Polynomial Factoring solution (version 10)

1. The quadratic formula says if $ax^2 + bx + c = 0$ then $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$. Use the quadratic formula to solve the following equation.

$$x^2 + 2x + 21 = 0$$

Simplify your answer(s) as much as possible.

Solution

$$x = \frac{-(2) \pm \sqrt{(2)^2 - 4(1)(21)}}{2(1)}$$
$$x = \frac{-(2) \pm \sqrt{4 - 84}}{2(1)}$$

$$x = \frac{-2 \pm \sqrt{-80}}{2}$$

$$x = \frac{-2 \pm \sqrt{-16 \cdot 5}}{2}$$

$$x = \frac{-2 \pm 4\sqrt{5}\,i}{2}$$

$$x = -1 \pm 2\sqrt{5}\,i$$

Notice that i in NOT under the square-root radical symbol!!

2. Express the product of -6 + 2i and -5 + 3i in standard form (a + bi).

Solution

$$(-6+2i)\cdot(-5+3i)$$

$$30 - 18i - 10i + 6i^2$$

$$30 - 18i - 10i - 6$$

$$30 - 6 - 18i - 10i$$

$$24 - 28i$$

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3. Write function $f(x) = x^3 + x^2 - 26x + 24$ in factored form. I'll give you a hint: one factor is (x+6).

Solution

$$f(x) = (x+6)(x^2 - 5x + 4)$$

$$f(x) = (x+6)(x-1)(x-4)$$

4. Polynomial p is defined below in factored form.

$$p(x) = -(x+6) \cdot (x+3) \cdot (x-1) \cdot (x-4)^2$$

Sketch a graph of polynomial y = p(x).

