Name:

Date:

# s17 Geometric Series Exam (Solution v18)

## Question 1

Consider the partial geometric series represented below with first term a = 946, common ratio  $r = \left(\frac{8}{11}\right)^{1/10}$ , and n = 10 terms.

$$S = 946 + 916.35 + 887.63 + 859.81 + 832.86 + 806.75 + 781.46 + 756.97 + 733.24 + 710.26$$

We can multiply both sides by r.

$$rS = 916.35 + 887.63 + 859.81 + 832.86 + 806.75 + 781.46 + 756.97 + 733.24 + 710.26 + 688$$

What is the value of S - rS?

Most terms cancel.

$$946 - 688 = 258$$

### Question 2

Consider the geometric series shown below, using ellipsis notation to indicate a continuation of the pattern without writing every term.

$$S = 6 + 6(7) + 6(7)^{2} + 6(7)^{3} + \cdots + 6(7)^{46} + 6(7)^{47} + 6(7)^{48} + 6(7)^{49}$$

Identify the initial term, the common ratio, and the number of terms.

first term 
$$= a = 6$$

common ratio = 
$$r = 7$$

number of terms = 
$$n = 50$$

### Question 3

Write a proof for the partial geometric series formula.

- a. Define the variables.
- b. Write the sum using variables and ellipsis notation. You can implicitly assume the number of terms is more than the number of terms you choose to write.
- c. Using annotated algebraic manipulation, produce the partial geometric series formula.

#### **Definitions**

a =first term

r = common ratio

n = number of terms

S = sum of partial geometric series

The partial geometric series is expressed using ellipsis notation.

$$S = a + ar + ar^{2} + ar^{3} + \dots + ar^{n-4} + ar^{n-3} + ar^{n-2} + ar^{n-1}$$

Multiply both sides by r.

$$rS = ar + ar^2 + ar^3 + ar^4 + \dots + ar^{n-3} + ar^{n-2} + ar^{n-1} + ar^n$$

Subtract the second equation from the first equation.

$$S - rS = a - ar^n$$

Factor out S from left side.

$$S(1-r) = a - ar^n$$

Divide both sides by (1-r). We technically need to enforce  $r \neq 1$  as a condition of the formula because otherwise we'd be dividing by 0 in this step, and division by 0 is not defined.

$$S = \frac{a - ar^n}{1 - r}$$