

Name: \_\_\_\_\_

Date: \_\_\_\_\_

**Exam: Function Reflections (Solution version 16)**

1. Let function  $f$  be defined by the polynomial below:

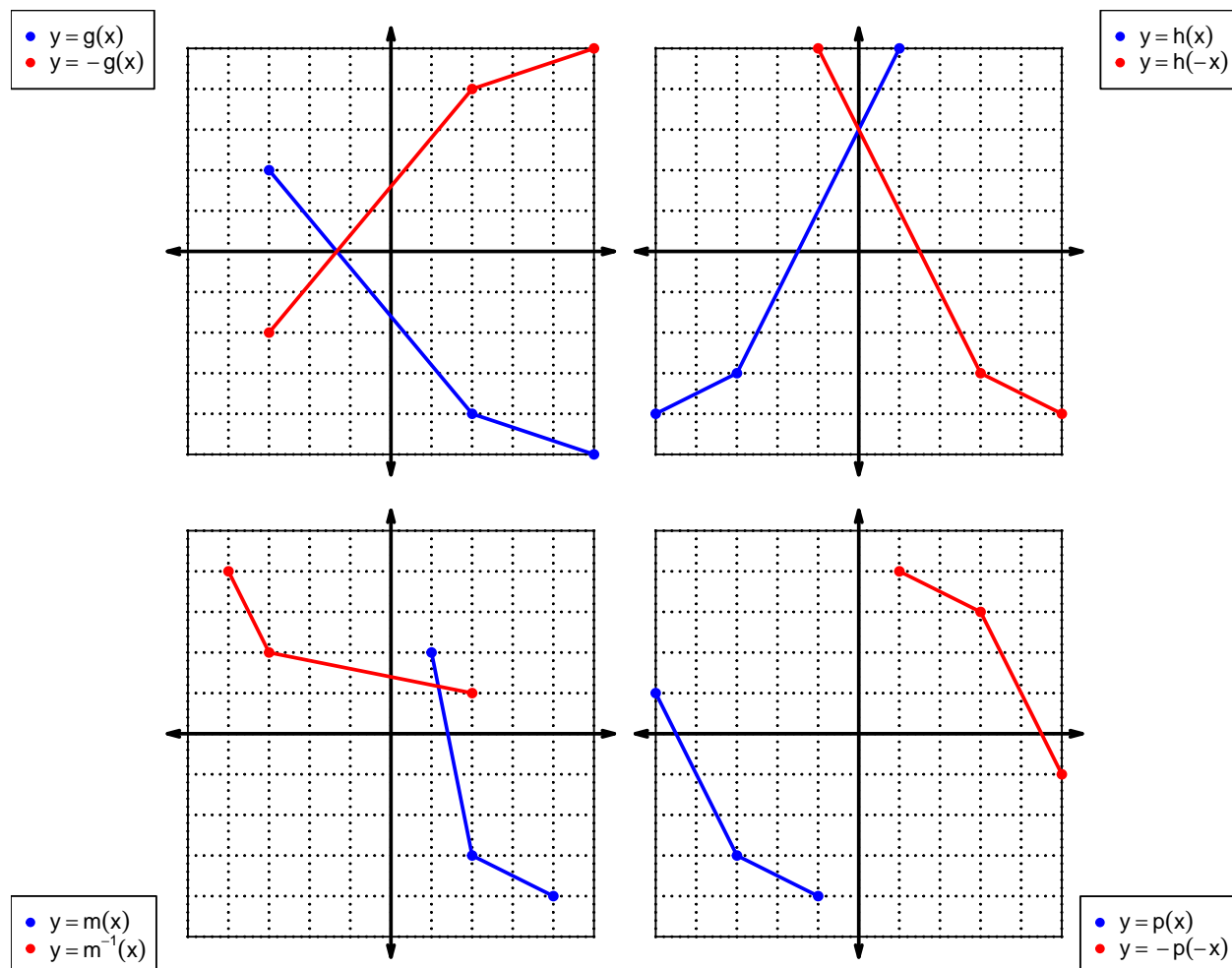
$$f(x) = 8x^4 + 4x^3 + 6x^2 - 9x + 5$$

Draw lines that match each function reflection with its polynomial:

**Reflections****Polynomials**

|          |   |   |                                |
|----------|---|---|--------------------------------|
| $f(-x)$  | ● | ● | $-8x^4 - 4x^3 - 6x^2 + 9x - 5$ |
| $-f(-x)$ | ● | ● | $8x^4 - 4x^3 + 6x^2 + 9x + 5$  |
| $-f(x)$  | ● | ● | $-8x^4 + 4x^3 - 6x^2 - 9x - 5$ |

2. In each  $xy$  plane shown below, a function is graphed with blue. Draw the indicated reflections (as a second curve, indicated in legend) with black (or with whatever you have). The  $x$  axis is horizontal and the  $y$  axis is vertical (as typical), and the scale is equal on both axes.



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For all questions on this page, the functions  $f$ ,  $g$ , and  $h$  are defined by the table below.

| $x$ | $f(x)$ | $g(x)$ | $h(x)$ |
|-----|--------|--------|--------|
| 1   | 8      | 8      | 5      |
| 2   | 1      | 9      | 6      |
| 3   | 5      | 2      | 1      |
| 4   | 9      | 3      | 7      |
| 5   | 2      | 4      | 4      |
| 6   | 4      | 1      | 9      |
| 7   | 6      | 5      | 2      |
| 8   | 7      | 6      | 3      |
| 9   | 3      | 7      | 8      |

3. Evaluate  $h(3)$ .

$$h(3) = 1$$

4. Evaluate  $f^{-1}(4)$ .

$$f^{-1}(4) = 6$$

5. By filling more rows of the table, it is possible to make function  $f$  **even**. If that were done, what would be the value of  $f(-7)$ ?

If function  $f$  is even, then

$$f(-7) = 6$$

6. By filling more rows of the table, it is possible to make function  $g$  **odd**. If that were done, what would be the value of  $g(-5)$ ?

If function  $g$  is odd, then

$$g(-5) = -4$$

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7. A function,  $f$ , is **even** if  $f(x) = f(-x)$  for all  $x$  in the domain. A function,  $g$ , is **odd** if  $g(x) = -g(-x)$  for all  $x$  in the domain.

Let polynomial  $p$  be defined with the following equation:

$$p(x) = -x^3 + x$$

- a. Express  $p(-x)$  as a polynomial in standard form.

$$p(-x) = -(-x)^3 + (-x)$$

$$p(-x) = x^3 - x$$

- b. Express  $-p(-x)$  as a polynomial in standard form.

$$-p(-x) = -(x^3 - x)$$

$$-p(-x) = -x^3 + x$$

- c. Is polynomial  $p$  even, odd, or neither?

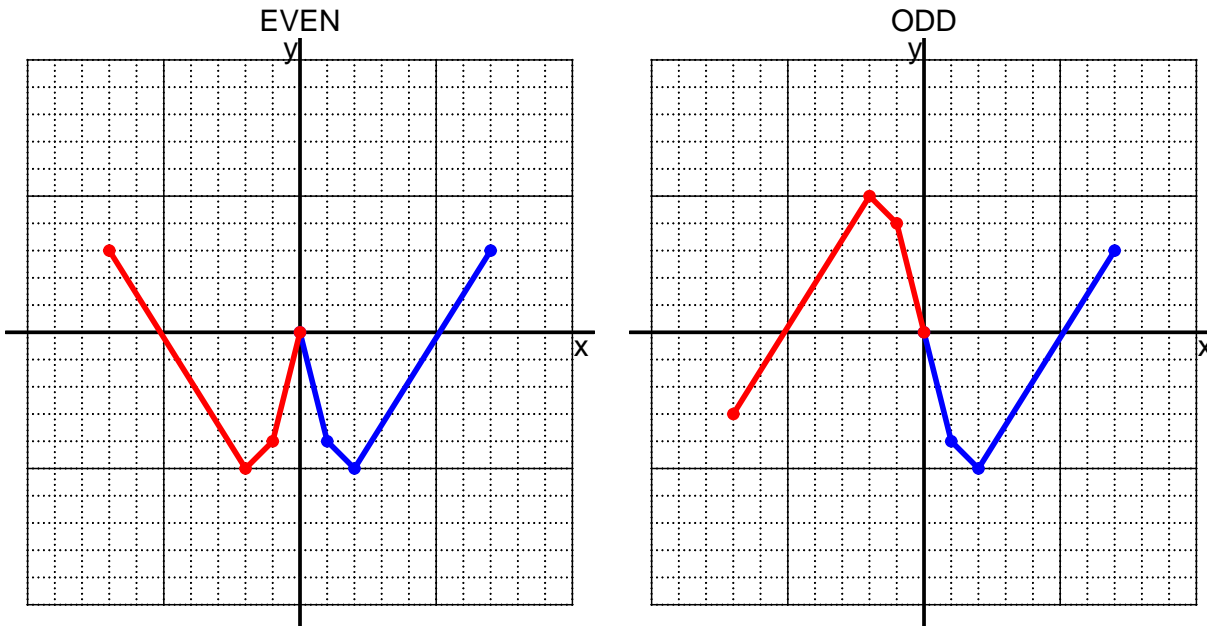
odd

- d. Explain how you know the answer to part c.

We see that  $p(x) = -p(-x)$  for all  $x$  because  $p(x)$  and  $-p(-x)$  are equivalent polynomials. Thus function  $p$  satisfies the criterion for being an odd function.

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8. I have drawn half of a function. Draw the other half to make it even or odd.



9. Let function  $f$  be defined with the equation below.

$$f(x) = 5(x - 9)$$

- a. Evaluate  $f(23)$ .

step 1: subtract 9  
step 2: multiply by 5

$$\begin{aligned} f(23) &= 5((23) - 9) \\ f(23) &= 70 \end{aligned}$$

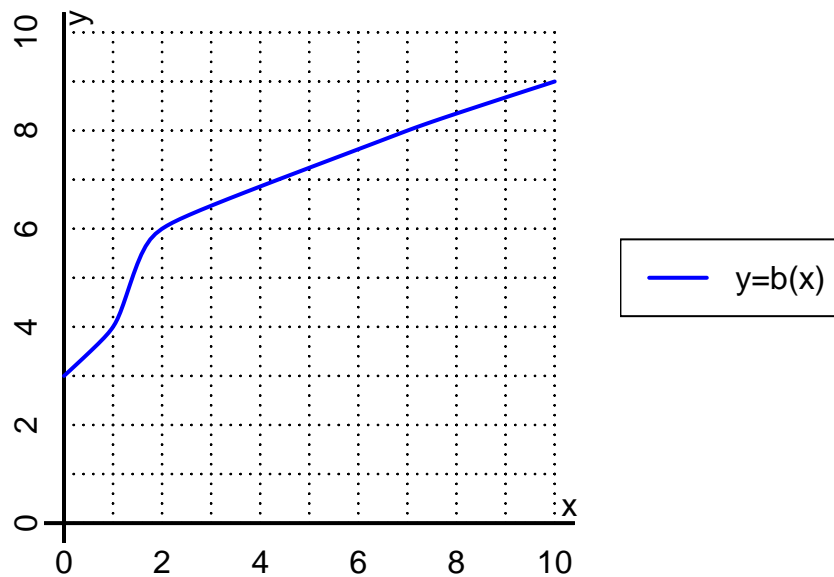
- b. Evaluate  $f^{-1}(25)$ .

step 1: divide by 5  
step 2: add 9

$$\begin{aligned} f^{-1}(x) &= \frac{x}{5} + 9 \\ f^{-1}(25) &= \frac{(25)}{5} + 9 \\ f^{-1}(25) &= 14 \end{aligned}$$

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10. The function  $b$  is represented by the curve  $y = b(x)$  graphed below.



a. Evaluate  $b(7)$ .

$$b(7) = 8$$

b. Evaluate  $b^{-1}(6)$ .

$$b^{-1}(6) = 2$$

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11. Function  $f$  is defined by the table below.

a. Complete the columns for  $-f(x)$  and  $f(-x)$  and  $-f(-x)$ .

| $x$ | $f(x)$ | $-f(x)$ | $f(-x)$ | $-f(-x)$ |
|-----|--------|---------|---------|----------|
| -2  | -9     | 9       | -9      | 9        |
| -1  | 7      | -7      | 7       | -7       |
| 0   | 0      | 0       | 0       | 0        |
| 1   | 7      | -7      | 7       | -7       |
| 2   | -9     | 9       | -9      | 9        |

b. Is function  $f$  even, odd, or neither?

even

c. How do you know the answer to part b?

Function  $f$  is even because column  $f(-x)$  matches column  $f(x)$  exactly.