

Name: \_\_\_\_\_ Date: \_\_\_\_\_

## Polynomial Operations SOLUTION (version 202)

1. Let polynomials  $p(x)$  and  $q(x)$  be defined below.

$$p(x) = 8x^5 - 10x^4 + 9x^2 + 4x - 5$$

$$q(x) = 5x^5 - 9x^4 + x^3 + 6x^2 + 10$$

Express the sum of  $p(x) + q(x)$  in standard form.

Get “unsimplified” forms. Then find  $p(x) + q(x)$  with addition/subtraction.

$$p(x) = (8)x^5 + (-10)x^4 + (0)x^3 + (9)x^2 + (4)x^1 + (-5)x^0$$

$$q(x) = (5)x^5 + (-9)x^4 + (1)x^3 + (6)x^2 + (0)x^1 + (10)x^0$$

$$p(x) + q(x) = (13)x^5 + (-19)x^4 + (1)x^3 + (15)x^2 + (4)x^1 + (5)x^0$$

$$p(x) + q(x) = 13x^5 - 19x^4 + x^3 + 15x^2 + 4x + 5$$

2. Let polynomials  $a(x)$  and  $b(x)$  be defined below.

$$a(x) = -2x^2 + 3x + 4$$

$$b(x) = -6x + 4$$

Express the product  $a(x) \cdot b(x)$  in standard form.

You can use a table for multiplication.

*	$-2x^2$	$3x$	$4$
$-6x$	$12x^3$	$-18x^2$	$-24x$
$4$	$-8x^2$	$12x$	$16$

$$a(x) \cdot b(x) = 12x^3 - 18x^2 - 8x^2 - 24x + 12x + 16$$

Combine like terms.

$$a(x) \cdot b(x) = 12x^3 - 26x^2 - 12x + 16$$

3. Express  $(x + 1)^6$  in standard (expanded) form.

Remember [the binomial theorem](#). It tells us to use Pascal’s triangle.

$$x^6 + 6x^5 + 15x^4 + 20x^3 + 15x^2 + 6x + 1$$

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4. Let polynomials  $f(x)$  and  $g(x)$  be defined below.

$$\begin{aligned}f(x) &= -3x^3 + 27x^2 + x - 12 \\g(x) &= x - 9\end{aligned}$$

The quotient of  $\frac{f(x)}{g(x)}$  can be expressed as a polynomial,  $h(x)$ , and a remainder,  $R$  (a real number).

$$\frac{f(x)}{g(x)} = h(x) + \frac{R}{x-9}$$

By using synthetic division or long division, express  $h(x)$  in standard form, and find the remainder  $R$ .

I prefer using synthetic division.

$$\begin{array}{r|rrrr}9 & -3 & 27 & 1 & -12 \\ & & -27 & 0 & 9 \\ \hline & -3 & 0 & 1 & -3\end{array}$$

So,

$$\frac{f(x)}{g(x)} = -3x^2 + 1 + \frac{-3}{x-9}$$

In other words,  $h(x) = -3x^2 + 1$  and the remainder is  $R = -3$ .

5. Let polynomial  $f(x)$  still be defined as  $f(x) = -3x^3 + 27x^2 + x - 12$ . Evaluate  $f(9)$ .

You could do this the hard way.

$$\begin{aligned}f(9) &= (-3) \cdot (9)^3 + (27) \cdot (9)^2 + (1) \cdot (9) + (-12) \\&= (-3) \cdot (729) + (27) \cdot (81) + (1) \cdot (9) + (-12) \\&= (-2187) + (2187) + (9) + (-12) \\&= -3\end{aligned}$$

Or, if you reference the [polynomial remainder theorem](#), you can state that you know  $f(9)$  equals the remainder when  $f(x)$  is divided by  $x - 9$ . Thus,  $f(9) = -3$ .