Polynomial Operations SOLUTION (version 105)

1. Let polynomials p(x) and q(x) be defined below.

$$p(x) = 2x^5 + 7x^3 + 10x^2 + 4x - 8$$

$$q(x) = -8x^5 + 9x^4 - 7x^2 - 6x + 5$$

Express the sum of p(x) + q(x) in standard form.

Get "unsimplified" forms. Then find p(x) + q(x) with addition/subtraction.

$$p(x) = (2)x^5 + (0)x^4 + (7)x^3 + (10)x^2 + (4)x^1 + (-8)x^0$$

$$q(x) = (-8)x^5 + (9)x^4 + (0)x^3 + (-7)x^2 + (-6)x^1 + (5)x^0$$

$$p(x) + q(x) = (-6)x^5 + (9)x^4 + (7)x^3 + (3)x^2 + (-2)x^1 + (-3)x^0$$

$$p(x) + q(x) = -6x^5 + 9x^4 + 7x^3 + 3x^2 - 2x - 3$$

2. Let polynomials a(x) and b(x) be defined below.

$$a(x) = 4x^2 - 3x + 7$$

$$b(x) = -9x - 4$$

Express the product $a(x) \cdot b(x)$ in standard form.

You can use a table for multiplication.

*	$4x^2$	-3x	7
-9x	$-36x^{3}$	$27x^{2}$	-63x
-4	$-16x^{2}$	12x	-28

$$a(x) \cdot b(x) = -36x^3 + 27x^2 - 16x^2 - 63x + 12x - 28$$

Combine like terms.

$$a(x) \cdot b(x) = -36x^3 + 11x^2 - 51x - 28$$

3. Express $(x+1)^6$ in standard (expanded) form.

Remember the binomial theorem. It tells us to use Pascal's triangle.

$$x^{6} + 6x^{5} + 15x^{4} + 20x^{3} + 15x^{2} + 6x + 1$$

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4. Let polynomials f(x) and g(x) be defined below.

$$f(x) = x^3 - 8x^2 + x - 11$$

$$g(x) = x - 8$$

The quotient of $\frac{f(x)}{g(x)}$ can be expressed as a polynomial, h(x), and a remainder, R (a real number).

$$\frac{f(x)}{g(x)} = h(x) + \frac{R}{x - 8}$$

By using synthetic division or long division, express h(x) in standard form, and find the remainder R.

I prefer using synthetic division.

So,

$$\frac{f(x)}{g(x)} = x^2 + 1 + \frac{-3}{x - 8}$$

In other words, $h(x) = x^2 + 1$ and the remainder is R = -3.

5. Let polynomial f(x) still be defined as $f(x) = x^3 - 8x^2 + x - 11$. Evaluate f(8).

You could do this the hard way.

$$f(8) = (1) \cdot (8)^3 + (-8) \cdot (8)^2 + (1) \cdot (8) + (-11)$$

$$= (1) \cdot (512) + (-8) \cdot (64) + (1) \cdot (8) + (-11)$$

$$= (512) + (-512) + (8) + (-11)$$

$$= -3$$

Or, if you reference the polynomial remainder theorem, you can state that you know f(8) equals the remainder when f(x) is divided by x - 8. Thus, f(8) = -3.

2