s17 Geometric Series Exam (Example v105)

Question 1

Consider the partial geometric series represented below with first term a=837, common ratio $r=\left(\frac{4}{9}\right)^{1/10}$, and n=10 terms.

$$S = 837 + 771.8 + 711.69 + 656.25 + 605.14 + 558 + 514.54 + 474.46 + 437.5 + 403.42$$

We can multiply both sides by r.

$$rS = 771.8 + 711.69 + 656.25 + 605.14 + 558 + 514.54 + 474.46 + 437.5 + 403.42 + 372$$

What is the value of S - rS?

Question 2

Consider the geometric series shown below, using ellipsis notation to indicate a continuation of the pattern without writing every term.

$$S = 3 + 3(2) + 3(2)^{2} + 3(2)^{3} + \cdots + 3(2)^{47} + 3(2)^{48} + 3(2)^{49} + 3(2)^{50}$$

Identify the initial term, the common ratio, and the number of terms.

Question 3

Write a proof for the partial geometric series formula.

- a. Define the variables.
- b. Write the sum using variables and ellipsis notation. You can implicitly assume the number of terms is more than the number of terms you choose to write.
- c. Using annotated algebraic manipulation, produce the partial geometric series formula.