

Name: \_\_\_\_\_

Date: \_\_\_\_\_

## s17 Geometric Series Exam (SLTN v360)

### Question 1

Consider the partial geometric series represented below with first term  $a = 917$ , common ratio  $r = \left(\frac{3}{7}\right)^{1/10}$ , and  $n = 10$  terms.

$$S = 917 + 842.5 + 774.06 + 711.17 + 653.4 + 600.32 + 551.55 + 506.74 + 465.57 + 427.75$$

We can multiply both sides by  $r$ .

$$rS = 842.5 + 774.06 + 711.17 + 653.4 + 600.32 + 551.55 + 506.74 + 465.57 + 427.75 + 393$$

What is the value of  $S - rS$ ?

Most terms cancel.

$$917 - 393 = 524$$

### Question 2

Consider the geometric series shown below, using ellipsis notation to indicate a continuation of the pattern without writing every term.

$$S = 6 + 6(8) + 6(8)^2 + 6(8)^3 + \cdots + 6(8)^{47} + 6(8)^{48} + 6(8)^{49} + 6(8)^{50}$$

Identify the initial term, the common ratio, and the number of terms.

$$\text{first term} = a = 6$$

$$\text{common ratio} = r = 8$$

$$\text{number of terms} = n = 51$$

### Question 3

Write a proof for the partial geometric series formula.

- Define the variables.
- Write the sum using variables and ellipsis notation. You can implicitly assume the number of terms is more than the number of terms you choose to write.
- Using annotated algebraic manipulation, produce the partial geometric series formula.

### Definitions

$a$  = first term

$r$  = common ratio

$n$  = number of terms

$S$  = sum of partial geometric series

The partial geometric series is expressed using ellipsis notation.

$$S = a + ar + ar^2 + ar^3 + \cdots + ar^{n-4} + ar^{n-3} + ar^{n-2} + ar^{n-1}$$

Multiply both sides by  $r$ .

$$rS = ar + ar^2 + ar^3 + ar^4 + \cdots + ar^{n-3} + ar^{n-2} + ar^{n-1} + ar^n$$

Subtract the second equation from the first equation.

$$S - rS = a - ar^n$$

Factor out  $S$  from left side.

$$S(1 - r) = a - ar^n$$

Divide both sides by  $(1 - r)$ . We technically need to enforce  $r \neq 1$  as a condition of the formula because otherwise we'd be dividing by 0 in this step, and division by 0 is not defined.

$$S = \frac{a - ar^n}{1 - r}$$