## Polynomial Operations SOLUTIONS (version 37)

1. Let polynomials p(x) and q(x) be defined below.

$$p(x) = 8x^5 + 2x^4 - 5x^2 + 4x - 1$$

$$q(x) = 3x^5 - x^4 - 4x^3 + 7x + 2$$

Express the sum of p(x) + q(x) in standard form.

Get "unsimplified" forms. Then find p(x) + q(x) with addition/subtraction.

$$p(x) = (8)x^5 + (2)x^4 + (0)x^3 + (-5)x^2 + (4)x^1 + (-1)x^0$$

$$q(x) = (3)x^5 + (-1)x^4 + (-4)x^3 + (0)x^2 + (7)x^1 + (2)x^0$$

$$p(x) + q(x) = (11)x^{5} + (1)x^{4} + (-4)x^{3} + (-5)x^{2} + (11)x^{1} + (1)x^{0}$$

$$p(x) + q(x) = 11x^5 + x^4 - 4x^3 - 5x^2 + 11x + 1$$

2. Let polynomials a(x) and b(x) be defined below.

$$a(x) = 4x^2 + 8x - 7$$

$$b(x) = -2x - 5$$

Express the product  $a(x) \cdot b(x)$  in standard form.

You can use a table for multiplication.

*	$4x^2$	8x	-7
-2x	$-8x^{3}$	$-16x^{2}$	14x
-5	$-20x^{2}$	-40x	35

$$a(x) \cdot b(x) = -8x^3 - 16x^2 - 20x^2 + 14x - 40x + 35$$

Combine like terms.

$$a(x) \cdot b(x) = -8x^3 - 36x^2 - 26x + 35$$

3. Express  $(x+1)^5$  in standard (expanded) form.

Remember the binomial theorem. It tells us to use Pascal's triangle.

$$x^5 + 5x^4 + 10x^3 + 10x^2 + 5x + 1$$

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4. Let polynomials f(x) and g(x) be defined below.

$$f(x) = 3x^3 + 25x^2 + 12x + 23$$
$$g(x) = x + 8$$

The quotient of  $\frac{f(x)}{g(x)}$  can be expressed as a polynomial, h(x), and a remainder, R (a real number).

$$\frac{f(x)}{g(x)} = h(x) + \frac{R}{x+8}$$

By using synthetic division or long division, express h(x) in standard form, and find the remainder R.

I prefer using synthetic division.

So,

$$\frac{f(x)}{g(x)} = 3x^2 + x + 4 + \frac{-9}{x+8}$$

In other words,  $h(x) = 3x^2 + x + 4$  and the remainder is R = -9.

5. Let polynomial f(x) still be defined as  $f(x) = 3x^3 + 25x^2 + 12x + 23$ . Evaluate f(-8).

You could do this the hard way.

$$f(-8) = (3) \cdot (-8)^3 + (25) \cdot (-8)^2 + (12) \cdot (-8) + (23)$$

$$= (3) \cdot (-512) + (25) \cdot (64) + (12) \cdot (-8) + (23)$$

$$= (-1536) + (1600) + (-96) + (23)$$

$$= -9$$

Or, if you reference the polynomial remainder theorem, you can state that you know f(-8) equals the remainder when f(x) is divided by x + 8. Thus, f(-8) = -9.

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