## Multiply fractions with prime factorization

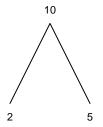
#### Example 1

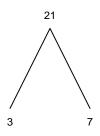
Using prime factorization, evaluate the product of two fractions shown below. Give your answer as a reduced fraction (not a mixed number).

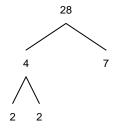
$$\frac{10}{21}\cdot\frac{28}{25}$$

#### Solution to example 1

First, use factor trees to determine the prime factorization of each number.









$$10 = 2^1 \cdot 5^1$$

$$21 = 3^1 \cdot 7^1$$

$$28 = 2^2 \cdot 7^1$$

$$25 = 5^2$$

Rewrite the fraction using prime factors. Also, remember  $\frac{a}{b} \cdot \frac{c}{d} \equiv \frac{ac}{bd}$ .

$$\frac{2\cdot 5\cdot 2\cdot 2\cdot 7}{3\cdot 7\cdot 5\cdot 5}$$

Eliminate common factors.

$$\frac{2\cdot\cancel{5}\cdot2\cdot2\cdot\cancel{7}}{3\cdot\cancel{7}\cdot\cancel{5}\cdot5}$$

$$\frac{2\cdot 2\cdot 2}{3\cdot 5}$$

Multiply the factors in the numerator, and multiply the factors in the denominator.

$$\frac{8}{15}$$

• Consider the product of fractions shown below.

 $\frac{39}{20}\cdot\frac{56}{65}$ 

• Make factor trees for 39, 20, 56, and 65.

• Rewrite the problem using prime factors and a single fraction.

• Consider the product of fractions shown below.

$$\frac{15}{8} \cdot \frac{4}{33}$$

• Make factor trees for 15, 8, 4, and 33.

• Rewrite the problem using prime factors and a single fraction.

• Consider the product of fractions shown below.

$$\frac{63}{10}\cdot\frac{25}{189}$$

• Make factor trees for 63, 10, 25, and 189.

• Rewrite the problem using prime factors and a single fraction.

• Consider the product of fractions shown below.

$$\frac{26}{15}\cdot\frac{18}{65}$$

• Make factor trees for 26, 15, 18, and 65.

• Rewrite the problem using prime factors and a single fraction.

• Consider the product of fractions shown below.

$$\frac{55}{12}\cdot\frac{9}{22}$$

• Make factor trees for 55, 12, 9, and 22.

• Rewrite the problem using prime factors and a single fraction.

• Consider the product of fractions shown below.

$$\frac{12}{55}\cdot\frac{65}{6}$$

• Make factor trees for 12, 55, 65, and 6.

• Rewrite the problem using prime factors and a single fraction.

• Consider the product of fractions shown below.

$$\frac{65}{9}\cdot\frac{15}{26}$$

• Make factor trees for 65, 9, 15, and 26.

• Rewrite the problem using prime factors and a single fraction.