

$$\begin{aligned} b) A(x) &= \pi (x^2 + 5)^2 \\ &= \pi [(x^2 + 5)(x^2 + 5)] \\ &= \pi [x^4 + 10x^2 + 25] \end{aligned}$$

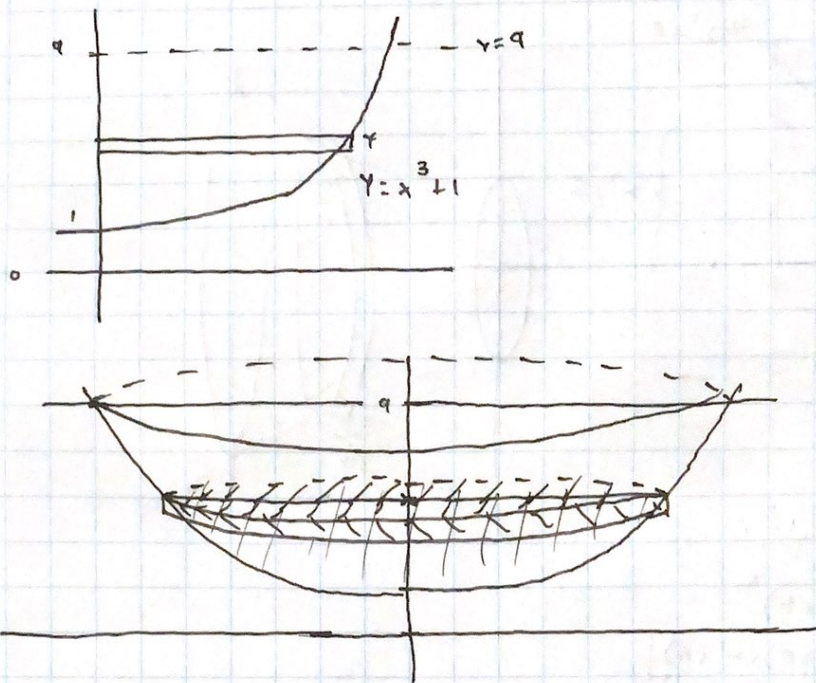
$$V = \int_0^3 \pi (x^4 + 10x^2 + 25) dx = \pi \int_0^3 x^4 + 10x^2 + 25 dx$$

$$c) V = \pi \int_0^3 x^4 + 10x^2 + 25 dx$$

$$= \pi \left[\frac{x^5}{5} + 10 \frac{x^3}{3} + 25x \right]_0^3 = \pi \left[(0) - \left(\frac{3^5}{5} + \frac{10 \cdot 3^3}{3} + \frac{25(3)}{1} \right) \right]$$

$$= -\pi \left[\right]$$

$$= 1068\pi/5.$$



A slice at height y will get a disk radius x

$$y = x^3 + 1$$

$$y - 1 = x^3$$

$$\sqrt[3]{y-1} = x$$

So the area of the cross-section is $A(y) = \pi (\sqrt[3]{y-1})^2$
 $= \pi (y-1)^{2/3}$

$$V = \int_1^9 A(y) dy = \int_1^9 \pi (y-1)^{2/3} dy$$

$$= \pi \int_1^9 (y-1)^{2/3} dy$$

$$= \pi \int_1^9 y^{2/3} - 1 dy$$

$$= \pi \left[\frac{3}{5} y^{5/3} - y \right]_1^9$$

$$= \frac{96\pi}{5}$$