

Name: _____

at1121exam_practice: Radicals and Squares (v615)

Question 1

Simplify the radical expressions.

$$\sqrt{75}$$

$$\sqrt{98}$$

$$\sqrt{8}$$

$$\frac{\sqrt{5 \cdot 5 \cdot 3}}{5\sqrt{3}}$$

$$\frac{\sqrt{7 \cdot 7 \cdot 2}}{7\sqrt{2}}$$

$$\frac{\sqrt{2 \cdot 2 \cdot 2}}{2\sqrt{2}}$$

Question 2

Find all solutions to the equation below:

$$8((x - 7)^2 - 10) = 48$$

First, divide both sides by 8.

$$(x - 7)^2 - 10 = 6$$

Then, add 10 to both sides.

$$(x - 7)^2 = 16$$

Undo the squaring. Remember the plus-minus symbol.

$$x - 7 = \pm 4$$

Add 7 to both sides.

$$x = 7 \pm 4$$

So the two solutions are $x = 11$ and $x = 3$.

Question 3

By completing the square, find both solutions to the given equation. *You must show work for full credit!*

$$x^2 - 16x = 80$$

$$x^2 - 16x + 64 = 80 + 64$$

$$x^2 - 16x + 64 = 144$$

$$(x - 8)^2 = 144$$

$$x - 8 = \pm 12$$

$$x = 8 \pm 12$$

$$x = 20 \quad \text{or} \quad x = -4$$

Question 4

A quadratic polynomial function is shown below in standard form.

$$y = 3x^2 - 24x + 42$$

Express the function in **vertex form** and identify the **location** of the vertex.

From the first two terms, factor out 3 .

$$y = 3(x^2 - 8x) + 42$$

We want a perfect square. Halve -8 and square the result to get 16 . Add and subtract that value inside the parentheses.

$$y = 3(x^2 - 8x + 16 - 16) + 42$$

Factor the perfect-square trinomial.

$$y = 3((x - 4)^2 - 16) + 42$$

Distribute the 3.

$$y = 3(x - 4)^2 - 48 + 42$$

Combine the constants to get **vertex form**:

$$y = 3(x - 4)^2 - 6$$

The vertex is at point $(4, -6)$.