$$\neg \Box A, i \qquad \qquad \neg \diamondsuit A, i$$

$$\downarrow \qquad \qquad \downarrow$$

$$\diamondsuit \neg A, i \qquad \qquad \Box \neg A, i$$

Both need to be true
$$\begin{cases} \Box A, i \\ iRj \end{cases}$$

$$A, j$$

$$\diamondsuit \mathbf{A},$$
i
$$\bigvee^{\diamondsuit \mathbf{A},\text{ i}}$$
j has to be new $\begin{cases} iRj\\A,j \end{cases}$

$$(A \supset B), i$$

$$\neg A, i \qquad B, i$$

$$(A \lor B),i$$

$$A,i \qquad B,i$$

$$\neg (A \land B), i$$

$$\neg A, i \qquad \neg B, i$$

$$\neg (A \supset B), i$$

$$\downarrow$$

$$A, i$$

$$\neg B, i$$

$$\neg (A \lor B), i$$
$$\neg A, i$$
$$\neg B, i$$

$$(A \equiv B),i$$

$$A,i \qquad \neg A,i$$

$$B,i \qquad \neg B,i$$

$$(\neg \neg A), i$$
 A, i

$$(A \wedge B), i$$

$$A, i$$

$$B, i$$

$$\neg (A \equiv B), i$$

$$\neg A, i \qquad A, i$$

$$B, i \qquad \neg B, i$$

 ρ (rho), reflexivity: for all w, wRw.

 σ (sigma), symmetry: for all w1 , w2 , if w1Rw2 , then w2Rw1.

 τ (tau), transitivity: for all w1, w2, w3, if w1Rw2 and w2Rw3, then w1Rw3

 η (eta), extendability: for all w1, there is a w2 such that w1Rw2.



Tableaux Rules for C

Tableaux Rules for C+

$$\neg (\mathbf{A} > \mathbf{B}), \, \mathbf{i}$$

$$\downarrow$$

$$\neg A, i$$

$$A, i$$

$$iR_A i$$

$$j \text{ has to be new } \begin{cases} iR_A j & iR_A i \\ \neg B, j & iR_A \end{cases}$$

Strict Conditional

$$A \rightarrow B \leftrightarrow \Box(A \supset B)$$

K3, L3, LP, RM3

 $\label{eq:K3-designated} \textbf{K3-designated truth value} = 1 \\ i = neither\ true\ nor\ false$

\supset	1	i	0
1	1	i	0
i	1	i	i
0	1	1	1

 $\begin{aligned} \textbf{L3} & \text{- designated truth value} &= 1 \\ i &= neither \ true \ nor \ false \end{aligned}$

U	1	i	0
1	1	i	0
i	1	1	i
0	1	1	1

 \mathbf{LP} - designated truth values = 1, i $i=both\ true\ and\ false$

⊃	1	i	0
1	1	i	0
i	1	i	i
0	1	1	1

 ${\bf RM3}$ - designated truth values = 1, i $i{=}both\ true\ and\ false$

\supset	1	i	0
1	1	0	0
i	1	i	0
0	1	1	1