Polynomial Factoring solution (version 628)

1. The quadratic formula says if $ax^2 + bx + c = 0$ then $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$. Use the quadratic formula to solve the following equation.

$$x^2 - 8x + 24 = 0$$

Simplify your answer(s) as much as possible.

Solution

$$x = \frac{-(-8) \pm \sqrt{(-8)^2 - 4(1)(24)}}{2(1)}$$

$$x = \frac{-(-8) \pm \sqrt{64 - 96}}{2(1)}$$

$$x = \frac{8 \pm \sqrt{-32}}{2}$$

$$x = \frac{8 \pm \sqrt{-16 \cdot 2}}{2}$$

$$x = \frac{8 \pm 4\sqrt{2}i}{2}$$

$$x = 4 \pm 2\sqrt{2}i$$

Notice that *i* in NOT under the square-root radical symbol!!

2. Express the product of 2+4i and 5-3i in standard form (a+bi).

Solution

$$(2+4i) \cdot (5-3i)$$

$$10-6i+20i-12i^{2}$$

$$10-6i+20i+12$$

$$10+12-6i+20i$$

$$22+14i$$

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3. Write function $f(x) = x^3 - x^2 - 22x + 40$ in factored form. I'll give you a hint: one factor is (x-2).

Solution

$$\begin{array}{c|ccccc} & 1 & -1 & -22 & 40 \\ 2 & 2 & 2 & -40 \\ \hline & 1 & 1 & -20 & 0 \end{array}$$

$$f(x) = (x-2)(x^2 + x - 20)$$

$$f(x) = (x-2)(x-4)(x+5)$$

4. Polynomial p is defined below in factored form.

$$p(x) = -(x+7)^{2} \cdot (x+3) \cdot (x-2)^{2} \cdot (x-6)^{2}$$

Sketch a graph of polynomial y = p(x).

