> # to drop the last discrete variable
> X <- pottery[,1:9]
> # get each col's mean
> col_mean <- colMeans(X)</pre>
> # get the cov matrix
> S <- cov(X)
> # solve() function can get inverse matrix directly
 # compute the generalised distance
  d <- apply(X, 1, # array; 1= row 2 = col</pre>
              function(X)
                t(X - col_mean) \ \%*\% \ solve(S) \ \%*\% \ (X - col_mean))
  plot(qc \leftarrow qchisq((1:nrow(X) - 1/2)/nrow(X), df = 9),
       sd<- sort(d),</pre>
       xlab = expression(paste(chi[9]^2," Quantile")),
       ylab = "Odered Distance", xlim = range(qc)*c(1, 1.1))
> oups <- which(rank(abs(qc-sd), ties="random") > nrow(X) - 3)
> text(qc[oups], sd[oups]-1.5, names(oups))
> abline(a=0, b=1)
```



From the Q-Q plots, one can see most of the elements do not perfectly follow the normal distribution except

the AL203 and the Ba0. These two variables present relatively good normal distribution. As for the Chisquare plot, if all the data are normally distributed, they should correspond to each others. Therefore, from the plot, we can easily find the outliers are the 5th, 6th, and the 44th observations.

0.4 Exercise 1.4

This question can be addressed in one line using cov2cor function

But here I provide another more specific code to achieve this goal. Could you please consider to give me extra credits? Just kidding..lol..

Finally, the results are exactly the same.

0.5 Exercise 1.5

0.5.1 E1.5 Part 1 Create the Euclidean Distance Matrix

Here I write a function to get the Euclidean distance matrix for any shape of observed matrix. Since for any m * n matrix, the size of euclidean distance is always m * m.

```
> # write a function that can get Eu-dist matrix any shape of matrix
> eudis_matrix <- function(a_matrix){
+  # first define a function to get the eu distance of any two vectors
+  eu_distance <- function(vec_1, vec_2){
+  d_2_vec <- (vec_1-vec_2)^2
+  d_2 <- sum(d_2_vec)</pre>
```

```
d <- sqrt(d_2)</pre>
+
       return(d)
+
       }
    m <- nrow(a_matrix)</pre>
    dist_matrix <- matrix(nrow = m, ncol = m)</pre>
+
    for (i in 1:m ) {
      for (j in 1:m) {
+
         dist_matrix[i,j] <- eu_distance(a_matrix[i,], a_matrix[j,])</pre>
+
    }
+
    return(dist_matrix)
```

The function seems good. Then, I tried it on the given dataset.

```
> # import the data
> multi_mat<- matrix(c(3,6,4,0,7,
                     4,2,7,4,6,
+
                     4,0,3,1,5,
                     6,2,6,1,1,
                     1,6,2,1,4,
                     5,1,2,0,2,
                     1,1,2,6,1,
                     1,1,5,4,4,
                     7,0,1,3,3,
                     3,3,0,5,1),10,5, byrow=T)
> # create the euclidean dis-matrix on the given dataset.
> round(eudis_matrix(multi_mat),2)
       [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
 [1,] 0.00 6.56 6.56 8.12 4.24 7.62 10.25 7.42 9.27 9.27
 [2,] 6.56 0.00 5.48 6.24 7.94 7.68 8.00 4.24 7.68
 [3,] 6.56 5.48 0.00 5.74 6.86 3.61 7.21 4.90 4.58
 [4,] 8.12 6.24 5.74 0.00 8.12 4.47 8.19 6.71 6.16 7.87
 [5,] 4.24 7.94 6.86 8.12 0.00 6.78 7.68 6.56 8.83 6.48
 [6,] 7.62 7.68 3.61 4.47 6.78 0.00 7.28 6.71 4.00
 [7,] 10.25 8.00 7.21 8.19 7.68 7.28 0.00 4.69 7.14
                                                     3.61
 [8,] 7.42 4.24 4.90 6.71 6.56 6.71 4.69 0.00 7.42 6.56
 [9,] 9.27 7.68 4.58 6.16 8.83 4.00 7.14 7.42 0.00
                                                     5.83
[10,] 9.27 8.77 7.14 7.87 6.48 6.16 3.61 6.56 5.83 0.00
```

Note each row of an empirical data n*p matrix represents an observation/vector with P dimensions. Therefore, the entry[i, j] on a n*n Euclidean distance matrix must be a scalar rather than a vector and represents the euclidean distance between ith observation/vector and jth observation/vector.

0.5.2 E1.5 Part 2 Create the City Block Distance Matrix

Here this question raises alternative concept called city block distance. It is the sum of the absolute differences of the blocks' coordinates.

```
> # write a function that can get city block distance
> city_matrix<-function(a_matrix){</pre>
```

```
# first define a function to get the eu distance of any two vectors
+
    city_distance <- function(vec_1, vec_2){</pre>
      city_dist <- sum(abs(vec_1-vec_2))</pre>
+
      return(city_dist)
      }
+
    m <- nrow(a_matrix)</pre>
    c_matrix <- matrix(nrow = m, ncol = m)</pre>
    for (i in 1:m ) {
+
      for (j in 1:m) {
         c_matrix[i,j] <- city_distance(a_matrix[i,], a_matrix[j,])</pre>
+
      }
+
    }
    return(c_matrix)
```

This function seems to work well. Try it on the given data:

```
> city_matrix(multi_mat)
        [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
 [1,]
           0
                13
                       11
                             16
                                     8
                                                21
                                                       15
                                                             20
                                                                     18
                                          14
 [<mark>2</mark>,]
          13
                 0
                       10
                             11
                                   17
                                          15
                                                16
                                                        8
                                                             15
                                                                     15
 [3,]
          11
                10
                        0
                             11
                                   11
                                           7
                                                14
                                                       10
                                                              9
                                                                     15
 [4,]
          16
                       11
                              0
                                   16
                                           8
                                                15
                                                       13
                                                             12
                                                                     14
                11
 [<mark>5</mark>,]
          8
                17
                       11
                             16
                                     0
                                          12
                                                13
                                                       11
                                                             16
                                                                     14
 [<mark>6,]</mark>
          14
                15
                       7
                              8
                                          0
                                                       13
                                                              8
                                                                     12
                                   12
                                                11
 [7,]
          21
                16
                       14
                             15
                                   13
                                          11
                                                 0
                                                        8
                                                             13
                                                                     7
 [8,]
          15
                 8
                       10
                             13
                                   11
                                          13
                                                  8
                                                        0
                                                             13
                                                                     13
 [<mark>9</mark>,]
          20
                15
                        9
                             12
                                   16
                                           8
                                                13
                                                       13
                                                              0
                                                                     12
[10,]
          18
                15
                       15
                                   14
                                          12
                                                       13
                                                             12
                                                                      0
                             14
```

Certainly, there is a simpler way to calculate the distance by using the dist() function. Here, I want to practice and hone my understanding about R coding and basic logic of types of distance. Therefore, this script might look not that concise and elegant. Thanks!