In terms of α and β , express all the lengths and other angle measures (θ and ϕ).



Variable	Algebraic expression
p =	
q =	
r =	
s =	
$\theta =$	
t =	
u =	
$\phi =$	
v =	
w =	

The angle-sum and angle-difference identities are true for any α and β :

$$\sin(\alpha \pm \beta) = \sin(\alpha)\cos(\beta) \pm \cos(\alpha)\sin(\beta)$$

$$\cos(\alpha \pm \beta) = \cos(\alpha)\cos(\beta) \mp \sin(\alpha)\sin(\beta)$$

You know the following:

$$\sin(315^\circ) = \frac{-\sqrt{2}}{2}$$
 $\sin(120^\circ) = \frac{\sqrt{3}}{2}$

$$\cos(315^\circ) = \frac{\sqrt{2}}{2}$$
 $\cos(120^\circ) = \frac{-1}{2}$

Determine $\sin(435^{\circ})$ exactly.

Prove that $\sin(2x) = 2\sin(x)\cos(x)$ for any x.

(Hint: start with an angle-sum formula from Question 2.)

Question 4

Prove that $cos(2x) = 2cos^2(x) - 1$ for any x.

(Hint: start with an angle-sum formula from Question 2. Also, you will need to use the Pythagorean Identity: $\sin^2(x) + \cos^2(x) = 1$)

Prove that $\cos\left(\frac{y}{2}\right) = \sqrt{\frac{1+\cos(y)}{2}}$. (Technically this assumes $\cos(y/2) > 0$, but let's not worry about that here.)

(Hint: use the identity proved in Question 4.)

Question 6

If you knew that $\cos(160^\circ) \approx -0.94$, then what is $\cos(80^\circ)$? Please set up an expression, but do **not** try to simplify or evaluate a decimal approximation.

(Hint: 160/2 = 80.)