

Name: \_\_\_\_\_

Date: \_\_\_\_\_

**Exam: Function Reflections (EXAM version 609)**

1. (worth 9 points) Let function  $f$  be defined by the polynomial below:

$$f(x) = 9x^5 + 5x^4 + 3x^3 - 4x^2 + 2x + 7$$

Draw lines that match each function reflection with its polynomial:

**Reflections**

**Polynomials**

$-f(-x)$  •

•  $-9x^5 - 5x^4 - 3x^3 + 4x^2 - 2x - 7$

$-f(x)$  •

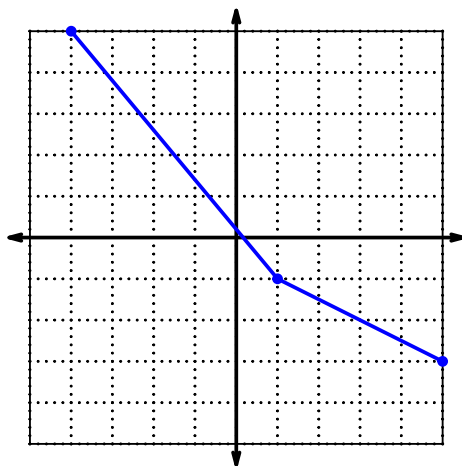
•  $9x^5 - 5x^4 + 3x^3 + 4x^2 + 2x - 7$

$f(-x)$  •

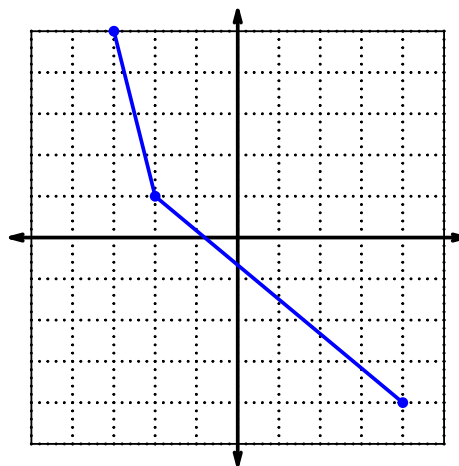
•  $-9x^5 + 5x^4 - 3x^3 - 4x^2 - 2x + 7$

2. (worth 20 points) In each  $xy$  plane shown below, a function is graphed with blue. Draw the indicated reflections (as a second curve, indicated in legend) with black (or with whatever you have). The  $x$  axis is horizontal and the  $y$  axis is vertical (as typical), and the scale is equal on both axes.

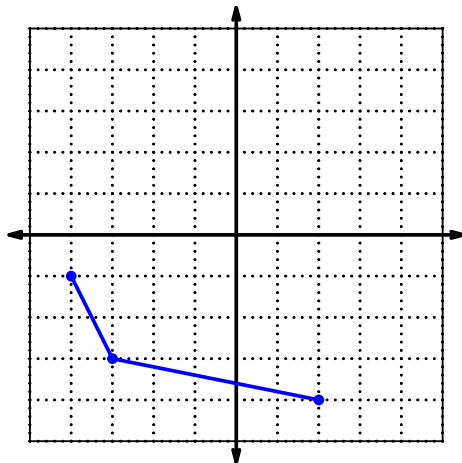
•  $y = g(x)$   
•  $y = -g(x)$



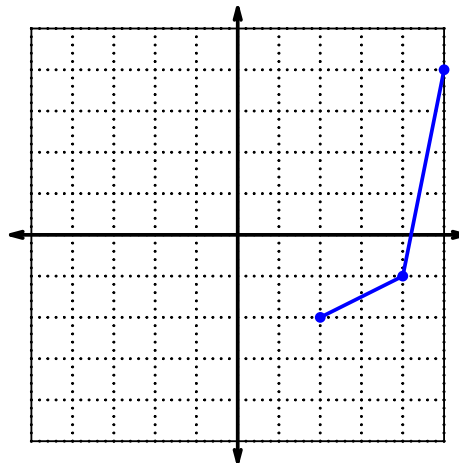
•  $y = h(x)$   
•  $y = -h(-x)$



•  $y = m(x)$   
•  $y = m^{-1}(x)$



•  $y = p(x)$   
•  $y = p(-x)$



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For all questions on this page, the functions  $f$ ,  $g$ , and  $h$  are defined by the table below.

$x$	$f(x)$	$g(x)$	$h(x)$
1	5	8	3
2	1	3	8
3	4	9	5
4	7	6	9
5	6	1	2
6	3	4	7
7	8	2	4
8	9	5	6
9	2	7	1

3. (worth 3 points) Evaluate  $h(5)$ .

4. (worth 3 points) Evaluate  $f^{-1}(7)$ .

5. (worth 3 points) Assuming  $f$  is an **even** function, evaluate  $f(-1)$ .

6. (worth 3 points) Assuming  $g$  is an **odd** function, evaluate  $g(-6)$ .

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7. (worth 15 points) A function,  $f$ , is **even** if  $f(x) = f(-x)$  for all  $x$  in the domain. A function,  $g$ , is **odd** if  $g(x) = -g(-x)$  for all  $x$  in the domain.

Let polynomial  $p$  be defined with the following equation:

$$p(x) = -x^3 - x$$

- a. Express  $p(-x)$  as a polynomial in standard form.

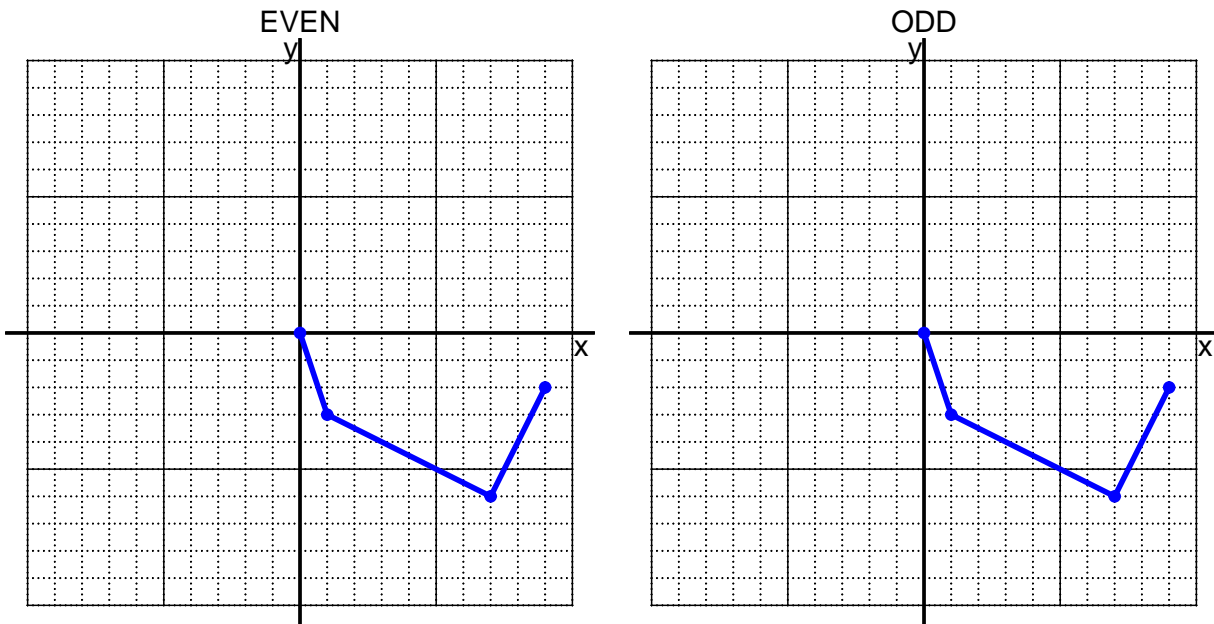
- b. Express  $-p(-x)$  as a polynomial in standard form.

- c. Is polynomial  $p$  even, odd, or neither?

- d. Explain how you know the answer to part c.

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8. (worth 10 points) I have drawn half of a function. Draw the other half to make it even or odd.



9. (worth 10 points) Let function  $f$  be defined with the equation below.

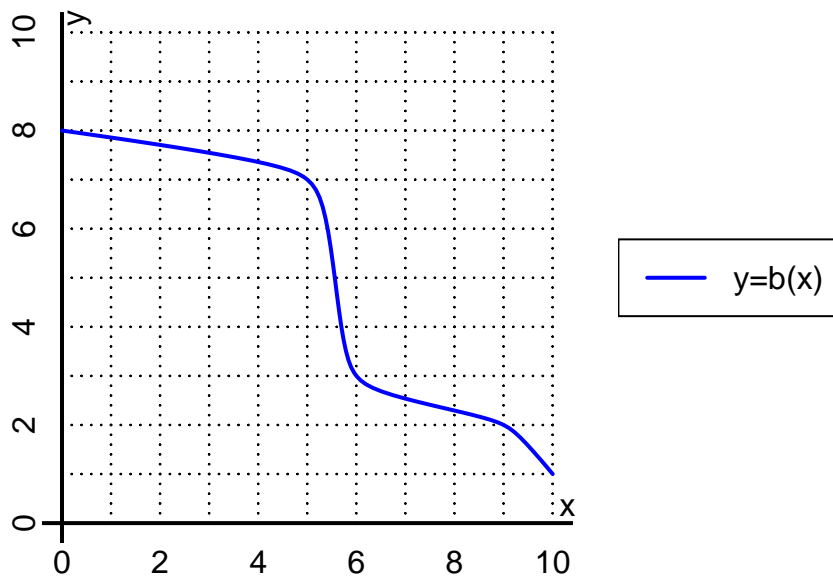
$$f(x) = 7x - 6$$

- a. Evaluate  $f(10)$ .

- b. Evaluate  $f^{-1}(57)$ .

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10. (worth 6 points) The function  $b$  is represented by the curve  $y = b(x)$  graphed below.



a. Evaluate  $b(9)$ .

b. Evaluate  $b^{-1}(7)$ .

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11. (worth 18 points) Function  $f$  is defined by the table below.

a. Complete the columns for  $-f(x)$  and  $f(-x)$  and  $-f(-x)$ .

$x$	$f(x)$	$-f(x)$	$f(-x)$	$-f(-x)$
-2	6			
-1	-3			
0	0			
1	-3			
2	6			

b. Is function  $f$  even, odd, or neither?

c. How do you know the answer to part b?