Polynomial Factoring solution (version 632)

1. The quadratic formula says if $ax^2 + bx + c = 0$ then $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$. Use the quadratic formula to solve the following equation.

$$x^2 + 12x + 63 = 0$$

Simplify your answer(s) as much as possible.

Solution

$$x = \frac{-(12) \pm \sqrt{(12)^2 - 4(1)(63)}}{2(1)}$$

$$x = \frac{-(12) \pm \sqrt{144 - 252}}{2(1)}$$

$$x = \frac{-12 \pm \sqrt{-108}}{2}$$

$$x = \frac{-12 \pm \sqrt{-36 \cdot 3}}{2}$$

$$x = \frac{-12 \pm 6\sqrt{3}\,i}{2}$$

$$x = -6 \pm 3\sqrt{3}\,i$$

Notice that *i* in NOT under the square-root radical symbol!!

2. Express the product of 6+3i and 4+9i in standard form (a+bi).

Solution

$$(6+3i) \cdot (4+9i)$$

$$24+54i+12i+27i^{2}$$

$$24+54i+12i-27$$

$$24-27+54i+12i$$

$$-3+66i$$

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3. Write function $f(x) = x^3 - 9x^2 + 20x - 12$ in factored form. I'll give you a hint: one factor is (x-6).

Solution

$$f(x) = (x-6)(x^2 - 3x + 2)$$

$$f(x) = (x-6)(x-2)(x-1)$$

4. Polynomial p is defined below in factored form.

$$p(x) = -(x+5)^2 \cdot (x+1)^2 \cdot (x-2)$$

Sketch a graph of polynomial y = p(x).

