Polynomial Factoring solution (version 629)

1. The quadratic formula says if $ax^2 + bx + c = 0$ then $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$. Use the quadratic formula to solve the following equation.

$$x^2 + 2x + 3 = 0$$

Simplify your answer(s) as much as possible.

Solution

$$x = \frac{-(2) \pm \sqrt{(2)^2 - 4(1)(3)}}{2(1)}$$
$$x = \frac{-(2) \pm \sqrt{4 - 12}}{2(1)}$$

$$x = \frac{-2 \pm \sqrt{-8}}{2}$$

$$x = \frac{-2 \pm \sqrt{-4 \cdot 2}}{2}$$

$$x = \frac{-2 \pm 2\sqrt{2}\,i}{2}$$

$$x = -1 \pm \sqrt{2}\,i$$

Notice that i in NOT under the square-root radical symbol!!

2. Express the product of -2 + 8i and -3 + 6i in standard form (a + bi).

Solution

$$(-2+8i)\cdot(-3+6i)$$

$$6 - 12i - 24i + 48i^2$$

$$6 - 12i - 24i - 48$$

$$6 - 48 - 12i - 24i$$

$$-42 - 36i$$

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3. Write function $f(x) = x^3 + 6x^2 - 7x - 60$ in factored form. I'll give you a hint: one factor is (x-3).

Solution

$$f(x) = (x-3)(x^2 + 9x + 20)$$

$$f(x) = (x-3)(x+4)(x+5)$$

4. Polynomial p is defined below in factored form.

$$p(x) = -(x+8)^2 \cdot (x+5) \cdot (x+1) \cdot (x-4)^2$$

Sketch a graph of polynomial y = p(x).

