Polynomial Factoring solution (version 4)

1. The quadratic formula says if $ax^2 + bx + c = 0$ then $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$. Use the quadratic formula to solve the following equation.

$$x^2 + 8x + 36 = 0$$

Simplify your answer(s) as much as possible.

Solution

$$x = \frac{-(8) \pm \sqrt{(8)^2 - 4(1)(36)}}{2(1)}$$
$$x = \frac{-(8) \pm \sqrt{64 - 144}}{2(1)}$$

$$x = \frac{-8 \pm \sqrt{-80}}{2}$$

$$x = \frac{-8 \pm \sqrt{-16 \cdot 5}}{2}$$

$$x = \frac{-8 \pm 4\sqrt{5}\,i}{2}$$

$$x = -4 \pm 2\sqrt{5}\,i$$

Notice that i in NOT under the square-root radical symbol!!

2. Express the product of 7 + 6i and 3 + 4i in standard form (a + bi).

Solution

$$(7+6i)\cdot(3+4i)$$

$$21 + 28i + 18i + 24i^2$$

$$21 + 28i + 18i - 24$$

$$21 - 24 + 28i + 18i$$

$$-3 + 46i$$

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3. Write function $f(x) = x^3 + 9x^2 + 8x - 60$ in factored form. I'll give you a hint: one factor is (x+5).

Solution

$$f(x) = (x+5)(x^2+4x-12)$$

$$f(x) = (x+5)(x-2)(x+6)$$

4. Polynomial p is defined below in factored form.

$$p(x) = (x+7)^2 \cdot (x+4)^2 \cdot (x-1)^2 \cdot (x-5)$$

Sketch a graph of polynomial y = p(x).

