



**Bilkent University**  
**Department of Industrial Engineering**

**IE 400 - Principles of Engineering Management**

**Term Project**

**Group: 41**

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## **Table of Contents**

**1. Depot-Train Assignment Problem**

**3**

**2. Railway Development Project**

**4**

# 1. Depot-Train Assignment Problem

**Objective Function:**

$$\text{Minimize}(\sum_{i=1}^{15} ((startToX_i + endToX_i) \times x_{i1}) + (startToY_i + endToY_i) \times x_{i2}))$$

**Decision Variable(s):**

$$x_{ij} = \{1 \text{ if train } i \text{ is assigned to depot } j, 0 \text{ otherwise}\}$$

**Parameter(s):**

$$pathStartingWith_{ik} = \{1 \text{ if the start node of the path of train } i \text{ is node } k, 0 \text{ otherwise}\}$$

$$startToX_i = \text{The distance from the start node of the path of train } i \text{ to depot } X$$

$$endToX_i = \text{The distance from the end node of the path of train } i \text{ to depot } X$$

$$startToY_i = \text{The distance from the start node of the path of train } i \text{ to depot } Y$$

$$endToY_i = \text{The distance from the end node of the path of train } i \text{ to depot } Y$$

**Constraint(s):**

$$\sum_{i=1}^{15} (x_{i1}) \geq 5$$

$$\sum_{i=1}^{15} (x_{i2}) \geq 5$$

$$\sum_{k=1}^8 (\sum_{i=1}^{15} (x_{ij} \times pathStartingWith_{ik})) \leq 3$$

$$x_{i1} + x_{i2} = 5, \text{ for all } i$$

## Objective Value and Values for Decision Variables:

$$\text{Objective value} = 35.0$$

Rows are assigned depots, columns are assigned trains.

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
X	1	1	0	0	0	1	0	1	1	0	1	1	0	0	1
Y	0	0	1	1	1	0	1	0	0	1	0	0	1	1	0

Here is the result (screenshot):

```
PS C:\Users\User\Desktop\ders\ie400\ie400-project\ie400-project> py part1.py
Version Identifier: 22.1.1.0 | 2023-06-15 | d64d5bd77
CXPARAM_Read_DataCheck 1
Found incumbent of value 45.000000 after 0.00 sec. (0.00 ticks)
Tried aggregator 3 times.
MIP Presolve eliminated 25 rows and 22 columns.
MIP Presolve added 1 rows and 1 columns.
MIP Presolve modified 5 coefficients.
Aggregator did 9 substitutions.
All rows and columns eliminated.
Presolve time = 0.00 sec. (0.06 ticks)

Root node processing (before b&c):
  Real time = 0.00 sec. (0.06 ticks)
Parallel b&c, 12 threads:
  Real time = 0.00 sec. (0.00 ticks)
  Sync time (average) = 0.00 sec.
  Wait time (average) = 0.00 sec.
-----
Total (root+branch&cut) = 0.00 sec. (0.06 ticks)
Obj Value: 35.0
Values of Decision Variables: [1.0, 0.0, 1.0, 0.0, 0.0, 1.0, 0.0, 1.0, 0.0, 1.0, 0.0, 1.0, 1.0, 0.0, 0.0, 1.0, 1.0, 0.0, 1.0, 0.0, 0.0, 1.0, 0.0, 1.0, 1.0, 0.0]
PS C:\Users\User\Desktop\ders\ie400\ie400-project\ie400-project>
```

## 2. Railway Development Project

### Objective Function:

$$\text{Minimize}(\text{totalEnergyCost} + \text{totalPurchaseCost} + \text{totalStationCost})$$

### Decision Variable(s):

$$N_i = \{1 \text{ if train } i \text{ is assigned to depot } X, 0 \text{ if train } i \text{ is assigned to depot } Y\}$$

$$E_i = \{1 \text{ if train } i \text{ is an electric train, } 0 \text{ if train } i \text{ is a diesel train}\}$$

$$c_{ijt} = \{1 \text{ if train } i \text{ is being charged at node } j \text{ in time } t, 0 \text{ otherwise}\}$$

$$s_j = \text{Number of electric charging stations at node } j$$

**Parameter(s):**

$$IN\_DEPOT\_CHARGE\_STATION = \$1000000$$

$$ON\_ROUTE\_CHARGE\_STATION = \$350000$$

$$IN\_DEPOT\_FUEL\_STATION = \$800000$$

$$ELECTRIC\_PURCHASE = \$750000$$

$$DIESEL\_PURCHASE = \$250000$$

$$ELECTRIC\_ENERGY\_BWH = \$20000$$

$$DIESEL\_ENERGY\_BWH = \$100000$$

$$pathDurations_i = \text{path durations of train } i = \{1, 15\}$$

$$exact\_timestamps_{ik} = \text{total elapsed time for train } i \text{ at the } k\text{'th node of its path}$$

$$exact\_paths_{ik} = k\text{'th node of train } i$$

$$totalEnergyCost = \sum_{i=1}^{15} (pathDurations_i \times E_i \times ELECTRIC\_ENERGY\_BWH) + \sum_{i=1}^{15} (pathDurations_i \times (1 - E_i) \times DIESEL\_ENERGY\_BWH)$$

$$totalPurchaseCost = \sum_{i=1}^{15} (E_i \times ELECTRIC\_PURCHASE + (1 - E_i) \times DIESEL\_PURCHASE)$$

$$totalStationCost = \sum_{j=1}^8 ((S_i \times ON\_ROUTE\_CHARGE\_STATION) +$$

$$(ceil) \left( \sum_{j=1}^{15} E_i \times N_i / 3 \right) \times IN\_DEPOT\_CHARGING\_STATION +$$

$$(ceil) \left( \sum_{j=1}^{15} E_i \times (1 - N_i) / 3 \right) \times IN\_DEPOT\_CHARGING\_STATION +$$

$$(ceil) \left( \sum_{j=1}^{15} (1 - E_i) \times N_i / 2 \right) \times IN\_DEPOT\_FUEL\_STATION +$$

$$(ceil) \left( \sum_{j=1}^{15} (1 - E_i) \times (1 - N_i) / 2 \right) \times IN\_DEPOT\_FUEL\_STATION)$$

$J_{ik}$  = Remaining energy of train  $i$  at  $k$ 'th node of  $exact\_path_{i,k}$

$$J_{ik} = E_i \times ((1 - c_{i,j,t}) \times (J_{i(k-1)} - (exact\_timestamps_{i,k} - exact\_timestamps_{i,(k-1)}) \\ + c_{i,exact\_paths_{i,k},exact\_timestamps_{i,k}} \times 8) + (1 - E_i) \times 20$$

**Constraint(s):**

$$\sum_{i=1}^{15} c_{i,j,t} \leq S_j \text{ for } j = \{1, 8\} \text{ } t = \{1, 20\}$$

$$J_{i(k-1)} - (pathTime[i][k] - pathTime[i][k - 1]) \geq 0$$

$$J_{i0} = (1 - E_i) \times 20 + E_i \times 8$$

**Objective Value and Values for Decision Variables:**

```
Train 0 is electric
Train 1 is electric
Train 2 is electric
Train 3 is electric
Train 4 is electric
Train 5 is electric
Train 6 is electric
Train 7 is electric
Train 8 is electric
Train 9 is electric
Train 10 is electric
Train 11 is electric
Train 12 is electric
Train 13 is electric
Train 14 is electric
Node F has 1.0 charging stations
Node A has 1.0 charging stations
Node H has 1.0 charging stations
Node X has 1.0 charging stations
Node C has 1.0 charging stations
Node B has 1.0 charging stations
Node D has 1.0 charging stations
Node E has 1.0 charging stations
Node G has 1.0 charging stations
Final Total Cost: 20090000.0
PS C:\Users\User\Desktop\ders\ie400\ie400-project\
```

As can be seen, all trains are determined to be electric trains. Nodes A, B, C, D, E, F, G, H (all nodes) and depot X are determined to include an electric charge station. There exists no fuel station due to the lack of diesel trains. Depot Y does not include any electric charge station. All nodes include just one electric charge station.

Lastly, the total cost is \$20,090,000.