



```
## [1] -1.000000000 -0.997589356 -0.994180191 -0.991769547 -0.989358904
## [6] -0.985949738 -0.983539095 -0.981128451 -0.977719286 -0.975308642
## [11] -0.972897998 -0.969488833 -0.967078189 -0.964667546 -0.961258380
## [16] -0.958847737 -0.956437093 -0.953027928 -0.950617284 -0.948206640
## [21] -0.944797475 -0.942386831 -0.939976187 -0.936567022 -0.934156379
## [26] -0.931745735 -0.928336570 -0.925925926 -0.923515282 -0.920106117
## [31] -0.917695473 -0.915284829 -0.911875664 -0.909465021 -0.907054377
## [36] -0.903645212 -0.901234568 -0.898823924 -0.895414759 -0.893004115
## [41] -0.890593471 -0.887184306 -0.884773663 -0.882363019 -0.878953854
## [46] -0.876543210 -0.874132566 -0.870723401 -0.868312757 -0.865902113
## [51] -0.862492948 -0.860082305 -0.857671661 -0.854262496 -0.851851852
## [56] -0.849441208 -0.846032043 -0.843621399 -0.841210755 -0.837801590
## [61] -0.835390947 -0.832980303 -0.829571138 -0.827160494 -0.824749850
## [66] -0.821340685 -0.818930041 -0.816519397 -0.813110232 -0.810699588
## [71] -0.808288945 -0.804879780 -0.802469136 -0.800058492 -0.796649327
## [76] -0.794238683 -0.791828039 -0.788418874 -0.786008230 -0.783597587
## [81] -0.780188422 -0.777777778 -0.775367134 -0.771957969 -0.769547325
## [86] -0.767136681 -0.763727516 -0.761316872 -0.758906229 -0.755497064
## [91] -0.753086420 -0.750675776 -0.747266611 -0.744855967 -0.742445323
## [96] -0.739036158 -0.736625514 -0.734214871 -0.730805706 -0.728395062
## [101] -0.725984418 -0.722575253 -0.720164609 -0.717753965 -0.714344800
## [106] -0.711934156 -0.709523513 -0.706114347 -0.703703704 -0.701293060
## [111] -0.697883895 -0.695473251 -0.693062607 -0.689653442 -0.687242798
## [116] -0.684832155 -0.681422989 -0.679012346 -0.676601702 -0.673192537
## [121] -0.670781893 -0.668371249 -0.664962084 -0.662551440 -0.660140797
## [126] -0.656731631 -0.654320988 -0.651910344 -0.648501179 -0.646090535
## [131] -0.643679891 -0.640270726 -0.637860082 -0.635449439 -0.632040273
## [136] -0.629629630 -0.627218986 -0.623809821 -0.621399177 -0.618988533
## [141] -0.615579368 -0.613168724 -0.610758081 -0.607348915 -0.604938272
## [146] -0.602527628 -0.599118463 -0.596707819 -0.594297175 -0.590888010
## [151] -0.588477366 -0.586066722 -0.582657557 -0.580246914 -0.577836270
## [156] -0.574427105 -0.572016461 -0.569605817 -0.566196652 -0.563786008
## [161] -0.561375364 -0.557966199 -0.555555556 -0.553144912 -0.549735747
## [166] -0.547325103 -0.544914459 -0.541505294 -0.539094650 -0.536684006
## [171] -0.533274841 -0.530864198 -0.528453554 -0.525044389 -0.522633745
## [176] -0.520223101 -0.516813936 -0.514403292 -0.511992648 -0.508583483
## [181] -0.506172840 -0.503762196 -0.500353031 -0.497942387 -0.495531743
## [186] -0.492122578 -0.489711934 -0.487301290 -0.483892125 -0.481481481
## [191] -0.479070838 -0.475661673 -0.473251029 -0.470840385 -0.467431220
## [196] -0.465020576 -0.462609932 -0.459200767 -0.456790123 -0.454379480
## [201] -0.450970315 -0.448559671 -0.446149027 -0.442739862 -0.440329218
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## [206] -0.437918574 -0.434509409 -0.432098765 -0.429688122 -0.426278957
## [211] -0.423868313 -0.421457669 -0.418048504 -0.415637860 -0.413227216
## [216] -0.409818051 -0.407407407 -0.404996764 -0.401587599 -0.399176955
## [221] -0.396766311 -0.393357146 -0.390946502 -0.388535858 -0.385126693
## [226] -0.382716049 -0.380305406 -0.376896240 -0.374485597 -0.372074953
## [231] -0.368665788 -0.366255144 -0.363844500 -0.360435335 -0.358024691
## [236] -0.355614048 -0.352204882 -0.349794239 -0.347383595 -0.343974430
## [241] -0.341563786 -0.339153142 -0.335743977 -0.333333333 -0.330922690
## [246] -0.327513524 -0.325102881 -0.322692237 -0.319283072 -0.316872428
## [251] -0.314461784 -0.311052619 -0.308641975 -0.306231332 -0.302822166
## [256] -0.300411523 -0.298000879 -0.294591714 -0.292181070 -0.289770426
## [261] -0.286361261 -0.283950617 -0.281539974 -0.278130808 -0.275720165
## [266] -0.273309521 -0.269900356 -0.267489712 -0.265079068 -0.261669903
## [271] -0.259259259 -0.256848615 -0.253439450 -0.251028807 -0.248618163
## [276] -0.245208998 -0.242798354 -0.240387710 -0.236978545 -0.234567901
## [281] -0.232157257 -0.228748092 -0.226337449 -0.223926805 -0.220517640
## [286] -0.218106996 -0.215696352 -0.212287187 -0.209876543 -0.207465899
## [291] -0.204056734 -0.201646091 -0.199235447 -0.195826282 -0.193415638
## [296] -0.191004994 -0.187595829 -0.185185185 -0.182774541 -0.179365376
## [301] -0.176954733 -0.174544089 -0.171134924 -0.168724280 -0.166313636
## [306] -0.162904471 -0.160493827 -0.158083183 -0.154674018 -0.152263374
## [311] -0.149852731 -0.146443566 -0.144032922 -0.141622278 -0.138213113
## [316] -0.135802469 -0.133391825 -0.129982660 -0.127572016 -0.125161373
## [321] -0.121752208 -0.119341564 -0.116930920 -0.113521755 -0.111111111
## [326] -0.108700467 -0.105291302 -0.102880658 -0.100470015 -0.097060850
## [331] -0.094650206 -0.092239562 -0.088830397 -0.086419753 -0.084009109
## [336] -0.080599944 -0.078189300 -0.075778657 -0.072369492 -0.069958848
## [341] -0.067548204 -0.064139039 -0.061728395 -0.059317751 -0.055908586
## [346] -0.053497942 -0.051087299 -0.047678133 -0.045267490 -0.042856846
## [351] -0.039447681 -0.037037037 -0.034626393 -0.031217228 -0.028806584
## [356] -0.026395941 -0.022986775 -0.020576132 -0.018165488 -0.014756323
## [361] -0.012345679 -0.009935035 -0.006525870 -0.004115226 -0.001704583
## [366] 0.001704583 0.004115226 0.006525870 0.009935035 0.012345679
## [371] 0.014756323 0.018165488 0.020576132 0.022986775 0.026395941
## [376] 0.028806584 0.031217228 0.034626393 0.037037037 0.039447681
## [381] 0.042856846 0.045267490 0.047678133 0.051087299 0.053497942
## [386] 0.055908586 0.059317751 0.061728395 0.064139039 0.067548204
## [391] 0.069958848 0.072369492 0.075778657 0.078189300 0.080599944
## [396] 0.084009109 0.086419753 0.088830397 0.092239562 0.094650206
## [401] 0.097060850 0.100470015 0.102880658 0.105291302 0.108700467
## [406] 0.111111111 0.113521755 0.116930920 0.119341564 0.121752208
## [411] 0.125161373 0.127572016 0.129982660 0.133391825 0.135802469
## [416] 0.138213113 0.141622278 0.144032922 0.146443566 0.149852731
## [421] 0.152263374 0.154674018 0.158083183 0.160493827 0.162904471
## [426] 0.166313636 0.168724280 0.171134924 0.174544089 0.176954733
## [431] 0.179365376 0.182774541 0.185185185 0.187595829 0.191004994
## [436] 0.193415638 0.195826282 0.199235447 0.201646091 0.204056734
## [441] 0.207465899 0.209876543 0.212287187 0.215696352 0.218106996
## [446] 0.220517640 0.223926805 0.226337449 0.228748092 0.232157257
## [451] 0.234567901 0.236978545 0.240387710 0.242798354 0.245208998
## [456] 0.248618163 0.251028807 0.253439450 0.256848615 0.259259259
## [461] 0.261669903 0.265079068 0.267489712 0.269900356 0.273309521
## [466] 0.275720165 0.278130808 0.281539974 0.283950617 0.286361261
## [471] 0.289770426 0.292181070 0.294591714 0.298000879 0.300411523

```

##	[476]	0.302822166	0.306231332	0.308641975	0.311052619	0.314461784
##	[481]	0.316872428	0.319283072	0.322692237	0.325102881	0.327513524
##	[486]	0.330922690	0.333333333	0.335743977	0.339153142	0.341563786
##	[491]	0.343974430	0.347383595	0.349794239	0.352204882	0.355614048
##	[496]	0.358024691	0.360435335	0.363844500	0.366255144	0.368665788
##	[501]	0.372074953	0.374485597	0.376896240	0.380305406	0.382716049
##	[506]	0.385126693	0.388535858	0.390946502	0.393357146	0.396766311
##	[511]	0.399176955	0.401587599	0.404996764	0.407407407	0.409818051
##	[516]	0.413227216	0.415637860	0.418048504	0.421457669	0.423868313
##	[521]	0.426278957	0.429688122	0.432098765	0.434509409	0.437918574
##	[526]	0.440329218	0.442739862	0.446149027	0.448559671	0.450970315
##	[531]	0.454379480	0.456790123	0.459200767	0.462609932	0.465020576
##	[536]	0.467431220	0.470840385	0.473251029	0.475661673	0.479070838
##	[541]	0.481481481	0.483892125	0.487301290	0.489711934	0.492122578
##	[546]	0.495531743	0.497942387	0.500353031	0.503762196	0.506172840
##	[551]	0.508583483	0.511992648	0.514403292	0.516813936	0.520223101
##	[556]	0.522633745	0.525044389	0.528453554	0.530864198	0.533274841
##	[561]	0.536684006	0.539094650	0.541505294	0.544914459	0.547325103
##	[566]	0.549735747	0.553144912	0.555555556	0.557966199	0.561375364
##	[571]	0.563786008	0.566196652	0.569605817	0.572016461	0.574427105
##	[576]	0.577836270	0.580246914	0.582657557	0.586066722	0.588477366
##	[581]	0.590888010	0.594297175	0.596707819	0.599118463	0.602527628
##	[586]	0.604938272	0.607348915	0.610758081	0.613168724	0.615579368
##	[591]	0.618988533	0.621399177	0.623809821	0.627218986	0.629629630
##	[596]	0.632040273	0.635449439	0.637860082	0.640270726	0.643679891
##	[601]	0.646090535	0.648501179	0.651910344	0.654320988	0.656731631
##	[606]	0.660140797	0.662551440	0.664962084	0.668371249	0.670781893
##	[611]	0.673192537	0.676601702	0.679012346	0.681422989	0.684832155
##	[616]	0.687242798	0.689653442	0.693062607	0.695473251	0.697883895
##	[621]	0.701293060	0.703703704	0.706114347	0.709523513	0.711934156
##	[626]	0.714344800	0.717753965	0.720164609	0.722575253	0.725984418
##	[631]	0.728395062	0.730805706	0.734214871	0.736625514	0.739036158
##	[636]	0.742445323	0.744855967	0.747266611	0.750675776	0.753086420
##	[641]	0.755497064	0.758906229	0.761316872	0.763727516	0.767136681
##	[646]	0.769547325	0.771957969	0.775367134	0.777777778	0.780188422
##	[651]	0.783597587	0.786008230	0.788418874	0.791828039	0.794238683
##	[656]	0.796649327	0.800058492	0.802469136	0.804879780	0.808288945
##	[661]	0.810699588	0.813110232	0.816519397	0.818930041	0.821340685
##	[666]	0.824749850	0.827160494	0.829571138	0.832980303	0.835390947
##	[671]	0.837801590	0.841210755	0.843621399	0.846032043	0.849441208
##	[676]	0.851851852	0.854262496	0.857671661	0.860082305	0.862492948
##	[681]	0.865902113	0.868312757	0.870723401	0.874132566	0.876543210
##	[686]	0.878953854	0.882363019	0.884773663	0.887184306	0.890593471
##	[691]	0.893004115	0.895414759	0.898823924	0.901234568	0.903645212
##	[696]	0.907054377	0.909465021	0.911875664	0.915284829	0.917695473
##	[701]	0.920106117	0.923515282	0.925925926	0.928336570	0.931745735
##	[706]	0.934156379	0.936567022	0.939976187	0.942386831	0.944797475
##	[711]	0.948206640	0.950617284	0.953027928	0.956437093	0.958847737
##	[716]	0.961258380	0.964667546	0.967078189	0.969488833	0.972897998
##	[721]	0.975308642	0.977719286	0.981128451	0.983539095	0.985949738
##	[726]	0.989358904	0.991769547	0.994180191	0.997589356	1.000000000
##	[1]	0.000000000	-0.002410644	-0.002410644	0.000000000	0.002410644
##	[6]	0.002410644	0.000000000	-0.002410644	-0.002410644	0.000000000

[illegible]

[illegible]

[illegible]

[illegible]

```
## [711] "blue" "blue" "blue" "blue" "blue" "blue" "blue" "blue" "blue" "blue"
## [721] "blue" "blue" "blue" "blue" "blue" "blue" "blue" "blue" "blue"
```

A Lindenmayer system (or L-system) is a set of rewrite rules. When these rules are iterated multiple times, we can get complex results from rather simple rules. For example:

- Start
 - A
- Rules
 - $A \rightarrow AB$
 - $B \rightarrow A$
- Iterations:
 1. A
 2. AB
 3. ABA
 4. ABAAB
 5. ABAABABA
 6. ABAABABAABAAB

It might help to see this spaced out...

```
5. A B A A B A B A
6. AB A AB AB A AB A AB
```

Practice

- Start
 - A
- Rules
 - $A \rightarrow BA$
 - $B \rightarrow AB$
- Write the first 5 iterations of this L-system:

When these letters correspond to drawing commands (like move forward, turn 15° , or go back to last saved spot), we can get fractals.