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CS 35201

Homework 2

1. If a binary signal is sent over a 3-kHz channel whose signal-to-noise ratio is 20 dB, what is the maximum achievable data rate? How about when the channel is noise free.

A) with noise

$B \log_2(1 + S/N) = \text{maximum number of bits/sec}$

$10 \log_{10}(S/N) = 20 \rightarrow S/N = 100$

$3000 \log_2(1+100) = 3000(6.6582114828) = 19,974.63445 \text{ bits/sec}$

B) without noise

$2 B \log_2 M = C$

$2(3000) \log_2(2) = 6000(1) = 6000 \text{ bits/sec}$

2. Ten signals, each requiring 4000 Hz, are multiplexed onto a single channel using FDM. What is the minimum bandwidth required for the multiplexed channel? Assume that the guard bands are 400 Hz wide. What is maximum achievable data rate with 8-level signals ?

A) What is the minimum bandwidth required for the multiplexed channel?

$(10 \times 4000) + (9 \times 400) = 43,600 \text{ Hz}$

B) What is maximum achievable data rate with 8-level signals ?

$2 B \log_2 M = C$

$2(43,600) \log_2(8) = 87,200(3) = 261,600 \text{ bits/sec}$

3. What is the latency of a call originating at the North Pole to reach the South Pole if the call is routed via Iridium satellites? Assume that the switching time at the satellites is 10 microseconds and earth's radius is 6371 km. Assume speed of light is $3 \times 10^8 \text{ m/s}$.

$(750 + 6371) \times 1000 = 7,121,000 \text{ m radius}$

$2 \times 3.14 \times 7,121,000 = 44,742,562.57 \text{ m circumference}$

$44,742,562.57 \text{ m} / 2 = 22,371,281.29 \text{ m distance from north pole to south pole}$

$22,371,281.29 \text{ m} / 300,000,000 = 0.07457093763 \text{ sec latency from north pole to south pole without satellites}$

180 degrees from north pole to south pole / 32 degrees between each satellite = 5.625 satellites
from north pole to south pole we'll round up to 6 since there can't be fractions of a satellite

$10 \text{ microseconds} / 1,000,000 = .00001 \text{ sec switching time per satellite}$

so,

$0.07457093763 + (.00001 \times 6) = 0.07457093763 + .00006 = 0.07463093763 \text{ seconds total latency from north pole to south pole}$

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4. In a typical mobile phone system with hexagonal cells, it is forbidden to reuse a frequency band in an adjacent cell. If 840 frequencies are available, how many can be used in a given cell?

Each cell has six sides so for each cell in use we need to reserve 7 cells. One for use and six for each of the used cell's sides.

So, $840 \text{ frequencies} / 7 \text{ cells} = 120 \text{ usable cells}$

5. Code Division Multiple Access (CDMA) is critical technology used in both cell phones and WiFi. Another name for that is Spread Spectrum.

(a) Briefly explain why do we call it Spread Spectrum?

We call it spread spectrum because, we take a signal with a particular bandwidth and spread it over a wider bandwidth in the frequency domain.

(b) How does direct sequence work? Give an example not in book or my lecture notes.

Direct sequence is a technique in which a transmitted signal is divided and transmitted simultaneously on as many frequencies as possible within a given frequency band. Direct sequence then adds redundant bits to the data to make it more immune to interference.

Example: GPS

(c) How does frequency hopping work? Give an example not in book or my lecture notes.

Frequency hopping is a technique in which transmitted signals are continuously changed among many different frequencies within a large spectral band.

Example: a variation adaptive frequency-hopping is used in Bluetooth