## Polynomial Operations SOLUTIONS (version 35)

1. Let polynomials p(x) and q(x) be defined below.

$$p(x) = 8x^5 + x^4 - 3x^2 + 9x - 5$$

$$q(x) = 9x^5 - 5x^4 - x^3 - 3x^2 - 10$$

Express the difference p(x) - q(x) in standard form.

Get "unsimplified" forms. Then find p(x) - q(x) with addition/subtraction.

$$p(x) = (8)x^5 + (1)x^4 + (0)x^3 + (-3)x^2 + (9)x^1 + (-5)x^0$$
  
$$q(x) = (9)x^5 + (-5)x^4 + (-1)x^3 + (-3)x^2 + (0)x^1 + (-10)x^0$$

$$p(x) - q(x) = (-1)x^5 + (6)x^4 + (1)x^3 + (0)x^2 + (9)x^1 + (5)x^0$$

$$p(x) - q(x) = -x^5 + 6x^4 + x^3 + 9x + 5$$

2. Let polynomials a(x) and b(x) be defined below.

$$a(x) = -6x^2 - 5x + 3$$

$$b(x) = -9x + 6$$

Express the product  $a(x) \cdot b(x)$  in standard form.

You can use a table for multiplication.

*	$-6x^2$	-5x	3
-9x	$54x^3$	$45x^{2}$	-27x
6	$-36x^{2}$	-30x	18

$$a(x) \cdot b(x) = 54x^3 + 45x^2 - 36x^2 - 27x - 30x + 18$$

Combine like terms.

$$a(x) \cdot b(x) = 54x^3 + 9x^2 - 57x + 18$$

3. Express  $(x+1)^6$  in standard (expanded) form.

Remember the binomial theorem. It tells us to use Pascal's triangle.

$$x^6 + 6x^5 + 15x^4 + 20x^3 + 15x^2 + 6x + 1$$

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4. Let polynomials f(x) and g(x) be defined below.

$$f(x) = -3x^3 - 24x^2 + x + 18$$
$$g(x) = x + 8$$

The quotient of  $\frac{f(x)}{g(x)}$  can be expressed as a polynomial, h(x), and a remainder, R (a real number).

$$\frac{f(x)}{g(x)} = h(x) + \frac{R}{x+8}$$

By using synthetic division or long division, express h(x) in standard form, and find the remainder R.

I prefer using synthetic division.

So,

$$\frac{f(x)}{g(x)} = -3x^2 + 1 + \frac{10}{x+8}$$

In other words,  $h(x) = -3x^2 + 1$  and the remainder is R = 10.

5. Let polynomial f(x) still be defined as  $f(x) = -3x^3 - 24x^2 + x + 18$ . Evaluate f(-8).

You could do this the hard way.

$$f(-8) = (-3) \cdot (-8)^3 + (-24) \cdot (-8)^2 + (1) \cdot (-8) + (18)$$

$$= (-3) \cdot (-512) + (-24) \cdot (64) + (1) \cdot (-8) + (18)$$

$$= (1536) + (-1536) + (-8) + (18)$$

$$- 10$$

Or, if you reference the polynomial remainder theorem, you can state that you know f(-8) equals the remainder when f(x) is divided by x + 8. Thus, f(-8) = 10.

2