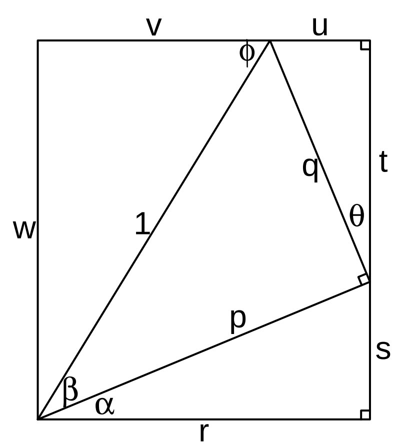
Question 1

In terms of α and β, express all the lengths and other angle measures (θ and ϕ).



Variable	Algebraic expression
p =	
q =	
r =	
s =	
θ =	
t =	
u =	
ϕ =	
v =	
w =	

Question 2

The angle-sum and angle-difference identities are true for any α and β:

$$\begin{aligned} \sin(\alpha \pm \beta) &= \sin(\alpha)\cos(\beta) \pm \cos(\alpha)\sin(\beta) \\ \cos(\alpha \pm \beta) &= \cos(\alpha)\cos(\beta) \mp \sin(\alpha)\sin(\beta) \end{aligned}$$

You know the following:

$$\sin(315^\circ) = \frac{-\sqrt{2}}{2} \qquad \sin(150^\circ) = \frac{1}{2}$$

$$\cos(315^\circ) = \frac{\sqrt{2}}{2} \qquad \cos(150^\circ) = \frac{-\sqrt{3}}{2}$$

Determine $\sin(465^\circ)$ exactly.

Question 3

Prove that $\sin(2x) = 2\sin(x)\cos(x)$ for any x.

(Hint: start with an angle-sum formula from Question 2.)

Question 4

Prove that $\cos(2x) = 2\cos^2(x) - 1$ for any x.

(Hint: start with an angle-sum formula from Question 2. Also, you will need to use the Pythagorean Identity: $\sin^2(x) + \cos^2(x) = 1$*)*

Question 5

Prove that $\cos\left(\frac{y}{2}\right) = \sqrt{\frac{1+\cos(y)}{2}}$. (Technically this assumes $\cos(y/2) > 0$, but let's not worry about that here.)

(Hint: use the identity proved in Question 4.)

Question 6

If you knew that $\cos(130°) \approx -0.64$, then what is $\cos(65°)$? Please set up an expression, but do **not** try to simplify or evaluate a decimal approximation.

(Hint: $130/2 = 65$.*)*