s18: EXP LOG (SLTN v314)
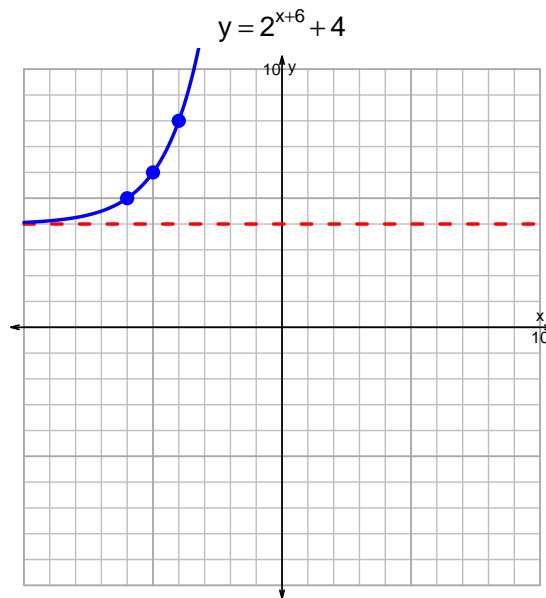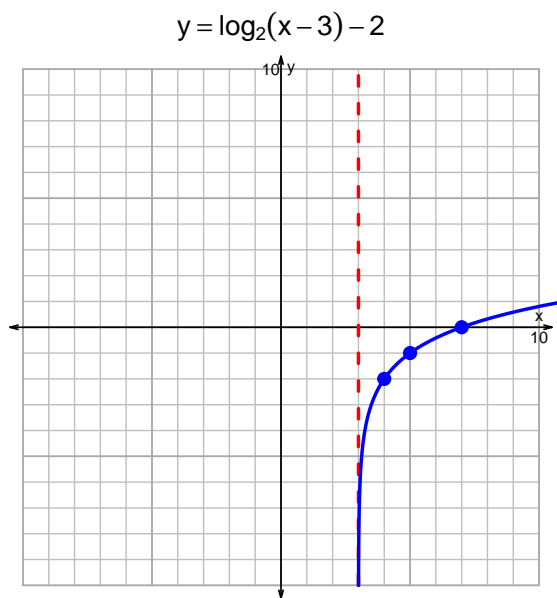
1. (10 pts) Graph $y = \log_2(x - 3) - 2$ and $y = 2^{x+6} + 4$ on the grids below. Also, draw any asymptotes with dashed lines.

$$y = \log_2(x-3) - 2 \qquad\qquad\qquad y = 2^{x+6} + 4$$

Somewhat useful hint: $2^3 = 8$, *and thus* $\log_2(8) = 3$.

2. (10 pts) Write (but do not evaluate) the solution to the equation below by writing a logarithmic expression. Please do not do any arithmetic; just move numbers around.

$$-17 = \left(\frac{-4}{7}\right) \cdot 2^{-5t/3}$$

Divide both sides by $\frac{-4}{7}$.

$$\frac{17 \cdot 7}{4} = 2^{-5t/3}$$

Take log, base 2, of both sides.

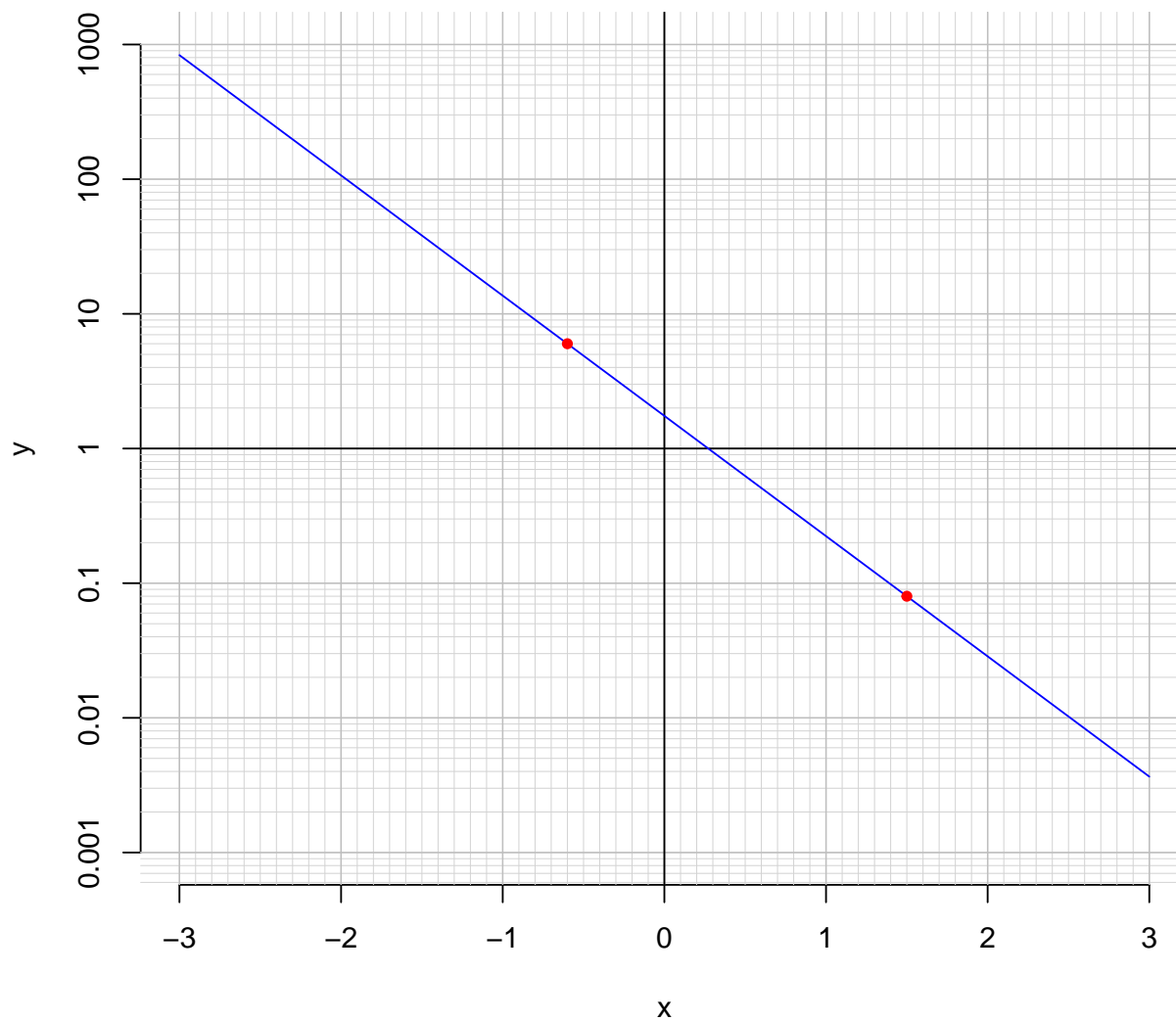$$\log_2\left(\frac{17 \cdot 7}{4}\right) = \frac{-5t}{3}$$

Divide both sides by $\frac{-5}{3}$.

$$\frac{-3}{5} \cdot \log_2\left(\frac{17 \cdot 7}{4}\right) = t$$

Switch sides.

$$t = \frac{-3}{5} \cdot \log_2\left(\frac{17 \cdot 7}{4}\right)$$

3. (10 pts) An exponential function $f(x) = 1.75 \cdot e^{-2.06x}$ is graphed below on a semi-log plot.

a. Using the plot above, evaluate $f(1.5)$.

$$f(1.5) = 0.08$$

b. The inverse function is logarithmic.

$$f^{-1}(x) = \frac{-1}{2.06} \cdot \ln\left(\frac{x}{1.75}\right)$$

Using the plot above, evaluate $f^{-1}(6)$.

$$f^{-1}(6) = -0.6$$