Polynomial Operations SOLUTION (version 151)

1. Let polynomials p(x) and q(x) be defined below.

$$p(x) = -x^5 + 4x^4 + 8x^2 - 3x + 10$$

$$q(x) = 2x^5 - 6x^3 - 5x^2 + 4x + 1$$

Express the sum of p(x) + q(x) in standard form.

Get "unsimplified" forms. Then find p(x) + q(x) with addition/subtraction.

$$p(x) = (-1)x^5 + (4)x^4 + (0)x^3 + (8)x^2 + (-3)x^1 + (10)x^0$$

$$q(x) = (2)x^5 + (0)x^4 + (-6)x^3 + (-5)x^2 + (4)x^1 + (1)x^0$$

$$p(x) + q(x) = (1)x^5 + (4)x^4 + (-6)x^3 + (3)x^2 + (1)x^1 + (11)x^0$$

$$p(x) + q(x) = x^5 + 4x^4 - 6x^3 + 3x^2 + x + 11$$

2. Let polynomials a(x) and b(x) be defined below.

$$a(x) = 7x^2 + 5x + 4$$

$$b(x) = 3x - 5$$

Express the product $a(x) \cdot b(x)$ in standard form.

You can use a table for multiplication.

*	$7x^2$	5x	4
3x	$21x^3$	$15x^{2}$	12x
-5	$-35x^{2}$	-25x	-20

$$a(x) \cdot b(x) = 21x^3 + 15x^2 - 35x^2 + 12x - 25x - 20$$

Combine like terms.

$$a(x) \cdot b(x) = 21x^3 - 20x^2 - 13x - 20$$

3. Express $(x+1)^5$ in standard (expanded) form.

Remember the binomial theorem. It tells us to use Pascal's triangle.

$$x^5 + 5x^4 + 10x^3 + 10x^2 + 5x + 1$$

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4. Let polynomials f(x) and g(x) be defined below.

$$f(x) = -2x^3 + 15x^2 - 6x + 1$$
$$g(x) = x - 7$$

The quotient of $\frac{f(x)}{g(x)}$ can be expressed as a polynomial, h(x), and a remainder, R (a real number).

$$\frac{f(x)}{g(x)} = h(x) + \frac{R}{x - 7}$$

By using synthetic division or long division, express h(x) in standard form, and find the remainder R.

I prefer using synthetic division.

So,

$$\frac{f(x)}{g(x)} = -2x^2 + x + 1 + \frac{8}{x - 7}$$

In other words, $h(x) = -2x^2 + x + 1$ and the remainder is R = 8.

5. Let polynomial f(x) still be defined as $f(x) = -2x^3 + 15x^2 - 6x + 1$. Evaluate f(7).

You could do this the hard way.

$$f(7) = (-2) \cdot (7)^3 + (15) \cdot (7)^2 + (-6) \cdot (7) + (1)$$

$$= (-2) \cdot (343) + (15) \cdot (49) + (-6) \cdot (7) + (1)$$

$$= (-686) + (735) + (-42) + (1)$$

$$= 8$$

Or, if you reference the polynomial remainder theorem, you can state that you know f(7) equals the remainder when f(x) is divided by x - 7. Thus, f(7) = 8.

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