s17 Geometric Series Exam (Example v104)

Question 1

Consider the partial geometric series represented below with first term a = 990, common ratio $r = \left(\frac{31}{55}\right)^{1/10}$, and n = 10 terms.

$$S = 990 + 934.84 + 882.74 + 833.56 + 787.11 + 743.25 + 701.83 + 662.73 + 625.8 + 590.93$$

We can multiply both sides by r.

$$rS \ = \ 934.84 + 882.74 + 833.56 + 787.11 + 743.25 + 701.83 + 662.73 + 625.8 + 590.93 + 558$$

What is the value of S - rS?

Question 2

Consider the geometric series shown below, using ellipsis notation to indicate a continuation of the pattern without writing every term.

$$S = 2 + 2(5) + 2(5)^{2} + 2(5)^{3} + \cdots + 2(5)^{74} + 2(5)^{75} + 2(5)^{76} + 2(5)^{77}$$

Identify the initial term, the common ratio, and the number of terms.

Question 3

Write a proof for the partial geometric series formula.

- a. Define the variables.
- b. Write the sum using variables and ellipsis notation. You can implicitly assume the number of terms is more than the number of terms you choose to write.
- c. Using annotated algebraic manipulation, produce the partial geometric series formula.