Polynomial Factoring solution (version 38)

1. The quadratic formula says if $ax^2 + bx + c = 0$ then $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$. Use the quadratic formula to solve the following equation.

$$x^2 + 4x + 28 = 0$$

Simplify your answer(s) as much as possible.

Solution

$$x = \frac{-(4) \pm \sqrt{(4)^2 - 4(1)(28)}}{2(1)}$$
$$x = \frac{-(4) \pm \sqrt{16 - 112}}{2(1)}$$

$$x = \frac{-4 \pm \sqrt{-96}}{2}$$

$$x = \frac{-4 \pm \sqrt{-16 \cdot 6}}{2}$$

$$x = \frac{-4 \pm 4\sqrt{6}\,i}{2}$$

$$x = -2 \pm 2\sqrt{6}i$$

Notice that i in NOT under the square-root radical symbol!!

2. Express the product of -9 + 8i and -2 - 6i in standard form (a + bi).

Solution

$$(-9+8i)\cdot(-2-6i)$$

$$18 + 54i - 16i - 48i^2$$

$$18 + 54i - 16i + 48$$

$$18 + 48 + 54i - 16i$$

$$66 + 38i$$

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3. Write function $f(x) = x^3 - 8x^2 + 17x - 10$ in factored form. I'll give you a hint: one factor is (x-5).

Solution

$$f(x) = (x-5)(x^2 - 3x + 2)$$

$$f(x) = (x-5)(x-1)(x-2)$$

4. Polynomial p is defined below in factored form.

$$p(x) = (x+5)^2 \cdot (x+1) \cdot (x-2)^2 \cdot (x-6)$$

Sketch a graph of polynomial y = p(x).

