

Midterm q6: Solve quadratic equations with rational solutions

All of these could technically be solved by factoring, but some will be easier with quadratic formula. You should do your work on a separate piece of paper. Solutions are on the back, shuffled.

1. Solve the quadratic equation: $5x^2 + 18x = -9$
2. Solve the quadratic equation: $6x^2 - 17x + 5 = 0$
3. Solve the quadratic equation: $20x^2 - 24x = -5x - 3$
4. Solve the quadratic equation: $10x^2 - 19x = -6$
5. Solve the quadratic equation: $14x^2 + 5x = 1$
6. Solve the quadratic equation: $6x^2 + 19x = 2x - 12$
7. Solve the quadratic equation: $12x^2 + 17x + 6 = 0$
8. Solve the quadratic equation: $x^2 - 5x = -6x + 20$
9. Solve the quadratic equation: $7x^2 - 17x + 10 = 0$
10. Solve the quadratic equation: $5x^2 - x = 6$
11. Solve the quadratic equation: $5x^2 - 4x - 9 = 0$
12. Solve the quadratic equation: $4x^2 - 9x = 9$
13. Solve the quadratic equation: $10x^2 + 25x = 8x - 3$
14. Solve the quadratic equation: $x^2 - 11x = -7x - 3$
15. Solve the quadratic equation: $x^2 + 17x = 9x + 9$
16. Solve the quadratic equation: $14x^2 - 13x + 3 = 0$
17. Solve the quadratic equation: $3x^2 + 7x = -4$
18. Solve the quadratic equation: $2x^2 - 7x + 6 = 0$
19. Solve the quadratic equation: $5x^2 - 14x = -7x - 2$
20. Solve the quadratic equation: $10x^2 - 10x = -3x + 3$

$$11. \quad x = \frac{9}{5} \text{ and } x = -1$$

$$7. \quad x = \frac{-3}{4} \text{ and } x = \frac{-2}{3}$$

$$20. \quad x = 1 \text{ and } x = \frac{-3}{10}$$

$$5. \quad x = \frac{1}{7} \text{ and } x = \frac{-1}{2}$$

$$6. \quad x = \frac{-3}{2} \text{ and } x = \frac{-4}{3}$$

$$19. \quad x = \frac{2}{5} \text{ and } x = 1$$

$$3. \quad x = \frac{1}{5} \text{ and } x = \frac{3}{4}$$

$$10. \quad x = \frac{6}{5} \text{ and } x = -1$$

$$18. \quad x = 2 \text{ and } x = \frac{3}{2}$$

$$13. \quad x = \frac{-1}{5} \text{ and } x = \frac{-3}{2}$$

$$8. \quad x = -5 \text{ and } x = 4$$

$$4. \quad x = \frac{3}{2} \text{ and } x = \frac{2}{5}$$

$$2. \quad x = \frac{1}{3} \text{ and } x = \frac{5}{2}$$

$$12. \quad x = 3 \text{ and } x = \frac{-3}{4}$$

$$15. \quad x = -9 \text{ and } x = 1$$

$$9. \quad x = \frac{10}{7} \text{ and } x = 1$$

$$16. \quad x = \frac{1}{2} \text{ and } x = \frac{3}{7}$$

$$14. \quad x = 3 \text{ and } x = 1$$

$$1. \quad x = -3 \text{ and } x = \frac{-3}{5}$$

$$17. \quad x = \frac{-4}{3} \text{ and } x = -1$$

Midterm practice: Factor quadratic, $a = \text{prime}$.

You should try to factor the expression. I recommend guess-and-check. If that is giving you too much trouble, try figuring out how you can use quadratic formula.

1. If n is an integer and $(x + n)$ is a factor of polynomial $3x^2 - 10x + 3$ then what is the value of n ?
2. If n is an integer and $(x + n)$ is a factor of polynomial $7x^2 + 18x + 8$ then what is the value of n ?
3. If n is an integer and $(x + n)$ is a factor of polynomial $7x^2 - x - 6$ then what is the value of n ?
4. If n is an integer and $(x + n)$ is a factor of polynomial $3x^2 + 7x + 2$ then what is the value of n ?
5. If n is an integer and $(x + n)$ is a factor of polynomial $3x^2 - 7x - 10$ then what is the value of n ?
6. If n is an integer and $(x + n)$ is a factor of polynomial $2x^2 + 9x - 5$ then what is the value of n ?
7. If n is an integer and $(x + n)$ is a factor of polynomial $7x^2 + 9x + 2$ then what is the value of n ?
8. If n is an integer and $(x + n)$ is a factor of polynomial $7x^2 + x - 6$ then what is the value of n ?
9. If n is an integer and $(x + n)$ is a factor of polynomial $2x^2 - 5x - 12$ then what is the value of n ?
10. If n is an integer and $(x + n)$ is a factor of polynomial $5x^2 - 4x - 9$ then what is the value of n ?
11. If n is an integer and $(x + n)$ is a factor of polynomial $5x^2 - 12x + 7$ then what is the value of n ?
12. If n is an integer and $(x + n)$ is a factor of polynomial $2x^2 - 3x - 2$ then what is the value of n ?
13. If n is an integer and $(x + n)$ is a factor of polynomial $5x^2 - 19x + 18$ then what is the value of n ?
14. If n is an integer and $(x + n)$ is a factor of polynomial $7x^2 - x - 8$ then what is the value of n ?
15. If n is an integer and $(x + n)$ is a factor of polynomial $7x^2 + 3x - 4$ then what is the value of n ?
16. If n is an integer and $(x + n)$ is a factor of polynomial $2x^2 + x - 15$ then what is the value of n ?
17. If n is an integer and $(x + n)$ is a factor of polynomial $2x^2 + 5x - 3$ then what is the value of n ?
18. If n is an integer and $(x + n)$ is a factor of polynomial $2x^2 + 9x + 10$ then what is the value of n ?
19. If n is an integer and $(x + n)$ is a factor of polynomial $3x^2 + 5x - 8$ then what is the value of n ?
20. If n is an integer and $(x + n)$ is a factor of polynomial $7x^2 - 15x + 2$ then what is the value of n ?

5. Factors as $(x+1)(3x-10)$ so $n=1$
16. Factors as $(x+3)(2x-5)$ so $n=3$
20. Factors as $(x-2)(7x-1)$ so $n=-2$
9. Factors as $(x-4)(2x+3)$ so $n=-4$
11. Factors as $(x-1)(5x-7)$ so $n=-1$
14. Factors as $(x+1)(7x-8)$ so $n=1$
8. Factors as $(x+1)(7x-6)$ so $n=1$
18. Factors as $(x+2)(2x+5)$ so $n=2$
10. Factors as $(x+1)(5x-9)$ so $n=1$
1. Factors as $(x-3)(3x-1)$ so $n=-3$
13. Factors as $(x-2)(5x-9)$ so $n=-2$
3. Factors as $(x-1)(7x+6)$ so $n=-1$
2. Factors as $(x+2)(7x+4)$ so $n=2$
7. Factors as $(x+1)(7x+2)$ so $n=1$
12. Factors as $(x-2)(2x+1)$ so $n=-2$
17. Factors as $(x+3)(2x-1)$ so $n=3$
4. Factors as $(x+2)(3x+1)$ so $n=2$
15. Factors as $(x+1)(7x-4)$ so $n=1$
19. Factors as $(x-1)(3x+8)$ so $n=-1$
6. Factors as $(x+5)(2x-1)$ so $n=5$

Midterm practice: Factor difference of squares

First factor any common factors. Then, identify the difference of squares to help factor the expression.

1. Fully factor $72x^2 - 2$
2. Fully factor $18x^2 - 2$
3. Fully factor $125x^2 - 5$
4. Fully factor $8x^2 - 2$
5. Fully factor $16x^2 - 4$
6. Fully factor $20x^2 - 5$
7. Fully factor $x^2 - 16$
8. Fully factor $3x^2 - 75$
9. Fully factor $75x^2 - 3$
10. Fully factor $80x^2 - 5$
11. Fully factor $50x^2 - 2$
12. Fully factor $2x^2 - 72$
13. Fully factor $x^2 - 81$
14. Fully factor $196x^2 - 4$
15. Fully factor $12x^2 - 3$
16. Fully factor $16x^2 - 1$
17. Fully factor $5x^2 - 45$
18. Fully factor $108x^2 - 3$
19. Fully factor $162x^2 - 2$
20. Fully factor $x^2 - 4$

$$4. \quad 2(2x+1)(2x-1)$$

$$12. \quad 2(x+6)(x-6)$$

$$2. \quad 2(3x+1)(3x-1)$$

$$19. \quad 2(9x+1)(9x-1)$$

$$5. \quad 4(2x+1)(2x-1)$$

$$6. \quad 5(2x+1)(2x-1)$$

$$17. \quad 5(x+3)(x-3)$$

$$7. \quad (x+4)(x-4)$$

$$11. \quad 2(5x+1)(5x-1)$$

$$18. \quad 3(6x+1)(6x-1)$$

$$16. \quad (4x+1)(4x-1)$$

$$10. \quad 5(4x+1)(4x-1)$$

$$1. \quad 2(6x+1)(6x-1)$$

$$14. \quad 4(7x+1)(7x-1)$$

$$15. \quad 3(2x+1)(2x-1)$$

$$13. \quad (x+9)(x-9)$$

$$9. \quad 3(5x+1)(5x-1)$$

$$20. \quad (x+2)(x-2)$$

$$3. \quad 5(5x+1)(5x-1)$$

$$8. \quad 3(x+5)(x-5)$$

Midterm practice: Solve with square rooting with \pm

Solve for x by undoing a series of operations. When you undo the squaring, remember to have a \pm of the square root. You should do your work on a separate piece of paper. Answers are on the back, but shuffled.

1. Solve the following equation: $9((x-5)^2 - 13) = 27$

2. Solve the following equation: $\frac{1}{20}(x-6)^2 + 16 = 21$

3. Solve the following equation: $5(x-10)^2 + 3 = 128$

4. Solve the following equation: $\frac{1}{19}((x+7)^2 - 5) = 4$

5. Solve the following equation: $\frac{1}{9}((x+9)^2 + 11) = 4$

6. Solve the following equation: $\frac{1}{16}(x+4)^2 + 19 = 23$

7. Solve the following equation: $\frac{1}{8}(x-6)^2 - 2 = 6$

8. Solve the following equation: $4(x-8)^2 - 9 = 91$

9. Solve the following equation: $\frac{1}{8}(x+7)^2 - 3 = -1$

10. Solve the following equation: $3(x+6)^2 - 18 = 30$

11. Solve the following equation: $\frac{1}{12}((x-5)^2 + 8) = 6$

12. Solve the following equation: $2(x+5)^2 - 15 = 17$

13. Solve the following equation: $9(x-9)^2 - 5 = 139$

14. Solve the following equation: $2(x+6)^2 + 8 = 106$

15. Solve the following equation: $5(x+4)^2 + 16 = 141$

16. Solve the following equation: $\frac{1}{12}(x+4)^2 - 14 = -11$

17. Solve the following equation: $\frac{1}{2}((x+5)^2 + 16) = 16$

18. Solve the following equation: $\frac{1}{2}((x-4)^2 + 20) = 60$

19. Solve the following equation: $2(x+7)^2 + 3 = 35$

20. Solve the following equation: $3((x+9)^2 + 8) = 99$

- 15. $x = 1$ and $x = -9$
- 16. $x = 2$ and $x = -10$
- 19. $x = -3$ and $x = -11$
- 11. $x = 13$ and $x = -3$
- 10. $x = -2$ and $x = -10$
- 13. $x = 13$ and $x = 5$
- 17. $x = -1$ and $x = -9$
- 6. $x = 4$ and $x = -12$
- 20. $x = -4$ and $x = -14$
- 2. $x = 16$ and $x = -4$
- 14. $x = 1$ and $x = -13$
- 9. $x = -3$ and $x = -11$
- 4. $x = 2$ and $x = -16$
- 5. $x = -4$ and $x = -14$
- 12. $x = -1$ and $x = -9$
- 8. $x = 13$ and $x = 3$
- 3. $x = 15$ and $x = 5$
- 18. $x = 14$ and $x = -6$
- 7. $x = 14$ and $x = -2$
- 1. $x = 9$ and $x = 1$

Midterm practice: Solve with completing the square

1. Use completing-the-square to solve the equation: $x^2 + 10x - 3 = 20$
2. Use completing-the-square to solve the equation: $x^2 - 10x + 3 = 86$
3. Use completing-the-square to solve the equation: $x^2 - 8x - 5 = 6$
4. Use completing-the-square to solve the equation: $x^2 - 12x + 8 = 26$
5. Use completing-the-square to solve the equation: $x^2 + 6x + 3 = 174$
6. Use completing-the-square to solve the equation: $x^2 - 10x - 5 = 82$
7. Use completing-the-square to solve the equation: $x^2 - 6x - 8 = -9$
8. Use completing-the-square to solve the equation: $x^2 + 18x + 4 = -57$
9. Use completing-the-square to solve the equation: $x^2 - 6x + 4 = 35$
10. Use completing-the-square to solve the equation: $x^2 + 16x - 5 = 93$
11. Use completing-the-square to solve the equation: $x^2 + 16x - 8 = -44$
12. Use completing-the-square to solve the equation: $x^2 + 8x + 2 = 133$
13. Use completing-the-square to solve the equation: $x^2 - 14x - 5 = 74$
14. Use completing-the-square to solve the equation: $x^2 - 14x + 1 = 152$
15. Use completing-the-square to solve the equation: $x^2 - 8x + 4 = 42$
16. Use completing-the-square to solve the equation: $x^2 - 6x - 6 = 97$
17. Use completing-the-square to solve the equation: $x^2 - 14x - 3 = 20$
18. Use completing-the-square to solve the equation: $x^2 + 14x + 8 = 57$
19. Use completing-the-square to solve the equation: $x^2 - 8x - 5 = 126$
20. Use completing-the-square to solve the equation: $x^2 + 8x + 5 = 43$

$$19. \quad x = 4 \pm 7\sqrt{3}$$

$$1. \quad x = -5 \pm 4\sqrt{3}$$

$$11. \quad x = -8 \pm 2\sqrt{7}$$

$$12. \quad x = -4 \pm 7\sqrt{3}$$

$$15. \quad x = 4 \pm 3\sqrt{6}$$

$$6. \quad x = 5 \pm 4\sqrt{7}$$

$$7. \quad x = 3 \pm 2\sqrt{2}$$

$$17. \quad x = 7 \pm 6\sqrt{2}$$

$$16. \quad x = 3 \pm 4\sqrt{7}$$

$$2. \quad x = 5 \pm 6\sqrt{3}$$

$$9. \quad x = 3 \pm 2\sqrt{10}$$

$$18. \quad x = -7 \pm 7\sqrt{2}$$

$$13. \quad x = 7 \pm 8\sqrt{2}$$

$$5. \quad x = -3 \pm 6\sqrt{5}$$

$$4. \quad x = 6 \pm 3\sqrt{6}$$

$$8. \quad x = -9 \pm 2\sqrt{5}$$

$$20. \quad x = -4 \pm 3\sqrt{6}$$

$$3. \quad x = 4 \pm 3\sqrt{3}$$

$$10. \quad x = -8 \pm 9\sqrt{2}$$

$$14. \quad x = 7 \pm 10\sqrt{2}$$