In terms of  $\alpha$  and  $\beta$ , express all the lengths and other angle measures ( $\theta$  and  $\phi$ ).



Variable	Algebraic expression
p =	
q =	
r =	
s =	
$\theta =$	
t =	
u =	
$\phi =$	
v =	
w =	

The angle-sum and angle-difference identities are true for any  $\alpha$  and  $\beta$ :

$$\sin(\alpha \pm \beta) = \sin(\alpha)\cos(\beta) \pm \cos(\alpha)\sin(\beta)$$

$$\cos(\alpha \pm \beta) = \cos(\alpha)\cos(\beta) \mp \sin(\alpha)\sin(\beta)$$

You know the following:

$$\sin(30^\circ) = \frac{1}{2}$$

$$\sin(225^\circ) = \frac{-\sqrt{2}}{2}$$

$$\cos(30^\circ) = \frac{\sqrt{3}}{2}$$

$$\cos(225^\circ) = \frac{-\sqrt{2}}{2}$$

Determine  $\cos(-195^{\circ})$  exactly.

Prove that sin(2x) = 2 sin(x) cos(x) for any x.

(Hint: start with an angle-sum formula from Question 2.)

## Question 4

Prove that  $cos(2x) = 2cos^2(x) - 1$  for any x.

(Hint: start with an angle-sum formula from Question 2. Also, you will need to use the Pythagorean Identity:  $\sin^2(x) + \cos^2(x) = 1$ )

Prove that  $\cos\left(\frac{y}{2}\right) = \sqrt{\frac{1+\cos(y)}{2}}$ . (Technically this assumes  $\cos(y/2) > 0$ , but let's not worry about that here.)

(Hint: use the identity proved in Question 4.)

## Question 6

If you knew that  $\cos(110^\circ) \approx -0.34$ , then what is  $\cos(55^\circ)$ ? Please set up an expression, but do **not** try to simplify or evaluate a decimal approximation.

(Hint: 110/2 = 55.)